

Measurement of non-linear optical coefficients of chalcogenide glasses near the fundamental absorption band edge

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Abstract. A time-resolved pump-probe method is used for the evaluation of non-linear optical coefficients of chalcogenide glasses from the As-S-Se and Ge-Se systems near their fundamental absorption band edges. The results are analyzed via comparison with the spectral dependencies of the non-linear optical coefficients of crystalline semiconductors; the role of electron transitions through the gap states of chalcogenide glasses is discussed.

OCIS codes: (190.4400) Nonlinear optics, materials; (160.2750) Glass and other amorphous materials; (320.2250) Femtosecond phenomena

1. Introduction

The non-linear optical response of chalcogenide glasses has been studied experimentally for the past 20 years. It was found that non-linear optical coefficients concerning to the third-order non-linear polarization were 2-3 orders greater than those of fused silica. As the optical bandgap energy E_g of a chalcogenide glass composition is usually less than 2.5 eV [1] their fundamental absorption band (FAB) edges correspond to the bandgap wavelengths $\lambda_g > 0.5 \mu\text{m}$. In fact, non-linear optical coefficients of the glass systems As-S-Se, Ge-Se, Ga-La-S and others have been measured mainly at the wavelengths λ : 1.064 μm , 1.25 μm and 1.55 μm of available ultra-fast lasers [2]. At these wavelengths, the ratio $R_e = h\nu/E_g$ ($h\nu$ is the laser photon energy) is less than 0.6. Meanwhile, the range $0.6 < R_e < 1$ is of current interest in both fundamental and applied research.

In the technology of waveguides inscription in optical glasses, the non-linear coefficients of refraction and absorption are basic parameters, which govern a high-intensity laser pulse energy deposition into a glass sample and final refractive index variation. When illuminated in a spectral range near the FAB edge, chalcogenide glasses exhibit specific photo-structural changes known as photodarkening [1]. The character of the non-linear optical response in a chalcogenide glass sample depends on whether the sample has been illuminated near to or far from the FAB edge [3].

Up to now, a theory of the non-linear optical response of non-crystalline semiconductors, in particular, chalcogenide glasses, has not been developed. In the theory of crystalline semiconductors, a two-band model [2,4,5] is usually used to describe the third-order non-linear polarization. However, this model is incompatible with non-crystalline semiconductors that have energy levels in their bandgaps (so called gap states). Nevertheless the theory of crystalline semiconductors was used in some papers for evaluation of the non-linear optical coefficients of refraction n_2 and absorption β_2 of chalcogenide glasses [6-9]. (These coefficients correspond to the intensity-dependent parts of the refractive index $n = n_0 + n_2I$ and absorption coefficient $\alpha = \alpha_0 + \beta_2I$, where n_0 and α_0 are, respectively, the linear refractive index and single-photon absorption coefficient, and I is intensity of the laser radiation.) Far from the FAB edge, when $\lambda > \lambda_g$, comparison of the theoretical values with experimental data provides some fit [7], but there is a discrepancy near the FAB edge because in the theory of the direct-gap crystalline semiconductors, n_2 is negative-valued over some part of the spectral range ($R_e > 0.7$) [4]. Meanwhile in accordance with the available experimental data [2], only $n_2 > 0$ has hitherto been observed in all the range of transparency of chalcogenide glasses.

In experiments on n_2 and β_2 measurements near the FAB edge, densities of photo-excited charge carriers in a sample can be large due to the single- and two- photon absorption. This effect can significantly violence the output parameters especially when laser pulses of nano- or pico- second durations are used for pumping [10].

In this work, a time-resolved pump-probe method was applied to evaluate n_2 and β_2 of chalcogenide glasses from the As-S-Se and Ge-Se systems near their FAB edges. In the experiment, a single femtosecond (fs) pump pulse was used for a glass sample illumination at each probe pulse delay. To avoid a cumulative effect, the sample was moved after each shot. Together with a thorough analysis of the short time scale dynamics of the non-linear optical response, this enabled us to realize the experimental conditions when the photo-excited free electrons density is small and can be neglected in a numerical model used for n_2 and β_2 evaluation.

2. Experiment

Samples of the compositions $\text{As}_{40}\text{S}_x\text{Se}_{60-x}$ ($x = 0, 15, 30, 45, 60$) (atomic %) and $\text{Ge}_{20}\text{Se}_{80}$, $\text{Ge}_{12}\text{Se}_{88}$ were fabricated from synthesized glass rods, shaped as thin disks (thickness ~ 1 mm) and polished to a $0.25 \mu\text{m}$ finish [11]. The FAB edges in absorption spectra obtained from spectrophotometric measurements [11, 12] are shown in Figure 1. The linear part of each curve corresponds to the Urbach tail [1]. The weak absorption tails (WAT) typically refer to the range where $\alpha_0 < 1 \text{ cm}^{-1}$. These glass samples were illuminated by laser pulses (HMFWD duration $\tau = 50$ fs) with the peak wavelength $\lambda^p = 0.79 \mu\text{m}$ ($h\nu^p = 1.57 \text{ eV}$).

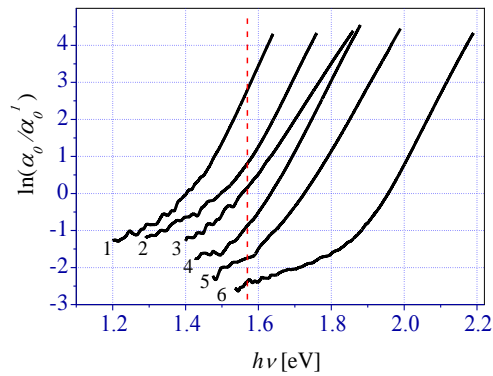


Figure 1. Logarithm of the absorption coefficient of the glass compositions $\text{As}_{40}\text{S}_x\text{Se}_{60-x}$, $x = 0$ (1), 15 (2), 30 (4), 45(5), 60 (6) and $\text{Ge}_{20}\text{Se}_{80}$ (3). The vertical dashed line indicates $h\nu^p = 1.57 \text{ eV}$. $\alpha_0^1 = 1 \text{ cm}^{-1}$

Fourier Transform interferometry [13] enabled us to measure the non-linear optical response of these glass samples with femtosecond resolution in time. In the experiment, a high intensity pump pulse was focused onto a sample by a lens with a focal distance of 300 mm after a 3 mm aperture. (A schematic of the experimental set-up is shown as the inset to Figure 2). The sample was moved after each shot. A probe pulse propagating with some delay Δt after the pump pulse was divided into two pulses at a Michelson interferometer. As the probe beam diameter was several times greater than the pump beam diameter, after the interferometer a disturbed central part of one probe beam overlapped with an unexcited peripheral part of the other one. An interference pattern was recorded at the spectrometer exit and finally a Fourier Transform was performed to extract the phase shift $\Delta\phi$ of the probe pulse at each transverse coordinate for each Δt . The magnitude and sign of $\Delta\phi$ induced due to the effect of cross-phase modulation were proportional to the variation of the real part of the refractive index upon the pump pulse illumination.

It was proposed in [13] that the dielectric constant of a glass sample varies due to the third-order non-linearity, free charge carriers excitation and their trapping at the gap-states. This can be observed in Figure 2, which displays the time dependence of $\Delta\phi$ averaged over the probe beam cross-section for the sample $\text{As}_{40}\text{S}_{60}$. At low pulse energy E (see the curve $\Delta\phi(\Delta t)$ at $E = 0.3 \mu\text{J}$ in Figure 2, filled circles), the dielectric constant changes predominantly due to the third-order non-linearity (optical Kerr effect) and this reveals itself as a positive-valued maximum in $\Delta\phi(\Delta t)$. At higher E (the curve $\Delta\phi(\Delta t)$ at $E = 9.2 \mu\text{J}$ in Figure 2, open triangles), this maximum is followed by a fast $\Delta\phi$ decrease down to negative values due to the photo-excitation of free electrons. At greater Δt , a subsequent slow increase in $\Delta\phi$ magnitude is observed; this is assumed to be due to the charge carriers recombination (followed by a permanent change of refractive index at $\Delta t > 4$ ps [3]). In chalcogenide glasses, the kinetics of charge carriers develops as both radiative and non-radiative recombination [14].

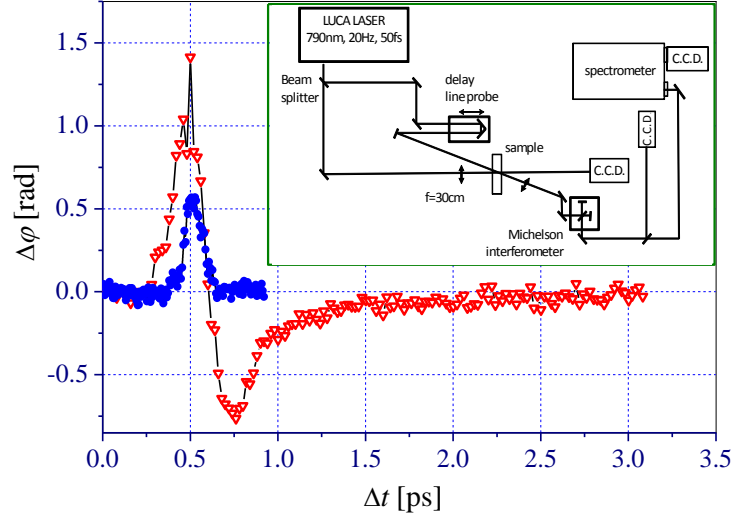


Figure 2. Time-resolved non-linear optical response of the glass samples: $\text{As}_{40}\text{S}_{60}$, $E = 0.3 \mu\text{J}$ (filled circles), $9.2 \mu\text{J}$ (open triangles); inset: the pump-probe set-up scheme.

At low E , when the density of photo-excited electron-hole pairs is negligibly small, the propagation of the laser pulses in the sample along the z – direction, normal to the sample surface, is described by the equations:

$$\partial I_{pu} / \partial z = -(\alpha_0 + \beta_2 I_{pu}) I_{pu} \quad (1a)$$

$$\partial I_{pr} / \partial z = -(\alpha_0 + 2\beta_2 I_{pu}) I_{pr} \quad (1b)$$

$$\partial \varphi_{pu} / \partial z = k n_2 I_{pu} \quad (1c)$$

$$\partial \varphi_{pr} / \partial z = 2k n_2 I_{pu} \quad (1d)$$

where $I_{pu}(r,z,t)$ and $I_{pr}(r,z,t)$, $\varphi_{pu}(r,z,t)$ and $\varphi_{pr}(r,z,t)$ are, respectively, the pump and probe pulse intensities and their phases; r is the transverse coordinate, t is the time in the moving frame coordinate system, and $k = 2\pi/\lambda^p$. The equations (1) do not include any derivatives with respect to the transverse coordinate r because at low E , we have found that the laser beam spot size in the sample did not vary significantly with Δt . A small angle between the pump and probe pulses equal to 18.5° in air (less than 7° in a sample) was also not taken into account.

From (1), the following expressions for evaluating n_2 and β_2 have been obtained:

$$\beta_2 = \left(1 + (1 - A)^{-1/2}\right) / \left(I_{pu}^0 L^{(\alpha)} \left(1 + (L/L_d)^2\right)^{-1/2}\right) \quad (2)$$

$$n_2 = \Delta\varphi(L) / (2k \int_0^L I_{pu}(z) dz) \quad (3)$$

Here $I_{pu}^0 = E \cdot \tau^{-1} \cdot (\pi w^2)^{-1}$ is the peak intensity of the pump pulse on the front surface of the sample, taking into account of the Fresnel reflection from the surface, w is the laser beam radius, $L^{(\alpha)} = (1 - \exp(-\alpha_0 L)) / \alpha_0$, L is the sample thickness. The probe pulse absorbance $A = 1 - I_{pr}^L / I_{pr}^0$, where I_{pr}^L and I_{pr}^0 are the peak intensities of the probe pulse at the back and front surfaces of the sample, respectively.

As the group velocity dispersion (GVD) coefficient of chalcogenide glasses is large at λ^p [1,2] (for $\text{As}_{40}\text{S}_{60}$, the dispersion length $L_d = 0.66$ mm that is comparable with the sample thickness $L = 0.88$ mm) the pump intensity decrease due to the pulse broadening is to be taken into account. In derivation of (2), (3), we have done this approximately as $I_{pu}^0 (1 + (z/L_d)^2)^{-1/2}$.

For the evaluation of n_2 and β_2 , the results of measurements for each sample have been analysed in order to identify the pump pulse energies when the density of the photo-excited electron-hole pairs is negligibly small (no obvious $\Delta\varphi$ decrease down to negative values, Figure.3). At these energies ($E \approx 0.2 - 0.3 \mu\text{J}$), the transverse profiles of $\Delta\varphi$ and A (Figure 3, inset) measured at the maximums Δt^{max} of the $\Delta\varphi(\Delta t)$ curves have been approximated by Gaussian functions and the mean values of $\Delta\varphi$ and A at the beam axis have been defined.

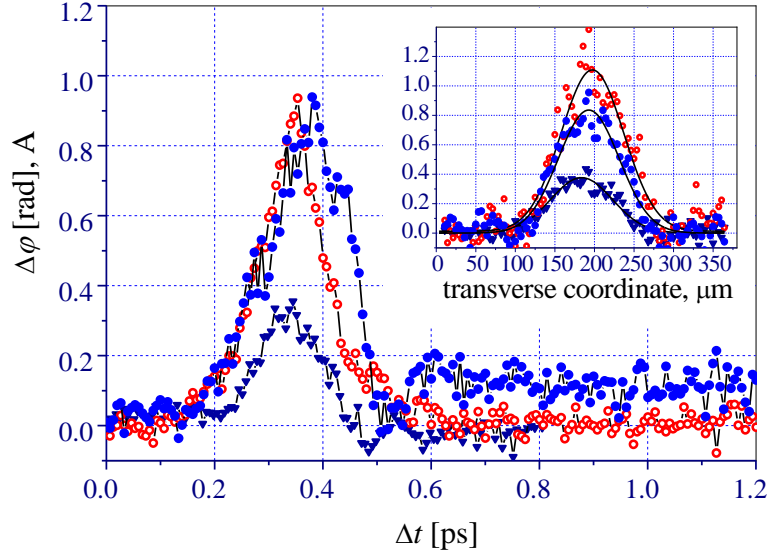


Figure 3. Time-resolved non-linear optical response of the glass samples: $\text{As}_{40}\text{S}_{30}\text{Se}_{30}$ (filled triangles), $\text{Ge}_{20}\text{Se}_{80}$ (open circles - $\Delta\varphi$, filled circles - A), $E = 0.3 \mu\text{J}$; inset: transverse profiles of $\Delta\varphi$ and A at $\Delta t = \Delta t^{max}$

3. Results

As the β_2 magnitudes of $\text{As}_{40}\text{S}_{60}$ at $\lambda = 0.8 \mu\text{m}$ have been measured in [15,16] by using femtosecond laser pulses, these results ($\beta_2 \approx 2 \text{ cm/GW}$) have been taken in this work for comparison. As is known from literature [10], using of the nano- or pico- second laser pulses provided greater magnitudes: $\beta_2 \approx 3\text{-}10 \text{ cm/GW}$. As follows from Figure 2, densities of the charge carriers at large E are large and this can violence the results of n_2 measurements with the long pulses. The increase of β_2 and n_2 magnitudes with the pump pulse duration due to thermal effects has been demonstrated in [17].

For $\text{As}_{40}\text{S}_{60}$ composition, a series of measurements was undertaken in order to evaluate mean β_2 and n_2 magnitudes (table 1) by using (2), (3). Other parameters in table 1 have been obtained using spectrophotometric measurements [12]. E_g has been evaluated as an iso - absorption gap at $\alpha_0 = 10^3 \text{ cm}^{-1}$. For the system As-S-Se, the obtained E_g magnitudes are in a good agreement with the results published in [18].

The same technique has been applied to other glass samples and the results are collected in table 1. Only positive values of n_2 have been obtained experimentally. At $E = 0.3 \mu\text{J}$, the magnitude of I_{pu}^0 for all the samples was around 20-25 GW/cm^2 . The non-linear part $\beta_2 I_{pu}^0$ of the absorption coefficient varied in the range 60 - 90 cm^{-1} that is much greater than α_0 (table 1) in (1a), (1b). Then the curve $A(\Delta t)$ at $E = 0.3 \mu\text{J}$ in Figure 3 is related mainly to the two-photon absorption in $\text{Ge}_{20}\text{Se}_{80}$. A weak absorption by free electrons reveals itself as a small shift of the curve maximum with respect to the maximum of $\Delta\varphi(\Delta t)$. Some residual absorption at $\Delta t > 0.6 \text{ ps}$ is due to the electrons transitions to the gap states [13]. Because of the large $\beta_2 I_{pu}^0$, the non-linear optical response develops at the front sample surface over a distance of less than 0.1 mm.

Table 1. Optical parameters defined at λ^p (0.79 μm)

Composition	E_g , eV	R_e	n_0	α_0 (cm^{-1})	β_2 (cm GW^{-1})	$n_2 \cdot 10^{14}$ ($\text{cm}^2 \text{W}^{-1}$)
$\text{As}_{40}\text{S}_{60}$	2.35	0.66	2.52	0.1	2.0	0.8
$\text{As}_{40}\text{S}_{45}\text{Se}_{15}$	2.20	0.71	2.65	0.2	2.2	0.4
$\text{As}_{40}\text{S}_{30}\text{Se}_{30}$	2.00	0.78	2.80	0.4	2.7	0.4
$\text{As}_{40}\text{S}_{15}\text{Se}_{45}$	1.90	0.82	2.95	2.2	4.0	0.6
$\text{Ge}_{20}\text{Se}_{80}$	2.03	0.77	2.52	1.2	3.9	1.3
$\text{Ge}_{12}\text{Se}_{88}$	1.95	0.80	2.68	3.5	3.9	0.9

4. Discussion

As comparative experimental data at λ^p are currently not available in literature, we have used the theory of the non-linear optical response of the crystalline semiconductors in order to analyze these results, similar to the approach used in [6-9]. The dependencies $\beta_2(h\nu)$, $n_2(h\nu)$ for direct-gap and indirect-gap crystalline semiconductors were obtained in [4] and [5], respectively, by using the non-linear Kramers-Kronig relation. For the direct-gap crystalline semiconductors,

$$n_2(h\nu) = n_2^0 \cdot F_1(h\nu) \quad (4)$$

with the spectral function [4]:

$$F_1(x) = K_1 \cdot \left(6x - 3x^2 - x^3 - \frac{3}{4}x^4 - \frac{3}{4}x^5 - 2 + 2(1-2x)^{3/2} \Theta(1-2x)\right) \cdot (2x)^{-6} \cdot (n_0^0 E_g^2)^{-2} \quad (5)$$

where $x = h\nu E_g$. In (5), $K_1 = K \cdot \hbar c \cdot E_p^{1/2} / 2$, K is a constant and E_p is related to the interband momentum matrix element that is nearly material independent [4], $\Theta(t) = 1$ ($t \geq 0$), 0 ($t < 0$). The magnitude of n_2 in the low frequency limit $n_2^0 = n_2(\nu \rightarrow 0)$ has been expressed by Lines [19] in terms of the Sellmeier gap energy E_s :

$$n_2^0 = Q \cdot d_b^2 \cdot ((n_0^0)^2 + 2)^3 \cdot ((n_0^0)^2 - 1) \cdot (n_0^0 \cdot E_s)^{-2}, [cm^2 / W] \quad (6)$$

where d_b [nm] is a mean length of the cation-anion link, and n_0^0 is the linear refractive index in the low frequency limit. For chalcogenide glasses, $E_s \approx 2.5 \cdot E_g$ [19]. The coefficient Q in (6) is a constant, which depends on a reference standard, i.e. a material for which n_2 values have been precisely measured. In [19], $Q = 1.7 \times 10^{-14}$ was obtained in theory, but in order to fit the reference standard for CS₂ at $\lambda = 1 \mu m$, the Q magnitude was taken as twice greater than this, i.e. as 3.4×10^{-14} .

The spectral dependence of the two-photon absorption coefficient:

$$\beta_2(h\nu) = K_2 \cdot F_2(h\nu) \quad (7)$$

where the spectral function from [4] defined in the range $h\nu > E_g/2$ is:

$$F_2(x) = (2x - 1)^{3/2} \cdot (2x)^{-5} \cdot (n_0^0 E_g^{3/2})^{-2} \quad (8)$$

and $K_2 = K \cdot E_p^{1/2}$. The magnitudes of n_0^0 have been evaluated by using the Moss rule: $n_0^0 = 3 / E_g^{1/4}$, where E_g is in units of eV [7].

For comparison with the obtained experimental data, spectral dependencies $n_2(\lambda)$ have been calculated by using (4) – (6) and are plotted in Figure 4a. The coefficient K_1 in (5) has been evaluated for each glass composition from the condition: $F_1(h\nu) \rightarrow 1$ when $\nu \rightarrow 0$, which fits (4). It was found that the experimental n_2 magnitudes available in the literature for As₄₀S₆₀ (open circles in Figure 4a at $\lambda > 1 \mu m$) are located between the curves $n_2(\lambda)$ plotted with $Q = 1.7 \cdot 10^{-14}$ (solid line 1) and $Q = 3.4 \cdot 10^{-14}$ (dashed line 1). Such a large variation of the measured n_2 values available in literature is likely to be due to the use of different laser pulse durations in the experimental set-ups, as has been mentioned above.

Similarly, we have plotted such curves for As₄₀S₃₀Se₃₀ (solid and dashed lines 2 in Figure 4a). As E_g of the composition Ge₂₀Se₈₀ is almost the same as that of As₄₀S₃₀Se₃₀ their calculated spectral curves are almost identical and they are plotted together on Figure 4a. Experimental data available for these samples are in an agreement with the curves $n_2(\lambda)$ at $\lambda > 1 \mu m$ within the experimental error 15-20% that is typical for measurements of the non-linear optical coefficients [2].

The spectral dependencies $\beta_2(\lambda)$ of the glass samples of the system As-S-Se have been calculated by using (7), (8) and are plotted in Figure 4b. The coefficient K_2 has been evaluated from the available data for As₄₀S₆₀: $\beta_2(\lambda) \approx 2$ cm/GW at $\lambda = 0.8 \mu m$ [15,16]. For the sample Ge₂₀Se₈₀, K_2 estimation was based on the result from [20]: $\beta_2(\lambda) = 1.8$ cm/GW at $\lambda = 1.064 \mu m$. In fact, there is little published experimental data for comparison. For crystalline semiconductors, $\beta_2(\lambda) = 0$ in the range $\lambda > 2\lambda_g$. However for chalcogenide glasses, there are non-zero literature data in this range [2, 18-24] as shown in Figure 4b. At these points, the non-linear absorption coefficient can be attributed to consecutive electron transitions involving the gap states (two-step transitions) [21].

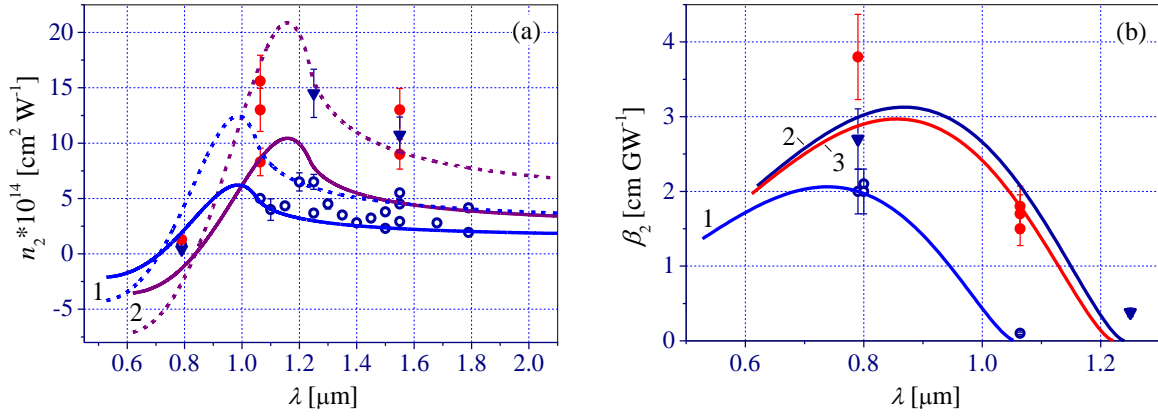


Figure 4. Experimental data from the present work at $\lambda^p = 0.79 \mu\text{m}$ and from [2,18-24] (symbols). Calculated wavelength dependencies of: a) n_2 ($Q = 1.7 \cdot 10^{-14}$ (solid lines), $3.4 \cdot 10^{-14}$ (dashed lines)); 1 - As₄₀S₆₀ (open circles), 2 - As₄₀S₃₀Se₃₀ (filled triangles) and Ge₂₀Se₈₀ (filled circles). b) β_2 , 1 - As₄₀S₆₀ (open circles), 2 - As₄₀S₃₀Se₃₀ (filled triangles), 3 - Ge₂₀Se₈₀ (filled circles)

As E_g is actually the main decisive parameter in the theory of the non-linear optical response of crystalline semiconductors, it is reasonable to analyze its role in the non-linear optical response of chalcogenide glasses. From the literature data shown in Figure 4a, it can be seen that at a given wavelength $\lambda > 1 \mu\text{m}$, n_2 is greater for the compositions with smaller E_g (table 1), as is already known [2]. Some agreement is also noticeable with the spectral dependencies of the direct-gap crystalline semiconductors (lines in Figure 4a). However near the FAB edge, the positive-valued n_2 measured in the present work (data at $\lambda^p = 0.79 \mu\text{m}$ in Figure 4a, taken from table 1) do not fit these dependencies, which have $n_2 < 0$ in the range $R_e > 0.7$, for some compositions, namely As₄₀S₃₀Se₃₀ and Ge₂₀Se₈₀. Far from the FAB edge, these compositions having approximately the same E_g ($\approx 2 \text{ eV}$, table 1) exhibit similar n_2 values (filled circles and triangles in Figure 4a at $\lambda > 1 \mu\text{m}$) within the experimental error. Near the FAB edge at λ^p , n_2 and β_2 of the Ge₂₀Se₈₀ sample are much larger than those measured for the As₄₀S₃₀Se₃₀ sample (Table 1).

In Figure 1, we can see that the sample Ge₂₀Se₈₀ was illuminated in the range of its Urbach tail ($\ln(\alpha_0/\alpha_0^1) > 0$), while the sample As₄₀S₃₀Se₃₀ - in the range of its WAT tail ($\ln(\alpha_0/\alpha_0^1) < 0$). The sample As₄₀S₁₅Se₄₅ illuminated at its Urbach tail has the magnitude of β_2 comparable with that measured here for Ge₂₀Se₈₀ (table 1). As the Urbach tail is associated with the photo-induced electron transitions involving the gap states [1,2], we can assume that probabilities of the two-step transitions through the real states in the bandgap are greater than for the two-photon transitions through virtual states as assumed in the two-band models of the crystalline semiconductors. If a sample is illuminated in the range of its WAT tail, the two-photon transitions should happen mainly through the virtual states because the density of gap states involved into these transitions is small. In Figure 1, this occurs for three samples of the composition As₄₀S_xSe_{60-x} ($x = 30, 45, 60$). In the range of the Urbach tail, the probabilities of the two-step transitions through the gap states may increase. This explains why the β_2 magnitude of the sample Ge₂₀Se₈₀ measured in the present work (filled circle at λ^p in Figure 4b) is greater than the one calculated at λ^p by using (7), (8) (line 3 in Figure 4b). Similarly for the sample As₄₀S₁₅Se₄₅, the β_2 magnitude measured and presented in table 1 is greater than the value of 3.2 cm/GW calculated at λ^p by using (7), (8).

5. Conclusions

In conclusion, Fourier Transform interferometry with the femtosecond resolution in time has been used to measure the nonlinear optical response of a variety of chalcogenide glasses of the systems As-S-Se and Ge-Se and evaluate their non-linear optical coefficients of refraction and absorption near the FAB edge. The technique has been based on the thorough analysis of the results of measurements at different pump pulse energies and identification of the conditions when the nonlinear optical response is defined predominantly by the optical Kerr effect. In fact, this effect driven by the electronic part of a polarization is much faster than structural transformations revealing in a permanent increase of

refractive index of a glass sample in a long-time scale dynamics of the non-linear optical response [3]. This separation in time of different contributing effects enabled us to have got the reliable and reproducible magnitudes of the non-linear optical coefficients near the FAB edge.

Comparison with the results of the theory of crystalline semiconductors has revealed that spectral dependence $\beta_2(h\nu)$ of the direct-gap crystalline semiconductors exhibit an agreement (within an experimental error) with the available literature data and our results for the glass samples illuminated at their WAT tails. For the samples illuminated at their Urbach tails, when electron transitions through the gap states are possible, the magnitudes of β_2 differ substantially from that calculated by using the results of the theory of the direct-gap crystalline semiconductors.

Our results of n_2 evaluation and the data available in literature reveal that n_2 magnitudes are always positive-valued that is different from the direct-gap crystalline semiconductors having negative-valued n_2 in some spectral range near the FAB edge. We can conclude that a shape of the spectral dependencies $n_2(h\nu)$ of chalcogenide glasses near the FAB edge is still unknown and needs further investigation.

Acknowledgments This research was supported by the LaserLab-Europe network (the project ref. number SLIC001675), the Royal Society (IJP—2010/R1, IES—2013/R2) and by the Russian Science Foundation (Grant No. 16-13-10251).

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Figure captions

Figure 1.

Logarithm of the absorption coefficient of the glass compositions $\text{As}_{40}\text{S}_x\text{Se}_{60-x}$, $x = 0$ (1), 15 (2), 30 (4), 45(5), 60 (6) and $\text{Ge}_{20}\text{Se}_{80}$ (3). The vertical dashed line indicates $h\nu^p = 1.57$ eV. $\alpha_0^1 = 1 \text{ cm}^{-1}$

Figure 2.

Time-resolved non-linear optical response of the glass samples: $\text{As}_{40}\text{S}_{60}$, $E = 0.3 \mu\text{J}$ (filled circles), $9.2 \mu\text{J}$ (open triangles); inset: the pump-probe set-up scheme.

Figure 3.

Time-resolved non-linear optical response of the glass samples: $\text{As}_{40}\text{S}_{30}\text{Se}_{30}$ (filled triangles), $\text{Ge}_{20}\text{Se}_{80}$ (open circles - $\Delta\phi$, filled circles - A), $E = 0.3 \mu\text{J}$; inset: transverse profiles of $\Delta\phi$ and A at $\Delta t = \Delta t^{max}$.

Figure 4.

Experimental data from the present work at $\lambda^p = 0.79 \mu\text{m}$ and from [2,18-24] (symbols). Calculated wavelength dependencies of: a) n_2 ($Q = 1.7 \cdot 10^{-14}$ (solid lines), $3.4 \cdot 10^{-14}$ (dashed lines)); 1 - $\text{As}_{40}\text{S}_{60}$ (open circles), 2 - $\text{As}_{40}\text{S}_{30}\text{Se}_{30}$ (filled triangles) and $\text{Ge}_{20}\text{Se}_{80}$ (filled circles). b) β_2 , 1 - $\text{As}_{40}\text{S}_{60}$ (open circles), 2 - $\text{As}_{40}\text{S}_{30}\text{Se}_{30}$ (filled triangles), 3 - $\text{Ge}_{20}\text{Se}_{80}$ (filled circles)