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# MEASURING THE IMPACTS OF TEACHERS II: TEACHER VALUE-ADDED AND STUDENT OUTCOMES IN ADULTHOOD 

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#### Abstract

Are teachers' impacts on students' test scores ("value-added") a good measure of their quality? This question has sparked debate partly because of a lack of evidence on whether high value-added (VA) teachers who raise students' test scores improve students' long-term outcomes. Using school district and tax records for more than one million children, we find that students assigned to high-VA teachers in primary school are more likely to attend college, earn higher salaries, and are less likely to have children as teenagers. Replacing a teacher whose VA is in the bottom 5\% with an average teacher would increase the present value of students' lifetime income by approximately $\$ 250,000$ per classroom.


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How can we measure and improve the quality of teaching in primary schools? One prominent but controversial method is to evaluate teachers based on their impacts on students' test scores, commonly termed the "value-added" (VA) approach. ${ }^{1}$ School districts from Washington D.C. to Los Angeles have begun to calculate VA measures and use them to evaluate teachers. Advocates argue that selecting teachers on the basis of their VA can generate substantial gains in achievement (e.g., Gordon, Kane, and Staiger 2006, Hanushek 2009), while critics contend that VA measures are poor proxies for teacher quality (e.g., Baker et al. 2010, Corcoran 2010). The debate about teacher VA stems primarily from two questions. First, do the differences in test-score gains across teachers measured by VA capture causal impacts of teachers or are they biased by student sorting? Second, do teachers who raise test scores improve their students' outcomes in adulthood or are they simply better at teaching to the test?

We addressed the first question in the previous paper in this volume (Chetty, Friedman, and Rockoff 2014) and concluded that VA measures that control for lagged test scores exhibit little or no bias. This paper addresses the second question. ${ }^{2}$ We study the long-term impacts of teachers by linking information from an administrative dataset on students and teachers in grades 3-8 from a large urban school district spanning 1989-2009 with selected data from United States tax records spanning 1996-2011. We match approximately $90 \%$ of the observations in the school district data to the tax data, allowing us to track approximately one million individuals from elementary school to early adulthood, where we measure outcomes such as earnings, college attendance, and teenage birth rates.

We use two research designs to estimate the long-term impacts of teacher quality: cross-sectional comparisons across classrooms and a quasi-experimental design based on teacher turnover. The first design compares the outcomes of students who were assigned to teachers with different VA, controlling for a rich set of student characteristics such as prior test scores and demographics. We implement this approach by regressing long-term outcomes on the test-score VA estimates constructed in Chetty, Friedman, and Rockoff (2014). The identification assumption underlying this research design is selection on observables: unobserved determinants of outcomes in adulthood such as student ability must be unrelated to teacher VA conditional on the observable characteristics. Although this is a very strong assumption, the estimates from this approach closely match the quasi-experimental estimates for outcomes where we have adequate precision to implement both designs, supporting its validity.

We find that teacher VA has substantial impacts on a broad range of outcomes. A 1 SD improvement in teacher VA in a single grade raises the probability of college attendance at age 20 by 0.82 percentage points, relative to a sample mean of $37 \%$. Improvements in teacher quality also raise the quality of the colleges

[^0]that students attend, as measured by the average earnings of previous graduates of that college. Students who are assigned higher VA teachers have steeper earnings trajectories in their 20s. At age 28, the oldest age at which we currently have a sufficiently large sample size to estimate earnings impacts, a 1 SD increase in teacher quality in a single grade raises annual earnings by $1.3 \%$. If the impact on earnings remains constant at $1.3 \%$ over the lifecycle, students would gain approximately $\$ 39,000$ on average in cumulative lifetime income from a 1 SD improvement in teacher VA in a single grade. Discounting at a 5\% rate yields a present value gain of $\$ 7,000$ at age 12 , the mean age at which the interventions we study occur. We also find that improvements in teacher quality significantly reduce the probability of having a child while being a teenager, increase the quality of the neighborhood in which the student lives (as measured by the percentage of college graduates in that ZIP code) in adulthood, and raise participation rates in $401(\mathrm{k})$ retirement savings plans.

Our second design relaxes the assumption of selection on observables by exploiting teacher turnover as a quasi-experimental source of variation in teacher quality. To understand this research design, suppose a high-VA 4th grade teacher moves from school $A$ to another school in 1995. Because of this staff change, students entering grade 4 in school $A$ in 1995 will have lower quality teachers on average than those in the prior cohort. If high VA teachers improve long-term outcomes, we would expect college attendance rates and earnings for the 1995 cohort to be lower on average than the previous cohort. Building on this idea, we estimate teachers' impacts by regressing changes in mean adult outcomes across consecutive cohorts of children within a school on changes in the mean VA of the teaching staff.

Using this design, we find that a 1 SD improvement in teacher VA raises the probability of college attendance at age 20 by 0.86 percentage points, nearly identical to the estimate obtained from our first research design. Improvements in average teacher VA also increase the quality of colleges that students attend. The impacts on college outcomes are statistically significant with $p<0.01$. Unfortunately, we have insufficient precision to obtain informative estimates for earnings using the quasi-experimental design.

Our quasi-experimental results rest on the identification assumption that high-frequency teacher turnover within school-grade cells is uncorrelated with student and school characteristics. Several pieces of evidence support this assumption. First, predetermined student and parent characteristics are uncorrelated with changes in the quality of teaching staff. Second, students' prior test scores and contemporaneous scores in the other subject are also uncorrelated with changes in the quality of teaching staff in a given subject. Third, changes in teacher VA across cohorts have sharp effects on college attendance exactly in the year of the change but not in prior years or subsequent years.

The long-term impacts of teacher VA are slightly larger for females than males. Improvements in English teacher quality have larger impacts than improvements in math teacher quality. The impacts of teacher VA
are roughly constant in percentage terms by parents' income. Hence, higher income households, whose children have higher earnings on average, should be willing to pay larger amounts for higher teacher VA. Teachers' impacts are significant and large throughout grades 4-8, showing that improvements in the quality of education can have large returns well beyond early childhood.

Our conclusion that teachers have long-lasting impacts may be surprising given evidence that teachers' impacts on test scores "fade out" very rapidly in subsequent grades (Rothstein 2010, Carrell and West 2010, Jacob, Lefgren, and Sims 2010). We confirm this rapid fade-out in our data, but find that teachers' impacts on earnings are similar to what one would predict based on the cross-sectional correlation between earnings and contemporaneous test score gains. This pattern of fade-out and re-emergence echoes the findings of recent studies of early childhood interventions (Deming 2009, Heckman et al. 2010b, Chetty et al. 2011).

To illustrate the magnitude of teachers' impacts, we evaluate Hanushek's (2009) proposal to replace teachers in the bottom $5 \%$ of the VA distribution with teachers of average quality. We estimate that replacing a teacher whose current VA is in the bottom 5 percent with an average teacher would increase the mean present value of students' lifetime income by $\$ 250,000$ per classroom over a teacher's career, accounting for drift in teacher quality over time. ${ }^{3}$ However, because VA is estimated with noise, the gains from deselecting teachers based on data from a limited number of classrooms are smaller. The present value gain from deselecting the bottom $5 \%$ of teachers using three years of test score data is $\$ 185,000$ per classroom on average. ${ }^{4}$ This gain is still about 10 times larger than recent estimates of the additional salary one would have to pay teachers to compensate them for the risk of evaluation based on VA measures (Rothstein 2013). This result suggests that VA could potentially be a useful tool for evaluating teacher performance if the signal quality of VA for long-term impacts does not fall substantially when it is used to evaluate teachers.

We also evaluate the expected gains from policies that pay bonuses to high-VA teachers to increase retention rates. The gains from such policies are only slightly larger than their costs because most bonus payments end up going to high-VA teachers who would have stayed even without the additional payment. Replacing low VA teachers may therefore be a more cost effective strategy to increase teacher quality in the short run than paying bonuses to retain high-VA teachers. In the long run, higher salaries could attract more high VA teachers to the teaching profession, a potentially important benefit that we do not measure here.

The paper is organized as follows. In Section I, we formalize our estimating equations and explain how the parameters we estimate should be interpreted using a simple statistical model. Section II describes the data sources and reports summary statistics as well as cross-sectional correlations between test scores and

[^1]adult outcomes. Sections III and IV present results on teachers' long-term impacts using the two research designs described above. We analyze the heterogeneity of teachers' impacts in Section V. Section VI presents policy simulations and Section VII concludes.

## I. Conceptual Framework

In this section, we first present a simple statistical model of students' long-term outcomes as a function of their teachers' value-added. We then describe how the reduced-form parameters of this statistical model should be interpreted. Finally, we show how we estimate the impacts of teacher VA on long-term outcomes given that each teacher's true value-added is unobserved.

Statistical Model. Consider the outcomes of a student $i$ who is in grade $g$ in calendar year $t_{i}(g)$. Let $j=j(i, t)$ denote student $i$ 's teacher in school year $t$; for simplicity, assume that the student has only one teacher throughout the school year, as in elementary schools. Let $\mu_{j t}$ represent teacher $j$ 's "test-score value-added" in year $t$, so that student $i$ 's test score in year $t$ is

$$
\begin{equation*}
A_{i t}^{*}=\boldsymbol{\beta} \mathbf{X}_{i t}+\mu_{j t}+\varepsilon_{i t} . \tag{1}
\end{equation*}
$$

Here, $\mathbf{X}_{i t}$ denotes observable determinants of student achievement, such as lagged test scores and family characteristics and $\varepsilon_{i t}$ denotes a student-level error that may be correlated across students within a classroom and with teacher value-added $\mu_{j t}$. We scale $\mu_{j t}$ in student test-score SDs so that the average teacher has $\mu_{j t}=0$ and the effect of a 1 unit increase in teacher value-added on end-of-year test scores is 1 . We allow teacher quality $\mu_{j t}$ to vary with time $t$ to account for the stochastic drift in teacher quality documented in our companion paper (Chetty, Friedman, and Rockoff 2014).

Let $Y_{i}^{*}$ denote student $i$ 's earnings in adulthood. Throughout our analysis, we focus on earnings residuals after removing the effect of observable characteristics:

$$
\begin{equation*}
Y_{i t}=Y_{i}^{*}-\boldsymbol{\beta}^{Y} \mathbf{X}_{i t} \tag{2}
\end{equation*}
$$

The earnings residuals $Y_{i t}$ vary across school years because the control vector $\mathbf{X}_{i t}$ varies across school years. We estimate the coefficient vector $\boldsymbol{\beta}^{Y}$ using variation across students taught by the same teacher using an OLS regression

$$
\begin{equation*}
Y_{i}^{*}=\alpha_{j}+\boldsymbol{\beta}^{Y} \mathbf{X}_{i t} \tag{3}
\end{equation*}
$$

where $\alpha_{j}$ is a teacher fixed effect. Importantly, we estimate $\boldsymbol{\beta}^{Y}$ using within-teacher variation to account for the potential sorting of students to teachers based on VA. If teacher VA is correlated with $\mathbf{X}_{i t}$, estimates of $\boldsymbol{\beta}^{Y}$ in a specification without teacher fixed effects are biased because part of the teacher effect is attributed
to the covariates. See Section I.B of our companion paper for further discussion of this issue.
We model the relationship between earnings residuals and teacher VA in school year $t$ using the following linear specification:

$$
\begin{equation*}
Y_{i t}=a+\kappa_{g} m_{j t}+\eta_{i t} \tag{4}
\end{equation*}
$$

where $m_{j t}=\mu_{j t} / \sigma_{\mu}$ denotes teacher $j$ 's "normalized value-added" (i.e., teacher quality scaled in standard deviation ( $\sigma_{\mu}$ ) units of the teacher VA distribution).

Interpretation of Reduced-Form Treatment Effects. The parameter $\kappa_{g}$ in (4) represents the reduced-form impact of a 1 SD increase in teachers' test-score VA in a given school year $t$ on earnings. There are two important issues to keep in mind when interpreting this parameter, which we formalize using a dynamic model of education production in Appendix A.

First, the reduced-form impact combines two effects: the direct impact of having a higher VA teacher in grade $g$ and the indirect impact of endogenous changes in other educational inputs. For example, other determinants of earnings such as investments in learning by children and their parents might respond endogenously to changes in teacher quality. One particularly important endogenous response is that a higher achieving student may be tracked into classes taught by higher quality teachers. Such tracking would lead us to overstate the impacts of improving teacher quality in grade $g$ holding fixed the quality of teachers in subsequent grades. In Section V.C, we estimate the degree of teacher tracking and use these estimates to identify the impact of having a higher VA teacher in each grade holding fixed future teacher quality, which we denote by $\widetilde{\kappa}_{g}$. The degree of tracking turns out to be relatively small in our data, and thus the reducedform estimates of $\kappa_{g}$ reported below are similar to the net impacts of each teacher $\widetilde{\kappa}_{g}{ }^{5}$ Although the net impacts $\widetilde{\kappa}_{g}$ still combine several structural parameters - such as endogenous responses by parents and children to changes in teacher quality - they are relevant for policy. For example, the ultimate earnings impact of retaining teachers on the basis of their VA depends on $\widetilde{\kappa}_{g}$.

Second, $\widetilde{\kappa}_{g}$ measures only the portion of teachers' earnings impacts that are correlated with their impacts on test scores. As a result, $\widetilde{\kappa}_{g}$ is a lower bound for the standard deviation of teachers' effects on earnings. Intuitively, some teachers may be effective at raising students' earnings even if they are not effective at raising test scores, for instance by directly instilling other skills that have long-term payoffs (Jackson 2013). In principle, one could estimate teacher $j$ 's "earnings value-added" $\left(\mu_{j t}^{Y}\right)$ based on the mean residual earnings of her students, exactly as we estimated test-score VA in our first paper. Unfortunately, the orthogonality condition required to obtain unbiased forecasts of teachers' earnings VA - that students' earnings are orthog-

[^2]onal to earnings VA estimates - does not hold in practice, as we discuss in Appendix A. We therefore focus on estimating the effect of being assigned to a high test-score VA teacher on earnings ( $\kappa_{g}$ ). Although $\kappa_{g}$ does not correspond directly to earnings VA, it reveals the extent to which the test-score based VA measures currently used by school districts are informative about teachers' long-term impacts.

Empirical Implementation. There are two challenges in estimating $\kappa_{g}$ using (4). First, unobserved determinants of earnings $\eta_{i t}$ may be correlated with teacher VA $m_{j t}$. We return to this issue in our empirical analysis and isolate variation in teacher VA that is orthogonal to unobserved determinants of earnings. Second, teachers' true test-score VA $m_{j t}$ is unobserved. We can solve this second problem by substituting estimates of teacher VA $\widehat{m}_{j t}=\hat{\mu}_{j t} / \sigma_{\mu}$ for true teacher VA in (4) under the following assumption.

Assumption 1 [Forecast Unbiasedness of Test-Score VA] Test-score value-added estimates $\widehat{\mu}_{j t}$ are forecast unbiased:

$$
\frac{\operatorname{Cov}\left(\mu_{j t}, \widehat{\mu}_{j t}\right)}{\operatorname{Var}\left(\widehat{\mu}_{j t}\right)}=\frac{\operatorname{Cov}\left(m_{j t}, \widehat{m}_{j t}\right)}{\operatorname{Var}\left(\widehat{m}_{j t}\right)}=1 .
$$

In our companion paper, we demonstrate that Assumption 1 holds for the VA estimates that we use in this paper. Equation (4) implies that $\operatorname{Cov}\left(Y_{i t}, \widehat{m}_{j t}\right)=\kappa_{g} \operatorname{Cov}\left(m_{j t}, \widehat{m}_{j t}\right)+\operatorname{Cov}\left(\eta_{i t}, \widehat{m}_{j t}\right)$. Hence, under Assumption 1,

$$
\frac{\operatorname{Cov}\left(Y_{i t}, \widehat{m}_{j t}\right)}{\operatorname{Var}\left(\widehat{m}_{j t}\right)}=\kappa_{g}+\frac{\operatorname{Cov}\left(\eta_{i t}, \widehat{m}_{j t}\right)}{\operatorname{Var}\left(\widehat{m}_{j t}\right)} .
$$

It follows that we can identify the impact of a 1 SD increase in a teacher's true VA $m_{j t}$ from an OLS regression of earnings residuals $Y_{i t}$ on teacher VA estimates $\widehat{m}_{j t}$,

$$
\begin{equation*}
Y_{i t}=\alpha+\kappa_{g} \widehat{m}_{j t}+\eta_{i t}^{\prime}, \tag{5}
\end{equation*}
$$

provided that unobserved determinants of earnings are orthogonal to teacher VA estimates $\widehat{m}_{j t}$.
Intuitively, we identify $\kappa_{g}$ using 2SLS by instrumenting for true teacher VA $m_{j t}$ with the teacher VA estimates we constructed in our companion paper. Forecast unbiasedness of test-score VA implies that the first stage of this 2SLS regression has a coefficient of 1 . Thus, the reduced form coefficient obtained from an OLS regression of earnings on VA estimates identifies $\kappa_{g}$.

The remainder of the paper focuses on estimating variants of (5). ${ }^{6}$

## II. Data

We draw information from two databases: administrative school district records and federal income tax records. This section describes the two data sources and the structure of the linked analysis dataset. We then provide descriptive statistics and report correlations between test scores and long-term outcomes as a

[^3]benchmark to interpret the magnitude of the causal effects of teachers. Note that the dataset we use in this paper is identical to that used in our first paper, except that we restrict attention to the subset of students who are old enough for us to observe outcomes in adulthood by 2011.

## A. School District Data

We obtain information on students, including enrollment history, test scores, and teacher assignments from the administrative records of a large urban school district. These data span the 1988-1989 through 2008-2009 school years and cover roughly 2.5 million children in grades 3-8. For simplicity, we refer to school years by the year in which the spring term occurs (e.g., the school year 1988-1989 is 1989). We summarize the key features of the data relevant for our analysis of teachers' long-term impacts here; see Section II of our first paper for a comprehensive description of the school district data.

Test Scores. The data include approximately 18 million test scores. Test scores are available for English language arts and math for students in grades 3-8 in every year from the spring of 1989 to 2009, with the exception of 7th grade English scores in 2002. We follow prior work by normalizing the official scale scores from each exam to have mean zero and standard deviation one by year and grade. The within-grade variation in achievement in the district we examine is comparable to the within-grade variation nationwide, so our results can be compared to estimates from other samples.

Demographics. The dataset contains information on ethnicity, gender, age, receipt of special education services, and limited English proficiency for the school years 1989 through 2009. The database used to code special education services and limited English proficiency changed in 1999, creating a break in these series that we account for in our analysis by interacting these two measures with a post-1999 indicator. Information on free and reduced price lunch is available starting in school year 1999.

Teachers. The dataset links students in grades 3-8 to classrooms and teachers from 1991 through 2009. This information is derived from a data management system which was phased in over the early 1990s, so not all schools are included in the first few years of our sample. In addition, data on course teachers for middle and junior high school students - who, unlike students in elementary schools, are assigned different teachers for math and English - are more limited. Course teacher data are unavailable prior to the school year 1994, then grow in coverage to roughly $60 \%$ by school year 1998 and $85 \%$ by 2003. These missing teacher links raise two potential concerns. First, our estimates (especially for grades 6-8) apply to a subset of schools with more complete information reporting systems and thus may not be representative of the district as a whole. Reassuringly, we find that these schools do not differ significantly from the sample as a whole on test scores and other observables. Second, and more importantly, missing data could generate biased estimates. We address this concern by showing that our estimates remain similar in a subsample of school-grade-subject cells with little or no missing data (Appendix Table 7).

Sample Restrictions. Starting from the raw dataset, we make a series of restrictions that parallel those in prior work to obtain our primary school district sample. First, because our estimates of teacher valueadded always condition on prior test scores, we restrict our sample to grades 4-8, where prior test scores are available. Second, we exclude the $6 \%$ of observations in classrooms where more than 25 percent of students are receiving special education services, as these classrooms may be taught by multiple teachers or have other special teaching arrangements. We also drop the $2 \%$ of observations where the student is listed as receiving instruction at home, in a hospital, or in a school serving solely disabled students. Third, we drop classrooms with less than 10 students or more than 50 students as well as teachers linked with more than 200 students in a single grade, because such students are likely to be mis-linked to classrooms or teachers ( $0.5 \%$ of observations). Fourth, when a teacher is linked to students in multiple schools during the same year, which occurs for $0.3 \%$ of observations, we use only the links for the school where the teacher is listed as working according to human resources records and set the teacher as missing in the other schools. Finally, because the adult outcomes we analyze are measured at age 20 or afterward, in this paper we restrict the sample to students who would have graduated high school by the 2008-09 school year (and thus turned 20 by 2011) if they progressed through school at a normal pace. ${ }^{7}$

## B. Tax Data

We obtain information on students' outcomes in adulthood from U.S. federal income tax returns spanning 1996-2011. ${ }^{8}$ The school district records were linked to the tax data using an algorithm based on standard identifiers (date of birth, state of birth, gender, and names) described in Appendix C of our companion paper, after which individual identifiers were removed to protect confidentiality. $87.4 \%$ of the students and $89.2 \%$ of student-subject-year observations in the sample used to analyze long-term impacts were matched to the tax data. ${ }^{9}$ We define students' outcomes in adulthood as follows.

Earnings. Individual wage earnings data come from W-2 forms, which are available from 1999-2011. Importantly, W-2 data are available for both tax filers and non-filers, eliminating concerns about missing data on formal sector earnings. We cap earnings in each year at $\$ 100,000$ to reduce the influence of outliers; $1.3 \%$ of individuals in the sample report earnings above $\$ 100,000$ at age 28 . We measure all monetary variables in 2010 dollars, adjusting for inflation using the Consumer Price Index. Individuals with no W-2 are coded as having 0 earnings. $33.1 \%$ of individuals have 0 wage earnings at age 28 in our sample.

[^4]Total Income. To obtain a more comprehensive definition of income, we define "total income" as the sum of W-2 wage earnings and household self-employment earnings (as reported on the 1040). For non-filers, we define total income as just W-2 wage earnings; those with no W-2 income are coded as having zero total income. $29.6 \%$ of individuals have 0 total income in our sample. ${ }^{10}$ We show that similar results are obtained using this alternative definition of income, but use W-2 wage earnings as our baseline measure because it (1) is unaffected by the endogeneity of tax filing and (2) provides a consistent definition of individual (rather than household) income for both filers and non-filers.

College Attendance. We define college attendance as an indicator for having one or more 1098-T forms filed on one's behalf. Title IV institutions - all colleges and universities as well as vocational schools and other postsecondary institutions eligible for federal student aid - are required to file 1098-T forms that report tuition payments or scholarships received for every student. Because the 1098-T forms are filed directly by colleges independent of whether an individual files a tax return, we have complete records on college attendance for all individuals. The 1098-T data are available from 1999-2011. Comparisons to other data sources indicate that 1098-T forms capture college enrollment accurately (see Appendix B).

College Quality. We construct an earnings-based index of college quality based on data from the universe of tax returns (not just the students from our school district). Using the population of all current U.S. citizens born in 1979 or 1980, we group individuals by the higher education institution they attended at age 20. We pool individuals who were not enrolled in any college at age 20 together in a separate "no college" category. For each college or university (including the "no college" group), we then compute the mean W-2 earnings of the students when they are age 31 (in 2010 and 2011). Among colleges attended by students in the school district studied in this paper, the average value of our earnings index is $\$ 44,048$ for four-year colleges and $\$ 30,946$ for two-year colleges. For students who did not attend college, the mean earnings level is $\$ 17,920$.

In Appendix B, we analyze the robustness of the college quality index to alternative specifications, such as measuring earnings and college attendance at different ages and defining the index based on total income instead of W-2 earnings. We find that rankings of college quality are very stable across cohorts and are robust to alternative specifications provided that earnings are measured after age 28 (Appendix Figure 1, Appendix Table 2).

Neighborhood Quality. We use data from 1040 forms to identify each household's ZIP code of residence in each year. For non-filers, we use the ZIP code of the address to which the W-2 form was mailed. If an individual did not file and has no W-2 in a given year, we impute current ZIP code as the last observed ZIP

[^5]code. We construct a measure of a neighborhood's SES using data on the percentage of college graduates in the individual's ZIP code from the 2000 Census.

Retirement Savings. We measure retirement savings using contributions to $401(\mathrm{k})$ accounts reported on W-2 forms from 1999-2011. We define saving for retirement as an indicator for contributing to a 401(k) at age 28.

Teenage Birth. We define a woman as having a teenage birth if she ever claims a dependent who was born while she was between the ages of 13 and 19 (as of $12 / 31$ in the year the child was born). This measure is an imperfect proxy for having a teenage birth because it only covers children who are claimed as dependents by their mothers and includes any other dependents who are not biological children but were born while the mother was a teenager. Despite these limitations, our proxy for teenage birth is closely aligned with estimates based on the American Community Survey (ACS). $15.8 \%$ of women in our core sample have teenage births, compared with $14.6 \%$ in the 2003 ACS. The unweighted correlation between state-level teenage birth rates in our data and the ACS is 0.80 .

Parent Characteristics. We also use the tax data to obtain information on five parent characteristics that we use as controls. Students were linked to parents based on the earliest 1040 form filed between tax years 1996 and 2011 on which the student was claimed as a dependent. We identify parents for $94.8 \%$ of the observations in the analysis dataset conditional on being matched to the tax data. ${ }^{11}$

We define parental household income as mean Adjusted Gross Income (capped at $\$ 117,000$, the 95 th percentile in our sample) between 2005 and 2007 for the primary filer who first claimed the child. ${ }^{12}$ Parents are assigned an income of 0 in years when they did not file a tax return. We define parental marital status, home ownership, and $401(\mathrm{k})$ saving as indicators for whether the first primary filer who claims the child ever files a joint tax return, makes a mortgage interest payment (based on data from 1040's for filers and 1099's for non-filers), or makes a 401(k) contribution (based on data from W-2's) between 2005 and 2007. Lastly, we define mother's age at child's birth using data from Social Security Administration records on birth dates for parents and children. For single parents, we define the mother's age at child's birth using the age of the filer who first claimed the child, who is typically the mother but is sometimes the father or another relative. ${ }^{13}$ When a child cannot be matched to a parent, we define all parental characteristics as zero, and we always include a dummy for missing parents in regressions that include parent characteristics.

[^6]
## C. Summary Statistics

The linked school district and tax record analysis dataset has one row per student per subject (math or English) per school year, as illustrated in Appendix Table 1. Each observation in the analysis dataset contains the student's test score in the relevant subject test, demographic information, and class and teacher assignment if available. Each row also includes all the students' available adult outcomes (e.g. college attendance and earnings at each age). We organize the data in this format so that each row contains information on a treatment by a single teacher conditional on pre-determined characteristics, facilitating the estimation of (5). We account for the fact that each student appears multiple times in the dataset by clustering standard errors as described in Section III.A.

After imposing the sample restrictions described above, the linked analysis sample contains 6.8 million student-subject-year observations (covering 1.1 million students) that we use to study teachers' long-term impacts. ${ }^{14}$ Table 1 reports summary statistics for this sample. Note that the summary statistics are student-subject-year means and thus weight students who are in the district for a longer period of time more heavily, as does our empirical analysis. On average, each student has 6.25 subject-school year observations.

The mean test score in the analysis sample is positive and has a standard deviation below 1 because we normalize the test scores in the full population that includes students in special education classrooms and schools (who typically have lower test scores). The mean age at which students are observed in school is 11.7 years. $77.1 \%$ of students are eligible for free or reduced price lunches.

The availability of data on adult outcomes naturally varies across cohorts. There are more than 5.9 million observations for which we observe college attendance at age 20. We observe earnings at age 25 for 2.3 million observations and at age 28 for 1.3 million observations. Because many of these observations at later ages are from older cohorts of students who were in middle school in the early 1990s, we were not able to obtain information on teachers. As a result, there are only 1.6 million student-subject-school year observations for which we see both teacher VA and earnings at age 25, 750,000 at age 28, and only 220,000 at age 30. The oldest age at which the sample is large enough to obtain informative estimates of teachers' impacts on earnings turns out to be age 28. Mean individual earnings at age 28 is $\$ 20,885$, while mean total income is $\$ 21,272$ (in 2010 dollars).

For students whom we are able to link to parents, the mean parent household income is $\$ 40,808$, while the median is $\$ 31,834$. Though our sample includes more low income households than would a nationally representative sample, it still includes a substantial number of higher income households, allowing us to analyze the impacts of teachers across a broad range of the income distribution. The standard deviation of

[^7]parent income is $\$ 34,515$, with $10 \%$ of parents earning more than $\$ 100,000$.

## D. Cross-Sectional Correlations

Appendix Tables 3-6 report coefficients from OLS regressions of various adult outcomes on test scores. Both math and English test scores are highly positively correlated with earnings, college attendance, and neighborhood quality and are negatively correlated with teenage births. In the cross-section, a 1 SD increase in test score is associated with a $\$ 7,700(36 \%)$ increase in earnings at age 28 . Conditional on the studentand class-level controls $\mathbf{X}_{i t}$ that we define in Section III.A below, a 1 SD increase in the current test score is associated with $\$ 2,600$ ( $12 \%$ ) increase in earnings on average.

Appendix Figure 2 presents binned scatter plots of selected outcomes vs. test scores both with and without controls. The unconditional relationship between scores and outcomes is S-shaped, while the relationship conditional on prior scores and other covariates is almost perfectly linear. We return to these results below and show that the causal impacts of teacher VA on earnings and other outcomes are commensurate to what one would predict based on these correlations.

## III. Research Design 1: Cross-Class Comparisons

Our first method of estimating teachers' long-term impacts builds on our finding that conditioning on prior test scores and other observables is adequate to obtain unbiased estimates of teachers' causal impacts on test scores (Chetty, Friedman, and Rockoff 2014). Given this result, one may expect that comparing the long-term outcomes of students assigned to different teachers conditional on the same control vector will yield unbiased estimates of teachers' long-term impacts. The next subsection formalizes the identification assumption and methodological details of this approach. We then present results for three sets of impacts: college attendance, earnings, and other outcomes such as teenage birth.

## A. Methodology

We begin by constructing earnings (or other long-term outcome) residuals $Y_{i t}=Y_{i}^{*}-\widehat{\boldsymbol{\beta}}^{Y} \mathbf{X}_{i t}$, estimating $\widehat{\boldsymbol{\beta}}^{Y}$ using within-teacher variation as in (3). We then regress students' earnings residuals on their teachers' normalized VA $\widehat{m}_{j t}$, pooling all grades and subjects:

$$
\begin{equation*}
Y_{i t}=\alpha+\kappa \widehat{m}_{j t}+\eta_{i t}^{\prime} \tag{6}
\end{equation*}
$$

Note that we do not residualize $\widehat{m}_{j t}$ with respect to the controls $\mathbf{X}_{i t}$ when estimating (6). In a partial regression, one typically residualizes $\widehat{m}_{j t}$ with respect to $\mathbf{X}_{i t}$ because the OLS regression of $Y_{i}^{*}$ on $\mathbf{X}_{i t}$ used to construct earnings residuals yields an estimate of $\boldsymbol{\beta}^{Y}$ that is biased by the correlation between and $\widehat{m}_{j t}$ and $\mathbf{X}_{i t}$. This problem does not arise here because we estimate $\boldsymbol{\beta}^{Y}$ from a regression with teacher fixed effects,
so the variation in $\mathbf{X}_{i t}$ used to identify $\boldsymbol{\beta}^{Y}$ is orthogonal to the variation in VA across teachers. ${ }^{15}$ Hence, regressing $Y_{i t}$ directly on $\widehat{m}_{j t}$ identifies the relationship between $Y_{i t}$ and $\widehat{m}_{j t}$ conditional on $\mathbf{X}_{i t}$.

Recall that each student appears in our dataset once for every subject-year with the same level of $Y_{i t}$ but different values of $\widehat{m}_{j t}$. Hence, $\kappa$ represents the mean impact of having a higher VA teacher for a single grade between grades 4-8. We present results on heterogeneity in impacts across grades and subgroups in Section V.

Estimating (6) using OLS yields an unbiased estimate of $\kappa$ under the following assumption.
Assumption 2 [Selection on Observables] Test-score value-added estimates are orthogonal to unobserved determinants of earnings conditional on $\mathbf{X}_{i t}$ :

$$
\begin{equation*}
\operatorname{Cov}\left(\widehat{m}_{j t}, \eta_{i t}^{\prime}\right)=0 . \tag{7}
\end{equation*}
$$

While we cannot be certain that conditioning on observables fully accounts for differences in student characteristics across teachers, as required by Assumption 2, the quasi-experimental evidence reported in the next section supports this assumption. In particular, quasi-experimental estimates of the impacts of teacher quality on test scores and college attendance are very similar to the estimates obtained from (6). ${ }^{16}$ This result supports the validity of the selection on observables assumption not only for test scores and college attendance but also for other outcomes as well, as any selection effects would presumably be manifested in all of these outcomes.

Four methodological issues arise in estimating (6): (1) estimating test-score VA $\widehat{m}_{j t}$, (2) specifying a control vector $\mathbf{X}_{i t}$, (3) calculating the standard error on $\kappa$, and (4) accounting for outliers in $\widehat{m}_{j t}$. The remainder of this subsection addresses these four issues. Note that our methodology closely parallels that in our companion paper. In particular, we use the same VA estimates and control vectors and calculate standard errors in the same way. We did not address outliers in our first paper because they only affect our analysis of long-term impacts, as we explain below.

Estimating Test-Score VA. We define normalized VA $\widehat{m}_{j t}=\widehat{\mu}_{j t} / \sigma_{\mu}$, where $\widehat{\mu}_{j t}$ is the baseline estimate of test-score VA for teacher $j$ in year $t$ constructed in our companion paper. ${ }^{17}$ We define $\sigma_{\mu}$ as the standard deviation of teacher effects for the corresponding subject and school-level using the estimates in Table 2 of our companion paper: 0.163 for math and 0.124 for English in elementary school and 0.134 for math and

[^8]0.098 for English in middle school. With this scaling, a 1 unit increase in $\widehat{m}_{j t}$ corresponds to a teacher who is rated 1 SD higher in the distribution of true teacher quality for her subject and school-level. Note that because $\widehat{\mu}_{j t}$ is shrunk toward the sample mean to account for noise in VA estimates, $S D\left(\widehat{\mu}_{j t}\right)<\sigma_{\mu}$ and hence the standard deviation of the normalized VA measure $\widehat{m}_{j t}$ is less than 1 . We demean $\widehat{m}_{j t}$ within each of the four subject (math vs. English) by school level (elementary vs. middle) cells in the estimation sample in (6) so that $\kappa$ is identified purely from variation within the subject-by-school-level cells.

Importantly, the VA estimates $\widehat{m}_{j t}$ are predictions of teacher quality in year $t$ based on test score data from all years excluding year $t$. For example, when predicting teachers' effects on the outcomes of students they taught in 1995, we estimate $\widehat{m}_{j, 1995}$ based on residual test scores from students in all years of the sample except 1995. To maximize precision, the VA estimates are based on data from all years for which school district data with teacher assignments are available (1991-2009), not just the subset of older cohorts for which we observe long-term outcomes.

Using a leave-year-out estimate of VA is necessary to obtain unbiased estimates of teachers' long-term impacts because of correlated errors in students' test scores and later outcomes. Intuitively, if a teacher is randomly assigned unobservably high ability students, her estimated VA will be higher. The same unobservably high ability students are likely to have high levels of earnings $\eta_{i t}^{\prime}$, generating a mechanical correlation between VA and earnings even if teachers have no causal effect $(\kappa=0)$. The leave-year-out approach eliminates this correlated estimation error bias because $\widehat{m}_{j t}$ is estimated using a sample that excludes the observations on the left hand side of (6). ${ }^{18}$

Control Vectors. We construct residuals $Y_{i t}$ using separate models for each of the four subject-by-schoollevel cells. Within each of these groups, we regress raw outcomes $Y_{i}^{*}$ on a vector of covariates $\mathbf{X}_{i t}$ with teacher fixed effects, as in (3), and compute residuals $Y_{i t}$. We partition the control vector $\mathbf{X}_{i t}$ that we used to construct our baseline VA estimates into two components: student-level controls $\mathbf{X}_{i t}^{I}$ that vary across students within a class and classroom-level controls $\mathbf{X}_{c t}$ that vary only at the classroom level. The studentlevel control vector $\mathbf{X}_{i t}^{I}$ includes cubic polynomials in prior-year math and English scores, interacted with the student's grade level to permit flexibility in the persistence of test scores as students age. We also control for the following student level characteristics: ethnicity, gender, age, lagged suspensions and absences, and indicators for grade repetition, free or reduced-price lunch, special education, and limited English. The class-level controls $X_{c t}$ consist of the following elements: (1) class size and class-type indicators (honors, remedial), (2) cubics in class and school-grade means of prior-year test scores in math and English (defined based on those with non-missing prior scores) each interacted with grade, (3) class and school-year means of all the individual covariates $\mathbf{X}_{i t}^{I}$, and (4) grade and year dummies.

[^9]In our baseline analysis, we control only for the class-level controls $\mathbf{X}_{c t}$ when estimating the residuals $Y_{i t}$. Let $Y_{c t}=Y_{c}^{*}-\boldsymbol{\beta}_{C} \mathbf{X}_{c t}$ denote the residual of mean outcomes $Y_{c}^{*}$ in class $c$ in year $t$, where $\boldsymbol{\beta}_{C}$ is estimated at the class level using within-teacher variation across classrooms as in (3), weighting by class size. We estimate the impact of teacher VA on mean outcomes using a class-level OLS regression analogous to (6), again weighting by class size:

$$
\begin{equation*}
Y_{c t}=\alpha+\kappa_{C} \widehat{m}_{j t}+\eta_{c t}^{\prime} \tag{8}
\end{equation*}
$$

The point estimate $\hat{\kappa}_{C}$ in (8) is identical to $\hat{\kappa}$ in (6) because teacher VA varies only at the classroom level. Formally, $\hat{\kappa}_{C}=\hat{\kappa}$ because deviations of individual-level controls $\left(\mathbf{X}_{i t}^{I}-\mathbf{X}_{c t}\right)$ and outcomes $\left(Y_{i}^{*}-Y_{c t}^{*}\right)$ from class means are uncorrelated with $\widehat{m}_{j t} .{ }^{19}$ Omitting individual-level controls allows us to implement our analysis on a dataset collapsed to classroom means, reducing computational costs.

Standard Errors. The dependent variable in (6) has a correlated error structure because students within a classroom face common class-level shocks and because our analysis dataset contains repeat observations on students in different grades. One natural way to account for these two sources of correlated errors would be to cluster standard errors by both student and classroom (Cameron, Gelbach, and Miller 2011). Unfortunately, two-way clustering of this form requires running regressions on student-level data and thus was computationally infeasible at the Internal Revenue Service. We instead cluster standard errors at the school by cohort level when estimating (8) at the class level, which adjusts for correlated errors across classrooms and repeat student observations within a school. The more conservative approach of clustering by school increases standard errors by $30 \%$ (for earnings), but does not affect our hypothesis tests at conventional levels of statistical significance (Appendix Table 7). ${ }^{20}$

Outliers. In our baseline specifications, we exclude classrooms taught by teachers whose estimated VA $\widehat{m}_{j t}$ falls in the top one percent for their subject and school level (above 2.03 in math and 1.94 in English in elementary school and 1.93 in math and 1.19 in English in middle school). We do so because these teachers' impacts on test scores appear suspiciously consistent with testing irregularities indicative of test manipulation. Jacob and Levitt (2003) develop a proxy for cheating that measures the extent to which a teacher generates very large test score gains that are followed by very large test score losses for the same students in the subsequent grade. Jacob and Levitt show that this proxy for cheating is highly correlated with

[^10]unusual answer sequences that directly reveal test manipulation. Teachers in the top $1 \%$ of our estimated VA distribution are significantly more likely to show suspicious patterns of test score gains followed by steep losses, as defined by Jacob and Levitt's proxy (see Appendix Figure 3). ${ }^{21}$ We therefore trim the top $1 \%$ of outliers in all the specifications reported in the main text. We investigate how trimming at other cutoffs affects our results in Appendix Table 8. The qualitative conclusion that teacher VA has long-term impacts is not sensitive to trimming, but including teachers in the top $1 \%$ reduces our estimates of teachers' impacts on long-term outcomes by $10-30 \%$. In contrast, excluding the bottom $1 \%$ of the VA distribution has little impact on our estimates, consistent with the view that test manipulation to obtain high test score gains is responsible for the results in the upper tail. Directly excluding teachers who have suspect classrooms based on Jacob and Levitt's proxy for cheating yields similar results to trimming on VA itself. Because we trim outliers, our baseline estimates should be interpreted as characterizing the relationship between VA and outcomes below the 99th percentile of VA.

## B. College Attendance

We begin by analyzing the impact of teachers' test-score VA on college attendance at age 20, the age at which college attendance rates are maximized in our sample. Figure 1a plots residual college attendance rates for students in school year $t$ vs. $\widehat{m}_{j t}$, the leave-year-out estimate of their teacher's VA in year $t$. To construct this binned scatter plot, we first residualize college attendance rates with respect to the classlevel control vector $\mathbf{X}_{c t}$ separately within each subject by school-level cell, using within-teacher variation to estimate the coefficients on the controls as described above. We then divide the VA estimates $\widehat{m}_{j t}$ into twenty equal-sized groups (vingtiles) and plot the mean of the college attendance residuals in each bin against the mean of $\widehat{m}_{j t}$ in each bin. Finally, we add back the mean college attendance rate in the estimation sample to facilitate interpretation of the scale. ${ }^{22}$ Note that this binned scatter plot provides a non-parametric representation of the conditional expectation function but does not show the underlying variance in the individual-level data. The regression coefficient and standard error reported in this and all subsequent figures are estimated on the class-level data using (8), with standard errors clustered by school-cohort.

Figure 1a shows that being assigned to a higher VA teacher in a single grade raises a student's probability of attending college significantly. The null hypothesis that teacher VA has no effect on college attendance is rejected with a t-statistic above 11 ( $p<0.001$ ). On average across subjects and grades, a 1 SD increase in a teacher's true test score VA in a single grade increases the probability of college attendance at age 20

[^11]by $\kappa=0.82$ percentage points, relative to a mean college attendance rate of $37.2 \%{ }^{23}$
We evaluate the robustness of this estimate to alternative control vectors in Table 2. Column 1 of Table 2 replicates the specification with the baseline control vector $\mathbf{X}_{c t}$ in Figure 1a as a reference. Column 2 replicates Column 1, adding parent controls $\mathbf{P}_{c t}^{*}$ to the control vector. The parent characteristics $\mathbf{P}_{c t}^{*}$ consist of classroom means of the following variables: mother's age at child's birth, indicators for parent's 401(k) contributions and home ownership, and an indicator for the parent's marital status interacted with a quartic in parent's household income. ${ }^{24}$ The estimate in Columns 2 is quite similar to that in Column 1. Column 3 of Table 2 replicates Column 1, adding class means of twice-lagged test scores $A_{c, t-2}^{*}$ to the control vector instead of parent characteristics. Again, the coefficient does not change appreciably. ${ }^{25}$ Both parent characteristics and twice-lagged test scores are strong predictors of college attendance rates even conditional on the baseline controls $\mathbf{X}_{c t}$, with F-statistics exceeding 300. Hence, the fact that controlling for these variables does not significantly affect the estimates of $\kappa$ supports the identification assumption of selection on observables in (7).

College Quality. We use the same set of specifications to analyze whether high-VA teachers also improve the quality of colleges that their students attend, as measured by the earnings of students who previously attended the same college (see Section II.B). Students who do not attend college are included in this analysis and assigned the mean earnings of individuals who do not attend college. Figure 1 b plots the earnings-based index of quality for college attended at age 20 vs. teacher VA, using the same baseline controls $\mathbf{X}_{c t}$ and technique as in Figure 1a. Again, there is a highly significant relationship between the quality of colleges students attend and the quality of the teachers they had in grades $4-8(t=14.4, p<0.001)$. A 1 SD improvement in teacher VA raises college quality by $\$ 299$ (or 1.11\%) on average, as shown in Column 4 of Table 2. Columns 5 and 6 replicate Column 4 adding parent characteristics and lagged test score gains to the baseline control vector. As with college attendance, the inclusion of these controls has only a modest effect on the point estimates.

The $\$ 299$ estimate in Column 4 combines intensive and extensive margin responses because it includes the effect of increased college attendance rates on projected earnings. Isolating intensive margin responses is more complicated because students who are induced to go to college by a high-VA teacher will tend to attend lower-quality colleges, pulling down mean earnings conditional on attendance. We take two approaches to overcome this selection problem and identify intensive-margin effects. First, we define colleges with

[^12]earnings-based quality above the student-weighted median in our sample ( $\$ 43,914$ ) as "high quality." We regress this high quality college indicator on teacher VA in the full sample, including students who do not attend college, and find that a 1 SD increase in teacher VA raises the probability of attending a high quality college by 0.72 percentage points, relative to a mean of $13.41 \%$ (Column 7 of Table 2). This increase is most consistent with an intensive margin effect, as students would be unlikely to jump from not going to college at all to attending a high quality college. Second, we derive a lower bound on the intensive margin effect by assuming that those who are induced to attend college attend a college of average quality. The mean college quality conditional on attending college is $\$ 41,756$, while the quality for all those who do not attend college is $\$ 17,920$. This suggests that at most $(41,756-17,920) \times 0.82 \%=\$ 195$ of the $\$ 299$ impact is due to the extensive margin response, confirming that teachers improve the quality of colleges that students attend.

Finally, we analyze the impact of teacher quality on the number of years in college. Column 8 replicates the baseline specification in Column 1, replacing the dependent variable with an indicator variable for attending college in at least 4 years between 18 and 22. A 1 SD increase in teacher quality increases the fraction of students who spend 4 or more years in college by 0.79 percentage points ( $3.2 \%$ of the mean). ${ }^{26}$ While we cannot directly measure college completion in our data, this finding suggests that higher quality teachers increase not just attendance but also college completion rates.

Figure 1c plots the impact of a 1 SD improvement in teacher quality on college attendance rates at all ages from 18-28. We run separate regressions of college attendance at each age on teacher VA, using the same specification as in Column 1 of Table 2. As one would expect, teacher VA has the largest impacts on college attendance rates before age 22. However, the impacts remain significant even in the mid 20 's, perhaps because of increased attendance of graduate or professional schools. These continued impacts on higher education affect our analysis of earnings impacts, to which we now turn.

## C. Earnings

The correlation between annual earnings and lifetime income rises rapidly as individuals enter the labor market and begins to stabilize only in the late twenties. We therefore begin by analyzing the impacts of teacher VA on earnings at age 28 , the oldest age at which we have a sufficiently large sample of students to obtain precise estimates. Although individuals' earnings trajectories remain quite steep at age 28, earnings levels at age 28 are highly correlated with earnings at later ages (Haider and Solon 2006), a finding we confirm within the tax data in Appendix Figure 4.

Figure 2a plots individual (W-2) wage earnings at age 28 against VA $\widehat{m}_{j t}$, conditioning on the same set of

[^13]classroom-level controls as above. Being assigned to a higher value-added teacher has a significant impact on earnings, with the null hypothesis of $\kappa=0$ rejected with $p<0.01$. A 1 SD increase in teacher VA in a single grade increases earnings at age 28 by $\$ 350,1.65 \%$ of mean earnings in the regression sample.

Columns 1-3 of Table 3 evaluate the robustness of this estimate to the inclusion of parent characteristics and lagged test score gains. These specifications mirror Columns 1-3 of Table 2, but use earnings at age 28 as the dependent variable. As with college attendance, controlling for these additional observable characteristics has relatively small effects on the point estimates, supporting the identification assumption in (7). The smallest of the three estimates implies that a 1 SD increase in teacher VA raises earnings by 1.34\%.

To interpret the magnitude of this $1.34 \%$ impact, consider the lifetime earnings gain from having a 1 SD higher VA teacher in a single grade. Assume that the percentage gain in earnings remains constant at $1.34 \%$ over the life-cycle and that earnings are discounted at a $3 \%$ real rate (i.e., a $5 \%$ discount rate with $2 \%$ wage growth) back to age 12 , the mean age in our sample. Under these assumptions, the mean present value of lifetime earnings at age 12 in the U.S. population is approximately $\$ 522,000 .{ }^{27}$ Hence, the financial value of having a 1 SD higher VA teacher (i.e., a teacher at the 84 th percentile instead of the median) is $1.34 \% \times \$ 522,000 \simeq \$ 7,000$ per grade. The undiscounted lifetime earnings gain (assuming a $2 \%$ growth rate but $0 \%$ discount rate) is approximately $\$ 39,000$ per student.

A second benchmark is the increase in earnings from an additional year of schooling, which is around 9\% (Gunderson and Oreopoulos 2010, Oreopoulos and Petronijevic 2013). Having a teacher in the first percentile of the value-added distribution (2.33 SD below the mean) is equivalent to missing $\frac{2.33 \times 1.34 \%}{9 \%}=1 / 3$ of the school year when taught by a teacher of average quality.

A third benchmark is the cross-sectional relationship between test scores and earnings. A 1 SD increase in teacher quality raises end-of-year scores by 0.13 SD of the student test score distribution on average across grades and subjects. A 1 SD increase in student test scores, controlling for the student- and class-level characteristics $\mathbf{X}_{i t}$, is associated with a $12 \%$ increase in earnings at age 28 (Appendix Table 3, Column 3, Row 2). The predicted impact of a 1 SD increase in teacher VA on earnings is therefore $0.13 \times 12 \%=$ $1.55 \%$, similar to the observed impact of $1.34 \%$.

Extensive Margin Responses and Other Sources of Income. The increase in wage earnings comes from a combination of extensive and intensive margin responses. In Column 4 of Table 3, we regress an indicator for having positive W-2 wage earnings on teacher VA using the same specification as in Column 1. A 1 SD increase in teacher VA raises the probability of working by $0.38 \%$. If the marginal entrant into the labor market were to take a job that paid the mean earnings level in the sample $(\$ 21,256)$, this extensive margin

[^14]response would raise mean earnings by $\$ 81$. Since the marginal entrant most likely has lower earnings than the mean, this implies that the extensive margin accounts for at most $81 / 350=23 \%$ of the total earnings increase due to better teachers.

Column 5 of Table 3 replicates the baseline specification in Column 1 using total income (as defined in Section II) instead of wage earnings. Reassuringly, the point estimate of teachers' impacts changes relatively little with this broader income definition, which includes self-employment and other sources of income. We therefore use wage earnings - which provides an individual rather than household measure of earnings and is unaffected by the endogeneity of filing - for the remainder of our analysis.

Earnings Trajectories. Next, we analyze how teacher VA affects the trajectory of earnings by examining wage earnings impacts at each age from 20 to 28 . We run separate regressions of wage earnings at each age on teacher VA using the same specification as in Column 1 of Table 3. Figure $2 b$ plots the coefficients from these regressions (which are reported in Appendix Table 9), divided by average earnings at each age to obtain percentage impacts. The impact of teacher quality on earnings rises almost monotonically with age. At early ages, the impact of higher VA is negative and statistically significant, consistent with our finding that higher VA teachers induce their students to go to college. As these students enter the labor force, they have steeper earnings trajectories than students who had lower VA teachers in grades 4-8. Earnings impacts become positive at age 23 , become statistically significant at age 24 , and grow through age 28 , where the earnings impact reaches $1.65 \%$, as in Figure 2a.

An alternative way to state the result in Figure $2 b$ is that better teachers increase the growth rate of students' earnings in their 20s. In Column 6 of Table 3, we verify this result directly by regressing the change in earnings from age 22 to age 28 on teacher VA. As expected, a 1 SD increase in teacher VA increases earnings growth by $\$ 286(2.5 \%)$ over this period. This finding suggests that teachers' impacts on lifetime earnings could be larger than the $1.34 \%$ impact observed at age 28 .

## D. Other Outcomes

In this subsection, we analyze the impacts of teacher VA on other outcomes, starting with our "teenage birth" measure, which is an indicator for filing a tax return and claiming a dependent who was born while the mother was a teenager (see Section II.B). Column 1 of Table 4 analyzes the impact of teacher VA on the fraction of female students who have a teenage birth. Having a 1 SD higher VA teacher in a single year from grades 4 to 8 reduces the probability of a teen birth by 0.61 percentage points, a reduction of roughly $4.6 \%$, as shown in Figure 3a. This impact is similar to the raw cross-sectional correlation between scores and teenage births (Appendix Table 3), echoing our results on earnings and college attendance.

Column 2 of Table 4 analyzes the impact of teacher VA on the socio-economic status of the neighborhood in which students live at age 28 , measured by the percent of college graduates living in that neighborhood.

A 1 SD increase in teacher VA raises neighborhood SES by 0.25 percentage points ( $1.8 \%$ of the mean) by this metric, as shown in Figure 3b. Column 3 of Table 4 shows that a 1 SD increase in teacher VA increases the likelihood of saving money in a $401(\mathrm{k})$ at age 28 by 0.55 percentage points (or $2.8 \%$ of the mean), as shown in Figure 3c.

Fade-Out of Test Score Impacts. The final set of outcomes we consider are teachers' impacts on test scores in subsequent grades. Figure 4 plots the impacts of teacher VA on test scores in subsequent years; see Appendix Table 10 for the underlying coefficients. To construct this figure, we residualize raw test scores $A_{i, t+s}^{*}$ with respect to the class-level controls $\mathbf{X}_{c t}$ using within-teacher variation and then regress the residuals $A_{i, t+s}$ on $\widehat{\mu}_{j t}$. We scale teacher VA in units of student test-score SDs in these regressions - by using $\widehat{\mu}_{j t}$ as the independent variable instead of $\widehat{m}_{j t}=\widehat{\mu}_{j t} / \sigma_{0}-$ to facilitate interpretation of the regression coefficients, which are plotted in Figure 4. The coefficient at $s=0$ is not statistically distinguishable from 1, as shown in our companion paper. Teachers' impacts on test scores fade out rapidly in subsequent years and appear to stabilize at approximately $25 \%$ of the initial impact after 3-4 years. ${ }^{28}$ This result aligns with existing evidence that improvements in education raise contemporaneous scores, then fade out in later scores, only to reemerge in adulthood (Deming 2009, Heckman et al. 2010b, Chetty et al. 2011).

## IV. Research Design 2: Teacher Switching Quasi-Experiments

The estimates in the previous section rely on the assumption that the unobserved determinants of students' long-term outcomes are uncorrelated with teacher quality conditional on observables. In this section, we estimate teachers' long-term impacts using a quasi-experimental design that relaxes and helps validate this identification assumption.

## A. Methodology

Adjacent cohorts of students within a school are frequently exposed to different teachers. We exploit this teacher turnover to obtain a quasi-experimental estimate of teachers' long-term impacts. To understand our research design, consider a school with three 4th grade classrooms. Suppose one of the teachers leaves the school in 1995 and is replaced by a teacher whose VA estimate is 0.3 higher, so that the mean test-score VA of the teaching staff rises by $0.3 / 3=0.1$. If the distribution of unobserved determinants of students' long-term outcomes does not change between 1994 and 1995, the change in mean college attendance rates between the 1994 and 1995 cohorts of students will reveal the impact of a 0.1 improvement in 4th grade teachers' test-score VA. More generally, we can estimate teachers' long-term impacts by comparing the

[^15]change in mean student outcomes across cohorts to the change in mean VA driven by teacher turnover provided that student quality is stable over time.

To formalize this approach, let $\widehat{m}_{j t}^{-\{t, t-1\}}$ denote the test-score VA estimate for teacher $j$ in school year $t$ constructed as in our companion paper using data from all years except $t-1$ and $t$. Similarly, let $\widehat{m}_{j, t-1}^{-\{t, t-1\}}$ denote the VA estimate for teacher $j$ in school year $t-1$ based on data from all years except $t-1$ and $t$. Let $Q_{\text {sgt }}$ denote the student-weighted mean of $\widehat{m}_{j t}^{-\{t, t-1\}}$ across teachers in school $s$ in grade $g$, which is the average estimated quality of teachers in a given school-grade-year cell; define $Q_{s g, t-1}$ analogously. ${ }^{29}$ Let $\Delta Q_{s g t}=Q_{s g t}-Q_{s g, t-1}$ denote the change in mean teacher value-added from year $t-1$ to year $t$ in grade $g$ in school $s$. Define mean changes in student outcome residuals $\Delta Y_{s g t}$ analogously. Note that because we exclude both years $t$ and $t-1$ when estimating VA, the variation in $\Delta Q_{\text {sgt }}$ is driven purely by changes in the teaching staff and not by changes in teachers' VA estimates. ${ }^{30}$ As above, this leave-out technique ensures that changes in $\Delta Y_{s g t}$ are not spuriously correlated with $\Delta Q_{s g t}$ due to estimation error in VA.

We estimate teachers' long-term impacts by regressing changes in mean outcomes across cohorts on changes in mean test-score VA:

$$
\begin{equation*}
\Delta Y_{s g t}=\alpha+\kappa \Delta Q_{s g t}+\Delta \eta_{s g t}^{\prime} \tag{9}
\end{equation*}
$$

Note that this specification is the same as the quasi-experimental specification we used to estimate the degree of bias in VA estimates in our companion paper, except that we use long-term outcomes as the dependent variable instead of test scores. The coefficient in (9) identifies the effect of a 1 SD improvement in teacher quality as defined in (6) under the following assumption.

Assumption 3 [Teacher Switching as a Quasi-Experiment] Changes in teacher quality across cohorts within a school-grade are orthogonal to changes in other determinants of student outcomes $\Delta \eta_{s g t}^{\prime}$ across cohorts:

$$
\begin{equation*}
\operatorname{Cov}\left(\Delta Q_{s g t}, \Delta \eta_{s g t}^{\prime}\right)=0 . \tag{10}
\end{equation*}
$$

This assumption could potentially be violated by endogenous student or teacher sorting. In practice, student sorting at an annual frequency is minimal because of the costs of changing schools. During the period we study, most students would have to move to a different neighborhood to switch schools, which families would be unlikely to do simply because a single teacher leaves or enters a given grade. While endogenous

[^16]teacher sorting is plausible over long horizons, the sharp changes we analyze are likely driven by idiosyncratic shocks such as changes in staffing needs, maternity leaves, or the relocation of spouses. Moreover, in our first paper, we present direct evidence supporting (10) by showing that both prior scores and contemporaneous scores in the other subject (e.g., English) are uncorrelated with changes in mean teacher quality in a given subject (e.g., math). We also present additional evidence supporting (10) below.

If observable characteristics $\mathbf{X}_{i t}$ are also orthogonal to changes in teacher quality across cohorts (i.e., satisfy Assumption 3), we can implement (9) simply by regressing the change in raw outcomes $\Delta Y_{s g t}^{*}$ on $\Delta Q_{s g t}$. We therefore begin with regressions of $\Delta Y_{s g t}^{*}$ on $\Delta Q_{s g t}$ and then confirm that changes in observable characteristics $\mathbf{X}_{i t}$ across cohorts are uncorrelated with $\Delta Q_{s g t}$.

## B. Results

Figure 5a presents a binned scatter plot of changes in mean college attendance rates $\Delta Y_{s g t}^{*}$ against changes in mean teacher value-added $\Delta Q_{\text {sgt }}$ across cohorts. We include year fixed effects (demeaning both the x and $y$ variables by school year), so that the estimate is identified purely from differential changes in teacher value-added across school-grade-subject cells over time. The corresponding regression coefficient, which is based on estimating (9) with year fixed effects but no other controls, is reported in Column 1 of Table 5a.

Changes in the quality of the teaching staff have significant impacts on changes in college attendance rates across consecutive cohorts of students in a school-grade-subject cell. The null hypothesis that $\kappa=0$ is rejected with $p<0.01$. The point estimate implies that a 1 SD improvement in teacher quality raises college attendance rates by 0.86 percentage points, with a standard error of 0.23 . This estimate is very similar to the estimates of 0.71-0.82 percentage points obtained from the first research design in Table 2 . However, the quasi-experimental estimate is much less precise because it exploits less variation.

This analysis identifies teachers' causal impacts provided that (10) holds. One natural concern is that improvements in teacher quality may be correlated with other improvements in a school - such as better resources in other dimensions - that also contribute to students' long-term success and thus lead us to overstate teachers' true impacts. To address this concern, Column 2 of Table 5a replicates the baseline specification in Column 1 including school by year fixed effects instead of just year effects. In this specification, the only source of identifying variation comes from differential changes in teacher quality across subjects and grades within a school in a given year. The coefficient on $\Delta Q_{s g t}$ changes very little relative to the baseline estimate that pools all sources of variation. Column 3 further accounts for secular trends in subject- or grade-specific quality by controlling for the change in mean teacher VA in the prior and subsequent year as well as cubics in the change in prior-year mean own-subject and other-subject scores across cohorts. Controlling for these variables has little impact on the estimate. This result shows that fluctuations in teacher quality relative to trend in specific grades generate significant changes in the affected students' college attendance rates.

In the preceding specifications, we imputed the sample mean of VA (0) for classrooms for which we could not calculate actual VA. This generates downward bias in our estimates because we mismeasure the change in teacher quality $\Delta Q_{s g t}$ across cohorts. Column 4 of Table 5a replicates Column 2, limiting the sample to school-grade-subject-year cells in which we can calculate the leave-two-year-out mean for all teachers in the current and preceding year. As expected, the point estimate of a one SD increase in teacher quality increases, but the confidence interval is significantly wider because the sample size is considerably smaller.

Finally, we further evaluate (10) using a series of placebo tests. In Column 5 on Table 5a, we replicate Column 2, replacing the change in actual college attendance with the change in predicted college attendance based on parent characteristics. We predict college attendance using an OLS regression of $Y_{i t}^{*}$ on the same five parent characteristics $\mathbf{P}_{i t}^{*}$ used in Section III.B, with no other control variables. Changes in mean teacher VA have no effect on predicted college attendance rates, supporting the assumption that changes in the quality of the teaching staff are unrelated to changes in student quality at an annual level.

In Figure 6a, we present an alternative set of placebo tests based on the sharp timing of the change in teacher quality. To construct this figure, we replicate the specification in Column 1 but include changes in mean teacher VA for the four preceding and subsequent cohorts as placebo effects (as well as year fixed effects):

$$
\begin{equation*}
\Delta Y_{s g t}^{*}=\alpha_{t}+\sum_{n=-4}^{4} \kappa_{n} \Delta Q_{s g, t+n}+\varphi_{t} \tag{11}
\end{equation*}
$$

Figure 6 a plots the vector of coefficients $\kappa=\left(\kappa_{-4}, \ldots, \kappa_{0}, \ldots, \kappa_{4}\right)$, which represent the impacts of changes in the quality of teaching staff at different horizons on changes in college attendance rates at time 0 . As one would expect, $\kappa_{0}$ is positive and highly significant while all the other coefficients are near 0 and statistically insignificant. That is, contemporaneous changes in teacher quality have significant effects on college attendance rates, but past or future changes have no impact, as they do not directly affect the current cohort of students. The placebo tests in Figure 6a strongly support the view that the changes in teacher VA have causal effects on college attendance rates. ${ }^{31}$

Figures 5 b and 6 b and Table 5 b replicate the preceding analysis using the earnings-based index of college quality as the outcome. We find that improvements in teachers' test score VA across cohorts lead to sharp changes in the quality of colleges that students attend across all of the specifications. The point estimate in the baseline specification (Column 1) implies that a 1 SD improvement in teacher VA raises college

[^17]quality by $\$ 197$ (s.e. $=\$ 60$ ), which is not statistically distinguishable from the estimates of $\$ 266-\$ 299$ obtained using the first research design. We find no evidence that predicted college quality based on parent characteristics is correlated with changes in teacher quality. In addition, changes in teacher VA again affect college quality in the year of the change rather than in preceding or subsequent years, as shown in Figure 6 b.

We used specifications analogous to those in Table 5 to investigate the impacts of teaching quality on other outcomes, including earnings at age 28. Unfortunately, our sample size for earnings at age 28 is roughly $1 / 7$ th the size of the sample available to study college attendance at age 20 . This is both because we have fewer cohorts of students who are currently old enough to be observed at age 28 in the tax data and because we have data on teacher assignments for much fewer schools in the very early years of our school district data. Because of the considerably smaller sample, we obtain very imprecise and fragile estimates of the impacts of teacher quality on earnings using the quasi-experimental design. ${ }^{32}$ Hence, we are forced to rely on estimates from the cross-class design in Table 3 to gauge earnings impacts. However, given that the cross-class and quasi-experimental designs yield very similar estimates of teachers' impacts on test scores, college attendance, and college quality, we expect the cross-class design to yield unbiased estimates of earnings impacts as well.

## V. Heterogeneity of Teachers' Impacts

In this section, we analyze whether teachers' impacts vary across demographic groups, subjects, and grades. Because analyzing subgroup heterogeneity requires considerable statistical precision, we use the first research design - comparisons across classrooms conditional on observables - which as noted above relies on a stronger identification assumption but is bolstered by generating results that are similar to the quasi-experimental design in the full sample. We estimate impacts on college quality at age 20 (rather than earnings at age 28) to maximize precision and obtain a quantitative metric based on projected earnings gains.

## A. Demographic Groups

In Panel A of Table 6, we study the heterogeneity of teachers' impacts across demographic subgroups. Each value reported in the first row of the table is a coefficient estimate from a separate regression of college quality on teacher VA conditional on controls. To be conservative, we include both student characteristics $\mathbf{X}_{c t}$ and parent characteristics $\mathbf{P}_{c t}^{*}$ in the control vector throughout this section and estimate specifications analogous to Column 5 of Table 2 on various subsamples. Columns 1 and 2 consider heterogeneity by gender. Columns 3 and 4 consider heterogeneity by parental income, dividing students into groups above

[^18]and below the median level of parent income in the sample. Columns 5 and 6 split the sample into minority and non-minority students.

Two lessons emerge from Table 6a. First, the point estimates of the impacts of teacher VA are larger for females than males, although we cannot reject equality of the impacts ( $p=0.102$ ). Second, the impacts are larger for higher-income and non-minority households in absolute terms. For instance, a 1 SD increase in VA raises college quality by $\$ 190$ for children whose parents have below-median income, compared with $\$ 380$ for those whose parents have above-median income. However, the impacts are more similar as a percentage of mean college quality: $0.80 \%$ for low-income students vs. $1.25 \%$ for high-income students.

The larger absolute impact for high socioeconomic students could be driven by two channels: a given increase in teacher VA could have larger impacts on the test scores of high SES students or a given increase in scores could have larger long-term impacts. The second row of coefficient estimates of Table 6a shows that a 1 SD increase in teacher VA raises test scores by approximately 0.13 SD on average in all the subgroups, consistent with the findings of Lockwood and McCaffrey (2009). In contrast, the cross-sectional correlation between scores and college quality is significantly larger for higher SES students (Appendix Table 5). Although not conclusive, these findings suggest that the heterogeneity in teachers' long term impacts is driven by the second mechanism, namely that high SES students benefit more from test score gains. ${ }^{33}$ Overall, the heterogeneity in treatment effects on college quality suggests that teacher quality - at least as measured by test-score VA - is complementary to family inputs and resources. This result implies that higher income families should be willing to pay more for high VA teachers.

## B. Subjects: Math vs. English

Panel B of Table 6 analyzes differences in teachers' impacts across subjects. For these regressions, we split the sample into elementary (Columns 1-3) and middle (Columns 4-5) schools. This distinction is important because students have the same teacher for both subjects in elementary school but not middle school.

In Column 1, we replicate the baseline specification in Column 5 of Table 2, restricting the sample to math classrooms in elementary school. Column 2 repeats this specification for English. In Column 3, we include each teacher's math and English VA together in the same specification, reshaping the dataset to have one row for each student-year (rather than one row per student-subject-year, as in previous regressions). Because a given teacher's math and English VA are highly correlated ( $r=0.6$ ), the magnitude of the two subject-specific coefficients drops by an average of $40 \%$ when included together in a single regression for elementary school. Intuitively, when math VA is included by itself in elementary school, it partly picks up

[^19]the effect of having better teaching in English as well.
We find that a 1 SD increase in teacher VA in English has larger impacts on college quality than a 1 SD improvement in teacher VA in math. This is despite the fact that the variance of teacher effects in terms of test scores is larger in math than English. In Table 2 of our companion paper, we estimated that the standard deviation of teacher effects on student test scores in elementary school is 0.124 in English and 0.163 in math. Using the estimates from Column 3 of Table 6b, this implies that an English teacher who raises her students' test scores by 1 SD raises college quality by $\frac{189 / 0.124}{106 / 0.163}=2.3$ times as much as a math teacher who generates a commensurate test score gain. Hence, the returns to better performance in English are especially large, although it is much harder for teachers to improve students' achievement in English (e.g., Hanushek and Rivkin 2010, Kane et al. 2013).

We find a similar pattern in middle school. In Column 4 of Table 6b, we replicate the baseline specification for the subset of observations in math in middle school. We control for teacher VA in English when estimating this specification by residualizing college quality $Y_{i t}^{*}$ with respect to the student and parent class-level control vectors $\mathbf{X}_{c t}$ and $\mathbf{P}_{i t}^{*}$ as well as $\widehat{m}_{j t}$ in English using a regression with math teacher fixed effects as in (3). Column 5 of Table 6b replicates the same regression for observations in English in middle school, controlling for math teacher VA. A 1 SD improvement in English teacher quality raises college quality by roughly twice as much as a 1 SD improvement in math teacher quality. Even though teachers have much smaller impacts on English test scores than math test scores, the small improvements that good teachers generate in English are associated with substantial long-term impacts.

## C. Impacts of Teachers by Grade

We estimate the impact of a 1 SD improvement in teacher quality in each grade $g \in[4,8]$ on college quality $\left(\kappa_{g}\right)$ by estimating the specification in Column 5 of Table 2 but interacting $\widehat{m}_{j t}$ with grade dummies. Because the school district data system did not cover many middle schools in the early and mid 1990s, we cannot analyze the impacts of teachers in grades 6-8 for more than half the students who are in 4th grade before 1994. To obtain a more balanced sample for comparisons across grades, we restrict attention to cohorts who would have been in 4th grade during or after 1994 in this subsection. ${ }^{34}$

The series in circles in Figure 7 plots the estimates of $\kappa_{g}$, which are also reported in Appendix Table 11. We find that teachers' long-term impacts are large and significant in all grades. Although the estimates in each grade have relatively wide confidence intervals, there is no systematic trend in the impacts. This pattern is consistent with the cross-sectional correlations between test scores and adult outcomes, which are also relatively stable across grades (Appendix Table 6). One issue that complicates cross-grade comparisons

[^20]is that teachers spend almost the entire school day with their students in elementary school (grades 4-5 as well as 6 in some schools), but only their subject period (Math or English) in middle school (grades 7-8). If teachers' skills are correlated across subjects - as is the case with math and English value-added, which have a correlation of 0.6 for elementary school teachers - then a high-VA teacher should have a greater impact on earnings in elementary school than middle school because they spend more time with the student. Hence, the fact that high-VA math and English teachers continue to have substantial impacts in middle school indicates that education has substantial returns well beyond early childhood.

Tracking and Net Impacts. The reduced-form estimates of $\kappa_{g}$ reported above include the impacts of being tracked to a better teacher in subsequent grades, as discussed in Section I. While a parent may be interested in the reduced-form impact of teacher VA in grade $g$, a policy that raises teacher quality in grade $g$ will not allow every child to get a better teacher in grade $g+1$. We now turn to identifying teachers' net impacts $\tilde{\kappa}_{g}$ in each grade, holding fixed future teachers' test-score VA.

Because we have no data after grade 8, we can only estimate teachers' net effects holding fixed teacher quality up to grade 8 . We therefore set $\tilde{\kappa}_{8}=\kappa_{8}$. We recover $\tilde{\kappa}_{g}$ from estimates of $\kappa_{g}$ by subtracting out the impacts of future teachers on earnings iteratively. The net impact of a 7th grade teacher is her reduced-form impact $\kappa_{7}$ minus her indirect impact via tracking to a better 8th grade teacher:

$$
\begin{equation*}
\tilde{\kappa}_{7}=\kappa_{7}-\rho_{78} \tilde{\kappa}_{8}, \tag{12}
\end{equation*}
$$

where $\rho_{78}$ is the extent to which teacher VA in grade 7 increases teacher VA in grade 8 conditional on controls. If we observed each teacher's true VA, we could estimate $\rho_{78}$ using an OLS regression that parallels (8) with the future teacher's true VA as the dependent variable:

$$
\begin{equation*}
m_{j, t_{i}(8)}=\alpha+\rho_{78} \widehat{m}_{j, t_{i}(7)}+\gamma_{1} \mathbf{X}_{c t}+\gamma_{2} \mathbf{P}_{c t}^{*}+\eta_{c t 78}^{\mu} . \tag{13}
\end{equation*}
$$

Since true VA is unobserved, we substitute VA estimates $\widehat{m}_{j, t_{i}(8)}$ for $m_{j, t_{i}(8)}$ on the left hand side of (13). This yields an attenuated estimate of $\rho_{78}$ because $\widehat{m}_{j, t_{i}(8)}$ is shrunk toward 0 to account for estimation error (see Section I.B of our companion paper). If all teachers taught the same number of classes and had the same number of students, the shrinkage factor would not vary across observations. In this case, we could identify $\rho_{78}$ by using $\widehat{m}_{j, t_{i}(8)}$ as the dependent variable in (13) and multiplying the estimate of $\rho_{78}$ by $S D\left(m_{j t}\right) / S D\left(\widehat{m}_{j t}\right)=1 / S D\left(\widehat{m}_{j t}\right)$. In the sample for which we observe college attendance, the standard deviation of teacher VA estimates is $S D\left(\widehat{m}_{j t}\right)=0.61$. We therefore multiply the estimate of $\rho_{78}$ and all the other tracking coefficients $\rho_{g g^{\prime}}$ by $1 / S D\left(\widehat{m}_{j t}\right)=1.63$. This simple approach to correcting for the attenuation bias is an approximation because the shrinkage factor does vary across observations. However, as we discuss below, the magnitude of the tracking coefficients is small and hence further adjusting for the
variation in shrinkage factors is unlikely to affect our conclusions.
We estimate $\rho_{78}$ in three steps. First, we residualize $\widehat{m}_{j, t_{i}(8)}$ with respect to the controls by regressing $\widehat{m}_{j, t_{i}(8)}$ on $\mathbf{X}_{c t}$ and $\mathbf{P}_{c t}^{*}$ with grade 7 teacher fixed effects, as in (3). Second, we run a univariate OLS regression of the residuals on $\widehat{m}_{j, t_{i}(7)}$. Finally, we multiply this coefficient by $1 / S D\left(\widehat{m}_{j t}\right)=1.63$ to obtain an estimate of $\hat{\rho}_{78}$. Using our estimate of $\hat{\rho}_{78}$, we apply (12) to identify $\tilde{\kappa}_{7}$ from the reduced-form estimates of $\kappa_{g}$ in Figure 7. Iterating backwards, we calculate $\kappa_{6}$ by estimating $\hat{\rho}_{68}$ and $\hat{\rho}_{67}$ and so on until we obtain the full set of net impacts. We show formally that this procedure recovers net impacts $\tilde{\kappa}_{g}$ in Appendix C.

The series in triangles in Figure 7 plots the estimates of the net impacts $\tilde{\kappa}_{g}$. The differences between the net impacts and reduced-form impacts are modest: the mean difference between $\kappa_{g}$ and $\tilde{\kappa}_{g}$ is $19.6 \%$ in grades 4-7. This is because the tracking coefficients $\rho_{g, g^{\prime}}$ are small. A 1 SD increase in current teacher quality typically raises future teacher quality by about 0.05 SD or less in elementary school and by about 0.25 SD in middle school (Appendix Table 12). The greater degree of tracking in middle school is consistent with the availability of subject-specific honors classes in grades 7 and 8 .

These results suggest that the vast majority of the reduced-form impacts estimated above reflect a teacher's own direct impact rather than the impacts of being tracked to better teachers in later grades. However, we caution that this approach to calculating teachers' net impacts has three important limitations. First, it assumes that all tracking to future teachers occurs exclusively via teachers' test-score VA. We allow students who have high-VA teachers in grade $g$ to be tracked to higher test-score VA $\left(m_{j t}\right)$ teachers in grade $g+1$, but not to teachers with higher earnings VA $\mu_{j t}^{Y}$. We are forced to make this strong assumption because we have no way to estimate teacher impacts on earnings that are orthogonal to VA, as discussed in Section I. Second, $\tilde{\kappa}_{g}$ does not net out potential changes in other factors besides teachers, such as peer quality or parental inputs. Hence, $\tilde{\kappa}_{g}$ cannot be interpreted as the "structural" impact of teacher quality holding fixed all other inputs in a general model of the education production function (e.g., Todd and Wolpin 2003). Finally, our approach assumes that teacher effects are additive across grades. We cannot identify complementarities in teacher VA across grades because our identification strategy forces us to condition on lagged test scores, which are endogenous to the prior teacher's quality. It would be very useful to relax these assumptions in future work to obtain a better understanding of how the sequence of teachers a child has affects her outcomes in adulthood.

## VI. Policy Analysis

In this section, we use our estimates to predict the potential earnings gains from selecting and retaining teachers on the basis of their VA. We make four assumptions in our calculations. First, we assume that the percentage impact of a 1 SD improvement in teacher VA on earnings observed at age 28 is constant at
$b=1.34 \%$ (Table 3, Column 2) over the lifecycle. ${ }^{35}$ Second, we ignore general equilibrium effects that may reduce wage rates if all children are better educated. Third, we follow Krueger (1999) and discount earnings gains at a $3 \%$ real annual rate (consistent with a $5 \%$ discount rate and $2 \%$ wage growth) back to age 12 , the average age in our sample. Under this assumption, the present value of earnings at age 12 for the average individual in the U.S. population is $\$ 522$, 000 in 2010 dollars, as noted above. Finally, we assume that teacher VA $m_{j t}$ is normally distributed.

To quantify the value of improving teacher quality, we evaluate Hanushek's $(2009,2011)$ proposal to replace teachers whose VA ratings are in the bottom 5 percent of the distribution with teachers of average quality. To simplify exposition, we calculate these impacts for elementary school teachers, who teach one class per day. We first calculate the earnings gains from selecting teachers based on their true test-score VA $m_{j t}$ and then calculate the gains from selecting teachers based on VA estimates $\widehat{m}_{j t}$. Selection on true VA is informative as a benchmark for the potential gains from improving teacher quality, but is not a feasible policy because we only observe estimates of teacher VA in practice. Hence, it is useful to compare the gains from policies that select teachers based on VA estimates using a few years of performance data with the maximum attainable gain if one were to select teachers based on true VA.

Selection on True VA. Elementary school teachers teach both math and English and therefore have two separate VA measures on which they could be evaluated. For simplicity, we assume that teachers are evaluated based purely on their VA in one subject (say math) and VA in the other subject is ignored. ${ }^{36}$ Consider a student whose teacher's true math VA is $\Delta m_{\sigma}$ standard deviations below the mean. Replacing this teacher with a teacher of mean quality (for a single school year) would raise the student's expected earnings by

$$
\begin{equation*}
G=\Delta m_{\sigma} \times \$ 522,000 \times b . \tag{14}
\end{equation*}
$$

Under the assumption that $m_{j t}$ is normally distributed, a teacher in the bottom $5 \%$ of the true VA distribution is on average 2.063 standard deviations below the mean teacher quality. Therefore, replacing a teacher in the bottom $5 \%$ of the VA distribution with an average teacher generates a present value lifetime earnings gain per student of

$$
G=\$ 522,000 \times 2.063 \times 1.34 \%=\$ 14,500 .
$$

For a class of average size (28.2), the total NPV earnings impact from this replacement is $G_{C}=\$ 407,000$.

[^21]The undiscounted cumulative lifetime earnings gains from deselection are 5.5 times larger than these present value gains ( $\$ 80,000$ per student and $\$ 2.25$ million per classroom) , as shown in Appendix Table 13. ${ }^{37}$ These simple calculations show that the potential gains from improving the quality of teaching - whether using selection based on VA, teacher training, or other policies - are quite large. ${ }^{38}$

Selection on Estimated VA. In practice, we can only select teachers on the basis of estimated VA $\widehat{m}_{j t}$. This reduces the gains from selection for two reasons: (1) estimation error in VA and (2) drift in teacher quality over time. To quantify the impact of these realities, suppose we use test score data from years $t=1, \ldots, n$ to estimate teacher VA in school year $n+1$. The gain in year $n+1$ from replacing the bottom $5 \%$ of teachers based on VA estimated using the preceding $n$ years of data is

$$
\begin{equation*}
G(n)=-\mathbb{E}\left[m_{j, n+1} \mid \widehat{m}_{j, n+1}<F_{\widehat{m}_{j, n+1}}^{-1}(0.05)\right] \times \$ 522,000 \times b, \tag{15}
\end{equation*}
$$

where $\mathbb{E}\left[m_{j, n+1} \mid \widehat{m}_{j, n+1}<F_{\widehat{m}_{j, n+1}}^{-1}(0.05)\right]$ denotes the expected value of $m_{j, n+1}$ conditional on the teacher's estimated VA falling below the 5th percentile. We calculate this expected value separately for math and English using Monte Carlo simulations as described in Appendix D. ${ }^{39}$

Figure 8a plots the mean gain per classroom $G_{C}(n)=28.2 \times G(n)$, averaging over math and English, for $n=1, \ldots, 10$. The values underlying this figure are reported in Appendix Table 13. The gain from deselecting teachers based on true VA, $G_{C}=\$ 407,000$, is shown by the horizontal line in the figure. The gains from deselecting teachers based on estimated VA are significantly smaller because of noise in VA estimates and drift in teacher quality. ${ }^{40}$ With one year of data, the expected gain per class is $\$ 226,000,56 \%$ of the gain from selecting on true VA. The gains grow fairly rapidly with more data in the first 3 years, but the marginal value of additional information is small. With three years of test score data, the gain is $\$ 266,000$, but the gain increases to only $\$ 279,000$ after 10 years. After three years, waiting for one more year would increase the gain by $\$ 4,000$ but has an expected cost of $\$ 266,000$. The marginal gains from obtaining one more year of data are outweighed by the expected cost of having a low VA teacher on the staff even after the first year (Staiger and Rockoff 2010). Adding data from prior classes yields relatively little information about current teacher quality both because of decreasing returns to additional observations and

[^22]drift. ${ }^{41}$
Drift in Quality over Subsequent School Years. The values in Figure 8a reflect the gains in the first year after the deselection of teachers, based on $\widehat{m}_{j, n+1}$ in school year $n+1$. Now consider the impacts of such a policy on the earnings of students in a subsequent school year $n+m$ :
$$
G(m, n)=-\mathbb{E}\left[m_{j, n+m} \mid \widehat{m}_{j, n+1}<F_{\widehat{m}_{j, n+1}}^{-1}(0.05)\right] \times \$ 522,000 \times b,
$$
where $\mathbb{E}\left[m_{j, n+m} \mid \widehat{m}_{j, n+1}<F_{\widehat{m}_{j, n+1}}^{-1}(0.05)\right]$ denotes the mean VA of teachers in year $n+m$ conditional on having estimated VA in year $n+1$ below the 5 th percentile.

The lower series in Figure 8 b plots $G_{C}(m, 3)=28.2 \times G(m, 3)$, the gains per class in school year $m$ from deselecting teachers based on their estimated VA for year $4\left(\widehat{m}_{j, 4}\right)$, constructed using the first 3 years of data. The first point in this series coincides with the value of $\$ 266,000$ in Figure 8a reported for $n=3$. Because teacher quality drifts over time, the gains fall in subsequent school years, as some of the teachers who were deselected based on their predicted VA in school year $n$ would have reverted toward the mean in subsequent years. Deselection based on VA estimates at the end of year 3 generates an average gain of $\$ 184,000$ per classroom per year over the subsequent 10 years, the median survival time in the district for teachers who have taught for 3 years.

The upper series in Figure 8b plots the analogous gains when teachers are deselected based on their true VA $m_{j, 4}$ in year 4 instead of their estimated VA $\widehat{m}_{j, 4}$. The first point in this series coincides with the maximum attainable gain of $\$ 407,000$ shown in Figure 8a. The gains again diminish over time because of drift in teacher quality. The average present value gain from deselection based on true VA over the subsequent ten years is approximately $\$ 250,000$ per classroom. This corresponds to an undiscounted lifetime earnings gain per classroom of students of approximately $\$ 1.4$ million.

The reason that estimation error and drift do not heavily erode the gains from deselection of low VA teachers is that very few of the teachers rated in the bottom $5 \%$ turn out to be high-VA teachers. For example, among math teachers in Elementary school, $3.2 \%$ of the teachers whose estimated VA based on 3 years of test score data $\left(\widehat{m}_{j, 4}\right)$ is in the bottom $5 \%$ have true VA $m_{j, 4}$ above the median. Nevertheless, because VA estimates are not perfect predictors of $m_{j t}$, there is still substantial room to use other measures - such as principal evaluations or student surveys - to complement VA estimates and improve predictions of teacher quality. ${ }^{42}$

[^23]Costs of Teacher Selection. The calculations above do not account for the costs associated with a policy that deselects teachers with the lowest performance ratings. First, they ignore downstream costs that may be required to generate earnings gains, most notably the cost associated with higher college attendance rates. Second, and more importantly, they ignore the fact that teachers need to be compensated for the added employment risk they face from such an evaluation system. Rothstein (2013) estimates the latter cost using a structural model of the labor market for teachers. Rothstein estimates that a policy that fires teachers if their estimated VA after 3 years falls below the 5th percentile would require a mean salary increase of $1.4 \%$ to equilibrate the teacher labor market. ${ }^{43}$ In our sample, mean teacher salaries were approximately $\$ 50,000$, implying that annual salaries would have to be raised by approximately $\$ 700$ for all teachers to compensate them for the additional risk. Based on our calculations above, the deselection policy would generate NPV gains of $\$ 184,000$ per teacher deselected, or $\$ 9,250$ for all teachers on average (because only one out of twenty teachers would actually be deselected). Hence, the estimated gains from this policy are more than 10 times larger than the costs. Together with the preceding results, Rothstein's (2013) findings imply that deselecting low VA teachers could be a very cost effective policy if the signal quality of VA does not fall substantially when used for personnel evaluation. ${ }^{44}$

Retention of High VA Teachers. An alternative approach to improving teacher quality that may impose lower costs on teachers is to increase the retention of high-VA teachers by paying them bonuses. Using Monte Carlo simulations analogous to those above, we estimate that retaining a teacher at the 95 th percentile of the estimated VA distribution (using 3 years of data) for an extra year would yield present value earnings gains in the subsequent school year of $\$ 522,000 \times 28.2 \times 1.34 \% \times \mathbb{E}\left[m_{j, n+1} \mid \widehat{m}_{j, n+1}=F_{\widehat{m}_{j, n+1}}^{-1}(0.95)\right]=$ $\$ 212,000$. In our data, roughly $9 \%$ of teachers in their third year do not return to the school district for a fourth year. The attrition rate is unrelated to teacher VA, consistent with the findings of Boyd et al. (2008). Clotfelter et al. (2008) estimate that a $\$ 1,800$ bonus payment in North Carolina reduces attrition rates by $17 \%$. Based on these estimates, a one time bonus payment of $\$ 1,800$ to high-VA teachers who return for a fourth year would increase retention rates in the next year by 1.5 percentage points and generate an average benefit of $\$ 3,180$. The expected benefit of offering a bonus to even an excellent ( 95 th percentile) teacher is only modestly larger than the cost because one must pay bonuses to $(100-9) / 1.5 \approx 60$ additional teachers for every extra teacher retained.

Replacing ineffective teachers is more cost-effective than attempting to retain high VA teachers because most teachers stay for the following school year and are relatively inelastic to salary increases. Of course,

[^24]increasing the salaries of high VA teachers could attract more talented individuals into teaching to begin with or increase teacher effort. The preceding calculations do not account for these effects.

## VII. Conclusion

Our first paper (Chetty, Friedman, and Rockoff 2014) showed that existing test-score value-added measures are a good proxy for a teacher's ability to raise students' test scores. This paper has shown that the same VA measures are also an informative proxy for teachers' long-term impacts. Although these findings are encouraging for the use of value-added metrics, two important issues must be resolved before one can determine how VA should be used for policy.

First, using VA measures to evaluate teachers could induce responses such as teaching to the test or cheating, eroding the signal in VA measures (e.g., Jacob 2005, Neal and Schanzenbach 2010). ${ }^{45}$ One can estimate the magnitude of such effects by replicating the analysis in this paper in a district that evaluates teachers based on their VA. If behavioral responses substantially reduce the signal quality of VA, policy makers may need to develop metrics that are more robust to such responses, as in Barlevy and Neal (2012). For instance, districts may also be able to use data on the persistence of test score gains to identify test manipulation and develop a more robust estimate of teacher quality, as in Jacob and Levitt (2003).

Second, one should compare the long-term impacts of evaluating teachers on the basis of VA to other metrics, such as principal evaluations or classroom observation. One can adapt the methods developed in this paper to evaluate these other measures of teacher quality. When a teacher who is rated highly by principals enters a school, do subsequent cohorts of students have higher college attendance rates and earnings? What fraction of a teacher's long-term impact is captured by test-score VA vs. other measures of teacher quality? By answering these questions, one could ultimately estimate the optimal weighting of available metrics to identify teachers who are most successful in improving students' long-term outcomes.

More generally, there are many aspects of teachers' long-term impacts that remain to be explored and would be helpful in designing education policy. For example, in this paper we only identified the impact of a single teacher on long-term outcomes. Are teachers' impacts additive over time? Do good teachers complement or substitute for each other across years? Similarly, it would be useful to go beyond the mean treatment effects that we have estimated here and determine whether some teachers are especially effective in improving lower-tail outcomes or producing stars.

Whether or not VA is ultimately used as a policy tool, our results show that parents should place great value on having their child in the classroom of a high value-added teacher. Consider a teacher whose true VA is 1 SD above the mean who is contemplating leaving a school. Each child would gain approximately

[^25]$\$ 39,000$ in total (undiscounted) lifetime earnings from having this teacher instead of the median teacher. With an annual discount rate of $5 \%$, the parents of a classroom of average size should be willing to pay this teacher $\$ 200,000$ ( $\$ 7,000$ per parent) to stay and teach their children during the next school year. Hence, the most important lesson of this study is that improving the quality of teaching - whether via the use of value-added metrics or other policy levers - is likely to have substantial economic and social benefits.

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## Online Appendix A: Structural Interpretation of Reduced-Form Parameters

This appendix formalizes how the reduced-form parameters we estimate should be interpreted in a stylized dynamic model of the education production function. The model we outline below follows previous work (e.g., Todd and Wolpin 2003), except that we focus exclusively on the role of teachers, abstracting from other inputs to the education production function, such as peers or parental investment.

## Dynamic Model: Setup

The model is characterized by a specification for scores, a specification for earnings (or other adult outcomes), and a rule that governs student and teacher assignment to classrooms.

Classroom Assignment Rule. School principals assign student $i$ in school year $t$ to a classroom $c=c(i, t)$ based on observed and unobserved determinants of student achievement. Principals then assign a teacher $j$ to each classroom $c$ based on classroom and teacher characteristics. For simplicity, we assume that each teacher teaches one class per year, as in elementary schools.

Test Scores. Let $j=j(c(i, t))$ denote student $i$ 's teacher in school year $t$. Let $\mu_{j t}$ represent teacher $j$ 's "test-score value-added" in year $t .{ }^{46}$ We scale $\mu_{j t}$ in student test-score SDs so that the average teacher has $\mu_{j t}=0$ and the effect of a 1 unit increase in teacher value-added on end-of-year test scores is 1 . Let $t_{i}(g)$ denote the calendar year in which student $i$ reaches grade $g ; t_{i}(0)$ denotes the year in which the student starts school (Kindergarten). As in Section I, student $i$ 's test score in year $t, A_{i t}^{*}$, is

$$
\begin{equation*}
A_{i t}^{*}=\boldsymbol{\beta} \mathbf{X}_{i t}+\mu_{j t}+\varepsilon_{i t} \tag{16}
\end{equation*}
$$

where $\mathbf{X}_{i t}$ denotes observable determinants of student achievement, such as lagged test scores and family characteristics and $\varepsilon_{i t}$ is an idiosyncratic student-level error.

Earnings. Earnings are a function of teacher quality over all years in school, up to grade $G=12$. Let $\tau_{j t}$ represent teacher $j$ 's "direct earnings value-added," i.e. the direct impact of teacher $j$ on earnings holding other factors fixed. We scale $\tau_{j t}$ so that the average teacher has $\tau_{j t}=0$ and the standard deviation of $\tau_{j t}$ is 1 . We assume that a teacher's direct earnings value-added $\tau_{j t}$ is linearly related to her test-score value-added $\mu_{j t}$ :

$$
\tau_{j t}=\phi \mu_{j t}+\tau_{j t}^{\perp}
$$

where $\phi$ measures the relationship between earnings- and test-score VA and $\tau \frac{\perp}{j t}$ represents the portion of a teacher's earnings impact that is orthogonal to her test-score impact.

[^26]For a student in grade $h$, we model earnings $Y_{i}^{*}$ as

$$
\begin{equation*}
Y_{i}^{*}=\beta^{Y} X_{i t}+\sum_{g=h}^{G} \gamma_{g} \tau_{j, t_{i}(g)}+\varepsilon_{i t}^{Y} \tag{17}
\end{equation*}
$$

where $\gamma_{g}$ measures the effect of teacher quality in grade $g$ on earnings. The error term $\varepsilon_{i t}^{Y}$ reflects individual heterogeneity in earnings ability, which may be correlated with academic ability $\varepsilon_{i t}$. The error $\varepsilon_{i t}^{Y}$ may also be correlated with $\mu_{j t}$ and $\tau_{j t}$ because the principal may systematically sort certain types of students to certain teachers. Accounting for such selection is the key challenge in obtaining unbiased estimates of teachers' causal impacts.

In the statistical model in (3), the teacher fixed effect $\alpha_{j}=\sum_{g=h}^{G} \gamma_{g} \tau_{j, t_{i}(g)}$ combines the effects of the current and subsequent teachers. We show how this affects the interpretation of the reduced-form treatment effects we estimate in the next subsection.

## Treatment Effects in the Dynamic Model

We define two notions of a teacher's treatment effect on earnings: total earnings value-added and the impact of test-score VA on earnings.

Total Earnings Value-Added. One natural definition of a teacher's impact on earnings is the effect of changing the teacher of class $c$ in grade $g$ from $j$ to $j^{\prime}$ in year $t$ on expected earnings:

$$
\begin{align*}
& \mu_{j t}^{Y}-\mu_{j^{\prime} t}^{Y}=\mathbb{E} Y_{i t}(j(i, t))-\mathbb{E} Y_{i t}\left(j^{\prime}(i, t)\right)  \tag{18}\\
= & \gamma_{g}\left(\tau_{j t}^{Y}-\tau_{j^{\prime} t}^{Y}\right)+\sum_{s=g+1}^{G} \gamma_{s}\left(\mathbb{E}\left[\tau_{j, t_{i}(s)}^{Y} \mid j(i, t)\right]-\mathbb{E}\left[\tau_{j, t_{i}(s)}^{Y} \mid j^{\prime}(i, t)\right]\right) \tag{19}
\end{align*}
$$

Being assigned teacher $j$ instead of $j^{\prime}$ affects earnings through two channels. The first term in (19) represents the direct impact of the change in teachers on earnings. The second term represents the indirect impact via changes in the expected quality of subsequent teachers to which the student is assigned. For example, a higher achieving student may be tracked into a more advanced sequence of classes taught by higher quality teachers. In a more general model, other determinants of earnings such as parental effort or peer quality might also respond endogenously to the change in teachers. We refer to $\mu_{j t}^{Y}$ as a teacher's "total earnings value-added," or "earnings VA" for short.

In principle, one can estimate teachers' total earnings VA using an approach identical to the one we used to estimate teachers' test-score VA in our first paper. We could predict a teacher's earnings VA $\widehat{\mu}_{j t}^{Y}$ in year $t$ based on mean residual earnings for students in other years with observational data. Such a prediction
would yield unbiased forecasts of teachers' impacts on earnings if

$$
\begin{equation*}
\frac{\operatorname{Cov}\left(\mu_{j t}^{Y}, \widehat{\mu}_{j t}^{Y}\right)}{\operatorname{Var}\left(\widehat{\mu}_{j t}^{Y}\right)}=1 \Rightarrow \frac{\operatorname{Cov}\left(\varepsilon_{i t}^{Y}, \widehat{\mu}_{j t}^{Y}\right)}{\operatorname{Var}\left(\widehat{\mu}_{j t}^{Y}\right)}=0 . \tag{20}
\end{equation*}
$$

This condition requires that unobserved determinants of students' earnings are orthogonal to earnings VA estimates. Although conceptually analogous to the requirement for forecast unbiasedness of test-score VA stated in Assumption 1, (20) turns out not to hold in practice. Tests for sorting on pre-determined characteristics analogous to those in Section IV of our first paper reveal that (20) is violated for earnings VA estimates based on the same control vector (prior test scores and student and classroom demographics) that we used to estimate test score VA. In particular, we find substantial "effects" of earnings VA estimates on parent income and family characteristics, indicating that our baseline control vector is unable to fully account for sorting when estimating earnings VA.

Why are we able to construct unbiased estimates of test score VA but not earnings VA? Controlling for lagged test scores effectively absorbs most unobserved determinants of student achievement on which students are sorted to classrooms, but does not account for unobserved determinants of earnings. To see how this can occur, let $\zeta_{i}$ denote a student's academic ability, which affects both test scores and earnings, and $\zeta_{i}^{Y}$ denote determinants of earnings that are orthogonal to academic achievement, such as family connections. Suppose students are sorted to teachers on the basis of both of these characteristics. The key difference between the two characteristics is that latent student ability $\zeta_{i}$ appears directly in $A_{i, t-1}$, whereas latent student earnings ability $\zeta_{i}^{Y}$ does not directly appear in $A_{i, t-1}$. As a result, variation in academic ability $\zeta_{i}$ can be largely purged from the error term $\widetilde{\varepsilon}_{i t}^{\prime}$ in the specification for test scores in (16) by controlling for $A_{i, t-1} \cdot{ }^{47}$ In contrast, family connections are not reflected in $A_{i, t-1}$ and therefore appear in the error term $\varepsilon_{i t}^{Y}$ in the specification for earnings in (17). Under such a data generating process, we would be able to identify teachers' causal impacts on test scores by controlling for $A_{i, t-1}$, but would not be able to identify teachers' causal impacts on earnings because there is systematic variation across teachers in students' earnings purely due to variation in family connections $\zeta_{i}^{Y}$ even conditional on $A_{i, t-1}$.

Consistent with this reasoning, we showed in our first paper that the key to obtaining forecast unbiased estimates of test-score VA was to control for prior test scores, $A_{i, t-1}$. If we observed an analog of lagged scores such as lagged expected earnings, we could effectively control for $\zeta_{i}^{Y}$ and potentially satisfy (20). Lacking such a control in our data, we cannot identify teachers' total earnings VA and defer this task to future work.

[^27]Impacts of Test-Score VA on Earnings. An alternative objective, which we focus on in our empirical analysis, is to identify the impacts of teachers' test-score based VA $\mu_{j t}$ on earnings. Let $\sigma_{\mu}$ denote the standard deviation of teachers' test-score VA. The reduced-form earnings impact of having a 1 SD better teacher, as measured by test-score VA, in grade $g$ is

$$
\begin{align*}
\kappa_{g}= & \mathbb{E}\left[Y_{i t} \mid \mu_{j^{\prime} t}=\mu_{j t}+\sigma_{\mu}\right]-\mathbb{E}\left[Y_{i t} \mid \mu_{j t}\right]  \tag{21}\\
= & \gamma_{g} \phi \sigma_{\mu}  \tag{22}\\
& +\sum_{s=g+1}^{G} \gamma_{s}\left(\mathbb{E}\left[\tau_{j, t_{i}(s)}^{Y} \mid \mu_{j^{\prime} t}\right]-\mathbb{E}\left[\tau_{j, t_{i}(s)}^{Y} \mid \mu_{j t}\right]\right) . \tag{23}
\end{align*}
$$

The reduced-form impact $\kappa_{g}$ consists of two terms. The first is the direct effect of having a better teacher in grade $g$ in school year $T$, which is attenuated by $\phi=\frac{\operatorname{Cov}\left(\tau_{j t}, \mu_{j t}\right)}{\operatorname{Var}\left(\mu_{j t}\right)}$ because we only pick up the portion of earnings impacts that projects onto test-score VA. The second is the impact of having different teachers in subsequent grades.

Impacts of Multiple Teachers. Let $\tilde{\kappa}_{g}$ denote the impact of teachers' test-score VA in grade $g$ on earnings holding fixed teachers' test-score VA in other grades. An intuitive specification to identify $\tilde{\kappa}_{g}$ is to generalize (5) and regress earnings on teacher VA in all grades simultaneously:

$$
\begin{equation*}
Y_{i}^{*}=\sum_{g=0}^{G}\left[\tilde{\kappa}_{g} \widehat{m}_{j, t_{i}(g)}+\widetilde{\boldsymbol{\beta}}_{g} \mathbf{X}_{i, t_{i}(g)}\right]+\varepsilon_{i}^{m} . \tag{24}
\end{equation*}
$$

Identifying $\left\{\tilde{\kappa}_{g}\right\}$ in (24) requires the orthogonality condition $\operatorname{Cov}\left(\widehat{m}_{j, t_{i}(g)}, \varepsilon_{i}^{m}\right)=0$. This orthogonality condition is violated if we do not include grade $g-1$ test scores $A_{i, g-1}$ in the control vector $X$ because teacher assignment is correlated with lagged test scores and other factors that directly affect earnings, as shown in Appendix Table 2 of our companion paper. But $A_{i, g-1}$ is endogenous to grade $g-1$ teacher VA $\widehat{m}_{j, t_{i}(g-1)}$, implying that we cannot identify $\tilde{\kappa}_{g}$ by directly estimating (24). To address this problem, we instead estimate the degree of teacher tracking and then recover the net impacts $\tilde{\kappa}_{g}$ from our reduced form estimates $\kappa_{g}$ using the iterative method in Section V.C.

Conceptually, estimating the effects of multiple teachers requires simultaneous quasi-random assignment of teachers in multiple grades. Our primary research design, which requires conditioning on lagged test scores, only yields quasi-random variation in teacher assignment one grade at a time. This is why we cannot directly estimate (24) and also cannot identify the substitutability or complementarity of teachers' impacts across grades.

## Online Appendix B: 1098-T Data and College Quality Index

Quality of 1098-T Data. We evaluate whether the 1098-T data capture college enrollment accurately in
three ways. ${ }^{48}$ First, we find that the correlation between enrollment counts for students age 18-21 based on 1098-T's and enrollment counts for colleges listed in the IPEDS dataset from the Department of Education exceeds 0.95 . Second, the aggregate counts of students enrolled in college are aligned with estimates based on the CPS. In 2009, 27.4 million 1098-T forms were issued (Internal Revenue Service, 2010). According to the Current Population Survey (US Census Bureau, 2010, Tables V and VI), in October 2008, there were 22.6 million students in the U.S. ( 13.2 million full time, 5.4 million part-time, and 4 million vocational). As an individual can be a student at some point during the year but not in October and can receive a 1098-T form from more than one institution, the number of 1098 - T forms for the calendar year should indeed be higher than the number of students as of October. Third, two independent evaluations of the Project STAR class size experiment using data from 1098-T's (Chetty et al. 2011) and the National Student Clearinghouse (Dynarski et al. 2013) obtained nearly identical point estimates of the impacts of class size on college attendance.

College Quality Index. Our index of college quality is based on the average earnings of the individuals who attend each college. The construction of such an index requires several choices, including (1) the age at which college attendance is measured, (2) the age at which earnings are measured, (3) the cohort of students used, and (4) the definition of earnings. In what follows, we assess the stability of rankings of colleges with respect to these four choices.

We begin by constructing measures of college quality that vary the four parameters above. In each case, we first identify all individuals who are U.S. citizens as of February 19, 2013 to remove those who were temporarily in the United States for college and for whom we do not have post-college earnings data. ${ }^{49}$ We group individuals by the higher education institution they attended and by age of attendance, as measured on December 31 of each year. ${ }^{50}$ We group individuals not enrolled at a higher education institution at a given age (i.e., those who have no 1098-T form filed on their behalf during the tax year) in a separate "no college" category. For each college (including the "no college" group), we then compute earnings of the students at various ages (in real 2010 dollars). We begin by defining earnings based on individual W-2 wage earnings and then consider broader income measures. We top code individual earnings at $\$ 10$ million to reduce the influence of outliers and we include only those who are alive at the age at which we measure earnings.

We first evaluate the stability of rankings of college quality with respect to the age at which we measure earnings. Appendix Figure 1a plots the percentile ranking of colleges based on earnings measured at age

[^28]23 (one-year after most students graduate from 4 year colleges) and age 27 (five-years post-college) vs. the oldest age at which we can measure earnings of college graduates in our sample, which is 32 (ten-years post-college). We hold the age of college attendance constant at 20 and focus on the cohort of students born in 1979. To construct this figure, we bin colleges into 100 percentiles based on their ranking using age 32 earnings (without any weighting) and compute the mean percentile ranking based on earnings at age 23 and 27 within each bin. Rankings at age 27 are very well aligned with rankings at age 32, but rankings at age 23 are very poorly aligned with measures based on older data. Colleges that have the highest-earning graduates at age 32 are commonly ranked average or even below-average based on data at age 23 .

In Appendix Figure 1b, we extend this analysis to cover all ages from 23-32. This figure plots the rank correlation between college quality measured at age 32 with college quality measured using earnings at earlier ages. Each point shows the correlation of an earnings-based percentile ranking at a given age with the ranking based on earnings at age 32 . The correlation is very low at age 23 and rises steeply at first before asymptoting to 1 . At age 28 and after, the correlations are all above 0.95 , implying that we obtain similar rankings irrespective of what age one uses to measure earnings of college graduates beyond this point. The stability of the index starting in the late 20 's is consistent with evidence from other studies that annual earnings starting in the late 20's are quite highly correlated with lifetime earnings (Haider and Solon 2006).

Panel A of Appendix Table 2 presents the rank correlations to corresponding to Appendix Figure 1b. The rest of Appendix Table 2 studies the rank correlations between college quality measures as we vary the other parameters. In Panel B, we vary the age at which we measure college attendance from 18 to 25, holding fixed the age of earnings measurement at 30 for the cohort born in 1981 (which is the oldest cohort for which we can measure college attendance at age 18). When we measure attendance between 18 and 22, college quality rankings are very highly correlated with each other. The correlations begin to fall when we measure attendance at later ages. This is intuitive, as ages 18-22 correspond to those at which most students would attend a 4-year college if they proceed through school at a normal pace.

Panel C of Appendix Table 2 varies the cohort of students included in the measure, including students born between 1979 and 1981. We hold fixed the ages of college attendance and earnings measurement at 20 and 30 , respectively. The measures are very highly correlated across cohorts, showing that the reliability of our index of college quality is quite high.

Finally, Panel D of Appendix Table 2 shows the relationship between college quality measures based on alternative definitions of earnings. In addition to our baseline measure of mean $\mathrm{W}-2$ earnings, we consider median W-2 earnings and mean total income (W-2 wages plus self-employment income from Form 1040). In each case we hold fixed age in college at 20, age of earnings measurement at 30, and focus on the 1979
cohort. The correlation between these measures exceeds 0.94 , showing that the rankings are not sensitive to the concept of income used to measure earnings. We view W-2 earnings as the preferred measure because it is unaffected by marriage and the endogeneity of filing.

Based on these results, we construct our preferred measure of college quality measuring college attendance at age 20 and mean W-2 earnings at age 31. These choices allow us to combine data from two cohorts - students born in 1979 and 1980 - for whom we measure earnings in 2010 and 2011, respectively. We code college quality as missing for a small number of institutions with fewer than 100 students across the two cohorts and for institutions founded in or after 2001. ${ }^{51}$ If students attended two or more colleges in a given year, we assign them the maximum college quality across all colleges attended.

## Online Appendix C: Identifying Teachers' Net Impacts

This appendix shows that the iterative method described in Section V.C recovers the net impacts of teacher $\mathrm{VA}, \tilde{\kappa}_{g}$, defined as the impact of raising teacher VA in grade $g$ on earnings, holding fixed VA in subsequent grades. The derivation below assumes that true VA is observed; when using VA estimates instead of true VA, one must account for attenuation due to shrinkage, as discussed in the text.

To simplify notation, we omit controls in this derivation; in practice, we residualize all the dependent variables in the regressions below with respect to the standard control vector. Furthermore, we replace the year subscript $t$ with a grade subscript $g$, so that $m_{j g}=m_{j, t_{i}(g)}$.

We begin by estimating the following equations using OLS for $g \in[4,8]$ :

$$
\begin{align*}
Y_{i g} & =\kappa_{g} m_{j g}+\varepsilon_{i g}^{m}  \tag{25}\\
m_{j g^{\prime}} & =\rho_{g g^{\prime}} m_{j g}+\eta_{i g g^{\prime}}^{\rho} \forall g^{\prime}>g \tag{26}
\end{align*}
$$

The first set of equations identifies the reduced-form impact of teacher VA in grade $g$ on earnings. The second set of equations identifies the impact of teacher VA in grade $g$ on teacher VA in future grade $g^{\prime}$. Note that identification of the tracking coefficients $\rho_{g g^{\prime}}$ using (13) requires the following variant of Assumption 2 :

Assumption 2A Teacher value-added in grade $g$ is orthogonal to unobserved determinants of future teacher value-added conditional on controls:

$$
\operatorname{Cov}\left(m_{j g}, \eta_{i g g^{\prime}}^{\rho}\right)=0 .
$$

After estimating $\left\{\kappa_{g}\right\}$ and $\left\{\rho_{g g^{\prime}}\right\}$, we recover the net impacts $\tilde{\kappa}_{g}$ as follows. In the additive model of teacher effects in Appendix A, earnings $Y_{i g}$ for a student in grade $g$ can be written as $\sum_{g^{\prime}=4}^{8} \tilde{\kappa}_{g^{\prime}} m_{j g^{\prime}}+\varepsilon_{i g}^{m}$.

[^29]Substituting this definition of $Y_{i g}$ into (25) and noting that $\rho_{g g^{\prime}}=\operatorname{Cov}\left(m_{j g^{\prime}}, m_{j g}\right) / \operatorname{Var}\left(m_{j g}\right)$ yields

$$
\kappa_{g}=\frac{\operatorname{Cov}\left(\sum_{g^{\prime}=4}^{8} \tilde{\kappa}_{g^{\prime}} m_{j g^{\prime}}+\varepsilon_{i g^{\prime}}^{m}, m_{j g}\right)}{\operatorname{Var}\left(m_{j g}\right)}=\sum_{g^{\prime}=4}^{8} \rho_{g g^{\prime}} \tilde{\kappa}_{g^{\prime}} .
$$

One implication of Assumption 2, the orthogonality condition needed to identify earnings impacts, is that

$$
\operatorname{Cov}\left(m_{j g^{\prime}}, m_{j g}\right)=0 \text { for } g^{\prime}<g
$$

since past teacher quality $m_{j\left(i, g^{\prime}\right)}$ is one component of the error term $\varepsilon_{i g t}^{\mu}$ in (25). Combined with the fact that $\rho_{g g}=1$ by definition, these equations imply that

$$
\begin{aligned}
\kappa_{g} & =\tilde{\kappa}_{g}+\sum_{g^{\prime}=g+1}^{8} \rho_{g g^{\prime}} \tilde{\kappa}_{g^{\prime}} \forall g<8 \\
\kappa_{8} & =\tilde{\kappa}_{8} .
\end{aligned}
$$

Rearranging this triangular set of equations yields the following system of equations, which can be solved by iterating backwards as in Section V.C:

$$
\begin{align*}
& \tilde{\kappa}_{8}=\kappa_{8}  \tag{27}\\
& \tilde{\kappa}_{g}=\kappa_{g}-\sum_{g^{\prime}=g+1}^{8} \rho_{g g^{\prime}} \tilde{\kappa}_{g^{\prime}} \quad \forall g<8 .
\end{align*}
$$

## Online Appendix D: Policy Simulations

Deselection based on Average VA in Math and English. Suppose we deselect the 5\% of elementary school teachers with the lowest mean standardized VA across math and English. Simulating a bivariate normal distribution with a within-year correlation between $\widehat{m}_{j t}$ across math and English of $r=0.6$, we calculate that teachers whose mean VA across subjects is in the bottom $5 \%$ have a standardized VA that is $\Delta m_{\sigma}=1.84$ SD below the mean in both math and English.

To calculate the long-term earnings impact of replacing such teachers, we must identify the impacts of changes in VA in one subject holding fixed VA in the other subject. Given the between-subject VA correlation of $r=0.6$, our earnings impact estimate of $b=1.34 \%$ reflects the effect of a 1 SD improvement in a given subject (e.g. math) combined with a 0.6 SD improvement in the other subject (English). Under the simplifying assumption that earnings impacts do not vary across subjects, the impact of a 1 SD improvement in VA in a given subject is $b_{s}=\frac{b}{1+0.6}=0.84 \%$. Therefore, replacing a teacher with mean VA in the bottom $5 \%$ with an average teacher for one school year in elementary school increases the present value of
a student's earnings by

$$
G^{\prime}=\$ 522,000 \times 2 \times 1.84 \times 0.84 \%=\$ 16,100
$$

and yields total gains of $\$ 454,000$ for an average-sized classroom.

Deselection on Estimated VA: Monte-Carlo Simulations. To calculate the integral in (15), we first construct $\Sigma_{A}$, the VCV matrix of $\vec{A}_{j}^{-t}$, the vector of past class average scores, using the parameters of the autocovariance vector of test scores reported in Columns 1 and 2 of Table 2 of our companion paper. We define the off-diagonal elements of $\Sigma_{A}$ directly based on the autocovariances $\sigma_{A s}$ reported in Table 2 of our first paper, setting the autocovariance $\sigma_{A s}=\sigma_{A 7}$ for $s>7$. We define the diagonal elements of $\Sigma_{A}$ as the variance of mean class test scores, which we compute based on the estimates in Table 2 as (Class + Teacher Level SD $)^{2}+(\text { Individual-Level } S D)^{2} / 28.2$, where 28.2 is the average number of students per class.

We then simulate draws of average class scores from a $N\left(0, \Sigma_{A}\right)$ distribution for one million teachers and calculate $\widehat{m}_{j, n+1}$ based on scores from the first $n$ periods using the same method used to construct the VA estimates in our companion paper. Finally, we calculate the conditional expectation in (15) as the mean test score in year $n+1$ for teachers with $\widehat{m}_{j, n+1}$ in the bottom $5 \%$ of the distribution.

We calculate the gains from deselection based on true VA in Figure 8 b using analogous Monte Carlo simulations, except that we draw scores from the VCV matrix of true VA $\Sigma_{\mu}$ instead of test scores $\Sigma_{A}$. The off-diagonal elements of the two matrices are identical, but the diagonal elements of $\Sigma_{\mu}$ reflect only the variance of teacher quality $\sigma_{\mu}^{2}$. We use the quadratic estimates of $\sigma_{\mu}$ reported in the last row of Table 2 in our companion paper for this simulation.

Note that if one's goal is to maximize expected gains over a teacher's tenure, one should deselect teachers after $n$ years based on mean predicted VA over all future years, discounted by the survival probabilities. We find that this more complex policy increases gains by less than $1 \%$ over 10 years relative to the policy of deselecting teachers based on VA estimates at the end of year 3 that we simulate in Figure 8b. Intuitively, because the VA drift process is close to an $\operatorname{AR}(1)$ process, the relative weights on average scores from a teacher's first three years do not change much when projecting beyond year 4.

The calculations we report in the text assume that VA estimates have zero forecast bias. While the estimates in our first paper do not reject this hypothesis, the upper bound on the $95 \%$ confidence interval for our quasi-experimental estimate of forecast bias is $9 \%$, which would imply $\mathbb{E}\left[m_{j, n+1} \mid \widehat{m}_{j, n+1}\right]=0.91 \widehat{m}_{j, n+1}$. This degree of forecast bias has modest impacts on the gains from deselection: for instance, the earnings gains per class in year 4 based on 3 years of test score data are $G_{C}(3)=\$ 242,000$.

TABLE 1
Summary Statistics for Linked Analysis Dataset

| Variable | Mean <br> $(1)$ | Std. Dev. <br> $(2)$ | Observations <br> $(3)$ |
| :--- | :---: | :---: | :---: |
| Student Data: |  |  |  |
| Class size (not student-weighted) | 28.2 | 5.8 | 240,459 |
| Number of subject-school years per student | 6.25 | 3.18 | $1,083,556$ |
| Test score (SD) | 0.12 | 0.91 | $6,035,726$ |
| Female | $50.4 \%$ |  | $6,762,896$ |
| Age (years) | 11.7 | 1.6 | $6,762,679$ |
| Free lunch eligible (1999-2009) | $77.1 \%$ |  | $3,309,198$ |
| Minority (Black or Hispanic) | $72.1 \%$ |  | $6,756,138$ |
| English language learner | $4.9 \%$ | $6,734,837$ |  |
| Special education | $3.1 \%$ |  | $6,586,925$ |
| Repeating grade | $2.7 \%$ |  | $6,432,281$ |
| Matched to tax data | $89.2 \%$ |  | $6,770,045$ |
| Matched to parents (cond. on match to tax data) | $94.8 \%$ |  | $6,036,422$ |
| Adult Outcomes: |  |  |  |
| Annual wage earnings at age 20 | 5,670 |  |  |
| Annual wage earnings at age 25 | 17,194 | 19,83 | $5,939,022$ |
| Annual wage earnings at age 28 | 20,885 | 24,297 | $2,321,337$ |
| Total income at age 28 | 21,780 | 24,281 | $1,312,800$ |
| In college at age 20 | $35.6 \%$ |  | $1,312,800$ |
| In college at age 25 | $16.5 \%$ |  | $5,939,022$ |
| More than 4 years of college, ages 18-22 | $22.7 \%$ |  | $2,321,337$ |
| College quality at age 20 | 26,408 | 13,461 | $4,514,758$ |
| Contributed to a 401(k) at age 28 | $19.1 \%$ |  | $1,934,570$ |
| Pct. college graduates in ZIP at age 28 | $13.7 \%$ |  | 929,800 |
| Had a child while a teenager (for women) | $14.3 \%$ |  | $3,032,170$ |
| Owned a house at age 25 | $4.3 \%$ |  | $2,321,337$ |
| Married at age 25 | $11.3 \%$ |  | $2,321,337$ |
| Parent Characteristics: |  |  |  |
| Annual Household income | 40,808 | 34,515 | $5,720,657$ |
| Owned a house | $34.8 \%$ |  | $5,720,657$ |
| Contributed to a 401k | $31.3 \%$ |  | $5,720,657$ |
| Married | $42.2 \%$ |  | $5,615,400$ |
| Age at child birth | 28.3 |  |  |
|  |  |  |  |

Notes: All statistics reported are for the linked analysis dataset described in Section II, which includes students from classrooms in which at least one student would graduate high school in or before 2009 if progressing at a normal pace. The sample has one observation per student-subject-school year. Student data are from the administrative records of a large urban school district in the U.S. Adult outcomes and parent characteristics are from 1996-2011 federal income tax data. All monetary values are expressed in real 2010 dollars. All ages refer to the age of an individual as of December 31 within a given year. Test score refers to standardized scale score in math or English. Free lunch is an indicator for receiving free or reduced-price lunches. We link students to their parents by finding the earliest 1040 form from 1996-2011 on which the student is claimed as a dependent. We are unable to link $10.8 \%$ of observations to the tax data; the summary statistics for adult outcomes and parent characteristics exclude these observations. Wage earnings are measured from $\mathrm{W}-2$ forms; we assign 0 's to students with no W-2's. Total income includes both W-2 wage earnings and self-employment income reported on the 1040. College attendance is measured from 1098-T forms. College quality is the average $\mathrm{W}-2$ earnings at age 31 for students who attended a given college at age 20 (see Section II.B for more details). 401(k) contributions are reported on W-2 forms. ZIP code of residence is determined from the address on a 1040 (or W-2 for nonfilers); percent college graduates in ZIP is based on the 2000 Census. We measure teen births for female students as an indicator for claiming a dependent who was born fewer than 20 years after the student herself was born. We measure home ownership from the payment of mortgage interest, reported on either the 1040 or a 1099 form. We measure marriage by the filing of a joint return. Conditional on linking to the tax data, we are unable to link $5.2 \%$ of observations to a parent; the summary statistics for parents exclude these observations. Parent income is average adjusted gross income during the three tax-years between 2005-2007. For parents who do not file, household income is defined as zero. Parent age at child birth is the difference between the age of the mother (or father if single father) and the student. All parent indicator variables are defined in the same way as the equivalent for the students and are equal to 1 if the event occurs in any year between 2005-2007.

TABLE 2
Impacts of Teacher Value-Added on College Attendance

| Dep. Var.: | College at Age 20 <br> (\%) <br> (1) | College at Age 20 <br> (\%) <br> (2) | College at Age 20 <br> (\%) <br> (3) | College <br> Quality at <br> Age 20 <br> (\$) <br> (4) | College Quality at Age 20 <br> (\$) <br> (5) | College Quality at Age 20 <br> (\$) <br> (6) | High <br> Quality College <br> (\%) <br> (7) | 4 or More Years of College, Ages 18-22 <br> (\%) <br> (8) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Teacher VA | $\begin{gathered} 0.82 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.71 \\ (0.06) \end{gathered}$ | $\begin{gathered} 0.74 \\ (0.09) \end{gathered}$ | $\begin{aligned} & 298.63 \\ & (20.74) \end{aligned}$ | $\begin{aligned} & 265.82 \\ & (18.31) \end{aligned}$ | $\begin{aligned} & 266.17 \\ & (26.03) \end{aligned}$ | $\begin{gathered} 0.72 \\ (0.05) \end{gathered}$ | $\begin{gathered} 0.79 \\ (0.08) \end{gathered}$ |
| Mean of Dep. Var. | 37.22 | 37.22 | 37.09 | 26,837 | 26,837 | 26,798 | 13.41 | 24.59 |
| Baseline Controls | X | X | X | X | X | X | X | X |
| Parent Chars. Controls |  | X |  |  | X |  |  |  |
| Lagged Score Controls |  |  | X |  |  | X |  |  |
| Observations | 4,170,905 | 4,170,905 | 3,130,855 | 4,167,571 | 4,167,571 | 3,128,478 | 4,167,571 | 3,030,878 |

Notes: Each column reports coefficients from an OLS regression, with standard errors clustered by school-cohort in parentheses. The regressions are estimated on the linked analysis sample (as described in the notes to Table 1). Teacher value-added is estimated using data from classes taught by a teacher in other years, following the procedure described in Section III.A. The dependent variable in Columns $1-3$ is an indicator for college attendance at age 20. The dependent variable in Columns $4-6$ is the earnings-based index of college quality. See notes to Table 1 and Section II for more details on the construction of these variables. The dependent variable in Column 7 is an indicator for attending a high-quality college, defined as quality greater than the median college quality among those attending college, which is $\$ 43,914$. The dependent variable in Column 8 is an indicator for attending four or more years of college between the ages of 18 and 22. All columns control for the baseline class-level control vector, which includes: class size and class-type indicators; cubics in class and school-grade means of lagged own- and crosssubject scores, interacted with grade level; class and school-year means of student-level characteristics including ethnicity, gender, age, lagged suspensions and absences, and indicators for grade repetition, special education, free or reduced-price lunch, and limited English; and grade and year dummies. Columns 2 and 5 additionally control for class means of parent characteristics, including mother's age at child's birth, indicators for parent's $401(\mathrm{k})$ contributions and home ownership, and an indicator for the parent's marital status interacted with a quartic in parent's household income. Columns 3 and 6 include the baseline controls and class means of twice-lagged test scores. We use within-teacher variation to identify the coefficients on all controls as described in Section I.A; the estimates reported are from regressions of outcome residuals on teacher VA with school by subject level fixed effects.

TABLE 3
Impacts of Teacher Value-Added on Earnings

| Dep. Var.: | Earnings at Age 28 | Earnings at Age 28 | Earnings at Age 28 | Working at Age 28 | Total Income at Age 28 | Wage Growth Ages 22-28 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (\$) | (\$) | (\$) | (\%) | (\$) | (\$) |
|  | (1) | (2) | (3) | (4) | (5) | (6) |
| Teacher VA | 349.84 | 285.55 | 308.98 | 0.38 | 353.83 | 286.20 |
|  | (91.92) | (87.64) | (110.17) | (0.16) | (88.62) | (81.86) |
| Mean of Dep. Var. | 21,256 | 21,256 | 21,468 | 68.09 | 22,108 | 11,454 |
| Baseline Controls | $X$ | X | X | X | X | X |
| Parent Chars. Controls |  | $X$ |  |  |  |  |
| Lagged Score Controls |  |  | $X$ |  |  |  |
| Observations | 650,965 | 650,965 | 510,309 | 650,965 | 650,965 | 650,943 |

Notes: Each column reports coefficients from an OLS regression, with standard errors clustered by school-cohort in parentheses. The regressions are estimated on the linked analysis sample (as described in the notes to Table 1). There is one observation for each student-subject-school year. Teacher value-added is estimated using data from classes taught by a teacher in other years, following the procedure described in Section III.A. The dependent variable in Columns 1-3 is the individual's wage earnings reported on $\mathrm{W}-2$ forms at age 28. The dependent variable in Column 4 is an indicator for having positive wage earnings at age 28. The dependent variable in Column 5 is total income (wage earnings plus self-employment income). The dependent variable in Column 6 is wage growth between ages 22 and 28 . All columns control for the baseline class-level control vector; Column 2 additionally controls for parent characteristics, while Column 3 additionally controls for twice-lagged test scores (see notes to Table 2 for details). We use within-teacher variation to identify the coefficients on all controls as described in Section I.A; the estimates reported are from regressions of outcome residuals on teacher VA with school by subject level fixed effects.

TABLE 4
Impacts of Teacher Value-Added on Other Outcomes

|  |  | Percent College <br> Grad in ZIP at <br> Age 28 | Have 401(k) at <br> Age 28 |
| :--- | :---: | :---: | :---: |
|  | $(\%)$ | $(\%)$ | $(\%)$ |
|  | $(1)$ | $(2)$ | $(3)$ |
| Teacher VA | -0.61 | 0.25 | 0.55 |
| Mean of Dep. Var. | 13.24 | $(0.04)$ | $(0.16)$ |
| Baseline Controls | $X$ | 13.81 | 19.81 |
| Observations | $2,110,402$ | 468,021 | 650,965 |

Notes: Each column reports coefficients from an OLS regression, with standard errors clustered by school-cohort in parentheses. The regressions are estimated on the linked analysis sample (as described in the notes to Table 1). There is one observation for each student-subject-school year. Teacher value-added is estimated using data from classes taught by a teacher in other years, following the procedure described in Section III.A. The dependent variables in Column 1-3 are an indicator for having a teenage birth, the fraction of residents in an individual's zip code of residence at age 28 with a college degree or higher, and an indicator for whether an individual made a contribution to a 401 (k) plan at age 28 (see notes to Table 1 and Section II for more details). Column 1 includes only female students. All regressions include the baseline class-level control vector (see notes to Table 2 for details). We use within-teacher variation to identify the coefficients on all controls as described in Section I.A; the estimates reported are from regressions of outcome residuals on teacher VA with school by subject level fixed effects.

TABLE 5
Impacts of Teacher Value-Added on College Outcomes: Quasi-Experimental Estimates

| Panel A: College Attendance at Age 20 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dep. Var.: | College Attendance (\%) |  |  |  | Pred. Coll. Attendance |
|  | (1) | (2) | (3) | (4) | (5) |
| Teacher VA | $\begin{gathered} 0.86 \\ (0.23) \end{gathered}$ | $\begin{gathered} 0.73 \\ (0.25) \end{gathered}$ | $\begin{gathered} 0.67 \\ (0.26) \end{gathered}$ | $\begin{gathered} 1.20 \\ (0.58) \end{gathered}$ | $\begin{gathered} 0.02 \\ (0.06) \end{gathered}$ |
| Year FE | X |  |  |  |  |
| School x Year FE |  | X | $X$ | X | X |
| Lagged Score Controls |  |  | $X$ |  |  |
| Lead and Lag Changes in Teacher VA |  |  | X |  |  |
| Number of School $\times$ Grade x Subject $\times$ Year Cells | 33,167 | 33,167 | 26,857 | 8,711 | 33,167 |
| Sample: | Full Sample | Full Sample | Full Sample | No Imputed Scores | Full Sample |
| Panel B: College Quality at Age 20 |  |  |  |  |  |
| Dep. Var.: | College Quality (\$) |  |  |  | Pred. Coll. Quality (\$) |
|  | (1) | (2) | (3) | (4) | (5) |
| Teacher VA | $\begin{aligned} & 197.64 \\ & (60.27) \end{aligned}$ | $\begin{aligned} & 156.64 \\ & (63.93) \end{aligned}$ | $\begin{aligned} & 176.51 \\ & (64.94) \end{aligned}$ | $\begin{gathered} 334.52 \\ (166.85) \end{gathered}$ | $\begin{gathered} 2.53 \\ (18.30) \end{gathered}$ |
| Year FE | X |  |  |  |  |
| School x Year FE |  | X | X | X | X |
| Lagged Score Controls |  |  | X |  |  |
| Lead and Lag Changes in Teacher VA |  |  | X |  |  |
| Number of School $x$ Grade x Subject $\times$ Year Cells | 33,167 | 33,167 | 26,857 | 8,711 | 33,167 |
| Sample: | Full Sample | Full Sample | Full Sample | No Imputed Scores | Full Sample |

Notes: Each column reports coefficients from an OLS regression, with standard errors clustered by school-cohort in parentheses. The regressions are estimated on the linked analysis sample (as described in the notes to Table 1), collapsed to school-grade-year-subject means. The independent variable for each regression is the difference in mean teacher value-added between adjacent school-grade-year-subject cells, where we estimate teacher value-added using data that omits both years (see Section IV.A for more details). Similarly, dependent variables are defined as changes in means across consecutive cohorts at the school-grade-year-subject level. In Panel A, the dependent variable is college attendance at age 20; in Panel B, the dependent variable is the earnings-based index of college quality (see Table 1 for details). In Column 1 we regress the mean change in the dependent variable on the mean change in teacher value-added, controlling only for year fixed-effects. Column 2 replicates Column 1 including school-year fixed effects. In Column 3, we add a cubic in the change in mean lagged scores to the specification in Column 2, as well as controls for the lead and lag change in mean teacher value-added. In Column 4, we restrict the sample to cells with no imputed VA; other columns impute the sample mean of 0 for classes with missing VA. Column 5 replicates Column 2, except that the dependent variable is the predicted value from an individual-level regression of the original dependent variable on the vector of parent characteristics defined in the notes to Table 2.

TABLE 6
Heterogeneity in Impacts of Teacher Value-Added

| Panel A: Impacts by Demographic Group |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Female <br> (1) | Male <br> (2) | Low Income (3) | High Income <br> (4) | Minority <br> (5) | Non-Minority (6) |
| Dep. Var.: | College Quality at Age 20 (\$) |  |  |  |  |  |
| Teacher VA | $\begin{aligned} & 290.65 \\ & (23.61) \end{aligned}$ | $\begin{aligned} & 237.93 \\ & (21.94) \end{aligned}$ | $\begin{aligned} & 190.24 \\ & (19.63) \end{aligned}$ | $\begin{aligned} & 379.89 \\ & (27.03) \end{aligned}$ | $\begin{aligned} & 215.51 \\ & (17.09) \end{aligned}$ | $\begin{aligned} & 441.08 \\ & (42.26) \end{aligned}$ |
| Mean of Dep. Var. Impact as \% of Mean | $\begin{gathered} 27,584 \\ 1.05 \% \end{gathered}$ | $\begin{gathered} 26,073 \\ 0.91 \% \end{gathered}$ | $\begin{gathered} 23,790 \\ 0.80 \% \end{gathered}$ | $\begin{gathered} 30,330 \\ 1.25 \% \end{gathered}$ | $\begin{gathered} 23,831 \\ 0.90 \% \end{gathered}$ | $\begin{gathered} 33,968 \\ 1.30 \% \end{gathered}$ |
| Dep. Var.: | Test Score (SD) |  |  |  |  |  |
| Teacher VA | $\begin{gathered} 0.135 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.136 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.128 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.129 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.136 \\ (0.001) \end{gathered}$ | $\begin{gathered} 0.138 \\ (0.001) \end{gathered}$ |
| Mean of Dep. Var. | 0.196 | 0.158 | -0.003 | 0.331 | -0.039 | 0.651 |
| Panel B: Impacts by Subject |  |  |  |  |  |  |
|  |  |  | Elementary Sc |  | Midd | School |
|  |  | (1) | (2) | (3) | (4) | (5) |
| Dep. Var.: | College Quality at Age 20 (\$) |  |  |  |  |  |
| Math Teacher VA |  | $\begin{aligned} & 207.81 \\ & (21.77) \end{aligned}$ |  | $\begin{aligned} & 106.34 \\ & (28.50) \end{aligned}$ | $\begin{aligned} & 265.59 \\ & (43.03) \end{aligned}$ |  |
| English Teacher VA |  |  | $\begin{aligned} & 258.16 \\ & (25.42) \end{aligned}$ | $\begin{aligned} & 189.24 \\ & (33.07) \end{aligned}$ |  | $\begin{aligned} & 521.61 \\ & (63.67) \end{aligned}$ |
| Control for Average VA in Other Subject |  |  |  |  | X | X |

Notes: In the first row of estimates in Panel A, we replicate the specification in Column 5 of Table 2 within various population subgroups. In Columns 1 and 2, we split the sample between males and females; in Columns 3 and 4, we split the sample based on the median parent household income (which is $\$ 31,905$ ); in Columns 5 and 6 , we split the sample based on whether a student belongs to an ethnic minority (black or hispanic). In the second row of estimates in Panel A, we replicate all of the regressions from the first row replacing college quality with score as the dependent variable. In Panel B, we split the sample into elementary schools (where the student is taught by the same teacher for both math and English) and middle schools (which have different teachers for each subject). Columns 1 and 2 replicate the specification in Column 5 of Table 2, splitting the sample by subject. In Column 3, we regress college quality on measures of math teacher value-added and English teacher value-added together in a dataset reshaped to have one row per student by school year. We restrict the sample so that the number of teacher-year observations is identical in Columns 1-3. Columns 4 and 5 replicate Column 5 of Table 2 for middle schools with an additional control for the average teacher value-added in the other subject for students in a given class.

APPENDIX TABLE 1
Structure of Linked Analysis Dataset

|  |  |  |  |  |  | Matched <br> to Tax |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Student | Subject | Year | Grade | Class | Teacher | Test Score | Earnings <br> at Age 28 |  |
|  |  |  |  |  |  |  |  |  |
| Bob | Math | 1992 | 4 | 1 | Jones | 0.5 | 1 | $\$ 35 \mathrm{~K}$ |
| Bob | English | 1992 | 4 | 1 | Jones | -0.3 | 1 | $\$ 35 \mathrm{~K}$ |
| Bob | Math | 1993 | 5 | 2 | Smith | 0.9 | 1 | $\$ 35 \mathrm{~K}$ |
| Bob | English | 1993 | 5 | 2 | Smith | 0.1 | 1 | $\$ 35 \mathrm{~K}$ |
| Bob | Math | 1994 | 6 | 3 | Harris | 1.5 | 1 | $\$ 35 \mathrm{~K}$ |
| Bob | English | 1994 | 6 | 4 | Adams | 0.5 | 1 | $\$ 35 \mathrm{~K}$ |
| Nancy | Math | 2002 | 3 | 5 | Daniels | 0.4 | 0 | . |
| Nancy | English | 2002 | 3 | 5 | Daniels | 0.2 | 0 | . |
| Nancy | Math | 2003 | 4 | 6 | Jones | -0.1 | 0 | . |
| Nancy | English | 2003 | 4 | 6 | Jones | 0.1 | 0 | . |
|  |  |  |  |  |  |  |  |  |

Notes: This table illustrates the structure of the linked analysis sample which combines information from the school district database and the tax data. There is one row for each student-subject-school year. Individuals who were not linked to the tax data have missing data on adult outcomes and parent characteristics. The values in this table are not real data and are for illustrative purposes only.

APPENDIX TABLE 2
Correlation of College Rankings Based on Alternative Measures

| Panel A: Correlation of College Rankings Across Ages at Which Earnings are Measured |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Age 23 | Age 24 | Age 25 | Age 26 | Age 27 | Age 28 | Age 29 | Age 30 | Age 31 | Age 32 |
| Age 23 | 1.000 |  |  |  |  |  |  |  |  |  |
| Age 24 | 0.858 | 1.000 |  |  |  |  |  |  |  |  |
| Age 25 | 0.747 | 0.949 | 1.000 |  |  |  |  |  |  |  |
| Age 26 | 0.676 | 0.901 | 0.967 | 1.000 |  |  |  |  |  |  |
| Age 27 | 0.614 | 0.852 | 0.928 | 0.972 | 1.000 |  |  |  |  |  |
| Age 28 | 0.577 | 0.822 | 0.900 | 0.950 | 0.979 | 1.000 |  |  |  |  |
| Age 29 | 0.553 | 0.802 | 0.882 | 0.934 | 0.962 | 0.983 | 1.000 |  |  |  |
| Age 30 | 0.519 | 0.774 | 0.860 | 0.916 | 0.948 | 0.968 | 0.980 | 1.000 |  |  |
| Age 31 | 0.505 | 0.761 | 0.848 | 0.905 | 0.937 | 0.958 | 0.971 | 0.986 | 1.000 |  |
| Age 32 | 0.495 | 0.750 | 0.838 | 0.897 | 0.930 | 0.952 | 0.964 | 0.977 | 0.987 | 1.000 |
| Panel B: Correlation of College Rankings Across Ages at Which College Attendance is Measured |  |  |  |  |  |  |  |  |  |  |
|  |  |  | Age 18 | Age 19 | Age 20 | Age 21 | Age 22 | Age 23 | Age 24 | Age 25 |
| Age 18 |  |  | 1.000 |  |  |  |  |  |  |  |
| Age 19 |  |  | 0.948 | 1.000 |  |  |  |  |  |  |
| Age 20 |  |  | 0.930 | 0.975 | 1.000 |  |  |  |  |  |
| Age 21 |  |  | 0.909 | 0.947 | 0.972 | 1.000 |  |  |  |  |
| Age 22 |  |  | 0.880 | 0.914 | 0.940 | 0.968 | 1.000 |  |  |  |
| Age 23 |  |  | 0.850 | 0.886 | 0.909 | 0.933 | 0.960 | 1.000 |  |  |
| Age 24 |  |  | 0.803 | 0.830 | 0.851 | 0.873 | 0.893 | 0.932 | 1.000 |  |
| Age 25 |  |  | 0.766 | 0.790 | 0.806 | 0.830 | 0.851 | 0.883 | 0.935 | 1.000 |
| Panel C: Correlation of College Rankings Across Birth Cohorts |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | Coho | t 1979 | Coho | t 1980 | Cohort | 1981 |
| Cohort 1 |  |  |  |  |  | 00 |  |  |  |  |
| Cohort 1 |  |  |  |  |  | 931 |  | 000 |  |  |
| Cohort 1 |  |  |  |  |  | 933 |  | 42 |  |  |
| Panel D: Correlation of College Rankings Across Earnings Definitions |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | Mean W-2 |  | Median W-2 |  | Mean W-2 + S-E |  |
| Mean W-2 Earnings |  |  |  |  | 1.000 |  | 1.000 |  |  |  |
| Median W-2 Earnings |  |  |  |  | 0.960 |  |  |  | 1.000 |  |
| Mean W-2 + Self-Employment Income |  |  |  |  | 0.989 |  | 0.943 |  |  |  |

Notes: This table displays Spearman rank correlations between alternative earnings-based indices of college quality, each of which is defined by four characteristics: age of earnings measurement, age of college attendance, cohort of students, and definition of earnings. Throughout this table, we construct college quality measures from only a single birth cohort of students; however, the preferred measure used in the text combines two cohorts. Panel A varies the age of earnings measurement from 23 to 32 , holding fixed the age of college attendance at 20, using only the 1979 cohort of students, and using mean W-2 wage earnings. Panel B varies the age of college attendance from 18 to 25 , holding fixed the age of earnings measurement at 30 , using only the 1981 cohort, and using mean W-2 wage earnings. Panel $C$ varies the birth cohort of students, holding fixed the age of college attendance at 20 , the age of earnings measurement at 30 , and using mean W -2 wage earnings. Panel D varies the measure of earnings between the baseline (mean W-2 wage earnings by college) and two alternatives (median W-2 wage earnings by college and mean total income by college), holding fixed the age of college attendance at 20 , the age of earnings measurement at 30, and using only the 1979 cohort of students.

| Dep. Var.: | $\begin{gathered} \text { College at Age } \\ 20 \end{gathered}$ | College Quality at Age 20 | Earnings at Age 28 | Teenage Birth | Percent College Grads in ZIP at Age 28 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (\%) | (\$) | (\$) | (\%) | (\%) |
|  | (1) | (2) | (3) | (4) | (5) |
| No Controls | $\begin{aligned} & 18.37 \\ & (0.02) \end{aligned}$ | $\begin{gathered} 6,366 \\ (6) \end{gathered}$ | $\begin{gathered} 7,709 \\ (23) \end{gathered}$ | $\begin{aligned} & -6.57 \\ & (0.02) \end{aligned}$ | $\begin{gathered} 1.87 \\ (0.01) \end{gathered}$ |
| With Controls | $\begin{gathered} 5.54 \\ (0.04) \end{gathered}$ | $\begin{gathered} 2,114 \\ (11) \end{gathered}$ | $\begin{gathered} 2,585 \\ (59) \end{gathered}$ | $\begin{aligned} & -1.58 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 0.34 \\ (0.01) \end{gathered}$ |
| Math | 6.04 | 2,295 | 2,998 | -1.21 | 0.31 |
| Full Controls | (0.06) | (16) | (83) | (0.07) | (0.02) |
| English | 5.01 | 1,907 | 2,192 | -2.01 | 0.37 |
| Full Controls | (0.06) | (16) | (88) | (0.06) | (0.02) |
| Mean of Dep. Var. | 37.71 | 26,963 | 21,622 | 13.25 | 13.43 |

Notes: Each cell reports coefficients from a separate OLS regression of an outcome in adulthood on test scores measured in standard deviation units, with standard errors reported in parentheses. The regressions are estimated on observations from the linked analysis sample (as described in the notes to Table 1). There is one observation for each student-subject-school year, and we pool all subjects and grades in estimating these regressions. The dependent variable is an indicator for attending college at age 20 in column 1, our earnings-based index of college quality in column 2 , wage earnings at age 28 in column 3 , an indicator for having a teenage birth (defined for females only) in column 4, and the fraction of residents in an individual's zip code of residence with a college degree or higher at age 28 in column 5 . See notes to Table 1 for definitions of these variables. The regressions in the first row include no controls. The regressions in the second row include the full vector of studentand class-level controls used to estimate the baseline value-added model described in Section III.A, as well as teacher fixed effects. The regressions in the third and fourth row both include the full vector of controls and split the sample into math and English test score observations. The final row displays of the mean of the dependent variable in the sample for which we have the full control vector (i.e., the sample used in the 2nd row).

APPENDIX TABLE 4
Cross-Sectional Correlations Between Test Scores and Earnings by Age

|  | Dependent Variable: Earnings (\$) |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Age: | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
|  | $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ | $(6)$ | $(7)$ | $(8)$ | $(9)$ |
| No Controls | 889 | 1,098 | 1,864 | 3,592 | 4,705 | 5,624 | 6,522 | 7,162 | 7,768 |
|  | $(20)$ | $(25)$ | $(28)$ | $(34)$ | $(39)$ | $(44)$ | $(48)$ | $(51)$ | $(54)$ |
| With Controls | 392 | 503 | 726 | 1,372 | 1,759 | 1,971 | 2,183 | 2,497 | 2,784 |
|  | $(64)$ | $(79)$ | $(91)$ | $(110)$ | $(125)$ | $(139)$ | $(152)$ | $(161)$ | $(171)$ |
| Mean Earnings | 6,484 | 8,046 | 9,559 | 11,777 | 14,004 | 16,141 | 18,229 | 19,834 | 21,320 |
| Pct. Effect | $6.1 \%$ | $6.2 \%$ | $7.6 \%$ | $11.6 \%$ | $12.6 \%$ | $12.2 \%$ | $12.0 \%$ | $12.6 \%$ | $13.1 \%$ |
| (with controls) |  |  |  |  |  |  |  |  |  |

Notes: Each cell in the first two rows reports coefficients from a separate OLS regression of earnings at a given age on test scores measured in standard deviation units, with standard errors in parentheses. See notes to Table 1 for our definition of earnings. We restrict this table to students born in cohorts 1979 and 1980, so that regressions are estimated on a constant subsample of the linked analysis sample. There is one observation for each student-subject-school year, and we pool all subjects and grades in estimating these regressions. The first row includes no controls; the second includes the full vector of student- and class-level controls used to estimate the baseline value-added model described in Section III.A as well as teacher fixed effects. Means of earnings for the estimation sample with controls are shown in the third row. The last row divides the coefficient estimates from the specification with controls by the mean earnings to obtain a percentage impact by age.

APPENDIX TABLE 5
Heterogeneity in Cross-Sectional Correlations Across Demographic Groups

| Dependent Variable: | Earnings at Age 28 | College at at Age 20 | College Quality Age 20 | Teenage Birth |
| :---: | :---: | :---: | :---: | :---: |
|  | (\$) | (\%) | (\$) | (\%) |
|  | (1) | (2) | (3) | (4) |
| Male | $\begin{gathered} 2,408 \\ (88) \\ {[22,179]} \end{gathered}$ | $\begin{gathered} 5.36 \\ (0.06) \\ {[34.24]} \end{gathered}$ | $\begin{gathered} 1,976 \\ (16) \\ {[26,205]} \end{gathered}$ | n/a |
| Female | $\begin{gathered} 2,735 \\ (80) \\ {[21,078]} \end{gathered}$ | 5.74 <br> (0.06) <br> [41.07] | $\begin{gathered} 2,262 \\ (17) \\ {[27,695]} \end{gathered}$ | $\begin{gathered} -1.58 \\ (0.05) \\ {[13.25]} \end{gathered}$ |
| Non-minority | $\begin{gathered} 2,492 \\ (139) \\ {[31,587]} \end{gathered}$ | 5.11 <br> (0.08) <br> [59.67] |  | $\begin{aligned} & -0.72 \\ & (0.04) \\ & {[2.82]} \end{aligned}$ |
| Minority | $\begin{gathered} 2,622 \\ (62) \\ {[17,644]} \end{gathered}$ | $\begin{gathered} 5.65 \\ (0.05) \\ {[28.98]} \end{gathered}$ | $\begin{gathered} 1,734 \\ (12) \\ {[23,917]} \end{gathered}$ | $\begin{gathered} -1.96 \\ (0.06) \\ {[17.20]} \end{gathered}$ |
| Low Parent Inc. | $\begin{gathered} 2,674 \\ (85) \\ {[18,521]} \end{gathered}$ | 5.14 <br> (0.06) <br> [26.91] | $\begin{gathered} 1,653 \\ (15) \\ {[23,824]} \end{gathered}$ | $\begin{gathered} -1.72 \\ (0.07) \\ {[16.67]} \end{gathered}$ |
| High Parent Inc. | $\begin{gathered} 2,573 \\ (92) \\ {[26,402]} \end{gathered}$ | $\begin{gathered} 5.73 \\ (0.06) \\ {[49.92]} \end{gathered}$ | $\begin{gathered} 2,539 \\ (18) \\ {[30,420]} \end{gathered}$ | $\begin{aligned} & -1.29 \\ & (0.06) \\ & {[9.21]} \end{aligned}$ |

Notes: Each column reports coefficients from an OLS regression, with standard errors in parentheses and the mean of the dependent variable in the estimation sample in brackets. These regressions replicate the second row (full sample, with controls and teacher fixed effects) of estimates in Columns 1-4 of Appendix Table 3, splitting the sample based on student demographic characteristics. The demographic groups are defined in exactly the same way as in Panel A of Table 6. We split rows 1 and 2 by the student's gender. We split the sample in rows 3 and 4 based on whether a student belongs to an ethnic minority (black or hispanic). We split the sample in rows 5 and 6 based on whether a student's parental income is higher or lower than median in the sample, which is $\$ 31,905$.

## APPENDIX TABLE 6

Cross-Sectional Correlations between Test Scores and Outcomes in Adulthood by Grade

| Dep. Variable: | Earnings at Age 28 | College at Age 20 | College Quality at Age 20 | Earnings at Age 28 | College at Age 20 | College Quality at Age 20 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | No Controls |  |  | With Controls |  |  |
|  | (\$) (1) | (\%) <br> (2) | (\$) (3) | (\$) (4) | (\%) <br> (5) | (\$) <br> (6) |
| Grade 4 | $\begin{gathered} 7,561 \\ (57) \end{gathered}$ | $\begin{aligned} & 18.29 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 6,378 \\ (13) \end{gathered}$ | $\begin{aligned} & 2,970 \\ & (122) \end{aligned}$ | $\begin{gathered} 6.78 \\ (0.09) \end{gathered}$ | $\begin{gathered} 2,542 \\ (23) \end{gathered}$ |
| Grade 5 | $\begin{gathered} 7,747 \\ (50) \end{gathered}$ | $\begin{aligned} & 18.27 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 6,408 \\ (13) \end{gathered}$ | $\begin{aligned} & 2,711 \\ & (108) \end{aligned}$ | $\begin{gathered} 5.28 \\ (0.08) \end{gathered}$ | $\begin{gathered} 2,049 \\ (23) \end{gathered}$ |
| Grade 6 | $\begin{gathered} 7,524 \\ (51) \end{gathered}$ | $\begin{aligned} & 17.95 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 6,225 \\ (14) \end{gathered}$ | $\begin{aligned} & 2,395 \\ & (140) \end{aligned}$ | $\begin{gathered} 4.92 \\ (0.10) \end{gathered}$ | $\begin{gathered} 1,899 \\ (27) \end{gathered}$ |
| Grade 7 | $\begin{gathered} 7,891 \\ (54) \end{gathered}$ | $\begin{aligned} & 18.23 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 6,197 \\ (14) \end{gathered}$ | $\begin{aligned} & 2,429 \\ & (198) \end{aligned}$ | $\begin{gathered} 4.48 \\ (0.11) \end{gathered}$ | $\begin{gathered} 1,689 \\ (29) \end{gathered}$ |
| Grade 8 | $\begin{gathered} 7,795 \\ (48) \end{gathered}$ | $\begin{aligned} & 19.10 \\ & (0.05) \end{aligned}$ | $\begin{gathered} 6,596 \\ (13) \end{gathered}$ | $\begin{aligned} & 2,113 \\ & (141) \end{aligned}$ | $\begin{gathered} 5.43 \\ (0.11) \end{gathered}$ | $\begin{gathered} 2,106 \\ (28) \end{gathered}$ |

Notes: Each column reports coefficients from an OLS regression, with standard errors in parentheses. The regressions in the first three columns replicate the first row (full sample, no controls) of estimates in Columns 1-3 of Appendix Table 3, splitting the sample by grade. The regressions in the second set of three columns replicate the second row (full sample, with controls and teacher fixed effects) of estimates in Columns 1-3 of Appendix Table 3, again splitting the sample by grade.

## APPENDIX TABLE 7

Robustness of Baseline Results to Student-Level Controls, Clustering, and Missing Data

| Dep. Var.: | College at Age 20 <br> (\%) <br> (1) | College Quality at Age 20 <br> (\$) <br> (2) | Earnings at Age 28 <br> (\$) <br> (3) |
| :---: | :---: | :---: | :---: |
| Panel A: Individual Controls |  |  |  |
| Teacher VA, with baseline controls | $\begin{gathered} 0.825 \\ (0.072) \end{gathered}$ | $\begin{aligned} & 299 \\ & (21) \end{aligned}$ | $\begin{aligned} & 350 \\ & (92) \end{aligned}$ |
| Observations | 4,170,905 | 4,167,571 | 650,965 |
| Teacher VA, with additional individual controls | $\begin{gathered} 0.873 \\ (0.072) \end{gathered}$ | $\begin{aligned} & 312 \\ & (21) \end{aligned}$ | $\begin{aligned} & 357 \\ & (90) \end{aligned}$ |
| Observations | 4,170,905 | 4,167,571 | 650,965 |
| Panel B: Clustering |  |  |  |
| Teacher VA, school clustered | $\begin{gathered} 0.825 \\ (0.115) \end{gathered}$ | $\begin{aligned} & 299 \\ & (36) \end{aligned}$ | $\begin{gathered} 350 \\ (118) \end{gathered}$ |
| Observations | 4,170,905 | 4,167,571 | 650,965 |
| Panel C: Missing Data |  |  |  |
| Teacher VA, cells > 95\% VA coverage | $\begin{gathered} 0.819 \\ (0.090) \end{gathered}$ | $\begin{aligned} & 277 \\ & (26) \end{aligned}$ | $\begin{gathered} 455 \\ (202) \end{gathered}$ |
| Observations | 2,238,143 | 2,236,354 | 363,392 |
| Teacher VA, cells > median match rate | $\begin{gathered} 0.912 \\ (0.094) \end{gathered}$ | $\begin{aligned} & 345 \\ & (28) \end{aligned}$ | $\begin{gathered} 563 \\ (203) \end{gathered}$ |
| Observations | 2,764,738 | 2,762,388 | 278,119 |

Notes: The table presents robustness checks of the main results in Tables 2 and 3. In Panel A, the first row replicates Columns 1 and 4 of Table 2 and Column 1 of Table 3 as a reference. The second row adds individual controls, so that the control vector exactly matches that used to estimate the value-added model (see Section III.A for details). Panel B clusters standard errors by school. In Panel C, the first row limits the sample to those school-grade-year-subject cells in which we are able to calculate teacher value-added for at least $95 \%$ of students. The second row limits the sample to those school-grade-year-subject cells in which the rate at which we are able to match observations to the tax data is more than the school-level-subject-specific median across cells.

|  | Percent Trimmed in Upper Tail |  |  |  |  |  | Bottom and Top 1\% <br> (7) | Jacob and Levitt Proxy <br> (8) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 5\% <br> (1) | $4 \%$ <br> (2) | $3 \%$ <br> (3) | $2 \%$ <br> (4) | 1\% <br> (5) | 0\% <br> (6) |  |  |
| Test Score | $\begin{gathered} 0.972 \\ (0.006) \end{gathered}$ | $\begin{gathered} 0.975 \\ (0.006) \end{gathered}$ | $\begin{gathered} 0.981 \\ (0.006) \end{gathered}$ | $\begin{gathered} 0.987 \\ (0.006) \end{gathered}$ | $\begin{gathered} 0.993 \\ (0.006) \end{gathered}$ | $\begin{gathered} 1.005 \\ (0.006) \end{gathered}$ | $\begin{aligned} & 0.996 \\ & 0.006 \end{aligned}$ | $\begin{gathered} 0.918 \\ (0.006) \end{gathered}$ |
| College at Age 20 | $\begin{gathered} 0.93 \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.90 \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.88 \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.86 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.82 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.72 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.79 \\ (0.07) \end{gathered}$ | $\begin{gathered} 1.10 \\ (0.09) \end{gathered}$ |
| College Quality at Age 20 | $\begin{aligned} & 329 \\ & (23) \end{aligned}$ | $\begin{aligned} & 320 \\ & (22) \end{aligned}$ | $\begin{aligned} & 315 \\ & (22) \end{aligned}$ | $\begin{aligned} & 307 \\ & (21) \end{aligned}$ | $\begin{aligned} & 299 \\ & (21) \end{aligned}$ | $\begin{aligned} & 276 \\ & (21) \end{aligned}$ | $\begin{aligned} & 292 \\ & (21) \end{aligned}$ | $\begin{aligned} & 371 \\ & (25) \end{aligned}$ |
| Earnings at Age 28 | $\begin{gathered} 404 \\ (102) \end{gathered}$ | $\begin{gathered} 405 \\ (100) \end{gathered}$ | $\begin{aligned} & 390 \\ & (99) \end{aligned}$ | $\begin{aligned} & 356 \\ & (96) \end{aligned}$ | $\begin{aligned} & 350 \\ & (92) \end{aligned}$ | $\begin{aligned} & 248 \\ & (91) \end{aligned}$ | $\begin{aligned} & 337 \\ & (94) \end{aligned}$ | $\begin{gathered} 391 \\ (118) \end{gathered}$ |

Notes: This table presents results that use alternative approaches to trimming the tails of the distribution of teacher VA. Each coefficient reports the coefficient on teacher VA from a separate OLS regression, with standard errors clustered by school-cohort in parentheses. The regressions in the first row replicate the baseline specification used in Column 1 of Table 3 in our companion paper (using VA scaled in units of student test-score SDs), except that we include only the class-level controls that correspond to the baseline set of controls in this paper (as in Section III.A). The regressions in rows 2-4 replicate the baseline specification used in Columns 1 and 4 of Table 2 and Column 1 of Table 3. Columns 1-6 report results for trimming the upper tail at various cutoffs. Column 7 shows estimates when both the bottom and top $1 \%$ of VA outliers are excluded. Finally, Column 8 excludes teachers who have more than one classroom that is an outlier according to Jacob and Levitt's (2003) proxy for cheating. Jacob and Levitt define an outlier classroom as one that ranks in the top $5 \%$ of a test-score change metric defined in the notes to Appendix Figure 3. The results in Column 5 ( $1 \%$ trimming) correspond to those reported in the main text.

APPENDIX TABLE 9
Impacts of Teacher Value-Added on Outcomes by Age

|  | Panel A: College Attendance |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: <br> Age: | College Attendance (\%) |  |  |  |  |  |  |  |  |  |  |
|  | $18$ <br> (1) | $19$ <br> (2) | 20 <br> (3) | $21$ <br> (4) | $22$ <br> (5) | 23 <br> (6) | $24$ <br> (7) | 25 <br> (8) | 26 <br> (9) | $\begin{gathered} 27 \\ (10) \end{gathered}$ | $\begin{gathered} 28 \\ (11) \end{gathered}$ |
| Teacher Value-Added | $\begin{gathered} 0.61 \\ (0.06) \end{gathered}$ | $\begin{gathered} 0.81 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.82 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.98 \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.71 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.44 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.58 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.46 \\ (0.08) \end{gathered}$ | $\begin{gathered} 0.50 \\ (0.07) \end{gathered}$ | $\begin{gathered} 0.46 \\ (0.09) \end{gathered}$ | $\begin{aligned} & -0.01 \\ & (0.11) \end{aligned}$ |
| Mean Attendance Rate | 29.4 | 36.8 | 37.2 | 35.7 | 32.2 | 24.4 | 20.31 | 17.3 | 15.7 | 13.9 | 12.3 |
| Panel B: Wage Earnings |  |  |  |  |  |  |  |  |  |  |  |
| Dependent Variable: <br> Age: | Earnings (\$) |  |  |  |  |  |  |  |  |  |  |
|  |  |  | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
|  |  |  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) |
| Teacher Value-Added |  |  | $\begin{gathered} -32 \\ (11) \end{gathered}$ | $\begin{aligned} & -35 \\ & (14) \end{aligned}$ | $\begin{aligned} & -18 \\ & (18) \end{aligned}$ | $\begin{gathered} 44 \\ (25) \end{gathered}$ | $\begin{gathered} 74 \\ (32) \end{gathered}$ | $\begin{aligned} & 141 \\ & (44) \end{aligned}$ | $\begin{aligned} & 230 \\ & (47) \end{aligned}$ | $\begin{aligned} & 254 \\ & \text { (63) } \end{aligned}$ | $\begin{aligned} & 350 \\ & \text { (92) } \end{aligned}$ |
| Mean Earnings |  |  | 5,696 | 7,293 | 9,473 | 12,582 | 15,080 | 17,547 | 18,833 | 20,229 | 21,256 |

Notes: These results present the regression estimates underlying the results in Panel C of Figure 1 (in Panel A) and Panel B of Figure 2 (in Panel B). The regressions in Panel A match the specification from Column 1 of Table 2, with college attendance measured at different ages; those in Panel B match the specification from Column 1 of Table 3.

APPENDIX TABLE 10
Impacts of Teacher Value-Added on Current and Future Test Scores

| Dep. Var.: |  | Test Score (SD) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | t | $\mathrm{t}+1$ | $\mathrm{t}+2$ | $\mathrm{t}+3$ | $\mathrm{t}+4$ |
|  | $(1)$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
|  |  |  |  |  |  |
| Teacher VA | 0.993 | 0.533 | 0.362 | 0.255 | 0.221 |
|  | $(0.006)$ | $(0.007)$ | $(0.007)$ | $(0.008)$ | $(0.012)$ |
| Observations | $7,401,362$ | $5,603,761$ | $4,097,344$ | $2,753,449$ | $1,341,266$ |
|  |  |  |  |  |  |

Notes: This table presents the regression estimates plotted in Figure 4; see notes to that figure for details.

APPENDIX TABLE 11
Impacts of Value-Added on College Quality by Grade

| College Quality at Age 20 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Panel A: Reduced-Form Coefficients |  |  |  |  |  |
|  | Grade 4 | Grade 5 | Grade 6 | Grade 7 | Grade 8 |
| Teacher Value-Added | $\begin{aligned} & 226 \\ & (31) \end{aligned}$ | $\begin{aligned} & 289 \\ & (33) \end{aligned}$ | $\begin{aligned} & 292 \\ & (48) \end{aligned}$ | $\begin{aligned} & 482 \\ & (61) \end{aligned}$ | $\begin{aligned} & 198 \\ & (48) \end{aligned}$ |
| Panel B: Coefficients Net of Teacher Tracking |  |  |  |  |  |
|  | Grade 4 | Grade 5 | Grade 6 | Grade 7 | Grade 8 |
| Teacher Value-Added | 194 | 270 | 173 | 402 | 198 |

Notes: This table presents the regression estimates plotted in Figure 7; see notes to that figure for details.

APPENDIX TABLE 12
Tracking: Impact of Current Teacher VA on Future Teachers' VA

|  | Future Teacher Value-Added |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Grade 5 | Grade 6 | Grade 7 | Grade 8 |
| Grade 4 Teacher VA | 0.028 | 0.057 | 0.024 | 0.027 |
|  | $(0.007)$ | $(0.006)$ | $(0.004)$ | $(0.005)$ |
| Grade 5 Teacher VA |  | 0.059 | 0.014 | 0.019 |
|  | $(0.006)$ | $(0.005)$ | $(0.014)$ |  |
| Grade 6 Teacher VA |  |  | 0.198 | 0.196 |
|  |  |  | $(0.012)$ | $(0.014)$ |
| Grade 7 Teacher VA |  |  | 0.405 |  |
|  |  |  | $(0.017)$ |  |

Notes: Each cell reports the coefficient from a separate regression of teacher valueadded in a subsequent grade on teacher value-added in the current grade, with standard errors at the school-cohort level. As in Figure 7, we first residualize each dependent variable (i.e. lead VA, two-year lead VA, etc.) with respect to the classroom-level baseline control vector (see notes to Table 2 for more details). We then regress residualized future VA on current VA interacted with grade. We multiply the resulting regression coefficients by 1.63 to account for the attenuation bias due to using VA estimates instead of true VA as the dependent variable (see text for details). All regressions are estimated using observations in the linked analysis sample for which the student is progressing through grades at normal pace (e.g., the student is in sixth grade two years after fourth grade).

APPENDIX TABLE 13
Earnings Impacts of Replacing Teachers Below 5th Percentile with Average Teachers

| Years Used to Estimate VA | Panel A: Impacts in First Year After Deselection |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Selection on Estimated VA |  | Selection on True VA |  |
|  | Present Value of Earnings Gain per Class | Undiscounted Sum of Earnings Gain per Class | Present Value of Earnings Gain per Class | Undiscounted Sum of Earnings Gain per Class |
| 1 | \$225,843 | \$1,249,636 | \$406,988 | \$2,251,954 |
| 2 | \$256,651 | \$1,420,105 |  |  |
| 3 | \$265,514 | \$1,469,147 |  |  |
| 4 | \$269,297 | \$1,490,081 |  |  |
| 5 | \$272,567 | \$1,508,174 |  |  |
| 6 | \$274,143 | \$1,516,891 |  |  |
| 7 | \$275,232 | \$1,522,918 |  |  |
| 8 | \$276,665 | \$1,530,845 |  |  |
| 9 | \$278,112 | \$1,538,851 |  |  |
| 10 | \$279,406 | \$1,546,013 |  |  |
|  | Panel B: Impacts in Subsequent School Years |  |  |  |
|  | Selection on Estimated VA in Yr. 4 |  | Selection on True VA in Yr. 4 |  |
| School Years Since Teacher was Hired | Present Value of Earnings Gain per Class | Undiscounted Sum of Earnings Gain per Class | Present Value of Earnings Gain per Class | Undiscounted Sum of Earnings Gain per Class |
| 4 | \$265,514 | \$1,469,147 | \$406,988 | \$2,251,954 |
| 5 | \$229,923 | \$1,272,213 | \$339,870 | \$1,880,574 |
| 6 | \$202,631 | \$1,121,202 | \$297,569 | \$1,646,511 |
| 7 | \$183,538 | \$1,015,557 | \$252,422 | \$1,396,703 |
| 8 | \$172,867 | \$956,509 | \$222,339 | \$1,230,251 |
| 9 | \$161,575 | \$894,032 | \$212,185 | \$1,174,067 |
| 10 | \$157,812 | \$873,209 | \$193,255 | \$1,069,324 |
| 11 | \$155,349 | \$859,581 | \$180,876 | \$1,000,824 |
| 12 | \$156,582 | \$866,400 | \$180,909 | \$1,001,007 |
| 13 | \$156,547 | \$866,206 | \$181,027 | \$1,001,662 |
| Avg. Gain | \$184,234 | \$1,019,405 | \$246,744 | \$1,365,288 |

Notes: In Panel A, we present the earnings impacts per classroom of a policy that deselects the bottom $5 \%$ of teachers after $N$ years and replaces them with a teacher of median quality, where we vary $N$ from 1 to 10. We calculate these values using the methods described in Section VI. The first column presents estimates of the NPV earnings gains of deselection based on teacher value-added that is estimated from $N$ years of observing a single average-sized ( 28.2 students) classroom per year of student scores. The third column shows the theoretical gain from deselecting teachers based on current true value-added; this value does not vary across years. Panel B presents the per class impacts of deselecting teachers (after 3 years of observation) in subsequent school years. Column 1 reports the present value of earnings gains in the ten years (i.e., years 4-13) after deselecting teachers based on their VA estimate in year 4, constructed using the past three years of data. The first number in Column 1 of Panel B matches the 3rd number in Column 1 of Panel A. Column 3 presents analogous values, instead deselecting teachers based on true value-added in year 4, so that the gains in the year 4 match the gains reported in Column 3 of Panel A. Columns 2 and 4 in each panel replicate Columns 1 and 3, presenting the undiscounted sum of future earnings impacts instead of present values. The bottom row in the table reports the unweighted means of the estimates from years 4-13 in Panel B for each column; these are the values reported in the introduction of the paper.

## FIGURE 1

## Effects of Teacher Value-Added on College Outcomes


b) College Quality at Age 20

c) Impact of Teacher Value-Added on College Attendance by Age


Notes: These figures are drawn using the linked analysis sample, pooling all grades and subjects, with one observation per student-subject-school year. Panels A and B are binned scatter plots of college attendance rates and college quality vs. normalized teacher VA $\hat{m}_{j t}$. These plots correspond to the regressions in Columns 1 and 4 of Table 2 and use the same sample restrictions and variable definitions. To construct these binned scatter plots, we first residualize the y-axis variable with respect to the baseline class-level control vector (defined in the notes to Table 2) separately within each subject by school-level cell, using within-teacher variation to estimate the coefficients on the controls as described in Section I.A. We then divide the VA estimates $\hat{m}_{j t}$ into twenty equal-sized groups (vingtiles) and plot the means of the y-variable residuals within each bin against the mean value of $\hat{m}_{j t}$ within each bin. Finally, we add back the unconditional mean of the $y$ variable in the estimation sample to facilitate interpretation of the scale. The solid line shows the best linear fit estimated on the underlying micro data using OLS. The coefficients show the estimated slope of the best-fit line, with standard errors clustered at the school-cohort level reported in parentheses. In Panel C, we replicate the regression in Column 1 of Table 2 (depicted in Panel A), varying the age of college attendance from 18 to 28 , and plot the resulting coefficients. The dashed lines show the boundaries of the $95 \%$ confidence intervals for the effect of value-added on college attendance at each age, with standard errors clustered by school-cohort. The coefficients and standard errors from the regressions underlying Panel C are reported in Appendix Table 9.

## FIGURE 2

## Effect of Teacher Value-Added on Earnings



Notes: Panel A is a binned scatter plot of earnings at age 28 vs. normalized teacher VA $\hat{m}_{j t}$. This plot corresponds to the regression in Column 1 of Table 3 and uses the same sample restrictions and variable definitions. See notes to Figure 1 for details on the construction of binned scatter plots. In Panel B, we replicate the regression in Column 1 of Table 3 (depicted in Panel A), varying the age at which earnings are measured from 20 to 28 . We then plot the resulting coefficients expressed as a percentage of mean wage earnings in the regression sample at each age. The dashed lines show the boundaries of the $95 \%$ confidence intervals for the effect of value-added on earnings at each age, with standard errors clustered by school-cohort. The coefficients and standard errors from the regressions underlying Panel B are reported in Appendix Table 9.

FIGURE 3

## Effects of Teacher Value-Added on Other Outcomes in Adulthood



Notes: These three figures are binned scatter plots corresponding to Columns 1-3 of Table 4 and use the same sample restrictions and variable definitions. See notes to Figure 1 for details on the construction of these binned scatter plots.

FIGURE 4

## Effects of Teacher Value-Added on Future Test Scores



Notes: This figure shows the effect of current teacher VA on test scores at the end of the current and subsequent school years. To construct this figure, we regress end-of-grade test scores in year $t+s$ on teacher VA $\hat{\mu}_{j t}$ in year $t$, varying $s$ from 0 to 4 . As in our companion paper, we scale teacher VA in units of student test-score SD's and include all students in the school district data in these regressions, without restricting to the older cohorts that we use to study outcomes in adulthood. We control for the baseline class-level control vector (defined in the notes to Table 2), using within-teacher variation to identify the coefficients on controls as described in Section I.A. The dashed lines depict $95 \%$ confidence intervals on each regression coefficient, with standard errors clustered by school-cohort. The coefficients and standard errors from the underlying regressions are reported in Appendix Table 10.

## FIGURE 5

## Effects of Changes in Teaching Staff Across Cohorts on College Outcomes

a) Change in College Attendance Across Cohorts vs. Change in Mean Teacher VA

b) Change in College Quality Across Cohorts vs. Change in Mean Teacher VA


Notes: These two figures plot changes in mean college attendance rates (measured in percentage points) and college quality across adjacent cohorts within a school-grade-subject cell against changes in mean teacher VA across those cohorts. These plots correspond to the regressions in Column 1 of Tables 5A and Table 5B and use the same sample restrictions and variable definitions. To construct these binned scatter plots, we first demean both the $x$ - and $y$-axis variables by school year to eliminate any secular time trends. We then divide the observations into twenty equal-size groups (vingtiles) based on their change in mean VA and plot the means of the y variable within each bin against the mean change in VA within each bin, weighting by the number of students in each school-grade-subject-year cell. Finally, we add back the unconditional (weighted) mean of the x and y variables in the estimation sample.

## FIGURE 6

## Timing of Changes in Teacher Quality and College Outcomes

a) Effects of Changes in Mean Teacher VA on College Attendance

b) Effects of Changes in Mean Teacher VA on College Quality


Notes: These figures evaluate whether the timing of changes in teacher quality across cohorts aligns with the timing of changes in college outcomes. The point at 0 represents the "treatment effect" of changes in teacher quality on changes in college outcomes for a given group of students; the other points are "placebo tests" that show the impacts of changes in teacher quality for previous and subsequent cohorts on the same set of students. To construct Panel A, we regress the change in mean college attendance between adjacent cohorts within a school-grade-subject cell on the change in mean teacher quality across those cohorts as well as four lags and four leads of the change in mean teacher quality within the same school-grade-subject. The regression also includes year fixed effects. Panel A plots the coefficients from this regression. We report the point estimate and standard error on the own-year change in mean teacher quality (corresponding to the value at 0 ). We also report p-values from hypothesis tests for the equality of the own-year coefficient and the one-year lead or one-year lag coefficients. These standard errors and p-values account for clustering at the school-cohort level. Panel B replicates Panel A, replacing the dependent variable with changes in mean college quality across adjacent cohorts.

## FIGURE 7

Impacts of Teacher Value-Added on College Quality by Grade


Notes: This figure plots the impact of a 1 SD increase in teacher VA in each grade from 4-8 on our earnings-based index of college quality (defined in the notes to Table 1). The upper (circle) series shows the reduced-form effect of improved teacher quality in each grade, including both the direct impact of the teacher on earnings and the indirect effect through improved teacher quality in future years. To generate this series, we replicate Column 5 of Table 2, interacting VA with grade dummies. We restrict the sample to cohorts who would have been in 4th grade during or after 1994 to obtain a balanced sample across grades. The dots in the series plot the coefficients on each grade interaction. The dashed lines show the boundaries of the $95 \%$ confidence intervals for the reduced-form effects, clustering the standard errors by school-cohort. The lower (triangle) series plots the impact of teachers in each grade on college quality netting out the impacts of increased future teacher quality. We net out the effects of future teachers using the tracking coefficients reported in Appendix Table 12 and solving the system of equations in Section V.C. Appendix Table 11 reports the reduced-form effects and net-of-future-teachers effects plotted in this figure.

## FIGURE 8

## Earnings Impacts of Deselecting Low Value-Added Teachers



Notes: This figure analyzes the impacts of replacing teachers with VA in the bottom $5 \%$ with teachers of average quality on the present value of lifetime earnings for a single classroom of average size ( 28.2 students). In Panel A, the horizontal line shows the hypothetical gain from deselecting the bottom $5 \%$ of teachers based on their true VA in the current school year. The series in circles plots the gains from deselecting teachers on estimated VA vs. the number of years of prior test score data used to estimate VA. Panel A shows gains for the school year immediately after deselection; Panel B shows the gains in subsequent school years, which decay over time due to drift in teacher quality. The lower series in Panel B (in circles) plots the earnings gains in subsequent school years from deselecting teachers based on their VA estimate at $t=4$, constructed using the past three years of data. The first point in this series (at $t=4$ ) corresponds to the third point in Panel A by construction. The upper series (in triangles) shows the hypothetical gains obtained from deselecting the bottom $5 \%$ of teachers based on their true VA at $t=4$; the first dot in this series matches the value in the horizontal line in Panel A. For both series in Panel $B$, we also report the unweighted mean gain over the first ten years after deselection. All values in these figures are based on our estimate that a 1 SD increase in true teacher VA increases earnings by $1.34 \%$ (Column 2 of Table 3). All calculations assume that teachers teach one class per year and report mean values for math and English teachers, which are calculated separately. We calculate earnings gains using Monte Carlo simulations based on our estimates of the teacher VA process as described in Section VI. All values in these figures and their undiscounted equivalents are reported in Appendix Table 13.

## APPENDIX FIGURE 1

## Stability of College Rankings by Age of Earnings Measurement

a) Rankings of Colleges Based on Earnings at Ages 23 and 27 vs. Age 32

b) Correlation of College Rankings Based on Earnings at Age 32

With Rankings Based on Earnings at Earlier Ages


Notes: In Panel A, we take all college attendees in 1999 at age 20, as recorded by 1098-T forms, and construct three separate college quality indices by averaging $\mathrm{W}-2$ earnings by college at ages 23,27 , and 32 . We convert each college quality measure into a percentile rank based on the within-age distribution of college quality. We then bin colleges into 100 equal-sized (percentile) bins using the college quality measure based on age 32 earnings and plot the mean percentile rank of colleges in each bin using the age 23 (in circles) and age 27 (in triangles) measures. The best-fit lines are estimated from an unweighted OLS regression of percentile ranks run at the college level. In Panel B, we take the same college attendees and calculate ten separate college quality measures by averaging $\mathrm{W}-2$ earnings by college at each age from $23-32$. We then plot the Spearman rank correlation between each college quality measure based on earnings at ages 23-31 and the college quality measure based on earnings at age 32 .

## APPENDIX FIGURE 2

## Correlations Between Outcomes in Adulthood and Test Scores



Notes: These figures present binned scatter plots corresponding to the cross-sectional regressions of outcomes in adulthood on test scores presented in Columns 1-4 of Appendix Table 3. See notes to Table 1 and Appendix Table 3 for further information on the variable definitions and sample specification. In each panel, the series in circles corresponds to the first row of estimates, without controls. The series in triangles corresponds to the second row of estimates, which includes the full control vector used to estimate the value-added model. To construct the series in circles, we bin raw test scores into twenty equal-sized groups (vingtiles) and plot the means of the outcome within each bin against the mean test score within each bin. To construct the series in triangles, we first regress both the test scores and adult outcomes on the individual and class controls and teacher fixed effects and compute residuals of both variables. We then divide the test score residuals into twenty equal-sized groups and plot the means of the outcome residuals within each bin against the mean test score residuals within each bin. Finally, we add back the unconditional mean of both test scores and the adult outcome in the estimation sample to facilitate interpretation of the scale. We connect the dots in the non-linear series without controls and show a best-fit line for the series with controls, estimated using an OLS regression on the microdata.

## APPENDIX FIGURE 3

Jacob and Levitt (2003) Proxy for Test Manipulation vs. Value-Added Estimates


Notes: This figure plots the relationship between our leave-out-year measure of teacher value added and Jacob and Levitt's proxy for cheating. The regressions are estimated on the linked analysis sample (as described in the notes to Table 1). Teacher value-added is estimated using data from classes taught by a teacher in other years, following the procedure described in Section III.A. The y-axis variable is constructed as follows: Let $\Delta \bar{A}_{c, t}=\bar{A}_{c, t}-\bar{A}_{c, t-1}$ denote the change in mean test scores from year $t-1$ and $t$ for students in classroom $c$. Let $R_{c, t}$ denote the ordinal rank of classroom $c$ in $\Delta \bar{A}_{c, t}$ among classrooms in its grade, subject, and school year and $r_{c, t}$ the ordinal rank as a fraction of the total number of classrooms in that grade, subject, and school year. Jacob and Levitt's (2003) measure for cheating in each classroom is $J L_{c}=\left(r_{c, t}\right)^{2}+\left(1-r_{c, t+1}\right)^{2}$. Higher values of this proxy indicate very large test score gains followed by very large test score losses, which Jacob and Levitt show to be correlated with a higher chance of having suspicious patterns of answers indicative of cheating. Following Jacob and Levitt, we define a classroom as an outlier if its value of $J L_{c}$ falls within the top $5 \%$ of classrooms in the data. To construct the binned scatter plot, we group classrooms into percentiles based on their teacher's estimated value-added, ranking classrooms separately by school-level and subject. We then compute the percentage of Jacob-Levitt outliers within each percentile bin and scatter these fractions vs. the percentiles of teacher VA. Each point thus represents the fraction of Jacob-Levitt outliers at each percentile of teacher VA. The dashed vertical line depicts the 99th percentile of the value-added distribution. We exclude classrooms with estimated VA above this threshold in our baseline specifications because they have much higher frequencies of Jacob-Levitt outliers. See Appendix Table 8 for results with trimming at other cutoffs.

## APPENDIX FIGURE 4

## Correlation of Earnings Over the Lifecyle



Notes: This figure plots the correlation of wage earnings at each age $x$ with wage earnings at age $x+12$. We calculate wage earnings as the sum of earnings reported on all W-2 forms for an individual in a given year. Individuals with no W-2 are assigned 0 wage earnings. Earnings at age $x$ are calculated in 1999, the first year in which we have W-2 data, and earnings at age $x+12$ are calculated in 2011, the last year of our data. We calculate these correlations using the population of current U.S. citizens. The dashed vertical line denotes age 28 , the age at which we measure earnings in our analysis of teachers' impacts.


[^0]:    ${ }^{1}$ Value-added models of teacher quality were pioneered by Hanushek (1971) and Murnane (1975). More recent examples include Rockoff (2004), Rivkin, Hanushek, and Kain (2005), Aaronson, Barrow, and Sander (2007), and Kane and Staiger (2008).
    ${ }^{2}$ Recent work has shown that early childhood education has significant long-term impacts (e.g. Heckman et al. 2010a, 2010b, Chetty et al. 2011), but there is no evidence to date on the long-term impacts of teacher quality as measured by value-added.

[^1]:    ${ }^{3}$ This calculation discounts the earnings gains at a rate of $5 \%$ to age 12 . The estimated total undiscounted earnings gains from this policy are approximately $\$ 50,000$ per child and $\$ 1.4$ million for the average classroom.
    ${ }^{4}$ The gains remain substantial despite noise because very few of the teachers with low VA estimates ultimately turn out to be excellent teachers. For example, we estimate that $3.2 \%$ of the math teachers in elementary school whose estimated VA is in the bottom $5 \%$ based on three years of data actually have true VA above the median.

[^2]:    ${ }^{5}$ An alternative approach to identify the direct impacts of teachers in each grade $g$ would be to include teacher VA in all grades simultaneously in the model in (4). Unfortunately, this is not feasible because our primary research design requires conditioning on lagged test scores and lagged scores are endogenous to teacher quality in the previous grade. For the same reason, we also cannot identify the substitutability or complementarity of teachers' impacts across grades. See Appendix A for further details.

[^3]:    ${ }^{6}$ Another way to identify $\kappa_{g}$ is to directly estimate the covariance of teachers' effects on earnings $\left(\mu_{j t}^{Y}\right)$ and test scores $\left(\mu_{j t}\right)$ in a correlated random effects or factor model. Chamberlain (2013) develops such an approach and obtains estimates similar to those reported here.

[^4]:    ${ }^{7}$ A few classrooms contain students at different grade levels because of retentions or split-level classroom structures. To avoid dropping a subset of students within a classroom, we include every classroom that has at least one student who would graduate school during or before 2008-09 if she progressed at the normal pace. That is, we include all classrooms in which $\min _{i}\left(12+\right.$ school year - grade $\left._{i}\right) \leq 2009$.
    ${ }^{8}$ Here and in what follows, the year refers to the tax year, i.e. the calendar year in which income is earned. In most cases, tax returns for tax year $t$ are filed during the calendar year $t+1$.
    ${ }^{9}$ We find little or no correlation between match rates and teacher VA in the various subsamples we use in our analysis and obtain very similar estimates of teachers' impacts on long-term outcomes when restricting the sample to school-grade-subject cells with above-median match rates (see Appendix Table 7).

[^5]:    ${ }^{10}$ According to the Current Population Survey, $27.2 \%$ of the non-institutionalized population between the ages of 25 and 29 was not employed in 2011. The non-employment rate in our sample may differ from this figure because it includes the institutionalized population in the denominator and applies to a relatively low-income urban public school district.

[^6]:    ${ }^{11}$ The remaining students are likely to have parents who did not file tax returns in the early years of the sample when they could have claimed their child as a dependent, making it impossible to link the children to their parents. Note that this definition of parents is based on who claims the child as a dependent, and thus may not reflect the biological parent of the child.
    ${ }^{12}$ Because the children in our sample vary in age by over 25 years whereas the tax data start only in 1996, we cannot measure parent characteristics at the same age for all children. For simplicity, we instead measure parent characteristics at a fixed time. Measuring parent income at other points in time yields very similar results (not reported).
    ${ }^{13}$ We set the mother's age at child's birth to missing for 78,007 observations in which the implied mother's age at birth based on the claiming parent's date of birth is below 13 or above 65 , or where the date of birth is missing entirely from SSA records.

[^7]:    ${ }^{14}$ For much of the analysis in our first paper, we restricted attention to the subset of observations in the core sample that have lagged scores and other controls needed to estimate the baseline VA model. Because we do not control for individual-level variables in most of the specifications in this paper, we do not impose that restriction here.

[^8]:    ${ }^{15}$ Teacher fixed effects account for correlation between $\mathbf{X}_{i t}$ and mean teacher VA. If $\mathbf{X}_{i t}$ is correlated with fluctuations in teacher VA across years due to drift, one may still obtain biased estimates of $\boldsymbol{\beta}^{Y}$. This problem is modest because only $20 \%$ of the variance in $\widehat{m} j t$ is within teacher. Moreover, we obtain similar results when estimating $\widehat{m}_{j t}$ and $\boldsymbol{\beta}^{Y}$ from regressions without teacher fixed effects and implementing a standard partial regression (Chetty, Friedman, and Rockoff 2011b). We estimate $\boldsymbol{\beta}^{Y}$ using within-teacher variation here for consistency with our approach to estimating teacher VA in the first paper; see Section 2.2 of that paper for further details.
    ${ }^{16}$ The test score results are reported in our companion paper. We do not have adequate precision to implement the quasi-experimental design for earnings or within specific subgroups, which is why the cross-sectional estimates remain valuable.
    ${ }^{17}$ Unless otherwise specified, the independent variable in all the regressions and figures in this paper is normalized test-score VA $\widehat{m}_{j t}$. For simplicity, we refer to this measure as "value-added" or VA below.

[^9]:    ${ }^{18}$ This problem does not arise when estimating the impacts of treatments such as class size because the treatment is observed; here, the size of the treatment (teacher VA) must itself be estimated, leading to correlated estimation errors.

[^10]:    ${ }^{19}$ In practice, the identity $\hat{\kappa}=\hat{\kappa}_{C}$ does not hold exactly because the class means $\mathbf{X}_{c t}$ are defined using all observations with non-missing data for the relevant variable. Some students are not matched to the tax data and hence are missing $Y_{i}^{*}$, while other students are missing some of the individual-level covariates $\mathbf{X}_{i t}^{I}$ (e.g., prior-year test scores). As a result, $\mathbf{X}_{c t}$ does not exactly equal the mean of $\mathbf{X}_{i t}^{I}$ within classrooms in the final estimation sample. To verify that the small discrepancies between $\mathbf{X}_{c t}$ and $\mathbf{X}_{i t}^{I}$ do not affect our estimates of $\kappa$, we show in Appendix Table 7 that the inclusion of individual controls $\mathbf{X}_{i t}^{I}$ has little impact on the point estimates of $\kappa$ by estimating (6) for a selected set of specifications on the individual data.
    ${ }^{20}$ In Appendix Table 7 of Chetty, Friedman, and Rockoff (2011b), we evaluated the robustness of our results to other forms of clustering for selected specifications. We found that school-cohort clustering yields more conservative confidence intervals than more computationally intensive techniques such as two-way clustering by student and classroom.

[^11]:    ${ }^{21}$ Appendix Figure 3 plots the fraction of classrooms that are in the top 5 percent according to Jacob and Levitt's proxy, defined in the notes to the figure, vs. our leave-out-year measure of teacher value-added. On average, classrooms in the top 5 percent according to the Jacob and Levitt measure have test score gains of 0.47 SD in year $t$ followed by mean test score losses of 0.42 SD in the subsequent year. Stated differently, teachers' impacts on future test scores fade out much more rapidly in the very upper tail of the VA distribution. Consistent with this pattern, these exceptionally high VA teachers also have very little impact on their students' long-term outcomes.
    ${ }^{22}$ In this and all subsequent scatter plots, we also demean $\widehat{m}_{j t}$ within subject-by-school-level groups to isolate variation within these cells as in the regressions, and then add back the unconditional mean of $\widehat{m}{ }_{j t}$ in the estimation sample.

[^12]:    ${ }^{23}$ These and all other estimates reported below reflect the value of a 1 SD improvement in actual teacher VA $m_{j t}$, as shown in Section I. Being assigned to a teacher with higher estimated VA yields smaller gains because of noise in $\widehat{m}_{j t}$ and drift in teacher quality, an issue we revisit in Section VI.
    ${ }^{24}$ We code the parent characteristics as 0 for the $5.2 \%$ of students whom we matched to the tax data but were unable to link to a parent, and include an indicator for having no parent matched to the student. We also code mother's age at child's birth as 0 for the small number of observations where we match parents but do not have data on parents' ages, and include an indicator for such cases.
    ${ }^{25}$ The sample in Column 3 has fewer observations than in Column 1 because twice lagged test scores are not observed in 4th grade. Replicating the specification in Column 1 on exactly the estimation sample used in Column 3 yields an estimate of $0.81 \%(0.09)$.

[^13]:    ${ }^{26}$ The magnitude of the four-year attendance impact ( 0.79 pp ) is very similar to the magnitude of the single-year attendance impact ( 0.82 pp ). Since the students who are on the margin of attending for one year presumably do not all attend for four years, this suggests that better teachers increase the number of years that students spend in college on the intensive margin.

[^14]:    ${ }^{27}$ We calculate this number using the mean wage earnings of a random sample of the U.S. population in 2007 to obtain an earnings profile over the lifecycle, and then inflate these values to 2010 dollars. See Chetty et al. (2011) for details.

[^15]:    ${ }^{28}$ Prior studies (e.g., Kane and Staiger 2008, Jacob, Lefgren, and Sims 2010, Rothstein 2010, Cascio and Staiger 2012) document similar fadeout after one or two years but have not determined whether test score impacts continue to deteriorate after that point. The broader span of our dataset allows us to estimate test score persistence more precisely. For instance, Jacob, Lefgren, and Sims estimate one-year persistence using 32,422 students and two-year persistence using 17,320 students. We estimate one-year persistence using more than 5.6 million student-year-subject observations and four-year persistence using more than 1.3 million student-year-subject observations.

[^16]:    ${ }^{29}$ In our baseline specifications, we impute teacher VA as the sample mean ( 0 ) for students for whom we have no leave-out-year VA estimate $\widehat{m}_{j t}^{-\{t, t-1\}}$, either because we have no teacher information or because the teacher did not teach in the district outside of years $\{t-1, t\}$. We show below that we obtain similar results when restricting to the subset of school-grade-subject-year cells with no missing data on teacher VA. See Section V of our companion paper for additional discussion on the effects of this imputation.
    ${ }^{30}$ Part of the variation in $\Delta Q_{s g t}$ comes from drift. Even for a given teacher, predicted VA will change because our forecast of VA varies across years. Because the degree of drift is small across a single year, drift accounts for $5.5 \%$ of the variance in $\Delta Q_{s g t}$. As a result, isolating the variation due purely to teacher switching using an instrumental variables specification yields very similar results (not reported).

[^17]:    ${ }^{31}$ In Figure 3 of our companion paper, we directly use event studies around the entry and exit of teachers in the top and bottom $5 \%$ to demonstrate the impacts of VA on test scores. We do not have adequate power to identify the impacts of these exceptional teachers on college attendance using such event studies. In the cross-cohort regression that pools all teaching staff changes, the $t$-statistic for college attendance is 3.78 (Column 1 of Table 5a in this paper). The corresponding t-statistic for test scores is 34.0 (Column 2 of Table 5 of the first paper). We have much less power here both because the college attendance is only observed for the older half of our sample and because college is a much noisier outcome than end-of-grade test scores.

[^18]:    ${ }^{32}$ For instance, estimating the specification in Column 1 of Table 5 with earnings at age 28 as the dependent variable yields a confidence interval of $(-\$ 581, \$ 665)$, which contains both 0 and values nearly twice as large as the estimated earnings impacts based on our first research design.

[^19]:    ${ }^{33}$ Importantly, the relationship between college quality and test scores conditional on prior characteristics $X_{i t}$ is linear throughout the test score distribution (Appendix Figure 2b). Hence, the heterogeneity is not due to non-linearities in the relationship between scores and college outcomes but rather the fact that the same increase in scores translates to a bigger change in college outcomes for high SES families.

[^20]:    ${ }^{34}$ Restricting the sample in the same way does not affect the conclusions above about heterogeneity across subjects or demographic groups, because these groups are balanced across cohorts.

[^21]:    ${ }^{35}$ We have inadequate precision to estimate wage earnings impacts separately by subject and grade level. We therefore assume that a 1 SD improvement in teacher VA raises earnings by $1.34 \%$ in all subjects and grade levels in the calculations that follow.
    ${ }^{36}$ School districts typically average math and English VA ratings to calculate a single measure of teacher performance in elementary schools (e.g., District of Columbia Public Schools 2012). In Appendix D, we show that the gains from evaluating teachers based on mean math and English VA are only $12 \%$ larger than the gains from using information based on only one subject because math and English VA estimates are highly correlated. Therefore, the results we report below slightly underestimate the true gains from selection on mean VA.

[^22]:    ${ }^{37}$ These calculations do not account for the fact that deselected teachers may be replaced by rookie teachers, who have lower VA. In our sample, mean test score residuals for students taught by first-year teachers are on average 0.05 SD lower (in units of standardized student test scores) than those taught by more experienced teachers. Given that the median teacher remains in the district for approximately 10 years, accounting for the effect of inexperience in the first year would reduce the expected benefits of deselection over a typical horizon by $\frac{0.05 / 10}{2.063 \times \sigma\left(m_{j t}\right)}=2 \%$, where $\sigma\left(m_{j t}\right)=0.14$ is the mean SD of teacher effects across elementary school subjects in our data (see Table 2 of the first paper).
    ${ }^{38}$ Moreover, these calculations do not include the non-monetary returns to a better education (Oreopoulos and Salvanes 2010), such as lower teenage birth rates.
    ${ }^{39}$ Without drift, the formula in (15) reduces to $r(n)^{1 / 2} \times 2.063 \times \$ 522,000 \times b$, where $r(n)$ denotes the reliability of the VA estimate using $n$ years of data, which is straightforward to calculate analytically. The original working paper version of our study (Chetty, Friedman, and Rockoff 2011b) used this version of the formula and an estimate of $b$ based on a model that did not account for drift.
    ${ }^{40}$ In Panel B of Appendix Table 13, we distinguish these two factors by eliminating estimation error and predicting current VA based on past VA instead of past scores. Without estimation error, $G_{C}(1)=\$ 340,000$. Hence, drift and estimation error each account for roughly half of the difference between $G_{C}(1)$ and $G_{C}$.

[^23]:    ${ }^{41}$ We also replicated the simulations using VA estimates that do not account for drift. When the estimation window $n$ is short, drift has little impact on the weights placed on test scores across years. As a result, drift-unadjusted measures yield rankings of teacher quality that are very highly correlated with our measures and thus produce similar gains. For instance, selection based on 3 years of data using VA estimates that do not adjust for drift yields gains that are $98 \%$ as large as those reported above. Hence, while accounting for drift is important for evaluating out-of-sample forecasts accurately, it may not be critical for practical policy applications for VA.
    ${ }^{42}$ Of course, these other measures will also be affected by drift and estimation error. For instance, classroom observations have significant noise and may capture transitory fluctuations in teacher quality (Kane et al. 2013).

[^24]:    ${ }^{43}$ In the working paper version of his study, Rothstein calculates the wage gains needed to compensate teachers for a policy that deselects teachers below the 20th percentile after 2 years. Jesse Rothstein kindly provided the corresponding estimates for the policy analyzed here in personal correspondence.
    ${ }^{44}$ Even if there is erosion, as long as the signal quality of VA is a continuous function of its weight in evaluation decisions, one would optimally place non-zero weight on VA, because the net gains would fall from the initial level of $\$ 184,000$ in proportion to the weight on VA.

[^25]:    ${ }^{45}$ As we noted above, even in the low-stakes regime we study, some unusually high VA teachers have test score impacts consistent with test manipulation. If such behavior becomes more prevalent when VA is used to evaluate teachers, the predictive content of VA as a measure of true teacher quality could be compromised.

[^26]:    ${ }^{46} \mathrm{To}$ simplify notation, we write $\mu_{j(i, t), t}$ as $\mu_{j t}$ and always denote by $j$ the teacher who taught student $i$ in the relevant year $t$. For instance, $\mu_{j, t-s}$ denotes the value-added in year $t-s$ of the teacher $j$ who taught student $i$ in year $t-s$. We adopt the same convention with $\tau_{j t}$ below as well.

[^27]:    ${ }^{47}$ In general, controlling for lagged test scores need not completely account for the variation in $\zeta_{i}$ because lagged test scores are noisy measures of latent ability. The fact that controlling for $A_{i, t-1}$ does eliminate bias in practice (as shown in our first paper) suggests that students are allocated to classrooms based on factors highly correlated with $A_{i, t-1}$ and other factors that directly affect earnings $\left(\zeta_{i}^{Y}\right)$.

[^28]:    ${ }^{48}$ Legally, colleges are not required to file 1098-T forms for students whose qualified tuition and related expenses are waived or paid entirely with scholarships or grants. However, the forms appear to be available even for such cases, perhaps because of automated reporting to the IRS by universities.
    ${ }^{49}$ Only current citizenship status is recorded in the database. As a result, the date at which we determine citizenship is simply the date we accessed the data.
    ${ }^{50}$ We include the small fraction of students who attend more than one college in a single year in the determination of college quality for each unique institution to which they are matched.

[^29]:    ${ }^{51}$ As a result, $0.21 \%$ of students who attend college at age 20 in our sample are missing information on college quality.

