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Matching NLO QCD computations with PYTHIA using MC@NLO

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ABSTRACT: We present the matching between a next-to-leading order computation in QCD and the PYTHIA parton shower Monte Carlo, according to the MC@NLO formalism. We study the case of initial-state radiation, and consider in particular single vector boson hadroproduction.

KEYWORDS: NLO Computations, Hadronic Colliders, QCD

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1 Introduction

Perturbation theory offers a systematic way to improve theoretical predictions for any given infrared-safe observable. Depending on whether the expansion parameter in the series is α_S , or is α_S times a logarithm or a logarithm squared of some function of the kinematics of the hard process, one obtains a fixed-order result or a resummed result, respectively. Cross sections expanded up to a certain order in α_S and those resummed are relevant to complementary kinematic regions of the phase-space. It is therefore convenient to combine the features of these two expansions, by defining a matched cross section which is equal to the former or to the latter in the appropriate phase-space region.

Fixed-order results are now generally available at the next-to-leading order (NLO), which corresponds to including in the cross section the coefficients of terms of order α_S^b (the leading order or Born level) and of order α_S^{b+1} . Thanks to the recent and rapid progress in the automated treatment of both the real and the virtual contributions to NLO computations, it is realistic to assume that phenomenological results at this accuracy will become available in the next few years for all of the reactions of interest to the LHC physics programme. The situation is much less encouraging for fixed-order cross sections at $\mathcal{O}(\alpha_S^{b+2})$ (or NNLO), where only a handful of results are available, for very small final-state multiplicities.

As far as resummed results are concerned, it is in general understood how to achieve a next-to-leading logarithmic (NLL) accuracy, which is equivalent to including terms proportional to $\alpha_S^n \log^{kn} \mathcal{Q}$ and to $\alpha_S^n \log^{kn-1} \mathcal{Q}$, with $k = 1, 2$ depending on the nature of \mathcal{Q} ; some results are also known to next-to-next-to-leading logarithmic accuracy (NNLL). Unfortunately, resummed computations are in general technically complicated, observable-dependent, and error-prone; although for some observable classes a semi-automated algorithm (CAESAR [1]) is available, the overall situation is far less satisfactory than for

NLO computations. For this reason, a very appealing alternative is that provided by Parton Shower Monte Carlos (PSMCs). Although formally PSMCs are equivalent to a LL-accurate resummation (which may become NLL in some corners of the phase space, for some PSMCs and subject to certain restrictions), in practice they are known to do much better than that, as comparisons with data and with analytically-resummed results clearly show. Furthermore, PSMCs are fully flexible, give one the possibility of including hadronization models in a consistent manner, and are the workhorses of experimental collaborations, thanks to their capabilities of simulating fully-realistic final-state configurations that can undergo detector simulations.

As is well known, the approximations that form the core of PSMCs severely limit their predictive power in those phase-space regions (corresponding to multi-jet configurations) which are of interest for most of new-physics searches at colliders. These limitations can be alleviated by viewing PSMC predictions as resummed results, to be included with the NLO corrections to the relevant production processes into a matched cross section. The definition of a formalism for matching NLO computations and MC simulations has attracted a considerable amount of attention. There are now several proposals, but only two of them, namely MC@NLO [2] or POWHEG [3], have made it to the stage of actually implementing several hadroproduction processes, and of being routinely used by experimental collaborations.

The MC@NLO formalism requires the computation of the cross section predicted by the PSMC at $\mathcal{O}(\alpha_s^{b+1})$. Because of the structure of PSMCs, the non-trivial information of this computation is actually process-independent, and is contained in the definitions of the parton branchings; the process-dependent part is entirely factorized in the Born matrix element. Thus, one essentially has to perform one set of computations (since typically initial- and final-state branchings are treated differently by the Monte Carlo) per PSMC, in order to be able to match an NLO computation with a parton shower simulation according to the MC@NLO approach. So far, these computations have been carried out for the case of HERWIG (see refs. [2, 4, 5]) and, more recently, for HERWIG++ [6]. In this paper, we present the first results relevant to the matching with PYTHIA 6.4. We limit ourselves to considering the case of initial-state branchings, and present some sample results for the Drell-Yan process.

This paper is organized as follows. In section 2 we describe the various steps necessary for an MC@NLO matching with PYTHIA, from the definition of the underlying parton-level NLO cross section to the MC@NLO short-distance cross sections used for the generation of hard-subprocess events, to be showered by PYTHIA. We present sample results in section 3, and we give our conclusions in section 4.

2 MC@NLO

2.1 NLO parton-level cross section

The starting point for the construction of MC@NLO is that of writing the short-distance parton-level cross section according to the subtraction formalism of refs. [7, 8] (which we shall call FKS subtraction henceforth). The default procedure in FKS is that of treating simultaneously (i.e. in one contribution to the partonic cross section) the two initial-state

collinear singularities, due to one given final-state parton being collinear to the initial-state parton coming from the left or from the right. On the other hand, in FKS one can also treat these two singularities independently, by defining two separate contributions to the short-distance cross section, each of which corresponds to one of the initial-state singularities; this procedure is explained in detail in ref. [9]. As we shall discuss in the following, when an NLO computation is matched to PYTHIA according to the MC@NLO formalism, it turns out to be convenient to adopt the latter strategy (at variance with the case of HERWIG, where the simultaneous subtraction suffices).

We shall assign the momenta entering the (real-emission) partonic subprocesses as follows:

$$a(p_1) + b(p_2) \longrightarrow V(k_1) + c(k_2), \tag{2.1}$$

with V representing a W or a Z boson, and a , b , and c being QCD partons; Born-like processes are simply obtained from eq. (2.1) by removing $c(k_2)$ from the r.h.s.. Only soft and initial-state collinear singularities are present in the processes of eq. (2.1). Hence, the \mathcal{S} functions required for a separate treatment of the collinear singularities are two and shall be denoted by

$$\mathcal{S}_+, \quad \mathcal{S}_-, \tag{2.2}$$

with the following properties:

$$\mathcal{S}_+ + \mathcal{S}_- = 1, \tag{2.3}$$

$$\lim_{\vec{k}_2 \parallel \vec{p}_1} \mathcal{S}_+ = 1, \tag{2.4}$$

$$\lim_{\vec{k}_2 \parallel \vec{p}_2} \mathcal{S}_- = 1, \tag{2.5}$$

$$\lim_{k_2^0 \rightarrow 0} \mathcal{S}_\pm \neq 0. \tag{2.6}$$

The expectation value for any observable O will then be written as

$$\langle O \rangle = \langle O \rangle_+ + \langle O \rangle_-, \tag{2.7}$$

where (see eqs. (4.14)–(4.16) of ref. [2])

$$\begin{aligned} \langle O \rangle_\pm = \sum_{ab} \int dx_1 dx_2 d\phi_2 \left[O(\mathbf{2}) \mathcal{S}_\pm(\mathbf{2}) \frac{d\Sigma_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ev}} + O(\mathbf{1}) \mathcal{S}_\pm(\mathbf{1}) \frac{1}{\mathcal{I}_1} \left(\frac{d\Sigma_{ab}^{(b)}}{d\phi_1} + \frac{d\Sigma_{ab}^{(sv)}}{d\phi_1} \right) \right. \\ \left. + O(\tilde{\mathbf{1}}) \frac{1}{\mathcal{I}_1} \frac{d\Sigma_{ab}^{(c\pm)}}{d\phi_1 dx} \Big|_{\text{ev}} - O(\mathbf{1}) \frac{1}{\mathcal{I}_1} \frac{d\Sigma_{ab}^{(c\pm)}}{d\phi_1 dx} \Big|_{\text{ct}} \right. \\ \left. - \{O(\mathbf{1}) \mathcal{S}_\pm(\mathbf{1}), O(\tilde{\mathbf{1}})\} \frac{d\Sigma_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ct}} \right]. \tag{2.8} \end{aligned}$$

As can be seen in ref. [2], the Σ terms in equation above are defined as the partonic short-distance cross sections, times the luminosity factors.

In writing eq. (2.8), we have split (using the \mathcal{S} functions) the Born ($\Sigma_{ab}^{(b)}$) and soft-virtual ($\Sigma_{ab}^{(sv)}$) contributions into two terms, and have associated them with the corresponding real-emission contributions (see refs. [5, 9]). We have also used the collinear limits of eqs. (2.4) and (2.5), that imply that the \mathcal{S} functions associated with the collinear counterterms are trivial. Finally, note that the collinear remainders $\Sigma_{ab}^{(c\pm)}$ need not be multiplied by the \mathcal{S} functions.

Equation (2.8) must be further manipulated in order to use it in MC@NLO; in particular, one has to apply the so-called event projection which allows one to define a unique kinematic configuration associated with all counterevents (for a given real-emission configuration) – see section A.4 of ref. [2]. As discussed in that paper, although event projection is largely arbitrary, in the context of MC@NLO it turns out to be convenient to derive it from the behaviour of the Monte Carlo one interfaces to. We shall therefore discuss in the next subsection the behaviour of PYTHIA relevant to this issue.

2.2 Event projection with PYTHIA

The way in which PYTHIA deals with the simulation of V production is the following [10, 11]. First, the hard process is generated. This implies the generation of the two Bjorken x 's entering such a process, which we shall denote by ζ_1 and ζ_2 for the parton coming from the left and from the right respectively. The partonic c.m. energy squared is

$$s_0 = \zeta_1 \zeta_2 S, \tag{2.9}$$

with S the collider energy squared. In the case of single- V production, $s_0 = m_V^2$, with m_V the mass of V (or its virtuality if lepton pair production is considered), but eq. (2.9) is obviously valid regardless of the production process. PYTHIA then begins the showers. Choosing on statistical basis which leg emits “first” (such an emission is the only one that matters as far as MC@NLO is concerned), the shower variables are related to the momenta given in eq. (2.1) as follows:

$$z = \frac{s_0}{(p_1 + p_2)^2}, \tag{2.10}$$

$$t_i = (p_i - k_2)^2, \tag{2.11}$$

with $i = 1, 2$ for the emissions from the parton coming from the left and from the right respectively. The branching generated with eqs. (2.10) and (2.11) is such that the Bjorken x 's associated with the initial-state partons of eq. (2.1) (which we shall denote by z_1 and z_2) are

$$z_1 = \zeta_1/z, \quad z_2 = \zeta_2 \tag{2.12}$$

for an emission from leg 1, and

$$z_1 = \zeta_1, \quad z_2 = \zeta_2/z \tag{2.13}$$

for an emission from leg 2. In the branching, the c.m. energy of the Born-level subprocess is conserved (which, in the present case, is equivalent to the requirement that the virtuality of V be a constant), and thus

$$s = (p_1 + p_2)^2 = z_1 z_2 S = s_0/z. \tag{2.14}$$

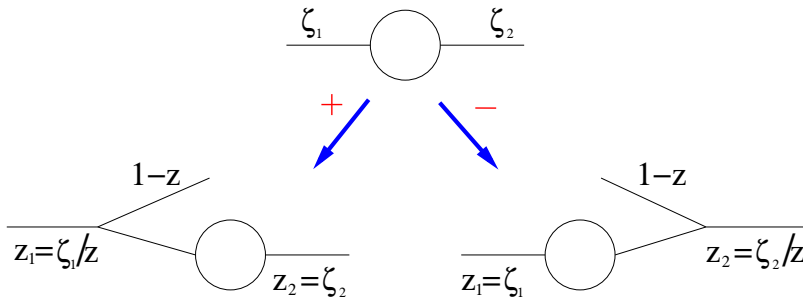


Figure 1. Assignments of momentum fractions in the case of initial-state branchings as done in PYTHIA. Branchings from legs 1 and 2 are denoted in MC@NLO by + and – respectively. The blob represents the final state at the Born level.

An easy way to achieve this is that of imposing that the Bjorken x ’s of the Born-level subprocesses, ζ_i , be separately conserved.

As shown in ref. [2], the event-projection procedure can be formally determined by constructing two “observables” that are conserved in the branching process. According to what has been discussed above, a possible choice is:

$$O_1 = \zeta_1 \zeta_2 S, \quad (2.15)$$

$$O_2 = \frac{1}{2} \log \frac{\zeta_1}{\zeta_2}. \quad (2.16)$$

It is worth noting that while eq. (2.15) is the same as in HERWIG, eq. (2.16) does not coincide with either of the HERWIG choices considered in ref. [2]; the implication of this fact is that we obtain two different event projections, depending on whether it is leg 1 or 2 that emits. We stress that eqs. (2.15) and (2.16), and the resulting manipulations we are now going to describe, do not depend on the nature of the Born-level final state (a V boson rather than — say — a three-jet configuration), owing to the fact that PYTHIA adopts the so-called s -approach [10] when doing initial-state branchings for all hadroproduction processes. In the context of the s -approach, the invariant mass ($\sqrt{s_0}$) of the final-state system at the Born level is kept constant during the branching. This allows one to formally replace V with the set of final-state particles at the Born level, and k_1 with the sum of their four momenta, which does not entail any changes to eqs. (2.9)–(2.14), from which we ultimately derive eqs. (2.15) and (2.16). The procedure described here is thus fully general, and is not restricted to V -boson production. We recall that event projection is a way to re-write the soft and collinear counterterms in a pure-NLO computation, so as all counterterms associated with a given \mathcal{S} contribution at the real-emission level (in the present case, $\mathcal{S}_+ d\Sigma^{(f)}$ or $\mathcal{S}_- d\Sigma^{(f)}$) have the same kinematics. In order to achieve this, it turns out to be convenient to define the counterterm kinematics starting from a fixed real-emission kinematics. This situation is depicted in figure 2 for soft counterterms (the case of collinear counterterms is essentially identical, the only differences being in the assignments of the momentum fractions of the incoming partons, which we shall specify in what follows). Since the event projections we define here are ultimately motivated by the

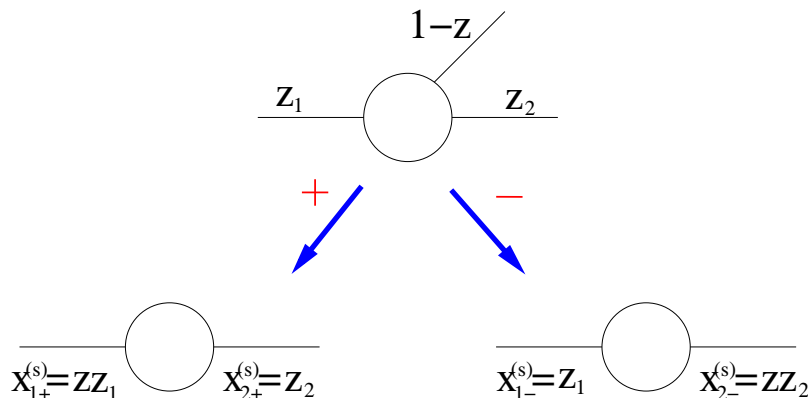


Figure 2. Assignments of momentum fractions according to the event-projection procedure, for the soft configurations. See the text for details.

branching strategy of PYTHIA, the procedure of figure 2 is by construction the inverse of that depicted in figure 1. We shall return to this point in section 2.4.

In order to actually obtain event projections, we use the master equations (A.36) and (A.37) of ref. [2]. For an emission from leg 1, these equations read in our case

$$O_1(\mathbf{2}(z_1, z_2, \phi_2)) = O_1(\mathbf{1}_s(x_{1+}^{(s)}, x_{2+}^{(s)}, \phi_2^{(s)})), \quad (2.17)$$

$$O_2(\mathbf{2}(z_1, z_2, \phi_2)) = O_2(\mathbf{1}_s(x_{1+}^{(s)}, x_{2+}^{(s)}, \phi_2^{(s)})), \quad (2.18)$$

and their analogues for the collinear case (where one formally replaces s with $c+$ in the r.h.s. of eqs. (2.17) and (2.18)). Note that, having treated separately the two collinear singularities in the NLO cross section, the case $c-$ need not be considered when studying branching from leg 1). We find:

$$x_{1+}^{(s)} = z z_1, \quad x_{2+}^{(s)} = z_2, \quad (2.19)$$

$$x_{1+}^{(c+)} = x_{1+}^{(s)}/z, \quad x_{2+}^{(c+)} = x_{2+}^{(s)}. \quad (2.20)$$

For an emission from leg 2, we find instead

$$x_{1-}^{(s)} = z_1, \quad x_{2-}^{(s)} = z z_2, \quad (2.21)$$

$$x_{1-}^{(c-)} = x_{1-}^{(s)}, \quad x_{2-}^{(c-)} = x_{2-}^{(s)}/z. \quad (2.22)$$

At this point, following what was done in section 4.4 of ref. [2], one uses eqs. (2.19) and (2.20) to perform the event projection transformation of $\langle O \rangle_+$, and eqs. (2.21) and (2.22) to deal with $\langle O \rangle_-$. Once event projection has been achieved, the MC@NLO short distance cross section can be defined by including the MC subtraction terms. We shall do this in the next subsection.

2.3 MC subtraction terms

At the NLO in α_S , the cross section resulting from PYTHIA is

$$d\sigma\Big|_{\text{MC}} = d\sigma^{(+)}\Big|_{\text{MC}} + d\sigma^{(-)}\Big|_{\text{MC}}, \quad (2.23)$$

where the two terms on the r.h.s. account for emissions from leg 1 and 2 respectively. They read:

$$d\sigma^{(+)}\Big|_{\text{MC}} = \sum_{abc} d\zeta_1 d\zeta_2 \frac{\alpha_S}{2\pi} d\sigma_{ab}^{(b)}(\zeta_1 P_1, \zeta_2 P_2) \frac{dt_1}{t_1} \frac{dz}{z} P_{ac}^{(0)}(z) f_c^{(H_1)}(\zeta_1/z) f_b^{(H_2)}(\zeta_2), \quad (2.24)$$

$$d\sigma^{(-)}\Big|_{\text{MC}} = \sum_{abc} d\zeta_1 d\zeta_2 \frac{\alpha_S}{2\pi} d\sigma_{ab}^{(b)}(\zeta_1 P_1, \zeta_2 P_2) \frac{dt_2}{t_2} \frac{dz}{z} P_{bc}^{(0)}(z) f_a^{(H_1)}(\zeta_1) f_c^{(H_2)}(\zeta_2/z). \quad (2.25)$$

Following what was done in section A.5 of ref. [2], we can manipulate the equations above to render them suitable for an integration together with the NLO parton-level cross section. First of all, one notes that the following identifications are valid owing to the construction of event projections:

$$\zeta_1 \equiv x_{1+}^{(s)}, \quad \zeta_2 \equiv x_{2+}^{(s)}, \quad (2.26)$$

in eq. (2.24), and

$$\zeta_1 \equiv x_{1-}^{(s)}, \quad \zeta_2 \equiv x_{2-}^{(s)}, \quad (2.27)$$

in eq. (2.25). We can therefore perform a change of integration variables:

$$d\sigma^{(\pm)}\Big|_{\text{MC}} = \sum_{ab} dz_1 dz_2 d\bar{\Sigma}_{ab}^{(\pm)}\Big|_{\text{MC}}, \quad (2.28)$$

with

$$d\bar{\Sigma}_{ab}^{(+)}\Big|_{\text{MC}} = \frac{1}{z} \frac{\partial(x_{1+}^{(s)}, x_{2+}^{(s)})}{\partial(z_1, z_2)} f_a^{(H_1)}(x_{1+}^{(s)}/z) f_b^{(H_2)}(x_{2+}^{(s)}) d\sigma_{ab}^{(+)}\Big|_{\text{MC}} \quad (2.29)$$

$$d\bar{\Sigma}_{ab}^{(-)}\Big|_{\text{MC}} = \frac{1}{z} \frac{\partial(x_{1-}^{(s)}, x_{2-}^{(s)})}{\partial(z_1, z_2)} f_a^{(H_1)}(x_{1-}^{(s)}) f_b^{(H_2)}(x_{2-}^{(s)}/z) d\sigma_{ab}^{(-)}\Big|_{\text{MC}} \quad (2.30)$$

and

$$\frac{d\sigma_{ab}^{(+)}\Big|_{\text{MC}}}{d\phi_2} = \sum_c \frac{8\pi\alpha_S}{m_V^2 \hat{t}_1} P_{ca}^{(0)}(z) \mathcal{M}_{cb}^{(b)}(x_{1+}^{(s)} P_1, x_{2+}^{(s)} P_2) \Theta_+, \quad (2.31)$$

$$\frac{d\sigma_{ab}^{(-)}\Big|_{\text{MC}}}{d\phi_2} = \sum_c \frac{8\pi\alpha_S}{m_V^2 \hat{t}_2} P_{cb}^{(0)}(z) \mathcal{M}_{ac}^{(b)}(x_{1-}^{(s)} P_1, x_{2-}^{(s)} P_2) \Theta_-. \quad (2.32)$$

Here, we have introduced the rescaled virtualities

$$\hat{t}_i = -t_i/m_V^2. \quad (2.33)$$

Furthermore, we have explicitly included the factors Θ_{\pm} , which are related to the choice of the maximum virtuality allowed during shower evolution. We have e.g.

$$|t_i| \leq m_V^2 \quad \Longrightarrow \quad \Theta_{\pm} = \Theta\left(y - \frac{1-3x}{1-x}\right), \quad (2.34)$$

with y being the relevant angular variable associated with the FKS parton in the FKS subtraction (here the cosine of the angle between \vec{k}_2 and \vec{p}_i for emissions from leg i), and $1-x$ the (normalized) energy of the FKS parton. In the case of PYTHIA, at variance with HERWIG, $x \equiv z$.

2.4 MC@NLO short-distance cross sections

At this point, we have all the ingredients needed to generate hard-subprocess events according to the MC@NLO formalism, which will be subsequently showered by PYTHIA. Recalling that we denote by $\overline{\Sigma}^{(\alpha)}$ the contributions $\Sigma^{(\alpha)}$ to the NLO parton-level cross sections after event projection, event generation will be performed following the procedure outlined in section 4.5 of ref. [2] (see also section 3 of ref. [5]), using the following integrals:

$$I_{\mathbb{H}}^{(\pm)} = \sum_{ab} \int dz_1 dz_2 d\phi_2 \left(\mathcal{S}_{\pm} \frac{d\overline{\Sigma}_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ev}} - \frac{d\overline{\Sigma}_{ab}^{(\pm)}}{d\phi_2} \Big|_{\text{MC}} \right), \quad (2.35)$$

$$I_{\mathbb{S}}^{(\pm)} = \sum_{ab} \int dz_1 dz_2 d\phi_2 \left[-\mathcal{S}_{\pm} \frac{d\overline{\Sigma}_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ct}} + \frac{d\overline{\Sigma}_{ab}^{(\pm)}}{d\phi_2} \Big|_{\text{MC}} + \frac{\mathcal{S}_{\pm}}{\mathcal{I}_1} \left(\frac{d\overline{\Sigma}_{ab}^{(b)}}{d\phi_1} + \frac{d\overline{\Sigma}_{ab}^{(sv)}}{d\phi_1} \right) + \frac{1}{\mathcal{I}_1} \left(\frac{d\overline{\Sigma}_{ab}^{(c\pm)}}{d\phi_1 dx} \Big|_{\text{ev}} - \frac{d\overline{\Sigma}_{ab}^{(c\pm)}}{d\phi_1 dx} \Big|_{\text{ct}} \right) \right]. \quad (2.36)$$

We remind the reader that all integrals defined in these equations are separately finite, and that

$$\sigma_{\text{tot}} = I_{\mathbb{S}}^{(+)} + I_{\mathbb{H}}^{(+)} + I_{\mathbb{S}}^{(-)} + I_{\mathbb{H}}^{(-)} \quad (2.37)$$

is an exact equation (with σ_{tot} the fully-inclusive NLO rate).

Although eqs. (2.35) and (2.36) solve the problem of the generation of hard-subprocess events, a further simplification is possible. We start by considering the integrals $I_{\mathbb{H}}^{(\pm)}$, that are used to generate \mathbb{H} events. These two integrals have to be computed separately. However, one observes that, for a given choice of (z_1, z_2, ϕ_2) , the kinematics associated with these two contributions are actually identical, and the integrals can therefore be computed together. This is equivalent to using the following integral for the generation of \mathbb{H} events:

$$I_{\mathbb{H}} \equiv I_{\mathbb{H}}^{(+)} + I_{\mathbb{H}}^{(-)} = \sum_{ab} \int dz_1 dz_2 d\phi_2 \left(\frac{d\overline{\Sigma}_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ev}} - \sum_{L=\pm} \frac{d\overline{\Sigma}_{ab}^{(L)}}{d\phi_2} \Big|_{\text{MC}} \right). \quad (2.38)$$

The first term in the integrand has been simplified thanks to eq. (2.3). For the computation of the second term in the integrand we stress that, as eq. (2.38) explicitly indicates, z_i are the integration variables. Therefore, when we evaluate eqs. (2.31) and (2.32), the variables $x_{i\pm}^{(s)}$ have to be computed according to eqs. (2.19) and (2.21). From the physical viewpoint, this implies that the two Born matrix elements appearing implicitly in $\overline{\Sigma}_{ab}^{(\pm)}$ are evaluated in two different kinematics configurations, that eventually result after the first branching in the same real-emission kinematics (z_1, z_2, ϕ_2) . This situation is precisely the one depicted in figure 2.

A simplification analogous to that of eq. (2.38) is also possible in the case of \mathbb{S} events, although the argument is slightly more involved. If one fixes (z_1, z_2, ϕ_2) (i.e., the real-emission kinematics), the kinematic configurations associated with $I_{\mathbb{S}}^{(+)}$ and $I_{\mathbb{S}}^{(-)}$ in eq. (2.36) are different, owing to the fact that the two integrals are computed using different event projections. Formally, one can introduce two mappings, $\mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(+)}$ and $\mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(-)}$, representing these

event projections; for a given real-emission kinematic configuration $\mathbf{2}$, the two Born-like configurations associated with $I_{\mathbb{S}}^{(+)}$ and $I_{\mathbb{S}}^{(-)}$ can be denoted by

$$\mathbf{1}^+ = \mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(+)} \mathbf{2}, \quad \mathbf{1}^- = \mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(-)} \mathbf{2} \quad (2.39)$$

respectively; $\mathbf{1}^+$ and $\mathbf{1}^-$ are the hard configurations to be showered by PYTHIA. The $\mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(\pm)}$ mappings are pictorially represented in figure 2 by the two thick arrows, with $\mathbf{2}$, $\mathbf{1}^+$, and $\mathbf{1}^-$ the configurations depicted in the upper part, lower left corner, and lower right corner of that figure respectively. On the other hand, one can fix a Born-like configuration $\mathbf{1}$ and, using the inverse of the maps $\mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(\pm)}$ (which we denote by $\mathcal{P}_{\mathbb{S} \rightarrow \mathbb{H}}^{(\pm)}$), work out the real-emission configurations to be used in the computation of the integrand of $I_{\mathbb{S}}^{(\pm)}$:

$$\mathbf{2}^+ = \mathcal{P}_{\mathbb{S} \rightarrow \mathbb{H}}^{(+)} \mathbf{1}, \quad \mathbf{2}^- = \mathcal{P}_{\mathbb{S} \rightarrow \mathbb{H}}^{(-)} \mathbf{1}. \quad (2.40)$$

As we have already stressed, although there is an ample freedom in choosing $\mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(\pm)}$, it is best to adopt a form motivated by what the PSMC does when branching. In practice, it is therefore convenient first to obtain $\mathcal{P}_{\mathbb{S} \rightarrow \mathbb{H}}^{(\pm)}$ from the PSMC, and then (by inverting them) $\mathcal{P}_{\mathbb{H} \rightarrow \mathbb{S}}^{(\pm)}$. In the case of PYTHIA, $\mathcal{P}_{\mathbb{S} \rightarrow \mathbb{H}}^{(\pm)}$ amount to performing a boost of the Born-level four momenta in the transverse direction, to balance the transverse momentum of the parton produced in the branching ($c(k_2)$ in eq. (2.1)), followed by a boost in the longitudinal direction, to e.g. the lab frame. The information on the latter is equivalent to the assignments of the momentum fractions of the incoming particles. The prescription for the transverse boost given above is obviously trivial in the case of V production (since $k_{1T} = -k_{2T}$), but can be applied to final states with arbitrary multiplicity. Thus, what done here is also valid for final states more complicated than single V .

The two procedures related to eq. (2.39) and (2.40) are equivalent, since the integrals are performed over the whole phase space (possibly subject to kinematic restrictions, which are however identical in the two cases). Equation (2.40) corresponds to the situation depicted in figure 1, except for the seemingly different assignments of the momentum fractions of the incoming particles. These differences are however immaterial, since such fractions are simply integration variables which can be manipulated and renamed at will. We shall now proceed to perform such manipulations, starting from a change of variables in eq. (2.36)

$$(z_1, z_2, \phi_2) \longrightarrow (x_{1\pm}^{(s)}, x_{2\pm}^{(s)}, \phi_2^{\pm}). \quad (2.41)$$

Furthermore, consistently with eq. (2.40), the integrands have to be computed with the suitable kinematic configurations, $\mathbf{2}^+$ or $\mathbf{2}^-$. We can take these two operations into account by the formal replacements

$$\overline{\Sigma}_{ab}^{(\alpha)}(\mathbf{2}(z_i)) \longrightarrow \widehat{\Sigma}_{ab}^{(\alpha)}(\mathbf{2}^{\pm}(x_{j\pm}^{(s)})) = \frac{\partial(z_1, z_2)}{\partial(x_{1\pm}^{(s)}, x_{2\pm}^{(s)})} \overline{\Sigma}_{ab}^{(\alpha)}(\mathbf{2}(z_i(x_{j\pm}^{(s)}))). \quad (2.42)$$

It is easy to realize that, in the case of the Born, soft-virtual, and soft counterterms contributions, we have by construction

$$\widehat{\Sigma}_{ab}^{(\alpha)} = \Sigma_{ab}^{(\alpha)}, \quad (2.43)$$

since for these terms the jacobian appearing in eq. (2.42) exactly compensates the one in the definition of the $\overline{\Sigma}_{ab}^{(\alpha)}$ terms, see eq. (4.18) of [2]. In general, this is not true for contributions with a purely collinear structure (such as the collinear counterterms to the real-emission matrix elements). Equations (2.41), (2.42), and (2.43) allow us to rewrite

$$I_{\mathbb{S}}^{(\pm)} = \sum_{ab} \int dx_{1\pm}^{(s)} dx_{2\pm}^{(s)} d\phi_2^{\pm} \left[-\mathcal{S}_{\pm} \frac{d\widehat{\Sigma}_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ct}} + \frac{d\widehat{\Sigma}_{ab}^{(\pm)}}{d\phi_2} \Big|_{\text{MC}} + \frac{\mathcal{S}_{\pm}}{\mathcal{I}_1} \left(\frac{d\Sigma_{ab}^{(b)}}{d\phi_1} + \frac{d\Sigma_{ab}^{(sv)}}{d\phi_1} \right) + \frac{1}{\mathcal{I}_1} \left(\frac{d\widehat{\Sigma}_{ab}^{(c\pm)}}{d\phi_1 dx} \Big|_{\text{ev}} - \frac{d\widehat{\Sigma}_{ab}^{(c\pm)}}{d\phi_1 dx} \Big|_{\text{ct}} \right) \right]. \quad (2.44)$$

At this point, the two integrals in eq. (2.44) correspond by construction to the same Born-like kinematic configuration (to be showered by PYTHIA), and can therefore be integrated together. It is thus convenient to *rename* the integration variables

$$(x_{1\pm}^{(s)}, x_{2\pm}^{(s)}, \phi_2^{\pm}) \longrightarrow (\zeta_1, \zeta_2, \phi_2), \quad (2.45)$$

and use

$$I_{\mathbb{S}} \equiv I_{\mathbb{S}}^{(+)} + I_{\mathbb{S}}^{(-)} \quad (2.46)$$

for the generation of \mathbb{S} events. One observes that in the integrand of eq. (2.46) there will be a term

$$\sum_{L=\pm} \frac{\mathcal{S}_L}{\mathcal{I}_1} \left(\frac{d\Sigma_{ab}^{(b)}}{d\phi_1} + \frac{d\Sigma_{ab}^{(sv)}}{d\phi_1} \right) = \frac{1}{\mathcal{I}_1} \left(\frac{d\Sigma_{ab}^{(b)}}{d\phi_1} + \frac{d\Sigma_{ab}^{(sv)}}{d\phi_1} \right), \quad (2.47)$$

where we have made use of eq. (2.3). The same kind of simplification will occur in the sum of the two soft counterterms. As far as the collinear counterterms are concerned, we stress that the \mathcal{S}_{\pm} terms that multiply them are equal to one (by construction of the \mathcal{S} functions — see eqs. (2.4) and (2.5)). We arrive therefore at the following form:

$$I_{\mathbb{S}} = \sum_{ab} \int d\zeta_1 d\zeta_2 d\phi_2 \left[-\frac{d\widehat{\Sigma}_{ab}^{(f)}}{d\phi_2} \Big|_{\text{ct}} + \sum_{L=\pm} \frac{d\widehat{\Sigma}_{ab}^{(L)}}{d\phi_2} \Big|_{\text{MC}} + \frac{1}{\mathcal{I}_1} \left(\frac{d\Sigma_{ab}^{(b)}}{d\phi_1} + \frac{d\Sigma_{ab}^{(sv)}}{d\phi_1} \right) + \frac{1}{\mathcal{I}_1} \sum_{L=\pm} \left(\frac{d\widehat{\Sigma}_{ab}^{(cL)}}{d\phi_1 dx} \Big|_{\text{ev}} - \frac{d\widehat{\Sigma}_{ab}^{(cL)}}{d\phi_1 dx} \Big|_{\text{ct}} \right) \right]. \quad (2.48)$$

Equations (2.38) and (2.48) are our final expressions, used for the generation of \mathbb{H} and \mathbb{S} events respectively. The net result of the various manipulations carried out in this section is that it is still possible to treat simultaneously the two initial-state collinear singularities, as was the case when matching with HERWIG. We point out that the fact that eqs. (2.38) and (2.48) do not depend upon the \mathcal{S} functions is not a property of V -boson production, but applies as well to all processes whose Born-level final-state particles are all colour singlets.¹ In fact, for this independence of \mathcal{S} functions to occur, we only need eq. (2.3) to hold, which is true in the cases just mentioned (see ref. [9] for further details on the construction of \mathcal{S}

¹It is also possible, but not mandatory, to treat in this way processes in which *all* strongly-interacting final-state particles are massive, as e.g. in $t\bar{t}$ production. See ref. [4] for an explicit example.

functions). Clearly, in order to make use of eq. (2.3), \mathcal{S}_+ and \mathcal{S}_- need be computed for the same kinematic configuration. This is in fact what happens, in spite of the fact that in the intermediate steps of the event-projection procedure we had to treat separately the $+$ and $-$ contributions. For \mathbb{H} events this is trivially true by construction — both $I_{\mathbb{H}}^{(\pm)}$ in eq. (2.35) are associated with the kinematic configuration denoted by $\mathbf{2}$ in eq. (2.39) (i.e. the upper part of figure 2). On the other hand, the short-distance cross sections for \mathbb{S} events we started from, eq. (2.36), are associated with two different kinematic configurations, denoted by $\mathbf{1}^\pm$ in eq. (2.39) (i.e. the lower part of figure 2). Thanks to the procedure described above, we have manipulated eq. (2.36) precisely to be able to associate the two \pm contributions with the same kinematic configuration, denoted by $\mathbf{1}$ in eq. (2.40) (i.e. the upper part of figure 1). Owing to the properties of event projections that we have discussed above, the whole procedure can obviously be carried out for any final-state multiplicity, with $\mathbf{2}$ and $\mathbf{1}$ formally replaced by the real-emission and Born-level configurations respectively. Finally, we stress that the manipulations performed here will also be valid in the case of strongly-interacting particles in the final state. The only difference is that, in such a case, eq. (2.3) will not hold any longer, and therefore the quantity $\mathcal{S}_+ + \mathcal{S}_-$ will appear in eqs. (2.38) and (2.48) as a factor multiplying the real-emission, soft counterterms, soft-virtual, and Born contributions (on the other hand, the purely collinear terms will be unchanged, owing to the fact that eqs. (2.4) and (2.5) hold regardless of the nature of the final state). Clearly, the contributions due to branchings of Born-level final-state strongly-interacting particles will be given by short-distance cross sections analogous to those of eqs. (2.38) and (2.48) (see e.g. section 3 of ref. [5]). The computation of such contributions is beyond the scope of the present work, and we postpone it to a future publication.

We conclude this section by stressing that, due to the form of the shower variables used by PYTHIA, the soft limit of the sum of the MC subtraction terms coincides with that of the real-emission matrix elements, which was not the case for HERWIG. This implies that here we can set $\mathcal{G} \equiv 1$, where \mathcal{G} is the function introduced in section A.5 of ref. [2] — we refer the reader to that paper for a discussion on this issue.

3 Results

In this section, we present sample results relevant to W^+ production in pp collisions at $\sqrt{S} = 14$ TeV. Our aim is not that of performing a phenomenological study, but rather that of presenting a few control plots that show that the matching of the NLO results for single vector boson production with PYTHIA according to the MC@NLO formalism works as we expect. This is non trivial, given the differences between HERWIG and PYTHIA, which in turn result in different short-distance MC@NLO cross sections, as discussed previously. We set $m_W = 80.4$ GeV, $\Gamma_W = 2.14$ GeV, and use CTEQ6.6 [12] PDFs. Our default scale choices are $\mu_F = \mu_R = m_T$, where m_T is the transverse mass of the W . When reconstructing jets, we adopt the k_T -jet-finding algorithm of ref. [13], with $Y_{\text{cut}} = (10 \text{ GeV})^2$.

In each of the plots we present in figures 3–5, we display three histograms. The solid (black) histograms are the results of MC@NLO with PYTHIA (which we shall call MC@NLO/PY) i.e. what has been computed in this paper. The dotted (red) histograms

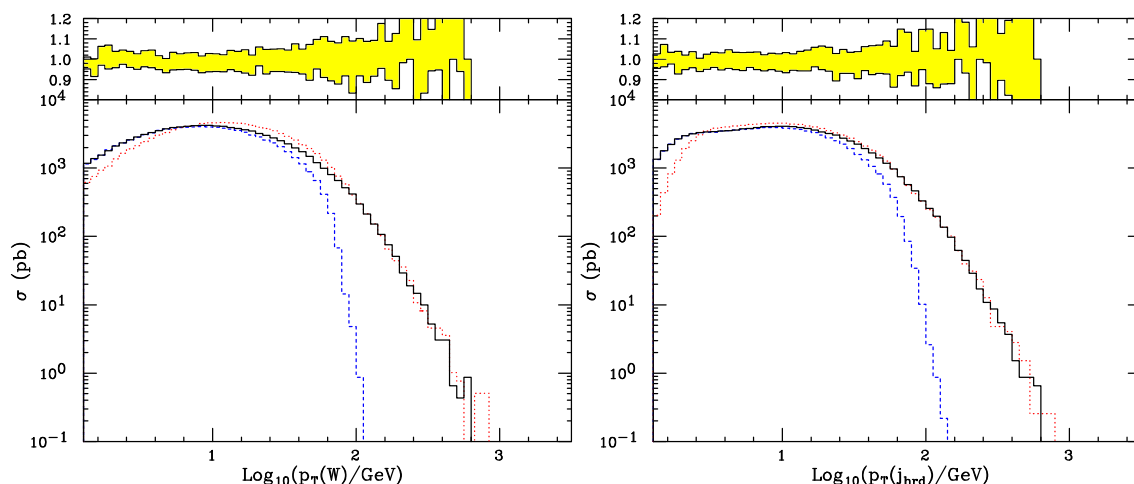


Figure 3. Solid (black): MC@NLO/PY. Dotted (red): MC@NLO/HW. Dashed (blue): PYTHIA standalone (rescaled), without matrix element corrections. Left pane: p_T of the W boson. Right pane: p_T of the hardest jet of the event. The insets show the fractional scale dependence of MC@NLO/PY, computed as described in the text.

are the results of MC@NLO with HERWIG (which we shall call MC@NLO/HW). Finally, the dashed (blue) histograms are the results obtained with PYTHIA standalone. When using PYTHIA for showering hard events, we set $MSTP(81)=0$ and $MSTP(91)=0$, which corresponds to switching off multiple interactions and primordial k_T respectively. We switch off matrix element corrections by setting $MSTP(68)=0$, which also forces the maximum virtuality in the shower to be equal to the vector boson mass, when standalone generation is performed. On the other hand, hard subprocess events generated by MC@NLO/PY are given to PYTHIA in the standard Les Houches format [14]; we set $PARP(67)=1$ and $SCALUP=m_W$ to have the same maximum scale in the shower as in the standalone generation. In order to facilitate the visual comparisons between MC@NLO/PY and PYTHIA, the results of the latter are rescaled (by different factors, depending on the observables considered). As has already been discussed at length in the literature, we expect MC@NLO to be identical in shape to the PSMC results in the regions of the phase space dominated by those large logarithms the PSMC is able to resum; this is the motivation for comparing MC@NLO/PY with PYTHIA standalone. Also, we expect MC@NLO to coincide, in shape and normalization, with the NLO results in the regions where hard emissions are dominant. Given that it has already been shown in the past that this is the case for MC@NLO/HW, here we compare MC@NLO/PY directly with MC@NLO/HW, rather than with the pure NLO results, since this will also give us the opportunity to observe the different behaviours of the two underlying PSMCs in the soft/collinear regions. As far as negative weights are concerned, for W production at the LHC their fraction with MC@NLO/PY is about 0.6%, while in the case of MC@NLO/HW is about 8%. Since the phase-space parametrizations used in the two codes are identical, this large difference is essentially due to the different choices of shower variables made by the two PSMCs.

In figure 3 we consider the transverse momentum distributions of the W^+ boson (left

pane), and of the hardest jet of the event (right pane). These distributions are interesting since in the large- p_T region they are dominated by hard emissions, whereas in the small- p_T one there are logarithmically-enhanced terms that need be resummed (the pure NLO results diverge there). The comparisons among the three results for the two distributions follow the same pattern, as we expect. At small p_T 's, the shapes of MC@NLO/PY and of PYTHIA are identical. To show this clearly, the latter results have been rescaled so as their first bins coincide with those resulting from MC@NLO/PY. On the other hand, the MC@NLO/PY and MC@NLO/HW results are quite different in this p_T region, owing to the different treatment of soft and collinear emissions by the two PSMCs. It is known that PYTHIA tends to give softer spectra than HERWIG, which is therefore what we expect to and do find with MC@NLO/PY and MC@NLO/HW. At large p_T 's, MC@NLO/PY coincides with MC@NLO/HW – both in shape and in absolute normalization, which is again what we expect.

In figure 3 we also show the scale dependence of MC@NLO/PY, determined according to the following procedure. The renormalization-scale variations are defined as the differences between the results obtained with $(\mu_R, \mu_F) = (m_T, m_T)$ (i.e. the default), and those obtained with $(\mu_R, \mu_F) = (fm_T, m_T)$, where $f = 1/2$ and $f = 2$; these differences are computed bin-by-bin for all observables studied. Likewise, for the factorization-scale variations one considers $(\mu_R, \mu_F) = (m_T, fm_T)$. The renormalization- and factorization-scale variations of like sign are then summed in quadrature, and the results are then summed to (for positive variations) or subtracted from (for negative variations) the default cross section. The ratios of the two predictions obtained in this way over the default cross section are displayed in the insets of figure 3 as the upper and lower bounds of the shaded areas, for the two observables considered there. In spite of the lack of statistics in the high- p_T tails² the trend is clear: the fractional scale dependence grows from about $\pm 5\%$ at low p_T 's to about $\pm 10\%$ at large p_T 's. This has to be compared with the pure-NLO result (not shown here) that features a decrease in the scale dependence, from $\pm 15\%$ at low p_T 's to $\pm 10\%$ at large p_T 's; this behaviour results from a dependence on μ_F almost constant w.r.t. p_T , and a dependence on μ_R decreasing with p_T (due to the running of α_S). The scale dependences of MC@NLO/PY and of the pure-NLO predictions are therefore consistent at large p_T 's. This is what we expect, since there the MC@NLO/PY result is basically coincident with the NLO one, the effect of the shower being negligible on these inclusive variables. The size of the scale dependence is also compatible with the fact that, in fixed-order perturbation theory, $\mathcal{O}(\alpha_S)$ is actually the first order that contributes to $p_T > 0$. This observation therefore applies also to low p_T 's in the case of the pure-NLO predictions, but it does not in the case of MC@NLO/PY. In fact, MC@NLO/PY fills the low- and intermediate- p_T regions mostly through the showering of S events. The shower, however, determines only the kinematics of the final-state configuration (i.e., the p_T of the W and of the hardest jet here), but the weights are given by the short-distance cross section of eq. (2.48), and therefore receive both $\mathcal{O}(\alpha_S^0)$ and $\mathcal{O}(\alpha_S)$ contributions. This implies that in the low- p_T region one expects

²MC@NLO outputs unweighted events. The plots presented here have been obtained with $5 \cdot 10^5$ -event samples, and therefore less than five hundred events have p_T 's larger than a few hundreds GeV.

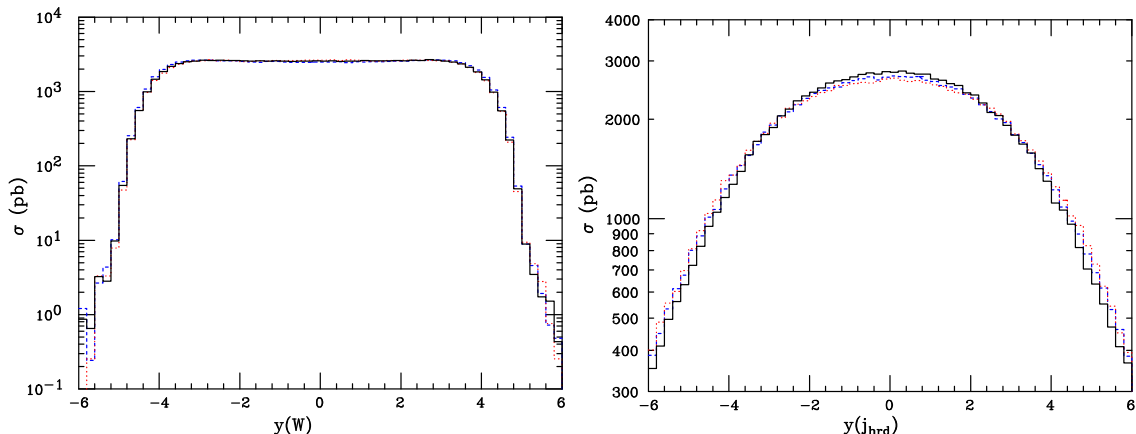


Figure 4. Same as in figure 3. Left pane: rapidity of the W boson. Right pane: rapidity of the hardest jet of the event.

MC@NLO/PY to have a scale dependence smaller than that of the tree-level $\mathcal{O}(\alpha_s)$ term alone, which is what we observe. We conclude this discussion by noting that other definitions can be given of the uncertainties associated with mass scales (e.g., variations may be summed linearly rather than in quadrature), without this changing the pattern found here. We also point out that the scale dependences of the rapidity observables which we shall discuss below are rather featureless (i.e., scale variations are independent of rapidities), and therefore they will not be shown in what follows.

In figure 4 we consider the rapidity distributions of the W^+ boson (left pane), and of the hardest jet of the event (right pane). In the absence of any cuts in p_T , the boson rapidity is an inclusive variable unaffected by large logarithms, and both NLO computations and MC simulations should predict it relatively well. We do indeed see an overall consistency among MC@NLO/PY, MC@NLO/HW, and PYTHIA standalone. Differences among the three predictions are larger in the case of the rapidity of the hardest jet, since this is a less inclusive variable w.r.t. the W rapidity, and is also more sensitive to hadronization corrections. The PYTHIA standalone results have been rescaled by the NLO K-factor, σ_{NLO}/σ_{LO} , before any cuts are applied and jets are reconstructed.

Finally, in figure 5 we consider the difference between the rapidities of the W^+ boson and of the hardest jet, for two different cuts on the transverse momentum of the hardest jet. The PYTHIA standalone results have been rescaled in the same way as in figure 4. This observable and its analogues (with y_W replaced by y_S , S being the system emerging from the hard process at the Born level - e.g. the $t\bar{t}$ pair in top-pair production) has attracted some attention in the past (see e.g. ref. [15] for a recent discussion), owing to the fact that MC@NLO/HW has a different behaviour around $y_S - y_j \simeq 0$ w.r.t. the underlying NLO computation — the former being flatter than the latter, or having a dip, depending on the nature of the system S . The “flatness” or the presence of a dip is a feature of MC simulations, and more specifically is a consequence of the choices made for initial conditions, as was done here for PYTHIA in eq. (2.34). It has to be stressed that this is true for both HERWIG and PYTHIA, as the dashed histogram on the right pane of

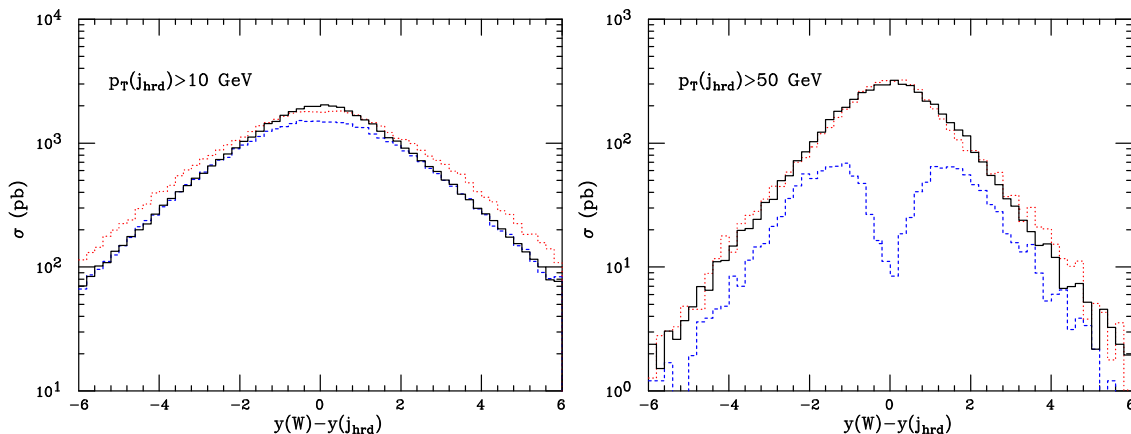


Figure 5. Same as in figure 3, for the difference in rapidity between the W boson and the hardest jet of the event. Two cuts on the p_T of the jet are considered.

figure 5 shows, and therefore has nothing to do with the presence of dead zones³ as such in HERWIG. In PYTHIA, the choice of initial conditions is much more flexible than in HERWIG, and one can make the dip of figure 5 disappear by choosing a large-enough scale as the maximum virtuality allowed for the shower. In doing so, however, one may extend the collinear approximation, that is the core of both HERWIG and PYTHIA, outside its proper range of validity, and we consider the choice made in eq. (2.34) a sensible one. Events in MC@NLO, or matrix element corrections in HERWIG and PYTHIA, will give a substantial contribution to the region $y_S - y_j \simeq 0$ (see the solid and dotted histograms in figure 5), where the predictions will become closer (w.r.t. those of MC simulations without matrix element corrections) to the pure-NLO results. Differences will in general remain, that can be formally ascribed to effects beyond NLO.

In order to further this argument, we consider an extension of the choice made in eq. (2.34). Namely, we parametrize the maximum virtuality allowed in the shower in terms of a number f introduced as follows:

$$|t_i| \leq (fm_V)^2 \quad \implies \quad \Theta_{\pm} = \Theta\left(y - \frac{1 - (1 + 2f^2)x}{1 - x}\right). \quad (3.1)$$

The plots shown so far have therefore been obtained with $f = 1$. In figure 6 we consider again the difference in rapidity of figure 5, with $f = 1/2$ (dotted red histograms) and with $f = 2$ (dashed blue histograms), together with our default choice $f = 1$ (solid black histograms); we point out that for the values of f considered here the fraction of negative weights is basically a constant. Two additional p_T cuts are also considered on top of those of figure 5. The results obtained with PYTHIA feature a very large sensitivity to the choice of f , while those obtained with MC@NLO/PY are fairly stable. One may be tempted to use the results of figure 6 in order to “tune” the parameter f , and obtain a PYTHIA prediction in decent agreement with that of MC@NLO/PY. However, this is an *a posteriori* procedure,

³Negative weights in MC@NLO are also not an issue. This is *a fortiori* true in MC@NLO/PY, where they are basically negligible.

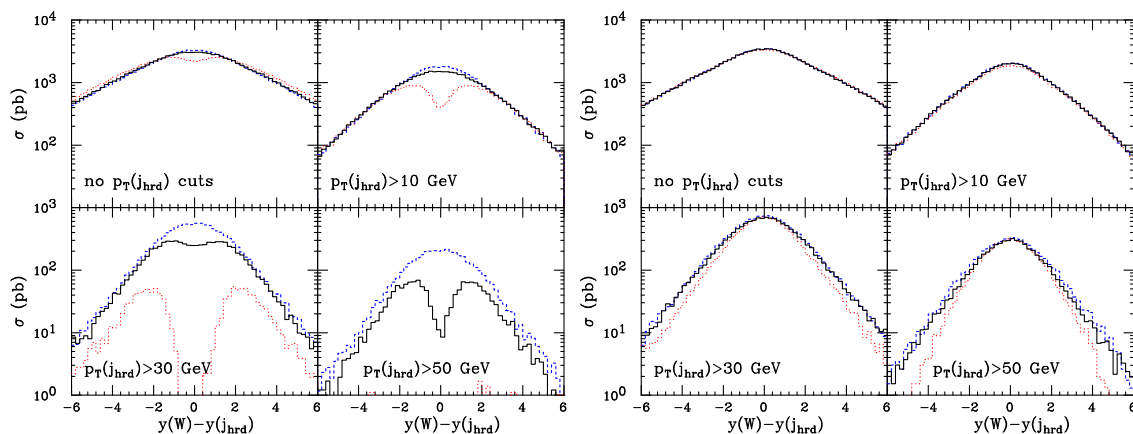


Figure 6. Rapidity differences between the W and the hardest jet of the event, with PYTHIA (left pane) and MC@NLO/PY (right pane), for different values of f in eq. (3.1). Four cuts on the p_T of the jet are considered.

which can be justified phenomenologically, but which implies that any possibility is given up of a sensible estimate of the theoretical uncertainties affecting the observable considered here; also, such a procedure is in general observable-dependent. Indeed, the left pane of figure 6 shows that, if no information on $2 \rightarrow 2$ matrix elements is included, this rapidity difference basically cannot be *predicted* by Monte Carlo at moderate and large p_T 's. This is not surprising, given that one is attempting to use the collinear approximation outside its range of validity: the correct result can be recovered (which is equivalent to choosing the argument of a logarithm so as its numerical value coincides with a given constant), but only in a heuristic way. The situation improves if the correct information on matrix elements is used, as in MC@NLO/PY. This is analogous to what happens when one varies the renormalization and factorization scales, at the LO and the NLO levels. As in the case of scale variations, extreme values for f will lead to problems; however, $f = \mathcal{O}(1)$ appears to be a safe choice, allowing one to realistically estimate theoretical uncertainties. We conclude by mentioning that other observables (such as those shown in figure 3 and 4) display the same pattern of dependence on f as the observable in figure 6. We shall discuss this issue further [16] by considering also the case of Higgs production, where the effects are more pronounced.

4 Conclusions

We have presented the construction of the matching between an NLO QCD computation and the virtuality-ordered PYTHIA Monte Carlo, according to the MC@NLO formalism. We have limited ourselves to considering only the case of initial-state radiation, and applied the formalism to the study of W hadroproduction. Owing to the different structures of HERWIG and PYTHIA, the short-distance MC@NLO cross sections used to generate hard events are different in the two cases. However, the FKS subtraction, which is the method used in MC@NLO for dealing with infrared singularities, needs no modifications, and is

able to treat both MCs. Likewise, no changes are needed in the MC@NLO formalism, and the matching with PYTHIA is achieved by performing a process-independent calculation.

For the process considered in this paper, the fraction of negative weights in MC@NLO/PY is much smaller than that in MC@NLO/HW. From the physical viewpoint, the pattern of the comparison between MC@NLO, pure-NLO, and PSMC results is the same for MC@NLO/PY as for MC@NLO/HW — MC@NLO shows the same behaviour as the NLO or MC where either one is most reliable, with a smooth transition between the hard and soft-collinear emission regions.

Although the process studied in this paper is particularly simple, the formulae given here will be basically sufficient for performing the matching in the case of more complicated reactions (and limited to initial-state branchings only). Therefore, the results presented here are the first step towards the construction of MC@NLO/PY for generic processes, where also final-state radiation is present, and towards the extension of this formalism to the p_T -ordered version of PYTHIA.

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