

Physics

Physics Research Publications

Purdue University

Year 2006

Measurement of the azimuthal angle distribution of leptons from W boson decays as a function of the W transverse momentum in p(p)over-bar collisions at root s = 1.8 TeV

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Measurement of the azimuthal angle distribution of leptons from W boson decays as a function of the W transverse momentum in $p\bar{p}$ collisions at $\sqrt{s} = 1.8$ TeV

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(Received 2 April 2005; published 3 March 2006)

We present the first measurement of the A_2 and A_3 angular coefficients of the W boson produced in proton-antiproton collisions. We study $W \rightarrow e\nu_e$ and $W \rightarrow \mu\nu_\mu$ candidate events produced in association with at least one jet at CDF, during Run Ia and Run Ib of the Tevatron at $\sqrt{s} = 1.8$ TeV. The corresponding integrated luminosity was 110 pb^{-1} . The jet balances the transverse momentum of the W and introduces QCD effects in W boson production. The extraction of the angular coefficients is achieved through the direct measurement of the azimuthal angle of the charged lepton in the Collins-Soper rest-frame of the W boson. The angular coefficients are measured as a function of the transverse momentum of the W boson. The electron, muon, and combined results are in good agreement with the standard model prediction, up to order α_s^2 in QCD.

DOI: [10.1103/PhysRevD.73.052002](https://doi.org/10.1103/PhysRevD.73.052002)

PACS numbers: 13.88.+e, 11.80.Cr, 12.15.-y, 12.38.Qk

I. INTRODUCTION

Measurements of the W boson differential cross section, as a function of energy and direction, provide information about the nature of both the underlying electroweak interaction, and the effects of chromodynamics (QCD). This differential cross section can be expressed as a function of the helicity cross sections of the W , allowing us to study the W polarization and associated asymmetries. Because of the difficulties in fully reconstructing a W boson in three dimensions at a hadron collider, the complete angular distribution of the W has not been determined yet. In this paper we present the first measurement of two of the four significant leading angular coefficients of the W boson produced at a hadron collider.

The total differential cross section for W boson production in a hadron collider, with a subsequent leptonic decay, is given by

$$\begin{aligned} \frac{d\sigma}{d(p_T^W)^2 dy d\cos\theta d\phi} = & \frac{3}{16\pi} \frac{d\sigma^u}{d(p_T^W)^2 dy} [(1 + \cos^2\theta) \\ & + \frac{1}{2}A_0(1 - 3\cos^2\theta) + A_1\sin 2\theta \cos\phi \\ & + \frac{1}{2}A_2\sin^2\theta \cos 2\phi + A_3\sin\theta \cos\phi \\ & + A_4\cos\theta + A_5\sin^2\theta \sin 2\phi \\ & + A_6\sin 2\theta \sin\phi + A_7\sin\theta \sin\phi], \quad (1) \end{aligned}$$

where p_T^W and y are the transverse momentum and the rapidity of the W in the laboratory frame, and θ and ϕ are the polar and azimuthal angles of the charged lepton from W boson decay in the Collins-Soper (CS) frame [1]. The factors $A_i(p_T^W, y)$ are the angular coefficients of the W boson, which are ratios of the helicity cross sections of the W and its total unpolarized cross section $d\sigma^u/d(p_T^W)^2 dy$. The CS frame [2] is the rest-frame of the W with a z -axis that bisects the angle between the proton direction and the direction opposite that of the antiproton (Fig. 1), and it is used because in this frame we can in principle exactly reconstruct the azimuthal angle ϕ and the polar quantity $|\cos\theta|$. Our ignorance of the W boson longitudinal momentum, which is due to our inability to measure the longitudinal momentum of the decay neutrino, only introduces a two-fold ambiguity on the sign of $\cos\theta$. It is

common to integrate Eq. (1) over y and study the variation of the angular coefficients as a function of p_T^W .

To study the angular distribution of the W we must choose a particular charge for the boson. In this paper we consider the W^- bosons; the W^+ bosons in our samples are CP transformed to be treated as W^- bosons. The angular coefficients for the W^+ are obtained by CP transforming Eq. (1) [3].

If the W is produced with no transverse momentum, it is polarized along the beam axis, due to the V-A nature of the weak interactions and helicity conservation. In that case A_4 is the only nonzero coefficient. If only valence quarks contributed to W production, A_4 would equal 2, and the angular distribution given by Eq. (1) would be $\sim(1 + \cos\theta)^2$, a result that was first verified by the UA1 experiment [4].

If the W is produced with non-negligible transverse momentum, balanced by the associated production of jets, the rest of the angular coefficients are present, and the cross section depends on the azimuthal angle ϕ as well. The last three angular coefficients A_5 , A_6 , and A_7 are nonzero only if gluon loops are present in the production of the W boson. Hence, in order to study all the angular coefficients and associated helicity cross sections of the W boson in a hadron collider, we must consider the production of the W with QCD effects up to order α_s^2 .

The importance of the determination of the W angular coefficients is discussed in [5], and summarized here. It allows us to measure for the first time the full differential cross section of the W and study its polarization, since the angular coefficients are directly related to the helicity cross sections. It also helps us verify the QCD effects in the production of the W up to order α_s^2 . For example, according to the standard model (SM), A_2 is not equal to A_0 only if the effects of gluon loops are taken into account. In addition, A_3 is only affected by the gluon-quark interaction and its measurement can be used to constrain the gluon parton distribution functions. Moreover, the next-to-leading order angular coefficients A_5 , A_6 , and A_7 are P -odd and T -odd and may play an important role in direct CP violation effects in W production and decay [6]. Finally, quantitative understanding of the W angular distribution could be used to test new theoretical models and to facilitate new discoveries.

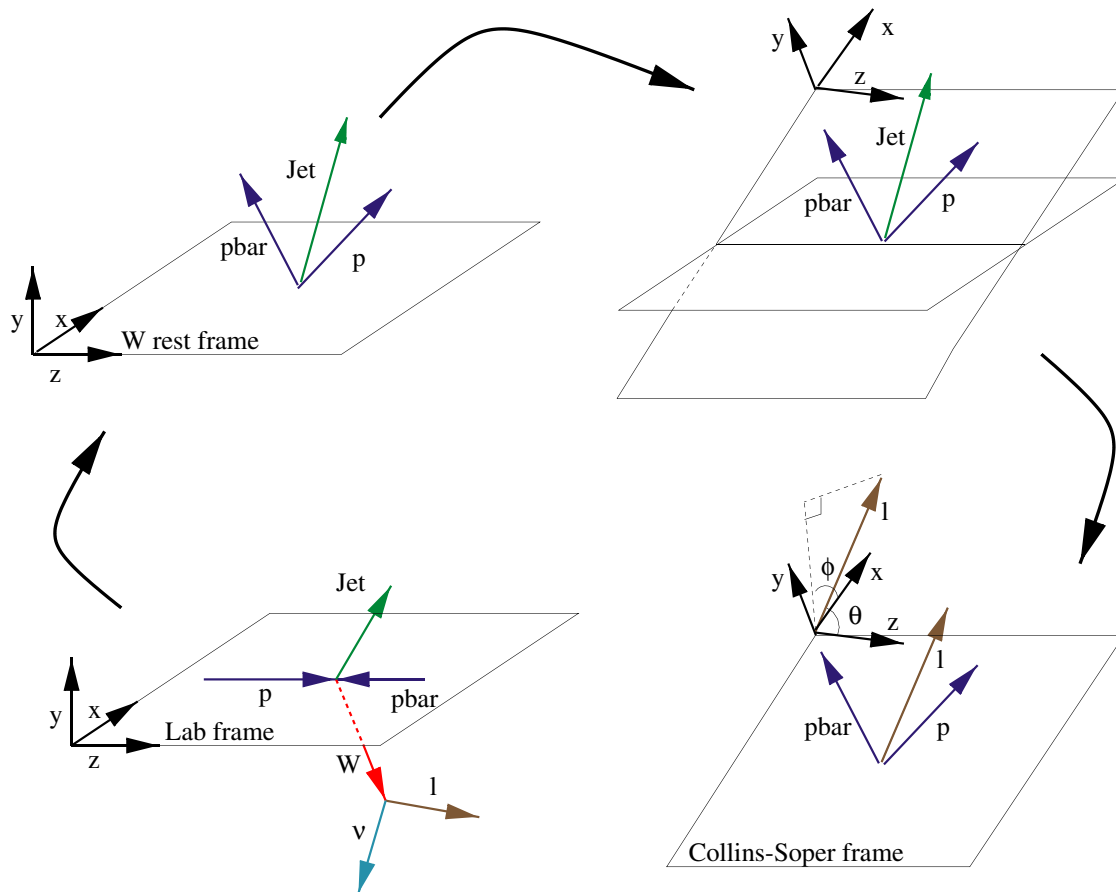


FIG. 1 (color online). Transforming from the laboratory frame to the Collins-Soper frame. We first boost to the W rest-frame, then rotate the x - z plane so that it coincides with the p - \bar{p} plane. Finally we rotate the frame around the y -axis so that the z -axis bisects the angle between \vec{p} and $-\vec{\bar{p}}$. The positive y axis is selected to have the same direction as $\vec{p}_{CS} \times \vec{\bar{p}}_{CS}$.

In this paper we present the first measurement of the A_2 and A_3 angular coefficients of the W boson. These coefficients fully describe the azimuthal differential cross section of the W boson, and they are two of the four significant coefficients that describe the total differential cross section of the W , given that A_1 and the next-to-leading order angular coefficients have considerably lower values [5,7]. This measurement is accomplished using the azimuthal angle of the charged lepton in the CS W rest-frame [8], and is presented as a function of the transverse momentum of the W boson. The CS polar angle analysis is more sensitive to the A_0 and A_4 angular coefficients (see [9,10] for a measurement of A_0). Because Eq. (1) arises solely from quantum field theory, without input from any specific theoretical model of W boson production, our experimental results are thus model-independent.

II. THE CDF DETECTOR AND EVENT SELECTION

A. The CDF detector

The Run I CDF detector is described in detail in [11]. It is a general purpose detector of charged leptons, hadrons,

jets, and photons, produced from proton-antiproton collisions at the Tevatron accelerator at Fermilab. The W and Z bosons are detected through their decay leptons, while the transverse momentum of the neutrinos is estimated from the missing transverse energy of the events (\cancel{E}_T).

The z -axis of the detector coincides with the direction of the proton beam and defines the polar angle θ_{lab} in the laboratory frame. The y -axis points vertically upward and the x -axis is in the horizontal plane, so as to form a right-handed coordinate system. The pseudorapidity, $\eta_{\text{lab}} = -\ln[\tan(\theta_{\text{lab}}/2)]$, and the azimuthal angle ϕ_{lab} are used to specify detector physical areas.

The tracking system of CDF consists of the silicon vertex detector (SVX), the vertex time projection chamber (VTX), and the central tracking chamber (CTC), all immersed in a 1.4 T magnetic field produced by a superconducting solenoid of length 4.8 m and radius 1.5 m. The SVX, a four layer silicon micro-strip vertex detector, is located immediately outside the beampipe. It is used to find secondary vertices and provides the impact parameter of tracks in the transverse $r - \phi_{\text{lab}}$ plane. The VTX, located outside the SVX, is a vertex time projection chamber that

provides $r - z$ tracking information up to a radius of 22 cm and pseudorapidity $|\eta_{\text{lab}}| \leq 3.5$. It measures the z -position of the primary vertex. Finally, surrounding the SVX and the VTX is the CTC, a 3.2 m long cylindrical drift chamber containing 84 layers of sense wires arranged in five superlayers of axial wires and four superlayers of stereo wires. The axial superlayers have 12 radially separated layers of sense wires, parallel to the z -axis, that measure the $r - \phi_{\text{lab}}$ position of the tracks. The stereo superlayers have six layers of sense wires with alternate $\sim \pm 3^\circ$ stereo angles with respect to the beamline, and measure a combination of $r - \phi_{\text{lab}}$ and z information. The stereo and axial data are combined to reconstruct the 3-dimensional track. The CTC covers the pseudorapidity interval $|\eta_{\text{lab}}| < 1.0$ and transverse momentum $p_T \geq 0.4$ GeV [12]. The combined momentum resolution of the tracking system is $\delta p_T/p_T = \sqrt{(0.0009 p_T)^2 + (0.0066)^2}$, where p_T is the transverse momentum in GeV.

The solenoid is surrounded by sampling calorimeters used to measure the electromagnetic and hadronic energy of electrons, photons, and jets. The calorimeters cover the pseudorapidity range $|\eta_{\text{lab}}| \leq 4.2$ and the azimuthal angle range $0 \leq \phi_{\text{lab}} \leq 2\pi$. They are segmented in $\eta_{\text{lab}} - \phi_{\text{lab}}$ towers pointing to the nominal interaction point at the center of the detector. The tower granularity is $(\Delta\eta_{\text{lab}} \times \Delta\phi_{\text{lab}}) = (0.1 \times 15^\circ)$ in the central region ($0 \leq |\eta_{\text{lab}}| \leq 1.1$) and $(0.1 \times 5^\circ)$ in the plug ($1.1 < |\eta_{\text{lab}}| \leq 2.4$) and forward ($2.4 < |\eta_{\text{lab}}| \leq 4.2$) regions. Each region has an electromagnetic calorimeter (CEM in the central region, PEM in the plug region, and FEM in the forward region) followed by a hadron calorimeter at larger radius from the beam (CHA, PHA, and FHA, respectively). The central calorimeters are segmented in 24 wedges per each half of the detector ($-1.1 \leq \eta_{\text{lab}} \leq 0$ and $0 \leq \eta_{\text{lab}} \leq 1.1$). The CEM is an 18 radiation length lead-scintillator stack with a position resolution of 2 mm and an energy resolution of $\delta E_T/E_T = \sqrt{(13.5\%/\sqrt{E_T})^2 + (2\%)^2}$, where E_T is the transverse energy in GeV. Located six radiation lengths deep inside the CEM calorimeter (184 cm from the beamline), proportional wire chambers (CES) with additional cathode strip readout provide shower position measurements in the z and $r - \phi_{\text{lab}}$ directions. The central hadron calorimeter (CHA) is an iron-scintillator stack which is 4.5 interaction lengths thick and provides energy measurement with a resolution of $\delta E_T/E_T = \sqrt{(50\%/\sqrt{E_T})^2 + (3\%)^2}$, where E_T is the transverse energy in GeV.

The central muon system consists of three components and is capable of detecting muons with transverse momentum $p_T \geq 1.4$ GeV and pseudorapidity $|\eta_{\text{lab}}| < 1.0$. The Central Muon Chambers (CMU) cover the region $|\eta_{\text{lab}}| < 0.6$ and consist of four layers of planar drift chambers outside the hadron calorimeter, allowing the reconstruction of the muons which typically pass the five absorption lengths of material. Outside the CMU there are three addi-

tional absorption lengths of material (0.6 m of steel) followed by four layers of drift chambers, the Central Muon Upgrade (CMP). The CMP chambers cover the same pseudorapidity region as the CMU, and they were introduced to limit the background caused from punch-through pions. Finally, the Central Muon Extension chambers (CMX) cover the region $0.6 \leq \eta_{\text{lab}} \leq 1.0$. These drift chambers are sandwiched between scintillators (CSX). Depending on the incident angle, particles have to penetrate six to nine absorption lengths of material to be detected in the CMX. The particle candidate stub provided by the muon system is matched with a track from the CTC in order to successfully reconstruct a muon.

B. The CDF triggers

CDF has a three-level trigger system designed to select events that can contain electrons, muons, jets, and \cancel{E}_T . The first two levels are implemented in hardware, while the third is a software trigger which uses a version of the offline reconstruction software optimized for speed and implemented by a CPU farm.

At level-1, electrons were selected by the presence of an electromagnetic trigger tower with energy above 6 GeV (Run Ia) or 8 GeV (Run Ib), where one trigger tower consisted of two adjacent physical towers (in pseudorapidity). Muons were selected by the presence of a track stub in the CMU, CMP, or CMX.

At level-2, electrons satisfied one of several triggers. In Run Ia, the event passed the trigger if the energy cluster in the CEM was at least 9 GeV with a seed tower of at least 7 GeV, and a matching track with $p_T > 9.2$ GeV was found by the Central Fast Tracker (CFT), the fast hardware processor that matched CTC tracks in the $r - \phi_{\text{lab}}$ plane with signals in the calorimeters and muon chambers. It also passed the trigger if there was an isolated cluster in the CEM calorimeter of at least 16 GeV. The most common Run Ib level-2 electron trigger requires the existence of a cluster in the CEM with at least 16 GeV and the existence of a matching track in the CFT with $p_T > 12$ GeV. The muon trigger at level-2 required a track of at least 9 GeV (Run Ia) or 12 GeV (Run Ib) that matched a CMX stub (CMX triggers), both CMU and CMP stubs (CMUP triggers), or a CMU stub but no CMP stub (CMNP triggers).

At level-3, reconstruction programs performed 3-dimensional track reconstruction. In the Run Ia level-3 electron trigger, most of the accepted events passed the requirement that the CEM cluster had $E_T > 18$ GeV, and was associated with a track of $p_T > 13$ GeV. The transverse energy of the cluster is defined as $E_T = E \sin\theta$, where E is the total energy deposited in the CEM, and θ is the polar angle measured from the event vertex to the centroid of the cluster. Cuts were applied on the shape of the electron shower profile and the energy deposition patterns. In the Run Ib level-3 electron trigger, CEM $E_T > 18$ GeV and CFT $p_T > 13$ GeV requirements were ap-

plied. The muon trigger at level-3 required that the CFT transverse momentum was greater than 18 GeV, the energy deposited in the hadron calorimeter was less than 6 GeV, the energy deposited in the electromagnetic calorimeter was less than 2 GeV, and the extrapolated CTC track was no more than 2 cm away from the muon stub in the CMU chambers and 5 cm in the CMP or CMX chambers in the x direction. Events that pass the level-3 trigger were recorded to tape for offline analysis.

C. The datasets

The events passing the three levels of our trigger system constitute the inclusive high- p_T electron and muon data samples. We apply kinematic and lepton identification cuts, described in Sections IIC 1 and IIC 2 to obtain the inclusive W electron and muon datasets, respectively. Using these datasets we arrive at the W + jet datasets by applying the jet selection cuts described in Section IIC 3.

1. Inclusive W electron selection

After passing the three levels of trigger requirements, the following event selection cuts are applied to the inclusive electron data sample:

- (a) The event must belong to a good run; some runs are not acceptable, because the beam was not stable, or at least one major part of the detector or data acquisition systems did not operate properly.
- (b) $E_T^e \geq 20$ GeV, where E_T^e is the transverse energy of the CEM cluster, corrected for differences in response, nonlinearities, and time-dependent changes.
- (c) $|\eta_{\text{lab}}^e| \leq 1$, where η_{lab}^e is the pseudorapidity of the electron.
- (d) The electron must fall in a fiducial part of the CEM calorimeter.
- (e) $\text{ISO}(0.4) \equiv E_{\Delta R=0.4}^{\text{Excess}}/E_T^{\text{cluster}} < 0.1$, where $E_{\Delta R=0.4}^{\text{Excess}}$ is the excess transverse energy (with respect to the electron's cluster transverse energy) in a cone of size $\Delta R = \sqrt{(\Delta\phi_{\text{lab}})^2 + (\Delta\eta_{\text{lab}})^2} = 0.4$ centered on the direction of the electromagnetic cluster, and E_T^{cluster} is the transverse energy of that cluster.
- (f) $E^{\text{HAD}}/E^{\text{EM}} < 0.055 + 0.00045E^e$, where E^{HAD} is the energy deposited in the hadron calorimeter, and E^{EM} is the energy deposited in the electromagnetic calorimeter.
- (g) $L_{\text{SHR}} \equiv 0.14 \sum_i \frac{E_i^{\text{meas}} - E_i^{\text{exp}}}{\sqrt{(0.14)^2 E_i^{\text{meas}} + (\Delta E_i^{\text{exp}})^2}} < 0.2$, where L_{SHR} is the *lateral shower profile*, E_i^{meas} is the energy measured in the i th-tower adjacent to the seed tower, E_i^{exp} is the expectation for the energy in that tower, ΔE_i^{exp} is the uncertainty on the expected energy, and $0.14\sqrt{E_i^{\text{meas}}}$ is the uncertainty in the measurement of the cluster energy.
- (h) $\chi_{\text{CES}}^2 < 10$. We measure the shower profile along the z direction using the CES strips and the shower profile along the x direction using the CES wires.

By comparing the measured x -shape and z -shape to the ones determined from test-beam studies we extract the chi-squared quantities for the two directions. The chi-squared we use is the average of the two.

- (i) $0.5 \leq E^e/p^e \leq 2.0$, where E^e is the corrected energy of the electron, and p^e is the beam-constrained momentum of the electron, i.e., the momentum determined when the fit trajectory of the CTC hits is constrained to pass through the beam line.
- (j) $|\Delta X| < 1.5$ cm and $|\Delta Z| < 3.0$ cm, where ΔX and ΔZ are the difference in the x and z directions, respectively, between the extrapolated CTC track and the CES position of the shower.
- (k) $|Z_{\text{VTX}}| \leq 60$ cm, where Z_{VTX} is the z position of the primary vertex.
- (l) Photon conversions are removed.

We next apply the following cuts:

- (a) $\cancel{E}_T > 20$ GeV, where \cancel{E}_T is the missing transverse energy in the event, calculated from the energy imbalance in the calorimeters, with a correction for the unclustered energy—calorimeter energy not taken into account by the jet clustering algorithm—and possible presence of muons.
- (b) $M_T^W > 40$ GeV, where M_T^W is the W transverse mass. This cut removes the background from W bosons decaying into tau leptons which subsequently decay into electrons.
- (c) The event must not be consistent with a Z decaying into two observed leptons, or a Z in which one of the decay tracks has not been identified.

The 73 363 events passing these cuts constitute our inclusive W electron data sample (Run Ia: 13 290 events and Run Ib: 60 073 events), corresponding to an integrated luminosity of 110 pb^{-1} (Run Ia: $19.65 \pm 0.71 \text{ pb}^{-1}$ and Run Ib: $90.35 \pm 3.70 \text{ pb}^{-1}$).

2. Inclusive W muon selection

After passing the three levels of trigger requirements, the following event selection cuts are applied to the inclusive muon data sample:

- (a) The event must belong to a good run.
- (b) $p_T^\mu \geq 20$ GeV, where p_T^μ is the beam-constrained transverse momentum of the muon (determined by a fit to the CTC hits, constrained by the beam line).
- (c) The muon must be fiducial and central (pseudorapidity $|\eta_{\text{lab}}^\mu| \leq 1$).
- (d) $\text{ISO}(0.4) \equiv E_{\Delta R=0.4}^{\text{Excess}}/p_T^\mu < 0.1$, where $E_{\Delta R=0.4}^{\text{Excess}}$ is the excess transverse energy (with respect to the muon's cluster transverse energy) in a cone of size $\Delta R = \sqrt{(\Delta\phi_{\text{lab}})^2 + (\Delta\eta_{\text{lab}})^2} = 0.4$ centered on the direction of the muon.
- (e) $E_{\text{HAD}} \leq 6$ GeV, where E_{HAD} is the energy deposited in the hadron calorimeter tower traversed by the muon.

- (f) $E_{\text{EM}} \leq 2$ GeV, where E_{EM} is the energy deposited in the electromagnetic calorimeter tower traversed by the muon.
- (g) $|\Delta X_{\text{CMU}}| < 2$ cm, $|\Delta X_{\text{CMP}}| < 5$ cm, $|\Delta X_{\text{CMX}}| < 5$ cm, where ΔX_{CMU} , ΔX_{CMP} , and ΔX_{CMX} are the differences between the x position of the stub in the muon chambers and the extrapolation of the CTC track to these muon chambers.
- (h) $|Z_{\text{VTX}}| \leq 60$ cm.
- (i) The event must pass the cosmic ray filter; if the muon track and another track can be fit as one continuous track consistent with a cosmic ray, the event is removed.
- (j) The impact parameter must be $|d_0| \leq 0.2$ cm.
- (k) $|Z_0 - Z_{\text{VTX}}| \leq 5$ cm, where Z_0 is the z -position of the muon track. This cut, combined with the previous two, significantly reduces the cosmic muon background.

We next apply the following cuts, as in the electron case:

- (a) $\cancel{E}_T > 20$ GeV.
- (b) $M_T^W > 40$ GeV.
- (c) The event must not be consistent with a Z decaying into two observed leptons, or a Z in which one of the decay tracks has not been identified.

The 38 601 events passing these cuts constitute our inclusive W muon data sample [Run Ia (CMUP): 4441 events, Run Ia (CMNP): 955 events, Run Ib (CMUP): 20 527 events, Run Ib (CMNP): 3273 events, and Run Ib (CMX): 9405 events], corresponding to an integrated luminosity of 107 pb^{-1} [Run Ia (CMUP): $18.33 \pm 0.66 \text{ pb}^{-1}$, Run Ia (CMNP): $19.22 \pm 0.69 \text{ pb}^{-1}$, Run Ib (CMUP): $88.35 \pm 3.62 \text{ pb}^{-1}$, Run Ib (CMNP): $89.20 \pm 3.66 \text{ pb}^{-1}$, and Run Ib (CMX): $88.98 \pm 3.65 \text{ pb}^{-1}$].

3. Inclusive W + jet event selection

Our final analysis dataset consists of those W events which include at least one jet with $E_T^{\text{jet}} > 15$ GeV, $|\eta_{\text{lab}}^{\text{jet}}| < 2.4$, and $\Delta R_{l-j}^{\text{lab}} > 0.7$, where $\Delta R_{l-j}^{\text{lab}} \equiv \sqrt{(\Delta \eta_{l-j}^{\text{lab}})^2 + (\Delta \phi_{l-j}^{\text{lab}})^2}$, and $\Delta \eta_{l-j}^{\text{lab}}$ and $\Delta \phi_{l-j}^{\text{lab}}$ are the differences in pseudorapidity and polar angle between the charged lepton and the jet in the laboratory frame. The results of the analysis pertain to the W^- boson. All W^+ bosons in the sample are CP transformed to be treated as W^- bosons [13].

These requirements leave 12 676 electron W + jet events and 6941 muon W + jet events, with $15 < p_T^W < 105$ GeV, where p_T^W is the transverse momentum of the W boson, defined as the vector sum of the \cancel{E}_T and charged lepton transverse momenta. The data event yields for the four p_T^W bins ($15 < p_T^W < 25$ GeV, $25 < p_T^W < 35$ GeV, $35 < p_T^W < 65$ GeV, and $65 < p_T^W < 105$ GeV) are presented in Table I.

The actual number of events is not of critical importance for us, because we are interested in the shape of the dis-

TABLE I. The electron (N_e) and muon (N_μ) CDF data event yields for inclusive W + jet production. The muon event yields are lower relative to the electron event yields, due to lower muon efficiencies and acceptances.

Data event yields for inclusive W + jet production		
p_T^W (GeV)	N_e	N_μ
15–25	5166	2821
25–35	3601	1869
35–65	3285	1880
65–105	624	371

tributions and not the absolute event yields. We thus analyze the distributions normalized to unity. We will come back to the actual event yields after the inclusion of the background (Section V) and systematic uncertainties (Section IX).

III. THE MONTE CARLO SIMULATION

A. The DYRAD Monte Carlo event generator

DYRAD [14] is the next-to-leading order W + jet event generator used to establish the SM prediction. We include the “1-loop” processes, since these affect the next-to-leading order angular coefficients and more completely simulate the events we study. This generator is of order α_s^2 in QCD, generating up to two jets passing the minimal requirement of $E_T^{\text{jet}} > 10$ GeV if the Feynman diagram does not contain any gluon loops, and generates up to one jet with the same requirement if a gluon loop is present in the Feynman diagram. As a result, DYRAD does not appropriately model events with more than two jets. These extra jets in the data occupy low and high values of the azimuthal angle ϕ in our CS frame. We are careful not to bias our measurement due to this effect (see Section VIII). The jet transverse energy cut of 10 GeV is required because the theoretical calculations are unreliable for small jet transverse energies due to infrared and collinear divergencies. A jet-jet angular separation cut of greater than 0.7 in $\eta_{\text{lab}}-\phi_{\text{lab}}$ space is imposed, which is important for the definition of a jet. No additional kinematic cuts for the jet, charged lepton, and neutrino are required in order to obtain a reliable theoretical prediction of the angular distribution of the W . The cross section for inclusive W + jet production calculated up to order α_s^2 is 722.51 ± 3.89 pb for W^- and W^+ bosons combined. The uncertainty is statistical from the MC integration; the systematic one will be presented in Sections IX F and IX G. This simulation uses $Q^2 = (M_W^{\text{pole}})^2$, where $M_W^{\text{pole}} = 80.3$ GeV is the pole mass of the W , CTEQ4M($\Lambda = 0.3$ GeV) parton distribution functions [15], and 0.7-cone jets in $\eta_{\text{lab}}-\phi_{\text{lab}}$ space.

In order to obtain smooth SM kinematic distributions up to $p_T^W = 100$ GeV, and especially smooth $\cos\theta$ vs ϕ distributions for different p_T^W regions, we generated a large

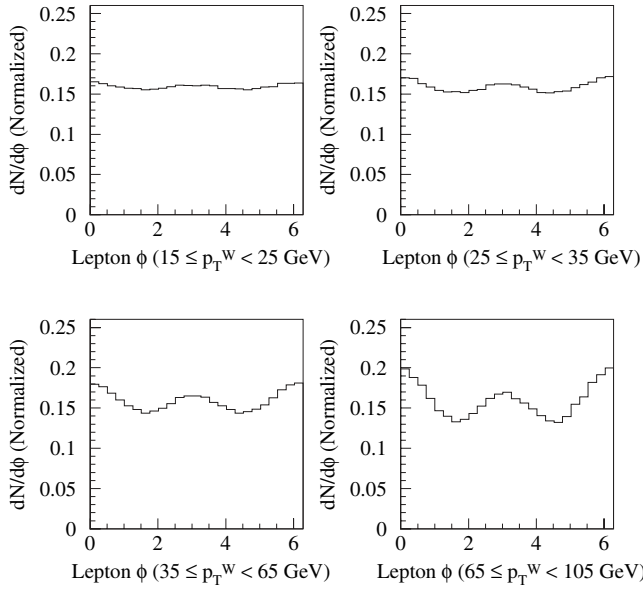


FIG. 2. The theoretical charged lepton ϕ distribution in the Collins-Soper W rest-frame for the four p_T^W regions, as generated by DYRAD. The distributions are normalized to unity.

sample of DYRAD events (~ 250 M). This Monte Carlo event sample size was required since events with negative weights, corresponding to the gluon loop matrix elements, produce significant fluctuations in the kinematic distributions with limited statistics. The DYRAD simulation allows us to establish the SM prediction for the ϕ distribution of the charged lepton and the predictions for the angular coefficients and helicity cross sections of the W up to order α_s^2 [7]. The generator-level ϕ distributions for four p_T^W bins are shown in Fig. 2. For zero p_T^W we expect a flat distribution, whereas the QCD effects at higher p_T^W result in two minima. In order to simulate the detector response, we pass the generator events through the fast Monte Carlo detector simulator, described in the next section.

B. The fast Monte Carlo detector simulation

The fast Monte Carlo (FMC) CDF detector simulation includes the detailed geometry of the detector, geometrical, and kinematic acceptances of all subdetectors, detector resolution effects parametrized using Gaussians obtained explicitly from data, detailed magnetic field map, and multiple Coulomb scattering effects. The integrated luminosities, lepton identification and trigger efficiencies, and all experimental cuts imposed on the W , leptons, \cancel{E}_T , and jets are incorporated. The effect of the underlying event, caused by interacting spectator quarks, is also included. The FMC program receives the particle four-momenta for each generated DYRAD event along with the next-to-leading order cross section prediction from DYRAD (which includes gluon loop effects) and produces kinematic distributions smeared by detector resolution, and

TABLE II. The electron (N_e) and muon (N_μ) FMC event yields for inclusive $W + \text{jet}$ production up to order α_s^2 . Contributions from backgrounds are not included yet. The uncertainties in the event yield predictions are dominated by the uncertainties associated with integrated luminosities, lepton identification and trigger efficiencies, and the DYRAD prediction of the $W + \text{jet}$ production cross section. Systematic uncertainties associated with PDF choice and Q^2 scale variation are not included yet. The event yields are estimated for an electron luminosity of 110 pb^{-1} and a muon luminosity of 107 pb^{-1} .

FMC event yields for inclusive $W + \text{jet}$ production

p_T^W (GeV)	N_e	N_μ
15–25	3867 ± 137	2027 ± 102
25–35	2632 ± 93	1384 ± 66
35–65	2474 ± 87	1314 ± 67
65–105	518 ± 18	279 ± 14

sculpted by geometrical and kinematic acceptances and efficiencies. The FMC also reports event yield predictions. The FMC successfully reproduces the kinematic features of inclusive W and Z boson production, as well as the features of vector boson production in association with a jet [8,16].

For the $W + \text{jet}$ data, we additionally require at least one “good” jet ($E_T^{\text{jet}} > 15 \text{ GeV}$ and $|\eta_{\text{lab}}^{\text{jet}}| < 2.4$) that also passes the $\Delta R_{l-j}^{\text{lab}} > 0.7$ cut, where $\Delta R_{l-j}^{\text{lab}}$ is the opening angle in $\eta_{\text{lab}} - \phi_{\text{lab}}$ space between the lepton and the leading good jet. The FMC event yields for inclusive $W + \text{jet}$ production up to order α_s^2 are presented in Table II. The

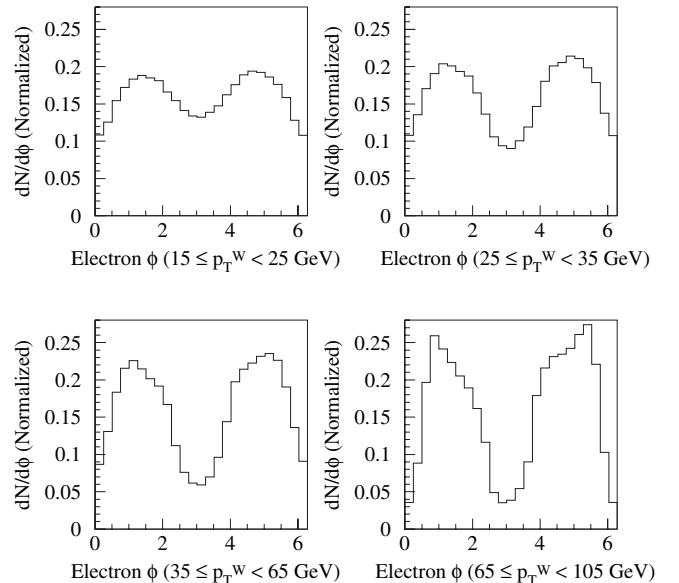


FIG. 3. The expected CDF electron ϕ distribution in the Collins-Soper W rest-frame for the four p_T^W regions, after experimental cuts and detector smearing, as generated by the FMC. The distributions are normalized to unity. The muon distributions are almost identical.

Parton Distribution Functions (PDF) systematics and the renormalization and factorization scale (Q^2) systematics will be included in Section VI.

The FMC detector simulation, along with DYRAD, shows how the acceptances and efficiencies of the detector and the analysis cuts affect the ϕ distributions that are experimentally observed. Figure 3 shows the expected measurement of the ϕ distributions for the electron dataset (the muon distributions are almost identical) for the four p_T^W bins. The effects of the acceptances and efficiencies are significant; instead of two minima we observe two maxima. The main reason for this is the charged lepton and neutrino p_T cuts, which limit the allowed $(\cos\theta, \phi)$ phase space considerably. The FMC plots are normalized to the FMC signal event yields, and all experimental cuts have been applied.

IV. ACCEPTANCES AND EFFICIENCIES

The lepton identification and trigger efficiencies are measured by using the leptons from CDF Run Ia and Ib Z data and by studying random-cone distributions of leptonic W and Z decay Run Ia and Ib data samples. The kinematic and geometrical acceptances are calculated using the DYRAD event generator, which produces the SM prediction, and the FMC detector simulation, which produces the CDF experimental expectation.

We are especially interested in the product of overall acceptance times efficiency (ae) as a function of $(\cos\theta, \phi)$ associated with each of the four p_T^W bins. We create 2-

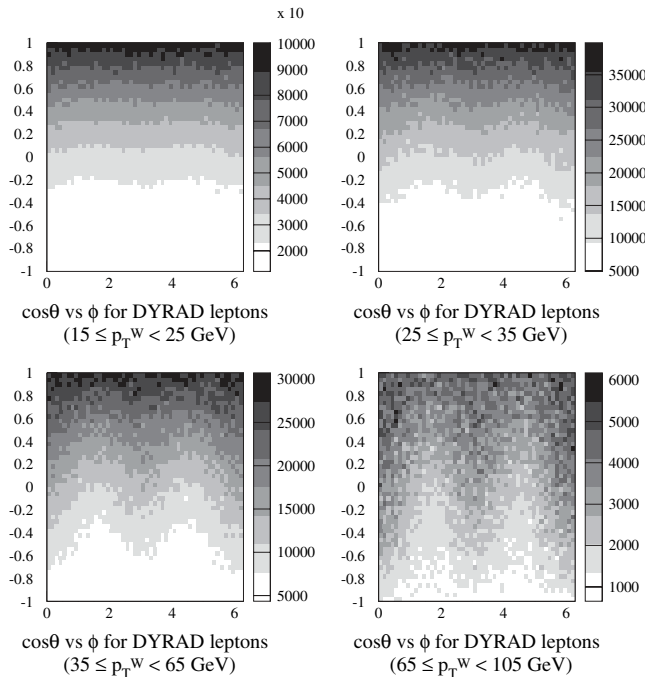


FIG. 4. The $\cos\theta$ vs ϕ phase space for the four p_T^W bins, for the DYRAD generator simulation (arbitrary units).

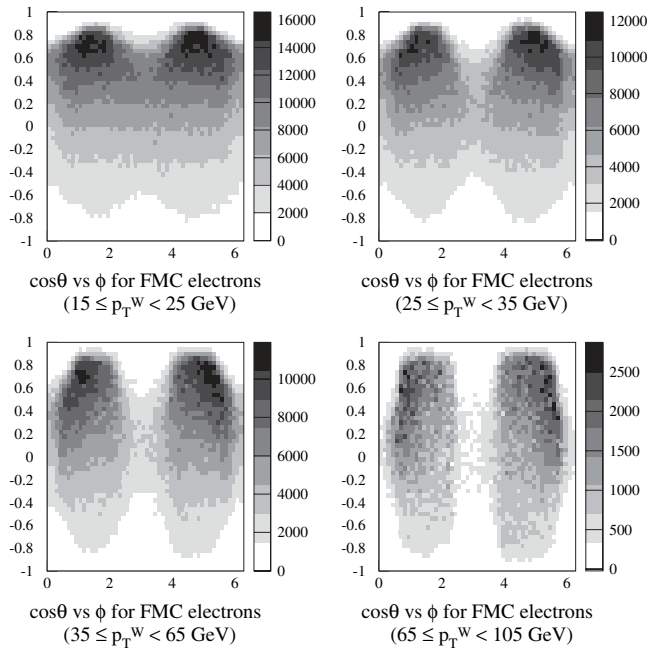


FIG. 5. The $\cos\theta$ vs ϕ phase space for the four p_T^W bins, for the electron FMC signal simulation (arbitrary units).

dimensional histograms of $\cos\theta$ vs ϕ for each of the four p_T^W bins, using the DYRAD simulation. This procedure is repeated using the FMC simulation, where the appropriate mixture of Run Ia and Run Ib W leptons is used, based on FMC event yield predictions.

The resulting plots are shown in Figs. 4–6 for DYRAD, FMC-electrons, and FMC-muons, respectively. We subse-

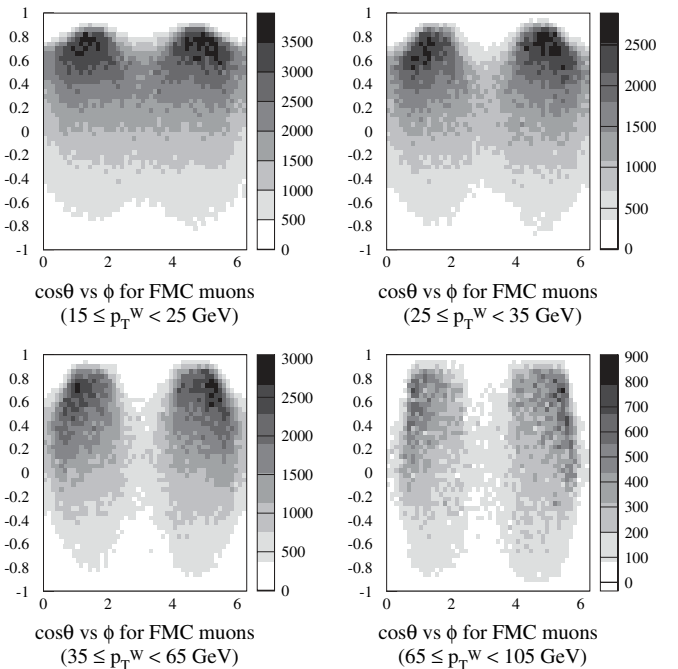


FIG. 6. The $\cos\theta$ vs ϕ phase space for the four p_T^W bins, for the muon FMC signal simulation (arbitrary units).

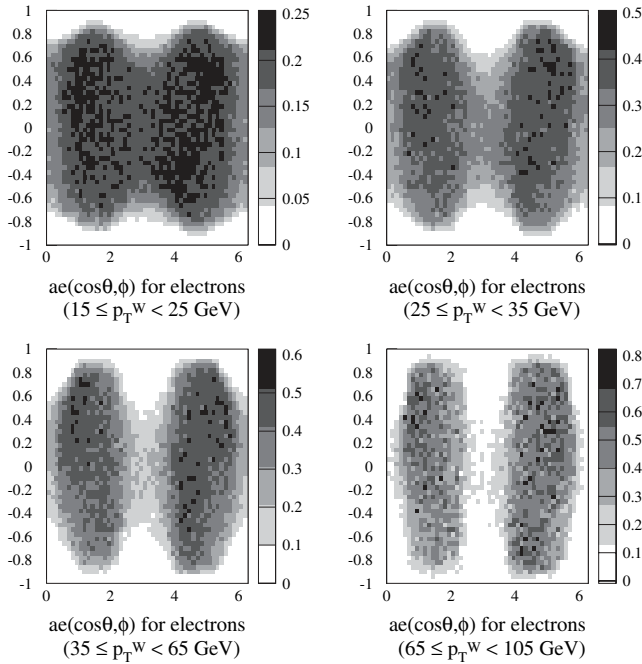


FIG. 7. Acceptance times efficiency for the electrons as a function of $\cos\theta$ and ϕ in the Collins-Soper frame.

quently divide the FMC 2-dimensional histograms by the corresponding DYRAD ones, producing the 2-dimensional differential acceptance times efficiency $ae(\cos\theta, \phi)$ of Figs. 7 and 8, for electrons and muons, respectively. The overall acceptance times efficiency is higher for the electrons. These $ae(\cos\theta, \phi)$ values are used for the

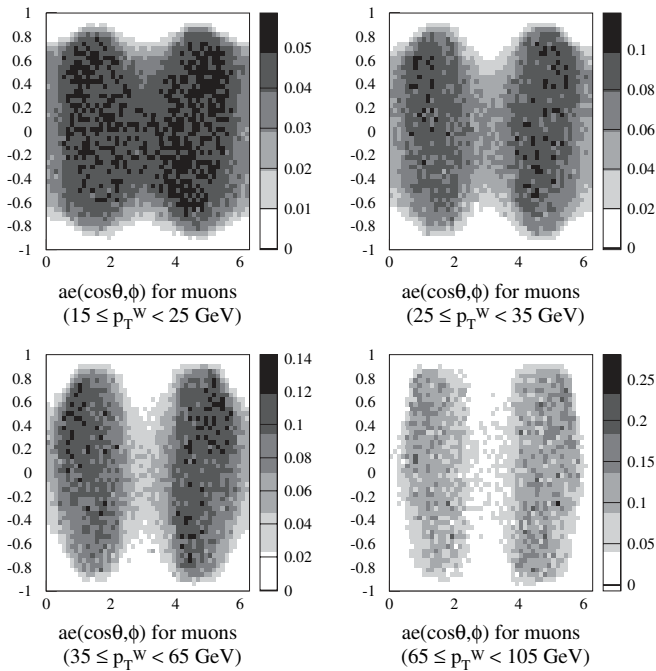


FIG. 8. Acceptance times efficiency for the muons as a function of $\cos\theta$ and ϕ in the Collins-Soper frame.

$\cos\theta$ -integration of the cross section, as described in Section VII.

V. BACKGROUND ESTIMATION

The main sources of background in the $(W \rightarrow e\nu_e) + \text{jet}$ and $(W \rightarrow \mu\nu_\mu) + \text{jet}$ processes are $Z + \text{jets}$ events where the Z is misidentified as a W (“one-legged” Z), $(W \rightarrow \tau\nu_\tau) + \text{jet}$ events, and QCD background resulting from jet misidentification. The $W + \gamma$ background is only a few events with run and event numbers the same as the $W + \gamma$ events of [16]; it is treated as a systematic uncertainty, which also gives an indication of the radiative effects in the measurement. This uncertainty is very small (see Section IX).

A small background contribution arises from $t\bar{t}$ production, where one of the produced W bosons decays leptonically and the other W boson decays hadronically to jets. This background is estimated to be 30 ± 7 events for the electron sample [17] and 16 ± 3 events for the muon sample, a 0.3% effect. An equally small background is the $Z \rightarrow \tau^+\tau^-$ production, where one of the tau leptons decays hadronically and the other one leptonically. This background is estimated to be 47 ± 1 events in the electron sample [17], and 25 ± 1 events in the muon sample, a 0.5% effect. To demonstrate the insignificance of the $t\bar{t}$ and $Z \rightarrow \tau^+\tau^-$ backgrounds, we perform our analysis including the charged lepton ϕ distribution for these background events, in several possible shapes, for the four p_T^W bins. The resulting change in the extracted values of the angular coefficients is negligible compared to our systematic and statistical uncertainties. Thus, we ignore the backgrounds associated with $t\bar{t}$ production and $Z \rightarrow \tau^+\tau^-$ decays.

Finally, the cosmic ray background in the muon $W + \text{jet}$ datasets is estimated to be significantly less than 0.1%, and is therefore neglected.

A. One-legged Z background

To study this background we generate a DYRAD sample of $Z + \text{jet}$ events and pass it through the FMC Monte Carlo simulation and the subsequent analysis program. This predicts how many Z bosons are misidentified as W bosons. In these cases, the Z bosons satisfy all kinematic and lepton identification cuts for W bosons, but one of their decay leptons, or *legs*, is undetected. The DYRAD cross section for $Z + \text{jet}$ up to order α_s^2 is 68.21 ± 0.37 pb. For this DYRAD simulation we used $Q^2 = (M_Z^{\text{pole}})^2 = 91.2$ GeV, the CTEQ4M($\Lambda = 0.3$ GeV) parton distribution functions, 0.7-cone jets, jet-jet angular separation greater than 0.7 in $\eta_{\text{lab}} - \phi_{\text{lab}}$ space, and $E_T^j > 10$ GeV. At the FMC level, we impose our usual W boson event selection cuts and additionally require at least one good jet ($E_T^{\text{jet}} > 15$ GeV and $|\eta_{\text{lab}}^{\text{jet}}| < 2.4$) that also passes the $\Delta R_{l-j}^{\text{lab}} > 0.7$ cut. These results are summarized in Table III. Overall we expect 123 ± 5 electron one-legged- $Z + \text{jet}$

TABLE III. Monte Carlo background estimation of the number of electron and muon one-legged $Z + \text{jet}$ events. The background fractions are calculated with respect to the FMC $W + \text{jet}$ event yields.

One-legged $Z + \text{jet}$ background				
p_T^W (GeV)	N_e	Fraction	N_μ	Fraction
15–25	47 ± 2	$1.22 \pm 0.07\%$	127 ± 7	$6.26 \pm 0.47\%$
25–35	30 ± 1	$1.14 \pm 0.05\%$	82 ± 4	$5.92 \pm 0.40\%$
35–65	25 ± 1	$1.01 \pm 0.05\%$	72 ± 4	$5.48 \pm 0.41\%$
65–105	5 ± 0	$0.96 \pm 0.03\%$	12 ± 1	$4.30 \pm 0.42\%$

events and 337 ± 18 muon one-legged- $Z + \text{jet}$ events passing the $W + \text{jet}$ cuts, without applying any cut on the W transverse momentum. Comparing these numbers to the FMC event yields for $W + \text{jet}$, the one-legged- $Z + \text{jet}$ background is $(1.14 \pm 0.06)\%$ for the electron $W + \text{jet}$ and $(5.90 \pm 0.43)\%$ for the muon $W + \text{jet}$ sample. This background is higher for the muon sample, because of the limited coverage of the muon chambers, which is responsible for higher yields of one-legged muon Z bosons.

To examine how this background affects the $W + \text{jet}$ lepton ϕ distribution, we plot the ϕ distribution for the leptons from these processes for the four p_T^W bins (Figs. 9 and 10). We see that the same pattern of two maxima at $\frac{\pi}{2}$ and $\frac{3\pi}{2}$ is present. The background plots are normalized to the expected event yields from the FMC, multiplied by a

factor of 5 (to make them visible), and superimposed on the signal FMC distributions, normalized to the signal FMC event yields. We include the one-legged Z FMC ϕ distribution in the complete theoretical prediction of the ϕ distributions, in order to correctly extract the angular coefficients.

B. ($W \rightarrow \tau\nu$) + jet background

If the W boson decays to a τ that subsequently decays leptonically, the three final neutrinos contribute to the \cancel{E}_T , which is incorrectly associated with a single neutrino. The signal of one charged lepton along with the \cancel{E}_T mimics that of a W directly decaying to the charged lepton. Most of the tau background is removed when we utilize the fact that the charged lepton and \cancel{E}_T coming from the τ decay are soft. As a result, the W transverse mass in the τ events is significantly smaller than that in the electron or muon events. By applying the p_T cuts for the leptons and the W transverse mass cut, we remove 92% of the tau $W + \text{jet}$ events at the DYRAD generator level.

To study the remaining tau background we start with a tau $W + \text{jet}$ DYRAD sample ($Q^2 = (M_W^{\text{pole}})^2$, CTEQ4M($\Lambda = 0.3 \text{ GeV}$) parton distribution function, and 0.7-cone jets in $\eta_{\text{lab}} - \phi_{\text{lab}}$ space), and we let the tau decay to an electron or a muon. We then vector-sum the three neutrinos resulting from the W and tau decays to form

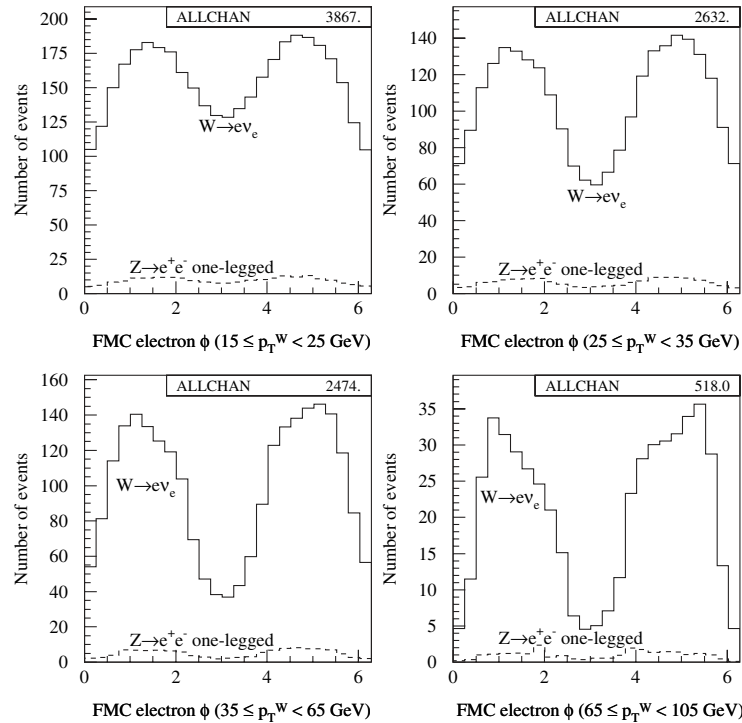


FIG. 9. Electron ϕ distributions for the four p_T^W bins for electron $W + \text{jet}$ FMC events (solid histogram) and for $Z + \text{jet}$ FMC background (multiplied by 5), where one of the electrons from the Z decay is undetected and the other one passes the detection and analysis requirements (dashed histogram). The histograms are normalized to the electron FMC signal event yields.

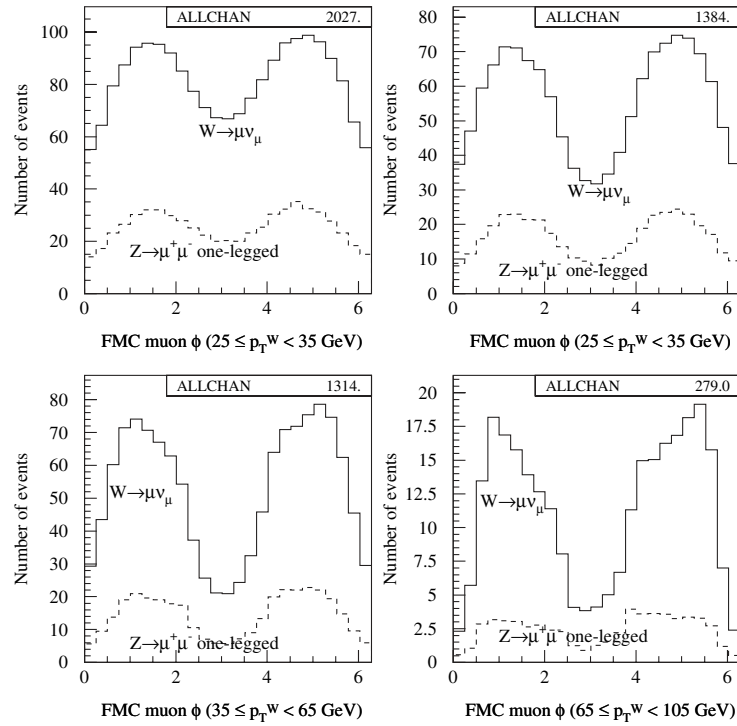


FIG. 10. Muon ϕ distributions for the four p_T^W bins for muon W + jet FMC events (solid histogram) and for Z + jet FMC background (multiplied by 5), where one of the muons from the Z decay is undetected and the other one passes the detection and analysis requirements (dashed histogram). The histograms are normalized to the muon FMC signal event yields.

a single \cancel{E}_T . Subsequently, we pass the events through the FMC detector simulator to see how many events pass the W + jet cuts after they are weighted by the detector acceptances and efficiencies. The branching ratios for the tau decays we use are 17.83% for electrons and 17.37% for muons [18]. At the FMC level, we require at least one good jet ($E_T^{\text{jet}} > 15$ GeV and $|\eta_{\text{lab}}^{\text{jet}}| < 2.4$) that also passes the $\Delta R_{l-j}^{\text{lab}} > 0.7$ cut. The tau background results are presented in Table IV. Overall we expect 247 ± 9 tau electrons and 130 ± 7 tau muons to infiltrate the W + jet samples, without applying any cut on the W transverse momentum. Comparing these numbers to the FMC event yields for the electron and muon W + jet samples, the tau back-

ground is $(2.28 \pm 0.12)\%$ for the electron W + jet sample, and $(2.28 \pm 0.17)\%$ for the muon W + jet sample.

To see how this background affects the W + jet lepton ϕ distribution, we plot the ϕ distribution for the leptons resulting from leptonic tau decays in W + jets events for the four p_T^W bins (Figs. 11 and 12). We see that the pattern of two maxima at $\frac{\pi}{2}$ and $\frac{3\pi}{2}$ is again present. The background plots are normalized to the expected event yields from the FMC, multiplied by a factor of 5, and superimposed on the signal FMC distributions, normalized to the signal FMC event yields. We include the τ -background FMC ϕ distribution in the complete theoretical prediction of the ϕ distributions, in order to correctly extract the angular coefficients.

C. QCD background

The QCD background in the case of inclusive W production and decay consists predominantly of dijet events, where one of the jets is misidentified as a lepton and the other one is not detected, resulting in the creation of \cancel{E}_T . In the W + jet case, the QCD background is multijet events, where at least one of the jets is detected, at least one is lost or mismeasured (resulting in \cancel{E}_T) and one is misidentified as a charged lepton to erroneously reconstruct a W . The number and distribution of QCD background events in the four p_T^W bins are determined from the Run Ia and Run Ib CDF data.

TABLE IV. Monte Carlo background estimation of the number of electron and muon W + jet events, where the W decays to a tau and the electron or muon is the decay product of the tau. The fractions of the backgrounds are calculated with respect to the FMC W + jet event yields.

$(W \rightarrow \tau \bar{\nu}_\tau \rightarrow \bar{\nu}_\tau \nu_\tau \bar{\nu}_{e/\mu} e/\mu) + \text{jet background}$				
p_T^W (GeV)	N_e	Fraction	N_μ	Fraction
15–25	86 ± 3	$2.22 \pm 0.11\%$	45 ± 2	$2.22 \pm 0.15\%$
25–35	57 ± 2	$2.16 \pm 0.10\%$	30 ± 2	$2.17 \pm 0.18\%$
35–65	56 ± 2	$2.26 \pm 0.11\%$	30 ± 2	$2.28 \pm 0.19\%$
65–105	15 ± 1	$2.89 \pm 0.22\%$	8 ± 0	$2.87 \pm 0.14\%$

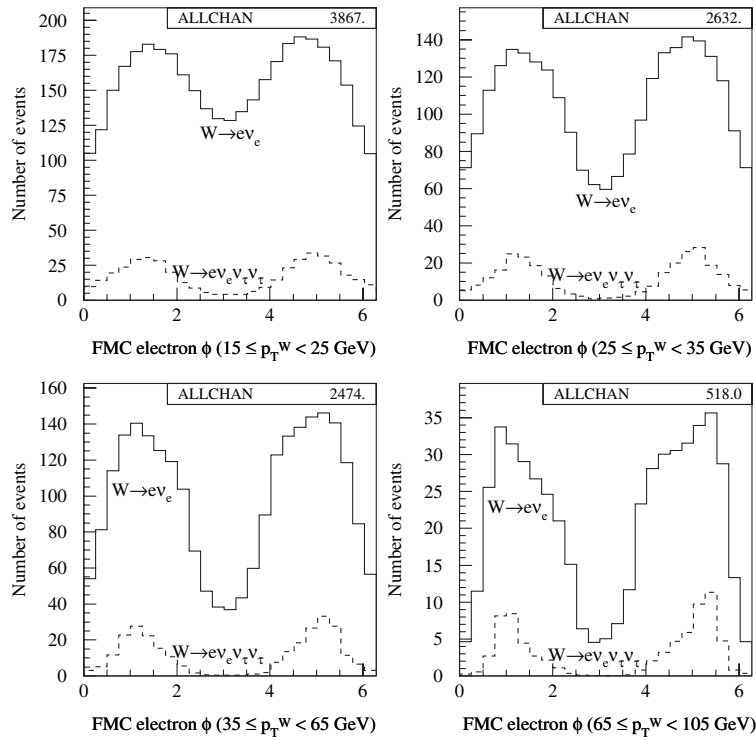


FIG. 11. Electron ϕ distributions for the four p_T^W bins for electron $W + \text{jet}$ FMC events (solid histogram) and for tau $W + \text{jet}$ FMC background (multiplied by 5), where the tau decays to an electron (dashed histogram). The histograms are normalized to the FMC signal event yields.

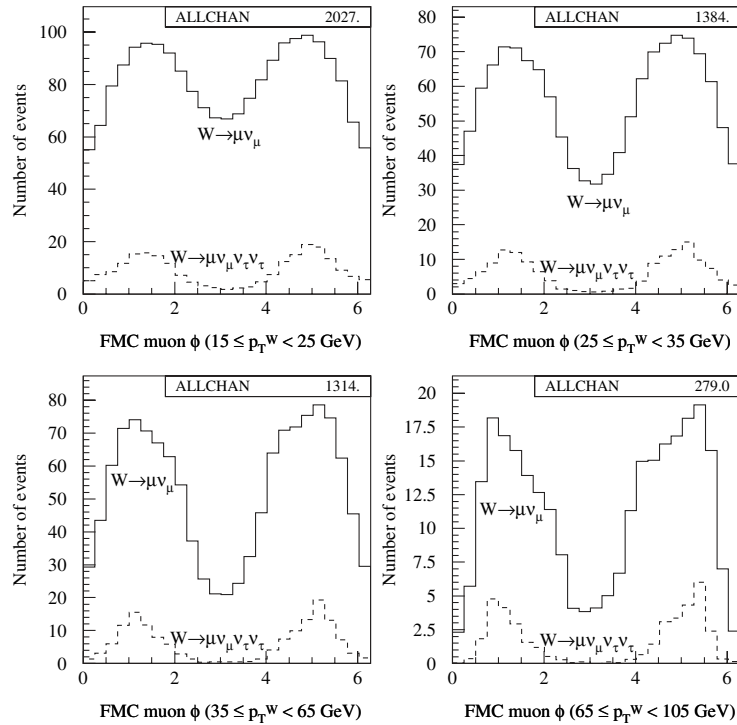


FIG. 12. Muon ϕ distributions for the four p_T^W bins for muon $W + \text{jet}$ FMC events (solid histogram) and for tau $W + \text{jet}$ FMC background (multiplied by 5), where the tau decays to a muon (dashed histogram). The histograms are normalized to the FMC signal event yields.

To measure the expected number of QCD background events in our data samples we look at leptons with isolation (ISO), defined in Section II, greater than 0.2. Our signal is in the $\text{ISO} < 0.1$ region and most of the events with lepton $\text{ISO} > 0.2$, but not all of them, are QCD background events. The upper histogram of Fig. 13 shows the isolation distribution of the electrons from $W + \text{jet}$ events, for the first p_T^W bin. When plotted on a semilog scale, the $\text{ISO} < 0.1$ and the $\text{ISO} > 0.2$ regions can be approximated with two straight lines. The technique we use extrapolates the $\text{ISO} > 0.2$ line into the $\text{ISO} < 0.1$ signal region to calculate its integral and obtain the number of events in the signal region, using the assumption that the QCD background shape is not altered in that region. This method would give us the true number of QCD background events, if the $\text{ISO} > 0.2$ region was filled exclusively with QCD events. In reality, only a fraction of these events are true QCD background, the rest being $W + \text{jet}$ events. Since we expect to have some $W + \text{jet}$ events in the region of lepton isolation from 0.1 to 0.2, we fit the area above 0.2 with a straight line (in the semilog histogram), which describes the QCD background. We also fit five continuous regions of lepton isolation, around the central region of $\text{ISO} = 0.20$ to $\text{ISO} = 0.65$ (namely 0.15–0.65, 0.25–0.65, 0.15–0.60, 0.20–0.65, and 0.25–0.70) to obtain a systematic uncertainty for this procedure.

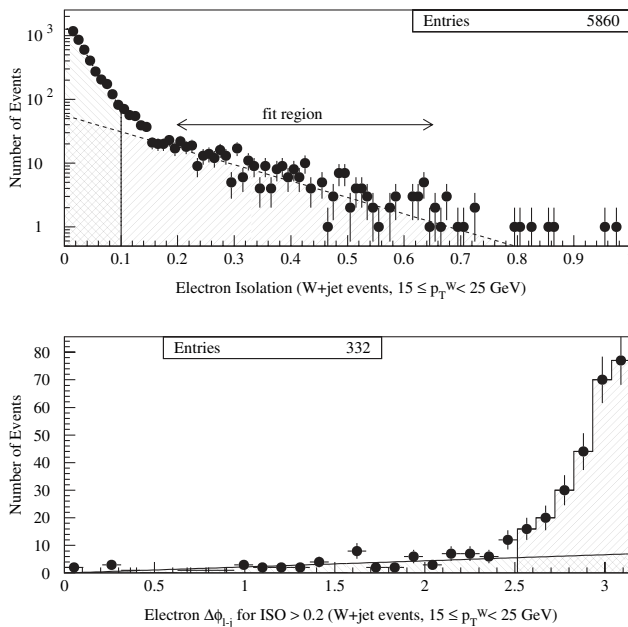


FIG. 13. Isolation of the electron in $W + \text{jet}$ events (upper histogram) and the difference in the azimuthal angles of the electron and the jet for high isolation events (lower histogram). These histograms are used to estimate the QCD background in the electron $W + \text{jet}$ data, for the $15 \leq p_T^W \leq 25$ GeV bin (see text). Corresponding histograms are used for the estimation of the QCD background in the three other electron $W + \text{jet}$ p_T^W bins.

Since not all of the extrapolated region is QCD background, we obtain a measurement of the percentage of the true QCD background in the electron $W + \text{jet}$ sample above electron isolation of 0.1, by making a histogram of $\Delta\phi_{l-j}^{\text{lab}}$ for the events with $\text{ISO} > 0.2$, where $\Delta\phi_{l-j}^{\text{lab}}$ is the difference in the ϕ angle between the electron and the highest- E_T jet, with no other requirements for that jet. We expect the $\Delta\phi_{l-j}^{\text{lab}}$ distribution to be almost flat for the $W + \text{jet}$ events, because no correlation exists between the jet and the lepton ϕ directions. In reality, this distribution decreases at low $\Delta\phi_{l-j}^{\text{lab}}$, due to the application of the lepton isolation cut in our data. For QCD background, we expect the $\Delta\phi_{l-j}^{\text{lab}}$ between the highest E_T jet and the jet resembling the lepton to peak at π . The lower histogram of Fig. 13 shows the $\Delta\phi_{l-j}^{\text{lab}}$ for the events with lepton isolation greater than 0.2 for electron $W + \text{jet}$ events and for the first p_T^W bin. We fit the region $\Delta\phi_{l-j}^{\text{lab}} \leq 2.5$ ($W + \text{jet}$ contribution) with a straight line. The region of the histogram $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ above that line corresponds to true QCD background. By dividing this part of the histogram by the total number of events with $\text{ISO} > 0.2$, we determine the true fraction of QCD background in the $\text{ISO} > 0.2$ region. We expect the same fraction to be valid in the signal region ($\text{ISO} < 0.1$). Therefore, the number of true QCD background events is obtained by multiplying the number of originally estimated QCD events with $\text{ISO} < 0.1$ (as obtained by extrapolating the $\text{ISO} > 0.2$ line into the signal region of the lepton isolation plot) by the QCD background fraction obtained from the $\Delta\phi_{l-j}^{\text{lab}}$ plot. The procedure is repeated for the four p_T^W bins. Table V shows the extracted fraction of QCD background in the $\text{ISO} > 0.2$ region for the four p_T^W bins. The electron $W + \text{jet}$ QCD background results are presented in Table VI.

In the study of the QCD background in the muon sample we face a new problem. We originally apply a cut to muon $W + \text{jet}$ data (`zmuo_veto`) in order to remove events that are consistent with the production of a Z boson, where one of the muons is nonisolated because it fails one (and only one) of the following cuts:

- The muon isolation cut $\text{ISO} < 0.1$
- The electromagnetic calorimeter cut $E^{\text{EM}} < 2$ GeV
- The hadron calorimeter cut $E^{\text{HAD}} < 6$ GeV

These dimuon events are true Z bosons that look like W bosons because one muon does not pass one of the above cuts due to inner bremsstrahlung or bremsstrahlung in the electromagnetic or hadronic calorimeters. The `zmuo_veto` cut mainly affects the tail of the muon isolation distribution ($\text{ISO} > 0.2$) and causes us to underestimate the QCD background, since we use that tail to estimate it. Therefore, for the muon $W + \text{jet}$ samples, for the purposes of determination of QCD background, we neglect this cut, in order to remove this bias at high muon isolation ($\text{ISO} > 0.2$) and make the transition from the low to high isolation smooth. Some of the muon Z background is thus counted as QCD

TABLE V. The linear least-squares fit parametrization of the $\Delta\phi_{l-j}^{\text{lab}}$ distribution for $\text{ISO} > 0.2$ electron $W + \text{jet}$ events (second column) allows us to estimate the number of $\text{ISO} > 0.2$ $W + \text{jet}$ events in the $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ region. The integral of this line, divided by the bin width ($\pi/30$) of the $\Delta\phi_{l-j}^{\text{lab}}$ histogram, is the number of $W + \text{jet}$ events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ shown in the third column. These events are subtracted from the total number of ($W + \text{jet} + \text{QCD}$) background events in the $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ region (fourth column). The result is divided by the total number of events in the $\text{ISO} > 0.2$ region, to obtain an estimate of the fraction of true QCD background events (fifth column).

p_T^W (GeV)	Fit parameterization of electron $W + \text{jet}$ events with $\text{ISO} > 0.2$	Electron $W + \text{jet}$ events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$	($W + \text{jet}$) + QCD events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$	Fraction of true QCD events
15–25	$2.21 \times \Delta\phi_{l-j}^{\text{lab}} - 0.05$	37.9	257	$0.66 = (257 - 37.9)/332$
25–35	$0.70 \times \Delta\phi_{l-j}^{\text{lab}} + 0.78$	16.9	98	$0.58 = (98 - 16.9)/141$
35–65	$1.04 \times \Delta\phi_{l-j}^{\text{lab}} + 0.45$	20.6	49	$0.31 = (49 - 20.6)/91$
65–105	$0.17 \times \Delta\phi_{l-j}^{\text{lab}} + 0.73$	7.5	10	$0.13 = (10 - 7.5)/20$

TABLE VI. The number of electron $W + \text{jet}$ events, the number of QCD background events before correction and their percentage in the signal region, and the fraction of true QCD background events and their percentage in the signal region, for the four p_T^W bins (see text for details).

p_T^W (GeV)	Number of electron $W + \text{jet}$	QCD events before correction	Percentage of QCD before correction	Fraction of true QCD events	Percentage of QCD background
15–25	5166	423^{+77}_{-42}	$8.18^{+1.11}_{-0.81}\%$	$0.66^{+0.04}_{-0.04}$	$5.40^{+0.80}_{-0.63}\%$
25–35	3601	353^{+26}_{-148}	$9.80^{+0.74}_{-4.1}\%$	$0.58^{+0.07}_{-0.08}$	$5.68^{+0.81}_{-2.50}\%$
35–65	3285	54^{+151}_{-25}	$1.64^{+4.60}_{-0.75}\%$	$0.31^{+0.13}_{-0.13}$	$0.51^{+1.44}_{-0.32}\%$
65–105	624	14^{+8}_{-3}	$2.24^{+1.24}_{-0.27}\%$	$0.13^{+0.87}_{-0.13}$	$0.29^{+1.96}_{-0.29}\%$

background; however we do not expect it to radically affect our QCD background estimation. In the isolation method we fit the background starting from $\text{ISO} = 0.17$ to $\text{ISO} = 0.40$, to increase the statistical significance of our estimation. We also fit five continuous regions of lepton isolation, around the central region of $\text{ISO} = 0.17$ to $\text{ISO} = 0.40$ (namely 0.16–0.40, 0.18–0.40, 0.16–0.35, 0.17–0.40, and 0.18–0.45) to obtain a systematic uncertainty for this procedure. The upper histogram of Fig. 14 shows the isolation distribution and fits for the muon $W + \text{jet}$ events and for the first p_T^W bin.

We obtain a measurement of the percentage of the true QCD background in the muon $W + \text{jet}$ sample above muon isolation of 0.2, by making a histogram of $\Delta\phi_{l-j}^{\text{lab}}$ for the events with $\text{ISO} > 0.2$, where $\Delta\phi_{l-j}^{\text{lab}}$ is the difference in the ϕ angle between the muon and the highest- E_T jet, with no other requirements for that jet. The lower histogram of Fig. 14 shows $\Delta\phi_{l-j}^{\text{lab}}$ for the events with isolation greater than 0.2 for muon $W + \text{jet}$ events, for the first p_T^W bin. The peak in the $\Delta\phi_{l-j}^{\text{lab}} = 0$ region is due to the muon bremsstrahlung processes that are not suppressed after we relax the zmuo_veto cut. We ignore these events when we fit to the straight line describing the $W + \text{jet}$ events with high isolation muons. Table VII shows the extracted fraction of QCD background in the $\text{ISO} > 0.2$ region for the four p_T^W bins. The muon $W + \text{jet}$ QCD background results are presented in Table VIII. For the highest muon p_T^W bin the predicted number of true $W + \text{jet}$ events is greater than the total number of events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$,

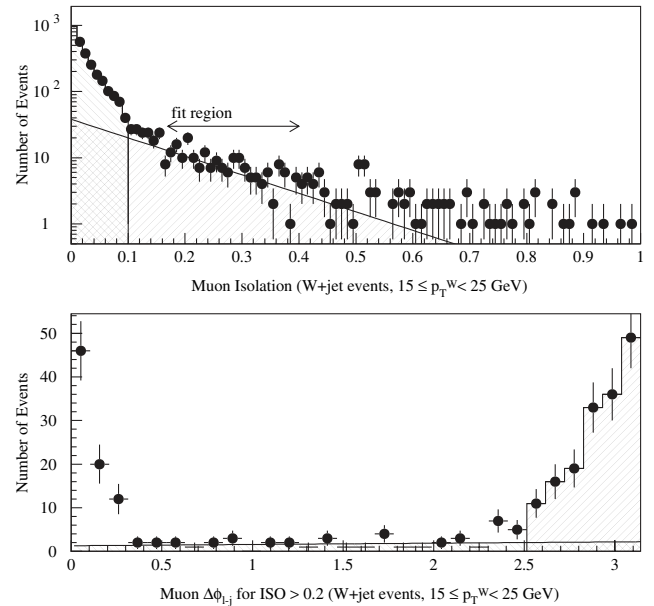


FIG. 14. Isolation of the muon in $W + \text{jet}$ events (upper histogram) and the difference in the azimuthal angles of the muon and the jet for high isolation events (lower histogram). These histograms are used to estimate the QCD background in the muon $W + \text{jet}$ data, for the $15 \leq p_T^W \leq 25$ GeV bin (see text). Corresponding histograms are used for the estimation of the QCD background in the three other muon $W + \text{jet}$ p_T^W bins. At low $\Delta\phi_{l-j}^{\text{lab}}$ the distribution increases, due to bremsstrahlung processes associated with residual muon $Z + \text{jet}$ background in the muon $W + \text{jet}$ sample. These events disappear if we apply the zmuo_veto cut (see text).

TABLE VII. The linear least-squares fit parametrization of the $\Delta\phi_{l-j}^{\text{lab}}$ distribution for $\text{ISO} > 0.2$ muon $W + \text{jet}$ events (second column) allows us to estimate the number of $\text{ISO} > 0.2$ $W + \text{jet}$ events in the $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ region. The integral of this line, divided by the bin width ($\pi/30$) of the $\Delta\phi_{l-j}^{\text{lab}}$ histogram, is the number of $W + \text{jet}$ events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ shown in the third column. These events are subtracted from the total number of ($W + \text{jet} + \text{QCD}$) background events in the $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ region (fourth column). The result is divided by the total number of events in the $\text{ISO} > 0.2$ region, to obtain an estimate of the fraction of true QCD background events (fifth column).

p_T^W (GeV)	Fit parametrization of muon $W + \text{jet}$ events with $\text{ISO} > 0.2$	Muon $W + \text{jet}$ events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$	($W + \text{jet}$) + QCD events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$	Fraction of true QCD events
15–25	$0.29 \times \Delta\phi_{l-j}^{\text{lab}} + 1.31$	13	164	$0.52 = (164 - 13)/288$
25–35	$0.46 \times \Delta\phi_{l-j}^{\text{lab}} + 0.79$	12.8	69	$0.40 = (69 - 12.8)/140$
35–65	$0.25 \times \Delta\phi_{l-j}^{\text{lab}} + 1.02$	10.5	19	$0.14 = (19 - 10.5)/61$
65–105	$0 \times \Delta\phi_{l-j}^{\text{lab}} + 1$	6.1	1	$0 = 0/6$

TABLE VIII. The number of muon $W + \text{jet}$ events without the application of the `zmuo_veto` cut, the number of QCD background events before correction and their percentage in the signal region, and the fraction of true QCD background events and their percentage in the signal region, for the four p_T^W bins (see text for details).

p_T^W (GeV)	Number of muon $W + \text{jet}$	QCD events before correction	Percentage of QCD before correction	Fraction of true QCD events	Percentage of QCD background
15–25	2779	280^{+102}_{-25}	$10.07^{+3.68}_{-0.90}\%$	$0.52^{+0.05}_{-0.04}$	$5.24^{+1.98}_{-0.62}\%$
25–35	1943	103^{+129}_{-4}	$5.30^{+6.64}_{-0.21}\%$	$0.40^{+0.08}_{-0.08}$	$2.12^{+2.69}_{-0.43}\%$
35–65	2002	139^{+50}_{-21}	$6.94^{+2.50}_{-1.05}\%$	$0.14^{+0.22}_{-0.14}$	$0.97^{+1.57}_{-0.97}\%$
65–105	389	11^{+0}_{-0}	$2.70^{+0.00}_{-0.00}\%$	0^{+1}_{-0}	$0^{+2.7}_{-0}\%$

which results in a fraction of true QCD background events above $\text{ISO} > 0.2$ equal to zero.

After we calculate the percentage of the QCD background in the signal region, we multiply it by the CDF $W + \text{jet}$ event yields to obtain the absolute prediction of the number of QCD background events in each of the four p_T^W bins, for both and electron and muon $W + \text{jet}$ data. The results are presented in Table IX.

To complete the study of the QCD background we need to estimate its shape to properly include this background in the standard model prediction of the lepton ϕ distribution in the CS frame, for each of the four p_T^W bins. We plot ϕ for the events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ for the electrons and muon datasets, as shown in Figs. 15 and 16, respectively. We fit the distributions to the sum of two Gaussians and two straight lines. For the last p_T^W bin of the electrons and the last two p_T^W bins of the muons, there

TABLE IX. QCD background estimation for the electron and muon $W + \text{jet}$ events. The fractions of the backgrounds are calculated with respect to the CDF Data $W + \text{jet}$ events.

QCD background				
p_T^W (GeV)	N_e	Fraction	N_μ	Fraction
15–25	279^{+41}_{-33}	$5.40^{+0.80}_{-0.63}\%$	148^{+56}_{-17}	$5.24^{+1.98}_{-0.62}\%$
25–35	205^{+29}_{-90}	$5.68^{+0.81}_{-2.50}\%$	40^{+50}_{-8}	$2.12^{+2.69}_{-0.43}\%$
35–65	17^{+47}_{-11}	$0.51^{+1.44}_{-0.32}\%$	18^{+30}_{-18}	$0.97^{+1.57}_{-0.97}\%$
65–105	2^{+12}_{-2}	$0.29^{+1.96}_{-0.29}\%$	0^{+10}_{-0}	$0^{+2.7}_{-0}\%$

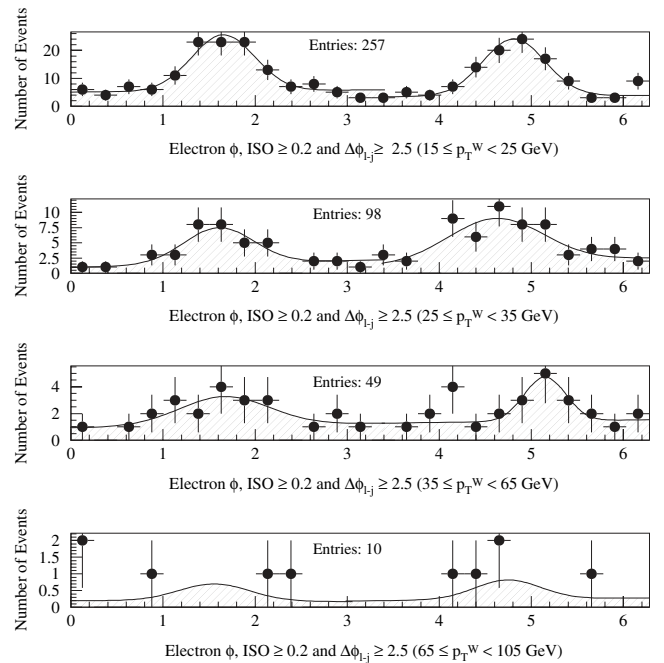


FIG. 15. The Collins-Soper ϕ distribution of electrons from $W + \text{jet}$ events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{lab}} > 2.5$ for each of the four p_T^W bins. These events are predominantly QCD background events. We fit the distribution of the first three p_T^W bins with two Gaussians on top of two straight lines. For the highest p_T^W bin we use the distribution of the total QCD background, normalized to the number of the QCD events in this bin (see text for details).

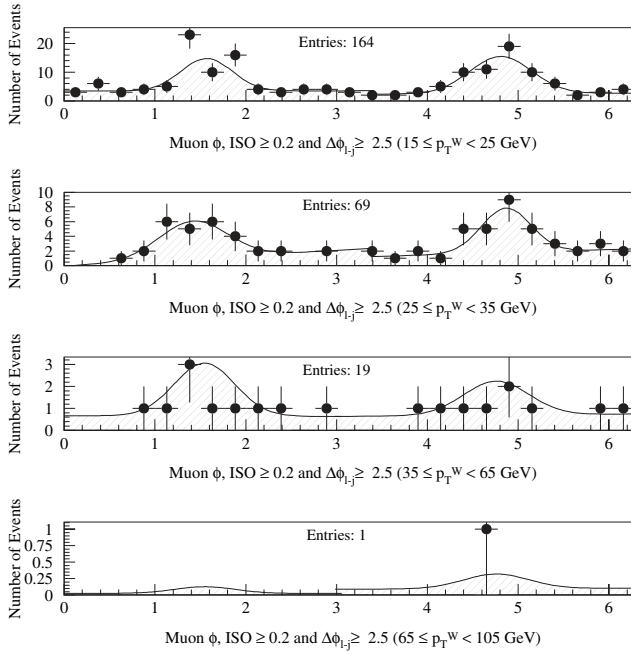


FIG. 16. The Collins-Soper ϕ distribution of muons from $W + \text{jet}$ events with $\text{ISO} > 0.2$ and $\Delta\phi_{l-j}^{\text{ab}} > 2.5$ for each of the four p_T^W bins. These events are predominantly QCD background events. We fit the distribution of the first two p_T^W bins with two Gaussians on top of two straight lines. For the two highest p_T^W bins we use the distribution of the total background, normalized to the number of the QCD events in those bins.

are not enough statistics for the fit, so we use the total distributions (for $15 \leq p_T^W \leq 105$ GeV) normalized to the number of events for those high p_T^W bins. We do not expect the shape of the QCD background to be significantly

altered with increasing p_T^W . We assume that these distributions are the same as the ones in the signal region ($\text{ISO} < 0.1$) after they are properly normalized. We use these distributions to add the QCD background to the standard model prediction, after they are normalized to the expected number of QCD background events, given by Table IX.

D. Summary of backgrounds and standard model event yields prediction

Backgrounds for electron and muon $W + \text{jet}$ events for each of the four p_T^W bins are summarized in Tables X and XI, respectively. We obtain the total $W + \text{jet}$ event yield prediction by adding these backgrounds to the FMC $W + \text{jet}$ signal prediction of Table II. To obtain the final uncertainties, we add linearly the uncertainties associated with the $W + \text{jet}$ signal and electroweak background and add the result to the QCD background uncertainty in quadrature. The total $W + \text{jet}$ event yields after the inclusion of the backgrounds are presented in Table XII. The PDF and Q^2 systematic uncertainties are also included (see Section IX).

VI. COMPARISON BETWEEN EXPECTED AND OBSERVED W DISTRIBUTIONS

We study the expected (FMC) W kinematical distributions after the inclusion of backgrounds and compare them to the experimental distributions. Figures 17 and 18 show the W transverse momentum for electrons and muons, respectively. The observed and simulated distributions have been normalized to unity. We observe good agreement between the observed and simulated p_T^W distributions. Figure 19 shows the W transverse mass distribution

TABLE X. Summary of electron $W + \text{jet}$ backgrounds. The background fractions are calculated with respect to the FMC signal event yields for the electroweak backgrounds and with respect to the data for the QCD background.

Electron $W + \text{jet}$ Backgrounds				
Background	$p_T^W = 15\text{-}25$ GeV	$p_T^W = 25\text{-}35$ GeV	$p_T^W = 35\text{-}65$ GeV	$p_T^W = 65\text{-}105$ GeV
$W \rightarrow \tau\nu_\tau$	86 ± 3 (2.22%)	57 ± 2 (2.16%)	56 ± 2 (2.26%)	15 ± 1 (2.89%)
$Z \rightarrow e^+e^-$	47 ± 2 (1.22%)	30 ± 1 (1.14%)	25 ± 1 (1.01%)	5 ± 0 (0.96%)
QCD	279^{+41}_{-33} (5.40%)	205^{+29}_{-90} (5.68%)	17^{+47}_{-11} (0.51%)	2^{+12}_{-2} (0.29%)

TABLE XI. Summary of muon $W + \text{jet}$ backgrounds. The background fractions are calculated with respect to the FMC signal event yields for the electroweak backgrounds and with respect to the data for the QCD background.

Muon $W + \text{jet}$ Backgrounds				
Background	$p_T^W = 15\text{-}25$ GeV	$p_T^W = 25\text{-}35$ GeV	$p_T^W = 35\text{-}65$ GeV	$p_T^W = 65\text{-}105$ GeV
$W \rightarrow \tau\nu_\tau$	45 ± 2 (2.22%)	30 ± 2 (2.17%)	30 ± 2 (2.28%)	8 ± 0 (2.87%)
$Z \rightarrow \mu^+\mu^-$	127 ± 7 (6.26%)	82 ± 4 (5.92%)	72 ± 4 (5.48%)	12 ± 1 (4.30%)
QCD	148^{+56}_{-17} (5.24%)	40^{+50}_{-8} (2.12%)	18^{+30}_{-18} (0.97%)	0^{+10}_{-0} (0%)

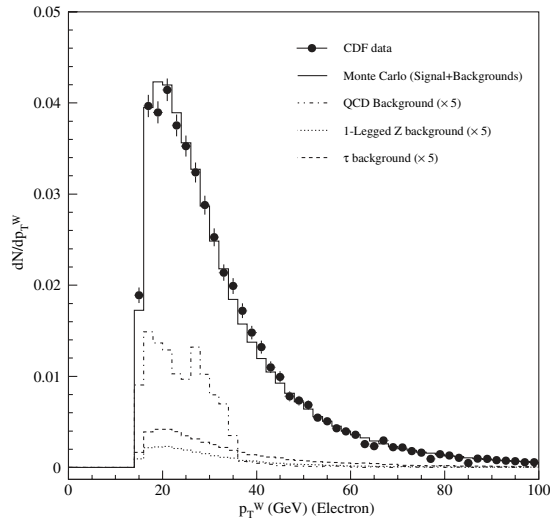


FIG. 17. The transverse momentum of the W for the electron $W + \text{jet}$ data sample (points) along with the FMC signal simulation including backgrounds (solid histogram). The backgrounds are multiplied by 5, to be visible. The data and expected signal + background distributions are normalized to unity.

for the electron $W + \text{jet}$ dataset and for the DYRAD events passed through the FMC detector simulation. Figure 20 shows the same distributions for the four p_T^W bins. Figures 21 and 22 show the same distributions for the muon $W + \text{jet}$ datasets. The observed and simulated distributions are again normalized to unity. In all of the above

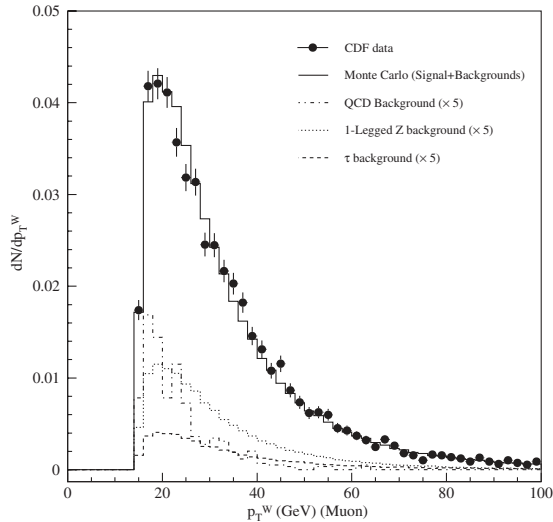


FIG. 18. The transverse momentum of the W for the muon $W + \text{jet}$ data sample (points) along with the FMC signal simulation including backgrounds (solid histogram). The backgrounds are multiplied by 5, to be visible. The data and expected signal + background distributions are normalized to unity.

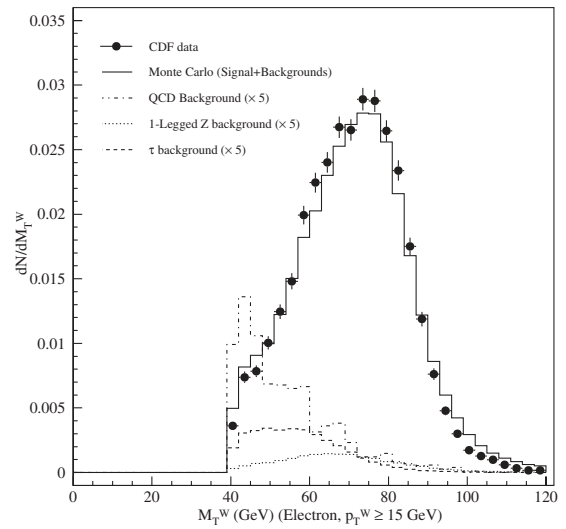


FIG. 19. The transverse mass of the W for the electron $W + \text{jet}$ data sample (points) along with the FMC signal simulation including backgrounds (solid histogram). The backgrounds are multiplied by 5, to be visible. The data and expected signal + background distributions are normalized to unity.

plots, the FMC distributions are produced with properly weighted signal and background contributions, for electron and muon detector regions.

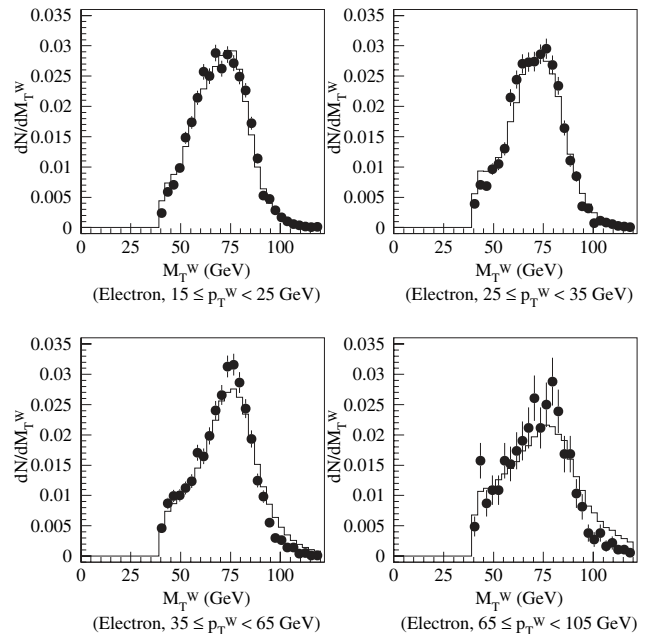


FIG. 20. The transverse mass of the W for the electron $W + \text{jet}$ data sample (points) along with the FMC signal simulation including backgrounds (histogram), for the four p_T^W bins. The data and expected signal + background distributions are normalized to unity.

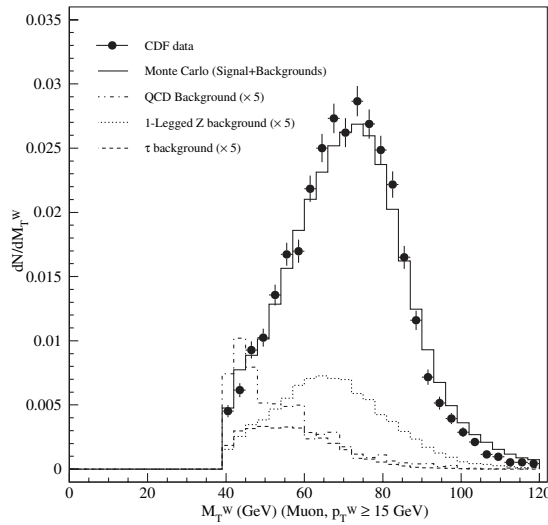


FIG. 21. The transverse mass of the W for the muon W + jet data sample (points) along with the FMC signal simulation including backgrounds (solid histogram). The backgrounds are multiplied by 5, to be visible. The data and expected signal + background distributions are normalized to unity.

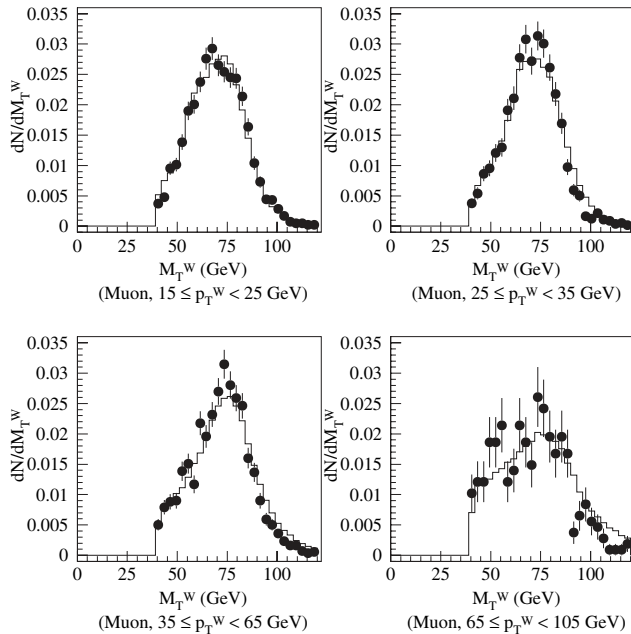


FIG. 22. The transverse mass of the W for the muon W + jet data sample (points) along with the FMC signal simulation including backgrounds (histogram), for the four p_T^W bins. The data and expected signal + background distributions are normalized to unity.

VII. DIRECT MEASUREMENT OF THE AZIMUTHAL ANGLE OF THE CHARGED LEPTONS FROM W DECAYS IN THE COLLINS-SOPER FRAME

For each W event we boost to the W rest-frame to calculate the azimuthal angle of the charged lepton. The longitudinal momentum of the W (p_z^W) is not known, because the longitudinal momentum of the neutrino is not measurable, so we use the mass of the W to constrain it. For a particular event, the longitudinal momentum of the neutrino is constrained by the mass of the W , according to the equation:

$$p_z^\nu = \frac{1}{(2p_T^l)^2} \left(A p_z^l \pm E^l \sqrt{A^2 - 4(p_T^l)^2 (p_T^\nu)^2} \right) = f(M_W), \quad (2)$$

where

$$A = M_W^2 + (p_T^W)^2 - (p_T^l)^2 - (p_T^\nu)^2, \quad (3)$$

E^l is the energy of the charged lepton, p_T^l is its transverse momentum, p_z^l is its longitudinal momentum, p_T^ν is the neutrino transverse momentum, and p_T^W is the transverse momentum of the W . This equation is unique for every event, since the kinematics of the lepton and neutrino, as well as the mass of the W , contribute to the shape of the curve $p_z^\nu = f(M_W)$. If the mass of the W was known on an event-by-event basis, there would be a two-fold ambiguity in the value of p_z^ν of the neutrino in the laboratory frame. Because the W boson has a finite width given by a PDF-convoluted Breit-Wigner distribution, $BW(M_W)$, we actually have two *distributions* of possible values of p_z^ν , $BW(M_W)f(M_W)$.

The choice of one of the two neutrino longitudinal momentum solutions does not affect the ϕ analysis, since both solutions result in the same charged lepton ϕ in the CS frame. For this analysis, only the choice of the W mass is of interest. The choice is made based on the 2-dimensional M^W vs M_T^W histograms constructed with DYRAD events. For a specific M_T^W we use a probability distribution of W masses and randomly select one for each event, based on that distribution. This method was devised to better reconstruct the $|\cos(\theta)|$ distribution [8], since the polar angle is very sensitive to the selection of the W mass. In our analysis, the azimuthal angle is not affected by the choice of mass, so the answer is almost the same even if we choose a mass based on the Breit-Wigner distribution and the requirement that the mass is greater than the measured transverse mass.

After obtaining a ϕ for every event, we proceed to analyze our sample. Theoretically, the W differential cross section, integrated over $\cos\theta$ and y is given by:

$$\frac{d\sigma}{d(p_T^W)^2 d\phi} = C(1 + \beta_1 \cos\phi + \beta_2 \cos 2\phi + \beta_3 \sin\phi + \beta_4 \sin 2\phi), \quad (4)$$

where

$$C = \frac{1}{2\pi} \frac{d\sigma}{d(p_T^W)^2}, \quad \beta_1 = \frac{3\pi}{16} A_3(p_T^W),$$

$$\beta_2 = \frac{A_2(p_T^W)}{4}, \quad \beta_3 = \frac{3\pi}{16} A_7(p_T^W), \quad \beta_4 = \frac{A_5(p_T^W)}{2}. \quad (5)$$

The theoretical ϕ distributions for the charged lepton from W boson decay in W + jet production are shown in Fig. 2.

From Eqs. (4) and (5), the reader might conclude that only the A_2 , A_3 , A_5 , and A_7 coefficients are measurable with the ϕ analysis, since the other angular coefficients are integrated out. However, in the actual W + jet data samples, what we measure is the number of events:

$$N(p_T^W, \phi) = \int \frac{d\sigma}{d(p_T^W)^2 d\phi d\cos\theta} ae(p_T^W, \cos\theta, \phi) d\cos\theta$$

$$\times \int \mathcal{L} dt + N_{bg}(p_T^W, \phi), \quad (6)$$

where \mathcal{L} is the instantaneous luminosity and $ae(p_T^W, \cos\theta, \phi)$ is the overall acceptance times efficiency, determined in Section IV, for a particular W transverse momentum and region in the $(\cos\theta, \phi)$ phase space. The quantity $N_{bg}(p_T^W, \phi)$ is the background for the given ϕ bin and p_T^W , estimated in Section V. Combining Eqs. (6) and (1), the measured distribution is

$$N(p_T^W, \phi) = C'(f_{-1}(p_T^W, \phi) + \sum_{i=0}^7 A_i(p_T^W) f_i(p_T^W, \phi))$$

$$+ N_{bg}(p_T^W, \phi), \quad (7)$$

where $C' = C \int \mathcal{L} dt$. The f_i are fitting functions, which are integrals of the product of the explicit functions $g_i(\cos\theta, \phi)$ and $ae(\cos\theta, \phi)$:

$$f_i(p_T^W, \phi) = \int_0^\pi g_i(\theta, \phi) ae(p_T^W, \cos\theta, \phi) d\cos\theta, \quad (8)$$

$$i = -1, \dots, 7,$$

where

$$g_{-1}(\theta, \phi) = 1 + \cos^2\theta, \quad g_0(\theta, \phi) = \frac{1}{2}(1 - 3\cos^2\theta),$$

$$g_1(\theta, \phi) = \sin 2\theta \cos\phi, \quad g_2(\theta, \phi) = \frac{1}{2}\sin^2\theta \cos 2\phi,$$

$$g_3(\theta, \phi) = \sin\theta \cos\phi, \quad g_4(\theta, \phi) = \cos\theta, \quad (9)$$

$$g_5(\theta, \phi) = \sin^2\theta \sin 2\phi, \quad g_6(\theta, \phi) = \sin 2\theta \sin\phi,$$

$$g_7(\theta, \phi) = \sin\theta \sin\phi.$$

Because we multiply the $g_i(\theta, \phi)$ functions by $ae(p_T^W, \cos\theta, \phi)$ before integrating over $\cos\theta$, no f_i is exactly zero and all of the angular coefficients A_i are in principle measurable. We have verified that the FMC-simulated ϕ distributions, fitted with a linear combination of f_i , result in angular coefficient values consistent with

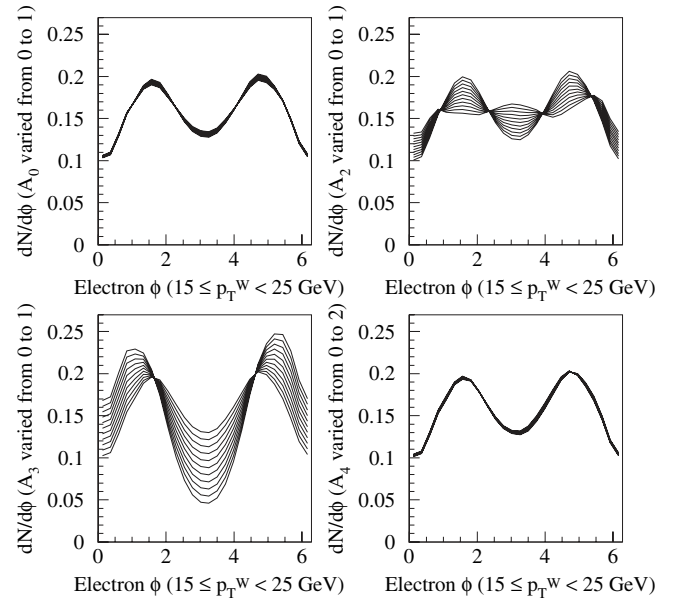


FIG. 23. The predicted electron ϕ distributions in the Collins-Soper W rest-frame for the first p_T^W bin, varying only one angular coefficient at a time and keeping the other angular coefficients at their standard model values. Only A_2 and A_3 significantly affect the shape of these distributions. The same is true for the other p_T^W bins and also for the muon ϕ distributions.

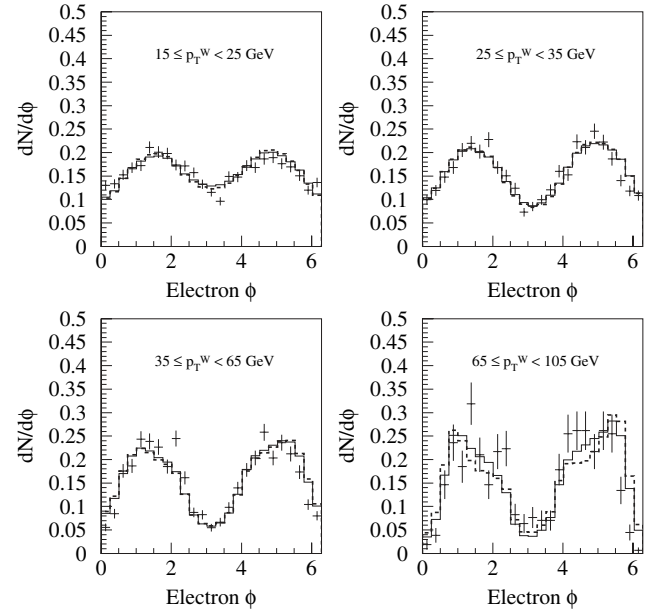


FIG. 24. The ϕ distributions for the electron CDF data (points), the SM Monte Carlo (solid lines), and the result of the fit (dashed lines) for the four bins of p_T^W . The errors are only statistical. The fit is performed from $\pi/2$ to $3\pi/2$ and resulted in χ^2/dof equal to 2.32, 1.80, 2.18, and 1.11 for the four bins, respectively (11 degrees of freedom). All distributions are normalized to unity.

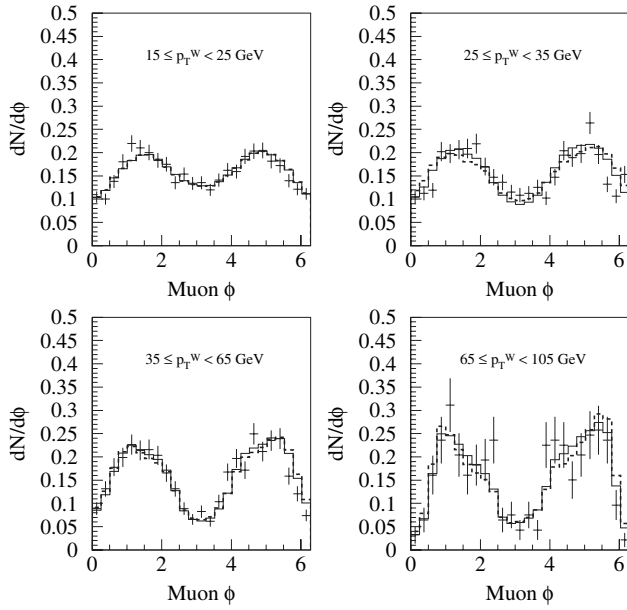


FIG. 25. The ϕ distributions for the muon CDF data (points), the SM Monte Carlo (solid lines), and the result of the fit (dashed lines) for the four bins of p_T^W . The errors are only statistical. The fit is performed from $\pi/2$ to $3\pi/2$ and resulted in χ^2/dof equal to 0.41, 1.39, 1.33, and 1.71 for the four bins, respectively (11 degrees of freedom). All distributions are normalized to unity.

the SM predictions [7]. This result supports the self-consistency of the method.

We use Simpson integration for the calculation of the f_i fitting functions given by Eq. (8). The explicit functions $g_i(\theta, \phi)$ are integrated over $\cos\theta$, after they are weighted with the value of $ae(p_T^W, \cos\theta, \phi)$ extracted from the 2-dimensional histograms of Figs. 7 and 8.

Although the use of Eq. (7) allows us in principle to measure all of the angular coefficients, in reality, the current statistics do not allow us to make a significant measurement of angular coefficients other than A_2 and A_3 . This is due to the fact that the fitting functions $f_{i \neq 2,3}$ are small, and the ϕ distributions are insensitive to large variations of the corresponding angular coefficients. Figure 23 shows how the expected electron ϕ distributions are modified as the angular coefficients A_i are varied, one coefficient at a time (the muon ϕ distributions are almost

identical). Using Eq. (7), we vary A_0, A_2 , and A_3 from 0 to 1 with a step size of 0.1, and A_4 from 0 to 2 with a step size of 0.2. We find that only A_2 and A_3 strongly affect the azimuthal distributions, thus only these two angular coefficients are measurable with our current ϕ analysis. Large variations of A_0 and A_4 result in small changes in the ϕ distributions, hence the uncertainties associated with the measurement of A_0 and A_4 are large; these two coefficients cannot be measured in a statistically significant manner with the ϕ analysis. The same is true for A_1, A_5, A_6 , and A_7 , all of which are consistent with zero for our current experimental precision.

Figure 24 shows the observed CS electron ϕ distributions for CDF electron $W + \text{jet}$ data for the four p_T^W bins. Figure 25 shows the corresponding ϕ distributions of the CDF muon $W + \text{jet}$ data. The solid lines are the SM theoretical predictions including backgrounds, whereas the points correspond to CDF $W + \text{jet}$ data (the error bars are statistical only). The theoretical prediction for the ϕ distributions is constructed using Eqs. (7) and (8). The free parameters are the angular coefficients A_i . The background ϕ shapes are given by Figs. 9, 11, and 15, for electrons and Figs. 10, 12, and 16 for muons, normalized to the event yields of Tables X and XI, respectively. The expected signal is normalized to the FMC signal event yields of Table XII, and subsequently the backgrounds are added to construct $N(p_T^W, \phi)$, according to Eq. (7). The total theoretically predicted distributions along with the experimental ones, are finally normalized to unity. The experimental results are in good agreement with the standard model prediction, which includes the effects of W polarization and QCD contributions up to order α_s^2 .

VIII. MEASUREMENT OF THE ANGULAR COEFFICIENTS

The values of the angular coefficients A_2 and A_3 are extracted using the least-squares fitting method and the data associated with Figs. 24 and 25. The least-squares fit is performed over the negative x -axis of the CS frame ($\pi/2 < \phi < 3\pi/2$) for the following two reasons.

Firstly, if a single jet perfectly balances the W boson, its momentum will be placed on the positive x -axis in the CS frame. In reality, the leading jet will be in the $x > 0$ region

TABLE XII. The expected total event yields for inclusive $W + \text{jet}$ production. The signal and electroweak backgrounds are calculated up to order α_s^2 . The PDF and Q^2 systematics have also been included (second set of uncertainties).

Expected signal + background event yields for inclusive $W + \text{jet}$ production						
p_T^W (GeV)	Electrons			Muons		
	$N_e(\text{Signal})$	$N_e(\text{Background})$	$N_e(\text{Total prediction})$	$N_\mu(\text{Signal})$	$N_\mu(\text{Background})$	$N_\mu(\text{Total prediction})$
15–25	3867 ± 137	412^{+41}_{-33}	$4279^{+148}_{-146} + 880/ - 660$	2027 ± 102	320^{+57}_{-19}	$2347^{+124}_{-112} + 484/ - 330$
25–35	2632 ± 93	292^{+29}_{-90}	$2924^{+100}_{-132} + 598/ - 408$	1384 ± 66	152^{+50}_{-10}	$1536^{+88}_{-72} + 329/ - 224$
35–65	2474 ± 87	98^{+47}_{-11}	$2572^{+102}_{-91} + 562/ - 383$	1314 ± 67	120^{+31}_{-19}	$1434^{+79}_{-75} + 312/ - 213$
65–105	518 ± 18	22^{+12}_{-2}	$540^{+22}_{-19} + 118/ - 81$	279 ± 14	20^{+10}_{-1}	$299^{+18}_{-15} + 66/ - 45$

of the $z - x$ plane, in proximity to the x -axis, as seen in Fig. 26 for the electron $W + \text{jet}$ data. The leading jet's ϕ in the CS frame will almost always be less than $\pi/2$ or greater than $3\pi/2$, as shown in Fig. 26. A kinematic correlation exists between the angular separation ΔR between the jet and the lepton in the $\phi_{\text{lab}} - \eta_{\text{lab}}$ space and the CS ϕ of the lepton, as shown in Fig. 26. The situation is similar for the possible subleading jets in the $W + \text{jet}$ events (Fig. 27). $W + \text{jet}$ events with more than two jets are not modeled in DYRAD simulation; their presence in the data creates extra biases in the low and high regions of the lepton ϕ distributions. Because of the lepton-jet angular separation and lepton isolation requirements in our $W + \text{jet}$ datasets we obtain a bias-free measurement of the angular coefficients A_2 and A_3 if we exclude the positive- x half-plane region of the CS frame.

Secondly, the term $A_3 f_3(\phi)$ in Eq. (7) is the smallest measurable term with our data. Therefore, a more significant measurement of the angular coefficient A_3 is obtained in the CS ϕ region where the rest of the terms (and mainly the predominant $A_4 f_4(\phi)$ term), contribute less. The ratio $A_3 f_3(\phi)/A_4 f_4(\phi)$ is significantly larger in the $\pi/2 < \phi < 3\pi/2$ region, and thus a more sensitive measurement of A_3 is obtained in this region. We normalize the theory to data from $\pi/2$ to $3\pi/2$ before we start the fitting procedure, which is carried out in the $x < 0$ region of the $z - x$ plane.

We use the MINUIT χ^2 minimization program [19] to fit the electron and muon ϕ distributions to the fitting func-

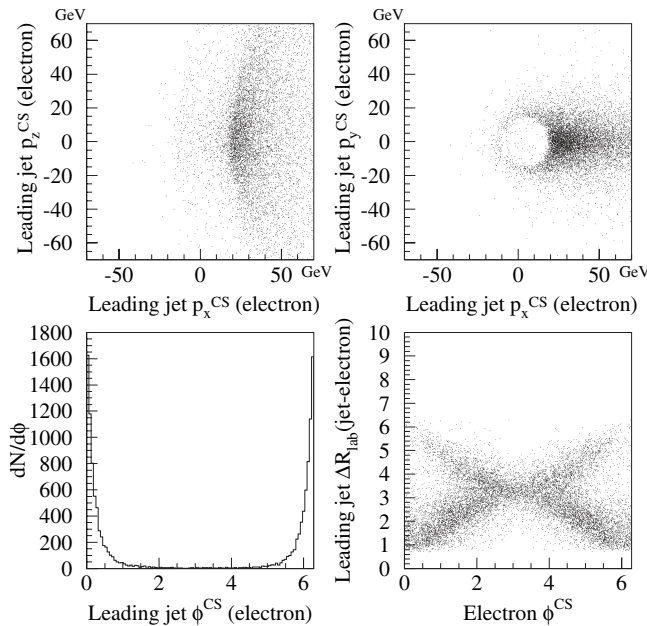


FIG. 26. The p_z vs p_x , p_y vs p_x , and ϕ of the leading jet in the CS frame and the ΔR between the jet and the lepton in the laboratory frame vs lepton ϕ in the CS frame, for electron CDF data.

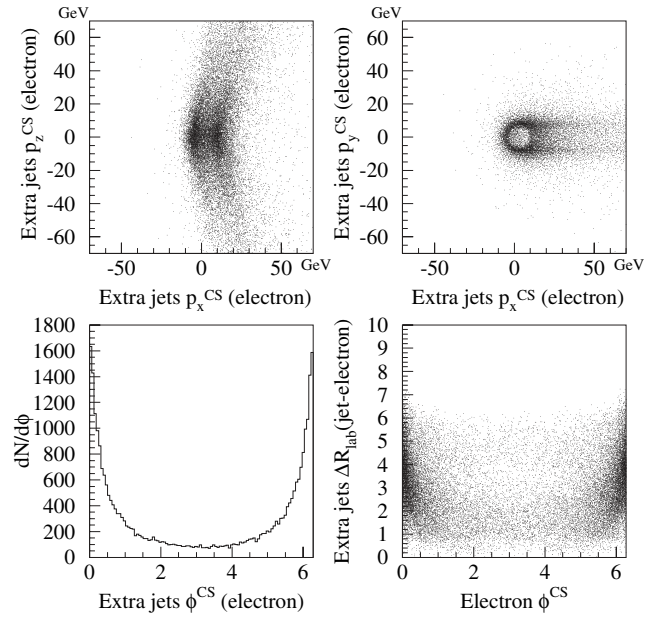


FIG. 27. The p_z vs p_x , p_y vs p_x , and ϕ of the extra jets in the CS frame and the ΔR between the jets and the lepton in the laboratory frame vs lepton ϕ in the CS frame, for electron CDF data.

tions f_i . Since these functions are not linearly independent, we cannot fit with all parameters free. For this reason we keep the angular coefficients A_0 and A_4 fixed at their SM values and allow A_2 and A_3 to vary. After we extract values for A_2 and A_3 , we fix these coefficients at these values, and we repeat the fit procedure varying only the A_0 and A_4 angular coefficients. The angular coefficients A_1 , A_5 , A_6 , and A_7 are always kept fixed at their SM values, since the theoretical prediction for these coefficients is very close to zero and the variation for the first 100 GeV of p_T^W is small in comparison to the experimental precision. We expect large statistical uncertainties for the extracted values of A_0 and A_4 , since they do not significantly affect the ϕ distribution. Large variations in their value only slightly alter the leptons' ϕ angular distribution.

The results of the MINUIT fits are shown as dashed histograms in Fig. 24 for the electron $W + \text{jet}$ data and Fig. 25 for the muon $W + \text{jet}$ data. Our measurements of the angular coefficients for the electron and muon $W + \text{jet}$ data are presented in Figs. 28 and 29, respectively. The bin centers are determined using the average value of p_T^W for the range of the four p_T^W bins. The measured angular coefficients associated with the electron and muon $W + \text{jet}$ data agree with the SM prediction and with each other. We emphasize that the SM prediction is only up to order α_s^2 in QCD. Systematic uncertainties on these results have not yet been discussed. The statistical uncertainties for A_0 and A_4 are very large, as expected, making the measurement of these coefficients unrealistic using the azimuthal angle analysis.

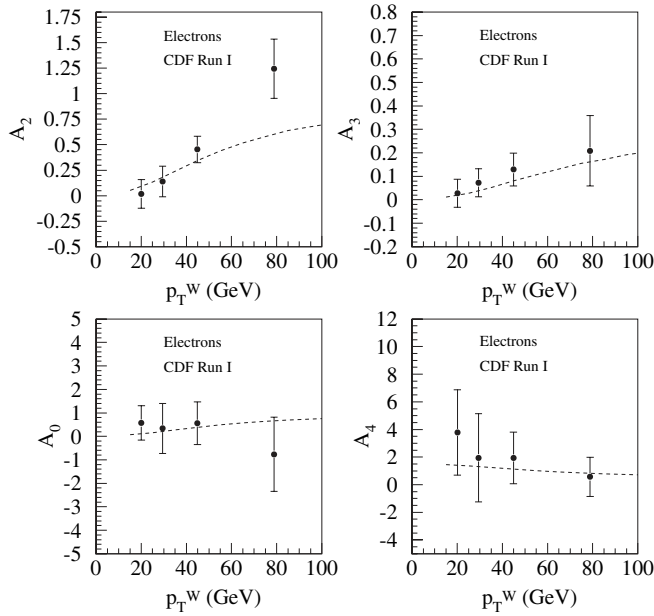


FIG. 28. The measurement of the angular coefficients for the $W + \text{jet}$ electron data (points) and the SM prediction up to order α_s^2 (line). The errors are only statistical.

Assuming weak-interaction lepton-universality, we combine the measurements of the angular coefficients obtained from the electron and muon $W + \text{jet}$ datasets, treating them as the results of two separate experiments. If A_e and A_μ are the electron and muon measurements with statistical uncertainties σ_e and σ_μ , respectively, then the combined measurement is $A_{\text{comb}} = (A_e/\sigma_e^2 +$

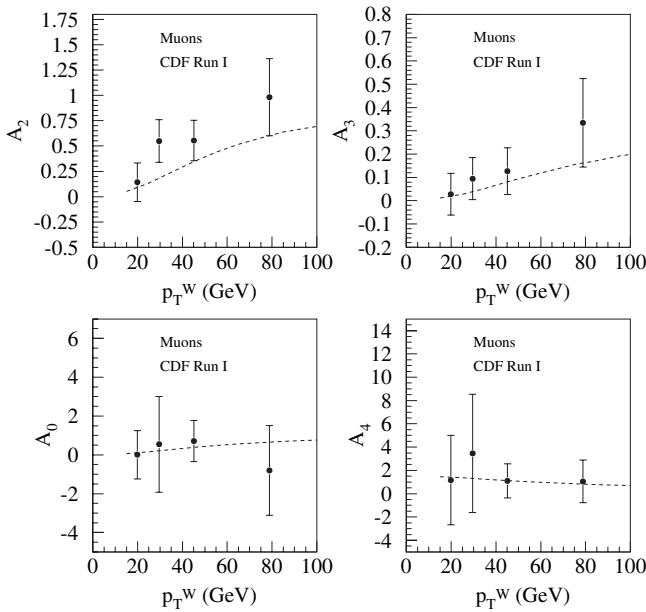


FIG. 29. The measurement of the angular coefficients for the $W + \text{jet}$ muon data (points) and the SM prediction up to order α_s^2 (line). The errors are only statistical.

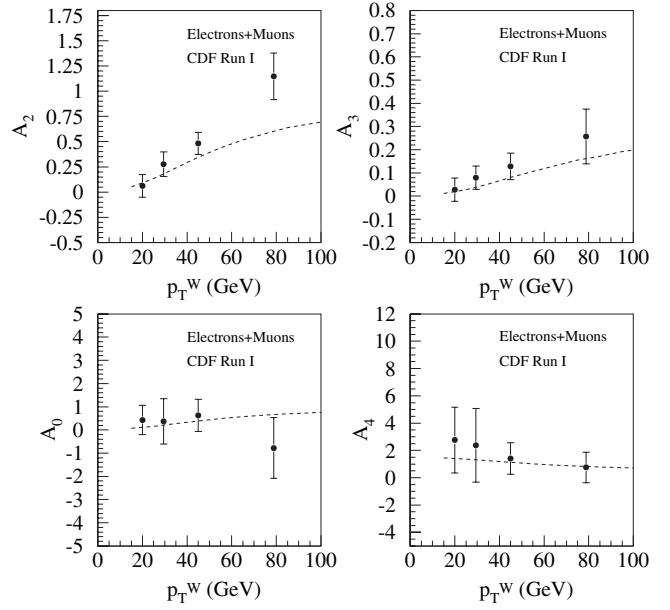


FIG. 30. The measurement of the angular coefficients for the combination of electrons and muons (points) and the SM prediction up to order α_s^2 (line). The errors are only statistical.

$A_\mu/\sigma_\mu^2)/(1/\sigma_e^2 + 1/\sigma_\mu^2)$, with statistical uncertainty $\sigma_{\text{comb}} = (1/\sigma_e^2 + 1/\sigma_\mu^2)^{-1/2}$. The result of this statistical combination, along with the SM prediction, is presented in Fig. 30.

IX. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties associated with the measurement of the angular coefficients A_i are related to the jet definition and energy scale, the selection of the W mass on an event-by-event basis, the background estimation, possible presence of $W + \gamma$ events in our datasets, the assumed values of A_0 and A_4 , the choice of parton distribution functions, and the renormalization and factorization scale Q^2 of the event. The jet systematic uncertainties, the variation of the A_0 and A_4 values, and Q^2 scale uncertainty are the dominant sources of systematics. The effect of the systematic uncertainties is summarized in Tables XIII, XIV, XV, and XVI, and described in detail in the following sections.

A. Jet systematic uncertainties

The number of data events passing the jet cuts is affected by the systematic uncertainties associated with the jet E_T scale and the rapidity requirement. The same systematic uncertainty has an effect on the measurement of the angular coefficients.

The uncertainty on jet E_T scale depends on the calorimeter stability, relative energy scale corrections, extra interactions, and underlying event corrections. The total uncertainty is a quadratic sum of these effects. The system-

atic uncertainty in the jet energy scale affects the reconstruction of the \cancel{E}_T and the W boson. For every FMC $W + \text{jet}$ event, we shift the energy of the jet by $\sigma_+ = 85\% \sqrt{E_T^{\text{jet}}}$, where E_T^{jet} is the energy of the jet in GeV, without changing its direction. We then correct the \cancel{E}_T value and recalculate all the kinematic variables associated with the W boson, jet, and \cancel{E}_T . We subsequently extract the new acceptance times efficiency $ae(\cos\theta, \phi)$ and analyze the data. We repeat this procedure for the energy shifted by $\sigma_- = -85\% \sqrt{E_T^{\text{jet}}}$ and calculate the systematic effect of the jet energy scale on the measurement of the angular coefficients, presented in Tables XIV for the electron, muon, and the combination of the two results. To obtain the combined results, we combine the electron and muon measurements for each p_T^W bin and for each choice of E_T^{jet} energy shift, using the statistical uncertainties of the central measurements. The difference between the shifted combined values and the central combined value determines the systematic uncertainty on the combined measurement. The same method is used for all the systematic uncertainty estimates.

We vary the jet E_T cut by $(\delta E_T) = \pm 850$ MeV in both data and MC and repeat the analysis each time, to determine its effect on the measurement of the angular coefficients and on the FMC-prediction of signal event yields. Table XIII shows the systematic uncertainty in the measurement of the $W + \text{jet}$ event yields associated with the jet E_T cut variation, for the four p_T^W bins. Overall, there is a $+6.4\% / -5.8\%$ effect in the electron event yields and a $+6.0\% / -5.7\%$ effect in the muon event yields due to the jet E_T cut.

The uncertainty on the rapidity η_{lab} of the jet is $\delta\eta_{\text{lab}} = \pm 0.2$. We vary the jet η_{lab} cut from 2.2 to 2.6 to obtain the variation in the data event yields presented in Table XIII, for the four p_T^W bins. Overall, there is a $+2.2\% / -2.4\%$ effect in the electron event yields and a $+0.7\% / -2.2\%$ effect in the muon event yields due to the jet $\eta_{\text{lab}}^{\text{jet}}$ cut.

In order to obtain an estimate of the systematic uncertainty in the measurement of the angular coefficients asso-

ciated with the jet E_T and η_{lab} cuts, we run the analysis for 11 values of the E_T^{jet} cut, from 14.15 GeV to 15.85 GeV, and for five values of $|\eta_{\text{lab}}^{\text{jet}}|$ cut, from 2.2 to 2.6. We record the variations in the measurement of the angular coefficients for electrons, muons, and the combination of the two results. The results for the four p_T^W bins are presented in Table XIV.

B. Systematic uncertainty due to W mass selection

As previously discussed, in order to boost to the W rest-frame, a mass value is selected for the W boson. We have four different methods for selecting this mass on an event-by-event basis. We investigate how each mass selection method affects our angular coefficients measurement. The first method selects a Breit-Wigner mass, which is greater than the measured transverse mass of the W boson. The second method selects the greater of the pole mass and the transverse mass. In the third method we select the pole mass or, in case it is less than the transverse mass, we select a Breit-Wigner mass, which is greater than the transverse mass. Finally the fourth method (default) selects a mass based on the distribution that results from the slice of the theoretical (DYRAD) M^W vs M_T^W 2-dimensional histogram (for $W + \text{jet}$ events) at the measured transverse mass of the W boson. This last method is preferred because it removes some biases in the measurement of the polar angle θ . In the ϕ analysis, the systematic uncertainty on the azimuthal angle ϕ due to the selection of the mass of the W is minimal. We run the analysis for the four mass selection methods and record the variations in the measurement of the angular coefficients for electrons, muons, and the combination of the two results. All methods give almost identical measurements of ϕ . The systematic uncertainties for the four p_T^W bins are presented in Table XIV.

C. Backgrounds estimate systematic uncertainty

There is an uncertainty in the estimation of the backgrounds, given by the uncertainties in Tables X and XI. We

TABLE XIII. Systematic uncertainties on $W + \text{jet}$ event yields due to the E_T^{jet} and $\eta_{\text{lab}}^{\text{jet}}$ cuts, and the total systematic uncertainty due to these sources, for the four p_T^W bins.

$W + \text{jet}$ event yield systematic uncertainties due to the E_T^{jet} and $\eta_{\text{lab}}^{\text{jet}}$ cuts				
p_T^W (GeV)	Charged Lepton	δN due to E_T^{jet}	δN due to $\eta_{\text{lab}}^{\text{jet}}$	Total systematic uncertainty
15–25	electron	+593 -515	+156 -154	+613 -538
	muon	+308 -290	+34 -81	+310 -301
25–35	electron	+179 -175	+78 -104	+195 -204
	muon	+95 -79	+12 -44	+96 -90
35–65	electron	+38 -50	+50 -43	+63 -66
	muon	+12 -29	+3 -29	+12 -41
65–105	electron	+0 -1	+1 -2	+1 -2
	muon	+0 -0	+0 -0	+0 -0

vary our prediction from the highest value to the lowest possible value for every background as well as the FMC signal event yields. These uncertainties do not include the PDF and Q^2 systematics. For each variation, we rerun the analysis programs for the electron and muon case, and we also combine the results. The systematic uncertainties are presented for the four p_T^W bins in Tables XIV and XV.

D. $W + \gamma$ systematic uncertainty

The $W + \text{jet}$ angular distribution can be affected by $W + \gamma$ production, for a hard γ well separated from the charged lepton from the W decay. Some of the events in our datasets are consistent with $W + \gamma$ production, according to [16]. We remove those events and remeasure A_2 and A_3 . The variation from the original measurement is treated as a systematic uncertainty. The systematic uncertainties for the four p_T^W bins are presented in Table XV.

E. A_0 and A_4 variation systematic uncertainty

In our analysis we keep A_0 and A_2 fixed at their SM values. To check how this affects our measurement, we set A_0 and A_2 at minimum and maximum values ($A_0(\text{min}) = 0$, $A_0(\text{max}) = 1$, $A_4(\text{min}) = 0$ and $A_4(\text{max}) = 2$) in all possible combinations and repeat the analysis 4 times. The systematic uncertainties for the four p_T^W bins are presented in Table XV.

F. PDF systematic uncertainty

To study the uncertainty associated with the parton distribution functions, we use the MRSA' [$\alpha_s(M_Z) = 0.105$ and $\Lambda = 0.150$] PDF [20] and repeat the analysis. The systematic uncertainties for the four p_T^W bins are presented in Table XV. When we use all PDFs of the MRSA and CTEQ families, we end up with a systematic uncertainty of $\pm 11\%$ on the DYRAD cross section, which affects both the central FMC signal event yields and the

TABLE XIV. Systematic uncertainties in the measurement of A_2 and A_3 along with their sources, for electron and muon $W + \text{jet}$ events and the combination of the electron and muon results.

Source of systematic uncertainty	p_T^W (GeV)	Electrons		Muons		Combination	
		δA_2	δA_3	δA_2	δA_3	δA_2	δA_3
Jet E_T cut	15–25	+0.0275	+0.0000	+0.0146	+0.0036	+0.0230	+0.0000
		-0.0533	-0.0064	-0.0502	-0.0032	-0.0523	-0.0043
	25–35	+0.0395	+0.0047	+0.0676	+0.0073	+0.0490	+0.0050
		-0.0109	-0.0039	-0.0559	-0.0017	-0.0261	-0.0027
Jet η_{lab} cut	15–25	+0.0433	+0.0030	+0.0177	+0.0042	+0.0357	+0.0031
		-0.0000	-0.0033	-0.0131	-0.0011	-0.0000	-0.0022
	25–35	+0.0000	+0.0167	+0.1519	+0.0055	+0.0556	+0.0024
		-0.0617	-0.0153	-0.0000	-0.0808	-0.0299	-0.0374
Jet energy scale	15–25	+0.0043	+0.0000	+0.0098	+0.0044	+0.0002	+0.0000
		-0.0324	-0.0036	-0.0374	-0.0000	-0.0175	-0.0018
	25–35	+0.0007	+0.0012	+0.0299	+0.0000	+0.0106	+0.0000
		-0.0346	-0.0022	-0.0221	-0.0085	-0.0304	-0.0032
M_W selection	15–25	+0.0093	+0.0023	+0.0070	+0.0038	+0.0070	+0.0013
		-0.0049	-0.0005	-0.0075	-0.0028	-0.0032	-0.0000
	25–35	+0.0000	+0.0022	+0.1021	+0.0000	+0.0112	+0.0000
		-0.0617	-0.0052	-0.0000	-0.0557	-0.0258	-0.0203
τ background	15–25	+0.0594	+0.0042	+0.0499	+0.0075	+0.0560	+0.0052
		-0.0588	-0.0014	-0.0694	-0.0044	-0.0626	-0.0023
	25–35	+0.0851	+0.0096	+0.0860	+0.0261	+0.0854	+0.0147
		-0.1105	-0.0020	-0.0994	-0.0141	-0.1068	-0.0057
Z background	15–25	+0.0017	+0.0204	+0.0142	+0.0183	+0.0054	+0.0197
		-0.0514	-0.0069	-0.0850	-0.0102	-0.0614	-0.0080
	25–35	+0.2468	+0.0836	+0.2989	+0.0382	+0.2660	+0.0662
		-0.3821	-0.0489	-0.3186	-0.0176	-0.3587	-0.0369
τ background	15–25	+0.0030	+0.0000	+0.0000	+0.0001	+0.0019	+0.0000
		-0.0000	-0.0011	-0.0016	-0.0000	-0.0000	-0.0007
	25–35	+0.0018	+0.0010	+0.0034	+0.0007	+0.0024	+0.0007
		-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000
Z background	15–25	+0.0068	+0.0034	+0.0000	+0.0038	+0.0012	+0.0035
		-0.0046	-0.0002	-0.0120	-0.0000	-0.0040	-0.0000
	25–35	+0.0000	+0.0032	+0.0560	+0.0000	+0.0000	+0.0013
		-0.0561	-0.0000	-0.0000	-0.0598	-0.0149	-0.0210
τ background	15–25	+0.0009	+0.0001	+0.0014	+0.0001	+0.0011	+0.0001
		-0.0009	-0.0000	-0.0013	-0.0001	-0.0011	-0.0001
	25–35	+0.0008	+0.0000	+0.0023	+0.0002	+0.0013	+0.0001
		-0.0010	-0.0001	-0.0018	-0.0002	-0.0013	-0.0002
Z background	15–25	+0.0008	+0.0001	+0.0018	+0.0002	+0.0011	+0.0001
		-0.0012	-0.0002	-0.0018	-0.0002	-0.0014	-0.0002
	25–35	+0.0024	+0.0003	+0.0000	+0.0000	+0.0015	+0.0002
		-0.0025	-0.0005	-0.0000	-0.0000	-0.0016	-0.0003
Z background	15–25	+0.0000	+0.0001	+0.0000	+0.0001	+0.0000	+0.0001
		-0.0009	-0.0000	-0.0017	-0.0000	-0.0012	-0.0000
	25–35	+0.0000	+0.0001	+0.0000	+0.0002	+0.0000	+0.0001
		-0.0010	-0.0000	-0.0037	-0.0000	-0.0019	-0.0000
Z background	15–25	+0.0000	+0.0001	+0.0000	+0.0002	+0.0000	+0.0001
		-0.0012	-0.0000	-0.0029	-0.0000	-0.0017	-0.0000
	25–35	+0.0000	+0.0003	+0.0001	+0.0006	+0.0000	+0.0004
		-0.0025	-0.0000	-0.0000	-0.0007	-0.0016	-0.0001

TABLE XV. Systematic uncertainties in the measurement of A_2 and A_3 along with their sources, for electron and muon $W + \text{jet}$ events and the combination of the electron and muon results (continued).

Source of systematic uncertainty	p_T^W (GeV)	Electrons		Muons		Combination	
		δA_2	δA_3	δA_2	δA_3	δA_2	δA_3
QCD background	15–25	+0.0140 -0.0127	+0.0009 -0.0009	+0.0329 -0.0125	+0.0010 -0.0030	+0.0206 -0.0126	+0.0009 -0.0015
	25–35	+0.0092 -0.0326	+0.0013 -0.0003	+0.0242 -0.0076	+0.0009 -0.0039	+0.0143 -0.0242	+0.0012 -0.0014
	35–65	+0.0018 -0.0149	+0.0010 -0.0001	+0.0062 -0.0087	+0.0013 -0.0015	+0.0000 -0.0086	+0.0004 -0.0000
	65–105	+0.0134 -0.0050	+0.0002 -0.0014	+0.0243 -0.0000	+0.0039 -0.0007	+0.0174 -0.0031	+0.0006 -0.0001
FMC signal event yield	15–25	+0.0031 -0.0065	+0.0000 -0.0023	+0.0000 -0.0004	+0.0012 -0.0032	+0.0019 -0.0043	+0.0000 -0.0016
	25–35	+0.0190 -0.0000	+0.0003 -0.0016	+0.0355 -0.0000	+0.0020 -0.0017	+0.0246 -0.0000	+0.0008 -0.0016
	35–65	+0.0173 -0.0000	+0.0023 -0.0033	+0.0030 -0.0022	+0.0039 -0.0000	+0.0115 -0.0000	+0.0028 -0.0022
	65–105	+0.0000 -0.0540	+0.0009 -0.0052	+0.0830 -0.0000	+0.0000 -0.0557	+0.0110 -0.0267	+0.0000 -0.0246
$W + \gamma$	15–25	+0.0000 -0.0060	+0.0000 -0.0031	+0.0022 -0.0000	+0.0021 -0.0000	+0.0000 -0.0031	+0.0000 -0.0015
	25–35	+0.0000 -0.0064	+0.0019 -0.0000	+0.0050 -0.0000	+0.0000 -0.0039	+0.0000 -0.0025	+0.0001 -0.0000
	35–65	+0.0103 -0.0000	+0.0023 -0.0000	+0.0026 -0.0000	+0.0015 -0.0000	+0.0080 -0.0000	+0.0020 -0.0000
	65–105	+0.0000 -0.0704	+0.0024 -0.0000	+0.0000 -0.0060	+0.0000 -0.0166	+0.0000 -0.0467	+0.0000 -0.0049
A_0 and A_4 variation	15–25	+0.0296 -0.2024	+0.0074 -0.0015	+0.0323 -0.1965	+0.0080 -0.0016	+0.0305 -0.2003	+0.0076 -0.0015
	25–35	+0.0691 -0.2326	+0.0155 -0.0051	+0.0553 -0.1745	+0.0240 -0.0081	+0.0644 -0.2129	+0.0181 -0.0060
	35–65	+0.1053 -0.1610	+0.0218 -0.0158	+0.0917 -0.1390	+0.0170 -0.0122	+0.1013 -0.1545	+0.0202 -0.0146
	65–105	+0.1189 -0.0708	+0.0150 -0.0277	+0.0963 -0.0553	+0.0167 -0.0312	+0.1106 -0.0651	+0.0157 -0.0290
PDF variation	15–25	+0.0000 -0.0159	+0.0013 -0.0000	+0.0000 -0.0419	+0.0017 -0.0000	+0.0000 -0.0251	+0.0014 -0.0000
	25–35	+0.0152 -0.0000	+0.0000 -0.0034	+0.0000 -0.0018	+0.0000 -0.0003	+0.0094 -0.0000	+0.0000 -0.0024
	35–65	+0.0000 -0.0068	+0.0011 -0.0000	+0.0759 -0.0000	+0.0000 -0.0003	+0.0178 -0.0000	+0.0006 -0.0000
	65–105	+0.0022 -0.0000	+0.0134 -0.0000	+0.4001 -0.0000	+0.0000 -0.0931	+0.1486 -0.0000	+0.0000 -0.0275
Q^2 variation	15–25	+0.1043 -0.0000	+0.0028 -0.0000	+0.1200 -0.0000	+0.0000 -0.0121	+0.1098 -0.0000	+0.0000 -0.0018
	25–35	+0.1319 -0.0000	+0.0000 -0.0104	+0.0668 -0.0000	+0.0000 -0.0076	+0.1099 -0.0000	+0.0000 -0.0096
	35–65	+0.1347 -0.0000	+0.0000 -0.0267	+0.0386 -0.0000	+0.0000 -0.0180	+0.1062 -0.0000	+0.0000 -0.0239
	65–105	+0.0000 -0.0959	+0.0101 -0.0000	+0.0000 -0.2251	+0.0162 -0.0000	+0.0000 -0.1434	+0.0124 -0.0000

electroweak backgrounds. These variations are used for the estimation of the total FMC event yields systematic uncertainty due to choice of PDF.

G. Q^2 systematic uncertainty

Finally we change the renormalization and factorization scale Q^2 so that it is equal to the square of the transverse

momentum of the W , instead of the default square of the pole mass of the W boson. The systematic uncertainties for the four p_T^W bins are presented in Table XV. If we try all Q^2 choices provided by DYRAD (total invariant mass squared, dynamic mass squared, total energy of the W squared, and transverse energy of the leading jet squared, in addition to the two mentioned above), we end up with a systematic uncertainty of $+19\%/ - 10\%$ on the DYRAD cross section, which affects both the central FMC signal event

TABLE XVI. Total systematic uncertainties in the measurement of A_2 and A_3 , for electron and muon $W + \text{jet}$ events and the combination of the electron and muon results. The systematic uncertainties of Tables XIV and XV are combined in quadrature.

Total systematic uncertainties						
p_T^W (GeV)	Electrons		Muons		Combination	
	δA_2	δA_3	δA_2	δA_3	δA_2	δA_3
15–25	+0.1275 -0.2209	+0.0092 -0.0087	+0.1390 -0.0140	+0.0128 -0.2189	+0.1307 -0.0064	+0.0094 -0.0064
25–35	+0.1779 -0.2622	+0.0191 -0.0131	+0.1492 -0.2098	+0.0362 -0.0208	+0.1641 -0.2428	+0.0239 -0.0137
35–65	+0.1779 -0.1699	+0.0305 -0.0321	+0.1276 -0.1643	+0.0263 -0.0243	+0.1530 -0.1665	+0.0289 -0.0293
65–105	+0.2743 -0.4229	+0.0883 -0.0587	+0.5503 -0.3941	+0.0453 -0.1629	+0.3297 -0.3977	+0.0692 -0.0764

TABLE XVII. The electron and muon CDF data event yields for inclusive $W + \text{jet}$ production, with statistical and systematic uncertainties. The systematic uncertainties are due to E_T^{jet} and $\eta_{\text{lab}}^{\text{jet}}$ cuts.

Data event yields for inclusive $W + \text{jet}$ production		
p_T^W (GeV)	N_e	N_μ
15–25	$5166 \pm 72^{+613}_{-538}$	$2821 \pm 53^{+310}_{-301}$
25–35	$3601 \pm 60^{+195}_{-204}$	$1869 \pm 43^{+96}_{-90}$
35–65	$3285 \pm 57^{+63}_{-66}$	$1880 \pm 43^{+12}_{-41}$
65–105	$624 \pm 25^{+1}_{-2}$	$371 \pm 19^{+0}_{-0}$

yields and the electroweak backgrounds. These variations are used for the estimation of the total FMC event yields systematic uncertainty due to Q^2 scale variation.

H. Overall analysis systematic uncertainties

Table XVI summarizes the total systematic uncertainties for the A_2 and A_3 measurement, for the four p_T^W bins and for the electron, muon, and combined results. To populate this table, we combine the systematics described above and presented in Tables XIV and XV.

I. Overall systematic uncertainties in data and Monte Carlo event yields

Combining the data event yield systematics due to E_T^{jet} and $\eta_{\text{lab}}^{\text{jet}}$ cut variations in quadrature, we get the final data event yields presented in Table XVII. Comparing with the FMC event yields of Table XII, we see that there is a reasonable agreement with the SM prediction. In Table XII we have also included the PDF and Q^2 FMC systematic uncertainties described earlier, combined in quadrature to give a systematic uncertainty of $+22\% / -15\%$ on the FMC signal event yields and electroweak background. We do not expect perfect agreement since the DYRAD generator produces up to two jets with $E_T^{\text{jet}} > 10$ GeV (order α_s^2), while in the data we have many events with more than two jets with $E_T^{\text{jet}} > 10$ GeV. If we impose a cut on the number of jets in the CDF data, by not accepting more than two jets in an event, and applying strict cuts on at least one jet, the disagreement is reduced by more than 50%. Nevertheless, we prefer not to constrain the dataset in such a manner. Note that the event yield

TABLE XVIII. The measurement of the A_2 coefficient along with the statistical and systematic uncertainties for electron and muon $W + \text{jet}$ events and the combination of the electron and muon results. The SM values up to order α_s^2 are also included.

Measurement of A_2 angular coefficient		
	p_T^W (GeV)	A_2
Electrons	15–25	$0.02 \pm 0.14^{+0.13}_{-0.22}$
	25–35	$0.14 \pm 0.15^{+0.18}_{-0.26}$
	35–65	$0.45 \pm 0.13^{+0.18}_{-0.17}$
	65–105	$1.24 \pm 0.29^{+0.27}_{-0.42}$
Muons	15–25	$0.14 \pm 0.19^{+0.14}_{-0.22}$
	25–35	$0.55 \pm 0.21^{+0.15}_{-0.21}$
	35–65	$0.55 \pm 0.20^{+0.13}_{-0.16}$
	65–105	$0.98 \pm 0.38^{+0.55}_{-0.39}$
Combination	15–25	$0.06 \pm 0.11^{+0.13}_{-0.22}$
	25–35	$0.28 \pm 0.12^{+0.16}_{-0.24}$
	35–65	$0.48 \pm 0.11^{+0.15}_{-0.17}$
	65–105	$1.15 \pm 0.23^{+0.33}_{-0.40}$
Standard Model	15–25	0.09
	25–35	0.19
	35–65	0.35
	65–105	0.60

TABLE XIX. The measurement of the A_3 coefficient along with the statistical and systematic uncertainties for electron and muon $W + \text{jet}$ events and the combination of the electron and muon results. The SM values up to order α_s^2 are also included.

Measurement of A_3 angular coefficient		
	p_T^W (GeV)	A_3
Electrons	15–25	$0.03 \pm 0.06^{+0.01}_{-0.01}$
	25–35	$0.07 \pm 0.06^{+0.02}_{-0.01}$
	35–65	$0.13 \pm 0.07^{+0.03}_{-0.03}$
	65–105	$0.21 \pm 0.15^{+0.09}_{-0.06}$
Muons	15–25	$0.03 \pm 0.09^{+0.01}_{-0.01}$
	25–35	$0.09 \pm 0.09^{+0.04}_{-0.02}$
	35–65	$0.13 \pm 0.10^{+0.03}_{-0.02}$
	65–105	$0.33 \pm 0.19^{+0.05}_{-0.16}$
Combination	15–25	$0.03 \pm 0.05^{+0.01}_{-0.01}$
	25–35	$0.08 \pm 0.05^{+0.02}_{-0.01}$
	35–65	$0.13 \pm 0.06^{+0.03}_{-0.03}$
	65–105	$0.26 \pm 0.12^{+0.07}_{-0.08}$
Standard Model	15–25	0.02
	25–35	0.04
	35–65	0.08
	65–105	0.16

measurements do not affect the angular coefficient measurements, since we are interested only in the *shapes* of the distributions, in the latter case.

X. FINAL RESULTS

Combining the statistical and systematic uncertainties associated with the A_2 and A_3 measurement, we obtain our

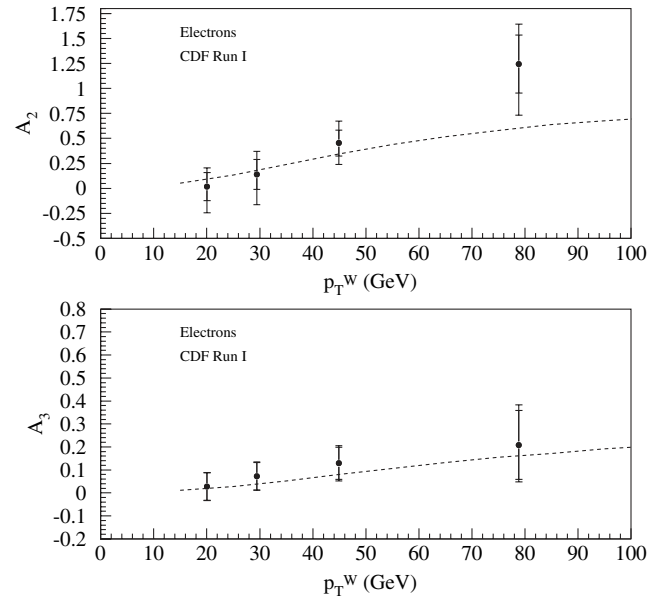


FIG. 31. Measured A_2 and A_3 using electron $W + \text{jet}$ events. The total (outer) and statistical (inner) uncertainties are shown along with the standard model 1-loop prediction up to order α_s^2 (dashed line).

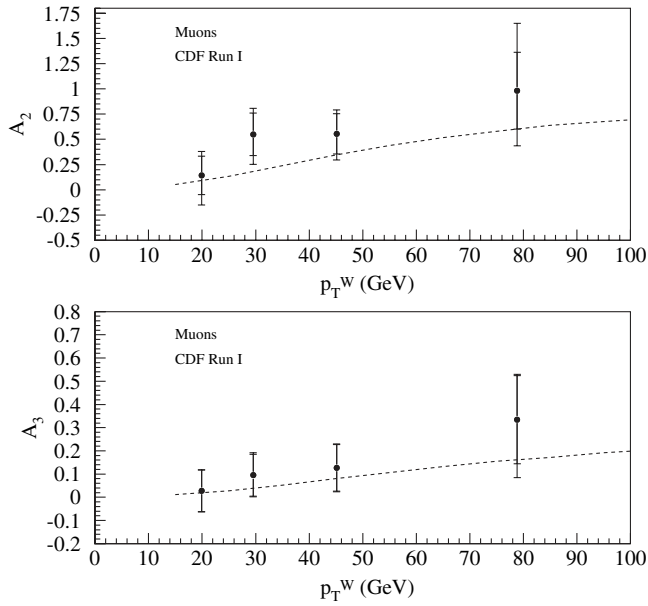


FIG. 32. Measured A_2 and A_3 using muon $W + \text{jet}$ events. The total (outer) and statistical (inner) uncertainties are shown along with the standard model 1-loop prediction up to order α_s^2 (dashed line).

final results, presented in Tables XVIII and XIX. Figure 31 shows the measurement of A_2 and A_3 for the electron $W + \text{jet}$ data and Fig. 32 shows the measurement of A_2 and A_3 for the muon $W + \text{jet}$ data. The combination of the electron and muon measurements of the two angular coeffi-

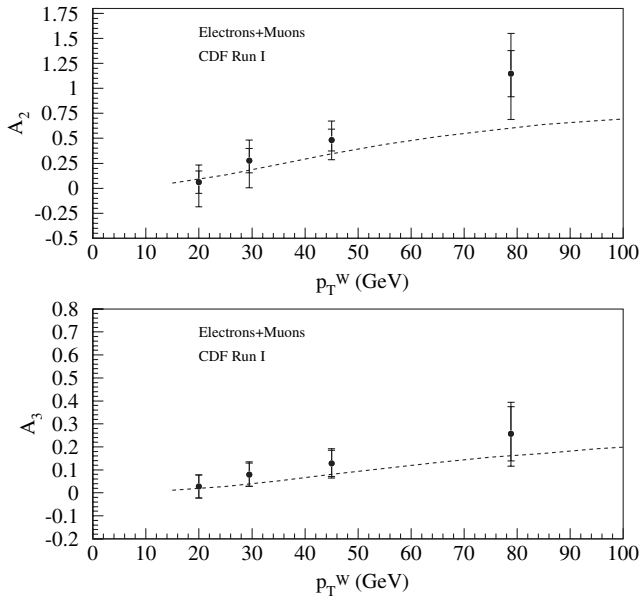


FIG. 33. Measured A_2 and A_3 using the combination of electron and muon measurements. The total (outer) and statistical (inner) uncertainties are shown along with the standard model 1-loop prediction up to order α_s^2 (dashed line).

icients is presented in Fig. 33. The standard model predictions for these angular coefficients, up to order α_s^2 , are also presented.

XI. CONCLUSIONS

We have made the first measurement of the A_2 and A_3 angular coefficients of W boson production and decay, using the CDF Run Ia and Run Ib electron and muon $W + \text{jet}$ data. Our datasets include at least one jet, satisfying the energy and pseudorapidity requirements. Because of finite statistical analyzing power of our $W + \text{jet}$ datasets and the characteristics of the W decay, only the measurement of A_2 and A_3 angular coefficients is statistically significant, with the analysis of the azimuthal angle of the charged lepton in the W rest-frame. The A_0 and A_4 coefficients are preferably measurable with a polar angle analysis, while A_1 and the next-to-leading order coefficients— A_5 , A_6 , and A_7 —are not measurable, with any meaningful statistical significance, with Run I $W + \text{jet}$ data.

At leading order, the A_2 and A_3 angular coefficients fully describe the azimuthal W angular distribution in the Collins-Soper W rest-frame. These angular coefficients are also part of the total W differential cross section, and can be expressed as ratios of the corresponding helicity cross sections of the W to its total unpolarized cross section. This measurement tests the standard model prediction for W polarization, and the associated QCD corrections present in the production of W bosons at high transverse momenta. We observe good agreement with the standard model prediction up to order α_s^2 in QCD.

ACKNOWLEDGMENTS

We thank K. Hagiwara for initial discussions on this subject. We thank W. Giele for many helpful, stimulating discussions and DYRAD $W + \text{jet}$ Monte Carlo event generator support. We also thank the Fermilab staff and the technical staffs of the participating institutions for their vital contributions. This work was supported by the U.S. Department of Energy and National Science Foundation; the Italian Istituto Nazionale di Fisica Nucleare; the Ministry of Education, Culture, Sports, Science and Technology of Japan; the Natural Sciences and Engineering Research Council of Canada; the National Science Council of the Republic of China; the Swiss National Science Foundation; the A. P. Sloan Foundation; the Bundesministerium fuer Bildung und Forschung, Germany; the Korean Science and Engineering Foundation and the Korean Research Foundation; the Particle Physics and Astronomy Research Council and the Royal Society, UK; the Russian Foundation for Basic Research; the Comision Interministerial de Ciencia y Tecnologia, Spain; and in part by the European Community's Human Potential Programme under Contract No. HPRN-CT-2002-00292, Probe for New Physics.

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