## Mathematical Techniques of Applied Probability

**Volume 2 Discrete Time Models: Techniques and Applications** 

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