TITLE Mathematics Learning and the Sexes：A Review． PUB DATE． NOTE

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The purpose of this paper was to explore the literature to see what differences，if any，exist between the sexes in mathematics achievement from pre－school through high school levels．Thirty－three studies were reported．Findings showed that there were no significant differences between boys＇and girls＇ mathematics achievement in pre－school or early elementary years．In upper elementary and early high school years，significant differences were not always apparent；however，when significant differences did appear they were more apt to be in the boys＇favor when the higher－level cognitive tasks were being measured and in the girls＇ favor when lower－level cognitive tasks were measured．No conclusions were reached concerning high school learners．Six questions were raised concerning the relationship between sex differences and mathematics achievement．（DT）

MATHEMATICS LEARNING AND THE SEXES: A REVIEN Elizabeth Fennema University of Wisconsin-Madison

Are there really sex differences in mathematics achievement? A Guide to Current Research: Elementary Sclool Mathematics (Glennon and CaIlahan, 1968, p. 30) states that "The evidence would suggest to the teacher that boys will achieve higher than girls on tests dealing with mathematical reasoning while the girls will achieve higher than boys on tests of computational ability." An equally prestigious review of research (Suydam and Riedesel, 1969, p. 129) states that there are no significant differences between the sexes in arithmetic achievement before 7 th grade but boys surpass girls after 7th grade. Aiken (1971, p. 203) states that "Sex differences in mathematical abilities are, of course, present at the kindergarten level and undoubtedly earlier." One could conclude from these reviews that a sex difference in learning mathematics does exist and that it is in favor of boys. However, Parsley et. al. $(1963,1964)$ in two of the few studies concerned basically with sex as an important variable, found few if any significant differences between boys' and girls' learning of mathematics.

Is boys' superiority in the learning of mathematics a myth or is it a reality? The purpose of this paper is to explore the literature in depth to see what differences if any do exist between the sexes in mathematics achievenent. If sex differences do not exist, then educators should discard their belicf about boys' superiority. However, if there are sex differences in learning mathematics, then the mathematics education profession has a direct responsibility to provide research data, curricular materials and teacher training that will enable boys and girls equally to fulfill their
cognitive potential in mathematics.
The studies that have been included are those reported since 1960 which used United States citizens as subjects. Such studies were difficult to find because often when sex is used as an independent variable, it is treated and discussed casually, if at all. Because of this, probably not all the relevant studies vere found, but it is assumed that all important studies reported since 1960 have been included. The studies included have been grouped into broad age/grade categories.

## Studies Related to Pre-School Subjects

Three investigators have reported on mathematical knowledge of boys and girls before they enter school, and these studies are summarized in Table I. None of the three studies report any significant differences between the mathematical knowledge of three, four, or five-year-old boys and girls. It seems safe to assume on the basis of the consistency of results of these three studies that boys and girls enter school with similar mathematical knowledge.

Insert Table I about here

## Studies Related to Early Elementary School Children

Table II summarizes nine studies which used early elementary school children as subjects. One study (Hervey, 1966) indicated that boys performed better than did girls. One study (Lesser, Fifer, and Clark, 1965) showed that boys performed better on one scale. Two studies (Lowery and Allen, 1970; Wozencraft, 1963) indicated that girls performed better than boys. In the five other studies, involving a variety of measures of math-
ematical learning, no significant differences were found. From the results of these studies, it appears reasonable to conclude that there are no consistent significant differences in the learning of mathematics by boys and girls in the early elementary years.

## Insert Table II about here



## Studies Related to Older Children

The picture concerning differences in learning mathematics by boys and girls becones more confused during the pre- and early adolescent years.

Eighteen studies summarized in Table III were found that used as subjects learners in this age range. These studies used a wide variety of instruments to assess learning. Nine studies used standardized achievemeni: tests which commonly were divided into two subtests: reasoning and computation (or fundamentals). Even though different standardized tests were used, they undoubtedly measure similar kinds of learning so it is profitable to look at the results of these studies combined. Four studies (Cleveland and Bosworth, 1967; Parsley et. al., 1963; McGuire, 1951; and Gainer, 1962) report no sj.gnificant differences. Zahn (1966) reported a difference which may be significant in favor of boys on the total score while Singhal and Crago (1971) and Wozencraft (1963) reported a significant difference in favor of girls on total score. Jarvis (1964) reported that boys scored significantly higher than girls on reasoning, while the reverse was true for computation. The superiority of girls over boys in computation was confirmed by Parsley, et. al. (1964).

Unkel (1966) investigated the discrepancy between an anticipated arith-
metic achievement (as determined by chronological age, grade placement, and mental age and actual arithmetic achievement of 918)children in grades 1-9. The California Achicvement Test was the criterion measure. Interestingly, the girls had significantly hi.gher discrepancy scores than the boys on tests involving arithmetic fundamentals. No significant difference in discrepancy scores was found in arithmetic reasoning. In other words, no significant differences were found between girls' and boys' performance on tests of arithmetic reasoning when intelligence was controlled but boys were performing significantly better on tests of arithmetic fundamentals. This finding appears to contradict the findings of Parsley and Jarvis who found girls significantly superior in arithmetic fundamentals. The discrepancy scores for boys and girls in arithnetic total score was surprisingly similar until 6th grade when the girls evidenced much higher discrepancy scores. This difference was in arithmetic fundamentals.

Insert Table III about here

One Parsley study (1964) has been widely quoted as supportive of the belief that boys achieve significantly better than girls in mathematics. Because this study used sex as the major independent variable and has affected the belief of many concerning achievement, it and the previous study on which it is based will. be discussed in depth.

In 1963, Parsley et. al. reported a study which used 2,651 boys and 2,369 girls in grades $2-8$ as subjects. Scores from the California Arithmetic test (Reasoning and Fundamentals) were analyzed on the basis of sex and critical ratios were reported. None of these ratios approached significance. The subjects were also categorized into five ability levels
by scores received on the California Test of Mental Ability and once again no significant differences between the sexes were found. These negligible results prompted the authors to duplicate the study the following year with 3,551 subjects and to add an additional analysis -- that of achievement level as it is related to intellectual ability (Parsley ct. al., 1964). On the basis of this, children were categorized as under-, average-, or overachievers. From this study the authors concluded that "Boys do excel in Arithmetic Reasoning, but not in Arithmetic Fundamentals." However, an examination of the data does not substantiate this conclusion. The number of significant differences found is show in Table IV. In Arithmetic Reasoning, boys scored significantly higher than girls 12 times while girls scored significantly higher than boys ${ }^{7}$ times. There were 75 individual compari.sons (t tests) reported (five grades by five ability levels by three achievement levels). As there was no control for alpha level the strong conclusion reached by the authors does not appear warranted. In the area of Arithmetic Fundamentals girls scored significantly higher than boys 24 times while boys scored significantly higher than girls three times. The authors do not conclude that girls excel in Arithmetic Fundamentals even when the case for this conclusion is stronger than the case for the boys excelling in Arithmetic Reasoning.

Insert Table IV about here

The data were also examined to determine if ability level and achievement level were related to sex. Table $V$ shows the significant differences found. Girls appear to out-perform boys in Arithmetic Fundamentals at all ability levels except the very highest while very bright boys outperform very bright
girls in Arithmetic Reasoning.

Insert Table V about here

It is not reasonable from this study to conclude that boys learn mathematics better than do girls. In fact, a strong case can be made for concluding that since girls outperform boys consistently in Arithmetic Fundamentals, girls learn mathematics better than do boys.

The National Longitudinal Study of Mathematical Ability (NLSMA) is one of the most extensive studies of mathematics achievement which has been done. Data concerning one group (the X-Population) were collected for five years as the students progressed from Grade 4 through Grade 8 (Carry and Weaver, 1969; Carry, 1970) and sdta from another group (the Y-Population) were collected for four years as the subjects progressed from Grade 7 through Grade 10 (ricLeod \& Kijpatrick, 1969 and 1971; Kilpatrick \& McLeod, 1971).* Although the main variable studied was the impact of various textbook series on learning, sex was also used as a basis for analysis. The sex data analyses were reported in the appendices of the various volumes and while it appears that the differences found between the sexes were large enough to be educationally significant, practically no discussion of these results are included in the reports. Due to the lack of discussion concerning the sex differences which were found in this important series of studies, the data from these studies will be examined here.

Evaluation instruments used to assess learning at all grade levels were classified by categories of mathematical content (number systems, geometry, and algebra) and by cognitive complexity of the task (Computation, Compre-

[^0]hension, Application, and Analysis). Data collected from these instruments were first analyzed for a sex X textbook interaction and if no significant interaction was found, the data were analyzed for sex differences. Tables VI and VII provide summaries of the total number of tests at each grade level, at each cognitive complexity and the number of significant differences found between the performance of girls and boys.

Insert Tables VI and VII about here

In both populations girls performed slightly better than did boys in the least complex skill (Computation). In 21 out of 50 tests of Computation girls surpassed boys, wilile boys surpassed girls 11 times. However, the highest percent of significant differences were found in the $X$-Population at Grades 4-6. With the older subjects of the Y-Population fewer significant differences in computation were found. In the 77 tests of more complex cognitive skills (Comprehension, Application, and Analysis) five tests had results which favored the girls while 54 tests showed significant differences in favor of boys. The conclusion is inescapable that the boys of these populations learned the mathematics measured by these tests better than did the girls of these populations. While the girls appear to have done slight.ly better at younger ages in a low level cognitive skill, by the time puberty was well established ( 9 th , 10th grades) boys are outperforming girls at all levels of cognitive complexity.

Six other studies are included in Table III. Muscio (1962) found significant differences in favor of boys on a test of quantitative understanding while Olander and Ehmer (1971) found significant differences in favor of girls in mathematical vocabulary. In tests which appear from their descriptions to measure abilicies similar to those of Standardized tests (Reasoning, Alexander (1962) D'Augustine (1966) and Sowder (1971) found no
significant differences.
Sheehan (1968) found ambivalent results. In this study, ninth grade girls performed significantly better than did boys when learning to solve algebra problems. However, when the influence of eighth grade mathematics achievement, algebra aptitude, pre-instructional score, I.Q., and reading ability were eliminated, the boys' scores were significantly higher t'ran the girls' scores. Why this last analysis was done is not clear as the subjects were randomly selected originally. Evidently girls had learned more before the study (as evidenced by eighth grade mathematics achievement- and pre-instructional score) and as a result were able to learn how to solve algebra problems better.

Although generalizing results $\underset{\text { Erom }}{ }$ so many divergent studies which analyzed different aspects of mathematics learning hides subtle and important variations, it appears safe to conclude that in overall performance on tests measuring mathematics learning that there are no significant differences that consistently appear between the learning of boys and girls in the fourth to ninth grade. There appears to be a trend, however, that if a difference does exist, girls tend to perform better in tests of mathemati.cs computation (Parsley, 1964; Wozencraft, 1963) and boys tend to perform better in tests of mathematical reasoning (Carry and Weaver, 1969; Carry, 1970; McLeod and Kilpatrick, 1969 and i971; Kilpatrick and McLeod, 1971; Jarvis, 1964; Zahn, 1966; Muscio, 1962).

## Studies Concerned with High Sc!iool Subjects

Although there appear to be psychological studies which focus on analytical and spatial ability, studies dealing with sex differences explicitly in mathematics achievement at the secondary school level reported since 1980
are difficult to find.
When data concerning high school learners is considered, there are at least two important confounding factors. More boys than girls drop out of school and boys drop out at younger ages (Fitzsimmons, 1969). Lower ability boys tend to drop out so that most samples of high school boys are more homogencous as far as ability is concerned than are the samples of girls. Girls do not elect mathematics courses as often as do boys. If, perchance, brighter girls tend not to elect mathematics, then a lower ability sample of girls will result. Comparing a sample of this type with a sample of boys from which lower ability learners have dropped out does not appear to be reasonable. Both of these confounding effects should be investigated be.. fore definite conclusions concerning this age group can be made. In Table VIII the three studies that were found are summarized. In one study (Backman, 1972) significant differences in favor of the boys were found. In one study (Easterday and Easterday, 1968) significant differences in favor of girls were found and in one study (Bhushan et. al., 1968) no significant differences were found. On the basis of these three different results, it is difficult to conclude anything but that more information is needed.

Insert Table VIII about here

## Summary and Questions

The purpose of this paper was to critically examine relevant literature in order to answer the question: "Are there sex differences in mathematics achievement?" Thirty-three studies were reported which should help in answering the question, but an answer to part of the question appears clearer than other parts. No significant differences tetween boys' and girls' math-
ematics achievement were found before boys and girls entered elementary school or during early elementary years. In upper elementary and early high school years significant differences were not always apparent. However, when significant differences did appear they were more apt to be in the boys' favor when higher level cognitive tasks were being measured and in the girls' favor when lower level cognitive tasks were being measured. No con-. clusion can be reached concerning high school learners.

This review has raised more questions than it has answered.

1. Are there clearly identifiable, consistent differences in mathematics achievement which can be attributed to the sex of learners?.
2. What is the relationship between sex role identity development and achievement in mathematics? As sexual role assumes increasing importance at puberty, the differences between the sexes in mathematics achievement appear to increase.
3. What sex-related factors influence mathematics achievement? Are these factors inherent or environmental? The lack of sexual differences in learning mathematics until fourth grade would suggest that these factors are environmental. On the other hand, Stafford (1972) suggests that inherent factors are more important.
4. Can learning environments be structured to enable boys and girls to achieve at similar levels in mathematics after puberty begins?
5. Is there "sexism" in mathematics education research and its reporting? The NNA Reports' emphasis and the conclusion reached in the Parsley study suggests that this question be considered.
6. Is there "sexism" in mathematics education? If mathematics educators believe that there is a sex difference in learning mathematics
(as was evidenced in the reviews cited) and have not attempted to help girls achieve at a similar level to boys, then this question must be answered in the affirmative.

AGE OF SUBJEGT
3 and 4 years
Pre-school

Entering
Kindergarten


Ability to acquire a problem solving
Ability to solve 4 types of open
sentences involving addition.
mathematical operation that would
enhance the solution. before instruction in the specific

Ability to solve verbal problems inclusion, seriation, ordination,
reordering and transitivity. Conservation of number and weight, class

Open and closed sentences
Ability to categorize items differing
on one, two, or three attributes.
Concept of addition
Early E1ementary School
Sex Differences in Mathematics Achievement
No significant differences found.

## 

No significant differences found.


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Table IV
Significant Differences Found Between Males and Females in Arithmetic Reasoning and Fundamentals*

Arithmetic Reasoning ** $\quad$ Arithmetic Fundamentals **

*Data from Parsley, Powell and $0^{\prime}$ Connor (1964)
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${ }^{b}$ Indicates number of tests at each level in which significant differences in performance were found.
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No significant differences

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[^0]:    * Data for the Z-Population were also collected but are unavailable at the present time.

