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## Measurements of neutral $B$ decay branching fractions to $K_{S}^{\mathbf{0}} \boldsymbol{\pi}^{+} \boldsymbol{\pi}^{-}$final states and the charge asymmetry of $\boldsymbol{B}^{\mathbf{0}} \rightarrow \boldsymbol{K}^{*+} \boldsymbol{\pi}^{-}$

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#### Abstract

We analyze the decay $B^{0} \rightarrow K_{S}^{0} \pi^{+} \pi^{-}$using a sample of $232 \times 10^{6} \Upsilon(4 S) \rightarrow B \bar{B}$ decays collected with the BABAR detector at the SLAC PEP-II asymmetric-energy $B$ factory. A maximum likelihood fit finds the following branching fractions: $\mathcal{B}\left(B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}\right)=(43.0 \pm 2.3 \pm 2.3) \times 10^{-6}, \mathcal{B}\left(B^{0} \rightarrow f_{0}(\rightarrow\right.$ $\left.\left.\pi^{+} \pi^{-}\right) K^{0}\right)=(5.5 \pm 0.7 \pm 0.5 \pm 0.3) \times 10^{-6} \quad$ and $\quad \mathcal{B}\left(B^{0} \rightarrow K^{*+} \pi^{-}\right)=(11.0 \pm 1.5 \pm 0.5 \pm 0.5) \times$ $10^{-6}$. For these results, the first uncertainty is statistical, the second is systematic, and the third (if present) is due to the effect of interference from other resonances. We also measure the $C P$-violating charge asymmetry in the decay $B^{0} \rightarrow K^{*+} \pi^{-}, \mathcal{A}_{K^{*} \pi}=-0.11 \pm 0.14 \pm 0.05$.


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Measurements of charmless three-body $B$ decays, which are dominated by their intermediate quasi-two-body decays, are important in furthering our understanding of quark couplings described by the Cabibbo-KobayashiMaskawa matrix [1]. $C P$ violation can be probed through the investigation of neutral $B$-meson decays to resonance channels with the final state $K_{S}^{0} \pi^{+} \pi^{-}$, such as $f_{0} K_{S}^{0}$ [2], $\rho^{0} K_{S}^{0}$ [3] and $K^{*+} \pi^{-}$[4].

By measuring the charmless branching fraction of $B^{0} \rightarrow$ $K_{S}^{0} \pi^{+} \pi^{-}$, along with those of its dominant resonant submodes, we can obtain information about the structure of the decay Dalitz plot. Such measurements have previously been performed by the CLEO [5], Belle [6] and BABAR [2-4] experiments.

QCD factorization models [7] have predicted branching fractions and asymmetries for charmless $B$ decays. Predictions have also been made using flavor $\mathrm{SU}(3)$ symmetry [8]. For $B^{0} \rightarrow K^{*+} \pi^{-}$, predictions [9] have been made for the branching fractions and charge asymmetry,

$$
\begin{equation*}
\mathcal{A}_{K^{*} \pi}=\frac{\Gamma_{\bar{B}^{0} \rightarrow K^{*-}} \pi^{+}-\Gamma_{B^{0} \rightarrow K^{*+} \pi^{-}}}{\Gamma_{\bar{B}^{0} \rightarrow K^{*-} \pi^{+}}+\Gamma_{B^{0} \rightarrow K^{*+} \pi^{-}}} \tag{1}
\end{equation*}
$$

which is a $C P$-violating quantity since the decay channel is a flavor eigenstate. $C P$ violation in charge asymmetry has already been observed by $B A B A R$ and Belle in $B^{0} \rightarrow$ $K^{+} \pi^{-}$[10].

In this paper the branching fractions of $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$, $B^{0} \rightarrow K^{*+} \pi^{-}$and $B^{0} \rightarrow f_{0}(980)\left(\rightarrow \pi^{+} \pi^{-}\right) K^{0}$ are presented, averaged over charge-conjugate states, along with a measurement of the charge asymmetry in $B^{0} \rightarrow K^{*+} \pi^{-}$. The selection criteria require events with a reconstructed $K_{S}^{0}$ in the final state. Results are stated in terms of the $K^{0}$ final state, taking into account the probabilities for $\mathcal{B}\left(K^{0} \rightarrow K_{S}^{0}\right)$ and $\mathcal{B}\left(K_{S}^{0} \rightarrow \pi^{+} \pi^{-}\right)$[11]. For the $B^{0} \rightarrow$ $K^{0} \pi^{+} \pi^{-}$branching fraction, the total charmless contribution to the Dalitz plot is measured (with charmed and charmonium resonances removed), including contributions from resonant charmless substructure.

The data used in this analysis were collected at the PEPII asymmetric-energy $e^{+} e^{-}$storage ring with the BABAR
detector [12]. The BABAR detector consists of a doublesided five-layer silicon tracker, a 40-layer drift chamber, a Cherenkov detector, an electromagnetic calorimeter and a magnet with instrumented flux return. The data sample has an integrated luminosity of $210 \mathrm{fb}^{-1}$ collected at the $\mathrm{Y}(4 \mathrm{~S})$ resonance, which corresponds to $(231.8 \pm 2.5) \times 10^{6} B \bar{B}$ pairs. It is assumed that the $Y(4 S)$ decays equally to neutral and charged $B$-meson pairs. In addition, $21.6 \mathrm{fb}^{-1}$ of data collected at 40 MeV below the $\mathrm{Y}(4 \mathrm{~S})$ resonance were used for background studies.

The reconstruction of candidate $B$ mesons combines two charged tracks and a $K_{S}^{0}$ candidate, with the $K_{S}^{0}$ being reconstructed from two oppositely charged tracks consistent with $\pi^{+} \pi^{-}$. The $B^{0}$ decay vertex is reconstructed from the two charged tracks that were not daughters of the $K_{S}^{0}$, with the requirements that the tracks originate from the beam-spot, have at least 12 hits in the drift chamber and have a transverse momentum greater than $100 \mathrm{MeV} / c . K_{S}^{0}$ candidates are required to have a reconstructed mass within $15 \mathrm{MeV} / c^{2}$ of the nominal $K_{S}^{0}$ mass [11], at least a 5 standard deviation separation between the $B^{0}$ decay vertex and its own decay vertex, and a cosine of the angle between the line joining the $B^{0}$ and $K_{S}^{0}$ decay vertices and the $K_{S}^{0}$ momentum vector greater than 0.999 . To identify pions we use measurements of energy loss $(\mathrm{d} E / \mathrm{d} x)$ in the tracking system, the number of photons detected by the Cherenkov detector and the corresponding Cherenkov angle. Candidate pions must fail the electron selection, which is based on $\mathrm{d} E / \mathrm{d} x$ measurements, shower shape in the calorimeter, and the ratio of energy in the calorimeter to momentum in the drift chamber. Using simulated Monte Carlo (MC) events, we determine an approximate mean and width $(\sigma)$ of the mass distribution for the resonances, and choose the resonance band to be $\pm 3 \sigma$ from the mean. For the decay $B^{0} \rightarrow K^{*+} \pi^{-}$we require $0.776<$ $m_{K_{S}^{0} \pi}<1.010 \mathrm{GeV} / c^{2}$ and for $B^{0} \rightarrow f_{0} K_{S}^{0}$ we require $0.879<m_{\pi^{+} \pi^{-}}<1.069 \mathrm{GeV} / c^{2}$.

The dominant source of background is continuum quark production ( $e^{+} e^{-} \rightarrow q \bar{q}$ where $q=u, d, s, c$ ). An eventshape variable, the cosine of the angle $\theta_{T}$ between the
thrust axis of the selected $B$ candidate and the thrust axis of the rest of the event [12], is used to suppress this background. The distribution of $\left|\cos \theta_{T}\right|$ is strongly peaked towards unity for continuum background but is flat for signal events. The requirement $\left|\cos \theta_{T}\right|<0.9$ reduces the relative amount of continuum background.

To separate signal events from the remaining background events, we use two kinematic variables and one event-shape variable. The first kinematic variable $\Delta E$, is the difference between the center-of-mass (CM) energy of the $B$ candidate and $\sqrt{s} / 2$, where $\sqrt{s}$ is the total CM energy of the $e^{+} e^{-}$beams. The second is the beam-energy-substituted mass $m_{\mathrm{ES}}=\sqrt{\left(s / 2+\mathbf{p}_{i} \cdot \mathbf{p}_{B}\right)^{2} / E_{i}^{2}-\mathbf{p}_{B}^{2}}$, where $\mathbf{p}_{B}$ is the $B$ momentum and $\left(E_{i}, \mathbf{p}_{i}\right)$ is the fourmomentum of the $\mathrm{Y}(4 \mathrm{~S})$ in the laboratory frame. We require these variables to be in the ranges $|\Delta E|<$ 0.1 GeV and $5.22<m_{\mathrm{ES}}<5.29 \mathrm{GeV} / c^{2}$. We construct a Fisher discriminant $(\mathcal{F})$ [13] using a linear combination of five event-shape variables: the cosine of the angle between the $B$-candidate momentum and the beam axis, the cosine of the angle between the $B$-candidate thrust axis and the beam axis, the zeroth and second angular moments of the energy flow about the thrust axis of the $B$ [2], and the output of the $B$-flavor tagging algorithm, which uses the information from the other $B$ [14]. This forms a more efficient Fisher discriminant than used in our previous measurement, Ref. [4].

Other $B$-meson decays can mimic a $K_{S}^{0} \pi^{+} \pi^{-}$final state. MC events are used to identify the $B$ decays that contribute background events to the data sample, and we use the available information on exclusive measurements [11,15] to find how many events from this background to expect in the data set. The largest $B$ background is seen to come from quasi two-body decays including charmonium mesons such as $J / \psi K_{S}^{0}, \chi_{c 0} K_{S}^{0}$ and $\psi(2 S) K_{S}^{0}$. In these cases the charmonium meson decays to $\pi^{+} \pi^{-}$or to $\mu^{+} \mu^{-}$that are misidentified as pions. Most of these events are removed by vetoing the reconstructed $\pi^{+} \pi^{-}$masses consistent with $3.04<m_{\pi^{+} \pi^{-}}<3.16 \mathrm{GeV} / c^{2}, \quad 3.32<m_{\pi^{+} \pi^{-}}<$ $3.51 \mathrm{GeV} / c^{2}$ and $3.63<m_{\pi^{+} \pi^{-}}<3.74 \mathrm{GeV} / c^{2}$, identifying the $J / \psi, \chi_{c 0}$ and $\psi(2 S)$ mesons, respectively. From simulated data we estimate that $126 \pm 8 B^{0} \rightarrow J / \psi K_{S}^{0}$ events and $6 \pm 3 B^{0} \rightarrow \psi(2 S) K_{S}^{0}$ events fall outside these vetoes, and these are included in the model. We veto events that are consistent with $B^{0} \rightarrow D^{-}\left(\rightarrow K_{S}^{0} \pi^{-}\right) \pi^{+}$by excluding those with $1.8<m_{K_{S}^{0} \pi}<1.91 \mathrm{GeV} / c^{2}$. However, Monte Carlo simulation shows that $71 \pm 8 B^{0} \rightarrow D^{-}(\rightarrow$ $\left.K_{S}^{0} \pi^{-}\right) \pi^{+}$background events still remain, where the reconstructed $D^{\mp}$ mass falls outside the veto as a result of using a $K_{S}^{0}$ or a $\pi$ from the other $B$ decay in the event. Other incorrectly reconstructed charmed decays $B \rightarrow D^{(*)} X$ are also included in the model.

After the above selection criteria are applied, $12.4 \%$ of events have more than one candidate that satisfies the
selection criteria. In a signal MC study, selecting the candidate whose $\cos \theta_{T}$ value is closest to zero is found to select the true signal candidate in $69.2 \%$ of such events. These requirements result in a final sample size of approximately 80000 events.

After all requirements, the largest charmless $B$ background to the $B^{0} \rightarrow K_{S}^{0} \pi^{+} \pi^{-}$measurement is the decay $B^{0} \rightarrow \eta^{\prime} K_{S}^{0}, \eta^{\prime} \rightarrow \rho^{0}(770) \gamma, \rho^{0} \rightarrow \pi^{+} \pi^{-}$, which tends to peak in the signal region and which contributes $54 \pm 19$ events. Table I shows the $B$-background modes for the $B^{0} \rightarrow K^{* \pm} \pi^{\mp}$ and $B^{0} \rightarrow f_{0} K_{S}^{0}$ channels. These events are effectively subtracted from the measured signal. To measure the nonresonant $B^{0} \rightarrow K_{S}^{0} \pi^{+} \pi^{-}$, we select a region of the Dalitz plot believed to be free of resonances, $(3<$ $m_{\pi^{+} \pi^{-}}<4 \mathrm{GeV} / c^{2}$ and $m_{K_{S}^{0} \pi^{ \pm}}>1.91 \mathrm{GeV} / c^{2}$ ). Backgrounds from other $B$ decays and from continuum events are subtracted. Assuming a uniform nonresonant distribution in the Dalitz plane, we set an upper limit of $2.1 \times 10^{-6}$ at a $90 \%$ confidence level on the nonresonant $B^{0} \rightarrow$ $K_{S}^{0} \pi^{+} \pi^{-}$branching fraction. All other branching fractions are taken from Refs. [11,15].

We use an extended maximum likelihood fit to extract the signal yield for each of the channels being investigated. The likelihood function for $N$ events is:

$$
\begin{equation*}
\mathcal{L}=\exp \left(-\sum_{j} N_{j}\right) \prod_{i}^{N}\left(\sum_{j=1}^{M} N_{j} P_{j}\left(\vec{x}_{i}\right)\right) \tag{2}
\end{equation*}
$$

where $i$ and $j$ are integers, $M$ is the number of hypotheses (signal, continuum background and $B$ background), $N_{j}$ is the number of events for the $j$ th hypothesis determined by maximizing the likelihood function, and $P_{j}\left(\vec{x}_{i}\right)$ is a probability density function (PDF) evaluated using the vector $\vec{x}_{i}$, in this case $m_{\mathrm{ES}}, \Delta E$, and $\mathcal{F}$. Correlations between these variables are small for signal and continuum background hypotheses and the total PDF is a product $P_{j}\left(\vec{x}_{i}\right)=$ $P_{j}\left(m_{\mathrm{ES}}\right) \cdot P_{j}(\Delta E) \cdot P_{j}(\mathcal{F})$. However for $B$ background, it is necessary to account for correlations observed between

TABLE I. The $B$-background modes for the channels $B^{0} \rightarrow$ $K^{* \pm} \pi^{\mp}$ and $B^{0} \rightarrow f_{0} K_{S}^{0} . B^{0} \rightarrow \rho^{0} K_{S}^{0}$ is included at a level consistent with Ref. [3]. $K^{* *}$ refers to heavier $K^{*}$ resonances, e.g. $K_{0}^{*}(1430)$.
\(\left.$$
\begin{array}{lcc}\hline B \text {-background } \\
\text { Mode }\end{array}
$$ $$
\begin{array}{c}\text { Number Expected } \\
\left(B^{0} \rightarrow K^{* \pm} \pi^{\mp}\right)\end{array}
$$ \begin{array}{c}Number Expected <br>

\left(B^{0} \rightarrow f^{0} K_{S}^{0}\right)\end{array}\right]\)| $B^{0} \rightarrow K^{* \pm} \pi^{\mp}$ | - | - |
| :--- | :---: | :---: |
| $B^{0} \rightarrow f_{0} K_{S}^{0}$ | $4 \pm 1$ | $14 \pm 4$ |
| $B^{0} \rightarrow \rho^{0} K_{S}^{0}$ | $5 \pm 2$ | $4 \pm 1$ |
| $B^{0} \rightarrow K^{* * \pm} \pi^{\mp}$ | $23 \pm 3$ | $5 \pm 1$ |
| Nonresonant | $7 \pm 1$ | 0 |
| $B^{0} \rightarrow D^{\mp} \pi^{ \pm}$ | $16 \pm 2$ | $19 \pm 7$ |
| $B^{0} \rightarrow \eta^{\prime} K_{S}^{0}$ | $1 \pm 1$ | 0 |
| $B^{0} \rightarrow J / \psi K_{S}^{0}$ | $6 \pm 1$ | 0 |

$m_{\mathrm{ES}}$ and $\Delta E$ by using a two-dimensional PDF for these variables.

The parameters of the signal and $B$-background PDFs are determined from MC simulation and fixed in the fit, along with the $B$-background normalization. The continuum background parameters are allowed to vary in the fit, to help reduce systematic effects from this dominant event type. Sideband data (which lie in the region $0.1<\Delta E<$ 0.3 GeV and $5.22<m_{\mathrm{ES}}<5.29 \mathrm{GeV} / c^{2}$ ) are used to model the continuum background PDFs. For the $m_{\mathrm{ES}}$ PDFs, a Gaussian distribution is used for signal and a threshold function [16] for continuum. For the $\Delta E$ PDFs, a sum of two Gaussian distributions with the same means is used for the signal and a first-order polynomial for the continuum background. Finally, for the $\mathcal{F}$ PDFs, a sum of two Gaussian distributions with distinct means and widths is used for signal and a sum of two Gaussian distributions with the same means is used to model the continuum background. The Fisher discriminant distribution of the $B$ backgrounds is modeled by an asymmetric Gaussian distribution that has different widths above and below the modal value. We use $B^{0} \rightarrow D^{-}\left(\rightarrow K_{S}^{0} \pi^{-}\right) \pi^{+}$as a calibration mode since it exhibits a one-to-one signal to continuum background ratio, allowing the signal parameters in a fit to be floated. A fit to these data is used in order to quantify any corrections and uncertainties due to MC. These corrections are applied to the fits to the charmless data sample.

To extract the branching fractions for the decay modes $B^{0} \rightarrow K^{*+} \pi^{-}$and $B^{0} \rightarrow f_{0} K^{0}$ we use the relation

$$
\begin{equation*}
\mathcal{B}=\frac{N_{\mathrm{sig}}}{2 N_{B^{0} \overline{B^{0}}} \varepsilon}, \tag{3}
\end{equation*}
$$

where $N_{\text {sig }}$ is the number of signal events fitted, $\varepsilon$ is the signal efficiency obtained from MC and $N_{B^{0} \bar{B}^{0}}$ is the total number of $B^{0} \bar{B}^{0}$ pairs.

For the charmless $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$branching fraction (and also for the nonresonant upper limit in the $B$-background studies above), it is necessary to account for the variation in efficiency, between approximately 5\% and $40 \%$, across the Dalitz plot and to know how the signal events are distributed across the Dalitz plot. To do this we assign to the $j$ th event $\mathcal{W}_{j}=\sum_{i} V_{s i g, i} P_{i}\left(\vec{x}_{j}\right) / \sum_{k} N_{k} P_{k}\left(\vec{x}_{j}\right)$ where $V_{\text {sig }, i}$ are the signal components of the covariance matrix obtained from the fit. This procedure projects out the signal distributions [17] shown in Figs. 1-4. The branching fraction is then calculated as $\mathcal{B}=$ $\sum_{j} \mathcal{W}_{j} /\left(\varepsilon_{j} N_{B^{0} B^{0}}\right)$, where $\varepsilon_{j}$ is the efficiency, as a function of Dalitz plot position, simulated in small bins using high statistics MC.

Figure 1 shows the signal distributions for $B^{0} \rightarrow$ $K^{0} \pi^{+} \pi^{-}$candidates and the distributions of events for all hypotheses. Figure 2 shows the signal distributions for both the $B^{0} \rightarrow K^{*+} \pi^{-}$and $B^{0} \rightarrow f_{0} K^{0}$ channels. The fitted signal yield and measured branching fraction are shown in


FIG. 1 (color online). Plots of the maximum likelihood fit to data for $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$candidates. Plots (a)-(c) show the distributions of all events that pass the selection criteria for (a) $m_{\mathrm{ES}}$ (b) $\Delta E$ and (c) Fisher, with the solid (blue) line indicating the total model, the (red) dotted line indicating shape of the continuum background model and the (black) dashed line indicating the signal model. Plots (d)-(f) show the signal distributions for (d) $m_{E S}$, (e) $\Delta E$ and (f) Fisher, where the (black) circles are the signal distribution [17] and the solid (blue) curve is the signal PDF that was fitted in the maximum likelihood fit.

Table II for all the modes under study. The average efficiency for $B^{0} \rightarrow K_{S}^{0} \pi^{+} \pi^{-}$signal events is $16.8 \%$ and the continuum background yield is $79000 \pm 280$ events. Figure 3 shows the signal mass projections of $m_{K_{S}^{0} \pi}$ and $m_{\pi^{+} \pi^{-}}$using $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$candidates. The $m_{K_{s}^{0} \pi}$ distribution clearly shows a peak at $0.9 \mathrm{GeV} / c^{2}$, corresponding to the $K^{*+}$ (892) mass and there is a broad structure above $1 \mathrm{GeV} / c^{2}$ that is the region where heavier kaon resonances can occur. The $m_{\pi^{+} \pi^{-}}$distribution shows evidence for resonance structure around $1 \mathrm{GeV} / c^{2}$ that corresponds to the $f_{0}$ and a broader structure below this that may be attributed as the $\rho^{0}(770)$. Figure 4 shows the efficiency corrected signal distribution of the cosine of the helicity angle, $\theta_{H}$, for $B^{0} \rightarrow K^{*+} \pi^{-}$.

Table III shows the systematic uncertainties that are assigned to the branching fraction measurements. Control channels in data and MC are used to assign uncertainties due to pion tracking, particle identification, and $K_{S}^{0}$ reconstruction efficiency. To calculate uncertainties due to the fitting procedure, a large number of MC samples are generated from the fitted PDFs, containing the amounts of signal and continuum events that are measured in data and the number of $B$-background events that were antici-


FIG. 2 (color online). Maximum likelihood fits for signal distributions. For $B^{0} \rightarrow K^{*+} \pi^{-}$the plots show (a) $m_{\mathrm{ES}}$, (b) $\Delta E$, and (c) the Fisher discriminant. The (black) circles are the signal distribution extracted from the data with the method of Ref. [17] and the solid curve is the signal PDF that resulted from the maximum likelihood fit. For $B^{0} \rightarrow f_{0} K^{0}$, plots show the distributions for (d) $m_{\mathrm{ES}}$, (e $\Delta E$, and (f) the Fisher discriminant, in an analogous fashion.
pated for the data set, as explained above. The differences between the generated and fitted values using these samples are used to ascertain the sizes of any biases. Small biases of the order of a few percent are observed that are a consequence of small correlations between fit variables and are therefore assigned as systematic uncertainties.

TABLE II. Signal yields and branching fractions for $B^{0} \rightarrow$ $K^{0} \pi^{+} \pi^{-}, B^{0} \rightarrow K^{*+} \pi^{-}$and $B^{0} \rightarrow f_{0} K^{0}$ where the first uncertainty is statistical and where, in the case of the branching fraction measurements, the second uncertainty is systematic and any third uncertainty is due to possible interference effects. The efficiency of selecting $B^{0} \rightarrow K^{*+}\left(\rightarrow K_{S}^{0} \pi^{+}\right) \pi^{-}$and $B^{0} \rightarrow$ $f_{0}\left(\rightarrow \pi^{+} \pi^{-}\right) K_{S}^{0}$ events was found to be $24 \%$ and $27 \%$ respectively, while the continuum background yields were $7300 \pm 86$ events and $13000 \pm 110$ events, respectively. The $B^{0} \rightarrow K^{*+} \pi^{-}$ branching fraction takes into account that $\mathcal{B}\left(K^{*+} \rightarrow K^{0} \pi^{+}\right)=$ $2 / 3$, assuming isospin symmetry.

| Mode | Signal Events <br> Yield | Branching Fraction <br> $(\times 10-6)$ |
| :--- | :---: | :---: |
| $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$ | $860 \pm 47$ | $43.0 \pm 2.3 \pm 2.3$ |
| $B^{0} \rightarrow f_{0}\left(\rightarrow \pi^{+} \pi^{-}\right) K^{0}$ | $120 \pm 16$ | $5.5 \pm 0.7 \pm 0.6 \pm 0.3$ |
| $B^{0} \rightarrow K^{*+} \pi^{-}$ | $140 \pm 19$ | $11.0 \pm 1.5 \pm 0.5 \pm 0.4$ |



FIG. 3 (color online). (a) shows the $m_{K_{S}^{0} \pi}$ signal distribution of $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$candidates [17]. The one-dimensional distribution is obtained by merging $m_{K \pi^{+}}^{2}$ and $m_{K \pi^{-}}^{2}$ into one ( $m_{K \pi}^{2}$ ) by folding the Dalitz plane along the line corresponding to $m_{K \pi^{+}}^{2}=m_{K \pi^{-}}^{2}$ in order to obtain the above $m_{K \pi}$ mass distribution. (b) shows the $m_{\pi^{+}} \pi^{-}$signal distribution of $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$ candidates [17]. The dashed lines indicate the expected mass of the labeled resonances.


FIG. 4. Distribution of the efficiency corrected cosine of the helicity angle, $\theta_{H}$, for $B^{0} \rightarrow K^{* \pm} \pi^{\mp}$ signal events.

TABLE III. Summary of contributions to the systematic uncertainty in the branching fractions measurements of $B^{0} \rightarrow$ $K^{0} \pi^{+} \pi^{-}, B^{0} \rightarrow K^{*+} \pi^{-}$and $B^{0} \rightarrow f_{0} K^{0}$. The uncertainties are shown as a percentage of the measured branching fraction.

| Error <br> source | $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$ <br> Error (\%) | $B^{0} \rightarrow f_{0} K^{0}$ <br> Error (\%) | $B^{0} \rightarrow K^{*+} \pi^{-}$ <br> Error $(\%)$ |
| :--- | :---: | :---: | :---: |
| Particle ID | 1.9 | 1.9 | 1.9 |
| Tracking | 1.6 | 1.6 | 1.6 |
| $K_{S}^{0}$ efficiency | 1.4 | 1.6 | 1.5 |
| Fit Bias | 1.7 | 6.1 | 2.6 |
| PDF params. | 0.1 | 0.1 | 0.3 |
| $B$ background | 4.2 | 5.9 | 2.0 |
| Efficiency | 0.9 | 0.1 | 0.1 |
| No. of $B \bar{B}$ | 1.1 | 1.1 | 1.1 |
| TOTAL | 5.4 | 9.1 | 4.5 |
| Interference | - | 4.7 | 4.0 |

The uncertainty of the $B$-background contribution to the fit is estimated by varying the measured branching fractions within their uncertainties. Each background is varied by $\pm 1 \sigma$ [11] and the effect on the fitted signal yield is added as a contribution to the uncertainty. For $B^{0} \rightarrow$ $K^{*+} \pi^{-}$there is an additional uncertainty in the $B$-background contributions due to the possible lineshapes of the $K_{0}^{* \pm}(1430)$, which can alter the amount of $B$ background expected. In order to assign a systematic uncertainty, fits to data are performed using two parametrizations, a relativistic Breit-Wigner lineshape and the LASS parametrization [18]. The latter is a coherent sum of a relativistic Breit-Wigner and an effective range term, and is used in the analysis of $B^{ \pm} \rightarrow K^{ \pm} \pi^{\mp} \pi^{ \pm}$[19]. The uncertainty due to simulated PDFs is obtained from the channel $B^{0} \rightarrow D^{-}\left(\rightarrow K_{S}^{0} \pi^{-}\right) \pi^{+}$and by varying the PDFs according to the precision of the parameters obtained from MC. In order to take correlations between parameters into account, the full correlation matrix is used when varying parameters. All PDF parameters that are originally fixed in the fit are then varied in turn and each difference from the nominal fit is combined and taken as a systematic uncertainty. The uncertainty in the efficiency is due to limited MC statistics, where over 1000000 MC events are generated for the decay $B^{0} \rightarrow K^{0} \pi^{+} \pi^{-}$and over 150000 MC events are generated for the decays $B^{0} \rightarrow$ $K^{*+} \pi^{-}$and $B^{0} \rightarrow f_{0} K_{S}^{0}$. The same uncertainty in the number of $B \bar{B}$ events is used for all channels.

For the quasi two-body modes, possible interference effects between the final state modes were investigated
by simulating the Dalitz plot using the measured branching fractions and random phases. The root-mean-squared of the distribution of the branching fraction is taken to be the uncertainty.

We measure the $C P$-violating charge asymmetry for the decay $B^{0} \rightarrow K^{*+} \pi^{-}$to be $\mathcal{A}_{K^{*} \pi}=-0.11 \pm 0.14 \pm 0.05$, where the first uncertainty is statistical and the second uncertainty is systematic. The charge asymmetry in the background is expected to be zero, as is the charge asymmetry in signal and background of the self-tagging decay $B^{0} \rightarrow D^{-} \pi^{+}$. As a cross-check, these are measured to be $-0.018 \pm 0.009,-0.013 \pm 0.029$ and $0.005 \pm 0.031$ respectively, where the uncertainties are statistical only.

The systematic uncertainty on $\mathcal{A}_{K^{*} \pi}$ is calculated by considering contributions due to track finding, particle identification, fit biases and $B$-background asymmetry uncertainties. Biases due to track finding and particle identification were found to be negligible. The fit-bias contribution to the systematic uncertainty is calculated using a large number of MC samples. The contribution from $B$ background is calculated by varying the number of expected events within their uncertainties [11] and by assuming a conservative $C P$-violating asymmetry of $\pm 0.5$ as there are no available measurements for these decays. The resulting systematic uncertainty on the asymmetry is measured to be $\pm 0.05$.

In summary, the branching fractions for $B^{0} \rightarrow$ $K^{0} \pi^{+} \pi^{-}, B^{0} \rightarrow K^{*+} \pi^{-}$, and $B^{0} \rightarrow f_{0}\left(\rightarrow \pi^{+} \pi^{-}\right) K^{0}$ decaying to a $K_{S}^{0} \pi^{+} \pi^{-}$state are measured and all agree with previous measurements [2,4-6]. We measure the direct $C P$-violating parameter $\mathcal{A}_{K^{*} \pi}$ for the decay $B^{0} \rightarrow$ $K^{*+} \pi^{-}$, with no evidence of $C P$ violation with the statistics used. These results supersede the previous results of the BABAR Collaboration $[2,4]$.

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