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1 Measurement of a Doubly-Substituted Methane
2 Isotopologue, $^{13}\text{CH}_3\text{D}$, by Tunable Infrared Laser
3 Direct Absorption Spectroscopy

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Abstract

Methane is an important energy resource and significant long-lived greenhouse gas. Carbon and hydrogen isotope ratios have been used to better constrain the sources of methane, but interpretations based on these two parameters alone can often be inconclusive. The precise measurement of a doubly-substituted methane isotopologue, $^{13}\text{CH}_3\text{D}$, is expected to add a critical new dimension to source signatures by providing the apparent temperature at which methane was formed or thermally equilibrated. We have developed a new method to precisely determine the relative abundance of $^{13}\text{CH}_3\text{D}$ by using tunable infrared laser direct absorption spectroscopy (TILDAS). The TILDAS instrument houses two continuous wave quantum cascade lasers; one tuned at $8.6\ \mu\text{m}$ to measure $^{13}\text{CH}_3\text{D}$, $^{12}\text{CH}_3\text{D}$ and $^{12}\text{CH}_4$, and the other at $7.5\ \mu\text{m}$ to measure $^{13}\text{CH}_4$. Using an astigmatic Herriott cell with an effective pathlength of 76 m, a precision of $0.2\ ‰$ (2σ) was achieved for the measurement of $^{13}\text{CH}_3\text{D}$ abundance in ca. 10 mL STP (i.e., 0.42 mmol) pure methane samples. Smaller quantity samples (ca. 0.5 mL STP) can be measured at lower precision. The accuracy of the $\Delta^{13}\text{CH}_3\text{D}$ measurement is $0.7\ ‰$ (2σ), evaluated by thermally-equilibrating methane with a range of δD values. The precision of $\pm 0.2\ ‰$ corresponds to uncertainties of $\pm 7^\circ\text{C}$ at 25°C and $\pm 20^\circ\text{C}$ at 200°C for estimates of apparent equilibrium temperatures. The TILDAS instrument offers a simple and precise method to determine $^{13}\text{CH}_3\text{D}$ in natural methane samples to distinguish geological and biological sources of methane in the atmosphere, hydrosphere, and lithosphere.

38

Introduction

39 Methane is the second most important long-lived greenhouse gas, and an increasingly
40 important energy resource.¹ Abrupt changes in reservoirs and fluxes of methane in the Earth's
41 surface may have been responsible for triggering abrupt climate change in the past². The
42 atmospheric methane level increased through much of the twentieth century, but the growth rate
43 slowed and the concentration appeared to have plateaued between 1999 and 2007, at which point
44 growth resumed.³ The main drivers for this secular trend have been debated, with explanations
45 ranging from changes in source (e.g., wetlands vs. fossil fuel emissions) and/or sink (oxidation
46 by OH radical) strengths.³⁻⁵

47 The majority of environmental methane is of biogenic (originating from microbial
48 methanogenesis) or thermogenic (produced by thermal cracking of higher molecular weight
49 hydrocarbons, kerogen and coal) origin, with contributions from biomass burning and, in certain
50 geologic environments, putative abiotic sources (e.g., serpentinite and deep crustal fluids).⁶⁻⁸

51 Carbon ($^{13}\text{C}/^{12}\text{C}$) and hydrogen (D/H) isotope ratios of methane and associated short-
52 chain hydrocarbons have been used to elucidate their sources^{9,10} but such data alone can often be
53 inconclusive because of significant overlap in isotopic signatures associated with microbial,
54 thermogenic and abiogenic gases. This is because the $^{13}\text{C}/^{12}\text{C}$ ratio of methane depends on the
55 carbon source (e.g., CO_2 , acetate) and its isotopic composition,¹¹ the isotope effects associated
56 with microbial methanogenesis or thermal cracking, and the effects of secondary processes, such
57 as oxidation and mixing.^{12,13} The D/H ratio of methane is also a complex function of reaction
58 pathways, the D/H ratio of environmental water, and the D/H ratio of precursor compounds.^{14,15}
59 Therefore, the development of a new constraint, such as an isotopic thermometer, could unlock
60 critical information to constrain the source of methane.

61 In this study, we report a methane isotope thermometry method based on the
62 measurements of the doubly-substituted (“clumped”) methane isotopologue, $^{13}\text{CH}_3\text{D}$. Following
63 earlier studies of doubly-substituted carbon dioxide ($^{13}\text{C}^{16}\text{O}^{18}\text{O}$),¹⁹ the precise measurements of
64 four or more isotopologues of methane ($^{12}\text{CH}_4$, $^{13}\text{CH}_4$, $^{12}\text{CH}_3\text{D}$, and $^{13}\text{CH}_3\text{D}$) may allow
65 estimation of the temperature at which a sample of methane was formed or thermally
66 equilibrated.^{20,21}

67 Carbon ($^{13}\text{C}/^{12}\text{C}$) and hydrogen (D/H) isotope ratios of methane have been routinely measured
68 by gas-source isotope-ratio mass spectrometry (IRMS). Conventional IRMS techniques for
69 measuring carbon- and hydrogen-isotope ratios involve combustion or pyrolysis of methane,
70 respectively, and measurement of the isotopologue ratios of the product CO_2 or H_2 .^{9,22} Direct
71 measurement of $^{13}\text{CH}_3\text{D}^+$ ion is required, however, for mass-spectrometric determination of
72 $^{13}\text{CH}_3\text{D}$. This is technically challenging because of the low fractional abundance of $^{13}\text{CH}_3\text{D}$ (ca. 3
73 to 8 ppm) and interferences from adduct ($^{13}\text{CH}_5^+$) and $^{12}\text{CH}_2\text{D}_2^+$ ions. Fragment ions (e.g., CH_3^+ ,
74 CH_2^+) also complicate mass-16 ($^{12}\text{CH}_4^+$) and mass-17 ($^{12}\text{CH}_3\text{D}^+$ and $^{13}\text{CH}_4^+$) signals. Resolving
75 these isobars requires the use of double-focusing high resolution gas-source IRMS.^{21,23} Stolper et
76 al. (2014)²¹ report the first precise measurements of methane clumped isotopologue abundance
77 (combined $^{13}\text{CH}_3\text{D}+^{12}\text{CH}_2\text{D}_2$) by using medium mass-resolving power ($M/\Delta M$) from 16,000 to
78 25,000; contributions of adduct ions ($^{13}\text{CH}_5^+$ on $^{13}\text{CH}_3\text{D}^+$, and $^{12}\text{CH}_5^+$ on $^{12}\text{CH}_3\text{D}^+$) were corrected
79 as a function of mass-16 ion current.

80 In this study, we report the application of tunable infrared laser direct absorption spectroscopy
81 (TILDAS) for the fully-resolved measurement of a clumped isotopologue of methane, $^{13}\text{CH}_3\text{D}$.
82 TILDAS is a virtually non-destructive technique, and offers a promising approach for precise
83 and direct measurements of methane isotopologues. Bergamaschi et al. (1994)²⁴ reported

84 measurements of $^{13}\text{CH}_4$ and $^{12}\text{CH}_3\text{D}$ using a lead salt diode laser tuned in the $\sim 3.3 \mu\text{m}$ regions (ν_3
85 band). Precisions of 0.44 and 5.1 ‰ were achieved for $\delta^{13}\text{C}$ and δD measurements,
86 respectively (δ values are defined as the deviation of the isotope ratios $^{13}\text{C}/^{12}\text{C}$ and D/H
87 with respect to reference materials). Recently, a tunable laser spectroscopy instrument
88 with an interband cascade laser tuned at $3.27 \mu\text{m}$ was used for the detection of methane on
89 the Mars *Curiosity* rover mission.²⁵ Tsuji et al., (2012)²⁶ reported the first optical measurement
90 of $^{13}\text{CH}_3\text{D}$ using a difference-frequency-generation laser in the $3.4 \mu\text{m}$ region. Their reported
91 analytical precision of 20‰ (1σ), however, was too large to resolve the thermodynamically-
92 predicted natural range of variation of $^{13}\text{CH}_3\text{D}$ abundances (ca. 6‰).

93 The TILDAS instrument used in this study takes advantage of quantum cascade lasers
94 (QCLs) that allow for continuous wave (cw) operation near room temperature, with high power
95 (tens of mW) and narrow linewidths ($< 0.001 \text{ cm}^{-1} \approx 30 \text{ MHz}$). These lasers access the $8 \mu\text{m}$ (ν_4)
96 band system of CH_4 , where several isolated absorption bands are available. Previously, a
97 TILDAS instrument equipped with a cwQCL achieved a precision of 0.2 to 0.5 ‰ for
98 $^{13}\text{CH}_4/^{12}\text{CH}_4$ ratios during continuous sampling of ambient air ($\sim 1.8 \text{ ppm CH}_4$ mixing ratio).^{27,28}
99 This report describes the application of a dual laser TILDAS instrument for the precise
100 measurement of the abundance of $^{13}\text{CH}_3\text{D}$ in pure samples of methane. We report here the
101 selection and characterization of absorption lines, the construction of a dual-inlet sample
102 introduction system, the results of calibration and performance testing, and some preliminary
103 data obtained by the TILDAS instrument.

104

Principle of Methane Isotopologue Thermometry

105 The goal of this study is to develop methane isotopologue thermometry based on the
106 following isotope exchange reaction among four isotopologues of methane:



107 The equilibrium constant (K) for this reaction is a function of temperature:

$$K(T) = \frac{[^{13}\text{CH}_3\text{D}][^{12}\text{CH}_4]}{[^{12}\text{CH}_3\text{D}][^{13}\text{CH}_4]} \quad (2)$$

108 where brackets represent the abundance (e.g., mixing ratio) of each methane isotopologue.

109 The equilibrium constant approaches unity at very high temperatures (>1,000K), and referred to
110 as a stochastic distribution. At lower temperatures, however, statistical mechanics theory
111 predicts that the equilibrium for (1) lies slightly toward the right ($K \approx 1.006$ at room temperature,
112 *see* Supporting Information, SI).

113 Defining $\Delta^{13}\text{CH}_3\text{D}$ as the natural logarithm for equation (2) gives:

$$\Delta^{13}\text{CH}_3\text{D} = \ln(K) = \ln \frac{[^{13}\text{CH}_3\text{D}]}{[^{12}\text{CH}_3\text{D}]} - \ln \frac{[^{13}\text{CH}_4]}{[^{12}\text{CH}_4]} \quad (3)$$

114 The definition of $\Delta^{13}\text{CH}_3\text{D}$ in equation (3) yields values that are practically identical to those
115 calculated using the definition used by Stolper et al. (2014)²¹ (i.e., the deviation from stochastic
116 distribution. *see* SI).

117 In this study, we use conventional delta notation to express ratios of isotopologue abundance in
118 a sample with respect to those of a reference. For example,

$$\delta^{13}\text{CH}_3\text{D} = \frac{([^{13}\text{CH}_3\text{D}]/[^{12}\text{CH}_4])_{\text{sample}}}{([^{13}\text{CH}_3\text{D}]/[^{12}\text{CH}_4])_{\text{reference}}} - 1 \quad (4)$$

119 For practical purposes (under expected ranges of multiply-substituted isotopologue abundance
120 for natural samples), $\delta^{13}\text{CH}_4$ is identical to $\delta^{13}\text{C}$ and $\delta^{12}\text{CH}_3\text{D}$ is identical to δD .

121

Experimental Section

122 **Synthesis of Methane Isotopologues**

123 Methane isotopologues, $^{13}\text{CH}_3\text{D}$, CH_3D (natural abundance $^{13}\text{C}/^{12}\text{C}$), and CH_4 (D-depleted)
124 were synthesized for spectral characterization and to produce a series of working standard gases.
125 The clumped methane isotopologue, $^{13}\text{CH}_3\text{D}$, was synthesized by the Grignard reaction from ^{13}C -
126 iodomethane and D_2O . Similarly, CH_3D (with natural-abundance ^{13}C) was synthesized from
127 iodomethane and D_2O . D-depleted methane was synthesized from aluminum carbide (Al_4C_3 ,
128 natural C isotope abundance) and D-depleted water (D content 2-3 ppm) (*See SI for detailed*
129 *description of synthesis procedures*).

130

131 **Selection of Absorption Lines**

132 Among several possible methane infrared band systems, a spectral region around $8.6\ \mu\text{m}$ was
133 selected. Tsuji et al. (2012)²⁶ reported measurements of $^{13}\text{CH}_3\text{D}$ in the $3.4\ \mu\text{m}$ region. However,
134 they used dry ice to cool the absorption cell in order to reduce hot bands and high-J fundamental
135 bands from major isotopologues. The absorption band system at $8.6\ \mu\text{m}$ is highly advantageous
136 because of less interference from hot bands in this region, and the availability of line parameters
137 in the HITRAN database.²⁹ A single deuterium substitution in CH_4 reduces its symmetry from T_d
138 to C_{3v} . As a result, the triply degenerate C-H bending mode of CH_4 centered at $1300\ \text{cm}^{-1}$ splits
139 into C-D bending of $^{13}\text{CH}_3\text{D}$ and $^{12}\text{CH}_3\text{D}$. The resultant C-D bending mode is about $150\ \text{cm}^{-1}$
140 lower in frequency than the C-H bending vibration. This relatively large frequency shift by
141 deuterium substitution allows us to measure $^{13}\text{CH}_3\text{D}$ and $^{12}\text{CH}_3\text{D}$ lines that are free from strong
142 lines originating from the much more abundant $^{12}\text{CH}_4$ (Figure 1).

143 The spectral window between 1168.885 and 1168.995 cm^{-1} was chosen to access three
144 isotopologue lines of $^{13}\text{CH}_3\text{D}$, $^{12}\text{CH}_3\text{D}$ and $^{12}\text{CH}_4$ (Figure 1 and 2). These three lines are
145 virtually-free from spectral interference, and have relatively low lower-state energies (59, 470,
146 and 861 cm^{-1} for $^{13}\text{CH}_3\text{D}$, $^{12}\text{CH}_3\text{D}$, and $^{12}\text{CH}_4$, respectively), such that temperature-dependence is
147 expected to be minor ($<0.15\%/10\text{mK}$, Table 1). The absorption line for $^{13}\text{CH}_4$ was measured in
148 a spectral window between 1330.94 and 1331.02 cm^{-1} (Figure 2). This line was selected because
149 the line strength is comparable to other isotopologues ($\sim 10^{-24}$ $\text{cm}/\text{molecule}$) such that the line
150 does not saturate.

151

152 TILDAS Spectrometer

153 The TILDAS instrument used in this study is based on direct absorption using the astigmatic
154 multipass Herriott cell developed by Aerodyne Research.³⁰ The instrument houses two
155 continuous wave quantum cascade lasers (QCLs) (Alpes Laser, Switzerland). The first laser
156 (L1) is tuned to $^{12}\text{CH}_4$ and $^{13}\text{CH}_4$ line at 1331 cm^{-1} , and the second (L2) is tuned to $^{12}\text{CH}_3\text{D}$, $^{12}\text{CH}_4$
157 and $^{13}\text{CH}_3\text{D}$ absorption lines at 1169 cm^{-1} . The lasers are housed in hermetically-sealed boxes,
158 and their temperatures are controlled by Peltier elements at 2.6 and -1.8 $^{\circ}\text{C}$ for L1 and L2,
159 respectively. The supply voltages to the QCLs are ramped at a rate of 1.4 kHz to scan the laser
160 frequency across 300 channels for L1 and 600 channels for L2 with additional 100 channels for
161 laser shut off to measure zero-light level. The laser frequency tuning rates are measured by a
162 germanium etalon, and fitted with a cubic spline function. The absorption cell is an astigmatic
163 multipass cell with 76 m effective pathlength with 32 cm base length, and an approximately 500
164 mL cell volume. The detector is a thermoelectrically-cooled photoconductive (HgCdTe)
165 detector. A spectral baseline was determined by filling the absorption cell with nitrogen (UHP

166 grade) at a pressure 50% higher than the CH₄ sample pressure to compensate for the higher index
167 of refraction of CH₄ compared to N₂. The cell temperature was monitored by a 30 kΩ thermistor,
168 and the pressure was measured by a capacitance manometer (10 torr full scale, MKS, Andover,
169 MA).

170 Significant efforts were made towards dampening temperature fluctuations to minimize the
171 temperature dependence of line strengths as well as to improve the stability of the optical train.
172 The optic housing is thermally insulated and temperature regulated at 295 K with air-liquid heat
173 exchangers and cooling water supplied by a recirculating chiller. The temperature stability of the
174 absorption cell is typically within 10 to 20 mK despite up to 2 K fluctuations in the laboratory air
175 temperature. The number density of each isotopologue is estimated at a rate of 1 Hz by a least-
176 square spectral fit assuming Voigt line profile, taking into account the temperature and pressure
177 inside the absorption cell (Figure 2).

178

179 **Gas Inlet System**

180 A gas inlet system was constructed to introduce sample CH₄ at a controlled pressure (Figure
181 3). TILDAS is commonly used to measure samples in a flow-through system for continuous
182 measurements. In this study, however, the CH₄ sample was introduced into a pre-evacuated
183 absorption cell by expansion and then isolated for absorption measurements. The leak rate of the
184 absorption cell is 0.01 torr/hour, which is negligible for the duration of analysis for a pair of
185 sample and reference measurement (ca. 12 minutes; Figure S-1).

186 The inlet system is constructed with twenty pneumatically-operated high-purity diaphragm or
187 bellow-sealed valves (DP or BK series, Swagelok, OH), a mass flow controller (Aalborg, NY),
188 two capacitance manometers (250 torr full scale, MKS, Andover, MA), two adjustable bellows

189 volumes, and a scroll pump (SH-110, Agilent). These components are controlled via custom-
190 built software routines implemented in LabVIEW (National Instruments). Sample CH₄ (5 to 10
191 mL STP) is introduced into the two separate adjustable bellows volumes (Metal Flex, Newport,
192 VT). The internal volume of the bellows can be adjusted between 50 mL and 490 mL using a
193 linear actuator, allowing the CH₄ pressure to be controlled to within ± 0.1 torr. A portion of
194 sample methane can be introduced into the laser cell by expanding it into the expansion volume
195 V1 (ca. 10 mL) (Figure 3).

196 Each measurement cycle (ca. 12 min) consists of the following sequence of events (Figure S-
197 1). First, baseline measurements are taken, during which UHP nitrogen is supplied from a mass
198 flow controller and flushed through the absorption cell. This is followed by pumping down the
199 cell using a turbomolecular pump. Sample CH₄ is introduced to the expansion volume (V1), and
200 then to the absorption cell at a pressure of 0.80 ± 0.006 (2σ) torr (0.53 mL STP or 22 μ mol).
201 After measurement of the sample CH₄, the cell is flushed with nitrogen, and evacuated. Then,
202 reference CH₄ is introduced into the absorption cell. The measurement cycles (baseline, sample,
203 reference) are repeated 5 to 10 times (time per cycle is 12 minutes). The bellows are compressed
204 after each measurement cycle to maintain the same sample pressure. The typical standard
205 deviation on $\Delta^{13}\text{CH}_3\text{D}$ for each cycle is 0.6 ‰ (2σ). Thus, the standard error of the mean
206 approaches 0.2 to 0.3 ‰ (2SEM) after 5 to 10 measurement cycles (Table S-1).

207 **Results**

208 **Line Parameters and Spectrum Analysis**

209 HITRAN line parameters for measured absorption lines are listed in Table 1. All target
210 isotopologue lines were found at expected transition frequencies (Figure 2). According to the

211 HITRAN database, the target $^{13}\text{CH}_3\text{D}$ line (ν_6 $A_1(4,4) \leftarrow A_2(3,3)$ and $A_2(4,4) \leftarrow A_1(3,3)$) is split
212 by 0.002 cm^{-1} . However, we found that the best spectral fit was obtained by assuming no
213 splitting, consistent with recent spectroscopy measurements.³¹ A spectrum was also taken with
214 synthesized $^{13}\text{CH}_3\text{D}$ at a cell pressure below 0.01 torr (estimated to be ca. 0.6 mtorr from the
215 absorption spectrum). The TILDAS spectrum showed a line shape corresponding to a single
216 Doppler line, suggesting that these two lines are nearly degenerate (Figure S-2).

217 Measured spectra were fit to a Voigt profile, from which the number density of each
218 isotopologue was estimated. The Voigt profile is a convolution of Gaussian and Lorentzian
219 functions, which arise from Doppler and pressure line broadenings, respectively. TILDAS
220 spectra were taken at CH_4 pressures between 0.4 and 2.1 torr CH_4 , in order to characterize
221 broadening line widths at different pressures. Gaussian and Lorentzian line widths were derived
222 from a least square fit applied for each pressure (Figure S-3). From this analysis, line widths
223 were parameterized as linear functions of pressure^{32,33}:

$$224 \quad \Gamma_G = \Gamma_D (1 + \gamma_{Dicke}) \times p\text{CH}_4 \quad (5)$$

$$225 \quad \Gamma_L = \gamma_P \times p\text{CH}_4 \quad (6)$$

226 where Γ_G and Γ_L are Gaussian and Lorentzian line widths, respectively, and Γ_D is the Doppler
227 line width without Dicke narrowing contribution. The terms, γ_{Dicke} and γ_P , account for the Dicke
228 narrowing and pressure broadening effects, respectively. At the CH_4 pressure used for
229 measurements (ca. 0.8 torr), the Voigt line width is largely due to Doppler broadening (1.8×10^{-3}
230 cm^{-1} , HWHM) with minor contributions from pressure broadening (10^{-4} cm^{-1}) for the main $^{12}\text{CH}_4$
231 line. The laser line width was estimated to be between 1×10^{-4} and $3 \times 10^{-4}\text{ cm}^{-1}$. Using the fit
232 parameters in Table 1, the typical fit residual is less than $\pm 0.02\%$ across measured spectral
233 regions (Figure 2). The derived pressure broadening factors (γ_P) are higher than HITRAN

234 values, part of which may be due to underestimated laser line widths or due to uncertainty in
235 laser tuning rates.

236

237 **Instrument Stability and Measurement Cycles**

238 To test the stability of the instrument, number densities of CH₄ isotopologues were monitored
239 continuously for over 6 hours at a cell CH₄ pressure of 0.8 torr. Allan variance analysis of the
240 data indicates one second Allan deviations of 0.30, 0.25 and 1.3‰ for δ¹³CH₄, δ¹²CH₃D, and
241 δ¹³CH₃D, respectively (Figure 4). White noise dominates the Allan variance up to 120 seconds
242 integration time but system drift becomes significant over timespans longer than 1000 seconds.
243 Ultimate precisions, down to 0.03, 0.04, and 0.2‰, for δ¹³CH₄, δ¹²CH₃D, and δ¹³CH₃D,
244 respectively, can be approached by 120 seconds signal averaging. This analysis indicates the
245 optimum measurement sequence to be longer than 120 seconds signal integration time but less
246 than 1000 seconds (16.6 min) for sample versus reference measurement cycles. Measurement
247 cycle for samples was designed based on the Allan variance analysis (Figure S-1).

248

249 **Heated Methane Calibration**

250 Standard reference materials with known ¹³CH₃D abundances do not yet exist. Therefore, in
251 order to calibrate the ¹³CH₃D isotopologue scale for TILDAS, a series of experiments were
252 carried out to produce CH₄ isotopologues by thermal equilibration (i.e., reaction 1) using a
253 conventional flame-seal tube technique.^{21,37}

254 A series of methane isotopologue mixtures were produced by the addition of pure
255 isotopologues to natural isotopologue abundance methane (AL1 and AL2). These mixtures
256 include one with ¹³CH₃D spike (Δ¹³CH₃D = 36.8 ‰, AL2-D3), and four (AL1-D2, AL1-D3,

257 AL2-D4, and AL1-D5) with a range of δD values from -628.6 to 273.3 ‰ (Table S-1). Aliquots
258 of these methane mixtures (ca. 8 to 10 mL STP) were condensed in quartz or pyrex tubes
259 containing silica gel and platinum catalyst (Platinum on alumina, Sigma Aldrich) at -196°C.
260 Prior to loading, the silica gel and platinum catalysts were baked at 300°C under vacuum for 1
261 hour to dehydrate, and then heated by a torch to activate the platinum catalyst (PtO₂ decomposes
262 to Pt above 400 °C under vacuum³⁸). These tubes were flame-sealed and heated in an oven at
263 temperatures between 200 and 400 °C (± 4 °C) for days to weeks (Table S-1).

264 Time Series Experiment

265 As a proof of concept, non-equilibrium isotopologue abundance methane ($\Delta^{13}\text{CH}_3\text{D}$ of +36.9
266 ‰, AL2-D3, Table S-1) was produced by adding synthesized ¹³CH₃D to natural-abundance
267 methane cylinder gas (Table S-1). A series of flame sealed tubes were prepared with the
268 isotopologue labeled methane and heated at 200°C. The tubes were quenched between 5 and 19
269 days, and the resulting methane was distilled at -196°C and analyzed by TILDAS. The large
270 positive $\Delta^{13}\text{CH}_3\text{D}$ signal disappeared after 8 days (at *e*-folding time of 0.52 day), and reached a
271 value of 0.08 ± 0.15 ‰ after 19 days (Figure 5). Ideally, the isotope exchange reaction does not
272 change the bulk isotopologue ratios (amount of the ¹³CH₃D spike is minor compared to ¹³CH₄ and
273 ¹²CH₃D). As expected, the value of $\delta^{13}\text{C}$ stayed nearly constant ($+0.11 \pm 0.03$ ‰) but the δD
274 value decreased by 21 to 23 ‰, suggesting that some chemical reaction did occur (Table S-1).
275 This is confirmed by gas chromatography analysis, which indicated the presence of H₂ and CO₂
276 in the heated methane samples. Hydrogen was likely formed from decomposition of methane to
277 H₂ and graphite; the oxygen in CO₂ may have come from PtO₂ film or residual water on silica gel
278 or Pt catalyst. The rapid disappearance of the $\Delta^{13}\text{CH}_3\text{D}$ signal indicates that the isotope

279 exchange reaction, however, occurred at a faster rate than the decomposition, consistent with
280 observations by Stolper et al. (2014).²¹

281

282 **δD Bracketing Experiment**

283 The δD values of natural methane samples can vary from -500 to -50‰.¹⁰ One of the major
284 challenges for accurate measurements of $\Delta^{13}\text{CH}_3\text{D}$ value is defining the linearity of the
285 instrument over a wide range of δD values. For example, if there is a very weak $^{12}\text{CH}_4$ absorption
286 line under $^{12}\text{CH}_3\text{D}$ that is not registered in the HITRAN database, the δD isotope scale will be
287 compressed (e.g., δD of -500‰ might be measured as -499‰). In order to test the linearity of
288 the instrument, isotopologue bracketing experiments were carried out following Stolper et al.
289 (2014)²¹ using a series of methane gases with δD values ranging from -629 to 263‰ (Figure 6;
290 Table S-1). Aliquots of these methane isotopologue mixtures were flame-sealed in quartz tubes
291 and heated at 400°C for one day or longer in the presence of Pt catalyst.

292 The $\Delta^{13}\text{CH}_3\text{D}$ values of these gases ranged from -1.60 to 0.11 ‰ after heating (Figure 6B).
293 The values of $\Delta^{13}\text{CH}_3\text{D}$ correlate with δD values with a least-squares fit of $\Delta^{13}\text{CH}_3\text{D} = -$
294 $0.0027 \cdot \delta\text{D} - 0.61$ (Figure 6B). From this correlation, a scale compression factor of 0.2% was
295 estimated (the difference between 0.0027 and 0.0020 is because the working standard, AL1, has
296 a non-zero δD value with respect to SMOW), and used to correct all the data. This suggests that
297 there could be a weak absorption line beneath $^{12}\text{CH}_3\text{D}$. A weak line with line strength $\sim 2 \times 10^{-27}$
298 cm/molecule (i.e., 0.2 % of $^{12}\text{CH}_3\text{D}$ line strength) would only produce a 0.01% signal in a fit
299 residual and would be difficult to detect (Figure 2). This “scale expansion correction” was
300 applied such that raw δD values (δD value with respect to reference gas AL1) were multiplied
301 by 1.002 to obtain the corrected δD values³⁹ (see SI). The corrected average $\Delta^{13}\text{CH}_3\text{D}$ value is -

302 0.88±0.66‰ (2σ) (Figure 6C), which is 0.3 ‰ higher than that measured for samples of the
303 laboratory working reference gas (AL1) that were heated to the same temperature (400°C). The
304 accuracy for Δ¹³CH₃D value is estimated to be 0.66‰ (2σ), and is limited by uncertainty in
305 measurements on heated methane samples used for the calibration.

306 It is unclear if this apparent bias of 0.3‰ is due to spectroscopic artifacts from TILDAS,
307 experimental procedures for thermal equilibrium experiments, or sample preparation steps. For
308 experiments with highly D-enriched (AL1-D3) or depleted (AL2-D4) starting methane, the δD
309 value changed from 273‰ down to 88‰ (AL1-D3) or from -629 to -379‰ (AL2-D4), clearly
310 indicating some chemical reactions occurred in addition to the isotope exchange. Experiments
311 run at 400°C yielded more H₂ and H₂O/CO₂ (both ca. 2 % of initial CH₄) compared to those run at
312 200°C experiments that yielded ca. 1% CO₂/H₂O of CH₄ without H₂, as estimated from pressure
313 during sample handling. These chemical reactions (e.g., decomposition of CH₄ to H₂ and
314 graphite) may be responsible for the bias for Δ¹³CH₃D. Stolper et al. (2014)²¹ reported that
315 sample introduction fractionated their Δ¹³CH₃D value by 0.49‰ when molecular sieve adsorbent
316 was not heated to 150 °C during desorption. A similar isotope fractionation due to incomplete
317 desorption from silica gel may also explain some scatter in the data. Potential isotope
318 fractionation during sample handling procedures is currently under investigation.

319

320 **Methane isotopologue temperature calibration**

321 A series of experiments was carried out to equilibrate reference methane (AL1) at temperatures
322 between 200 and 400 °C, and to compare with theoretical estimates (Figure 7, Table S-1).
323 Methane equilibrated at 200, 300 and 400°C yielded Δ¹³CH₃D (with respect to unheated AL1)
324 values of 0.14±0.15, -0.71±0.14, and -1.23±0.39 ‰ (2SEM), indicating that reference gas AL1

325 (commercial UHP grade methane) has $\Delta^{13}\text{CH}_3\text{D}$ value of $+2.29\pm 0.15$ ‰ with respect to a
326 stochastic $^{13}\text{CH}_3\text{D}$ abundance. Thus, our working standard gas, AL1, has an apparent $^{13}\text{CH}_3\text{D}$
327 isotopic temperature of $212\pm 10^\circ\text{C}$.

328

329 Methane Isotopologue temperatures of cylinder gas and natural gas

330 Methane from commercially-available cylinders of high-purity methane (AL1, AS1, and AS2)
331 and from a natural gas tap at MIT (“house gas”) were measured using TILDAS. Results of these
332 measurements are shown in Table 2. The three cylinders of methane and the house natural gas
333 yield $\delta^{13}\text{C}$ values ranging from -33.6 to -42.4 ‰ (with respect to VPDB), δD values between $-$
334 127 and -161 ‰ (with respect to VSMOW), and $\Delta^{13}\text{CH}_3\text{D}$ values of 2.3 to 3.0 ‰ (with respect to
335 the stochastic distribution). The values for $\delta^{13}\text{C}$ and δD are within the typical range for methane
336 in natural gas from thermogenic sources.¹⁰ The derived $\Delta^{13}\text{CH}_3\text{D}$ temperature ranges from 151
337 to 212°C , consistent with the temperature range within which thermogenic methane is thought to
338 be generated (the “gas window”). Repeated measurements on two in-house cylinder gasses, AS1
339 and AS2, with respect to a working standard gas (AL1) yield precisions (2σ reproducibility) for
340 $\Delta^{13}\text{CH}_3\text{D}$ of 0.17 ‰ ($n=7$) and 0.08 ‰ ($n=5$), respectively (Table 2).

341

Conclusions

342 We have developed a method to precisely determine the relative abundance of a doubly-
343 isotope substituted isotopologue of methane, $^{13}\text{CH}_3\text{D}$, by measuring the mid-infrared absorption
344 spectrum at 8.6 μm using a TILDAS instrument. A sample gas inlet system was developed for
345 the TILDAS, with which a precision of 0.2 ‰ (2σ) and an accuracy of 0.7 ‰ (2σ) were achieved
346 for the measurement of $\Delta^{13}\text{CH}_3\text{D}$ values. Current accuracy is limited by the calibration of

347 $\Delta^{13}\text{CH}_3\text{D}$ values against a series of thermally-isotopologue-equilibrated methane samples with a
348 range of δD (and $\delta^{13}\text{C}$) values. Future studies will include the development of a robust heating
349 and sample transfer protocol as well as further analysis of spectral features including a potential
350 interfering absorption line beneath the $^{12}\text{CH}_3\text{D}$ line. Large quantities of sample (ca. 10 mL STP
351 or 420 μmol methane) were used in this study, although samples as small as 0.5 mL STP
352 ($=21\mu\text{mol}$) can be analyzed at precisions of $\pm 0.6\%$ (2σ). Commercially-available cylinders of
353 high-purity methane and natural gas from an in-house tap have $^{13}\text{CH}_3\text{D}$ temperatures between
354 150 and 210 $^\circ\text{C}$, consistent with their inferred thermogenic origin. TILDAS instruments are
355 compact, consume little power compared to high-resolution mass-spectrometers,²¹ and offer a
356 simple and fully resolved measurement of the doubly substituted methane isotopologue, $^{13}\text{CH}_3\text{D}$,
357 at natural-abundance levels. The excellent precision attained for $^{13}\text{CH}_4$, and for $^{12}\text{CH}_3\text{D}$ of
358 0.04‰ by the TILDAS instrument opens up the possibility to apply this technique to high
359 precision analysis of other multiply substituted isotopologues and multiple isotope systems (e.g.,
360 $^{43}\text{C}^{16}\text{O}^{18}\text{O}$, $^{12}\text{C}^{16}\text{O}^{17}\text{O}$, $^{14}\text{N}^{15}\text{N}^{18}\text{O}$, $^{33}\text{SO}_2$, and $^{36}\text{SO}_2$).

361

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373 reviewers for constructive comments.

374 **Supporting Information Available.** Additional information as noted in text. This information
375 is available free of charge via the Internet at <http://pubs.acs.org/>.
376

377 **References**

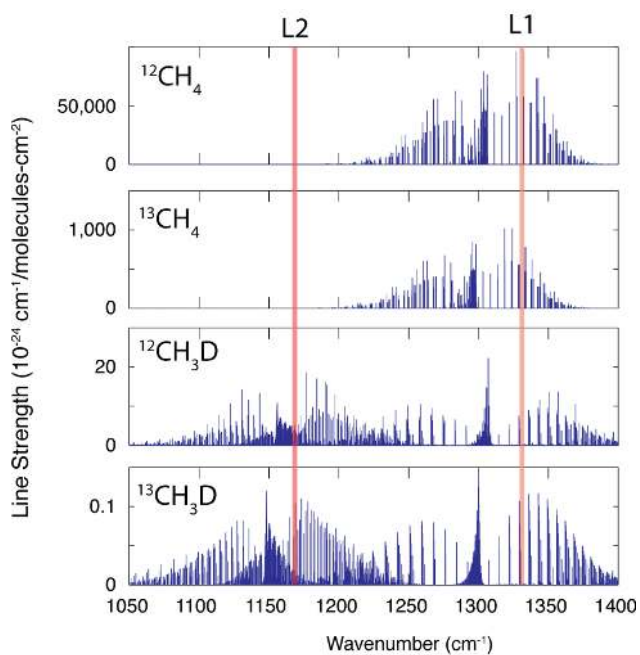
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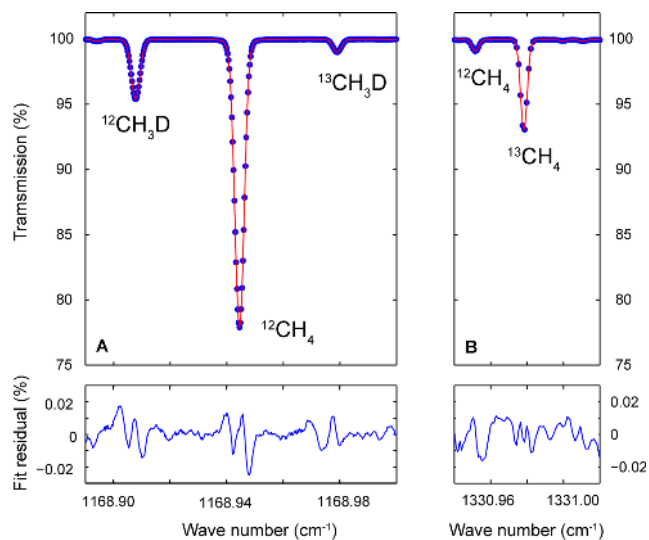
457 **Figure 1.** Absorption line positions and strength for four major isotopologues of methane from

458 HITRAN database. Shaded area indicates the spectral windows accessed by two QCL lasers (L1

459 and L2).

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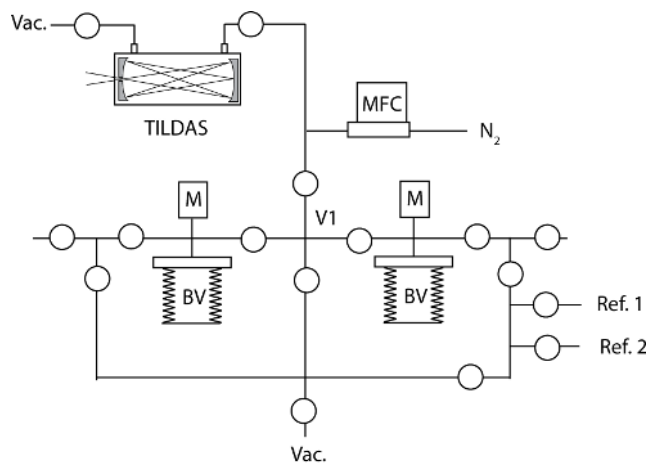
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Figure 2. TILDAS Spectrum and fit residual. Left panel (A) is for L2 and right (B) is for L1. Absorption cell is filled with 0.8 torr methane. Blue points are measurements and red lines are spectral fit.

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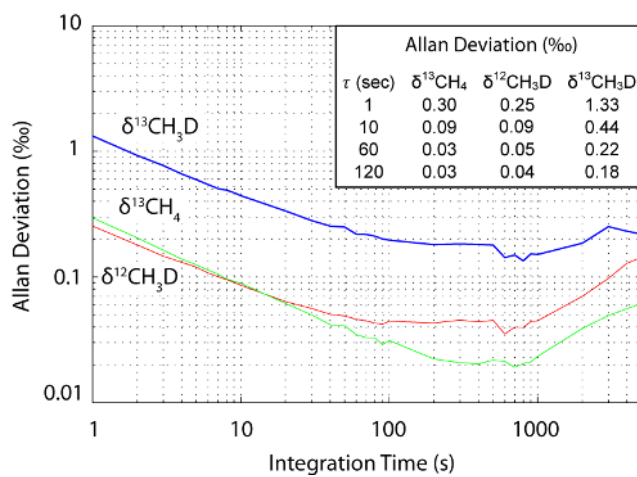
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478 **Figure 3.** Sample Inlet System constructed for TILDAS instrument. Open Circles are high purity
479 vacuum valves, M: pressure manometer, BV: adjustable bellow volume. MFC: mass flow
480 controller.

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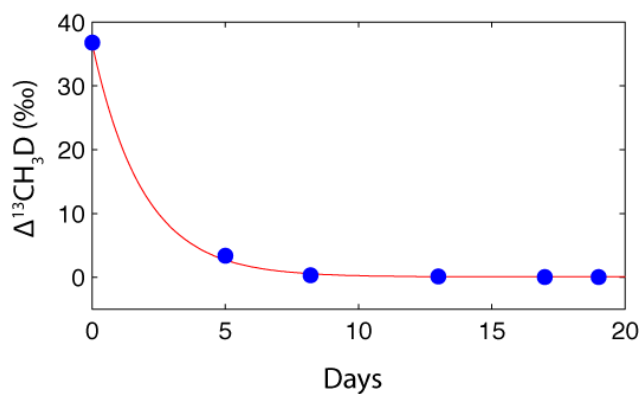
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485 **Figure 4.** Allan deviation plot for 0.8 torr CH_4 in the laser cell.

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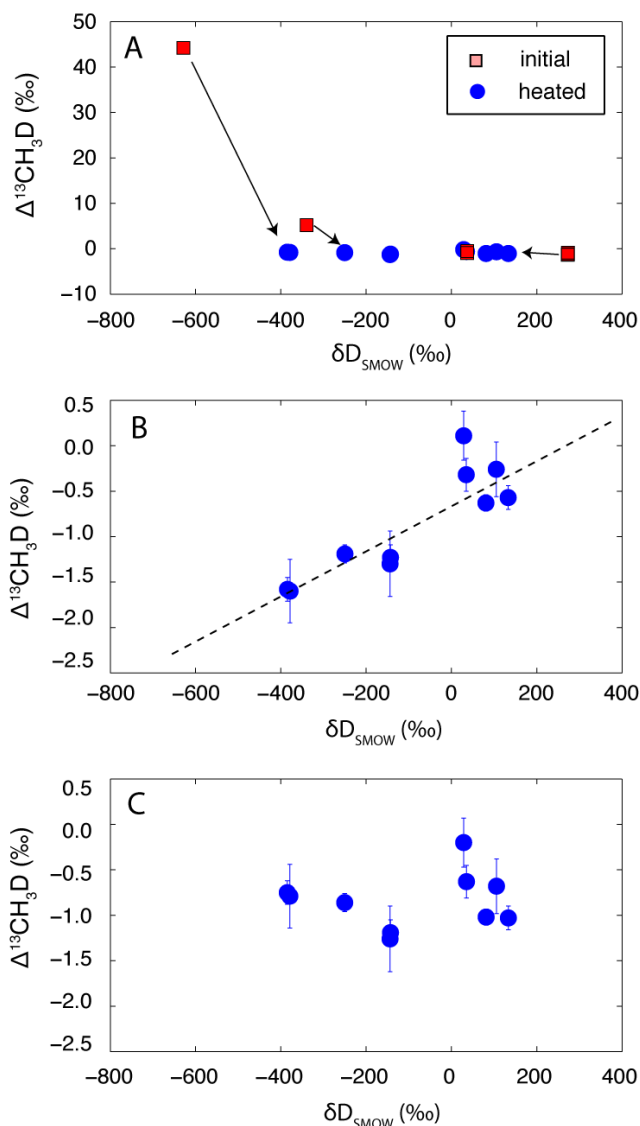
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493 **Figure 5.** Result of time-series experiment, showing the change of $\Delta^{13}\text{CH}_3\text{D}$ values for $^{13}\text{CH}_3\text{D}$
494 spiked methane (AL2-D3) that is thermally processed at 200°C (Table S-1). Line is a model fit
495 assuming first order kinetics with e -folding time of 0.52 days.

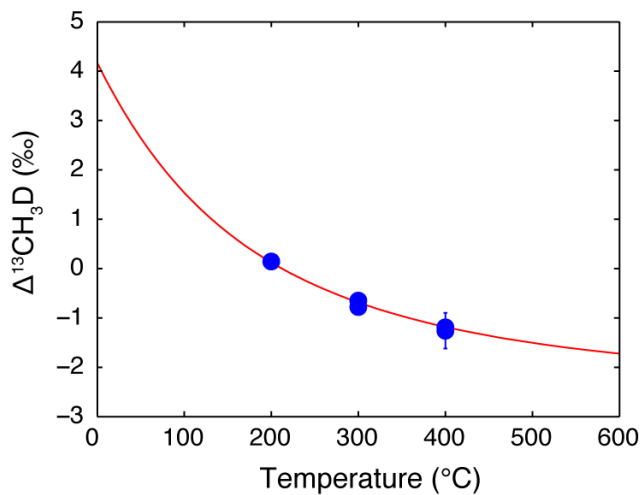
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 499 **Figure 6.** Result of δD bracketing experiments. A) $\Delta^{13}\text{CH}_3\text{D}$ and δD values for initial methane
 500 (square) and heated (circle) methane at 400°C . B) raw results without δD scale correction.
 501 Dashed line is a least square fit ($\Delta^{13}\text{CH}_3\text{D} = -0.0027 \times \delta\text{D} - 0.61$ ‰). C) after δD scale expansion
 502 correction of 1.002. The average $\Delta^{13}\text{CH}_3\text{D}$ value is -0.84 ± 0.33 ‰ (1σ). See Supporting
 503 Information for the definition and normalization of δD values.

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512 **Figure 7.** $\Delta^{13}\text{CH}_3\text{D}$ values for methane (working standard gas AL1) thermally equilibrated
513 between 200 and 400 °C. The values of $\Delta^{13}\text{CH}_3\text{D}$ are with respect to unheated AL1. The solid
514 line is a theoretical estimate, assuming $\Delta^{13}\text{CH}_3\text{D}$ value of reference AL1 is -2.29 ‰ against
515 stochastic distribution.

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523 **Table 1.** Parameters for absorption lines selected for this study. Line position, strength, lower
 524 state energy is from HITRAN database. Also shown is the temperature dependence of
 525 absorption strength ($d\delta/dT$).

	Frequency (cm^{-1})	Strength ($\text{cm}/\text{molecule}$)	Lower State Energy (cm^{-1})	γ_P ($\text{cm}^{-1}\text{atm}^{-1}$)		γ_{Dicke} (atm^{-1})	$d\delta/dT$ (%/10mK)
				HITRAN	This study		
$^{12}\text{CH}_4$	1168.9466	4.45E-24	470.79	0.073	0.101	-11.4	0.08
$^{13}\text{CH}_4$	1330.9787	1.72E-24	1554.10	0.075	0.091	-9.8	0.25
$^{12}\text{CH}_3\text{D}$	1168.9099	1.01E-24	861.04	0.071	0.080	-12.4	0.14
$^{13}\text{CH}_3\text{D}$	1168.9812*	2.09E-25	58.87	0.081	0.126	-25.7	0.01

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527 *In the HITRAN database, this line is split into 1168.98118 and 1168.98325 cm^{-1} .

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534 **Table 2.** Isotopologue compositions for laboratory cylinder methane (AL1, AS1 and AS2). The
 535 numbers in bold italic letters for AL1 indicate IRMS data, which is used to define $\delta^{13}\text{C}$ and δD
 536 of the TILDAS instrument. 2σ represents $2\times$ standard deviation for repeated measurements
 537 (n , in parentheses).

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	$\delta^{13}\text{C}_{\text{PDB}}$	2σ	$\delta\text{D}_{\text{SMOW}}$	2σ	$\Delta^{13}\text{CH}_3\text{D}^{*1}$	2σ	Temperature ($^{\circ}\text{C}$)	2σ
Cylinder Methane								
AL1	-34.5	0.5	-127	5	2.29	0.10	212	-10/+11
AS1 (7)	-42.40	0.09	-161.07	0.07	2.79	0.17	167	-13/+14
AS2 (5)	-38.6	0.14	-133.5	0.04	2.49	0.08	193	-8/+7
House Natural Gas								
house gas (4)	-33.6	0.16	-140.7	0.16	3.00	0.54	151	-35/+44

540 *1: $\Delta^{13}\text{CH}_3\text{D}$ is with respect to stochastic (infinite-temperature) distribution.

541

Supporting Information for

“Measurement of Doubly-Substituted Methane Isotopologue, $^{13}\text{CH}_3\text{D}$, by Tunable Infrared Laser Direct Absorption Spectroscopy “

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Supporting information includes:

- 1) Detailed protocol for synthesis of methane isotopologues.
- 2) Detailed definition and derivation of $\Delta^{13}\text{CH}_3\text{D}$, $\delta^{13}\text{C}$ and δD values, and theoretical estimate of the equilibrium constant (K) of isotope exchange reaction (1), and
- 3) Three figures (Figure S-1, S-2 and S-3) and one Table (Table S-1), which are mentioned in the main text.

1. Synthesis of Methane Isotopologues

The clumped methane isotopologue, $^{13}\text{CH}_3\text{D}$, was synthesized by the Grignard reaction. The Grignard reagent was synthesized from ^{13}C -iodomethane (1.2 mL, $^{13}\text{CH}_3\text{I}$, 99 atom % from Sigma Aldrich) and magnesium (0.5 g) in diethyl ether (9 mL) under helium flow, refluxing with a dry ice condenser, by the reaction:



Deuterium oxide (0.7 mL, 99.96 atom %D, Cambridge Isotope Laboratory) was added dropwise to produce $^{13}\text{CH}_3\text{D}$:



The product $^{13}\text{CH}_3\text{D}$ was adsorbed on a trap filled with activated charcoal immersed in liquid nitrogen. After the reaction, the carrier helium gas was pumped out and methane was desorbed from the trap. Mass-spectrometer analysis showed better than 99% purity. Similarly, CH_3D (with natural-abundance ^{13}C) was synthesized from iodomethane and D_2O .

D-depleted methane was synthesized from aluminum carbide (Al_4C_3 , natural C isotope abundance) and D-depleted water (D content 2-3 ppm) via the reaction:



Reaction (S3) readily proceeds at 80 °C. The product CH_4 was distilled at -110 °C. Gas chromatography analysis showed better than 99% purity with trace quantities of CO_2 .

2. Definition and derivation of $\Delta^{13}\text{CH}_3\text{D}$, $\delta^{13}\text{C}$ and δD values, and theoretical estimate of the equilibrium constant (K)

The equilibrium constant (K) of the isotope exchange reaction among four isotopologues of methane:



was estimated by conventional theories of stable isotope fractionation.¹⁻³ Fundamental frequencies for $^{12}\text{CH}_4$ were taken from experimental values,⁴ and the frequency shifts for three isotopologues ($^{13}\text{CH}_4$, $^{12}\text{CH}_3\text{D}$, and $^{13}\text{CH}_3\text{D}$) relative to $^{12}\text{CH}_4$ were estimated using molecular dynamics simulation at HF/6-31G* basis set.

The temperature dependence of the equilibrium constant can be approximated as:

$$\ln(K) = -5.256 \times 10^{-1} \text{ T}^{-1} + 1.0126 \times 10^3 \times \text{ T}^{-2} - 1.0579 \times 10^5 \times \text{ T}^{-3} \quad (\text{S5}).$$

Previous study has shown that different levels of theory yield similar results.² Total partition function sums can also be calculated from spectroscopic data for each isotopologues.^{5,6} Partition function sum of $^{12}\text{CH}_4$ and $^{13}\text{CH}_4$ from Fischer et al. (2003) and $^{12}\text{CH}_3\text{D}$ and $^{13}\text{CH}_3\text{D}$ from Laraia et al. (2011), however, yield $K = 1.0009$ at 296K, as opposed to 1.0057 derived by our model. The main reason could be due to the fundamental vibrational frequencies for $^{13}\text{CH}_3\text{D}$ used by Laraia et al. (2011).

Our definition of the $\Delta^{13}\text{CH}_3\text{D}$ value

$$\Delta^{13}\text{CH}_3\text{D} = \ln(K) = \ln \frac{[^{13}\text{CH}_3\text{D}]}{[^{12}\text{CH}_3\text{D}]} - \ln \frac{[^{13}\text{CH}_4]}{[^{12}\text{CH}_4]} \quad (\text{S6}).$$

yields practically identical value to that defined by Stolper et al. (2014)³ that referenced against “stochastic $^{13}\text{CH}_3\text{D}$ abundance”, which is estimated from $^{13}\text{CH}_4$ and $^{12}\text{CH}_3\text{D}$. This is because,

$$\begin{aligned} \Delta^{13}\text{CH}_3\text{D} &\equiv \ln \frac{[^{13}\text{CH}_3\text{D}]}{[^{12}\text{CH}_3\text{D}]} - \ln \frac{[^{13}\text{CH}_4]}{[^{12}\text{CH}_4]} = \ln \frac{[^{13}\text{CH}_3\text{D}]}{[^{12}\text{CH}_3\text{D}]} \frac{[^{12}\text{CH}_3\text{D}]}{[^{12}\text{CH}_4]} - \ln \frac{[^{13}\text{CH}_4]}{[^{12}\text{CH}_4]} \frac{[^{12}\text{CH}_3\text{D}]}{[^{12}\text{CH}_4]} \\ &\approx \ln \left(\frac{^{13}\text{CH}_3\text{D}}{^{12}\text{CH}_4} \right)_{\text{measured}} - \ln \left(\frac{^{13}\text{CH}_3\text{D}}{^{12}\text{CH}_4} \right)_{\text{stochastic}} \\ &= \ln \left(\frac{\left(\frac{^{13}\text{CH}_3\text{D}}{^{12}\text{CH}_4} \right)_{\text{measured}}}{\left(\frac{^{13}\text{CH}_3\text{D}}{^{12}\text{CH}_4} \right)_{\text{stochastic}}} \right) \end{aligned}$$

$$\approx \frac{\left(\frac{^{13}\text{CH}_3\text{D}}{^{12}\text{CH}_4}\right)_{\text{measured}}}{\left(\frac{^{13}\text{CH}_3\text{D}}{^{12}\text{CH}_4}\right)_{\text{stochastic}}} - 1 \quad (\text{S7}).$$

In practice, $\Delta^{13}\text{CH}_3\text{D}$ values are measured by comparing those of samples to laboratory working reference gas:

$$\Delta^{13}\text{CH}_3\text{D}_{\text{sample}} = \ln \frac{^{13}R_{\text{sample}}}{^{13}R_{\text{reference}}} - \ln \frac{^{13}r_{\text{sample}}}{^{13}r_{\text{reference}}} - \Delta^{13}\text{CH}_3\text{D}_{\text{reference}} \quad (\text{S8})$$

where, $^{13}R = ^{13}\text{CH}_3\text{D}/^{12}\text{CH}_3\text{D}$ and $^{13}r = ^{13}\text{CH}_4/^{12}\text{CH}_4$ of sample and working reference CH_4 . Equation (S8) shows that there will be a constant offset to account for the non-zero $\Delta^{13}\text{CH}_3\text{D}$ value of the working reference gas. This value can be determined by calibrating against methane equilibrated at a range of known temperatures. For our reference gas (AL1) the $\Delta^{13}\text{CH}_3\text{D}_{\text{reference}}$ value was estimated to be $-2.29 \pm 0.1 \text{ ‰}$ (Figure 7).

The apparent systematic relationship between δD and $\Delta^{13}\text{CH}_3\text{D}$ for bracketing experiments suggests unaccounted weak absorption line underneath $^{12}\text{CH}_3\text{D}$. If the hidden absorption line is due to $^{12}\text{CH}_4$, correction for this will be analogous to abundance sensitivity correction for isotope ratio-mass spectrometer due to tailing of the main isotopologue line onto minor isotopologue.⁷ The absorption of the unaccounted line is estimated to be 0.01 ‰ such that it may not be detected from the fit residual (Figure 2). The isotope delta scale will contract due to constant bias both for reference and sample isotopologue ratios. Following Ono et al. (2006)⁷, when signal size for sample and reference is balanced, the correction is:

$$\delta\text{D}_{\text{corrected}} = (1+b) \delta\text{D}_{\text{measured}} \quad (\text{S9})$$

where the value b describes the relative contribution of $^{12}\text{CH}_4$ onto $^{12}\text{CH}_3\text{D}$ ($b=0.002$ is our best estimate), δD values in equation (S9) are with respect to working reference gas (AL1). The equation (S9) was used to correct δD values from which the ratio $^{12}\text{CH}_3\text{D}/^{12}\text{CH}_4$ is derived, and

then used to correct $\Delta^{13}\text{CH}_3\text{D}$ values. The magnitude of the correction is less than 0.8 ‰ when $\delta\text{D}_{\text{SMOW}}$ is between -500‰ and 250 ‰.

Delta values in this study are reported with respect to PDB (Pee Dee Belemnite) and SMOW (Standard Mean Ocean Water). For isotopologue ratios, these are:

$$\delta^{13}\text{C} = \frac{(^{13}\text{CH}_4/^{12}\text{CH}_4)_{\text{sample}}}{(^{13}\text{C}/^{12}\text{C})_{\text{PDB}}} - 1 \quad , \quad (\text{S10})$$

and

$$\delta\text{D} = \frac{(^{12}\text{CH}_3\text{D}/^{12}\text{CH}_4)_{\text{sample}}}{4 \cdot (\text{D}/\text{H})_{\text{SMOW}}} - 1 \quad (\text{S11})$$

Factor four in equation (S11) reflects four H atoms in CH_4 . These delta values are derived by comparison with laboratory reference gas (AL1), which has $\delta^{13}\text{C}$ and δD of $-34.5 \pm 0.5\text{‰}$ and $-127 \pm 5\text{‰}$ (2σ), respectively, as measured by GC-IRMS at the University of Toronto (Table 2). These uncertainties include analytical precision and overall accuracy.

Reference in Supporting Information

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- (4) Shimanouchi. *Tables of molecular vibrational frequencies Consolidated Volume I*; National Bureau of Standards, 1972, p 1--160.
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- (7) Ono, S.; Wing, B.; Rumble, D.; Farquhar, J. *Chemical Geology* **2006**, 225, 30-39.

3. Supporting figures and a table

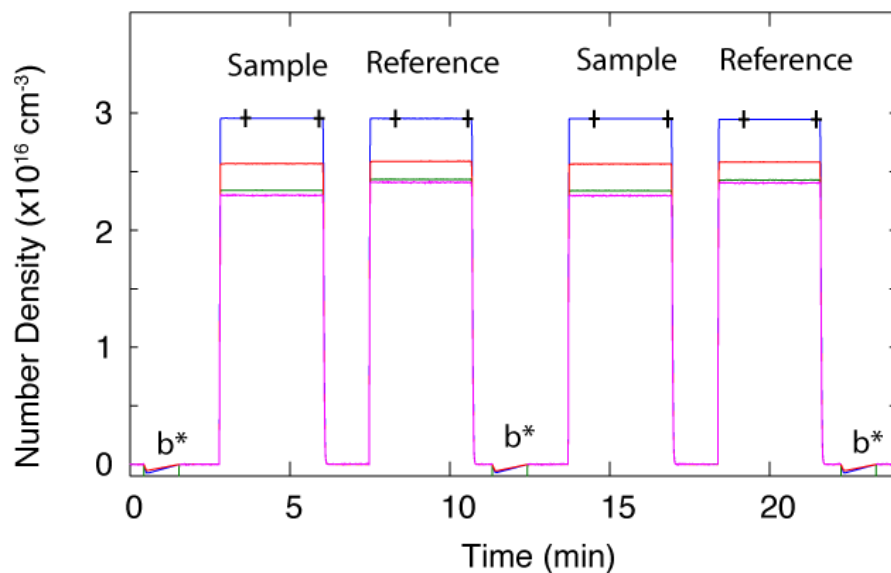


Figure S-1. Example of measurement cycles. Each line shows the number density as a function of time (blue ¹³CH₄, red, ¹²CH₄, green ¹²CH₃D, and purple, ¹³CH₃D). Signals were averaged between two crosses. Each measurement cycle consists of baseline calibration (marked as b*, 60 seconds), and measurements of sample and reference (190 seconds each). Number density for minor isotopologues was divided by its fractional abundance used by HITRAN database.

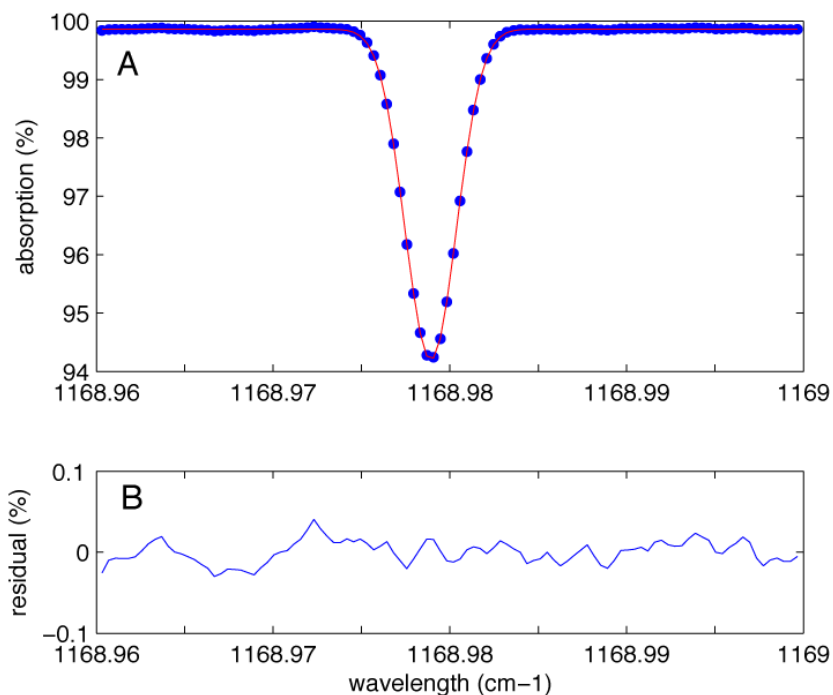


Figure S-2. TILDAS spectrum for pure $^{13}\text{CH}_3\text{D}$ (measurements in blue points, and fit in red line) (A), and residual for spectrum fitting. Best fit was obtained with single absorption line with Doppler line width of 0.001688 cm^{-1} (0.001696 cm^{-1} is theoretical value). Cell pressure is less than 1 mbar.

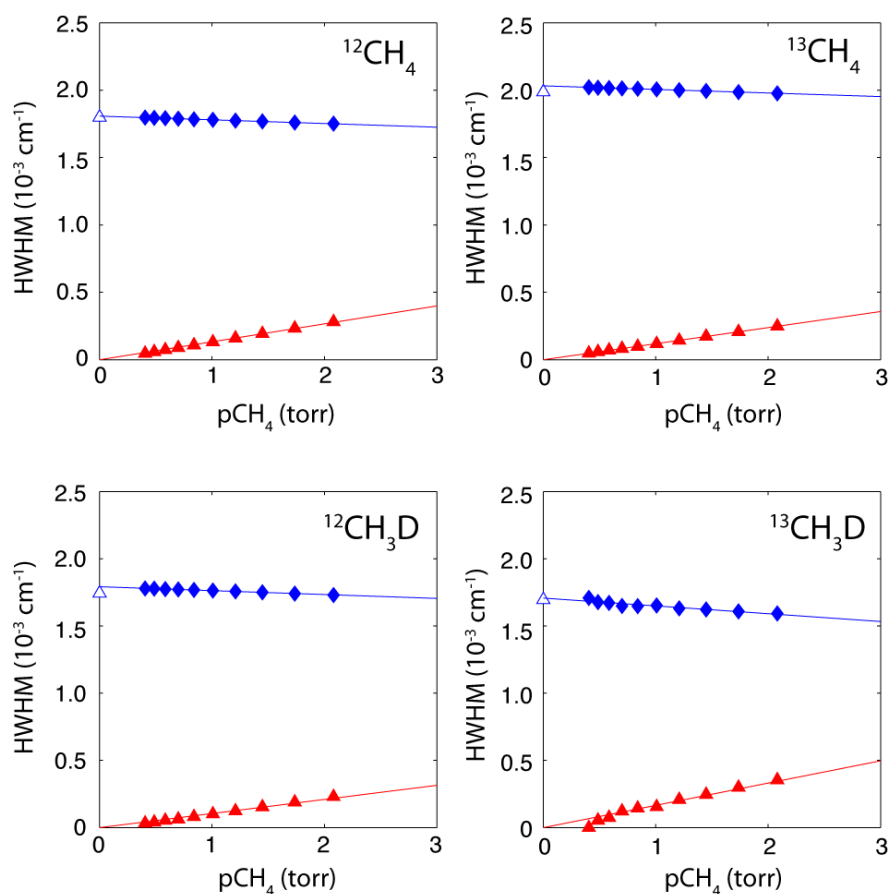


Figure S-3. Line width parameters derived from least square fit of absorption lines between 0.4 to 2.1 torr CH_4 . The spectrum was deconvoluted to Gaussian (filled diamond) and Lorentzian components (solid triangle). Also shown is the expected Doppler line width (open triangle).

Table S-1. Results for heated methane experiments.

CH ₄ source	T (°C)	Duration (days)	$\delta^{13}\text{C}_{\text{PDB}}$	2SEM* ¹	$\delta\text{D}_{\text{SMOW}}$ ^{*2}	2SEM* ¹	$\Delta^{13}\text{CH}_3\text{D}$ ^{*2}	2SEM* ¹
Time Series Experiment								
AL2-D3	initial		-39.01	0.02	-133.69	0.02	36.77	0.20
AL2-D3	initial		-39.01	0.02	-133.72	0.05	36.97	0.20
AL2-D3	200	5.0	-38.93	0.01	-152.45	0.03	3.48	0.10
AL2-D3	200	8.2	-38.86	0.03	-155.31	0.02	0.46	0.28
AL2-D3	200	13.0	-38.90	0.01	-155.84	0.05	0.21	0.20
AL2-D3	200	17.0	-38.87	0.02	-154.83	0.03	0.12	0.15
AL2-D3	200	19.0	-38.92	0.02	-157.10	0.03	0.08	0.15
Thermal Equilibrium Experiment								
AL1	200	11	-34.29	0.01	-146.83	0.01	0.14	0.09
AL1	200	20	-34.58	0.04	-143.70	0.03	0.14	0.12
AL1	300	12	-34.51	0.01	-147.64	0.02	-0.65	0.07
AL1	300	20	-34.63	0.02	-153.94	0.03	-0.78	0.12
AL1	400	2	-34.96	0.02	-143.82	0.08	-1.26	0.36
AL1	400	6	-34.93	0.02	-142.92	0.04	-1.19	0.14
δD Bracketing Experiment								
AL1-D2	initial		-34.53	0.02	36.75	0.04	-0.95	0.18
AL1-D2	initial		-34.47	0.03	36.96	0.01	-0.52	0.15
AL1-D2	400	1	-34.51	0.02	35.23	0.07	-0.63	0.18
AL1-D2	400	16	-34.50	0.03	28.75	0.04	-0.20	0.27
AL1-D3	initial		-34.53	0.02	272.88	0.03	-1.34	0.20
AL1-D3	initial		-34.51	0.01	273.36	0.03	-0.88	0.16
AL1-D3	initial		-34.50	0.02	273.42	0.05	-1.21	0.15
AL1-D3	400	1	-34.53	0.03	105.82	0.05	-0.68	0.30
AL1-D3	400	17	-34.97	0.02	133.59	0.03	-1.03	0.13
AL1-D3	400	9	-34.50	0.02	81.39	0.03	-1.02	0.09
AL1-D5	initial		-40.31	0.03	-339.65	0.04	5.19	0.18
AL1-D5	400	14	-38.99	0.02	-250.33	0.03	-0.86	0.10
AL2-D4	initial		-50.48	0.02	-628.62	0.05	44.22	0.23
AL2-D4	400	2	-45.50	0.01	-385.07	0.03	-0.75	0.13
AL2-D4	400	4	-45.64	0.24	-378.91	0.26	-0.79	0.35

*1: Standard error of the mean (SEM) is estimated from standard deviation from 10 to 14 measurement cycles.

*2: Reported δD and $\Delta^{13}\text{CH}_3\text{D}$ value includes scale expansion factor of 1.002 for δD . $\Delta^{13}\text{CH}_3\text{D}$ value is with respect to reference gas AL1 (i.e., subtraction of 2.29 ‰ yields the $\Delta^{13}\text{CH}_3\text{D}$ value with respect to stochastic distribution).