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## Magnetic resonance fingerprinting with quadratic RF phase for measurement of $T_2^*$ simultaneously with $\delta_f$ , $T_1$ , and $T_2$

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### Abstract

**Purpose:** This study explores the possibility of using a gradient moment balanced sequence with a quadratically varied RF excitation phase in the magnetic resonance fingerprinting (MRF) framework to quantify  $T_2^*$  in addition to  $\delta_f$ ,  $T_1$ , and  $T_2$  tissue properties.

**Methods:** The proposed quadratic RF phase-based MRF method (qRF-MRF) combined a varied RF excitation phase with the existing balanced SSFP (bSSFP)-based MRF method to generate signals that were uniquely sensitive to  $\delta_f$ ,  $T_1$ ,  $T_2$ , as well as the distribution width of intravoxel frequency dispersion,  $\Gamma$ . A dictionary, generated through Bloch simulation, containing possible signal evolutions within the physiological range of  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $\Gamma$ , was used to perform parameter estimation. The estimated  $T_2$  and  $\Gamma$  were subsequently used to estimate  $T_2^*$ . The proposed method was evaluated in phantom experiments and healthy volunteers ( $N = 5$ ).

**Results:** The  $T_1$  and  $T_2$  values from the phantom by qRF-MRF demonstrated good agreement with values obtained by traditional gold standard methods ( $r^2 = 0.995$  and  $0.997$ , respectively; concordance correlation coefficient =  $0.978$  and  $0.995$ , respectively). The  $T_2^*$  values from the phantom demonstrated good agreement with values obtained through the multi-echo gradient-echo method ( $r^2 = 0.972$ , concordance correlation coefficient =  $0.983$ ). In vivo qRF-MRF-measured  $T_1$ ,  $T_2$ , and  $T_2^*$  values were compared with measurements by existing methods and literature values.

**Conclusion:** The proposed qRF-MRF method demonstrated the potential for simultaneous quantification of  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $T_2^*$  tissue properties.

### Keywords

magnetic resonance fingerprinting; multiparametric mapping; quantitative MRI;  $T_2^*$

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CONFLICT OF INTEREST

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## 1 | INTRODUCTION

Transverse relaxation time  $T_2^*$  is an MR tissue property that provides insight into underlying tissue physiology and pathology. The clinical value of such insight has led to the incorporation of  $T_2^*$  contrast-dependent methods such as MR-SWI and BOLD contrast-based techniques within various clinical protocols. The  $T_2^*$  tissue property is affected by tissue iron concentration, making it sensitive to iron containing blood products, and has been observed to change in several disease states. Parkinson's disease is associated with increased iron in the substantia nigra, globus pallidus, and hippocampus.<sup>1-4</sup> Alzheimer's disease has been associated with increased iron stores in the basal ganglia, as well as hippocampal and cortical regions of the brain.<sup>1,5,6</sup> Huntington's disease has been associated with increased iron concentration in the globus pallidus and putamen.<sup>3</sup> Outside of the brain,  $T_2^*$ -sensitive techniques are used to monitor iron overload of the liver and heart in transfusion-dependent patients.<sup>7,8</sup> Iron nanoparticle-based MR contrast agents have also been engineered for versatile biological specificity that rely on MR  $T_2^*$ -sensitive methods for detection.<sup>9</sup>

Empirically,  $T_2^*$  is the exponential decay time constant of the tissue MR signal. This time constant can be decomposed into two components described by the following relationship:

$$\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{1}{T_2'} \quad (1)$$

where  $T_2$  is the time constant of non-refocusable transverse magnetization decay, and  $T_2'$  is the time constant of refocusable transverse magnetization decay arising from intravoxel frequency dispersion. Although both  $T_2$  and  $T_2'$  properties are affected by tissue iron concentrations, neither property alone is specific to pathologies affecting tissue iron.<sup>10</sup> For example,  $T_2$  is also affected by tissue water content, and  $T_2'$  is also affected by macroscopic field inhomogeneities and other sources of tissue susceptibility.<sup>8</sup> Thus, MR methods capable of simultaneous quantification of  $T_2$ ,  $T_2'$ , and  $T_2^*$  properties may provide greater sensitivity and specificity to pathology. For this reason, methods such as the GESFIDE (Gradient-Echo Sampling of Free Induction Decay and Echo)<sup>11</sup> sequence have been developed. These methods require relatively long acquisition times because they must sample both refocused and non-refocused signal echoes, and as a result, have not yet gained widespread adoption.

Magnetic resonance fingerprinting (MRF) is a recently developed framework for the simultaneous quantification of multiple tissue properties.<sup>12</sup> In its initial implementation, the framework was applied to reduce quantification time for brain tissue  $T_1$  and  $T_2$  relaxation properties by incorporating spatial and temporal incoherence to transient signals in a balanced SSFP-based pulse sequence (bSSFP-MRF).<sup>12</sup> Other MRF implementations have since been developed to increase measurement robustness,<sup>13</sup> be applied to other organ systems,<sup>14,15</sup> or quantify additional tissue properties.<sup>16,17</sup> Application of the MRF framework to  $T_2^*$  quantification may enable fast and robust quantification of  $T_2^*$  along with other tissue properties within a clinical exam. However, the initially proposed bSSFP-MRF method has only slight  $T_2^*$  sensitivity.<sup>18</sup>

This work introduces the novel quadratic RF phase-based MRF (qRF-MRF) method for the robust measurement of tissue  $T_2^*$  simultaneously with tissue  $T_1$ ,  $T_2$ , and off-resonance ( $\delta$ )

properties within a single acquisition. The method was adapted from the original bSSFP-MRF method because of its sensitivity to  $T_1$ ,  $T_2$ , and off-resonance ( $\delta_f$ ) properties.<sup>12</sup> The qRF-MRF  $T_2^*$  sensitivity is obtained using a varied RF phase scheme that is able to generate both high signal amplitude and signal dependence to intravoxel variations in  $\delta_f$ . These properties are exploited to generate unique signal evolutions with high SNR within the MRF framework for robust and rapid quantification.

## 2 | THEORY

Traditional bSSFP experiments have a well-characterized amplitude and phase behavior.<sup>19,20</sup> Typical acquisition parameters in bSSFP experiments include constant high flip angle (FA), constant short TR, constant (linear) increment in RF excitation phase (PH), and zero net gradient moment per TR. The signal observed from isochromats are highly dependent on the relative RF phase increment, defined as the difference between the PH increment and the phase accumulated over the duration of a TR due to  $\delta_f$  precession.

Figure 1A shows the amplitude and phase profiles for isochromats with different relative RF phase increments. When using large flip angles, isochromats with a relative RF phase increment approximately equal to an odd multiple of  $\pi$  have high amplitudes and similar phase values at sampling time TE. Signals from such isochromats are coherent during bSSFP experiments, regardless of the presence or absence of  $\delta_f$  variations, due to their similar phase values. Without sensitivity to  $\delta_f$  variations, the generated signals by these isochromats are not sensitive to  $T_2'$ . Isochromats with relative phase increments close to an even multiple of  $\pi$  behave differently. Such isochromats have a steep phase profile, allowing for  $\delta_f$  variation-dependent signal attenuation through phase cancellation. However, these isochromats have low signal amplitude, and signals from them cannot be reliably detected. Without signal regimes with both high amplitude and steep phase profile, the traditional bSSFP experiment is not sensitive to  $T_2'$ , and therefore is not appropriate for  $T_2^*$  quantification.

Adjustments to the typical acquisition parameters during a bSSFP experiment can substantially increase  $T_2'$  sensitivity. Figure 1B shows the amplitude and phase profiles corresponding to a bSSFP experiment with a low FA and a reduced number of preparation pulses. Here, isochromats with an even multiple of  $\pi$  RF phase increment maintain the steep phase profile necessary for generation of  $T_2^*$ -weighted signal through intravoxel signal dephasing, but will transiently develop a large transverse amplitude before its steady state. In fact, this amplitude may surpass 50% of  $M_0$ , even greater than those encountered in traditional bSSFP experiments.

Approaches using such acquisition parameters for  $T_2^*$ -weighted signal generation in bSSFP experiments have been explored previously.<sup>21</sup> These approaches depend on the selection of acquisition parameters such that the resulting  $\delta_f$ -frequencies with steep phase profile coincide with the imaging regions of interest. The  $\delta_f$ -frequencies associated with this band, with the potential for  $T_2^*$ -weighted signal generation, is dependent on the choice of PH and TR used. Since PH and TR may be varied across imaging frames within an experiment, the frequency positions of this band, during the  $n_{th}$  frame, is approximately given by

$$\delta_{f(n)} \approx \frac{PH(n) - PH(n-1) - 2N\pi}{TR(n)^* 2\pi}, \quad (2)$$

where  $N$  is any integer. As traditional bSSFP experiments use constant PH and TR parameters, the resulting band is also constant. The  $T_2^*$  sensitive regimes may be limited due to the macroscopic field inhomogeneity would the imaging FOV. By using a varied PH or TR between frames, the band can vary accordingly and allow for greater FOV coverage.

In the proposed method, a quadratic RF phase increment was selected such that PH was constantly varied. As a result, high-amplitude  $T_2^*$ -weighted signal bands were swept through different  $\delta_f$  values. Figure 1C shows the transient amplitude and phase profiles of an experiment with a quadratic RF phase, demonstrating preserved high amplitude and steep phase characteristics necessary for  $T_2'$  and  $T_2^*$  sensitivity. In this way, macroscopic field inhomogeneity would not limit the sensitive FOV.

### 3 | METHODS

#### 3.1 | Pulse sequence design

The proposed acquisition strategy used in qRF-MRF is based on a bSSFP-type sequence with a varied FA, TR, and PH. Pulse sequence FAs, TRs, and PHs were selected to generate unique signal shapes for combinations of  $\delta_f$ ,  $T_1$ ,  $T_2$ , and intravoxel frequency dispersion properties within clinically relevant ranges. Figure 2A–C shows the FAs, TRs, and PHs used in the proposed method. Because bSSFP-MRF already fulfills both pulse sequence design criteria for the subset of  $\delta_f$ ,  $T_1$  and  $T_2$  properties, the initial 900 time frames of the proposed qRF-MRF method were performed using the identical FA, TR, and PH scheme as the bSSFP-MRF method,<sup>12</sup> organized into 3 “bSSFP blocks” of 300 frames each.

For the remaining frames, a new scheme of acquisitions, using seven repeated “qRF blocks” dedicated toward intravoxel frequency dispersion sensitivity, was performed by using low FA with quadratically varied PH increment. The FA pattern (Figure 2A) of each qRF block consisted of a smoothly varied base shape that ranged from  $0^\circ$ – $6^\circ$  for odd-numbered blocks, and  $0^\circ$ – $12^\circ$  for even-numbered blocks. The qRF blocks used a constant 11.5-ms TR (Figure 2B). Within the first and second halves of each qRF block, the PH (Figure 2C) of the piecewise  $n_{th}$  frame is given by

$$PH(n) = -1.24 * n^2 + 180n \quad (3)$$

and

$$PH(n) = -1.24 * n^2 - 180n, \quad (4)$$

respectively. Each qRF block consisted of only 293 frames to reduce repetition of combinations of the sampled gradient trajectory with the FA, TR, and PH acquisition parameters used throughout the method. Finally, 49 frames, acquired with  $0^\circ$  FA excitation, were appended to the end of the sequence, such that a total of 3000 frames were acquired in the method, consistent with the bSSFP-MRF method.

Figure 2D shows the corresponding frequency positions of  $T_2^*$ -sensitive bands during different frames of the method, as calculated by Eq. (2). These bands remain relatively stationary near  $\approx \pm 40$  Hz during the initial 900 frames, where constant alternated RF phase is used. Minor fluctuations in the position of resonance bands during these frames occurs as a result of the variations in TR. However, isochromats with  $\delta_f$  values near bands during these frames develop the signal voids typically associated with bSSFP null-bands due to the relatively high FA. After the qRF blocks are initiated, the bands linearly traverse the full span of possible  $\delta_f$  values. During these frames, isochromats develop transverse magnetization amplitude during particular frames, depending on  $\delta_f$  value, an example of which is shown in Figure 2E. For frames in which a band traverses through a given isochromat's  $\delta_f$  value, a high transverse magnetization is developed.

A variable-density spiral trajectory<sup>22</sup> designed with zeroth-moment and first-moment nulling was used to acquire data. The spiral trajectory required 24 and 48 interleaves to fully sample the inner and outer region of k-space, respectively. One spiral interleaf was sampled each frame, resulting in highly undersampled k-space data per frame. Previous MRF methods used a constant rotation of  $7.5^\circ$  of the spiral trajectory between frames to obtain spatial incoherence. In the current method, incoherence was further increased by adopting a bit-reversed ordering of sampled spiral interleaves that repeated itself every 48 frames. All acquisitions were single slice with FOV =  $300 \times 300$  mm<sup>2</sup>, matrix size =  $256 \times 256$  (in-plane pixel size of  $1.2 \times 1.2$  mm<sup>2</sup>), and slice thickness of 5 mm. All 3000 frames for each single 2D slice were acquired in 35 seconds.

### 3.2 | Dictionary

A dictionary-based approach was used to perform parameter estimation for  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $T_2^*$  properties from undersampled image frame data following reconstruction. The dictionary used for parameter estimation was generated in two steps. First, a base dictionary,  $S_{base}(n, \delta_f, T_1, T_2)$ , describing the signal at each of the 3000 frames,  $n$ , for different combinations of  $\delta_f$ ,  $T_1$  and  $T_2$  values, was simulated using the Bloch equation as described previously.<sup>12</sup> This base dictionary was calculated for a wide range of 421 possible  $\delta_f$  values, 89 possible  $T_1$  values, and 99 possible  $T_2$  values. Values for  $\delta_f$  ranged from  $\pm 70$  Hz with 0.33-Hz step size. Values for  $T_1$  ranged from 50 ms to 3700 ms with a variable step size, in which each value was 5% greater than the value immediately smaller than it. Values for  $T_2$  ranged from 5 ms to 135 ms with a constant step size of 3 ms, and then 135 ms to 2000 ms with a variable step size, each with a value 5% greater than the value immediately smaller than it.

This base dictionary was then convolved by a shape function,  $L(\delta_f, \Gamma)$ , to generate the full dictionary,  $S(n, \delta_f, T_1, T_2, \Gamma)$ , such that

$$S(n, \delta_f, T_1, T_2, \Gamma) = (S_{base}(n, \delta_f, T_1, T_2) * L(\delta_f, \Gamma))[\delta_f]. \quad (5)$$

In the current work, the shape function was limited to a Lorentzian distribution, parameterized by the  $\Gamma$  value that represents the FWHM of the distribution as described by

$$L(\delta_f, \Gamma) = \frac{\frac{\Gamma}{2}}{\delta_f^2 + \left(\frac{\Gamma}{2}\right)^2} . \quad (6)$$

Although the Lorentzian distribution may not precisely reflect the underlying distribution in vivo, this shape was chosen such that the pulse sequence simulation of a gradient-echo (GRE)-type pulse sequence would generate a monoexponentially decaying transverse signal evolution. Curve-fitting this simulated signal evolution would yield the decay time constant,  $T_2^*$ , given by

$$\frac{1}{T_2^*} = \frac{1}{T_2} + \pi \Gamma . \quad (7)$$

Shapes, given by  $L(\delta_f, \Gamma)$ , were generated for 52 different values of  $\Gamma$ . Values for  $\Gamma$  ranged from 0 (the Dirac delta function) to 40 Hz. Between the values of 0 Hz and 0.825 Hz,  $\Gamma$  varied with a constant step size of 0.075 Hz. Between 0.825 Hz and 40 Hz,  $\Gamma$  increased with a variable step size that increased 10% per value. Before the convolution step in Eq. (5), each Lorentzian shape was truncated to span  $\pm 20$  Hz and normalized. After computation,  $S(TR, \delta_f, T_1, T_2, \Gamma)$  was decimated to 1-Hz resolution in  $\delta_f$  values to reduce memory requirements. The final dictionary, consisting of 30 251 520 entries, spanned 101 values for  $\delta_f$  that ranged from  $\pm 50$  Hz. Dictionary generation was implemented in MATLAB (The MathWorks, Natick, MA) using custom-developed code.

### 3.3 | Pattern recognition

The inner-product-based pattern recognition method used in this work has been described previously.<sup>12,13</sup> For each pixel, the calculated dictionary and measured time course signals were normalized to their sum-squared magnitudes. The inner products between each pixel and dictionary entry was calculated, and the entry corresponding to the maximum value of the inner product was taken to represent the closest signal evolution to the acquired pixel. The estimated values for  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $\Gamma$  were then derived from this entry. Relative proton density was derived from the scaling factor between the measured pixel signal and the matched dictionary entry. The value of  $T_2^*$  for each pixel was calculated from match-derived  $T_2$  and  $\Gamma$  values using Eq. (7).

### 3.4 | Phantom experiments

To evaluate the accuracy of qRF-MRF, a phantom study was performed. All studies were performed using a 16-channel head receiver array on a Siemens Magnetom Skyra 3T system (Siemens AG Medical Solutions, Erlangen, Germany). The accuracy of  $T_1$  and  $T_2$  were compared against traditional Cartesian spin-echo methods. Both phantom composition and traditional spin-echo methods have been described previously.<sup>23</sup> Briefly, the phantom consisted of 10 cylindrical compartments with different concentrations of gadopentate dimeglumine (Magnevist) and agarose (Sigma-Aldrich, St. Louis, MO). Reference  $T_1$  values were measured using an inversion-recovery spin echo (8 log-spaced TIs ranging from 21 ms-3500 ms with 12-ms TE and 10-second TR). The  $T_2$  values were measured using a repeated spin-echo sequence (7 log-spaced echoes that ranged from 13 ms-203 ms using a

TR of 10 seconds). Reference  $T_2^*$  values used the multi-echo GRE method ( $25^\circ$  FA excitation using 15 linearly spaced echoes ranging from 4 ms-152 ms with a TR of 200 ms).  $T_1$  values were calculated pixel-wise by solving the equation  $S(TI) = a + b \exp(-TI/T_1)$  using a 3-parameter nonlinear least-squares fitting routine. The  $T_2$  values were determined pixel-wise by solving the equation  $S(TE) = a \exp(-TE/T_2)$  using a 2-parameter nonlinear least-squares fitting routine. The  $T_2^*$  values were fit similarly to  $T_2$ . The concordance correlation coefficient (CCC)<sup>24</sup> was used to assess measurement accuracy.

To assess how the number of frames affected quantification, the values for  $T_1$ ,  $T_2$ , and  $T_2^*$  were obtained from the dictionary pattern-recognition process using different numbers of frames. The number of frames was varied from 200–3000 frames with a 200-frame increment.

### 3.5 | In vivo experiments

In vivo volunteer brain data were acquired in an internal review board-approved study, with written informed consent obtained before each scan. The proposed qRF-MRF method was performed in five volunteers. For comparison of quantified  $\delta_f$ ,  $T_1$ , and  $T_2$  properties, bSSFP-MRF<sup>25</sup> maps were acquired using 3000 time frames. For  $T_2^*$  measurement validation, a multi-echo GRE method using Cartesian-based sampling ( $25^\circ$  FA excitation using 11 echoes ranging from 4 ms-80 ms using a TR of 200 ms) was acquired. Quantified properties were assessed for each method in manually drawn regions of interest corresponding to the gray matter, white matter, the substantia nigra, and the red nucleus. The CCC<sup>24</sup> was used to assess agreement between quantified maps by qRF-MRF, bSSFP-MRF, and multi-echo GRE methods.

### 3.6 | Postprocessing

The postprocessing for all fingerprinting data was consistent with previous methods.<sup>12</sup> Acquired spiral data were reconstructed as described previously.<sup>13</sup> Briefly, the nonuniform fast Fourier transform,<sup>26</sup> using measured spiral trajectories,<sup>27</sup> was used to separately reconstruct each undersampled time frame from each coil. These frames were combined using the adaptive coil combination method.<sup>28</sup> Finally, all time frames were normalized to the combined coil sensitivity map.<sup>29</sup>

## 4 | RESULTS

Figure 3 shows example entries from the qRF-MRF dictionary. In each plot, the first 1800 of 3000 total frames of representative signal evolutions are shown. Shown in each subplot are seven signal evolutions that differ in only 1 of the 4 of the varied dictionary properties,  $\delta_f$ ,  $T_1$ ,  $T_2$  and  $\Gamma$ , while the other 3 properties are held constant. During the first 900 frames of the qRF-MRF method, changes in the shape of signal evolutions due to each property of  $\delta_f$ ,  $T_1$ , and  $T_2$  are apparent. This is expected, as the FA, TR, and PH scheme in these frames are identical to bSSFP-MRF. However, only subtle differences can be observed due to variations of the  $\Gamma$  property. Starting from the 901st frame, a different scheme of low FA, constant TR, and quadratic PH starts. During these acquisition blocks, substantial signal shape variations can be observed due to  $\delta_f$ ,  $T_2$ , and  $\Gamma$  properties. As shown in Figure 3A, the frames with

high signal during qRF blocks depends on  $\delta_f$  value. Despite the signal now arising from the sum of a distribution of  $\delta_f$  values, high signal frames are still band-dependent. Changes in  $T_1$  (Figure 3B) during qRF blocks are not as apparent as changes during bSSFP blocks. Changes in  $T_2^*$ , either by a decrease in  $T_2$  (Figure 3C) or increase in  $\Gamma$  value (Figure 3D), result in blunting of high-amplitude signal response during qRF blocks due to the dephasing.

Figure 4 shows the quantitative maps from phantom experiments. Figure 4A–E displays the maps obtained directly through the qRF-MRF dictionary-matching process. The  $\delta_f$  map, shown in Figure 4A, shows substantial variation across the imaging FOV due to in-plane  $B_0$  field inhomogeneity. For most phantom compartments, the  $\delta_f$  variation was restricted between  $\pm 40$  Hz. For these phantom compartments,  $T_1$  and  $T_2$  maps showed homogenous quantification. Pixels that mapped to  $+40$  Hz in  $\delta_f$  also showed errors in  $T_1$  and  $T_2$  quantification. This is due to the null-band behavior of bands for  $\pm 40$  Hz during bSSFP acquisition blocks. The  $\Gamma$  maps were smooth within phantom compartments, but differed in spatial distribution as compared with  $T_1$ ,  $T_2$ , or  $\delta_f$  maps. The  $\Gamma$  in compositionally homogenous phantoms primarily represented the summed effects of in-plane and through-plane  $B_0$  field inhomogeneity. The edges of phantom compartments, in which susceptibility differences near air interfaces can be expected to introduce intravoxel frequency variation, mapped to large matched  $\Gamma$  values. Relative  $M_0$  maps calculated from the ratio between measured and matched signal evolutions are shown in Figure 4E. The relative  $M_0$  map was smooth with the exception of pixels with propagated  $T_1$  and  $T_2$  errors at  $+40$  Hz  $\delta_f$ . Figure 4F shows the corresponding  $T_2^*$  map. The reference multi-echo GRE  $T_2^*$  map is shown in Figure 4G. The CCC between qRF-MRF-measured and GRE-measured  $T_2^*$  maps was 0.90.

Figure 5 shows two example signal evolutions from the phantom experiment with superimposed corresponding matched fingerprints. Both signal evolutions originated from pixels within the same compartment. Dictionary matching of both signals obtained the same  $\delta_f$ ,  $T_1$ , and  $T_2$  values but different  $\Gamma$  values, and thus different  $T_2^*$  values, due to local variations in intravoxel  $B_0$  field homogeneity. High-amplitude noise-appearing undersampling artifacts are apparent within the measured signal evolutions. However, the matching process was still able to recognize the best matching dictionary shape and extract the corresponding  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $\Gamma$  properties.

Figure 6A–C shows the correlation of quantified  $T_1$ ,  $T_2$ , and  $T_2^*$  values obtained using all 3000 frames qRF-MRF against standard spin-echo and GRE methods, along with their corresponding linear regression,  $R^2$  coefficient of determination, and concordance correlation results. Figure 6D–F shows the mean and SD of quantified  $T_1$ ,  $T_2$ , and  $T_2^*$  values according to the number of frames used in the matching process. Quantification of  $T_1$  required fewer frames than  $T_2$  and  $T_2^*$  to accurately quantify. Dictionary matching using less than 900 frames, before the qRF acquisition blocks, showed unreliable  $T_2$  and  $T_2^*$  quantification. After the 900th frame, the SD of the  $T_2$  and  $T_2^*$  measurements decreased. Slight changes in the mean and SD of the quantification of  $T_1$ ,  $T_2$ , and  $T_2^*$  values was observed as the number of frames increased. Coefficient of variation, defined as the ratio between the SD and the mean of the measurements, for  $T_2^*$  within each compartment is shown in Figure 6G. Due to differences in local  $B_0$  inhomogeneity between phantom compartments, the coefficient of variation between compartments varied considerably



between compartments. However, within the same phantom compartment, the qRF-MRF and GRE methods showed comparable coefficient of variations, with the exception of the shortest  $T_2^*$  compartment. In this compartment, the TEs used for the GRE method insufficiently covered the  $T_2^*$  decay curve, which led to a variability in quantification.

Figure 7 shows representative reference bSSFP-MRF and qRF-MRF maps acquired in vivo. Visually, the qRF-MRF quantitative maps agreed well with maps from comparison bSSFP-MRF. The  $\delta_f$ -maps obtained using both qRF-MRF and bSSFP-MRF showed similar macroscopic  $B_0$  field distributions. Vessels were visible in  $\delta_f$ -maps obtained by both bSSFP-MRF and qRF-MRF. Compared with bSSFP-MRF, the qRF-MRF  $\delta_f$ -map showed smoother matching results. Similar to phantom experiments, errors in  $T_1$  and  $T_2$  can be observed in pixels at  $\pm 40$  Hz  $\delta_f$  in both qRF-MRF and bSSFP-MRF methods. The CCCs between the shown bSSFP-MRF and qRF-MRF maps were  $0.45 \pm 0.11$ ,  $0.89 \pm 0.03$ , and  $0.60 \pm 0.05$  for  $\delta_f$ ,  $T_1$ , and  $T_2$  properties, respectively. The CCC between all bSSFP-MRF and qRF-MRF maps was  $0.35 \pm 0.13$ ,  $0.83 \pm 0.06$ , and  $0.53 \pm 0.11$  for  $\delta_f$ ,  $T_1$  and  $T_2$  properties, respectively.

Figure 8 shows the qRF-MRF quantified  $T_2^*$  maps, corresponding to the same images as in Figure 7, above their respective GRE  $T_2^*$  maps. Vessels are visible in  $T_2^*$  maps obtained by both GRE and qRF-MRF, due to the paramagnetic properties of iron in blood. The CCCs between the qRF-MRF and GRE-estimated  $T_2^*$  maps was  $0.82 \pm 0.06$  for the shown maps, and  $0.77 \pm 0.11$  across all maps. The simultaneously acquired  $\delta_f$ ,  $T_1$ ,  $T_2$ , relative  $M_0$ , and  $T_2^*$  maps by qRF-MRF alongside the corresponding reference method acquired maps can be seen in Supporting Information Figure S1. Results of the region of interest analysis for in vivo  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $T_2^*$  values are listed in Table 1.

Quantitative  $\Gamma$  maps are shown in Figure 9A. Anatomical regions near air–tissue interfaces exhibited large  $\Gamma$  values. Blood vessels exhibited moderate  $\Gamma$  values. A zoomed-in  $\Gamma$  map of axial slice through midbrain structures is shown in Figure 9B. The corresponding  $T_2$  and  $T_2^*$  maps are reproduced in Figure 9C–F using a shared scale and color map. Higher  $\Gamma$  values and decreased  $T_2$  and  $T_2^*$  values within substantia nigra and red nucleus can be observed, due to higher tissue iron content within these tissues. The contrast of fine structures was preserved between qRF-MRF and reference maps.

## 5 | DISCUSSION

In this work, the proposed qRF-MRF method allowed the simultaneous quantification of  $\delta_f$ ,  $T_1$ , and  $T_2^*$  tissue properties in 35 seconds per slice. The accuracy of the method was demonstrated in a phantom and in healthy volunteers. The ability to rapidly, robustly, and simultaneously quantify  $\delta_f$ ,  $T_1$ ,  $T_2$ , relative  $M_0$ , and  $T_2^*$  properties has many potential applications. For instance, through the knowledge of  $\delta_f$ ,  $T_1$ ,  $T_2^*$  and relative  $M_0$  properties, synthetic SWI<sup>30</sup> may be possible, alongside synthetic  $T_1$ -weighted and  $T_2$ -weighted images that require knowledge of  $T_1$ ,  $T_2$ , and relative  $M_0$  properties. Another application lies in improving contrast agent sensitivity. Because MR contrast agents typically induce changes in multiple tissue  $T_1$ ,  $T_2$  and  $T_2'$  properties, simultaneous detection of these properties may be able improve accuracy in contrast agents' detection and quantification.<sup>31</sup> Mapping of  $T_2$  and  $T_2^*$  tissue properties within midbrain structures may also enhance tissue iron

quantification. This may lead to the increased capacity to diagnose and monitor the diseases that are known to accumulate iron in these structures. However, the potential of the proposed qRF-MRF method for each of these applications must still be demonstrated.

The unique signal evolution that develops during qRF acquisition blocks has several beneficial properties for tissue property quantification. With respect to the components of  $T_2^*$  quantification, the imaging frames with highest SNR also have the highest  $T_2$  and  $\Gamma$  sensitivity. Additionally, qRF-MRF appeared to quantify  $\delta_f$  more robustly as compared with bSSFP-MRF. Both in the current and previous<sup>32</sup> works, bSSFP-MRF, using direct pattern matching, was observed to be susceptible to locally discontinuous  $\delta_f$  quantification errors. These errors had the potential to propagate to errors in  $T_1$  and  $T_2$  quantification. The qRF-MRF method appears to be more robust to this type of error.

Previously, a Cartesian EPI readout-based MRF method (MRF-EPI) was proposed for simultaneous measurement of  $T_1$  and  $T_2^*$  tissue properties.<sup>33</sup> The MRF-EPI method differed substantially from the current method in the use of a series of parallel imaging-based single-shot readouts with spoiled GRE acquisitions using variable FA, TE, and TR to generate image series that were sensitive to  $T_1$  and  $T_2^*$  values. Although the MRF-EPI method quantified relatively fewer tissue properties using a lower resolution and matrix size, MRF-EPI only required 10 seconds per slice. Future studies may seek to combine the approach of MRF-EPI with the current proposed method to further enhance robustness and speed of  $T_2^*$  quantification.

Currently, the underlying frequency dispersion distribution during the dictionary-generation process was limited to Lorentzian shapes. This choice was made because simulation of a multi-echo GRE experiment would produce the consistent mono-exponential decay signal behavior assumed during GRE quantification. This assumption may not be accurate or appropriate in various situations. For instance, white matter has been shown to have a myelin signal component with both distinct rapid  $T_2^*$  relaxation and substantial frequency shift.<sup>34</sup> Incorporation of the underlying causes of tissue-susceptibility differences due to vessel geometry or myelin into the signal model has previously been shown to enable potential quantification of these properties.<sup>16,17,35</sup> The qRF-MRF method may be sensitive to these properties as well. Although modeling these additional properties would result in an exponentially larger dictionary size, compression methods have been developed that may enable exploring this potential in the future.<sup>36–39</sup>

Several limitations remain in the proposed method. The first 900 frames of bSSFP-MRF were maintained at the beginning of the qRF-MRF acquisition. This was done because simulations showed decreased signal-shape differences with respect to changes in  $T_1$  during qRF blocks as compared with bSSFP blocks. However, as a result of these high FA bSSFP blocks, the current qRF-MRF method was still susceptible to banding artifacts near  $\pm 40$  Hz, coinciding with the off-resonance position of the bands during the first 900 frames, as shown in Figure 2D. Examples of these artifacts can clearly be seen in the phantom results (Figure 4B–D) corresponding to pixels with off-resonance value near 40 Hz (Figure 4A). Alternative banding-free schemes with sensitivity for  $T_1$ , such as FISP-MRF,<sup>13</sup> will be investigated in the future.

Another limitation of qRF blocks was the relative temporal sparseness of qRF-MRF signals as compared with bSSFP-MRF signals. The choices used in the current method were selected to increase incoherence of aliasing artifacts with respect to the signal evolution. The assessment of the number of frames necessary for accurate tissue-property measurements suggested that after approximately 2000 frames, accuracy of  $T_1$ ,  $T_2$ , and  $T_2^*$  quantification largely stabilized. However, matching precision improved up through the complete 3000 frames. Further improvements to accuracy and robustness may be made by optimizations to the acquisition parameters (FA, TR, and PH choices) or property estimation method, such as by adopting an iterative reconstruction method,<sup>32,40–42</sup> which may improve robustness to aliasing artifacts. These kinds of improvements would enable further reduction in acquisition time, by reducing the number of frames necessary for robust quantification.

Like all quantitative methods, property estimation depends on the accuracy of the underlying signal model. Although qRF-MRF quantification of  $T_1$ ,  $T_2$ , and  $T_2^*$  properties in phantom was shown to be accurate, several discrepancies appeared during in vivo experiments. Gray and white matter  $T_2$  was consistently lower, as measured through qRF-MRF, as compared with both reference bSSFP and literature values. However,  $T_2^*$  measurements in the same regions agreed well with the reference and literature values. Because  $T_2^*$  is directly derived from quantified  $T_2$  and  $\Gamma$  values, this suggests a corresponding underestimation of  $\Gamma$  values in gray and white matter. In one literature study, reports for  $R_2'$  values (theoretically related to  $\Gamma$  by scaled factor of  $\pi$ ) varied from  $2.7 \text{ s}^{-1}$  to  $3.5 \text{ s}^{-1}$  for gray matter, and  $2.8 \text{ s}^{-1}$  to  $4.3 \text{ s}^{-1}$  for white matter, depending on the quantification method used.<sup>43</sup> Although none of the literature quantification methods can be considered a gold standard, the reported values appear to be consistent with an underestimation of  $\Gamma$  in gray and white matter in the current work. Several reasons may explain the accurate  $T_2^*$  measurement yet biased  $T_2$  and  $\Gamma$  measurements in vivo, which are not present in phantom experiments such as magnetization transfer effects.<sup>44</sup> Flow is another possible explanation, as none of the gradients used in the current method were flow compensated. Fresh spins flowing into the imaging plane likely have an additional effect on measured signal evolutions. Given that  $T_2$  and  $\Gamma$  represent the irreversible and reversible components of signal decay, respectively, it is also likely that many other “irreversible” effects in vivo that are not currently in the signal model, including diffusion, motion, magnetization transfer, or eddy current effects, may manifest preferentially as an apparent shortening in  $T_2$  value. These considerations are topics of careful future evaluation.

## 6 | CONCLUSIONS

In this work, we proposed a novel MR method, developed within the MRF framework, that can be used to simultaneously quantify  $\delta_f$ ,  $T_1$ ,  $T_2$ , and  $T_2^*$  properties. Using the flexibility of MRF experiment design, a quadratic RF phase was incorporated in a novel scheme to develop transient signals with high amplitude and a frequency-dependent phase. As a result, signals become uniquely sensitive to intravoxel susceptibility-induced field variation. Combined with Bloch equation-based template-matching approaches, intravoxel field variation can be estimated from measured signals, alongside other tissue properties. Accurate quantification of  $T_1$ ,  $T_2$ , and  $T_2^*$  tissue properties was achieved in phantom experiments at the current pixel sizes in 35 seconds per slice. In vivo experiments showed

robust and artifact-free property maps, with good agreement in  $T_2^*$  quantification with the gold-standard multi-echo GRE method.

## Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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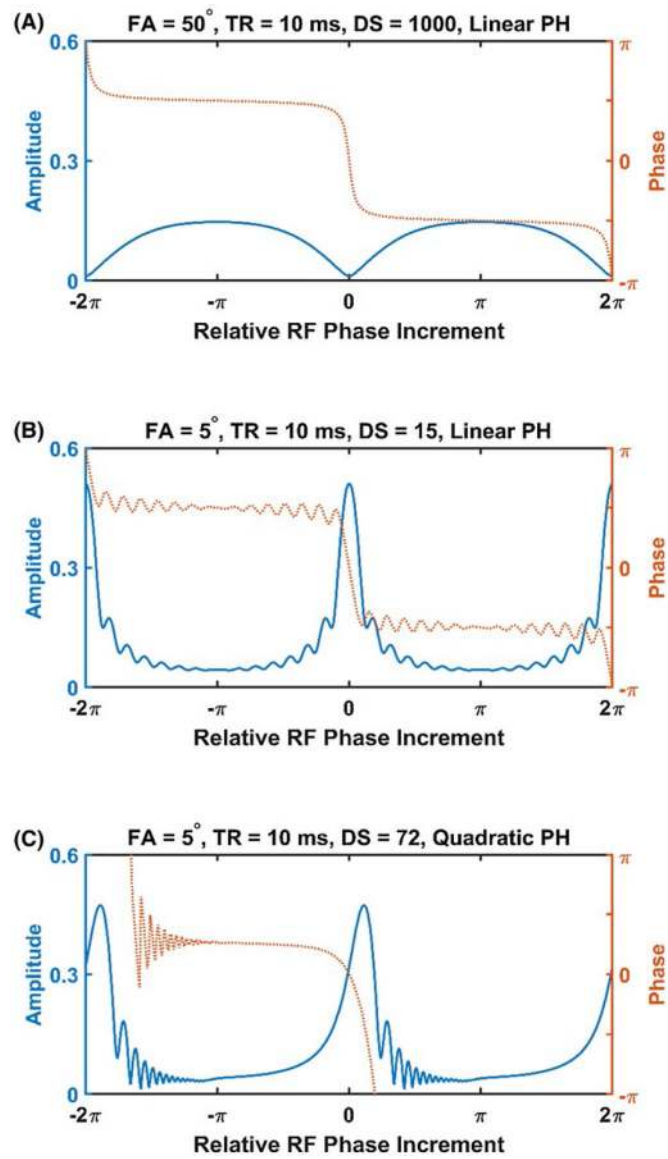
National Institute of Health (F30-HL124894, R01-EB017219, R01-DK098503, R01-EB016728, R01-EB023704, R01-HL073315, R01-HL094557, R21-HL126215, TL1-TR000441, and T32-EB007509) and Siemens Healthineers

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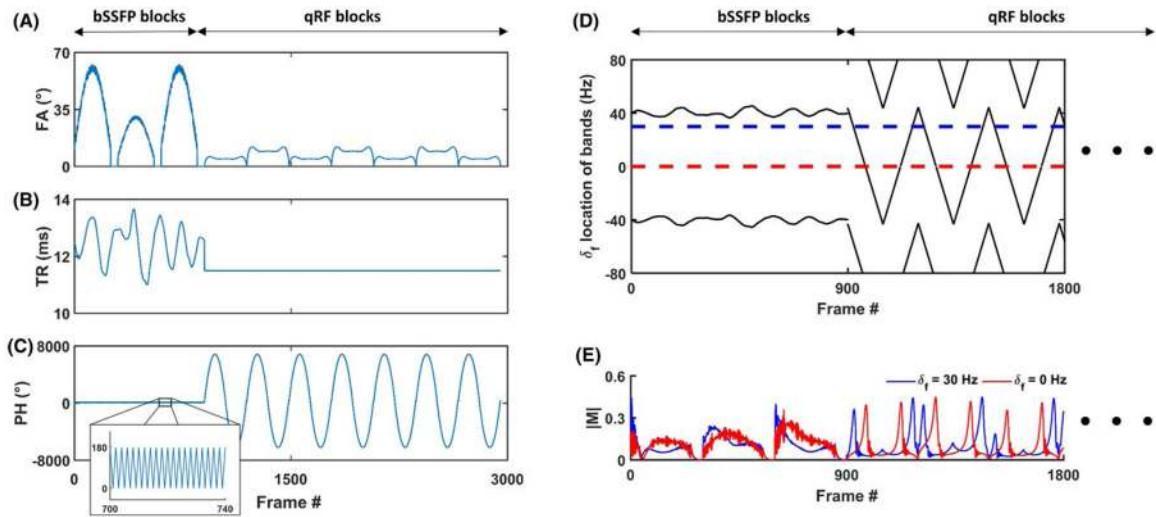
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**FIGURE 1.**

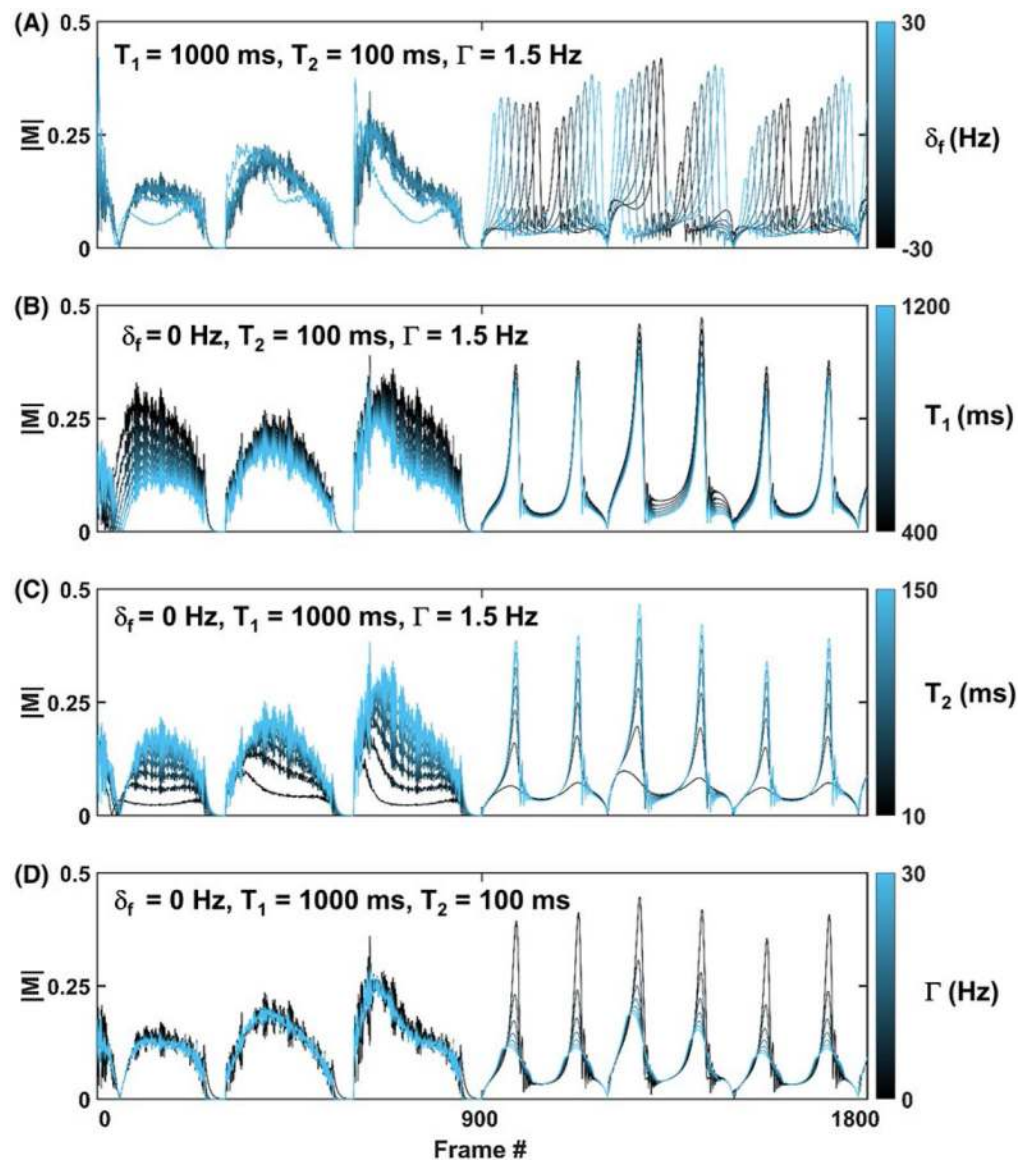
Amplitude and phase responses during variations of balanced SSFP (bSSFP)-type sequences. Responses are plotted as functions of the relative phase increment between consecutive RF phase from a rotating reference frame locked to the isochromat precession frequency. Traditional bSSFP (A) with high flip angle (FA), many preparation dummy scans (DS), and linear RF phase increment (PH) generates high signal amplitude with flat phase response when PH increment is an odd multiple of  $\pi$ . Low FA bSSFP with low DS (B) shows high signal amplitude with steep phase response for PH increments near even multiples of  $\pi$ . Low FA with a quadratic PH evolution (C) shows a similar response profile as low-FA bSSFP. High amplitude and steep phase response is maintained regardless of DS number with quadratic RF phase



**FIGURE 2.**

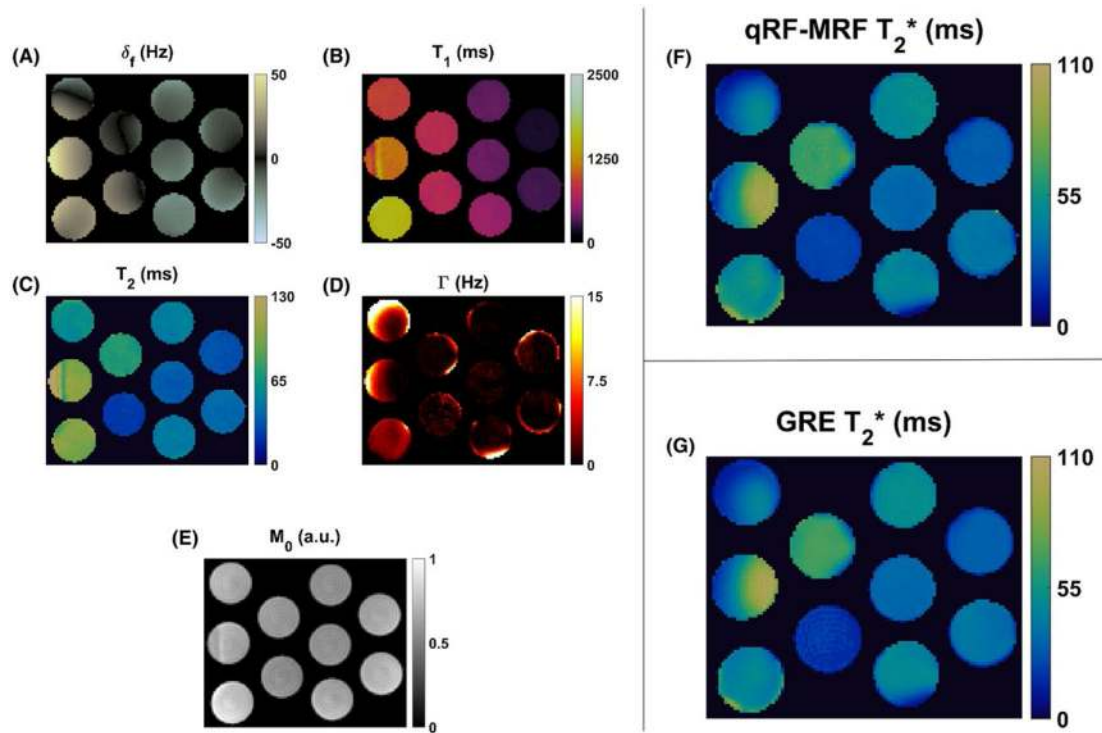
Pulse sequence description. The FA (A), TR (B), and RF PH (C) used during acquisition of each time frame of the proposed method are shown. During the first 900 time frames, three bSSFP-based blocks of excitations are using parameters identical to previously established bSSFP-MRF, including the use of alternated phase cycling. During the latter 2100 time frames, seven quadratic RF (qRF) blocks of excitations are acquired using low FA, constant TR, and quadratic PH acquisition parameters. The resulting off-resonance frequency position of high  $T_2^*$ -sensitive bands (D), calculated using Eq. (2), are shown for the first 1800 frames. Two example signal evolutions (E), differing only in  $\delta_f$  value, are shown to illustrate signal behavior caused by the addition of quadratic phase RF. During quadratic RF lobes, high-amplitude signals from isochromats develop whenever resonance bands intersect the respective  $\delta_f$  value





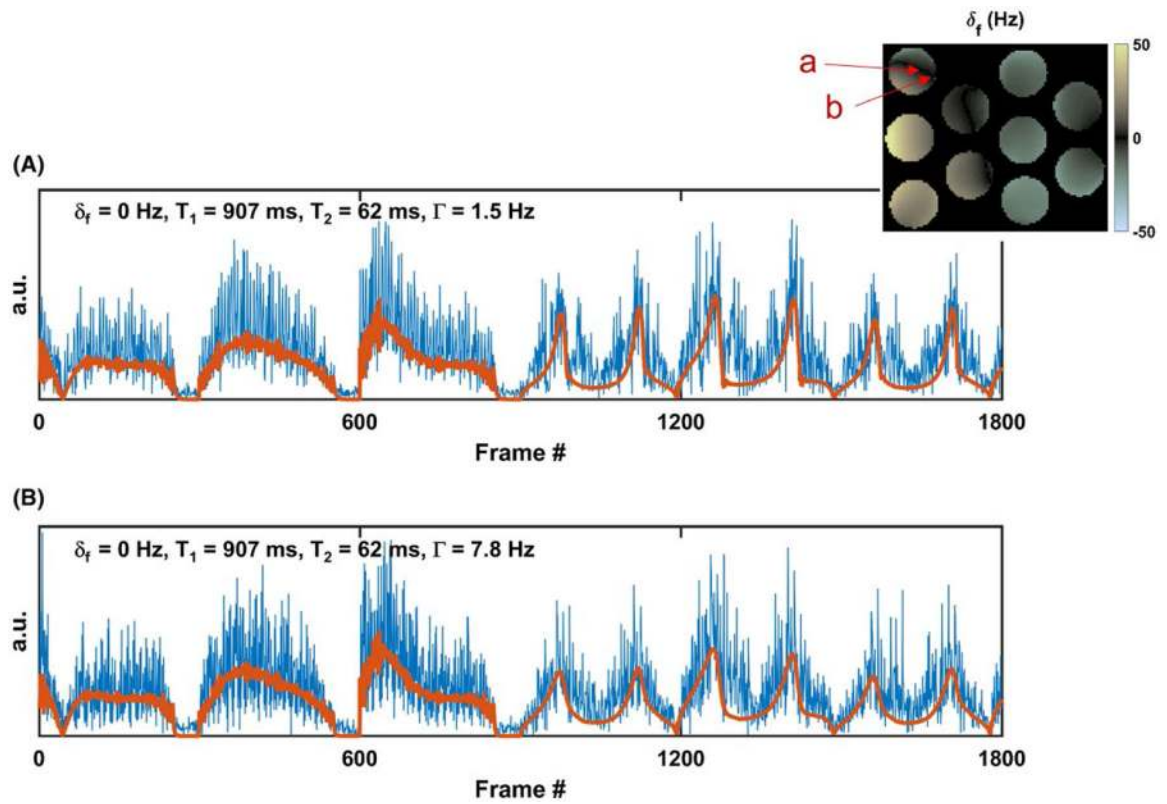
**FIGURE 3.**

Sets of representative dictionary entries. In each plot, only 1 of the 4 matched dictionary properties is varied (color bar), whereas the remaining 3 are fixed (values shown in insets). The 4 matched dictionary properties are  $\delta_f$  (A),  $T_1$  (B),  $T_2$  (C), and intravoxel frequency dispersion  $\Gamma$  (D)

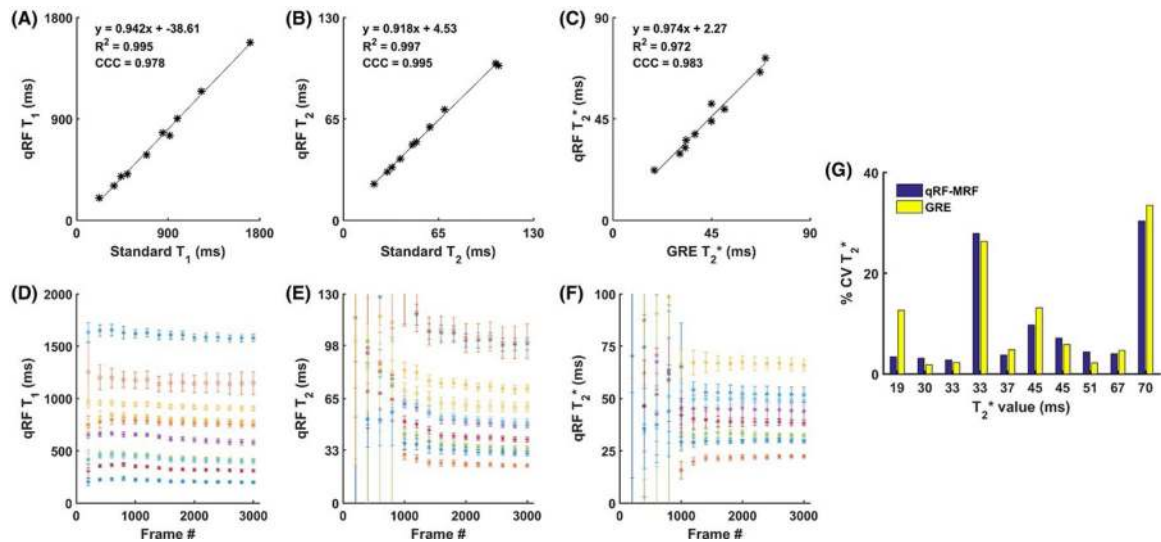


**FIGURE 4.**

Values of  $\delta_f$  (A),  $T_1$  (B),  $T_2$  (C),  $\Gamma$  (D), and relative  $M_0$  (E) are shown for phantom with varied concentrations of gadopentate dimeglumine and agarose generated using qRF-MRF. The resulting qRF-MRF  $T_2^*$  map (F) shown was derived from  $T_2$  and  $\Gamma$  maps using Eq. (7). The comparison multi-echo gradient-echo (GRE) quantified  $T_2^*$  map (G) is also shown

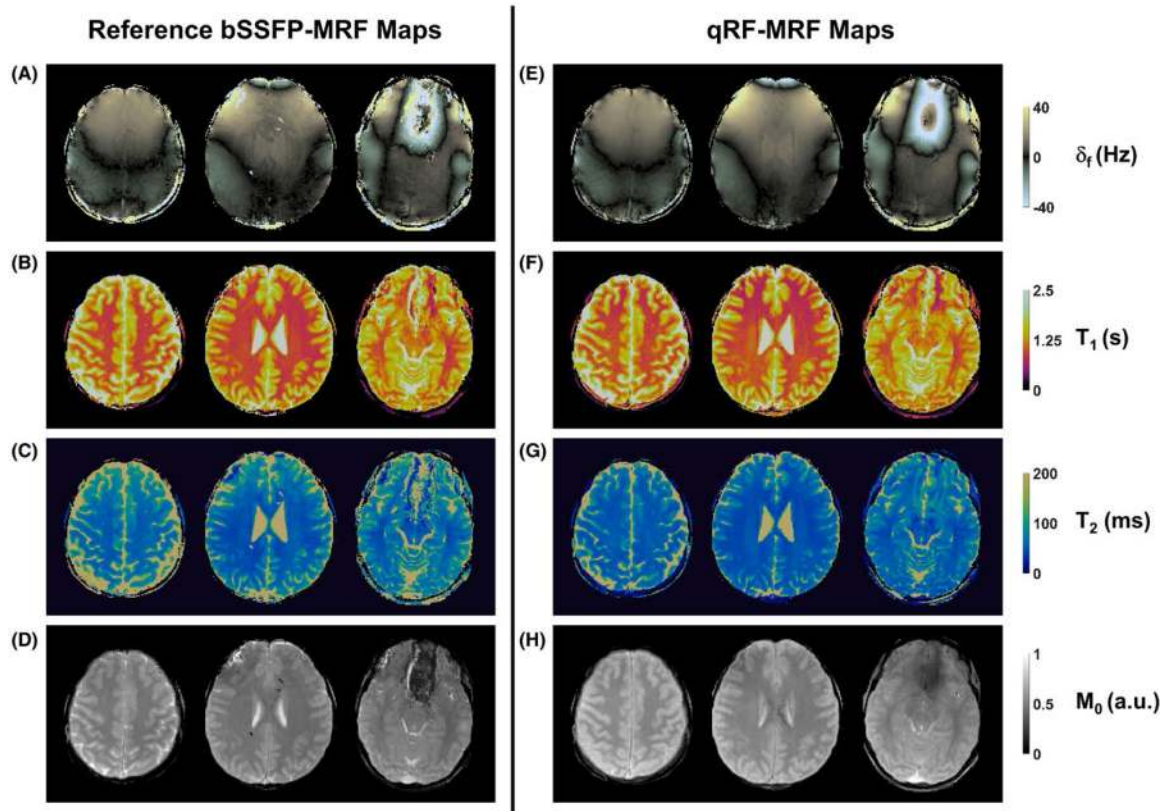
**FIGURE 5.**

Example undersampled time-frame data, with best matching dictionary entries, from two pixels originating within the same homogenous phantom compartment shown in Figure 4 ( $\delta_f$  subfigure reproduced in inset). Differences in underlying signal shapes represent differences primarily caused by local field homogeneity within pixels. Property values extracted from the best dictionary matches are shown in inset



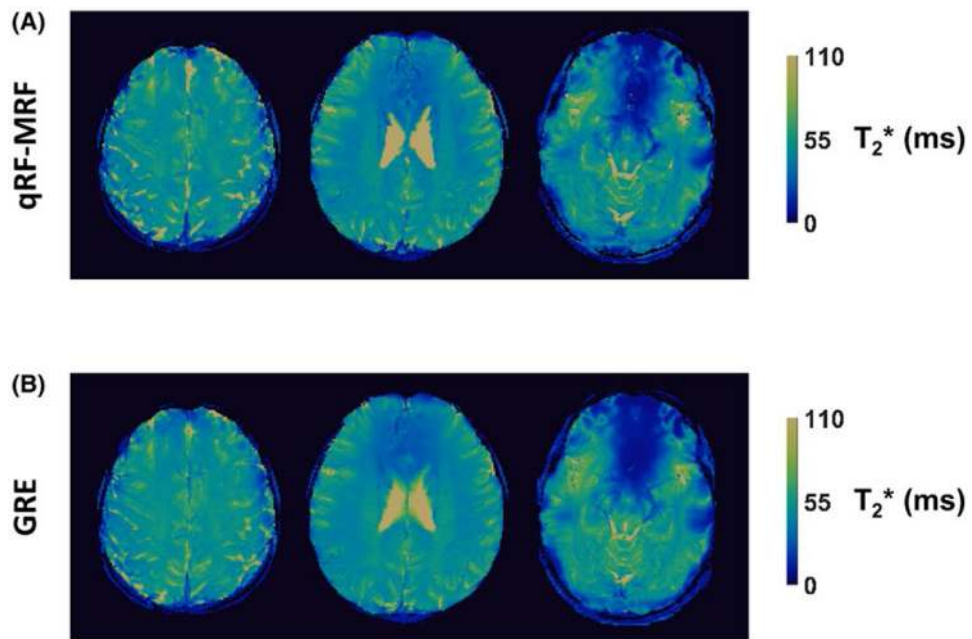
**FIGURE 6.**

Accuracy and reproducibility of qRF-MRF. The values of  $T_1$  (A) and  $T_2$  (B) values were measured within each phantom compartment using qRF-MRF against spin-echo methods. The  $T_2^*$  (C) values were measured within each phantom compartment using qRF-MRF against the multi-echo GRE method. The mean and SD of  $T_1$  (D),  $T_2$  (E), and  $T_2^*$  (F) measured within each compartment are shown with increasing number of time frames used during the dictionary-matching process. G, Coefficient of variation given by the SD divided by the mean, for  $T_2^*$  measurement for both qRF-MRF and GRE methods against the GRE-measured mean  $T_2^*$  value. The 2 compartments with large CV variation caused by poor local field homogeneity were excluded from (F) and plotted using circle markers in (D) and (E). Abbreviations: CCC, concordance correlation coefficient; CV, coefficient of variation

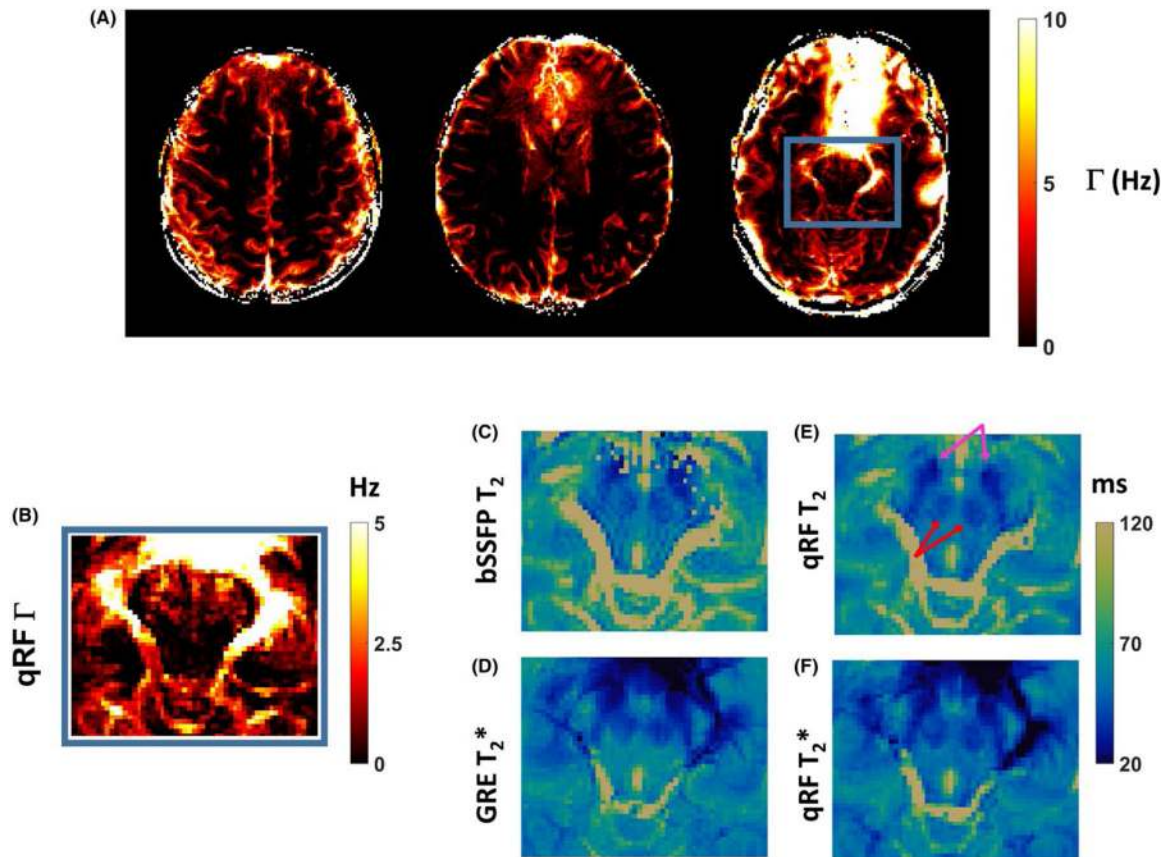


**FIGURE 7.**

Representative in vivo tissue property maps. Maps were acquired using both reference (left) and the qRF-MRF method (right) in healthy volunteers. Reference maps for  $\delta_f$  (A),  $T_1$  (B),  $T_2$  (C), and relative  $M_0$  (D) were generated using the bSSFP-MRF method with the same number of time frames as the qRF-MRF method. The qRF-MRF method simultaneously generated  $\delta_f$  (E),  $T_1$  (F),  $T_2$  (G), and relative  $M_0$  (H) maps are shown using the same scale as references maps. The total acquisition time for each scan was 38 seconds and 35 seconds per slice for each bSSFP-MRF and qRF-MRF scan, respectively



**FIGURE 8.** Representative in vivo T<sub>2</sub>\* maps. The qRF-MRF T<sub>2</sub>\* maps (A), generated simultaneously with other tissue property maps shown in Figure 7, are shown above their corresponding multi-echo GRE-measured reference T<sub>2</sub>\* map (B). The GRE maps were acquired in 51 seconds each



**FIGURE 9.**

A, The  $\Gamma$  maps acquired using the qRF-MRF method from the same experiments shown in Figures 7 and 8. B, Zoomed-in FOV of the  $\Gamma$  map to the midbrain structures. C,D, Corresponding zoomed maps from reference  $T_2$  (C) and  $T_2^*$  (D) maps. E-F, Corresponding zoomed maps from qRF-MRF-acquired  $T_2$  (E) and  $T_2^*$  (F) methods. The same scale and color map used for the  $T_2$  and  $T_2^*$  maps are shown. The lower  $T_2$  value associated with substantia nigra (pink arrows) and red nucleus (red arrows) can be observed across all methods for both  $T_2$  and  $T_2^*$  values

**TABLE 1**Region of interest analysis for in vivo T<sub>1</sub>, T<sub>2</sub>, and T<sub>2</sub>\* values

		qRF-MRF	Reference method <sup>a</sup>	Literature <sup>10,13,45-48</sup>
White matter (ms)	T <sub>1</sub>	988 ± 66	917 ± 60	~690–1100
	T <sub>2</sub>	44 ± 4	42 ± 5	~56–80
	T <sub>2</sub> *	43 ± 4	46 ± 7	~45–48
Gray matter (ms)	T <sub>1</sub>	1395 ± 227	1210 ± 351	~1286–1393
	T <sub>2</sub>	63 ± 10	76 ± 9	~78–117
	T <sub>2</sub> *	51 ± 9	49 ± 10	~42–52
Substantia nigra (ms)	T <sub>1</sub>	1081 ± 69	978 ± 130	1147
	T <sub>2</sub>	34 ± 2	38 ± 7	~42–47
	T <sub>2</sub> *	25 ± 5	26 ± 6	~22–28
Red nucleus (ms)	T <sub>1</sub>	1057 ± 97	958 ± 156	
	T <sub>2</sub>	39 ± 6	42 ± 8	~46–48
	T <sub>2</sub> *	32 ± 6	31 ± 6	~24–31

<sup>a</sup>Measured using bSSFP-MRF for T<sub>1</sub> and T<sub>2</sub> multi-echo GRE for T<sub>2</sub>\*