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## Measurement of $C P$ asymmetries in $B^{0} \rightarrow \phi K^{0}$ and $B^{0} \rightarrow K^{+} K^{-} K_{s}^{\mathbf{0}}$ decays

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## (BABAR Collaboration)

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#### Abstract

We measure the time-dependent $C P$ asymmetry parameters in $B^{0} \rightarrow K^{+} K^{-} K^{0}$ based on a data sample of approximately $227 \times 10^{6} B$-meson pairs recorded at the $\Upsilon(4 S)$ resonance with the $B A B A R$ detector at the PEP-II $B$-meson Factory at SLAC. We reconstruct two-body $B^{0}$ decays to $\phi(1020) K_{S}^{0}$ and $\phi(1020) K_{L}^{0}$, and the three-body decay $K^{+} K^{-} K_{S}^{0}$ with $\phi(1020) K_{S}^{0}$ excluded. For the $B^{0} \rightarrow \phi K^{0}$ decays, we measure $\sin 2 \beta_{\text {eff }}\left(\phi K^{0}\right)=+0.50 \pm 0.25(\text { stat })_{-0.04}^{+0.07}($ syst $)$. The $B^{0} \rightarrow K^{+} K^{-} K_{S}^{0}$ decays are dominated by $K^{+} K^{-} S$ wave, as determined from an angular analysis; we measure $\sin 2 \beta_{\text {eff }}\left(K^{+} K^{-} K_{S}^{0}\right)=+0.55 \pm 0.22$ (stat) $\pm$ 0.04 (syst) $\pm 0.11(C P)$, where the last error is due to the uncertainty in the fraction of $C P$-even contributions to the decay amplitude. We find no evidence for direct $C P$ violation.


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In the standard model (SM) of particle physics, the decays $B^{0} \rightarrow K^{+} K^{-} K^{0}$ [1] are dominated by $b \rightarrow s \bar{s} s$ gluonic penguin amplitudes, but can also be affected by amplitudes that are suppressed by elements of the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [2]. These CKM-suppressed amplitudes cannot be precisely known in a model-independent way [3], but are in general expected to be small [4]. Let $2 \beta_{\text {eff }}$ be the $C P$-violating phase difference between decays with and without mixing, and $\beta=\arg \left(-V_{c d} V_{c b}^{*} / V_{t d} V_{t b}^{*}\right)$ where $V_{i j}$ are elements of the CKM quark mixing matrix. The difference $\left|\beta-\beta_{\text {eff }}\right|$ is expected to be nearly zero, with theoretical uncertainties of a few degrees for $B^{0} \rightarrow \phi K^{0}$ [5]. Larger uncertainties exist for $B^{0} \rightarrow K^{+} K^{-} K_{S}^{0}$ with $B^{0} \rightarrow$ $\phi K_{S}^{0}$ decays excluded, due in part to an extra CKMsuppressed tree amplitude contribution [4].

Since additional decay diagrams with non-SM particles and interactions introducing new $C P$-violating phases may contribute to $\beta_{\text {eff }}$, measurements of $\sin 2 \beta_{\text {eff }}$ in these channels and their comparisons with the SM expectation are sensitive probes for physics beyond the SM [4]. The value of $\sin 2 \beta$ has been measured in $B^{0} \rightarrow J / \psi K_{S}^{0}[6,7]$ with an average of $0.742 \pm 0.037$. The $B A B A R$ and Belle collaborations have measured $\sin 2 \beta_{\text {eff }}$ in $\phi K^{0}[+0.47 \pm$ $0.34_{-0.06}^{+0.08}$ with $114 \times 10^{6} B \bar{B}$ pairs [8] and $-0.96 \pm$ $0.50_{-0.11}^{+0.09}$ with $152 \times 10^{6} B \bar{B}$ pairs ( $\phi K_{S}^{0}$ only) [9], respectively], and in $K^{+} K^{-} K_{S}^{0}$ excluding $\phi K_{S}^{0}(+0.57 \pm$ $0.26 \pm 0.04_{-0.00}^{+0.17}$ with $122 \times 10^{6} B \bar{B}$ pairs [10] and $+0.51 \pm 0.26 \pm 0.05_{-0.00}^{+0.18}$ with $152 \times 10^{6} B \bar{B}$ pairs [9], respectively).

At $B$ factories, the neutral $B$ mesons are exclusively produced in pairs. We select events for which one $B$ ( $B_{\text {rec }}$ ) is reconstructed as $B^{0} \rightarrow K^{+} K^{-} K^{0}$ and the other ( $B_{\mathrm{tag}}$ ) is partially reconstructed as either $B^{0}$ or $\bar{B}^{0}$. We define $\Delta t=t_{\text {rec }}-t_{\text {tag }}$ to be the difference between the proper decay times of the $B$ mesons. The decay rate $\mathrm{f}_{+}\left(\mathrm{f}_{-}\right)$for the final state $f$ when the $B_{\text {tag }}$ decays as a $B^{0}$ ( $\bar{B}^{0}$ ) is given by

$$
\begin{align*}
\mathrm{f}_{ \pm}(\Delta t)= & \frac{\mathrm{e}^{-|\Delta t|} / \tau_{B^{0}}}{4 \tau_{B^{0}}}\left[1 \pm S_{f} \sin \left(\Delta m_{d} \Delta t\right)\right. \\
& \left.\mp C_{f} \cos \left(\Delta m_{d} \Delta t\right)\right] \tag{1}
\end{align*}
$$

where $\tau_{B^{0}}$ is the $B^{0}$ lifetime and $\Delta m_{d}$ is the $B^{0}-\bar{B}^{0}$ mixing
frequency. The parameter $S_{f}$ is nonzero if there is $C P$ violation in the interference between decays with and without mixing, while a nonzero value for $C_{f}$ would entail direct $C P$ violation. In the limit where the CKMsuppressed amplitudes do not contribute, the SM predicts no direct $C P$ violation ( $C_{f}=0$ ) since the dominant decay amplitudes have the same $C P$-violating phase, and that $S_{f}=-\eta_{f} \times \sin 2 \beta_{\text {eff }}$. For $B^{0} \rightarrow \phi K_{S}^{0}$ decays, the effective eigenvalue $\eta_{f}=-1$; for $B^{0} \rightarrow \phi K_{L}^{0} \eta_{f}=+1$. For $B^{0} \rightarrow K^{+} K^{-} K_{S}^{0}$ decays, $\eta_{f}=2 f_{\text {even }}-1$, where $f_{\text {even }}$ is the fraction of $C P$-even contributions to the $B^{0} \rightarrow$ $K^{+} K^{-} K_{S}^{0}$ amplitude. Then the value of $\eta_{f}$ depends on the angular momentum of the $K^{+} K^{-}$system: it is -1 for relative $P$ wave and +1 for $S$ wave.

In this paper, we present a measurement of $\sin 2 \beta_{\text {eff }}$ with almost twice the number of events as for the previous $B A B A R$ results $[8,10]$. We reconstruct $B^{0}$ candidates in two independent modes, $\phi K^{0}$ (with the $K^{0}$ either a $K_{L}^{0}$ or a $K_{S}^{0}$ ) and $K^{+} K^{-} K_{S}^{0}$ (with the $\phi$ mass region excluded). $K_{S}^{0}$ 's are detected via their $\pi^{+} \pi^{-}$decay only. We extract the $C P$ asymmetry parameters using extended maximumlikelihood fits. Using an angular moment analysis [11], we extract the $K^{+} K^{-} P$-wave fractions in the data. These fractions are used to check the assumption that $\eta_{f}=-1$ for $\phi K_{S}^{0}$ and +1 for $\phi K_{L}^{0}$ by bounding the $S$-wave contamination in the $\phi$ mass region, and to measure $\eta_{f}$ for $K^{+} K^{-} K_{S}^{0}$.

This analysis is based on $227 \times 10^{6} B \bar{B}$ pairs collected with the $B A B A R$ detector [12] at the PEP-II asymmetricenergy $e^{+} e^{-}$storage rings at SLAC, operating at the $\Upsilon(4 S)$ resonance [center-of-mass (c.m.) energy $\sqrt{s}=$ $10.58 \mathrm{GeV}]$. In Ref. [12] we describe the silicon vertex tracker (SVT) and drift chamber (DCH) used for track and vertex reconstruction, the electromagnetic calorimeter (EMC) and instrumented flux return (IFR) used for $K_{L}^{0}$ reconstruction, and the detector of internally reflected Cherenkov light (DIRC), which, together with the EMC, the IFR, and the ionization $d E / d x$ from the SVT and DCH , is used for particle identification.

The $B^{0}$-candidate reconstruction and selection is similar to that described in Refs. [8,10]. We consider a $K^{+} K^{-}$pair to be a $\phi$ candidate if its invariant mass is within $15 \mathrm{MeV} / c^{2}$ (about 3 times the apparent width in the

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$K^{+} K^{-}$invariant mass spectrum) of the central $\phi$ mass value [13]. For a given $B^{0} \bar{B}^{0}$ meson pair, we obtain $\Delta t$ from the measured distance between the fully reconstructed $B_{\text {rec }}$ meson decay point and the $B_{\text {tag }}$ decay point along the beam direction, and the known boost of the $\mathrm{Y}(4 S)$ system $(\beta \gamma=0.56)$. A multivariate tagging algorithm determines the flavor of the $B_{\text {tag }}$ meson [6] and classifies it in one of seven mutually exclusive tagging categories.

We use two kinematic variables to discriminate between signal $B$ decays and combinatorial background. The energy difference between the measured $e^{+} e^{-}$c.m. energy of the $B$ candidate and $\sqrt{s} / 2$ is $\Delta E$. Its distribution peaks at zero for signal, with a width of about 20 MeV for $\phi K_{S}^{0}$ and $K^{+} K^{-} K_{S}^{0}$. The width is only about 3 MeV for $\phi K_{L}^{0}$, because for this mode we constrain the $B^{0}$ candidate's mass to the nominal value [13]. The beam-energysubstituted mass, $m_{\mathrm{ES}}$, is used for candidates without a $K_{L}^{0}$. It is defined as $m_{\mathrm{ES}} \equiv \sqrt{\left(s / 2+\mathbf{p}_{i} \cdot \mathbf{p}_{B}\right)^{2} / E_{i}^{2}-\mathbf{p}_{B}^{2}}$, where the $B$ momentum $\mathbf{p}_{B}$ and the four-momentum of the initial state ( $E_{i}, \mathbf{p}_{i}$ ) are defined in the laboratory frame. It peaks at the $B^{0}$ mass for signal, with a width of about 3 MeV . For $\phi K_{S}^{0}$ candidates, we require $|\Delta E|<100 \mathrm{MeV}$ and $m_{\mathrm{ES}}>5.21 \mathrm{GeV} / c^{2}$; for $\phi K_{L}^{0}$ candidates, we require $|\Delta E|<80 \mathrm{MeV}$; and for $K^{+} K^{-} K_{S}^{0}$ candidates, we require $|\Delta E|<200 \mathrm{MeV}$ and $m_{\mathrm{ES}}>5.2 \mathrm{GeV} / c^{2}$.

The dominant background is continuum $e^{+} e^{-} \rightarrow q \bar{q}$ ( $q=u, d, s, c$ ) events; these tend to be jetlike in the $e^{+} e^{-}$c.m. frame, while $B$ decays tend to be spherical. To enhance discrimination between signal and continuum, we use Fisher discriminants $(\mathcal{F})$ to combine four event-shape-related variables $[8,10]$. The other background originates from $B$ decays. For the $\phi K^{0}$ final state, opposite- $C P$ contributions from the $K^{+} K^{-} K^{0}$ final state ( $K^{+} K^{-} S$ wave) are estimated from data with a moment analysis [11] (see below) to be less than $6.6 \%$ at $95 \%$ confidence level. The mode $\phi K_{L}^{0}$ has additional background. Its dominant $C P$ contamination is from the mode $\phi K^{* 0} \rightarrow \phi K_{L}^{0} \pi^{0}$, for which we expect approximately eight events in the region $|\Delta E|<10 \mathrm{MeV}$. In the final likelihood fit we explicitly parametrize backgrounds from $B$ decays both with and without charm.

For the $K^{+} K^{-} K_{S}^{0}$ mode, we apply invariant mass cuts to suppress background from $B$ decays that proceed through a $b \rightarrow c$ transition, namely, those containing $D^{0}, J / \psi, \chi_{c 0}$, or $\psi(2 S)$ decaying into $K^{+} K^{-}$, or $D^{+}$or $D_{s}^{+}$decaying into $K^{+} K_{S}^{0}$. Finally, to suppress $B$ decays into final states with pions, we require the rate for a charged pion to be misidentified as a kaon to be less than $2 \%$.

A total of 4300,8238 , and 27368 events have a candidate that passes the $\phi K_{S}^{0}, \phi K_{L}^{0}$, or $K^{+} K^{-} K_{S}^{0}$ selection criteria, respectively. From simulation, we find the final selection efficiencies for signal to be $40 \%, 20 \%$, and $26 \%$, respectively.

We extract the $K^{+} K^{-} K_{S}^{0}, \phi K_{S}^{0}$, and $\phi K_{L}^{0}$ event yields and $C P$ parameters with two extended maximumlikelihood fits. One is to the $K^{+} K^{-} K_{S}^{0}$ candidates; the other is to both the $\phi K_{S}^{0}$ and $\phi K_{L}^{0}$ candidates, with the assumption that $C_{\phi K_{s}^{0}}=C_{\phi K_{L}^{0}}$ and $S_{\phi K_{s}^{0}}=-S_{\phi K_{L}^{0}}$. We verified the fit procedure for the $\phi K^{0}$ mode with samples of $\phi K^{+}$ and $J / \psi K^{0}$ events. We found for the former a null asymmetry as expected, and for the latter results that are consistent with previous measurements [6]. We verified the fit procedure for the $K^{+} K^{-} K_{S}^{0}$ mode with a sample of $K_{S}^{0} K_{S}^{0} K^{+}$events, for which we found a null asymmetry as expected.

The likelihood function used in each extended maximum-likelihood fit to its $N_{k}$ candidates tagged in category $k$ is

$$
\begin{equation*}
\mathcal{L}_{k}=e^{-N_{k}^{\prime}} \prod_{i=1}^{N_{k}}\left\{N_{S} \epsilon_{k} \mathcal{P}_{i, k}^{S}+N_{C, k} \mathcal{P}_{i, k}^{C}+\sum_{j=1}^{n_{B}} N_{B, j} \epsilon_{j, k} \mathcal{P}_{i, j, k}^{B}\right\} \tag{2}
\end{equation*}
$$

where $N_{k}^{\prime}$ is the sum of the signal, continuum, and $n_{B}$ $B$-background yields tagged in category $k ; N_{S}$ is the number of $\phi K_{S}^{0}, \phi K_{L}^{0}$, or $K^{+} K^{-} K_{S}^{0}$ signal events; $\epsilon_{k}$ is the fraction of signal events tagged in category $k ; N_{C, k}$ is the number of continuum background events tagged in category $k ; N_{B, j}$ is the number of $B$-background events of class $j$; and $\epsilon_{j, k}$ is the fraction of $B$-background events of class $j$ tagged in category $k$. Each $B$-background class comprises similar $B$ decays. The $B$-background event yields are fixed parameters and are zero for the $\phi K_{S}^{0}$ sample. The total likelihood $\mathcal{L}$ is the product of the likelihoods for each tagging category.

The probability density functions (PDFs) $\mathcal{P}_{k}^{S}, \mathcal{P}_{k}^{C}$, and $\mathcal{P}_{j, k}^{B}$, for signal, continuum background, and $B$-background class $j$, respectively, are the products of the PDFs of the discriminating variables. The signal PDF is thus given for the $K^{+} K^{-} K_{S}^{0}$ sample by $\mathcal{P}\left(m_{\mathrm{ES}}\right) \cdot \mathcal{P}(\Delta E) \cdot \mathcal{P}(\mathcal{F})$. $\mathcal{P}\left(\Delta t ; \sigma_{\Delta t}\right)$, for the $\phi K_{S}^{0}$ sample by $\mathcal{P}\left(m_{\mathrm{ES}}\right) \cdot \mathcal{P}(\Delta E)$. $\mathcal{P}(\mathcal{F}) \cdot \mathcal{P}\left(m_{K K}\right) \cdot \mathcal{P}\left(\cos \theta_{H}\right) \cdot \mathcal{P}\left(\Delta t ; \sigma_{\Delta t}\right)$, and for the $\phi K_{L}^{0}$ sample by $\mathcal{P}(\Delta E) \cdot \mathcal{P}(\mathcal{F}) \cdot \mathcal{P}\left(m_{K K}\right) \cdot \mathcal{P}\left(\cos \theta_{H}\right)$. $\mathcal{P}\left(\Delta t ; \sigma_{\Delta t}\right)$, where $\theta_{H}$ is the angle between the $K^{+}$candidate and the parent $B_{\text {rec }}$ flight direction in the $K^{+} K^{-}$rest frame. The quantity $\sigma_{\Delta t}$ is the uncertainty in the measurement of $\Delta t$ for a given event. The time-dependent $C P$ parameters defined in Eq. (1), diluted by the effects of mistagging and the $\Delta t$ resolution, are contained in $\mathcal{P}_{k}^{S}\left(\Delta t, \sigma_{\Delta t}\right)$. As in our $J / \psi K_{S}^{0}$ analysis [6], the $\Delta t$-resolution function for signal and $B$-background events is a sum of three Gaussian distributions, which have two distinct means as well as three distinct widths. The widths are the error of the measured $\Delta t$ scaled by three independent factors.

In the fits to data, we leave unconstrained the parameters describing the $C P$ asymmetry, the $\Delta t$-resolution functions, the tagging characteristics, and the event yields. We also
leave unconstrained the means of the signal $m_{\mathrm{ES}}$ and $\Delta E$ Gaussian PDFs, the widths of the signal $\Delta E$ PDFs, the mean of the signal $m_{K K} \mathrm{PDF}$ (which is parametrized by a relativistic $P$-wave Breit-Wigner function), and all parameters of the $K^{+} K^{-} K_{S}^{0}$ candidates' signal PDF for $\mathcal{F}$. We take from simulation any other parameters of the $m_{\mathrm{ES}}$, $\Delta E, \mathcal{F}, \cos \theta_{H}$, and $m_{K K}$ PDFs for signal and $B$ background. The parameters describing the signal and $B$-background $\Delta t$-resolution function are determined by a simultaneous fit to an independent sample of reconstructed $B^{0}$ decays to flavor eigenstates, with more than 100000 events [6]. We use the world-averaged values for $\tau_{B^{0}}$ and $\Delta m_{d}$ [13]. The fits to the $\phi K^{0}$ and $K^{+} K^{-} K_{S}^{0}$ candidates have a total of 35 and 34 free parameters, respectively.

We use an angular moment analysis based on the $\cos \theta_{H}$ distribution to extract the $K^{+} K^{-} K_{S}^{0} C P$ content, and also to bound the $S$-wave contamination in the $\phi$ mass region. In this approach, we expand the decay distribution for a given $K^{+} K^{-}$invariant mass in terms of moments $\left\langle P_{\ell}\right\rangle$ of conveniently normalized Legendre polynomials $P_{\ell}\left(\cos \theta_{H}\right)$ :

$$
\begin{equation*}
\left|\mathcal{A}\left(m_{K K}\right)\right|^{2}=\sum_{\ell}\left\langle P_{\ell}\right\rangle \cdot P_{\ell}\left(\cos \theta_{H}\right), \tag{3}
\end{equation*}
$$

where $\mathcal{A}\left(m_{K K}\right)$ is the mass-dependent decay amplitude. We normalize $P_{\ell}\left(\cos \theta_{H}\right)$ such that the integral of $P_{\ell}\left(\cos \theta_{H}\right)^{2}$ over $\cos \theta_{H}$ from -1 to 1 equals unity. We extract the moments by summing over all events:

$$
\begin{equation*}
\left\langle P_{\ell}\right\rangle=\sum_{j} P_{\ell}\left(\cos \theta_{H, j}\right) \mathcal{W}_{j} / \varepsilon_{j}, \tag{4}
\end{equation*}
$$

where $\mathcal{W}_{j}$ is the weight for event $j$ to belong to the signal decay and is calculated by the sPlot technique of Ref. [14]. The efficiency $\varepsilon_{j}$ is evaluated from a large MC sample in bins of $m_{K K}$ and $\cos \theta_{H}$. Limiting ourselves to the two lowest partial waves, we can write the total decay amplitude in terms of the $S$-wave ( $C P$-even) and the $P$-wave ( $C P$-odd) amplitudes,

$$
\begin{align*}
\mathcal{A}\left(m_{K K}\right) \approx & \mathcal{A}_{S}\left(m_{K K}\right) P_{0}\left(\cos \theta_{H}\right) \\
& +e^{i \phi_{p}} \mathcal{A}_{P}\left(m_{K K}\right) P_{1}\left(\cos \theta_{H}\right) \tag{5}
\end{align*}
$$

where $\phi_{p}$ is the relative phase between the real partialwave amplitudes $\mathcal{A}_{S}\left(m_{K K}\right)$ and $\mathcal{A}_{P}\left(m_{K K}\right)$. If we compare Eq. (5) to Eq. (3), we can relate the moments (of order $\ell \leq$ 2) to the wave intensities and thus to the total fraction of $C P$-even events, $f_{\text {even }}$, as

$$
\begin{equation*}
f_{\mathrm{even}}=\frac{\mathcal{A}_{S}\left(m_{K K}\right)^{2}}{\mathcal{A}_{S}\left(m_{K K}\right)^{2}+\mathcal{A}_{P}\left(m_{K K}\right)^{2}}=1-\sqrt{\frac{5}{4}} \frac{\left\langle P_{2}\right\rangle}{\left\langle P_{0}\right\rangle} \tag{6}
\end{equation*}
$$

where $\mathcal{A}_{S}\left(m_{K K}\right)^{2}$ and $\mathcal{A}_{P}\left(m_{K K}\right)^{2}$ are the $S$ - and $P$-wave intensities, respectively. In the normalization, the total number of signal events is $\sqrt{2}\left\langle P_{0}\right\rangle$.

Systematic errors on the $C P$-asymmetry parameters are listed in Table I. We account for uncertainties in the $\Delta t$ resolution, the beam-spot position, and the detector alignment. We also estimate errors due to the effect of doubly

TABLE I. Systematic uncertainties on the $C P$ parameters.

| Source | $S_{\phi K}$ | $C_{\phi K}$ | $S_{K K K}$ | $C_{K K K}$ |
| :--- | :---: | :---: | :---: | :---: |
| Detector effects | $\pm 0.02$ | $\pm 0.02$ | $\pm 0.02$ | $\pm 0.01$ |
| DCSD | $\pm 0.01$ | $\pm 0.03$ | $\pm 0.00$ | $\pm 0.03$ |
| Fit bias | $\pm 0.01$ | $\pm 0.01$ | $\pm 0.02$ | $\pm 0.01$ |
| $B^{0}-\bar{B}^{0}$ tagging | $\pm 0.01$ | $\pm 0.02$ | $\pm 0.00$ | $\pm 0.01$ |
| $S$-wave contamination | +0.06 | $\pm 0.02$ | $\cdots$ | $\cdots$ |
| Other | $\pm 0.03$ | $\pm 0.02$ | $\pm 0.01$ | $\pm 0.01$ |
| Total | ${ }_{-0.04}^{+0.07}$ | $\pm 0.05$ | $\pm 0.03$ | $\pm 0.04$ |

CKM-suppressed decays (DCSD) of the $B_{\text {tag }}$ [15]. The uncertainty due to possible biases in the fit procedure is conservative and includes effects on the $C P$ parameters of correlations among the fit variables, which have been determined with full-detector MC simulations. Uncertainties in the $B^{0}-\bar{B}^{0}$ tagging efficiency in both signal and background are also included. Finally, we account for errors due to the $C P$ content of the background, uncertainties in the PDF parametrization, and the uncertainties of $\tau_{B^{0}}$ and $\Delta m_{d}$ [13]. For each mode we add the individual contributions in quadrature to obtain the total systematic uncertainty.

We also consider the systematic error due to the $C P$-even fraction of the $K^{+} K^{-} K_{S}^{0}$ mode. We do not find evidence for the existence of higher moments $\left\langle P_{\ell}\right\rangle$, $\ell=$ $3 \ldots 6$, which could arise from intermediate $D$-wave decays into $K^{+} K^{-}$or decays proceeding through an isospin-1 resonance into $K^{ \pm} K_{S}^{0}$. Nevertheless, we estimate a systematic error from the $D$ wave by examining the $\left\langle P_{2}\right\rangle$ moment in the $K^{+} K^{-}$mass region $(1.1-1.7) \mathrm{GeV} / c^{2}$, corresponding to the $f_{2}(1270), a_{2}(1320)^{0}$, and $f_{2}^{\prime}(1525)$ resonances, and assuming that $\left\langle P_{2}\right\rangle$ arises only from $D$ wave and $S-D$ interference. Since the moment itself is consistent with zero, we assign a systematic error of $4 \%$ based on the $\left\langle P_{2}\right\rangle$ error. We account for the possible presence of $a_{0}(980)^{+}, a_{0}(1450)^{+}$, and $a_{2}(1320)^{+}$in the $K^{ \pm} K_{S}^{0}$ subsys-

TABLE II. $\quad C P$-asymmetry parameters and yields from the final extended maximum-likelihood fits, as well as the fraction of $C P$-even contributions to the amplitude, $f_{\text {even }}$, which is assumed to be zero for $\phi K_{S}^{0}$ and unity $\phi K_{L}^{0}$. The first errors are statistical, and the second are systematic; the third error on $\sin 2 \beta_{\text {eff }}$ for $K^{+} K^{-} K_{S}^{0}$ is due to the uncertainty in the $C P$ content. The values of $S$ and $C$ are fit simultaneously for the $\phi K_{S}^{0}$ and $\phi K_{L}^{0}$ candidates; the sign of $S$ for $\phi K_{S}^{0}$ is shown. When finding $\sin 2 \beta_{\text {eff }}$ for $K^{+} K^{-} K_{S}^{0}$, we constrain $C_{K K K}$ to 0 .

| $\sin 2 \beta_{\text {eff }}$ | $$ | $\begin{gathered} K^{+} K^{-} K_{S}^{0} \\ \left(\text { no } \phi K_{S}^{0}\right) \\ +0.55 \pm 0.22 \pm 0.04 \pm 0.11 \end{gathered}$ |
| :---: | :---: | :---: |
| $f_{\text {even }}$ | 0 1 1 | $0.89 \pm 0.08 \pm 0.06$ |
| $S$ | $+0.50 \pm 0.25_{-0.04}^{+0.07}$ | $-0.42 \pm 0.17 \pm 0.03$ |
| C | $0.00 \pm 0.23 \pm 0.05$ | $+0.10 \pm 0.14 \pm 0.04$ |
| Yield | $114 \pm 12 \quad 98 \pm 18$ | $452 \pm 28$ |

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tem $(4.6 \%)$. We also estimate a bias due to the modeling of the efficiency from MC events $(2.5 \%)$. We find the total systematic error on $f_{\text {even }}$ to be $\pm 0.06$. This leads to a systematic error on $\sin 2 \beta_{\text {eff }}$ of $\pm 0.11$.

Table II shows the measured $C P$ parameters and yields from the final extended maximum-likelihood fits. Note that when fitting $\sin 2 \beta_{\text {eff }}$ for $K^{+} K^{-} K_{S}^{0}$, we constrain $C_{K K K}$ to zero. All yields are consistent with our previously measured branching fractions [10,16]. Figure 1 shows the signal-enhanced distributions of $m_{\mathrm{ES}}$ for $\phi K_{S}^{0}$ and $K^{+} K^{-} K_{S}^{0}$ events and of $\Delta E$ for $\phi K_{L}^{0}$ events, together with the result from the final extended maximumlikelihood fits. Figure 2 shows the time-dependent asymmetry distributions. As a cross check, we also fit $\phi K_{S}^{0}$ and


FIG. 1. Distributions of (a) $m_{\mathrm{ES}}$ for $\phi K_{S}^{0}$ candidates, (b) $\Delta E$ for $\phi K_{L}^{0}$ candidates, and (c) $m_{\mathrm{ES}}$ for $K^{+} K^{-} K_{S}^{0}$ candidates excluding $\phi K_{S}^{0}$, together with the results from the final extended maximum-likelihood fits after applying a requirement on the ratio of signal likelihood to signal-plus-background likelihood (computed without the displayed variable) to reduce the background. The requirement is chosen to roughly maximize $N_{S}^{2} /\left(N_{S}+N_{C}\right)$ where $N_{C}$ is the total number of continuum events, and is applied only for the purpose of making these plots. The curves are projections from the likelihood fits for total yield (solid lines), continuum background (short dashed lines), and total background [long dashes in (b) only]. The efficiency of the likelihood-ratio cut is (a) $79 \%$ for signal and $5 \%$ for background, (b) $35 \%$ for signal, $16 \%$ for $B$-background, and $3 \%$ for continuum background, and (c) $77 \%$ for signal and $5 \%$ for background.


FIG. 2. The time-dependent asymmetry distributions for (a) $\phi K_{S}^{0}$, (b) $\phi K_{L}^{0}$, and (c) $K^{+} K^{-} K_{S}^{0}$ with no $\phi K_{S}^{0}$ decays. The asymmetry is defined as $A_{B^{0} / \bar{B}^{0}}=\left(N_{B^{0}}-N_{\bar{B}^{0}}\right) /\left(N_{B^{0}}+\right.$ $\left.N_{\bar{B}^{0}}\right)$, where $N_{B^{0}}\left(N_{\bar{B}^{0}}\right)$ is the number of $B_{\text {tag }}$ mesons identified as a $B^{0}\left(\bar{B}^{0}\right)$ for a given measured value of $\Delta t$. The signal-tobackground ratio is enhanced with a cut on the likelihood ratio as in Fig. 1.


FIG. 3. Distributions of $S$ - and $P$-wave intensities and $C P$ even fraction as a function of $K^{+} K^{-}$invariant mass. Notice that the first bin integrates a wider mass range than the $\phi$ resonance occupies. Insets show $S$ - and $P$-wave intensities in the $\phi$ mass region.
$\phi K_{L}^{0}$ separately. Our fit to only $\phi K_{S}^{0}$ events gives $S=$ $0.29 \pm 0.31$ and $C=-0.07 \pm 0.27$. Our fit to only $\phi K_{L}^{0}$ events gives $S=1.05 \pm 0.51$ and $C=0.31 \pm 0.49$.

For the $K^{+} K^{-} K_{S}^{0}$ final state including the $\phi$ mass region, the distributions of the $S$ - and $P$-wave intensities, and the $C P$-even fraction, as a function of $K^{+} K^{-}$invariant mass, are shown in Fig. 3. The total fraction of $C P$-even events with the $\phi$ mass region excluded is given in Table II. We successfully verified our value of $f_{\text {even }}$ with a different method [17] that uses the event rates in $B^{+} \rightarrow K^{+} K_{S}^{0} K_{S}^{0}$ and the isospin-related channel $B^{0} \rightarrow K^{+} K^{-} K_{S}^{0}$.

To summarize, in a sample of $227 \times 10^{6} B \bar{B}$ meson pairs, we measure the $C P$ content and $C P$ parameters in $B^{0}$-meson decays into $\phi K^{0}$, and into $K^{+} K^{-} K_{S}^{0}$ with the $\phi$ mass region excluded. We determine the fraction of $C P$-even and $C P$-odd contributions with an angular analysis. In $B^{0} \rightarrow \phi K^{0}$, our values for $\sin 2 \beta_{\text {eff }}$ and $C_{\phi K}$ are in good agreement with our previously published values [8], and the small $S$-wave contamination is treated as a systematic uncertainty. In $B^{0} \rightarrow K^{+} K^{-} K_{S}^{0}$, the $K^{+} K^{-}$system is
observed to be dominated by $S$ wave; this, along with the measured value of $\sin 2 \beta_{\text {eff }}$, is consistent with previous measurements based on isospin symmetry [9,10]. Both of our $\sin 2 \beta_{\text {eff }}$ values are consistent to within 1 standard deviation with the value of $\sin 2 \beta$ measured in $B^{0} \rightarrow c \bar{c} s$ decays [6].

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[1] Throughout this paper, charge conjugate reactions are included implicitly.
[2] N. Cabibbo, Phys. Rev. Lett. 10, 531 (1963); M. Kobayashi and T. Maskawa, Prog. Theor. Phys. 49, 652 (1973).
[3] D. London and R.D. Peccei, Phys. Lett. B 223, 257 (1989); N. G. Deshpande and J. Trampetic, Phys. Rev. D 41, 895 (1990); R. Fleischer, Z. Phys. C 62, 81 (1994); N. G. Deshpande and X. G. He, Phys. Lett. B 336, 471 (1994); Y. Grossman, Z. Ligeti, Y. Nir, and H. Quinn, Phys. Rev. D 68, 015004 (2003); M. Gronau and J.L. Rosner, Phys. Lett. B 564, 90 (2003).
[4] A.B. Carter and A.I. Sanda, Phys. Rev. D 23, 1567 (1981); I. I. Bigi and A. I. Sanda, Nucl. Phys. B193, 85 (1981); R. Fleischer and T. Mannel, Phys. Lett. B 511, 240 (2001); Y. Grossman, G. Isidori, and M. P. Worah, Phys. Rev. D 58, 057504 (1998); Y. Grossman, Z. Ligeti, Y. Nir, and H. Quinn, Phys. Rev. D 68, 015004 (2003); Y. Grossman and M.P. Worah, Phys. Lett. B 395, 241 (1997); R. Fleischer, Int. J. Mod. Phys. A 12, 2459 (1997); D. London and A. Soni, Phys. Lett. B 407, 61 (1997).
[5] Throughout this paper, $\phi$ refers to the $\phi(1020)$.
[6] B. Aubert et al. (BABAR Collaboration), hep-ex/0408127 [Phys. Rev. Lett. (to be published)].
[7] K. Abe et al. (Belle Collaboration), Phys. Rev. D 71, 072003 (2005); 71, 079903(E) (2005).
[8] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 93, 071801 (2004).
[9] K. Abe et al. (Belle Collaboration), Phys. Rev. Lett. 91, 261602 (2003).
[10] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 93, 181805 (2004).
[11] G. Costa et al., Nucl. Phys. B175, 402 (1980); S. U. Chung, Phys. Rev. D 56, 7299 (1997).
[12] B. Aubert et al. (BABAR Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 479, 1 (2002).
[13] S. Eidelman et al. (Particle Data Group), Phys. Lett. B 592, 1 (2004).
[14] M. Pivk and F. R. Le Diberder, physics/0402083.
[15] O. Long, M. Baak, R. N. Cahn, and D. Kirkby, Phys. Rev. D 68, 034010 (2003).
[16] B. Aubert et al. (BABAR Collaboration), Phys. Rev. D 69, 011102 (2004).
[17] A. Garmash et al. (Belle Collaboration), Phys. Rev. D 69, 012001 (2004).


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