

# Measurement of the Phase and Intensity Profile of Surface Plasmon Laser Emission

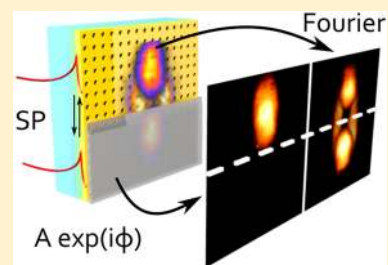
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**S** Supporting Information

**ABSTRACT:** We study the near- and far-field radiation patterns of surface plasmon (SP) lasers in metal hole arrays and observe radially polarized vortex-vector laser beams in both near and far field. Besides the intensity profile, also the complementary phase profile is obtained with a beam block experiment, where we block part of the beam in the near field, measure the resulting changes in the far field, and retrieve the phase using an iterative algorithm. This phase profile provides valuable information on the feedback mechanisms and coherence of the laser and shows that our SP laser operates in a phase-slip mode instead of a pure dark mode. To explain our observations, we extend the standard model for distributed feedback lasers by introducing a position dependence in the optical gain and refractive index.

**KEYWORDS:** surface plasmon laser, distributed feedback, phase retrieval, metal hole array, plasmonic crystal laser, active mirror



Optically coherent laser radiation can be generated if both gain and optical feedback are present in a medium. Our physical understanding of these phenomena originates from comparisons between measured intensity distributions and models of both the amplitude and the phase of the radiation. The optical phase is typically discarded because it evolves too fast to resolve directly with an optical detector or a camera. The inability to measure both amplitude and phase of the emitted laser radiation presents a recurring challenge in optics and limits progress in the field.

More ingenious schemes are needed to observe the phase using slow detectors. One of the simplest schemes uses the mixing of the amplitude and phase information on the light field upon propagation. At the laser exit the amplitude contains information where the light is emitted, while the phase profile contains information about the propagation direction. Recording the intensity distribution on different positions allows retrieval of the phase information by an iterative algorithm.<sup>1–3</sup>

The ability to resolve both amplitude and phase is particularly relevant for lasers that emit nonstandard beam profiles that are not yet fully understood. Examples of such lasers are surface-emitting distributed feedback lasers, such as photonic and plasmonic crystal lasers. Two-dimensional surface-emitting photonic-crystal lasers often emit donut beams with azimuthal polarization,<sup>4</sup> while surface plasmon lasers create radially polarized vector-vortex beams.<sup>5</sup> Devices can be tailored to emit other beam shapes,<sup>6</sup> but information about the phase and amplitude profile is scarce and either has low resolution<sup>7</sup> or an electrical contact blocks the view.<sup>8</sup>

A better understanding of gain and feedback in plasmonic systems is important for improving photonics applications that use the strong confinement and light–matter interaction provided by plasmons. These applications include ultrasensitive molecule sensors (SERS),<sup>9</sup> anticounterfeiting measures,<sup>10</sup>

perfect absorbers,<sup>11</sup> ultrafast optical modulators,<sup>12</sup> and future metal–dielectric metamaterials consisting of arrays of plasmonic subwavelength elements.<sup>13,14</sup> The strong plasmonic response of passive media is accompanied by ohmic loss due to scattering of the free electrons in the material. Adding media with active gain can resolve this issue,<sup>15–17</sup> and overcompensation typically leads to laser action, as has been demonstrated in two-dimensional metal particle arrays<sup>18</sup> and metal hole arrays.<sup>5</sup>

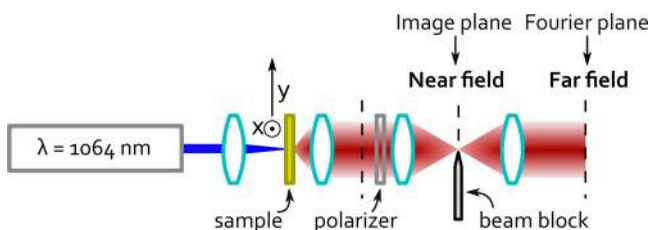
In this Letter, we present the first experimental observation of the phase and amplitude profile of a two-dimensional surface plasmon laser retrieved via the combination of a beam-block experiment and an iterative algorithm. The metal hole array in our study acts as a second-order Bragg grating, which provides a natural output channel and enables easy observation of the intracavity field. Our observations go beyond the standard description of distributed feedback lasers. We extend the standard approach by including a position-dependent gain and refractive index, which are both induced by the optical pump beam, and obtain good agreement between experiment and theory.

## ■ DEVICE

The semiconductor–gold samples that we study contain metal hole arrays with a square lattice, with hole diameters of 160 nm and a lattice spacing of 470 nm (see Figure 2a for a SEM image). The device dimensions studied here are 50 × 50 and 100 × 100 μm. The Au film is 100 nm thick and is deposited on a 127 nm In<sub>x</sub>Ga<sub>1–x</sub>As ( $x = 0.536$ ) gain layer on an InP substrate (see Figure 2e for a schematic side cut). Between the gold and the InGaAs, a thin InP spacer layer and a SiN passivation layer

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**Figure 1.** Schematic of the experimental setup to measure the amplitude and phase profile of the laser emission.

were incorporated. The gain layer is sufficiently thin such that the only supported optical mode is the surface plasmon (SP) mode. Similar samples are described in more detail in ref 5.

## EXPERIMENT

Our experimental geometry is as shown in Figure 1. The sample is mounted in a cryostat with optical access on both sides and cooled to 80 K. We pump the active layer of the sample using a continuous wave laser with a wavelength of 1064 nm through the transparent InP substrate. The pump beam has a Gaussian profile that can be varied in size between 20 and 50  $\mu\text{m}$  full width at half-maximum. The light emitted by the SP laser is collected in transmission on the metal side of the device with a 20 $\times$  microscope objective (NA = 0.4) combined with a tube lens ( $f = 200$  mm) to create a 4- $f$  imaging system. Hence, the optical field in the image plane is a scaled version of the radiative field at the sample; in this paper, we call this the near field.

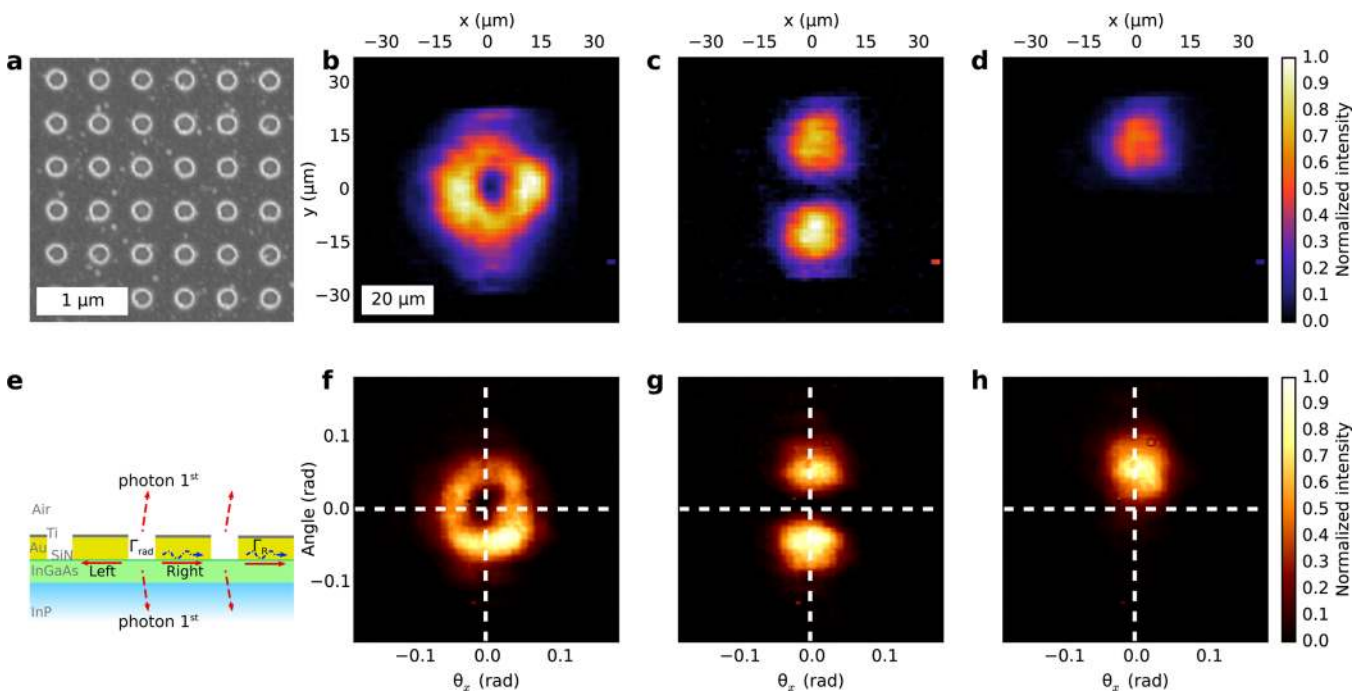
In some of the experiments we position a razor blade in the near field to block part of the beam. To inspect the near field, we image it with a lens ( $f = 100$  mm) on a CCD camera.

Subsequently, this lens is replaced by a lens with a longer focal distance ( $f = 200$  mm) such that the far field is retrieved in the back-focal plane. A bandpass filter ( $\lambda = 1490 \pm 6$  nm) that transmits the laser light is used to reduce the broadband spontaneous emission in the measurements.

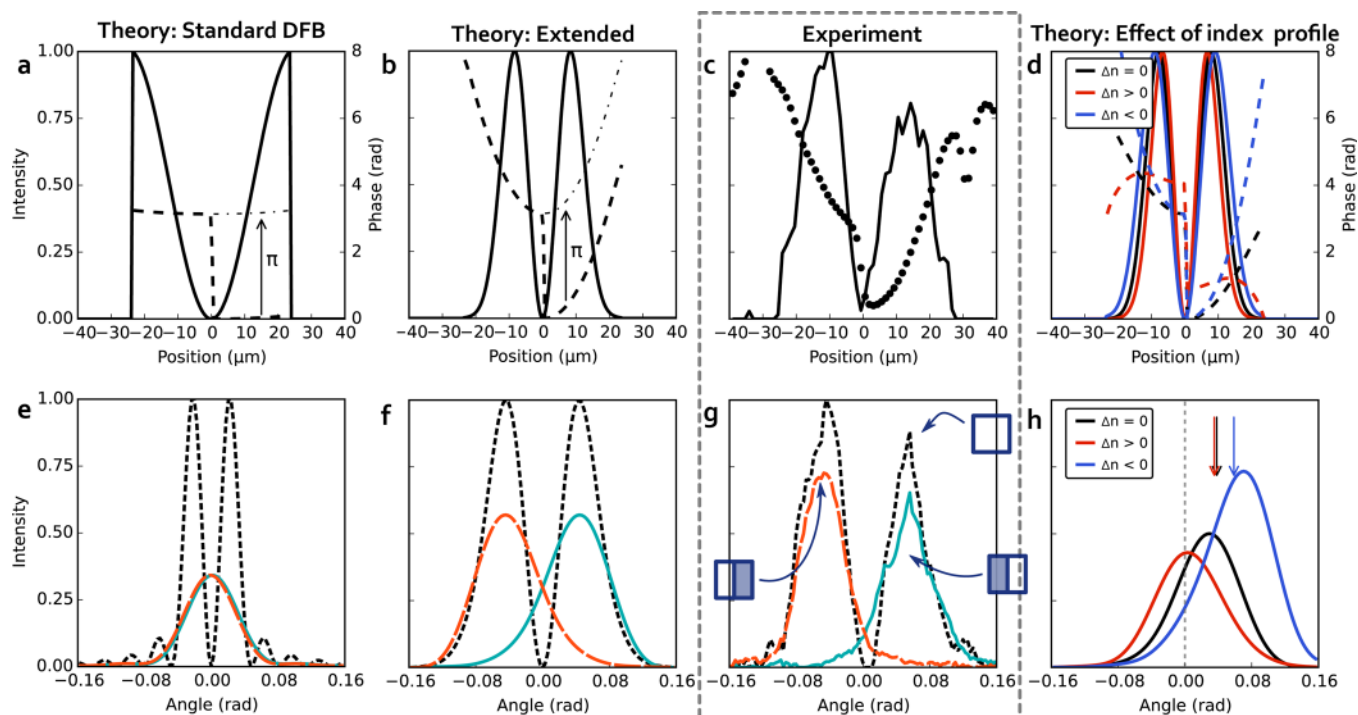
## RESULTS

Figure 2 show the measured near field (top) and far field (bottom) of the SP laser. Images are shown for the unpolarized light (b, f), with a linear polarizer transmitting  $y$ -polarized light (c, g), and with half of the near field blocked (d, h). The near field is donut shaped; that is, it is circular with a dark center. The laser area is comparable to the size of the pump, being 40  $\mu\text{m}$  in this case. The dark central spot is remarkable and raises questions about the apparent lack of energy in the center of the device. Figure 2c shows a polarization-resolved measurement. Since this image rotates along when rotating the polarized axis, we conclude that the near-field donut is radially polarized. The observation of a clear donut in the near field is only apparent when the pump beam is small enough. In our experiments, we observe that larger pump beams (up to 100  $\mu\text{m}$ ) result in a larger laser area and spatial inhomogeneity. Nonetheless, there is always a dark spot somewhere, as expected for a topological defect. Under some experimental conditions the laser hops between several spatial modes with different locations of the dark spot, and hence the central dark spot becomes less visible after averaging.

Figure 2f–h show the observed far-field intensity profiles and display that the far field is also a radially polarized donut beam. This similarity is not trivial and warrants further investigation. In order to observe the associated phase profile, we perform an experiment in which we block half of the near field with a razor



**Figure 2.** Our SP laser and its emission, measured in near and far field. (a) Scanning electron microscopy image of the metal hole array. (e) Cross section through the sample, indicating the layer stack, the left and right traveling waves, and the emitted light. (b–d) Near-field and (f–h) far-field intensity profiles of a surface plasmon laser. (b, f) Donut-shaped beams in both near and far field. (c, g) Profiles observed behind a polarizer that transmits vertically polarized light. (d, h) What happens when we block the lower part of the near field. Vertical cross sections are shown in Figure 3c,g.



**Figure 3.** Cross sections through the center along the vertical direction of the (a–d) near field and (e–h) far field. In (a–d), the solid lines show the intensity envelope and the dashed lines show the phase of the near field. To stress the symmetry in (a) and (b), a  $\pi$ -shifted copy of the phase is displayed as a dashed-dotted line. In (e–h), the dashed curves show the far-field intensity profiles of the full beam, while the colored curves show the resulting far fields when blocking the right (red dashed) or left (blue solid) half of the near field. The framed figures (c, g) are the experimental data taken from Figure 2 and the reconstructed phase of the near field. The other figures are based on theory: (a, d) Standard DFB theory with uniform gain and index, (b, f) extended theory that includes a position-dependent gain and refractive index, (d, h) extended theory with variations in the magnitude of the index profile. Note that panel (h) displays the far field for only one blocking condition. The arrows indicate the opening angle of the beam without beam block.

blade and observe the far field. The resulting near field, shown in Figure 2d, is trivial and presented mainly for didactic reasons. The resulting far field, shown in Figure 2h, depicts that the two-lobed far field is now reduced to a single lobe, while the angle of the maximum emission is hardly changed. This observation provides valuable information about the phase profile of the near field, because it indicates the existence of a phase gradient in the near field.

To quantify the full two-dimensional phase profile of the optical field, we retrieve the phase profile with an iterative Gerchberg–Saxton-based algorithm;<sup>1</sup> see Methods. We find that the retrieved near-field phase exhibits a  $\pi$ -phase jump in the dark center of the device and exhibits a phase gradient in the radial direction, with a slope that increases toward the edge of the device. A cross section of this phase profile is depicted in Figure 3c,g. These figures also show cross sections of the near- and far-field intensity profiles presented earlier in Figure 2. The far field of the full beam has no light in the center, whereas there is emission along the surface normal in the beam block experiments. Because the far field of the full beam should be equal to the coherent sum of the two halves, the dark center in the far field must be formed by interference of emission from the two halves of the sample. This in turn indicates the existence of long-range coherence across the sample. In the rest of this Letter we will discuss the implications of our observations and compare them with theory.

## DISCUSSION

We first compare our results with the standard distributed feedback (DFB) theory<sup>19</sup> for one-dimensional systems with a finite size. In this theory, the field in the device is decomposed in two traveling waves, which are coupled by scattering at the holes. The relevant parameters are the length  $L$  of the device and the coupling rate  $\kappa$ . The product  $\kappa L$  determines the behavior of the laser. This theory yields the threshold condition of the laser: wavelength, gain, and the field profiles of the traveling waves.

The solutions are either symmetric or antisymmetric around the center of the device. In an infinitely large index-coupled system these are dark (nonradiating) and bright (radiating) modes, which are located at the exact center of the Brillouin zone ( $k = 0$ ).<sup>20–22</sup> However, in a “real” laser, the coherence length  $l_{\text{coh}}$  is limited by the finite sample size and the scattering,<sup>19</sup> which breaks the description of a continuous band structure into discrete modes with a detuning from the Bragg wavelength. The relevant modes are at  $\Delta k = \pi/l_{\text{coh}}$  and there is no mode at the center of the Brillouin zone.

Scattering in the out-of-plane direction induces radiative loss, which increases the threshold of the radiative solution.<sup>23</sup> Our device operates in a transverse-magnetic (TM) mode, and hence the coupled mode with the symmetric out-of-plane  $E$ -field distribution is the nonradiating mode with the lowest threshold, as explained in the Supporting Information.

Figure 3a,b displays the calculated symmetric coupled mode solution of the standard DFB theory for our measured backscatter rate  $\kappa/\beta_0 = 0.012$ ,<sup>21</sup> device length  $L = 50 \mu\text{m}$ ,

and refractive index  $n_0 = 3.268$ ,<sup>24</sup> corresponding to  $\kappa L = 8$ . The calculated near field shown in Figure 3a contains the essential features of Figure 3c: it has two lobes with opposite sign, indicated by a  $\pi$ -phase jump in the center of the device. However, in contrast to the experiment the calculated phase in each of the lobes is almost constant. As a consequence, the far-field profiles depicted in Figure 3e are very different from the observations depicted in Figure 3g: the calculated profile is too narrow and is oscillatory at larger angles. Furthermore, the emission by half of the device is incorrectly predicted to be a single lobe located close to the surface normal.

To explain our observations, we extend the standard DFB theory by introducing a position dependence of the gain and refractive index (see Supporting Information for derivation). Both are mainly set by the carrier density, which is position dependent due to inhomogeneous pumping and diffusion, and to a lesser extent by the local temperature associated with heating of the device. We model the local gain and index as the Gaussian profile of the pump beam and note that deviations from an exact Gaussian shape are unimportant. In the center of the pumped area there is an effective gain, as discussed below, while outside the pumped area there is an effective loss (negative gain), which is mainly caused by absorption in the gain layer. We solve the coupled mode equations by an active mirror approach,<sup>25</sup> which is relatively simple and powerful, as explained in the Supporting Information. The resulting fields at the threshold are shown in Figure 3b,f. The phase in the near field now increases toward the edge of the samples, very comparable to our measurements. Hence, also the far-field profiles of the beam block experiment are very similar to our observations: the maxima are now at the same angle as the lobes of the full beam.

Figure 3d,h illustrates the predicted effect of index guiding and antiguiding on the laser, with a Gaussian gain and index profile, with  $\Delta n = 0$ ,  $\Delta n = +0.13$ , and  $\Delta n = -0.13$ , between the pumped center and the unpumped edges. The differences are best visible in a beam block experiment (see Figure 3h), where the angle of the maxima of the lobe moves inward for  $\Delta n > 0$  and outward for  $\Delta n < 0$ . The near fields depicted in Figure 3d show index guiding for  $\Delta n > 0$  and index antiguiding for  $\Delta n < 0$ . This guiding can also be interpreted as a plasmonic band gap with spatial dependence.<sup>26,27</sup> Our experimental data can be best fitted with  $\Delta n = -0.05$ , which is consistent with the typical refractive index changes of pumped bulk material.<sup>28</sup>

The gain profile, in contrast to the index profile, leads to guiding, because the effective gain in the center of the pumped area is higher than its surroundings. The gain and loss used in the model have realistic values: The unpumped areas have an effective intensity loss of<sup>24</sup>  $\sim 3000 \text{ cm}^{-1}$ . At the threshold, the net gain in the center is  $\sim 340 \text{ cm}^{-1}$ . The required material intensity gain is the sum of the net gain and the ohmic loss of our device with transparent InP<sup>24</sup> ( $270 \text{ cm}^{-1}$ ), divided by the confinement factor in the gain layer<sup>15</sup> (0.32), and it is around  $2000 \text{ cm}^{-1}$ , which is a reasonable number for a semiconductor operated at high carrier densities.<sup>29,30</sup>

For completeness we note that we have used a one-dimensional model to describe a two- (or even three)-dimensional system. Hence the derived numbers may differ somewhat from reality. From literature on DFB theory in two dimensions,<sup>31,32</sup> we expect that the influence of such 2D coupling on the derived numbers is rather low in our system, because it already operates in the overcoupled regime and the 2D coupling is small compared to the 1D coupling. In earlier

work<sup>21,24</sup> we measured  $k_2/k_3 \approx 0.3$ , where  $k_2$  and  $k_3 = \kappa$  are the scattering rates of respectively  $90^\circ$  and  $180^\circ$  scattering.<sup>31</sup> This extra coupling will only marginally change the detuning<sup>32</sup> and threshold.<sup>31</sup> Other authors have extended the standard DFB theory to two dimensions to answer the question under which conditions the symmetric mode can lase.<sup>33</sup> These analyses confirm that 2D DFB lasers are expected to emit donut-shaped beams.

## CONCLUSION

This paper reports the first measurement and reconstruction of the phase and the amplitude of surface plasmon laser emission. Our two-dimensional plasmonic crystal emits donut-shaped and radially polarized light, both in the near field and in the far field. By blocking half of the laser emission we retrieve the phase of the emission and demonstrate the existence of long-range coherence and lasing in a symmetric nonradiative mode. Our observations cannot be explained with the standard DFB theory, which assumes a device with uniform properties. We extend this theory by introducing position dependence of the gain and refractive index and find good agreement with our measurements on surface-emitting DFB lasers. This provides the following three insights: First, due to the round trip phase condition, the laser is in a phase-slip mode and not in a dark mode, and hence the laser can radiate. Second, we attribute the lack of emission in the center of the near field to interference between in-plane counterpropagating waves. Third, the central zero in the far field also results from the symmetry of the lasing mode and demonstrates the existence of long-range coherence over the full sample.

Our results demonstrate a powerful method to analyze surface-emitting lasers. This method can also be deployed on surface plasmon lasers with other lattice symmetries or on photonic-crystal lasers in order to understand and improve their characteristics. Furthermore, our results indicate that much of the current knowledge about one- and two-dimensional photonic-crystal lasers can be applied to understand and improve surface plasmon lasers.

## METHODS

The phase of the fields is retrieved with an iterative Gerchberg–Saxton-based algorithm.<sup>1–3</sup> The near- and far-field measurements are used as support for the algorithm. The phase is retrieved for three sets of conjugate measurements in parallel: (i) the full polarization resolved measurements shown in Figure 2c,g and measurements with either a blocked (ii) bottom (Figure 2d,h) or (iii) top (measurements not shown). Every fifth iteration, the reconstructed phase of alternately the bottom or top part is applied on the full near-field reconstruction. After 30 iterations, we end with 10 iterations on the full fields. The algorithm converges and is stable to noise.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsp Photonics.6b00239.

A derivation of the extended DFB theory, with an explanation of how the resulting equations can be solved in the time domain and spatial domain and a comparison with previous efforts (PDF)

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### Notes

The authors declare no competing financial interest.

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