# Low mass stars, brown dwarf candidates and the mass function of the young open cluster NGC 2547 

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#### Abstract

We present a catalogue of $R_{\mathrm{c}} I_{\mathrm{c}} Z$ photometry over an area of 0.855 square degrees, centred on the young open cluster NGC 2547. The survey is substantially complete to limits of $R_{c}=$ 21.5, $I_{\mathrm{c}}=19.5, Z=19.5$. We use the catalogue to define a sample of NGC 2547 candidates with model-dependent masses of about $0.05-1.0 \mathrm{M}_{\odot}$. After correcting for incompleteness and estimating contamination by foreground field dwarfs, we investigate the mass function of the cluster, its binary content, and search for evidence of mass segregation among the lower mass stars. There is ample evidence for mass segregation between high ( $>3 \mathrm{M}_{\odot}$ ) and lower mass stars, but over the range $0.1<M<0.7 \mathrm{M}_{\odot}$, the data are consistent with no further mass segregation. By fitting King profiles we conclude that at least 60 per cent of the low-mass stellar population are contained within our survey. The cluster mass function is remarkably similar to the Pleiades for $0.075<M<0.7 \mathrm{M}_{\odot}$. Because of its age ( $\simeq 30 \mathrm{Myr}$ ), we demonstrate that this mass function is robust to a number of systematic uncertainties likely to affect older and younger clusters and is therefore one of the best available estimates for the initial mass function in young disc populations. For $0.05<M<0.075 \mathrm{M}_{\odot}$ there is some evidence for a deficit of brown dwarfs in NGC 2547 compared with other clusters. This deficit may extend to lower masses or may only be a dip, perhaps caused by an imperfect understanding of the mass-magnitude relationship at temperatures of around 2800 K . Incompleteness in both our survey and the luminosity functions from which we estimate contamination by foreground objects leave this question open. The binary fraction for systems with mass ratios greater than about 0.5 is $20-35$ per cent for M dwarfs in NGC 2547, quite consistent with that found in the field and other young clusters. The full photometric catalogue and our lists of candidate cluster members are made available in electronic format.


Key words: methods: data analysis - techniques: photometric - stars: formation - stars: pre-main-sequence - open clusters and associations: individual: NGC 2547.

## 1 INTRODUCTION

The open cluster NGC 2547 (= C0809-491) is important for efforts to understand the formation and evolution of low-mass, pre-main-sequence (PMS) stars. Its isochronal age is about 30 Myr , it is relatively close ( $\simeq 400-450 \mathrm{pc}$ ), has low reddening $[E(B-V)=$ $0.06]$ and a rich population of identified early and late-type members (see Clariá 1982; Jeffries, Totten \& James 2000; Naylor et al. 2002, hereafter N02). Being close and quite compact, it serves as an ideal laboratory to investigate evolutionary tracks and isochrones, rotation rates, magnetic activity and light element abundances of low-mass PMS stars as they approach the zero-age main sequence (ZAMS). In particular, NGC 2547 occupies an important and comparatively little-studied niche of parameter space with an age between those
of regions of recent star formation, and clusters like the Pleiades, where low-mass stars have already reached the ZAMS.
Jeffries \& Tolley (1998) first identified the low-mass PMS population of NGC 2547 as counterparts to ROSAT X-ray sources. A number of these counterparts were positively identified as F - to K-type cluster members by Jeffries et al. (2000) using radial velocities. A $B V I_{\mathrm{c}}$ photometric study of NGC 2547 was presented by N02. Their survey covered an approximately square area of 0.32 square degrees and identified several hundred candidate cluster members with masses from $6 \mathrm{M}_{\odot}$ down to about $0.25 \mathrm{M}_{\odot}$ at $V \simeq 20.5$. N02 concluded that the mass function (MF) was similar in shape to that of the Pleiades and of field stars over this mass range, but that the total mass of NGC 2547 could be a few times less than the Pleiades. Littlefair et al. (2003) have used the same list of candidate members
to show that stars with mass $>3 \mathrm{M}_{\odot}$ in NGC 2547 are much more centrally concentrated than lower mass objects. Because NGC 2547 is no more than 10 dynamical crossing times old, it seems likely that most of this segregation must be primordial (e.g. Bonnell et al. 2001), rather than due to dynamical evolution.

The N02 survey did not cover a sufficiently large area or go to sufficient depths to discover whether the spatial distribution of lowmass ( $<1 \mathrm{M}_{\odot}$ ) cluster members was independent of mass. The possibility of differential mass segregation between lower mass stars is important. Some recent theories concerning the formation of very low-mass stars and brown dwarfs suggest they are ejected as lowmass fragments from protostellar multiple systems before they have a chance to accrete significant material (e.g. Reipurth \& Clarke 2001). Such objects may have a greater velocity dispersion than their higher mass siblings and hence be less spatially concentrated in a cluster (Sterzik \& Durisen 2003). This in turn would mean that a cluster MF measured over a limited volume would underestimate the contribution from the lowest mass stars and brown dwarfs. However, alternative simulations of brown dwarf formation (e.g. Bate, Bonnell \& Bromm 2003) predict that the initial velocity dispersions of low-mass stars and brown dwarfs will be similar and little mass segregation or preferential evaporation of very low-mass objects would be expected prior to full dynamical relaxation.

In this paper we present a new $R_{\mathrm{c}} I_{\mathrm{c}} Z$ photometric survey of NGC 2547. This survey is deeper than that of N02, extending to just below the substellar boundary, encompassing the 'turnover' of the observed MF seen in the field and in the Pleiades at $\sim 0.2 \mathrm{M}_{\odot}$ (see Chabrier 2003, and references therein). The new survey also covers a wider area ( 0.855 square degrees), allowing us to explore the question of mass segregation among lower mass cluster candidates in more detail. The observational data and analysis are presented in Section 2. The selection of candidate cluster members and an evaluation of completeness and contamination are addressed in Section 3.

In Section 4 we evaluate the mass segregation, luminosity and mass functions for NGC 2547. We discuss the results and draw our conclusions in Sections 5 and 6.

## 2 OBSERVATIONS AND DATA ANALYSIS

### 2.1 Observations

The observations were obtained between 1999 February 4 and 9 inclusive, using a $2048 \times 2048$ CCD mounted at the Cassegrain focus of the $0.91-\mathrm{m}$ telescope of the Cerro Tololo Interamerican Observatory. The camera had a field of view of approximately $13.5 \times$ 13.5 square arcmin. The data set consists of multiple exposures of 24 overlapping fields taken using each of a Harris $R$ filter, a KronCousins $I$ filter and a Gunn $Z$ filter. The approximate field centres and a $\log$ of the separate exposures obtained are listed in Table 1. Seeing varied between 0.9 and 2.0 arcsec in the individual frames (with a median of 1.3 arcsec and standard deviation of 0.2 arcsec). Exposure times were adjusted a little to achieve a reasonably uniform sensitivity across the mosaic. The area covered is illustrated in Fig. 1 and covers 0.855 square degrees in total. Two of the individual fields are situated about a degree from the cluster centre but along a line of constant galactic latitude. We intended to use these fields as a check on the field contamination present in the photometrically selected cluster candidates.
Individual images were bias subtracted (overscan subtracted and then a median of overscan-subtracted bias frames was subtracted) and flat-fielded using twilight sky flats from the same observing night. The $Z$ frames were affected by fringing of night sky spectral lines. We dealt with these by constructing a median image from all the sky-subtracted $Z$ frames taken during the run. This 'fringeframe' was then multiplied by a constant and subtracted from each of the individual $Z$ frames. The constant was modified iteratively

Table 1. Log of observations.

| Field | Field Centre (J2000) |  |  | Exposures (s) |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | RA | Dec. | $R$ | $I$ | $Z$ |
|  |  |  |  |  |  |
| 01 | 081220.6 | -493400 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 02 | 081116.3 | -493400 | $7 \times 200$ | $7 \times 100$ | $3 \times 300$ |
| 03 | 081012.0 | -493400 | $5 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 04 | 080907.7 | -493400 | $6 \times 200$ | $5 \times 100$ | $2 \times 300$ |
| 06 | 080803.4 | -492330 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 07 | 080907.7 | -492330 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 08 | 081012.0 | -492330 | $6 \times 200$ | $7 \times 100$ | $4 \times 300$ |
| 09 | 081116.3 | -492330 | $6 \times 200$ | $6 \times 100$ | $3 \times 300$ |
| 10 | 081220.6 | -492330 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 11 | 081220.6 | -491300 | $900+600$ | $3 \times 100$ | $3 \times 300$ |
| 12 | 081116.3 | -491300 | $6 \times 300$ | $3 \times 100$ | $3 \times 300$ |
| 13 | 081012.0 | -491300 | $7 \times 200+100$ | $3 \times 100$ | $4 \times 200+100$ |
| 14 | 080907.7 | -491300 | $7 \times 200+100$ | $3 \times 100$ | $4 \times 200+100$ |
| 15 | 080803.4 | -491300 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 16 | 080805.3 | -490308 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 17 | 080907.7 | -490230 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 18 | 081012.0 | -490230 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 19 | 081116.3 | -490230 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 20 | 081220.6 | -490230 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 22 | 081116.3 | -485200 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 23 | 081012.0 | -485200 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 24 | 080907.7 | -485200 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 51 | 080450.6 | -483100 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
| 52 | 081533.4 | -495530 | $6 \times 200$ | $5 \times 100$ | $3 \times 300$ |
|  |  |  |  |  |  |



Figure 1. A Digitized Sky Survey image of the region around NGC 2547. The area surveyed in this paper are marked together with an approximate identification of the fields defined in Table 1.
until the mean absolute deviation in the sky was minimized and approached the nominal value expected from the sky signal and gain of the CCD. After this procedure no visible trace of the fringing pattern could be discerned.

The CCD was affected by a number of bad columns and pixels. We also found that occasional images were affected by 27 bad rows at the bottom of the CCD. Bad pixel masks were constructed for all frames and used in the subsequent reduction. The bad pixels were replaced with the median of surrounding pixels. It is worth emphasizing that these patched pixels were used in the initial source searching of the summed frames, but the final combined photometry uses only stellar images with no patched pixels where possible.

### 2.2 Photometric calibration

Photometric calibration was achieved with reference to measurements of Landolt (1992) standard fields taken on a number of occasions on each night. The flux from standard stars was measured inside a 6 -arcsec radius aperture and sky-subtracted using the median sky measured in a much larger annulus.

The $I_{\mathrm{c}}$ and $R_{\mathrm{c}}-I_{\mathrm{c}}$ values listed in Landolt (1992) were used to find a weighted least-squares solution to the following equations on each night
$I_{\mathrm{c}}=i+c_{r i}\left(R_{\mathrm{c}}-I_{\mathrm{c}}\right)-k_{i} X+z_{i}$,
$R_{\mathrm{c}}-I_{\mathrm{c}}=a(r-i)-k_{r i} X+z_{r i}$,
where $i$ and $r$ are instrumental magnitudes (corrected for exposure time), $k_{i}$ and $k_{r i}$ are extinction coefficients, $X$ is the airmass of an observation, $z_{i}$ and $z_{r i}$ are photometric zero-points, $c_{r i}$ is a colour term to take into account any mismatch between the $I$ filter we used and the Cousins system, and $a$ is a similar term for the $R_{\mathrm{c}}-I_{\mathrm{c}}$ colour.

For our best photometric night (1999 February 7) we obtained a solution with $c_{r i}=0.074, k_{i}=0.237, a=0.975, k_{r i}=0.090$. The rms discrepancy from this fit using 26 points was 0.04 mag in $I_{\mathrm{c}}$ and 0.02 mag in $R_{\mathrm{c}}-I_{\mathrm{c}}$. The addition of about 0.02 mag in quadrature
to the instrumental $i$ and $r-i$ uncertainties leads to a reduced chisquared of 1 . However, only two standards with $R_{\mathrm{c}}-I_{\mathrm{c}}>1.5$ were measured and one of these (SA 98-L5) has quite uncertain colours. Systematic errors of up to 0.1 mag in the colours and magnitudes cannot be ruled out for stars with $R_{\mathrm{c}}-I_{\mathrm{c}}>1.5$, although it is encouraging that the colour terms in equations (1) and (2) are small and the residuals to the fits at $R_{\mathrm{c}}-I_{\mathrm{c}}<1.5$ do not suggest any non-linearities in the calibration.

There is no equivalent of the Landolt standards for the $I_{\mathrm{c}}-Z$ colour. Instead we used observations of stars in Landolt field SA 98 which have had their $I_{\mathrm{c}}-Z$ colours defined by Zapatero-Osorio et al. (1999), along with two early A stars from Landolt field SA 99 for which we assumed that $I_{\mathrm{c}}-Z=R_{\mathrm{c}}-I_{\mathrm{c}}$. Using an equation of the form
$I_{\mathrm{c}}-Z=b(i-z)-k_{i z} X+z_{i z}$,
we found $b=0.85$ and $k_{i z}=0.07$, with an rms discrepancy of less than 0.01 mag from nine points.

These coefficients were applied to five of our fields which were taken on the same night and in an airmass range comparable to the standards (fields $1,2,6,7,10$ ) . These fields were considered 'photometric' in a normalization procedure that uses the considerable (2-3 arcmin) overlaps between the fields (described below and in more detail by N02). The remaining fields were put on to the standard system using the same coefficients, but their zero-points were allowed to vary in the normalization procedure.

### 2.3 Photometry and astrometry in the cluster

From the processed CCD frames the analysis proceeded using the CLUSTER software suite described in detail by N02. In brief, this consisted of searching for objects in the summed $I$-band image of each field. A signal-to-noise ratio threshold of 5 was used for the search. Shifts between each frame and the summed $I$-band image were parametrized with a six-coefficient solution, and optimal photometry (see Naylor 1998) of each object performed in each individual frame at fixed positions determined from the summed $I$-band image. Bright, unsaturated stars in each frame were used to derive the 'profile correction', which was applied to the optimal photometry values to place them onto the system defined by the aperture photometry of standard stars. The profile correction was successfully modelled as a quadratic function of the horizontal and vertical coordinates in each frame.

Profile-corrected photometry measurements were adjusted for differences in the airmass of each frame, weighted by their statistical errors and combined. Additional, magnitude-independent errors of between 0.004 and 0.010 mag were added (in quadrature) to the results for each individual frame to yield a plot of reduced chi-squared versus signal-to-noise ratio for each field which had a uniform value of 1 (see N 02 for details). Instrumental magnitudes were combined with the average airmass of each set of observations and equations (1), (2) and (3) used to obtain preliminary magnitudes and colours for stars in each field.

Astrometric calibration was defined by approximately 1000 objects in each frame that were identified on UK Schmidt $J$ plates as part of the SuperCOSMOS sky survey (Hambly et al. 2001a). The rms discrepancy in position for each identified object, after correction for proper motions in the SuperCOSMOS catalogue, was $0.20-0.25$ arcsec. This uncertainty is mainly in the positions from the SuperCOSMOS catalogue - comparison of positions for stars in our final catalogue with those common to the NGC 2547 catalogue presented by N02, which was calibrated using the same

SuperCOSMOS data, indicate an internal astrometric precision for each catalogue of 0.05 arcsec (rms) in each coordinate.
The overlapping regions between fields were used to refine the photometry and produce a uniformly calibrated mosaic. A shift was applied to the colours and magnitudes of each field which minimized the average discrepancies of all the stars in the overlap regions, subject to the constraint that the average shift applied to all those fields considered 'photometric' (see Section 2.2) was zero. After this procedure the rms discrepancy in the photometry for each field was 0.010 mag in $I, 0.007 \mathrm{mag}$ in $R_{\mathrm{c}}-I_{\mathrm{c}}$ and 0.009 mag in $I_{\mathrm{c}}-Z$. The final catalogue was produced by averaging the results for stars found in more than one field.
There were several departures from the procedures described by N02 which are worth noting.
(i) In N02 the source searching algorithm looked for 'islands' of pixels which were some multiple of the noise above the sky level. This threshold was iteratively reduced by factors of 4 in order to isolate stars situated in the wings of other stars, where the original minimum flux at a point between them may not fall below the threshold. It became apparent during the reduction of this data set that a better thresholding step is a factor of $\sqrt{ } 2$. In the case of sky-limited, Gaussian stars, this ensures that stars which are formally resolved (i.e. their flux profiles overlap at a point beyond their full width at half maximum, FWHM) are clearly separated as two sources by our search technique in the course of at least one iteration. Though this choice slows down the source searching procedure it is far from being the rate-determining step in the overall data reduction process.
(ii) The photometry in the catalogue now uses the character-based flagging scheme described in Burningham et al. (2003) to identify non-stellar objects, stars lying on bad pixels, poor sky estimation, etc.
(iii) In our reduction scheme, 'non-stellar' means that the optimal photometry technique will not yield a reliable measurement because the object is significantly extended, confused with another object or affected by the flux from a nearby brighter star. We found that testing for non-stellarity only in the summed $I$-band image was insufficient. Faint, very red, low-mass cluster candidates might appear isolated in the $I$ band, but their $R$-band flux could be biased upward by a nearby, unrelated field star with a bluer spectrum. Hence the estimated $R_{\mathrm{c}}-I_{\mathrm{c}}$ colour of the cluster candidate could be significantly underestimated. To counter this, an additional test for non-stellarity was made in the summed $R$-band image. If either test resulted in a non-stellar classification then this was reflected in the flags of all three magnitudes and colours. It was not necessary to extend the test to a summed $Z$-band image because the vast majority of stars (see Figs 2 and 3 ) are bluer than the faint cluster candidates.
(iv) The sky estimation technique (see Naylor 1998) is robust to nearby stars inside the 'sky box' or smooth gradients in the sky background. However, curvature in the background, such as for objects situated in the wings of very bright or saturated stars will result in a histogram of pixel values that is highly asymmetric or not well fit by the skewed Gaussian model we adopt. To avoid spurious detections or significantly mis-estimated sky backgrounds, we demand that the reduced chi-squared of the fit to the sky histogram is less than 3 and that the skewness parameter is less than 0.3. If either test is failed then an 'ill-determined sky' flag is set.

### 2.4 The final catalogue

The final catalogue contains 133788 stars, of which 49223 have one or more quality flags set. It is available in electronic format


Figure 2. The $I$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ CMD for the entire catalogued area of NGC 2547. Only unflagged objects with signal-to-noise ratio better than 10 are shown.


Figure 3. The $I$ versus $I_{\mathrm{c}}-Z$ CMD for the entire catalogued area of NGC 2547. Only unflagged objects with signal-to-noise ratio better than 10 are shown.
(http://www.blackwellpublishing.com/products/journals/suppmat/ MNR/MNR7886/MNR7886sm.htm) and is described in Appendix A.

Before using the catalogue it is worth examining sources of internal and external errors in the catalogue measurements.
(i) The astrometry has an internal precision of about 0.05 arcsec (1 sigma) in each coordinate for objects with a signal-tonoise ratio (in the $I$ band) of $>10$. The systematic external uncertainties are equivalent to the external uncertainties present in the SuperCOSMOS astrometric calibration (about $\pm 0.2$ arcsec compared with the International Celestial Reference Frame - Hambly et al. 2001b).
(ii) The uncertainties for the magnitudes and colours reflect a combination of the statistical uncertainties of the optimal photometry flux measurements with an additional, small, magnitudeindependent error added to each frame (see Section 2.3).
(iii) The catalogue does not include uncertainties revealed by the rms discrepancies in the zero-points of the overlapping regions
between fields (see Section 2.3). These uncertainties should be added to the errors presented in the final catalogue if stars are to be compared or combined across different fields or the survey as a whole (as is the case in this paper).
(iv) Finally there are systematic external photometric uncertainties, which are generally less than 0.02 mag but perhaps as large as 0.1 mag for the reddest stars (see Section 2.2 and below). These may be important when comparing with other catalogues or with theoretical models.

As a check on external photometric precision we compared our $I_{\mathrm{c}}$ photometry with that in N02. A subset of stars with no quality flags set and $I_{\mathrm{c}}$ errors less than 0.1 mag was selected from each catalogue. These subsets were cross-correlated using a $1.0-\operatorname{arcsec}$ correlation radius, finding 13032 matches. We find the following weighted least-squares fit relationships after adding the small errors revealed by the rms discrepancies in the zero-points of the overlapping regions in each data set:

$$
\begin{aligned}
& I_{\mathrm{c}}-I_{\mathrm{N} 02}=-0.012(3)+0.0019(2) I_{\mathrm{c}} \\
& I_{\mathrm{c}}-I_{\mathrm{N} 02}=-0.004(9)+0.043(2)\left(R_{\mathrm{c}}-I_{\mathrm{c}}\right)
\end{aligned}
$$

for $12<I_{\mathrm{c}}<20$ and $0.1<R_{\mathrm{c}}-I_{\mathrm{c}}<2.0$, and where the numbers in brackets are 1 -sigma uncertainties in the final significant figure. Higher order polynomials provide no significantly better fits. One of the strengths we claim for our techniques is the complete trustworthiness of the internal photometry errors (for unflagged objects). The reduced chi-squared values for the above fits, of 1.37 and 1.22 respectively, provide reassurance that this is the case, especially given the likelihood that at least some stars are truly variable. There is a significant difference and trend with colour between the N02 and our values - the N02 $I_{\mathrm{c}}$ values are about 0.08 mag brighter at $R_{\mathrm{c}}-I_{\mathrm{c}}=2$. As both data sets suffer from the same lack of very red calibration stars it would be unwise to attach more weight to one than the other.

## 3 CLUSTER MEMBERSHIP

### 3.1 Colour-magnitude diagrams

Figs 2 and 3 show the $I_{\mathrm{c}}$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ and $I_{\mathrm{c}}$ versus $I_{\mathrm{c}}-Z$ colourmagnitude diagrams (CMDs) for all unflagged stars with a signal-to-noise ratio (in colour and magnitude) better than 10 (62722 and 55174 stars, respectively).

The NGC 2547 PMS is clearly visible in both diagrams. It is better delineated when looking at the positions of X-ray active stars (see Section 3.2 and N02), but we show these diagrams to make obvious the concentration of cluster stars (especially in Fig. 2 for $0.9<R_{\mathrm{c}}-I_{\mathrm{c}}<2.0$ ) and their separation from the contaminating background.

### 3.2 Model isochrones

To select cluster members and assign masses to stars on the basis of their colours and magnitudes, we must choose an isochrone that adequately models the data. To aid this process we fit a subset of the catalogue identified as optical counterparts to XMM-Newton X-ray sources. The rationale is that young stars in NGC 2547 are known to be very X-ray active, typically orders of magnitude more active than contaminating field stars at a similar position in the observed CMDs (Jeffries \& Tolley 1998). An X-ray selected sample should present a relatively clean PMS sample with which to fit model isochrones. The details of the XMM-Newton observations will be presented


Figure 4. X-ray selected objects in the field of NGC 2547 with 20, 30 and 40 Myr empirical isochrones generated from the B02 models at an assumed distance modulus and reddening of 8.1 and $E(R-I)=0.043$. The dashed line indicates a 30 Myr isochrone taken directly from the B 02 models.
elsewhere (Jeffries et al. in preparation). In brief, they consist of a $50-\mathrm{ks}$ pointing at the centre of the cluster, from which a total of 213 significant X-ray sources were found in one or a combination of the two $P N$ plus EPIC detectors and within a 17 -arcmin radius of the XMM-Newton field centre. These sources were correlated with our photometric catalogue, but to to minimize the number of spurious correlations, we restricted the catalogue to $I_{c}<18$, because experiments showed that no plausible PMS cluster members were Xray detected at lower luminosities. The X-ray optical counterparts are displayed in Figs 4, 5 and 6. The objects in the lower left of these plots are not cluster members and are most likely extragalactic X-ray sources that are randomly correlated with faint objects in the bulk of the CMD background population.

To select appropriate isochrones we used the models of D'Antona \& Mazzitelli (1997, DM97) and Baraffe et al. (2002, hereafter B02 - with mixing length parameter set to 1.9 scaleheights for masses greater than $\left.0.6 \mathrm{M}_{\odot}\right)$. The B 02 models predict optical and infrared magnitudes as a function of age and mass, using the same model atmospheres that provide boundary conditions for the evolutionary model. However, it is well known that there are problems (mainly at $V$ and $R$ ) with these magnitudes, probably due to omissions in the various sources of opacity at these wavelengths (see Baraffe et al. 1998). In Fig. 4 we show a model $30-\mathrm{Myr}$ B02 isochrone (as a dashed line) constructed assuming an intrinsic distance modulus of 8.1 - clearly it is not a reasonable match to the data, being far too blue for the fainter X-ray sources.

Instead, we adopt the approach of Jeffries, Thurston \& Hambly (2001) and N02. We assume that the large amount of excellent photometric data for the Pleiades defines an empirical isochrone at an age of $\simeq 120 \mathrm{Myr} .{ }^{1}$ Combined with empirical $I_{\mathrm{c}}$-band bolometriccorrection versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ relationships (a quadratic fit to data from Leggett 1992 and Leggett et al. 1996), this empirical isochrone is used to determine a colour- $T_{\text {eff }}$ relation that can be applied to

[^0]

Figure 5. As for Fig. 4, but using the DAM97 models.


Figure 6. The $I$ versus $I_{\mathrm{c}}-Z$ CMD for the X-ray selected targets in NGC 2547 (circles) plus Pleiades BDs from Zapatero-Osorio et al. (1999) shifted to the same distance as NGC 2547 (triangles). The solid line indicates the lower envelope used in our membership selection criteria for NGC 2547. The dashed line is the PMS locus we have assumed for NGC 2547 when generating a simulated catalogue (see Section 3.4).
isochrones at any age. Isochrones are generated from each set of evolutionary models, converted to colours and magnitudes and adjusted for the distance modulus, extinction and reddening for NGC 2547. The data here cannot determine any of these parameters independently of age, so we assume an intrinsic distance modulus of 8.1 (see N02), visual extinction, $A_{\mathrm{V}}$, of 0.19 mag (Clariá 1982) and $E\left(R_{\mathrm{c}}-I_{\mathrm{c}}\right)$ of 0.043 .
$I_{\mathrm{c}}$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ isochrones are shown in Figs 4 and 5 for the B02 and DM97 models, respectively. The isochrones are a good fit to the X-ray selected cluster members at ages of $35 \mathrm{Myr}(\mathrm{B} 02)$ and 30 Myr (DM97) for the range of colours of low mass objects discussed in this paper $\left(R_{\mathrm{c}}-I_{\mathrm{c}}>0.7\right)$. The age uncertainties are dominated by uncertainties in the cluster distance modulus - a plausible $\pm 0.1$ error in distance modulus leads to a $\mp 5 \mathrm{Myr}$ age change. There are significant differences in the shapes of the B02 and DM97 isochrones for $I_{\mathrm{c}}>17$. In principle these differences could be tested by firm membership information for fainter cluster candidates. In practice we need to perform our analysis for both isochrones in terms of
selection of candidate members and subsequent calculation of MFs etc.

The same approach cannot be adopted for the $I_{\mathrm{c}}$ versus $I_{\mathrm{c}}-Z$ CMD where there is insufficient, consistently calibrated Pleiades photometry from which to define the $I_{\mathrm{c}}-Z$ versus $T_{\text {eff }}$ relation. Instead, for $I_{c}<17.5$ we define a locus that forms a conservative lower boundary to the X-ray selected stars and for fainter stars we extend this boundary by assuming that NGC 2547 candidates must lie above a set of consistently calibrated Pleiades low-mass stars (from Zapatero-Osorio et al. 1999). Our X-ray selected stars, the Pleiades objects (shifted to the same distance modulus as NGC 2547) and our defined lower boundary are shown in Fig. 6. The point of inflexion at $I_{\mathrm{c}}-Z \simeq 0.5$ does appear to be a genuine feature of the models and filter bandpasses (e.g. Moraux et al. 2003).

### 3.3 Selection criteria

Selection of candidate members in the CMDs is an arbitrary process to some extent. As our aims are to produce luminosity and mass functions (LFs and MFs) we choose to err on the side of generosity, defining tests that all members should pass (although see Section 3.4), at the expense of including more contaminating field objects (see Section 3.5). For each of the two sets of model isochrones in the $I_{\mathrm{c}}$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ CMD we select cluster candidates according to the following tests.
(i) The star must be unflagged and have photometric errors less than 0.1 mag in $I_{\mathrm{c}}$ and $I_{\mathrm{c}}-Z$ and less than 0.2 mag in $R_{\mathrm{c}}-I_{\mathrm{c}}$. The less stringent constraint on $R_{\mathrm{c}}-I_{\mathrm{c}}$ is justified because it is approximately twice as sensitive to effective temperature as $I_{\mathrm{c}}-Z$.
(ii) The star must be redder in $I_{c}-Z$ than the boundary defined by the solid line in Fig. 6.
(iii) The star must lie between 0.9 mag above and 0.25 mag below the chosen isochrone in Figs 4 and 5. In addition, we allow a further degree of freedom by adding the photometric error (the sum of uncertainties in the colour and magnitude after allowing for the gradient of the isochrone). Furthermore, for stars with $R_{\mathrm{c}}-I_{\mathrm{c}}>$ 1.5 we allow another $\pm 0.05$ mag of possible error (in $I_{\mathrm{c}}$ and $R_{\mathrm{c}}-I_{\mathrm{c}}$ ) to allow for plausible uncertainties in the photometric calibration.
(iv) For stars that pass the above tests there is still the possibility that the $I_{\mathrm{c}}-Z$ and $R_{\mathrm{c}}-I_{\mathrm{c}}$ of a star may be incompatible. Although we do not have a good estimate of the intrinsic $I_{c}-Z$ locus at faint magnitudes, we iteratively reject stars that lie more than $4 \sigma$ from a cubic fit to candidate members in the $I_{\mathrm{c}}-Z$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ plot, where $\sigma$ is the appropriately combined photometric uncertainty in both colours. This test is only applied to stars with $R_{\text {c }}-I_{\text {c }}>0.7$ because the sample is dominated at bluer colours by background giants (see Section 3.5).
(v) Finally, those stars that pass all tests and lie more than 0.5 mag above the $I_{\mathrm{c}}$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ isochrone are classified as possible binary systems with large mass ratios. The threshold of 0.5 mag corresponds roughly to mass ratios, $q \geqslant 0.35-0.65$ (see Section 4.5).

Figs 7, 8 and 9 show the results of this selection procedure in the case of the DM97 isochrone in Fig. 5. The selected candidate members are given in Tables A2 and A3 which are available in electronic format - see Appendix A.

### 3.4 Completeness

Completeness is an important issue when deriving LFs and MFs in clusters and is rarely addressed comprehensively in the literature. There are several reasons why members of the NGC 2547 cluster


Figure 7. The selected stars from our total catalogue. Circles are 'single' stars, triangles are possible unresolved, high mass-ratio binary systems. The solid line is the 30 Myr DM97 isochrone used in the selection procedure.


Figure 8. The selected stars from our total catalogue. Symbols as for Fig. 7. The solid line is the locus above which our candidates are required to lie.
may not appear in our final lists of candidate members. (i) They may not be detected at all, either because they are too faint or too close to another star. (ii) They may be flagged as non-stellar or fall on bad pixels or be otherwise flagged as having poor quality photometry. (iii) Their photometry may scatter outside the selection criteria defined in the previous section. It is not sufficient to simply decide upon a magnitude threshold above which one expects to merely detect some fraction of stars.

To estimate completeness we generated a catalogue of 'ghost' stars (see N02), that were scaled copies (with the appropriate noise characteristics) of bright, unflagged stars in the total catalogue. The colours and magnitudes of the ghosts were allocated according to the isochrones defined for $I_{\mathrm{c}}$ versus $R_{\mathrm{c}}-I_{\mathrm{c}}$ in Section 3.2. For $I_{\mathrm{c}}-Z$ we used the isochrone defined in Fig. 6. It is important to provide appropriate colours for the ghosts, as completeness will certainly be colour-dependent. It is impossible to precisely simulate the properties (LF, binary frequency, binary mass ratio distribution) of the cluster without knowing what they are a priori. We made


Figure 9. The selected stars from our total catalogue. Symbols as for Fig. 7 and crosses indicate those stars which passed selection on both CMDs but which have positions in this plot that are $>4$ times their error bar away from the mean trend defined by all other cluster candidates. The abrupt change in slope at $R_{\mathrm{c}}-I_{\mathrm{c}} \leqslant 0.7$ is probably due to heavy contamination by background giants.
the simplification that the cluster can be represented with a single star population and a binary star population with unit mass ratio. Because we allowed quite generous bounds on our selection criteria in Section 3.3, this simplification should not have any great influence on the derived completeness information.

Two simulations were run. The first contained 2013 ghost stars placed on the single star cluster isochrones between $15.75<I_{\text {c }}$ $<22.0$ (we used the DM97 $I_{\text {c }}$ versus $R_{\text {c }}-I_{\text {c }}$ isochrone), with a declining $\mathrm{LF}\left(\mathrm{LF} \propto \exp \left[-I_{\mathrm{c}} / 4\right]\right)$ that roughly mimics that seen in the data (see Section 4.2), although with a shallower gradient. ${ }^{2}$ The second contained 862 ghost stars placed on a binary sequence, 0.75 mag above the single star locus, covering the same magnitude range and with the same LF. This binary frequency (number of binary systems divided by total number of systems) of 30 per cent is about the average frequency of binary systems found (using the definition in Section 3.3) in our data with $R_{\mathrm{c}}-I_{\mathrm{c}}>0.8$.

The ghosts were placed in individual image frames according to their positions in the catalogue. The spatial distribution of the ghosts was tied to the parents from which they were scaled and was approximately uniform. The individual frames were summed and searched and pass through precisely the same operations as the genuine data. The number of ghosts was only a small perturbation (typically $\sim 100$ ghosts in a frame containing 8000 other stars) on the detection efficiency. They did not significantly increase the crowding in the frame and rarely did ghosts interfere with the detection and photometry of another ghost. However, the number of ghosts was large enough compared with the numbers of candidate NGC 2547 members that statistical uncertainties in completeness are unimportant in our final derived LFs and MFs.

CMDs for recovered ghosts that were unflagged and have the required signal-to-noise-ratios are shown in Figs 10 and 11. Some ghosts (a few per cent) were found with colours and magnitudes completely different to those simulated. We examined a number

[^1]

Figure 10. The RI CMD of ghost stars recovered by our detection and photometry procedures and which are unflagged and pass the necessary signal-to-noise thresholds for inclusion as canididate members. The solid and dashed lines show the injected single star and binary sequences.


Figure 11. As for Fig. 10 but for the $I Z$ CMD. The lower of the two solid line indicates the lower envelope for candidate membership in this diagram (see Fig. 8).
of these pathological objects and found that these were instances where the ghost was placed almost directly on top of an already existing star and was not flagged as non-stellar. As most stars in our fields are bluer than the cluster sequence, the photometry of these objects tended to be bluer than expected. This could happen to real cluster stars, so it is appropriate that these are included in completeness considerations. It is also clear that in the absence of detailed a priori knowledge of the mass-ratio distribution, any attempt to determine binary frequencies based on position in the CMDs will be compromised by scatter for $I_{\mathrm{c}}>18.5\left(R_{\mathrm{c}}-I_{\mathrm{c}}>\right.$ 2.0).

We determined two 'completeness functions' (CFs) using these simulations. The first is the percentage of ghosts as a function of $I_{\mathrm{c}}$ that were detected, unflagged and satisfied our signal-to-noise ratio criteria in Section 3.3. The second took the recovered ghosts through the full membership selection procedure, discarding those with colours and magnitudes inconsistent with membership. This


Figure 12. (Top panel: the CF determined either by the fraction of stars that are detected, unflagged and of sufficient signal-to-noise ratio to enter our candidate member catalogue (solid line) or the fraction of stars that pass all the membership criteria (dashed line). Bottom panel: a comparison of this latter definition of CF for the inner 15 arcmin radius subset of our survey (error diamonds) with the CF for the area outside this (error crosses). Note that uncertainties have been estimated using the binomial distribution.
second CF is appropriate for correcting the observed cluster LFs and MFs. Fig. 12 shows the results. The upper plot (for the whole surveyed area) demonstrates that the second definition of CF results in significantly lower completeness at fainter magnitudes - a difference that could change the slope of a completeness-corrected LF or MF.

Both CFs were investigated for any spatial variation. It could be the case that the presence of more bright stars and hence higher and more complicated background in the cluster centre could compromise sensitivity or photometric accuracy. We derived CFs for the inner 15 -arcmin radius (using the cluster centre defined by Littlefair et al. 2003) and compared them to CFs outside this area and these are shown in the lower plot of Fig. 12. There is some evidence that the inner CF is lower for $I_{\mathrm{c}}>19.5$, but not for brighter stars. In subsequent derivations of MFs and LFs we use a linear interpolation of the appropriate CF, depending on whether stars are inside or outside this inner circle. We will also assume that the CF for stars with $I_{\mathrm{c}}<15.75$ is 95 per cent.

### 3.5 Contamination

Another issue hindering accurate reconstruction of LFs and MFs is contamination of CMDs by objects unassociated with the cluster. Our photometrically selected sample of cluster candidates contains contaminants, consisting of background giants and foreground dwarfs. Background G/K giants can be seen in Fig. 2 as a dense 'finger' of contamination dominating the cluster sequence at $0.5<R_{\mathrm{c}}-$ $I_{\mathrm{c}}<0.7$. It is doubtful that evolved stars make much contribution to contamination outside of these colours. The cluster is at galactic latitude $-8^{\circ} 6$ and longitude $264^{\circ} 5$. A background M giant/supergiant with $R_{\mathrm{c}}-I_{\mathrm{c}} \geqslant 1.0$ would have an absolute $I$ magnitude of less than -2 and, in order to have $I_{\mathrm{c}} \geqslant 15$ and encroach on the NGC 2547 PMS, would be at a distance $\geqslant 25 \mathrm{kpc}$ and be more than 3.7 kpc out of the plane. The space density of such objects is essentially zero more than 2 kpc above the plane (Branham 2003) and so if we restrict our analysis to stars with $R_{\mathrm{c}}-I_{\mathrm{c}}>0.7$ then we need not consider contamination by background giants any further.

Contamination by older foreground field dwarfs with similar colours but lower luminosities than the NGC 2547 PMS stars is a more serious problem. The separation of the PMS from the bulk concentration of field objects in the CMDs is encouraging, but a quantitative estimate is desirable. We simulate the field star population using the $I$-band luminosity function of stars within 8 pc (taken from Reid \& Hawley 2000). Taking this local LF (in stars $\mathrm{pc}^{-3} \mathrm{mag}^{-1}$ ) as a weighting function, we assign absolute $I$ magnitudes randomly to a large number of stars. The local LF contains many resolved binary systems, the vast majority of which would be unresolved in our survey. To account for this we assume 75 per cent of stars are part of binary systems (the fraction found in the 8-pc sample), consisting of two stars drawn randomly from the local LF. We further assume that the spatial density varies as $N_{0} \exp (-z / h)$, where $z$ is the height below the galactic plane, $h=270 \mathrm{pc}$ is the scaleheight for low-mass stars (see Kroupa, Tout \& Gilmore 1993) and $N_{0}$ is the density implied by the local LF. We populate a cone of length 1.2 kpc in the direction of NGC 2547 and assume reddening increases linearly at about $E\left(R_{\mathrm{c}}-I_{\mathrm{c}}\right)=0.1 \mathrm{kpc}^{-1}$. Stars are given intrinsic $R_{\mathrm{c}}-I_{\mathrm{c}}$ using an empirical 5-Gyr isochrone, generated as described in Section 3.2. ${ }^{3} I_{\mathrm{c}}-Z$ colours are assigned using a polynomial relationship between $R_{\mathrm{c}}-I_{\mathrm{c}}$ and $I_{\mathrm{c}}-Z$ found for all stars in our catalogue with $17<I_{\mathrm{c}}<19$.

We generate a simulated catalogue corresponding to 5 square degrees of sky coverage - about six times larger than our actual survey area and sufficient to ensure that correction for contamination plays little role in the statistical uncertainties in the final LFs and MFs. To account for measurement uncertainties and completeness we have injected the simulated stars into our data set using the same 'ghosting' technique described in Section 3.4. To restrict the numbers of ghosts to $<5$ per cent of the number of stars in the genuine data, we have clipped the input catalogue to include only those stars with $12<I_{\mathrm{c}}<21.5$ and which lie sufficiently close to the NGC 2547 sequence to stand any chance of contaminating the final membership catalogue.

After running the simulated data through the CLUSTER pipeline we recover 7697 of the original 8391 ghosts, of which 646 had bad quality flags. Fig. 13 shows a subset of the recovered field star ghosts, corresponding to 0.855 square degrees on the sky (we simply plot a fraction of the recovered catalogue). From this the reader can

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Figure 13. The recovered CMD for simulated field dwarfs (see Section 3.5) for a survey area of 0.855 square degrees and including stars out to a distance of 1200 pc . The solid and dashed lines show the DM97 and B02 isochrones that were used to select members in Section 3.3. Only unflagged stars with a signal-to-noise ratio sufficient for membership status are shown.


Figure 14. The luminosity functions (LFs) for contaminating field stars that have colours and magnitudes that would satisfy our membership selection criteria using the DM97 or B02 isochrones (solid and dashed lines), respectively.
judge the level of contamination by comparison with Fig. 2. We pass the full 5 square degree simulated catalogue through our membership selection procedure to find the subset of field stars that would have been selected as candidate members. LFs/MFs (corrected for incompleteness, see Sections 4.2 and 4.3) can be obtained for this contaminating sample from whatever area of the real catalogue we choose to construct the cluster LF/MF. This has the additional advantage of accounting for differing sensitivities due to the overlap regions or variations in exposure time and seeing.

Example 'observed' (i.e. uncorrected for completeness) contaminating field star LFs (taken from the full survey area), expressed in numbers of stars per square degree are shown in Fig. 14. The main feature of the LF is a broad peak at $I_{\mathrm{c}} \simeq 16-17$, which is apparent as an enhancement in the density of contaminating stars in Fig. 2, and which is due to a maximum in the space density of stars with
absolute $I_{\mathrm{c}} \simeq 9$. If the DM97 empirical cluster isochrone is used to select candidate members there are an average 127 contaminating stars per square degree expected for the range $14.25<I_{\mathrm{c}}<20.25$. The B02 empirical isochrone is fainter than that of DM97 for $R_{c}$ $-I_{\mathrm{c}}>1.5$, resulting in more contamination at these colours and a total of 179 contaminants per square degree for $14.25<I_{c}<20.25$.

A test of our contamination simulation is provided by fields 51 and 52 , which are $60-75 \mathrm{arcmin}$ from the cluster centre. There is evidence (see Section 4.1) that the density of cluster candidates is much lower in these fields than in the cluster centre, or possibly zero. If this is the case, then the candidate members in these fields represent the contamination level.

We find 11 candidate members with $14.25<I_{c}<20.25$ in fields 51 and 52 when selected using the DM97 isochrone or 13 when using the B 02 isochrone. Our contamination simulations predict we should have seen $12.4 \pm 0.5$ or $17.5 \pm 0.6$ field dwarf contaminants, respectively. This close agreement offers reasonable support for our contamination model, although we must bear in mind two issues. First, the 8 -pc sample is quite small: there are only 138 stars belonging to 103 systems defining the field star LF. Secondly, the 8-pc sample is probably complete to $M_{I_{\mathrm{c}}} \simeq 12$, but thereafter is likely to be increasingly incomplete (Reid, Gizis \& Hawley 2002). The field dwarfs that contaminate our cluster sample will be those of the right colour and distance to fall within the photometric selection bounds. More distant intrinsically bright stars will be too blue, and very close intrinsically faint stars will be too red. The contribution to the contamination will be dominated by a $\sim 1$ mag range of the nearby star LF, at a distance commensurate with their coincidence with the NGC 2547 PMS. The consequent uncertainties on each of the histogram points in Fig. 14 arising from Poisson errors in the nearby star LF are therefore of order 20 per cent at $I_{\mathrm{c}} \simeq 16$, about 30 per cent at $I_{\mathrm{c}} \simeq 20$ and in all cases larger than the statistical errors in our simulations.

More significantly, an unreddened dwarf with $M_{I_{\mathrm{c}}} \simeq 12$ has $R_{\mathrm{c}}$ $-I_{\mathrm{c}} \simeq 1.95$ and will contaminate the PMS of NGC 2547 at $I_{\mathrm{c}} \simeq$ 18.5 for the DAM 97 isochrone, or $I_{\mathrm{c}} \simeq 19.0$ for the B02 isochrone. At fainter magnitudes in NGC 2547 it is probable that the contamination by field dwarfs is underestimated by the simulation. A comparison of the $5.2-\mathrm{pc}$ sample which is believed to be complete beyond $M_{I_{\mathrm{c}}} \simeq 12$ (but of course contains far fewer stars), suggests that the 8-pc LF could be underestimated by a factor of 2 for $11<$ $M_{I_{\mathrm{c}}}<14$ (Reid \& Hawley 2000). Insufficient area at large distances from the cluster centre has been observed to empirically rule out this possibility. For instance, there are either one or two candidate members with $18.75<I_{\mathrm{c}}<20.25$ lying in fields 51 and 52 , depending on whether the DAM97 or B02 isochrones are adopted. The contamination simulation predicts we should have seen $0.80 \pm$ 0.13 or $2.20 \pm 0.21$ respectively.

## 4 RESULTS

### 4.1 Mass segregation

The work of Littlefair et al. (2003) showed that high-mass stars $\left(>3 \mathrm{M}_{\odot}\right)$ are more centrally concentrated in NGC 2547 than their lower mass siblings. If this trend continued to even lower masses then any derived low-mass LF or MF for NGC 2547 would depend on the radius out to which candidate members are included, unless this radius can be made large enough to encompass most cluster members of all relevant masses. However, the possible problems with uncertain contamination lead to a conflicting need to minimize the radius used for LF/MF estimation.

To look for mass segregation in NGC 2547 we need to assign a mass to each of our candidate members. For candidates classified as single (see Section 3.3), masses are assigned using a relationship between $I_{\mathrm{c}}$ and mass that comes from the same empirical isochrone used to select the members. A complication arises for possible binary systems in that a binary may have twice the (system) mass of a single star with the same colour. In this paper we assume that the $\sim 30$ per cent of candidate members classed as possible binary systems, on the basis that they are $>0.5 \mathrm{mag}$ brighter than the single star isochrone, are all unit mass ratio binary systems with equal luminosity components. We subtract 0.75 mag from their $I_{\mathrm{c}}$ values, calculate the mass of each star as if it were a single star and assume that the system mass is double this. We are actually sensitive to binaries with $q \geqslant 0.35-0.65$ (depending on the colour - see Fig. 22 and Section 4.5) but, because binaries with $q<1$ are redder than the intrinsic primary star colour, we find that this approximation still yields a system mass that is within about 10 per cent of that which would be determined using the correct $q$ value.
Fig. 15 shows the completeness-corrected mass density (per square arcmin) and number density (of systems) for candidate NGC 2547 members with $14.5<I_{\mathrm{c}}<19.5$ (corresponding to $0.71>M$ $>0.057 \mathrm{M}_{\odot}$ for the DAM97 isochrone or $0.72>M>0.060 \mathrm{M}_{\odot}$ for the B02 isochrone), selected using the DAM97 isochrone. The bottom panel of this figure shows the average mass for the candidates. The magnitude limits were chosen to (i) avoid strong contamination by background giants and (ii) avoid any strong spatial dependence in the completeness corrections (see Section 3.4). The dashed histograms show the same quantities for the simulated field dwarf contamination. The plots show the expected concentration of mass towards the centre of the cluster, but there is no sign of any decrease in the average mass with radius. This leads us to believe that there is no strong mass segregation over this mass range. The result is not model dependent. The bottom panel shows the radial dependence of the average mass obtained by repeating the analysis using candidate members and masses assigned using the B02 cluster isochrone. However, the analysis is affected by increasing background contamination as a function of radius and does not yield any quantitative limit on the amount of segregation that could be present.

To overcome these problems we divided the magnitude-selected sample into two subsets with masses above and below $0.25 \mathrm{M}_{\odot}$, corresponding to $I_{\mathrm{c}} \simeq 17.0$ for single stars with both sets of model isochrones. Using the DAM97 isochrone, the average masses of systems in these two subsets are 0.16 and $0.50 \mathrm{M}_{\odot}$, respectively. The bottom two panels of Fig. 16 show the radial number density profiles for the subsets. The horizontal dashed lines on these plots represent the average number density of field objects found for similarly defined subsets in our simulated contamination catalogue.

We fitted these profiles with King functions (see King 1962) plus a constant background density and fixed the tidal radius of the cluster using $r_{t}=1.46 M_{c}^{1 / 3}$ (Pinfield, Hodgkin \& Jameson 1998; Jeffries, Thurston \& Hambly 2001), where $M_{c}$ is the mass of the cluster. Assuming $M_{c}=450 \mathrm{M}_{\odot}$ (see Section 5.2) and a distance modulus of 8.1, then $r_{t}=92 \mathrm{arcmin}$. In one set of fits the background density was fixed at the average value found from the simulated contamination catalogue and in another the background was a free parameter. We were careful to integrate the King profile over the 5 -arcmin radial bins that were necessary to accumulate sufficient counts for chi-squared fitting to be valid. Because all the data lie well inside the tidal radius, the best-fit core radii and normalizations of the King functions are quite insensitive to $r_{t}$. The results of our


Figure 15. Top panel: The (completeness-corrected) spatial mass density of candidate members with $14.5<I_{\mathrm{c}}<19.5$ (based on the DAM97 isochrone) as a function of radius. The dashed line is the equivalent plot for candidate members selected from our simulated field dwarf catalogue (which has much smaller statistical errors) scaled to the correct survey area. (Middle) The (completeness-corrected) spatial density of candidate member systems, the dashed line indicates the candidate member systems selected from our simulated field dwarf catalogue. Bottom panel: The average mass per star system. Circles show the results from the DAM97 isochrone, triangles show the equivalent analysis using the B02 isochrone. The B02 points have been offset to the right by 1 arcmin for clarity.


Figure 16. Radial number density for systems of progressively lower average mass. System masses have been calculated according to the DAM97 isochrones. The solid lines indicate the King profile fits assuming a fixed background density of contaminating field systems, which is indicated by a dashed line. The higher mass fits are assumed to have zero contamination (see text).

Table 2. The results of King model fitting to the radial number density profiles.

D’Antona \& Mazzitelli (1997)

| Average Mass | $0.16 \mathrm{M}_{\odot}$ | $0.16 \mathrm{M}_{\odot}$ | $0.50 \mathrm{M}_{\odot}$ | $0.50 \mathrm{M}_{\odot}$ | $1.89 \mathrm{M}_{\odot}$ | $3.85 \mathrm{M}_{\odot}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $r_{c}$ (arcmin) | $16.5_{-3.6}^{+5.6}$ | $17.9_{-4.7}^{+6.0}$ | $14.7{ }_{-2.5}^{+3.1}$ | $15.4{ }_{-3.1}^{+3.9}$ | $8.6_{-1.9}^{+2.4}$ | $1.4{ }_{-1.3}^{+1.8}$ |
| Normalization ( $\operatorname{arcmin}^{-2}$ ) | $0.141_{-0.024}^{+0.029}$ | $0.147_{-0.028}^{+0.028}$ | $0.222_{-0.033}^{+0.038}$ | $0.227_{-0.032}^{+0.037}$ | $0.195_{-0.047}^{+0.057}$ | $0.289_{-0.126}^{+2.248}$ |
| Background ( $\operatorname{arcmin}^{-2}$ ) | 0.012 | $0.008_{-0.007}^{+0.008}$ | 0.024 | $0.021_{-0.008}^{+0.007}$ | 0.000 | 0.000 |
| $\chi^{2} / n_{\text {dof }}$ | 3.7/6 | 3.5/5 | 5.8/6 | 5.6/6 | 2.2/3 | 2.1/3 |
| $n(25)$ | 83.2 | 89.6 | 123.1 | 129.3 | 70.0 | 8.3 |
| $n\left(r_{t}\right)$ | 138.6 | 153.9 | 195.9 | 209.2 | 95.6 | 9.3 |
|  | Baraffe et al. (2002) |  |  |  |  |  |
| Average Mass | $0.16 \mathrm{M}_{\odot}$ | $0.16 \mathrm{M}_{\odot}$ | $0.51 \mathrm{M}_{\odot}$ | $0.51 \mathrm{M}_{\odot}$ |  |  |
| $r_{c}$ (arcmin) | $11.3{ }_{-3.2}^{+4.2}$ | $11.7_{-4.4}^{+6.1}$ | $14.5{ }_{-2.4}^{+3.1}$ | $16.2_{-3.2}^{+3.9}$ |  |  |
| Normalization ( $\operatorname{arcmin}^{-2}$ ) | $0.131_{-0.035}^{+0.045}$ | $0.132_{-0.038}^{+0.044}$ | $0.208_{-0.032}^{+0.035}$ | $0.220_{-0.033}^{+0.034}$ |  |  |
| Background ( $\operatorname{arcmin}^{-2}$ ) | 0.0267 | $0.026_{-0.011}^{+0.009}$ | 0.0257 | $0.019_{-0.007}^{+0.008}$ |  |  |
| $\chi_{\text {/ndof }}^{2}$ | 2.0/7 | 1.9/6 | 9.9/6 | 9.1/5 |  |  |
| $n(25)$ | 60.6 | 62.8 | 114.5 | 128.4 |  |  |
| $n\left(r_{t}\right)$ | 88.7 | 92.8 | 181.3 | 211.9 |  |  |

fitting are shown in Table 2. For comparison we modelled the radial number density profiles of two higher mass subsets of stars from the membership catalogues of N 02 . The subsets are chosen with $V<$ 9 ( 2.8 to $5.9 \mathrm{M}_{\odot}$, average mass $3.85 \mathrm{M}_{\odot}$ ) and $9<V<13$ (1.1 to $2.8 \mathrm{M}_{\odot}$, average mass $1.89 \mathrm{M}_{\odot}$ ). Masses were assigned to individual systems using the best-fitting empirical $V, V-I_{\mathrm{c}}$ DAM97 isochrone described by N02. The N02 catalogue does not extend beyond a 25 -arcmin radius and so we could not fit the background density, but it is expected to be very small for these brighter subsamples and so we fixed it at zero (see Littlefair et al. 2003).

The results in Table 2 indicate a significant difference in spatial distribution for the high and low-mass stars. Note that because there are only eight stars in the highest mass subsample that we considered, the quoted parameters and uncertainties (based on a chi-squared fitting technique) should not be taken too literally. The mass segregation implied by the much smaller core radius compared with the lower mass subsamples has however been confirmed, using a number of statistical tests, by Littlefair et al. (2003). Our results show only marginal evidence for any further mass segregation below $1 \mathrm{M}_{\odot}$. To put this on a more quantitative basis we fit simultaneous King models to the two subsamples with average mass of $0.50 \mathrm{M}_{\odot}$ and $0.16 \mathrm{M}_{\odot}$ using the ratio of the core radii, expressed as $r_{c, 0.16} / r_{c, 0.50}$, as a free parameter. We find best-fitting ratios of $1.13_{-0.30}^{+0.40}$ for the case of fixed background values and the DAM97 isochrone, or $1.15_{-0.37}^{+0.52}$ if the background densities are allowed to vary. The 95 per cent upper limits to the ratio are 1.92 and 2.16, respectively.
We have also fitted a simple power law of the form $r_{c} \propto M^{-\beta}$ to these two points plus the core radius of the subsample with an average mass of $1.89 \mathrm{M}_{\odot}$. We would expect $\beta=0$ if no mass segregation is present over this mass range or $\beta \simeq 0.5$ in the case of dynamical equipartition (Pinfield et al. 1998). We find $\beta=0.26 \pm$ 0.13 or $\beta=0.30 \pm 0.15$ for the cases of a fixed or free background, respectively, and 90 per cent confidence intervals of $0.07<\beta<$ 0.45 and $0.09<\beta<0.51$.

Selecting candidate members and assigning masses using the B02 isochrone, we obtain essentially indistinguishable results for the subsample with average mass $0.51 \mathrm{M}_{\odot}$, but in the lower mass subsample the empirical and model background estimates are sig-
nificantly higher. This results in smaller core radii estimates (see Table 2), although consistent with those from the DAM97 modelling within the statistical uncertainties. The ratio $r_{c, 0.16} / r_{c, 0.51}=$ $0.78_{-0.14}^{+0.34}$ or $0.74_{-0.16}^{+0.39}$ for the cases of fixed or freely fitted background densities. The 95 per cent upper limits on the ratio are 1.48 and 1.57 , respectively.

We conclude that there is evidence for strong mass segregation between stars with $M>2.8 \mathrm{M}_{\odot}$ and lower mass stars; weaker evidence for mass segregation of stars above and below $1 \mathrm{M}_{\odot}$; that for lower mass stars $\left(<0.7 \mathrm{M}_{\odot}\right)$ the radial distributions are consistent with no mass segregation; that strong mass segregation of the form $r_{c} \propto M^{-\beta}$ with $\beta>0.5$ for $0.1<M<2.8 \mathrm{M}_{\odot}$ is ruled out at the 95 per cent level, and that growth of the core radius by as much as a factor of 2 between $0.16 \mathrm{M}_{\odot}$ and $0.50 \mathrm{M}_{\odot}$ is quite unlikely in the case of the DAM97 modelling and is ruled out for the B 02 models.

### 4.2 Luminosity function

Having established limits on how much mass segregation may be present in NGC 2547 we estimate the cluster LF by binning stars in $I_{\mathrm{c}}$ magnitude bins out to some limiting radius. We choose a radius of 25 arcmin, because this significantly exceeds the core radii for stars of all masses making our LF insensitive to any mild mass segregation, and because beyond this radius the contamination density becomes equal to or greater than the density of cluster stars, compromising the precision of the LF.

The King profile fits in the last subsection allow us to estimate what fraction of cluster members lie inside this radius by comparing the integral of the King profile out to the tidal radius, with that out to a radius of 25 arcmin . These results (for the differing mass subsets) are given in Table 2. Of course the estimates of the numbers out to the tidal radius are reliant on the assumption that a King profile is the correct form for the spatial density at large radii.

The encouraging feature from the point of view of this paper is that, at least for the two lowest mass subsets, the fraction of cluster members inside a 25 -arcmin radius only varies in a narrow range between 58 and 68 per cent depending on mass, background estimate and selected evolutionary model. This is a consequence of the


Figure 17. Top panel: the LF determined using the B02 models to assess cluster membership and contamination by background for the inner 25 -arcmin radius of NGC 2547. The dashed line shows the LF of all stars satisfying the membership criteria. The solid line shows the LF after subtraction of the estimated contamination and the circles with errors bars show the contamination-subtracted LF after correction for incompleteness. Bottom panel: equivalent plots using the DAM97 models for membership selection. Points shown with downward pointing arrows are 2 -sigma upper limits. The asterisks demonstrate the effect of doubling the background contamination at those magnitudes.
lack of demonstrable mass segregation and the relatively consistent estimates of core radii from both the DAM97 and B02 models. Additionally, although the background contamination density varies by a factor of 2-3 between the DAM97 and B02 models in the lowest mass subset, it does not dominate in either until radii greater than 25 arcmin. As a result, when estimating the MFs and the LFs for stars from the survey described in this paper, there is no compelling reason to apply any differential correction due to mass segregation, although such an effect may be present at levels of 10 per cent for $0.1<M<0.7 \mathrm{M}_{\odot}$.

To construct an LF we place cluster candidates into 0.5 mag bins (in $I_{\mathrm{c}}$ ) and apply completeness corrections by incrementing the binned value by the reciprocal of the completeness correction per star. We do the same for the simulated sample of contaminating field dwarfs selected as candidate cluster members and subtract this from the cluster candidate LF, propagating the statistical uncertainties
according to the binomial distribution. The results are shown in Fig. 17 for the cases where the DAM97 or B02 isochrones were used for membership selection. The effects of completeness correction and the contamination subtraction are indicated.

The large peak in the LF at $12<I_{\mathrm{c}}<14.5$ is attributable to contaminating background giants. Our contamination model does not include these, so they are not subtracted correctly. At fainter magnitudes the LF exhibits a shallow rise, reaching a peak at $I_{\mathrm{c}}$ $\simeq 17$, and then declines sharply, reaching a minimum at $I_{\mathrm{c}} \simeq 19.5$ that is consistent with there being no objects in NGC 2547 at this magnitude. Comparing the dashed lines, solid lines and points with error bars in Fig. 17, we can see that the accuracy of the contamination subtraction and completeness correction are unlikely to have a great bearing on the above statements and there also seems to be little model dependency in the results.

The LF appears to rise again for $I_{\mathrm{c}}>20$, but here we have to caution the reader that the completeness corrections are large and the contamination model may itself be incomplete at colours corresponding to these magnitudes (see Section 3.5). Our estimates of the LF are probably upper limits at this point, but Fig. 17 shows that, even if the subtracted contamination in the final three bins is increased by a factor of 2 , it makes little difference to the overall LF shape.

The LF of NGC 2547 (which has a distance modulus of about 8.1) can be compared with LFs found for other young clusters and the field. For example, Barrado y Navascués et al. (2002) find that the $I$-band LF for low-mass members of the $70-90 \mathrm{Myr}$ old Alpha Per cluster peaks at $M_{I} \simeq 10$ and then declines by a factor of three by $M_{I} \simeq 13$. Moraux et al. (2003) find a similar peak in the Pleiades. We have obtained the Pleiades data from Moraux et al. (2003), corrected it for the 30 per cent contamination in the brown dwarf regime suggested in that paper, found the LF, shifted it to match the distance modulus of NGC 2547 and applied an arbitrary normalization to provide an approximate match to NGC 2547 at $I_{\mathrm{c}} \simeq$ 17. The comparison can be seen in Fig. 18, where statistical uncertainties on the Pleiades points are quite similar to those in NGC 2547. The decline in the NGC 2547 LF appears to be steeper than in the Pleiades (and Alpha Per) and the LF peak occurs at $M_{I} \simeq 9$, more like that found for the very young ( $\sim 5 \mathrm{Myr}$ ) Sigma Orionis cluster, by Béjar et al. (2001). Of course because the luminosity-mass relation will be a function of age as young low-mass stars descend their PMS tracks, this is not necessarily surprising. Béjar et al. also show a (marginal) minimum in the $I$-band LF for $11<M_{I}<13$, but their photometrically selected sample may (like ours) be contaminated with non-members at fainter magnitudes.

In Fig. 18 the NGC 2547 LF is compared with the LF of the local 8 -pc sample from Reid \& Hawley (2000), which has been shifted to the distance modulus of NGC 2547 and arbitrarily normalized to agree with the NGC 2547 LF at $I \sim 15$. Here the comparison is far from favourable; there appear to be significantly more faint stars in the nearby sample. Partly this must be an age effect - when comparing stars at similar absolute $I_{\mathrm{c}}$ magnitude in the field and NGC 2547 we are comparing stars with very different masses. For instance, $18.5<I_{\mathrm{c}}<19.5$ corresponds to $0.095>M>0.057 \mathrm{M}_{\odot}$ according to the DAM97 NGC 2547 isochrone. Allowing for the distance modulus of NGC 2547, the same magnitude range corresponds to $0.197>M>0.124 \mathrm{M}_{\odot}$ in a group of stars with age 5 Gyr. If the mass function declines with mass over this range, then it would be unsurprising to find more faint stars in the field sample. The local LF also contains stars from many resolved binary systems (see Section 3.5). The majority of these would not be resolved in NGC 2547 (or other young clusters) and so a straightforward


Figure 18. The contamination-subtracted and completeness corrected LF for NGC 2547 compared with scaled LFs for stars within 8 pc of the Sun (from Reid \& Hawley 2000) and the Pleiades (from Moraux et al. 2003). The dashed line shows the LF for all nearby stars, the solid line shows the LF when binary systems among the nearby stars are assumed to be unresolved (see text). The triangles show the Pleiades LF, and have uncertainties similar to those on the NGC 2547 points.
comparison with the nearby LF is not likely to be valid, as many faint stars in NGC 2547 will be hidden in binary systems. Instead we show in Fig. 18 what the local LF would look like if none of the binary systems were resolved. This accounts for some of the discrepancy, but much remains - and the discrepancy will be enhanced at fainter magnitudes if the 8-pc sample is incomplete.

### 4.3 Mass function

The cluster MF is estimated by calculating the mass of each candidate member using a mass $-I_{\mathrm{c}}$ relationship derived from the isochrones that were used to fit the cluster CMDs. In this paper we define the MF using the form $\mathrm{d} N / \mathrm{d} \log M \propto M^{-\alpha}$, where the canonical initial mass function (IMF) for field stars derived by Salpeter (1955) would have $\alpha=+1.35$.

Unresolved binarity is a problem in two ways: a binary star that appears above the single star cluster locus will be treated as one star with a slightly higher mass than either of its two components. The second problem is that binary stars with unequal mass components will have a derived primary star mass that is approximately correct, but the hidden, lower mass secondary component will not be included in the MF. Sagar \& Richtler (1991), Kroupa (2001) and Chabrier (2003) show that these two effects could result in systematic underestimates of $\alpha$ by between 0.3 and 1 , depending on the mass range considered, the binary fraction and the steepness of the MF.

In Section 4.1 we discussed a simple correction for binarity that results in reasonably accurate estimates of system masses, but does not really assist us in generating the stellar MF because $q$ can only be loosely constrained for the photometric binaries and an unknown fraction of the remaining 'single' stars are actually low- $q$ binary systems. Attempting to correct the observed MF for binarity is important in estimating the total cluster mass, but not for comparing cluster MFs with each other or with the field MF, so long as corrections are applied consistently, or not at all. A caveat is that there must be no significant differences in binary fraction or $q$ distribution.


Figure 19. Top panel: the MF (determined using the B02 models) for the inner 25 -arcmin radius of NGC 2547. The dashed histogram shows the MF of all stars satisfying the membership criteria. The solid histogram shows the MF after subtraction of the estimated contamination and the circles with errors bars show the contamination-subtracted MF after correction for completeness. Bottom panel: equivalent plots using the DAM97 models. Points shown with downward pointing arrows are 2 -sigma upper limits. The smooth dashed curves show the log-normal system IMF for the young disc and open clusters proposed by Chabrier (2003), with an arbitrary normalization.

There is, however, little evidence for any enhanced binary frequency in younger clusters compared to the field (see Bouvier et al. 2001, and Section 4.5). Halbwachs et al. (2003) also conclude that both the binary frequency and the $q$ distributions of field $\mathrm{F}-\mathrm{K}$ binaries and their counterparts in the Pleiades and Praesepe are indistinguishable.

We derive the MF of NGC 2547 in a similar way to that done for the LFs. Each star is assigned to a bin (we use bins of size 0.1 dex in log mass), a completeness correction is applied and the MF due to (completeness-corrected) contamination is subtracted. The MFs for the cases where the DAM97 or B02 models were used are shown in Fig. 19 in the form of $\mathrm{d} N / \mathrm{d} \log M$ versus $\log M$.

The features apparent in the LFs are mirrored here. There is a strong peak in the MFs for $0.7<M<1.0 \mathrm{M}_{\odot}$ which we attribute to contamination by giant stars - the two highest mass points in Fig. 19 should be considered extremely conservative upper limits. Both plots show a roughly flat MF for $0.2<M<0.7 \mathrm{M}_{\odot}$, which then turns downwards towards the brown dwarf regime. There is a
minimum at $I_{\mathrm{c}}=19.5$ corresponding to a $\log M=-1.24$ for the DAM97 isochrones and $\log M=-1.22$ for the B02 isochrones. The MFs are consistent with zero at this point, unless the level of background contamination has been seriously overestimated. However, incompleteness in the local LF used to generate the contaminating sample means that the converse is more likely, especially for the the lowest mass two and three points of the B02 and DAM97 MFs respectively. These should probably be considered (increasingly conservative) upper limits to the MF of NGC 2547.

Many authors have described the MF of the field and young clusters in terms of a power law $\left(\mathrm{d} N / \mathrm{d} \log M \propto M^{-\alpha}\right)$. There are problems with this approach, not least the arbitrary way in which the mass range for the fits is chosen (see below). For the range -1.3 $<\log M<-0.4$ we obtain $\alpha=-1.06 \pm 0.20$ for the DAM97 MF, with a relatively poor chi-squared of 12.0 for 7 degrees of freedom. Alternatively, we obtain $\alpha=-1.23 \pm 0.25$ for the B02 MFs, with a reduced chi-squared of 6.2 . However, it would also be perfectly reasonable to model both MFs with a flat function ( $\alpha \simeq 0$ ) for -0.8 $<\log M<-0.2$ followed by a rather steeper decline with $\alpha \simeq-$ 2 below this.

A value of $\alpha \simeq 0$ for $-0.8<\log M<-0.2$ is rather typical of that found in the field and for a number of young clusters such as the Pleiades (see Meusinger, Schilbach \& Souchay 1996; Gould, Bahcall \& Flynn 1997; Kroupa 2001). It is also consistent with the results obtained for stars overlapping this mass range in the NGC 2547 survey of N02. Chabrier (2003) hypothesises that the disc MF has a log-normal form (shown as a smooth dashed curve with arbitrary normalization in Fig. 19), with a characteristic mass (when binary systems are not resolved) of $0.22 \mathrm{M}_{\odot}$ and a Gaussian sigma of 0.57 dex. The field MF is not well constrained below $0.1 \mathrm{M}_{\odot}$, but Chabrier claims that an extension of this log-normal form does a reasonable job of describing the very low mass and substellar MF in a number of young clusters, notably the Pleiades and Alpha Per. The authors that obtained the data upon which this conclusion is based have tended rather to fit power-law MFs with indices of -0.2 $<\alpha<-0.6$ over a variety of mass ranges within the limits $-0.4<$ $\log M<-1.6$ (e.g. Béjar et al. 2001; Barrado et al. 2002; Jameson et al. 2002; Moraux et al. 2003).

Our MF for NGC 2547 is reasonably consistent with Chabrier's log-normal model down to masses of $0.2 \mathrm{M}_{\odot}$, but then declines more steeply. When expressed as a power law, the MF for NGC 2547 also seems to drop more rapidly towards lower masses than in most young clusters. Much of this discrepancy may be down to the variation in mass limits over which power-law fits are applied. A better way to compare clusters is to derive MFs from the original data using the same magnitude-mass relationships. Taking the $I_{\mathrm{c}}$ magnitudes for stars and brown dwarf candidates in the Pleiades (Moraux et al. 2003), we have used the $I_{\mathrm{c}}$-mass relationships used in this paper to calculate the Pleiades MF. As discussed by Moraux et al., we apply no correction for mass segregation and correct for 30 per cent contamination among the brown dwarf candidates.

Fig. 20 shows the comparison between the MFs of NGC 2547 and the Pleiades (derived using DAM97 models, an age of 120 Myr and a distance modulus of 5.6). The MFs have been scaled to roughly agree with that of NGC 2547 at $0.3 \mathrm{M}_{\odot}$. The agreement between the MFs is exceptionally good down to the substellar limit, with a similar level of statistical precision in both clusters. There is then a suggestion that there are fewer brown dwarfs in NGC 2547 than the Pleiades. This statement is based on one well-defined point in the MF (at $\log M=-1.15$ ), which is about 5-sigma discrepant from the Pleiades point, and the knowledge that lower mass points in NGC


Figure 20. The corrected MF (for the inner 25 arcmin radius) of NGC 2547 (circles) compared with the MF of the Pleiades (triangles) derived from data presented by Moraux et al. (2003). Both MFs were calculated using empirical $I_{\mathrm{c}}$ versus mass relationships derived from the DAM97 models. An arbitrary normalization has been applied to the Pleiades points as well as a small shift in $\log M$ to clearly distinguish the two sets of points.

2547 may well be afflicted with a higher level of contamination than we have assumed. The Pleiades MF also features a $\sim 2 \sigma$ dip at $\log M=-1.05$. Dobbie et al. (2002) have suggested that sharp dips in the MF close to the substellar limit may be as a result of an imperfect understanding of cool atmospheres and hence the massmagnitude relationship (see Section 5.3). The Pleiades MF also seems a little inconsistent with the log-normal form proposed by Chabrier (2003) and this is not changed if the MF is calculated using the B02 isochrones.

Both data sets favour a narrower Gaussian sigma of around 0.4 in $\log M$, although the point at $\log M=-1.15$ in NGC 2547 would still lie well below even this model. Finally, as a cautionary tale, we find that a power law MF fitted between $-1.6<\log M<-0.4$ in the Pleiades yields $\alpha=-0.77 \pm 0.12$ (and similar using the B02 models), but a fit between $-1.2<\log M<-0.7$ yields $-1.9 \pm$ 0.6 !

### 4.4 The overall mass function of NGC 2547

We can combine the low-mass MF determined here with the cluster candidates from N02 to estimate a cluster MF over two orders of magnitude in mass $-0.06<M<6.0 \mathrm{M}_{\odot}$. We calculate an MF from the $V$ magnitudes of the N02 survey by using a $V$-mass relationship defined by the empirical 30-Myr DAM97 isochrone used to select members in that paper. For stars with $M>3 \mathrm{M}_{\odot}$ the isochrones of Schaller et al. (1992) are used. The data are corrected for completeness, but no correction is made for binarity and there is assumed to be no contamination.

To compare the MFs from the N02 and our survey we must account for the differing survey areas and the (mass-dependent) spatial distribution of the cluster candidates. The MFs are normalized to what would be seen out to the tidal radius if King profiles accurately represent the spatial distributions. The corrections are applied in a mass-dependent way using the four models (with fixed background) from Table 2. For the record we multiplied the MF contribution from $V<9$ stars by 1.16 , the $9<V<13$ stars by 1.73 , the $V>13$ stars


Figure 21. The 'whole-cluster' MF of NGC 2547 taken from the N02 survey (triangles) and this paper (circles) and using a 30-Myr DAM97 isochrone. Corrections have been made for completeness, and contamination (only for the data from this paper). Approximate corrections have been applied to include all objects out to the cluster tidal radius, accounting for the differing survey areas and mass-segregation (see text). The dashed line shows the form of the IMF proposed by Chabrier (2003).
by 1.94 in the N02 data, and the $14.5<I_{\mathrm{c}}<17.0$ and $I_{\mathrm{c}}>17.0$ stars from this paper by 1.59 and 1.67 , respectively.

The final MFs are plotted for both data sets in Fig. 21. Where the data sets overlap in mass, the agreement is reasonable. The N02 MF is higher for $M<0.8 \mathrm{M}_{\odot}$, but this is probably because no contamination has been allowed for - the MF from this paper is far more reliable in this mass range. The 'spike' in the MF at $\simeq 1 \mathrm{M}_{\odot}$, caused by background giants, is lower in the N02 data set because many giants were cleaned from this sample by selection in the $B$ $-V$ versus $V-I_{\text {c }}$ diagram. The cluster is not well fitted by the log-normal plus power-law form suggested by Chabrier (2003), but could be well represented over the range $0.06<M<6.0 \mathrm{M}_{\odot}$ with three power laws, as suggested by Kroupa (2001), with $\alpha \simeq 2.2 \pm$ 0.3 for $1<M<6 \mathrm{M}_{\odot}, \alpha \simeq-0.1 \pm 0.3$ for $0.2<M<0.7 \mathrm{M}_{\odot}$ and $\alpha \simeq-2.2 \pm 0.5$ for $0.06<M<0.2 \mathrm{M}_{\odot}$. As an aid to future work, Table 3 lists our best estimate of the 'whole cluster' MF for NGC 2547.

### 4.5 Binarity

The binary frequency and distribution of binary periods and mass ratios are important diagnostics of the star formation process (e.g. see Halbwachs et al. 2003; Fisher 2004). In Fig. 22 we show the fraction of stellar systems as a function of $R_{\mathrm{c}}-I_{\mathrm{c}}$ that are identified as binary systems according to the photometric selection techniques in described in Section 3.3. The binary fraction is defined as the number of binary systems divided by the total number of systems. The numbers of systems in each case were taken from within a radius of 25 arcmin of the cluster centre, corrected for completeness, and a completeness-corrected number of contaminating field dwarfs from a similar area was subtracted before performing the division.

The bluest bins are based on quite small number statistics and the very bluest bin may contain a few contaminating giant stars. We also cannot trust the results for $R_{\mathrm{c}}-I_{\mathrm{c}} \geqslant 2.0$ for several reasons, as follows. (i) These stars will have $I_{\mathrm{c}} \geqslant 18.5$ and the uncertainties in their colours will confuse the sensitivity of our test for binarity and


Figure 22. Top panel: the frequency of photometrically selected binary systems (with $I_{\mathrm{c}}$ more than 0.5 mag above the single star isochrone) as a function of colour for the DAM97 isochrone selection (solid histogram with errors). The frequency is expressed as number of binary systems divided by total number of systems and has been corrected for completeness and contamination by field dwarfs. The threshold mass ratio $(q)$ value corresponding to a $0.5 \mathrm{mag} I_{\mathrm{c}}$ discrepancy from the single star sequence is shown as a dashed line. Bottom panel: a similar plot when selection is made using the B02 isochrone.
bias it in a way that is difficult to predict (see Section 3.4). (ii) At these faint magnitudes there is a significant difference in the completeness correction for binaries and single stars at the same colour - to the extent that many single stars would simply not have been detected. The binary fraction is then heavily reliant on the accuracy of the completeness corrections at low levels of completeness. (iii) Our estimate of the sample contamination is likely to be too low at these colours. This will likely lower the true binary fraction because the fall off for the background density as a function of decreasing magnitude at a given colour in the CMD is quite steep.

For $0.9<R_{\mathrm{c}}-I_{\mathrm{c}}<1.9$ we obtain weighted mean binary fractions of $0.25 \pm 0.07$ and $0.30 \pm 0.08$ when using the DAM97 and B02 models, respectively. There is marginal evidence that this fraction is higher for $R_{\mathrm{c}}-I_{\mathrm{c}}>1.3$ (corresponding to masses of approximately $<0.56 \mathrm{M}_{\odot}$ and $<0.58 \mathrm{M}_{\odot}$ according to the DAM97 and B02 cluster isochrones we have used). This is counterbalanced by the increasing range of $q$ values to which our binary identification

Table 3. The 'whole cluster' mass function for NGC 2547.

| $\log M$ | $N(\log M)$ | Notes |
| :--- | :---: | :---: |
| 0.75 | $12 \pm 12$ | 1 |
| 0.60 | $18 \pm 10$ | 1 |
| 0.45 | $65 \pm 29$ | 1 |
| 0.35 | $177 \pm 56$ | 1 |
| 0.25 | $212 \pm 61$ | 1 |
| 0.15 | $301 \pm 73$ | 1 |
| 0.05 | $508 \pm 98$ | 1,3 |
| -0.05 | $1524 \pm 175$ | 1,3 |
| -0.15 | $662 \pm 115$ | 1,3 |
| -0.25 | $463 \pm 102$ | 2 |
| -0.35 | $420 \pm 103$ | 2 |
| -0.45 | $426 \pm 104$ | 2 |
| -0.55 | $381 \pm 99$ | 2 |
| -0.65 | $384 \pm 102$ | 2 |
| -0.75 | $461 \pm 106$ | 2 |
| -0.85 | $266 \pm 81$ | 2 |
| -0.95 | $267 \pm 79$ | 2 |
| -1.05 | $143 \pm 61$ | 2 |
| -1.15 | $<92$ | 2,4 |
| -1.25 | $70 \pm 60$ | 2,5 |
| -1.35 | $187 \pm 113$ | 2,5 |
| -1.45 | $170 \pm 163$ | 2,5 |

Notes. 1: Data from N02. 2: Data from this paper. 3: Contaminated by giants. 4: 2-sigma upper limit. 5: Probable additional contamination.
technique is sensitive (see Fig. 22), which ranges (with some slight model dependency) from about $0.65<q<1.0$ at $R_{\mathrm{c}}-I_{\mathrm{c}} \simeq 1.1$ to $0.35<q<1.0$ for $R_{\mathrm{c}}-I_{\mathrm{c}} \simeq 1.9$, due to the changing slope of the cluster single stars locus and the $I_{\mathrm{c}}$-mass relationship.

The deduced binary fraction for M dwarfs in NGC 2547 is similar to binary fractions deduced for field M dwarfs. Fischer \& Marcy (1992) find that $42 \pm 9$ per cent of $M$ dwarf primaries form multiple systems with $q>0.2$. Henry \& McCarthy (1990) find 34 per cent binarity for M dwarfs within 5.2 pc , and the 8-pc sample of M dwarfs has 33 per cent binarity (Reid \& Hawley 2000). These latter two surveys almost certainly suffer from a little incompleteness at the smallest mass ratios. Comparable photometrically selected binarity statistics for young clusters suggests a binary fraction of 26 per cent among the K and early M stars of the Pleiades (with $q>0.4-$ Stauffer et al. 1984) and $36 \pm 5$ per cent for M5-M6 dwarfs in the Pleiades (with $q>0.35$ - Pinfield et al. 2003). We conclude that the binary fraction for M dwarfs in NGC 2547 is consistent with that in either the field or the Pleiades.

## 5 DISCUSSION

Most measurements of the IMF to date have been made in either very young star-forming regions (e.g. IC 348, Trapezium, $\sigma$ Ori), where low-mass stars and brown dwarfs are intrinsically luminous, or in older, rich clusters with large populations of low-mass objects (e.g. Alpha Per, Pleiades, M35, NGC 2516). There are disadvantages to both these methods. In the star forming regions one must contend with the presence of discs, uncertainties in reddening and age as well as spreads in these quantities. In addition there are likely systematic uncertainties in low-mass evolutionary models due to to the non-negligible influence of the initial conditions at very young ages (B02). In older clusters ( $>10 \mathrm{Myr}$ ) these particular systematic uncertainties will be less, but there are then problems with mass seg-
regation and the evaporation of low-mass objects, uncertainties in the colours, bolometric corrections and hence the magnitude-mass relationship for very cool low-mass objects and the observational bias that older clusters necessarily started off very rich and populous in order to exist now in their current form. These very rich concentrations of stars may have had a different IMF to that in less dense star forming regions.

NGC 2547 forms an important bridge between these two categories of objects. It is old enough that age spreads and reddening are not an issue and systematic uncertainties in the evolutionary models are not too important. On the other hand it is not old enough to have undergone very significant mass segregation among its low-mass population and is a smaller cluster than the Pleiades (see below).

### 5.1 The IMF and NGC 2547

The major result of this paper is that the MF of NGC 2547 is remarkably consistent with that of the Pleiades down to the hydrogen burning limit (HBL). Just below the HBL there seems to be a dip in the MF of NGC 2547 that is not present in the Pleiades, or in a number of other young clusters. This dip is present at quite a high level of significance - for example, whereas we might have expected to detect about 10 objects in our NGC 2547 MF (using the DAM97 isochrones and multiplying by the likely level of incompleteness) with $-1.1<\log M<-1.2$ if it had a similar MF to the Pleiades, we only detected two such objects in NGC 2547, both of which have a reasonably high probability of being contaminating objects. Spreading the range to $-1.1<\log M<-1.3$ the comparison becomes about 15 expected from a Pleiades MF versus six seen in NGC 2547 (of which about three are expected to be contamination). At lower masses the MF of NGC 2547 appears to recover to levels seen in the Pleiades, but we cannot be certain that this is the case, because our estimates of the contamination level at colours corresponding to this mass in NGC 2547, are likely to be too low (see Section 3.5).

Our MF for NGC 2547 (and also the Pleiades) appears significantly lower (for $M<0.1 \mathrm{M}_{\odot}$ ), than the log-normal form hypothesised to be universal among young disc clusters and star forming regions by Chabrier (2003). Because of its age NGC 2547 provides a unique constraint on the form of the initial mass function for disc stars, but we must consider several possible sources of systematic error.

### 5.1.1 Methodology problems

The possible problems that could have arisen in our analysis procedures are centred upon (i) subtraction of background contamination; (ii) correction for incompleteness and (iii) model dependence of the results.
(i) A weakness in our analysis is that we were forced to rely upon a model to estimate the background contamination because we did not observe sufficient area at large distances from the cluster to make a precise observational estimate. However, the observations we have were sufficient to show that our background estimates are not likely to be wrong by factors of 2 , except perhaps at the very lowest masses $\leqslant 0.05 \mathrm{M}_{\odot}$, where we make no claim to have accurately determined the NGC 2547 MF. Because of the relatively high contrast between the cluster and background at $r<25 \operatorname{arcmin}$, uncertainties in the contamination cannot change our main conclusions, though they could alter the exact slope of the MF at low masses, particularly if the B 02 isochrones (for which the low-mass cluster members


Figure 23. The contamination-subtracted and completeness corrected MFs for NGC 2547 calculated using DAM97 isochrones at 30 Myr (solid histogram) and a $32 \mathrm{Myr} I_{\mathrm{c}}$ versus mass relation direct from the models of (triangles with error bars) Baraffe et al. (1998). The dashed line shows the arbitrarily normalised young disc IMF proposed by Chabrier (2003).
are more heavily contaminated by background) turn out to be more appropriate than those of DAM97. If anything, we believe our model underpredicts the amount of contamination at the lowest masses, which would lead to fewer brown dwarfs in NGC 2547.
(ii) We have made great efforts to ensure our completeness corrections are as accurate as possible - including a number of effects rarely addressed in the literature to date (for example, the spatial and colour dependence of completeness and the effects of non-Gaussian uncertainties which scatter stars sufficiently for them to be excluded as candidate cluster members). Our survey is substantially complete ( $>60$ per cent for $I_{\mathrm{c}}<19.5$, corresponding to $M \simeq 0.06 \mathrm{M}_{\odot}$. To explain the discrepancy between NGC 2547 and the log-normal disc MF of Chabrier (2003) would require these completeness corrections to be smaller by factors of $2-3$ for $M \leqslant 0.1 \mathrm{M}_{\odot}\left(I_{\mathrm{c}} \geqslant 18.4\right)$. Systematic errors of this size seem most unlikely (see for instance the tests performed in N02).
(iii) We have used those readily available models which cover the required mass range in our data. There are some model dependencies in the results - notably that the DAM97 models do allow the possibility of some mass segregation at low-masses, while the B02 models do not. These differences are as a result of the slightly differing candidate members selected using the two models and the concomitant differences in the estimated levels of contamination. However, the magnitude-mass relationships are remarkably similar and so the MF of NGC 2547 is essentially the same for both sets of models. These magnitude-mass relationships make use of empirical relationships between colour and bolometric correction and an assumed age and distance for the Pleiades. An alternate approach adopted by many authors is to use the theoretical bolometric corrections and magnitudes directly calculated in the Baraffe et al. (1998) nextaen models to estimate masses. To test for sytematic error, we recalculated the MF of NGC 2547 using this technique. The result is shown in Fig. 23 and illustrates very little sensitivity to this change. This is probably because there is very little disagreement between the theoretical bolometric corrections of Baraffe et al. (1998) and the empirical bolometric corrections adopted in this paper over the colour range of interest for NGC 2547. This is not likely to be the case for brown dwarfs in older clusters, where photospheric tem-
peratures may be cool enough for dust formation and hence bluer colours and fainter magnitudes for the same mass. However, Dobbie et al. (2002) have suggested this may be a problem even at temperatures as warm as 2700 K (corresponding to $R_{\mathrm{c}}-I_{\mathrm{c}} \simeq 2.15$ or 2.30 for the B02 or DAM97 model isochrones we have used), causing a dip in MFs derived from models that do not incorporate these effects (see Section 5.3). Such temperatures are present at the faint end of our NGC 2547 sample and we cannot be sure that our MFs are not susceptible to systematic effects ignored (or included incompletely) in all available models.

### 5.1.2 Hidden binary companions

In Section 4.3, we pointed out the problem of unresolved binarity in determining the true MF. We ignored the problem, with the caveat that, when making comparisons with the field and other clusters, we must assume that the binary frequency and $q$ distribution (as a function of mass) is similar. A recent series of papers (Kroupa \& Bouvier 2003; Kroupa et al. 2003) have highlighted that differences in binary properties can lead to apparent differences in the observed MF. The particular example discussed is the apparent deficit of brown dwarfs in the Taurus-Auriga association (TA) compared with the Orion Nebula Cluster (ONC - see Briceño et al. 2002). The hypothesis is that many 'missing' brown dwarfs are still locked in binary systems in the TA, while these binaries have been disrupted in the denser environs of the ONC.

Therefore, a possible solution to the apparent deficit of high-mass brown dwarfs in NGC 2547 compared to the Pleiades could be an enhanced binary fraction, especially of low- $q$ systems. The results discussed in Section 4.5 partly argue against this possibility. The binary frequencies of $q>0.4$ binaries with primary masses $0.1<$ $M<0.3$ are similar to those in the Pleiades. However, there could still be an anomalously high number of $q<0.4$ systems in NGC 2547, which we could not identify with our photometric techniques and in any case we have not been able to estimate a binary fraction below the HBL.

### 5.1.3 Incorrect cluster age

The low-mass isochronal age of NGC 2547 is about 30 Myr , but there has been some debate in the literature concerning this age. Clariá (1982) and Jeffries \& Tolley (1998) find an age of about 50 Myr from the high-mass turn-off in the cluster, albeit defined by only one or two stars. Jeffries et al. (2003) and Oliveira et al. (2003) conclude that the pattern of lithium depletion seen amongst the low-mass members of NGC 2547 may also be best explained (using the same models used to fit isochronal ages) if the cluster age is 50 Myr . A similar pattern is exhibited in other young clusters, where the isochronal age (both low and high mass) is found to be younger than the age determined from Li depletion mechanisms (e.g. Barrado y Navascués, Stauffer \& Patten 1999).

Our low-mass data are incapable of simultaneously fixing the age and distance of NGC 2547, because at ages around 30 Myr the isochrones are almost parallel (certainly for $R_{\text {c }}-I_{\text {c }}>0.5$ see Figs 4 and 5). Hence a change of age can be compensated by a change in distance modulus (considering only the low-mass data presented here). To check the age dependence of our MFs we increase the assumed age of the cluster to 50 Myr and decrease the distance modulus to 7.8 and 7.7 in the case of the B02 and DAM97 models, respectively. These isochrones yield new $I_{\mathrm{c}}$-mass relationships that can then be used to generate MFs.


Figure 24. The contamination-subtracted and completeness corrected MFs for NGC 2547 calculated using DAM97 isochrones at 30 Myr and a distance modulus of 8.1 (solid line) compared with 50 Myr and a distance modulus of 7.7 (points with error bars).

We find that after correction for the differing distance moduli, the mass-magnitude relationships are almost identical over the mass range of interest here. Fig. 24 shows a comparison of the MFs derived assuming a cluster age of 30 and 50 Myr and the DAM97 evolutionary models. Uncertainty in the cluster age at this level cannot affect any of our conclusions.

### 5.1.4 Mass segregation

If mass segregation is present in the cluster then a survey that does not extend to the cluster tidal radius may underestimate the contribution from low-mass stars/brown dwarfs. An example of this is M35, a cluster which is old enough ( 175 Myr ) to be dynamically relaxed (see below), which shows a sharp downturn in its MF below $0.2 \mathrm{M}_{\odot}$ from a survey of limited area (Barrado y Navascués et al. 2001), and which shows clear evidence for mass segregation (Kalirai et al. 2003).

The analysis in Section 4.1 failed to reveal significant mass segregation in NGC 2547 between samples with mean masses of $0.16 \mathrm{M}_{\odot}$ and $0.50 \mathrm{M}_{\odot}$. Mass segregation of the form $r_{c} \propto M^{-0.5}$ is expected in the case of energy equipartion (Pinfield et al. 1998). We can rule this out in the case where we use the B02 isochrones and it is very unlikely when using the DAM97 isochrones.

An approximate calculation can be used to check whether this is reasonable. Jeffries et al. (2000) measured a 1D velocity dispersion of $<0.9 \mathrm{~km} \mathrm{~s}^{-1}$ for solar-mass stars in NGC 2547, although given that this is similar to the estimated radial velocity measurement errors, this must be a very conservative upper limit. This gives a crossing time-scale (for 2 core radii) of $>4 \mathrm{Myr}$. The number of stars/systems $\left(>0.1 \mathrm{M}_{\odot}\right)$ in the cluster is $\sim 500$ and using Binney \& Tremaine's (1987) approximate formula
$t_{\text {relax }} \simeq t_{\text {cross }}\left(\frac{N}{8 \ln N}\right)$,
an estimate for the relaxation time-scale is $>40 \mathrm{Myr}$.
Numerical simulations for general clusters and specifically for NGC 2547 confirm these approximate results (e.g. Adams et al. 2002; Littlefair et al. 2003). At an age of about 30 Myr , little mass segregation is expected in NGC 2547 . That which is, should
affect the highest mass stars first. Hence any major mass segregation seen, such as that obvious between stars with $M>3 \mathrm{M}_{\odot}$ and the rest of the cluster, is most likely primordial in nature. The relatively constant behaviour of the cluster core radius for stars from $0.1<M<0.7 \mathrm{M}_{\odot}$ ) does not support any suggestion that they were formed with a mass-dependent spatial distribution or velocity dispersion.

What little evidence for mass segregation that exists (for the DAM97 models) would have very little effect on the measured MF. Extrapolating the King profiles to the tidal radius we see that the ratio of 0.16 to $0.50 \mathrm{M}_{\odot}$ stars will only increase by a factor of $\simeq 1.05$ from that measured within a radius of 25 arcmin.

### 5.1.5 Evaporation of low-mass objects

N -body simulations show that the process of dynamical relaxation leads to the preferential evaporation of low-mass objects, in addition to mass segregation (e.g. de la Fuente Marcos \& de la Fuente Marcos 2000). Adams et al. (2002) show that dynamical evaporation is unlikely to be a factor until the cluster age is significantly greater than the relaxation time. As there is little sign of mass segregation we can safely conclude that dynamical evaporation is also unlikely to be important in NGC 2547.

However, several authors have put forward models where very low-mass stars and especially brown dwarfs are preferentially expelled from protostellar multiple systems, before they have had chance to accrete significant masses - the 'ejection hypothesis' (e.g. Reipurth \& Clarke 2001; Sterzik \& Durisen 2003). As a result they are likely to have a larger initial velocity dispersion than higher mass stars, resulting in preferential mass segregation and evaporation from a cluster. A number of problems have emerged with the 'ejection hypothesis'. For example, the spatial distribution of lowmass stars and brown dwarfs are found to be similar in some young star forming regions (e.g. López-Martí et al. 2004). Our results cannot directly contradict the ejection hypothesis, because there are too few objects with $M<0.1 \mathrm{M}_{\odot}$ to assess their spatial distribution. The escape velocities for low-mass objects in NGC 2547 and the Pleiades (using the cluster masses derived below) are quite similar at $\sim 1 \mathrm{~km} \mathrm{~s}^{-1}$, so a similar fraction of brown dwarfs might be expected to have escaped in this way.

The early ejection of brown dwarfs from a cluster would result in a cluster MF significantly depleted of brown dwarfs compared with the field. Unfortunately, constraints on the field brown dwarf MF are still too loose to pinpoint any inconsistency between cluster and field MFs at the lowest masses (e.g. Chabrier 2003).

### 5.2 The mass of NGC 2547

The total mass of NGC 2547 can be estimated by summing the number of stellar systems estimated within the tidal radius ( $n_{t}$ in Table 2) multiplied by their average mass, which comes to about $350 \mathrm{M}_{\odot}$. We need to add an extra contribution due to NGC 2547 stars that lie within the magnitude range heavily contaminated by giants. Assuming that the MF is roughly flat and has $\mathrm{d} N / \mathrm{d} \log$ $M \simeq 300$ between $\log M=-0.15$ (corresponding to $I_{\mathrm{c}} \simeq 14.5$ ) and $\log M=+0.05$ (corresponding to $V \simeq 13.0$ ), multiplying by a factor of 1.25 to approximately account for binarity ( 50 per cent binarity and a flat $q$ distribution) and a factor of 1.6 to account for stars out to the tidal radius, we arrive at an extra $100 \mathrm{M}_{\odot}$ in this mass range. The total cluster is therefore about $450 \mathrm{M}_{\odot}$ for
$M>0.057 \mathrm{M}_{\odot},{ }^{4}$ which can be compared with a total Pleiades mass of $735 \mathrm{M}_{\odot}$ derived by Pinfield et al. (1998). Uncertainties in the shape of the mass function, choice of evolutionary isochrones and uncertainties in the King profile corrections make the total mass of NGC 2547 uncertain by no more than $\pm 100 \mathrm{M}_{\odot}$.

### 5.3 Possible variations in the IMF?

Although the MF of NGC 2547 is almost identical to the Pleiades down to the HBL, we have tentatively identified a deficit of highmass brown dwarfs in NGC 2547. We can go further and state that, because our contamination model suffers an unknown level of incompleteness for masses less than about $0.06 \mathrm{M}_{\odot}$ in NGC 2547, our analysis (using either the DAM97 or B02 models) is consistent with there being no brown dwarfs in NGC 2547. Clearly this requires further testing. In particular, a deeper, wider survey, perhaps incorporating near-infrared data, would provide a much more secure empirical estimate of the amount of background contamination at very red colours.
Many believe that the IMF in young clusters and associations may be universal (e.g. Kroupa 2002), but evidence is now emerging for significant differences in the measured MFs in differing star forming regions. The TA and IC 348 young star-forming regions both appear to show a factor of 2 or more deficit in the ratio of brown dwarfs to low-mass stars, when compared with regions such as the Pleiades or the ONC (Briceño et al. 2002; Luhman et al. 2003; Preibisch, Stanke \& Zinnecker 2003). In particular, the MF for IC 348 presented by Luhman et al. (2003) shows a sharp 0.6 dex fall below $0.1 \mathrm{M}_{\odot}$ that is quite reminiscent of what we have found for NGC 2547. These authors speculate that either the low stellar density in these regions or the absence of very high mass stars ( $>6 \mathrm{M}_{\odot}$ ) may be important factors. It could be that the far-ultraviolet radiation from hot stars is an important factor in terminating accretion in low-mass objects, resulting in more brown dwarfs.

The lack of brown dwarfs in NGC 2547 could be interesting in this context. The most massive star in the cluster has $M<6 \mathrm{M}_{\odot}$ and an extrapolation of the high-mass end of the present-day MF suggests that more massive stars may never have been present (see N02).

An alternative explanation might involve an incomplete understanding of cool atmospheres in low-mass stars. Dobbie et al. (2002) have identified a number of 'dips' in the LFs of young clusters (Pleiades, $\sigma$ Ori, Alpha Per, IC 2391) which, whilst individually not very significant, collectively seem to point to a drop in the LF (and consequently the MF) at effective temperatures of about 2700 K . Dobbie et al. interpret this as the onset of dust formation with grains somewhat larger than assumed in most models, which would lead to enhanced opacity at near infrared wavelengths and a modified mass-magnitude relationship. Our observations may support this idea. The 'gap' in the CMD seen in Fig. 7 occurs at colours corresponding to 2800-2900 K in the B02 and DAM97 models. Given the likely systematic errors in $R_{\mathrm{c}}-I_{\mathrm{c}}$ this could be consistent with the 2700 K value proposed by Dobbie et al. If the LF and MF of NGC 2547 really did increase again for $I_{\mathrm{c}}>19.5$ then NGC 2547 might be the clearest example yet of this phenomenon.

[^3]
## 6 CONCLUSIONS

In this paper we have presented optical/near infrared photometry of NGC 2547 that is both deeper and covers a wider area ( 0.855 square degrees) than previously published surveys. The survey has been used to collate a catalogue of candidate members and investigate the degree of mass segregation and the mass function (MF) for the cluster. The main conclusions of our work can be summarized as follows.
(i) The cluster shows strong evidence for mass segregation, in that stars with $M>3 \mathrm{M}_{\odot}$ are much more centrally concentrated than lower mass stars. There is some evidence for mass segregation above and below $1 \mathrm{M}_{\odot}$, but lower mass stars have spatial distributions that are consistent with no further mass segregation for $0.1<M$ $<0.7 \mathrm{M}_{\odot}$. By fitting King profiles we have estimated that at least 60 per cent of the cluster's low-mass population is included within our survey.
(ii) The MF for $0.075<M<0.7 \mathrm{M}_{\odot}$ in NGC 2547 has been determined with roughly the same statistical precision as available for the best Pleiades studies (and much more precisely than field MF determinations) and is in remarkable agreement with the Pleiades MF (and other young clusters) over this mass range. Because of its age ( $\simeq 30 \mathrm{Myr}$ ), NGC 2547 is not badly affected by a number of systematic uncertainties which could well affect studies of both younger and older clusters (age spreads and uncertainties, reddening, discs, very cool atmospheres, dynamical evolution) and neither are our results very dependent on which stellar evolutionary models are used. Our analysis therefore represents one of the most precise and robust determinations of a low-mass disc population MF, and possibly the initial MF if primordial velocity dispersions are reasonably mass-independent.
(iii) Below the hydrogen burning limit we have identified an apparent dearth of high-mass brown dwarf candidates in NGC 2547 ( $0.05<M<0.075 \mathrm{M}_{\odot}$ ). This deficit may extend to lower masses, but increasing incompleteness in both our survey and our estimates of contaminating foreground M dwarfs leave this question open. Alternatively, we may be seeing an example of the 'missing M dwarf' phenomenon, identified by Dobbie et al. (2002), which could result from an imperfect understanding of atmospheres with temperatures of around 2700 K and would not reflect a true deficit of brown dwarfs. A deeper, wider survey of NGC 2547 is called for to verify this result, to provide a better empirical estimate of contamination among the lowest mass cluster candidates, and hence show whether the deficit we have seen is merely a dip or a genuine lack of brown dwarfs.
(iv) The total mass of NGC 2547 for stars with $M>0.06 \mathrm{M}_{\odot}$ is $(450 \pm 100) \mathrm{M}_{\odot}$ and about a factor of 2 smaller than the Pleiades.
(v) The binary fraction of M dwarfs in NGC 2547 is between 20 and 35 per cent for systems with mass ratios greater than 0.35 to 0.65 . This fraction is consistent with values determined for populations of low-mass stars found in the field and other young clusters.
(vi) Finally, we have provided in electronic format both our entire photometric catalogue as well as subsets of photometrically selected cluster candidates. These catalogues contain data with robust and precisely determined photometric and astrometric uncertainties.

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## APPENDIX A: CATALOGUES

Three electronic catalogues are available from this paper. The first is our entire photometric/astrometric catalogue, containing 133788 entries. A sample is shown below in Table A1 as a guide to its form and content. We also provide subsets of this catalogue which contain candidate members of NGC 2547, selected according to the criteria in Section 3.3. Table A2 lists the candidate members selected using the B02 isochrone, while Table A3 lists those selected using the DAM97 isochrone. The two catalogues contain 726 and 744 entries respectively, with 682 objects common to both. Note that these catalogues suffer from incompleteness and contamination as described in Sections 3.4 and 3.5. The format of these catalogues is one row per star consisting of a field number (note though that a star may have been detected in more than one field because of the overlaps), star identifier in that field, $x$ and $y$ pixel positions on a reference frame in that field, right ascension and declination (J2000.0), and three sets of magnitude, magnitude error and magnitude flags corresponding to the $I_{\mathrm{c}}, R_{\mathrm{c}}-I_{\mathrm{c}}$ and $I_{\mathrm{c}}-Z$ values respectively. The flags consist of two alphabetic characters for each magnitude, referring to the first and second measurements that contribute to the final magnitude. Objects with no problems in their detection or measurement are flagged 'OO', the other flags are described in Burningham et al. (2003).

The catalogues can be obtained from the online version of the journal at http://www.blackwellpublishing.com/products/journals/ suppmat/MNR/MNR7886/MNR7886sm.htm, from the Centre de Données astronomiques de Strasbourg or the Cluster Collaboration web page at www.astro.ex.ac.uk/people/timn/Catalogues/ description.html

Table A1. A sample of the full photometric and astrometric catalogue for NGC 2547 . The full table is only available electronically.

| Field | Star | J2000 position |  | Pixel position |  | Mag. | $I_{\text {c }}$ <br> Error | Flag | $R_{\text {c }}-I_{\text {c }}$ |  |  | Mag. | $I_{\mathrm{c}}$ <br> Error | Flag |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | RA | Dec. | X | Y |  |  |  | Mag. | Error | Flag |  |  |  |
| 51 | 3612 | 08045.376 | -48 2416.58 | 2036.691 | 66.065 | 25.449 | 0.755 | OE | -5.519 | 0.735 | OE | -0.167 | 0.904 | EE |
| 51 | 4639 | 08045.386 | -48 2811.35 | 2034.791 | 651.172 | 19.949 | 0.105 | OO | 0.798 | 0.113 | OO | -0.180 | 0.196 | OO |
| 51 | 5500 | 08045.386 | -48 2556.23 | 2035.732 | 314.446 | 20.910 | 0.250 | OO | 0.574 | 0.261 | OO | 0.789 | 0.311 | OO |
| 51 | 3903 | 08045.396 | -48 2944.64 | 2033.890 | 883.673 | 19.030 | 0.044 | OO | 0.421 | 0.046 | OO | 0.108 | 0.081 | OO |
| 51 | 2055 | 08045.422 | -48 3013.26 | 2033.065 | 955.029 | 17.524 | 0.021 | OO | 0.540 | 0.023 | OO | 0.273 | 0.033 | OI |
| 51 | 914 | 08045.445 | -48 2458.94 | 2034.706 | 171.642 | 17.425 | 0.026 | NN | 0.413 | 0.029 | NN | 0.161 | 0.033 | NN |
| 51 | 4781 | 08045.484 | -48 3027.57 | 2031.394 | 990.664 | 19.693 | 0.098 | OO | 0.061 | 0.110 | OO | 0.614 | 0.142 | OI |
| 51 | 3497 | 08045.504 | -48 3553.37 | 2028.676 | 1802.636 | 19.215 | 0.052 | OO | 0.745 | 0.056 | OO | 0.338 | 0.069 | OO |
| 51 | 4520 | 08045.527 | -48 2623.64 | 2032.090 | 382.744 | 20.322 | 0.126 | OO | 0.869 | 0.141 | OO | 0.026 | 0.211 | OO |
| 51 | 1225 | 08045.553 | -48 2718.73 | 2031.014 | 520.017 | 17.736 | 0.015 | OO | 0.394 | 0.016 | OO | 0.138 | 0.023 | OO |
| 51 | 3702 | 08045.589 | -48 261.73 | 2030.705 | 328.098 | 18.685 | 0.067 | NN | 0.765 | 0.075 | NN | 0.276 | 0.082 | NN |
| 51 | 1446 | 08045.602 | -483632.15 | 2025.960 | 1899.284 | 17.595 | 0.032 | NN | 0.440 | 0.034 | NN | 0.158 | 0.040 | NN |
| 51 | 1105 | 08045.606 | -48 3539.95 | 2026.239 | 1769.169 | 17.266 | 0.011 | OO | 0.556 | 0.012 | OO | 0.157 | 0.016 | OO |
| 51 | 5222 | 08045.609 | -48 3655.65 | 2025.646 | 1957.868 | 19.032 | 0.099 | NN | 4.309 | 0.755 | NN | -2.119 | 0.154 | NN |
| 51 | 6203 | 08045.622 | -48 331.15 | 2026.984 | 1373.438 | 20.080 | 0.107 | OO | 1.018 | 0.124 | OO | 0.408 | 0.140 | OO |
| 51 | 552 | 08045.629 | -48 2640.95 | 2029.409 | 425.844 | 16.429 | 0.006 | OO | 0.711 | 0.007 | OO | 0.212 | 0.009 | OO |
| 51 | 2619 | 08045.632 | -48 3047.40 | 2027.668 | 1040.092 | 18.994 | 0.044 | OO | 0.460 | 0.046 | OO | 0.072 | 0.072 | OO |
| 51 | 1854 | 08045.635 | -48 2425.17 | 2030.183 | 87.482 | 18.151 | 0.046 | NN | 0.549 | 0.050 | NN | 0.131 | 0.059 | NN |
| 51 | 2059 | 08045.638 | -48 3021.57 | 2027.665 | 975.724 | 17.768 | 0.037 | IO | 0.497 | 0.040 | IO | 0.267 | 0.045 | OI |
| 51 | 2194 | 08045.642 | -48 3420.88 | 2025.907 | 1572.124 | 18.413 | 0.057 | NN | 0.835 | 0.064 | NN | 0.580 | 0.060 | NN |
| 51 | 423 | 08045.668 | -48 263.84 | 2028.733 | 333.376 | 16.348 | 0.006 | OO | 0.554 | 0.007 | OO | 0.183 | 0.008 | OO |

Table A2. A sample of the subset of the full catalogue containing candidate members of NGC 2547 selected using a Baraffe et al. (2002) isochrone (see Section 3.3). The full table is only available electronically.

| Field | Star | J2000 position |  | Pixel position |  | $I_{\text {c }}$ |  |  | $R_{\text {c }}-I_{\text {c }}$ |  |  | $I_{\text {c }}-Z$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | RA | Dec. | X | Y | Mag. | Error | Flag | Mag. | Error | Flag | Mag. | Error | Flag |
| 51 | 48 | 8410.205 | -483126.50 | 1914.251 | 1137.169 | 13.068 | 0.003 | OO | 0.570 | 0.004 | OO | 0.190 | 0.004 | OO |
| 51 | 260 | 8412.936 | -48 2712.39 | 1848.160 | 503.670 | 15.352 | 0.004 | OO | 1.246 | 0.005 | OO | 0.326 | 0.005 | OO |
| 51 | 4399 | 8414.176 | -48 2435.24 | 1818.334 | 111.949 | 20.033 | 0.087 | OO | 2.421 | 0.196 | OO | 0.682 | 0.100 | OO |
| 51 | 31 | 8417.313 | -4828 23.15 | 1739.295 | 679.771 | 12.827 | 0.003 | OO | 0.363 | 0.007 | OO | 0.093 | 0.004 | OO |
| 51 | 2012 | 8419.765 | -48 2858.81 | 1678.399 | 768.470 | 18.473 | 0.025 | OO | 1.786 | 0.039 | OO | 0.579 | 0.029 | OO |
| 51 | 55 | 8423.267 | -48 2443.58 | 1592.836 | 132.166 | 13.799 | 0.003 | OO | 0.705 | 0.004 | OO | 0.250 | 0.004 | OO |

Table A3. A sample of the subset of the full catalogue containing candidate members of NGC 2547 selected using a D'Antona \& Mazzitelli (1997) isochrone (see Section 3.3). The full table is only available electronically.

| Field | Star | J2000 position |  | Pixel position |  | $I_{\text {c }}$ |  |  | $R_{\text {c }}-I_{\text {c }}$ |  |  | $I_{\text {c }}-Z$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | RA | Dec. | X | Y | Mag. | Error | Flag | Mag. | Error | Flag | Mag. | Error | Flag |
| 51 | 48 | 8410.205 | -48 3126.50 | 1914.251 | 1137.169 | 13.068 | 0.003 | OO | 0.570 | 0.004 | OO | 0.190 | 0.004 | OO |
| 51 | 260 | 8412.936 | -48 2712.39 | 1848.160 | 503.670 | 15.352 | 0.004 | OO | 1.246 | 0.005 | OO | 0.326 | 0.005 | OO |
| 51 | 4399 | 8414.176 | -48 2435.24 | 1818.334 | 111.949 | 20.033 | 0.087 | OO | 2.421 | 0.196 | OO | 0.682 | 0.100 | OO |
| 51 | 106 | 8415.530 | -48 2730.30 | 1783.775 | 548.145 | 14.182 | 0.003 | OO | 0.634 | 0.004 | OO | 0.212 | 0.004 | OO |
| 51 | 31 | 8417.313 | -4828 23.15 | 1739.295 | 679.771 | 12.827 | 0.003 | OO | 0.363 | 0.007 | OO | 0.093 | 0.004 | OO |
| 51 | 55 | 8423.267 | -4824 43.58 | 1592.836 | 132.166 | 13.799 | 0.003 | OO | 0.705 | 0.004 | OO | 0.250 | 0.004 | OO |

This paper has been typeset from a $\mathrm{T}_{\mathrm{E}} \mathrm{X} / \mathrm{EA} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ file prepared by the author.


[^0]:    ${ }^{1}$ We use RI data for confirmed Pleiades proper-motion members from Stauffer (1982), Stauffer et al. (1984), Bouvier et al. (1998) and Moraux, Bouvier \& Stauffer (2001). Where necessary, Kron-Cousins photometry is transformed to Cousins photometry using the equations in Bessell \& Weis (1987).

[^1]:    ${ }^{2}$ We anticipated that incompleteness would grow with magnitude, so this choice was approximately consistent with the measured LF. N02 explain why an appropriate choice of LF is important.

[^2]:    ${ }^{3}$ The empirical 5-Gyr isochrones generated from the B02 and DM97 models are so similar that it makes no difference which is used for the simulation. The isochrones are also age-insensitive for ages $\geqslant 500 \mathrm{Myr}$.

[^3]:    ${ }^{4}$ Which is what we assumed in order to calculate the tidal radius in Section 4.1. In practice, as the reader might have guessed, it required an iteration of the analysis to arrive at this consistency.

