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# Memories in a network with excitatory and inhibitory plasticity are encoded in the spiking irregularity

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## Abstract

Cell assemblies are thought to be the substrate of memory in the brain. Theoretical studies have previously shown that assemblies can be formed in networks with multiple types of plasticity. But how exactly they are formed and how they encode information is yet to be fully understood. One possibility is that memories are stored in silent assemblies. Here we used a computational model to study the formation of silent assemblies in a network of spiking neurons with excitatory and inhibitory plasticity. We found that even though the formed assemblies were silent in terms of mean firing rate, they had an increased coefficient of variation of inter-spike intervals. We also found that this spiking irregularity could be readout with support of short-term plasticity, and that it could contribute to the longevity of memories.

## Introduction

Cortical synapses are plastic, allowing sensory experience to be stored in network connectivity. Concurrent activation of ensembles of neurons is thought promote cell assembly formation by potentiating their synapses [1]. Stronger synapses within neurons allows them to be more easily activated together, even in the presence of partial cues. How exactly cell assemblies are formed and how their synapses and firing activity encode information, however, is yet to be fully understood. Theoretical work [2, 3, 4, 5, 6, 7, 8] has shown it is possible to create such assemblies by combining different forms of synaptic plasticity. In some of these models [3, 4], when strongly connected assemblies are formed, spontaneous activity is characterized by an overall stable firing rate across the excitatory population, but with the firing rate of individual assemblies transitioning between periods of high and low activity.

25 Cell assemblies, however, may not necessarily be persistently active at all times. Assemblies could also  
26 be stored in a latent or quiescent state, from where they can be retrieved by a cue [9]. Storing them in  
27 a silent state could be advantageous from an energy efficiency point of view [10], specially if they are not  
28 being constantly recalled. Inhibitory engrams have been proposed as a way of implementing this type of  
29 silent assembly, and were suggested to form when increased excitation within a highly active ensemble of  
30 neurons would be matched by increased inhibition [11]. Theoretical work [2, 5, 6] has shown such silent  
31 assemblies can be formed by combining traditional spike-timing dependent forms of excitatory plasticity [12,  
32 13, 14] with inhibitory plasticity [2, 15, 16]. In these models, inhibitory plasticity counteracts the effect of  
33 excitatory potentiation, leading to the formation of cell assemblies in which the excitatory neurons receive  
34 increased excitatory and inhibitory currents (EI assemblies).

35 Although silent EI assemblies do not reactivate themselves during spontaneous activity, the memories  
36 they encode can still be reactivated by specific stimulation. Vogels, Sprekeler et al. [2] have shown that  
37 memories could be retrieved by momentarily disrupting balance within the assembly by stimulating a fraction  
38 of their neurons. Similarly, in Yger et al. [5], strengthening of the assembly led to stronger neural response  
39 upon stimulation. Since neurons belonging to an EI assembly receive increased excitation and inhibition,  
40 memories encoded by the EI assembly could also be reactivated by disinhibition [17, 18]. A transient decrease  
41 in inhibitory drive leads to a net increase in excitatory input to excitatory neurons belonging to the assembly,  
42 resulting in an increase in their activity. In Barron et al. [17], for example, dormant memories embedded in  
43 a network model could be retrieved by decreasing the efficacy of inhibitory synapses.

44 Here, we study how stronger connectivity within EI assemblies influences spontaneous activity. More  
45 specifically, we show that neural stimulation does form EI assemblies that are silent in terms of firing rate, but  
46 leaves a trace in the regularity of their spike trains. Therefore, we suggest it is possible to readout assembly  
47 information not only with specific stimulation, but also during spontaneous activity. In a feedforward model,  
48 we show that an increase in excitatory current leads to an increase in irregular firing in a neuron receiving  
49 feedforward plastic inhibition. We also show this irregularity can be readout with support of short-term  
50 plasticity (STP) [19]. We extend these results to a network model with excitatory [13] and inhibitory  
51 [2] plasticity, and show that neurons belonging to an EI assembly fire indeed more irregularly. During  
52 spontaneous activity, we demonstrate that irregularity can be readout with STP, even though assembly  
53 neurons are not being specifically stimulated and their mean firing rate is indistinguishable from the other  
54 excitatory neurons in the network. Furthermore, we analyze the decay of excitatory weights, and find  
55 that memory lifetime is increased due to the irregular firing of the neurons within the EI assemblies. Put  
56 together, our results suggest that, in silent assemblies, memories may be encoded in regularity of firing  
57 during spontaneous activity, which allows them to be readout without specific stimulation, and that this

58 could contribute to their longevity.

## 59 Results

### 60 iSTDP leads to more irregular firing upon increased excitatory currents

61 Inhibitory plasticity has been previously proposed as a mechanism to promote balance between excitatory  
62 and inhibitory currents to a neuron [2, 20], promoting homeostasis of the post-synaptic firing rate [2]. Such  
63 homeostatic regulation of firing rate at different levels of input currents, however, could have an effect on  
64 higher order statistics of post-synaptic firing. We therefore started by testing the effect of inhibitory plasticity  
65 on the irregularity of firing when a neuron received different intensities of excitatory current. For that, we  
66 used the inhibitory spike-timing dependent plasticity model (iSTDP) proposed by Vogels, Sprekeler et al.  
67 [2], which has been previously shown to reproduce multiple experimental results [2, 21, 22]. We simulated  
68 a single LIF neuron that received input from one excitatory source with a fixed weight  $W_{E \rightarrow E} = J$ , and  
69 from one inhibitory source through iSTDP [2] (Figure 1A). After the inhibitory weight had reached an  
70 equilibrium value, and the neuron fired at target rate, we increased the strength of the excitatory connection  
71  $W_{E \rightarrow E}$ . As expected, just after an increase of the excitatory current, the output neuron fired at a higher  
72 rate, triggering an upregulation of the inhibitory weight by iSTDP (Figure 1B-C), until the output neuron  
73 fired again at target rate (Figure 1C). We then repeated this procedure systematically, for different values of  
74 increase in strength of the excitatory connection  $W_{E \rightarrow E} = 2J, 3J, 4J, 5J$ . We observed that after plasticity  
75 had converged, the neuron fired always at target rate, but with a CV that increased with  $W_{E \rightarrow E}$  (Figure 1D).

76 To better understand this result, we calculated the expected firing rate and CV for an LIF neuron  
77 as a function of the mean and variance of its subthreshold membrane potential [24, 23] (see Methods for  
78 details of the calculation). Although higher excitatory and higher inhibitory currents contribute to the mean  
79 with different signs, they both contribute positively to the variance [24, 23]. This means that the same  
80 firing rate can be achieved by different combinations of mean and variance of the subthreshold membrane  
81 potential (contour lines on Figure 1E). At the same time, different combinations of mean and variance of  
82 the subthreshold membrane potential will lead to different values of CV (Figure 1F). More specifically, for  
83 a given fixed firing rate, the CV will be higher when mean is lower and variance is higher (Figure 1G).  
84 Therefore, for a neuron receiving inhibitory plastic input under iSTDP, an increase in excitatory currents  
85 leads to lower mean membrane potential and more irregular spikes.

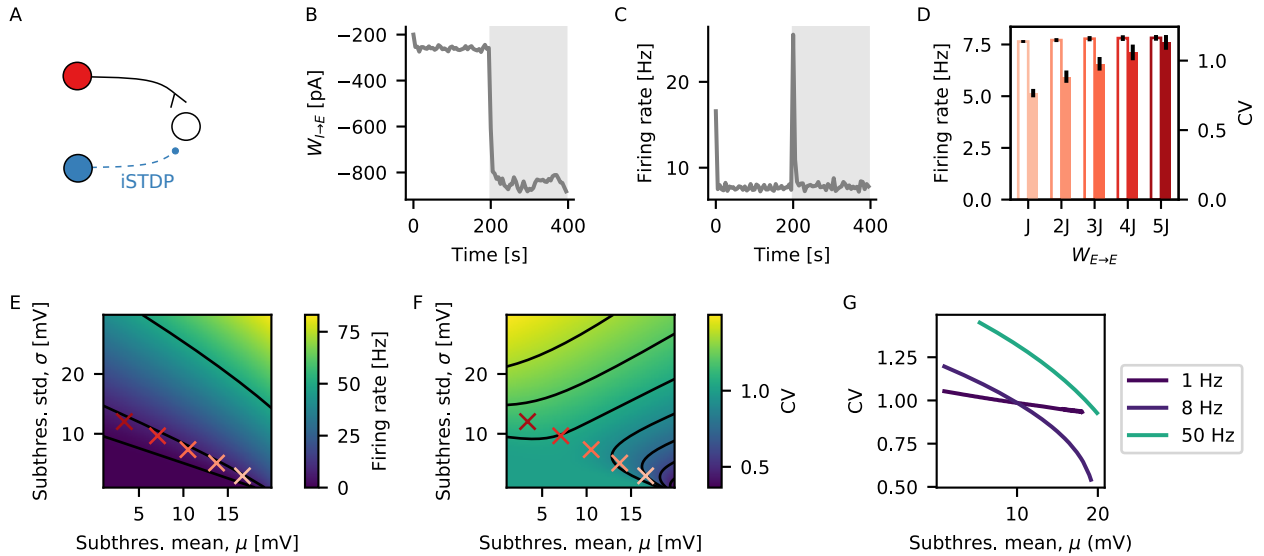


Figure 1: **iSTDP leads to more irregular firing upon increased excitatory currents.** (A) A single LIF neuron receives input from one excitatory source with a fixed weight, and one inhibitory source through iSTDP. (B) Synaptic weight from the inhibitory source to the output neuron as a function of time. The grey shaded area indicates the period where the weight from the excitatory source is increased from  $W_{E \rightarrow E} = J$  to  $W_{E \rightarrow E} = 4J$ . (C) Firing rate of the output neuron as a function of time. Grey shaded area as in (B). (D) Mean firing rate (edge colored) and CV (full colored) of the output neuron for different values of increase in excitatory current  $W_{E \rightarrow E} = J, 2J, 3J, 4J, 5J$ . Black lines show standard deviation across 10 independent output neurons. Firing rate and CV are calculated using the last 50s of the simulation. (E) Predicted firing rate of a LIF neuron as a function of mean ( $\mu$ ) and standard deviation ( $\sigma$ ) of its subthreshold membrane potential from theoretical calculations [23]. The red crosses indicate mean and standard deviation of subthreshold membrane potential from neurons in (D), with matching colors. Black lines show contour lines for firing rate equal 1, 8 and 50 Hz. (F) Same as (E) for CV. (G) Predicted CV from theory as a function of mean subthreshold membrane potential for a fixed firing rate, matching the contour lines on (E).

## 86 Different levels of irregularity can be readout with short-term plasticity (STP)

87 If the irregularity of spike trains can carry information about previous stimulation, one important question  
 88 is whether it can be decoded by an output neuron. To that end, we connected an output LIF neuron  
 89 to multiple inputs with same rate and CV (Figure 2A). For a given input firing rate, the postsynaptic  
 90 subthreshold membrane potential had a constant mean  $\mu_{V_m}$  (Figure 2B), and a standard deviation  $\sigma_{V_m}$   
 91 that increased with CV (Figure 2C). The increase in  $\sigma_{V_m}$  alone, however, was not enough to trigger large  
 92 modulation of output firing rate with input CV. Therefore, we found that an increase in CV of the input  
 93 neurons led to slightly increased firing rate of the output neuron (Figure 2D)

94 Previously, STP has been shown to increase postsynaptic sensitivity to bursts [25]. Here, introducing  
 95 short-term facilitation [19] (STF) in the connections to the output neuron (Figure 2E) led to modulation of  
 96 the mean  $\mu_{V_m}$  (Figure 2F), as well as the standard deviation  $\sigma_{V_m}$  (Figure 2G), of the subthreshold voltage  
 97 with the CV of the input neurons. This in turn was reflected in a larger modulation of output rate with

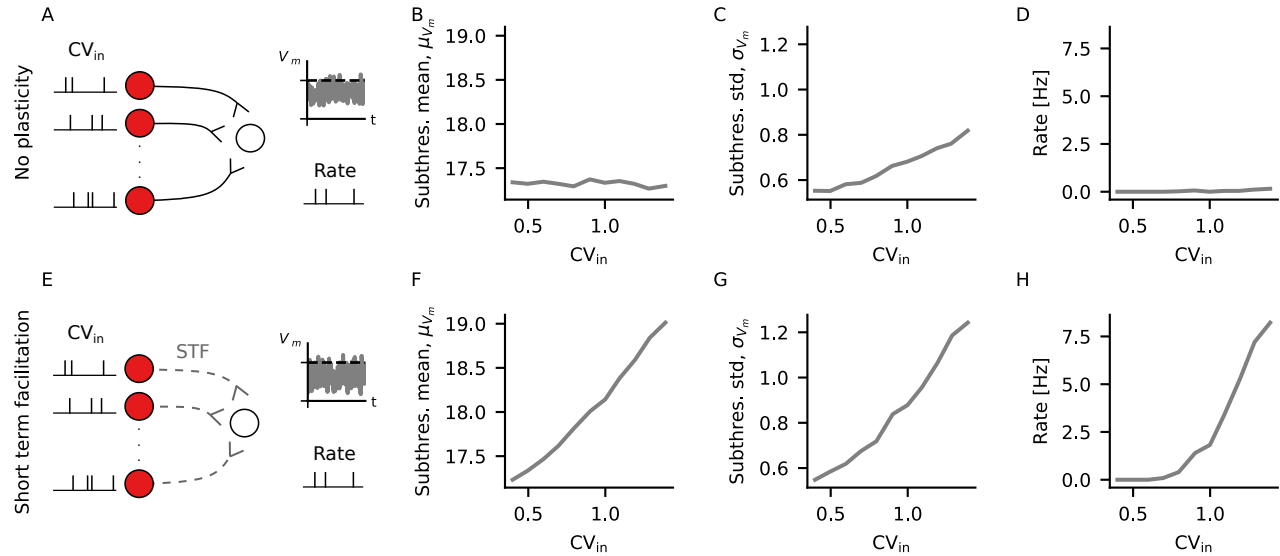


Figure 2: **Different levels of irregularity can be readout with short-term plasticity (STP).** (A) An output neuron receives input through static excitatory connections from multiple neurons firing at the same rate and CV. The small plots on the right illustrate what is measured from the output neuron, namely its subthreshold membrane potential and its firing rate (B) Mean subthreshold membrane potential of the output neuron in (A), for different values of CV. (C) Standard deviation of the subthreshold membrane potential of the output neuron in (A) for different values of CV. (D) Output firing rate of the neuron in (A) for different values of CV. (E-H) Same as (A-D), but with output neuron receiving input through plastic excitatory connections following short-term facilitation.

98 input CV (Figure 2H). In summary, although higher values of input CV lead to larger standard deviation  
 99 of the subthreshold voltage of the output neuron in the presence of static synapses, this has only a small  
 100 effect on the firing rate of the output neuron. In the presence of STF, on the other hand, higher input CV  
 101 also leads to higher mean subthreshold voltage of the output neuron, leading to a larger modulation of the  
 102 output rate with input CV. Therefore, the irregularity of spike trains can be decoded with the support of  
 103 STF.

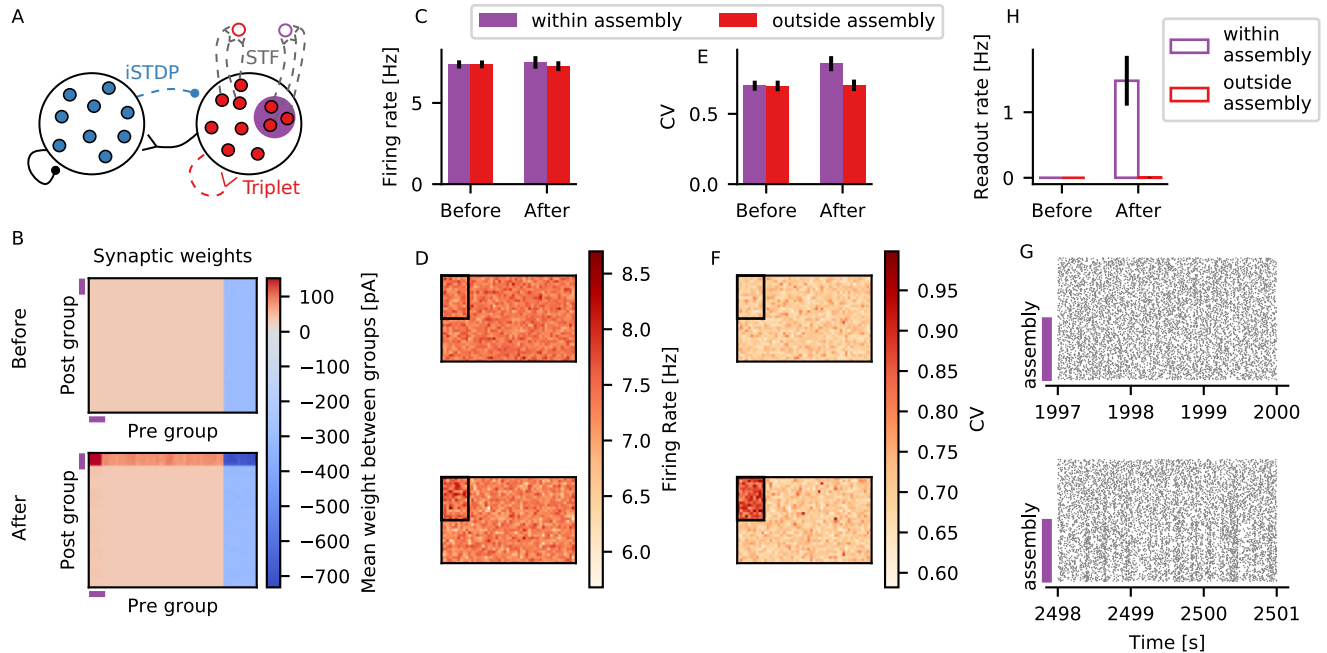
## 104 **Assemblies formed by excitatory and inhibitory plasticity are silent but leave a** 105 **trace in terms of irregular firing**

106 Inhibitory plasticity has been proposed to support the formation of balanced excitatory-inhibitory assemblies  
 107 (EI assemblies) by matching high excitatory currents in neurons following increased excitatory plasticity [11,  
 108 2]. We just showed that an increase in excitatory current led to more irregular firing of a neuron receiving  
 109 inhibitory input through iSTDP (Figure 1) and that a difference in irregularity modulated the output firing  
 110 rate of a neuron receiving plastic input under STF (Figure 2). Put together, this suggests that formation of  
 111 EI assemblies leaves a trace on the regularity of spike trains, which can be readout with STP.

112 In order to test this idea, we started by investigating whether the formation of EI assemblies left a  
113 trace on irregularity of firing in a model similar to the one presented in Vogels et al. [2]. We simulated a  
114 recurrent network of excitatory and inhibitory LIF neurons in which inhibitory-to-excitatory synapses were  
115 plastic according to the iSTDP rule [2] and other synapses were static (Supplementary Figure 1A). We also  
116 included two output neurons, one receiving input from the neurons within the EI assembly and the other  
117 receiving input from a group of excitatory neurons outside the assembly (Supplementary Figure 1A). Both  
118 output neurons received those inputs through connections that were plastic according to STF. Once the  
119 excitatory neurons had reached their target firing rate, we formed an assembly by hardwiring an increase in  
120 excitatory weights between assembly neurons by a factor of 6. As shown in Vogels et al. [2], this increase in  
121 recurrent excitatory weights led to an increase in firing rate of assembly neurons, which triggered an increase  
122 in incoming inhibitory weights through the iSTDP rule [2] (Supplementary Figure 1B). Following a transient  
123 period, the within assembly excitatory neurons fired again at target rate (Supplementary Figure 1C-D),  
124 but with higher CV (Supplementary Figure 1E-F). Moreover, following the assembly formation, the output  
125 neuron connected to the assembly fired with higher rate than the one connected to excitatory neurons outside  
126 the assembly (Supplementary Figure 1H).

127 We proceeded by including excitatory plasticity on this recurrent network, such that assemblies could be  
128 formed by specific stimulation of neurons. Starting from the previous model of recurrent network (Supple-  
129 mentary Figure 1A), we made excitatory-to-excitatory synapses plastic according to a triplet-based model of  
130 STDP [13] (Figure 3A). This triplet model was built as an extension of classical pair-based STDP models, and  
131 has been shown to reproduce a series of experiments on plasticity [13]. In this model, weights are potentiated  
132 by post-pre-post triplets, such that high post-synaptic firing rate leads to LTP [13]. An EI assembly was  
133 then formed by stimulating a subset of the excitatory neurons (Figure 3A). The increase in activity following  
134 stimulation led to potentiation of both excitatory synapses through the triplet rule and inhibitory synapses  
135 through iSTDP, as shown in Vogels et al. [2] (Figure 3B). After a transient period, given the homeostatic  
136 nature of the iSTDP rule [2], the mean firing rate of the stimulated neurons was indistinguishable from the  
137 rest of the network (Figure 3C-D). At this point, due to the increase in synaptic weights (Figure 3B), the  
138 neurons belonging to the assembly received more excitatory and more inhibitory currents than before the  
139 stimulation protocol, which led to more irregular spike trains (Figure 3E-F).

140 The increase in excitatory-to-excitatory weights also led to higher correlation between assembly neurons  
141 (Figure 3G and see Supplementary Figure 3 for full population raster plots). This means that the formed  
142 assemblies are ‘silent’ in terms of mean firing rate, but not in terms of correlation. The strength of within  
143 assembly connectivity was determined here by the maximum weight allowed for excitatory-to-excitatory  
144 connections  $W_{E \rightarrow E}^{max}$ . If weaker assemblies were formed, the effect on CV was smaller than the observed one.



**Figure 3: Assemblies formed by excitatory and inhibitory plasticity are silent but leave a trace in terms of irregular firing.**

(A) The simulated network is composed of excitatory (red) and inhibitory (blue) LIF neurons. Inhibitory-to-excitatory connections (dotted blue) are plastic according to iSTDTP [2] and excitatory-to-excitatory (dotted red) according to the triplet rule [13]. An EI assembly is formed when a subset of the excitatory neurons (purple) is stimulated. One readout neuron receives input from the EI assembly (purple edge color) and another readout neuron receives input from a subset of excitatory neurons outside of the assembly, but with same size as the assembly (red edge color). The readout synapses are plastic under STF (dotted grey). Inhibitory-to-inhibitory and excitatory-to-inhibitory connections (black) are static. (B) Mean synaptic weight between groups of neurons. Neurons are sorted such that the first 160 neurons are assembly neurons. Neurons are then divided into groups of 40 neurons, and shown is the average synaptic weight between groups. Shown are excitatory (red scale) and inhibitory (blue scale) synaptic weights to excitatory neurons only. Synaptic weights which are not plastic are not shown. The purple lines indicate the position of groups comprising assembly neurons only. (C) Mean firing rate of neurons within the assembly (purple) and outside the assembly (red) before and 500 s after stimulation. Black lines show standard deviation across neurons for a single simulation run. (D) Firing rate of all excitatory neurons in the network before (*top*) and 500 s after (*bottom*) stimulation. Neurons are displayed in a 32 x 50 grid. The black square on each panel indicates neurons belonging to the assembly. (E-F) Same as (C-D) for the CV. (C-F) Mean firing rate and CV are calculated using 50 s of activity. (G) Raster plots showing 3 s activity of 160 neurons within the assembly and 160 excitatory neurons outside of the assembly before stimulation (*top*) and 500 s after stimulation (*bottom*). The purple lines indicate neurons belonging to the assembly. (H) Firing rate of the readout neuron connected to the assembly (purple edge) or outside assembly (red edge), before and after stimulation. Black lines show standard deviation across 5 independent simulation runs.

145 If stronger assemblies were formed, on the other hand, there was an increase in correlation (Supplementary  
146 Figures 2 and 3).

147 As previously seen in the network without excitatory plasticity (Supplementary Figure 1H), we also  
148 observed that the output neuron connected to the EI assembly fired with a larger firing rate than the output  
149 neuron connected to the random group of excitatory neurons (Figure 3H). This is probably due to higher



150 correlation within assembly neurons, but also due to higher CV. Even though all neurons in the network  
151 fired at the same mean rate, the neurons belonging to the EI assembly fired more irregular spike trains. Due  
152 to STF, short intervals between spikes led to more STF and, consequently, higher activity of the output  
153 neuron, as previously seen (Figure 2).

154 In summary, in neurons belonging to an EI assembly, assembly embedding encodes a trace in the regularity  
155 of their spike trains, which can be decoded by an output neuron through plastic connections with STF. Put  
156 together, this suggests that there are traces of the memory available from the neuronal activity even during  
157 seemingly silent moments, which could be potentially used for downstream processing without the need for  
158 an externally stimulated recall.

### 159 **Stronger assemblies decay more slowly due to both the irregular spiking and** 160 **correlations**

161 Due to the homeostatic nature of iSTDP, assembly neurons fired at target rate after formation of the  
162 assembly (Figure 3C-D). Given that this value was below the threshold for potentiation of the triplet rule,  
163 the stronger weights between assembly neurons decayed with time (Figure 4 and Supplementary Figure 4).  
164 We were therefore interested in how the decay of excitatory weights was influenced by the strength of the  
165 assemblies. In order to test that, we performed the following simulations. After forming an assembly by  
166 stimulating a subgroup of neurons, the external input was set back to its baseline value and we measured  
167 the weight decay between pairs of synaptically connected neurons belonging to the assembly (Figure 4A).  
168 We performed separate simulations in which the assemblies were formed with different strengths, by setting  
169 different values of maximum allowed excitatory-to-excitatory weights  $W_{E \rightarrow E}^{\max}$ .

170 We observed that the stronger assemblies decayed more slowly than the weaker ones (Figure 4B-D).  
171 Slower decay of stronger assemblies could be explained by increased correlation caused by the stronger  
172 excitatory weights (Figure 4D). Increased correlation means there should be a higher occurrence of pre-post  
173 pairs within short time windows. Considering the triplet rule [13], it is expected that such an increase should  
174 lead to more potentiation between excitatory weights and, therefore, slower decay of the assemblies. At the  
175 same time, the triplet rule is also known to potentiate post-pre-post triplets [13]. In that case, we should  
176 also expect more potentiation in cases where the postsynaptic neuron is firing with higher CV, given that  
177 higher CV translates into an increased occurrence of shorter intervals between two consecutive post-synaptic  
178 spikes.

179 Therefore, we also expected a slower decay of assembly weights due to higher CVs, and not exclusively  
180 due to increased correlation coefficient (CC). In order to test this, we tried to disentangle the effects of CC

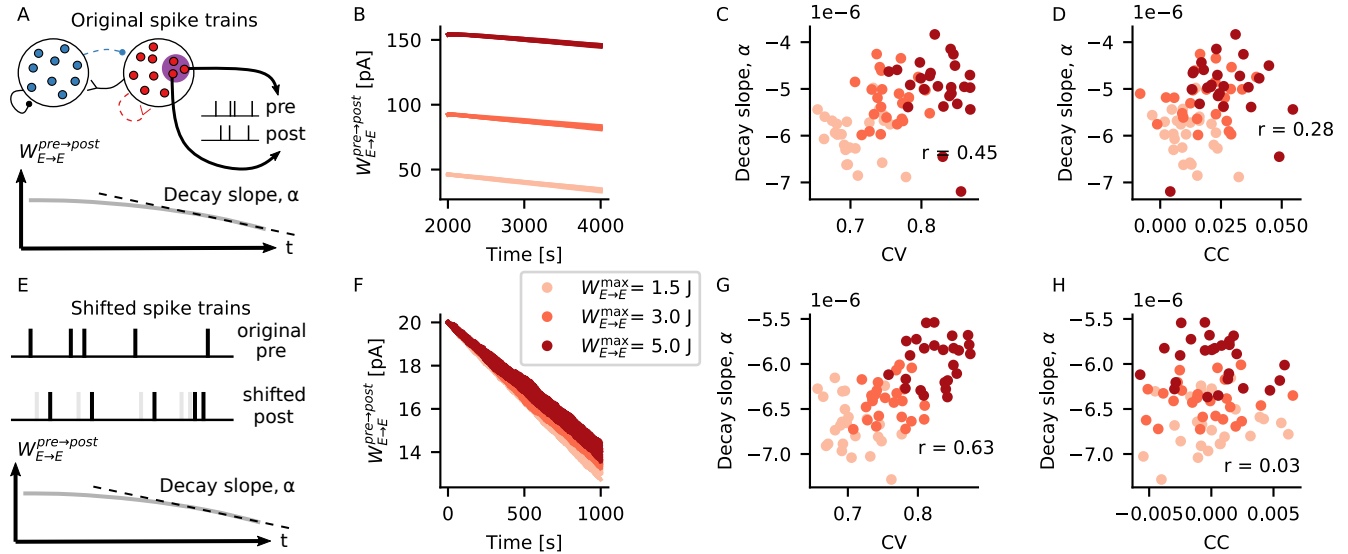


Figure 4: **Stronger assemblies decay more slowly due to both the irregular spiking and correlations.** (A) Spike trains of 5 pairs of synaptically connected assembly neurons and the time series of the excitatory weight between them are extracted from each of the 5 independent simulation runs shown on Figure 3. A linear function is fitted to the last 1000s of the weight decay, and its decay slope  $\alpha$  is extracted. (B) Excitatory weight between assembly neurons during 2000s after the embedding of the assembly. Shown are the weights between 5 different pairs of connected neurons, for each of 3 different assembly strengths (shades of red,  $W_{E \rightarrow E}^{max} = 1.5, 3$  and 5 J). (C) Slope of weight decay  $\alpha$  plotted against mean CV between pre- and post-synaptic spike trains for different strengths of assembly. (D) Slope of weight decay  $\alpha$  plotted against correlation coefficient (CC) between pre- and post-synaptic spike trains for different strengths of assembly. (C-D) Mean CV and CC are calculated using the last 50s of simulation,  $r$  shows the Pearson's correlation coefficient between  $x$  and  $y$  values. (E) For each pair of pre- and post-synaptic neurons in (A), the post-synaptic spike train is shifted by 3s, and the synaptic weight between the last 1000s of the pre- and manipulated post-synaptic spike trains is calculated. (F-H) Same as (B-D), but for the shifted spike trains.

181 and CV by calculating the weight decay of manipulated spike trains. For each pair of pre-post spike trains  
 182 recorded in our intact simulation (Figure 4A), we artificially shifted the post-synaptic spike train by 3s,  
 183 and calculated the weight decay for the manipulated spike train (Figure 4E). By performing this shift we  
 184 observed two things. Firstly, as expected, shifting the spike trains led to lower correlation between spike trains  
 185 (Figure 4H) and overall faster decay of assembly weights (Figure 4F-H). Secondly, the weights of assemblies  
 186 with higher CV decayed more slowly even for the shifted spike trains (Figure 4G), when correlation between  
 187 pre and post activity was almost zero (Figure 4H). Taken together, these results indicate that not only CC,  
 188 but also higher CVs lead to slower decay of assemblies.

## 189 Discussion

190 Cell assemblies are considered to be the substrate of memories in the brain. But how exactly memories are  
191 encoded in the synaptic weights and the firing statistics of assembly neurons is yet to be fully understood.  
192 Our results suggest that, in the presence of inhibitory plasticity [2], a memory trace can be encoded in  
193 the regularity of neuronal firing. More specifically, we have shown that increasing excitatory input to a  
194 neuron, which also received plastic feedforward inhibition [2], caused the neuron to fire spike trains with  
195 higher coefficient of variation of inter-spike intervals (CV). We have also shown that this change in CV could  
196 be readout with the support of short-term facilitation [19]. In a recurrent network model with excitatory  
197 [13] and inhibitory [2] plasticity, we have shown that embedding a cell assembly left a trace in terms of  
198 irregular firing, which suggests the memory could still be available for influencing downstream processing  
199 even when the memory is stored in a silent state. Furthermore, we have shown that excitatory weights within  
200 the assembly decayed more slowly for stronger assemblies, due to both increased irregularity and increased  
201 correlation between assembly neurons.

202 In our current work, within assembly excitatory weights decayed back to baseline levels if the formed  
203 assembly was not reactivated by external input (Figure 4 and Supplementary Figure 4). This means that  
204 any memory encoded in the assembly would be slowly forgotten if no external reactivation was performed.  
205 A memory that is not forgotten without external reactivation would require that assembly weights are  
206 strengthened during spontaneous activity. Previous theoretical work has shown that in a network with  
207 multiple plasticity mechanisms, the structure of cell assemblies can be reinforced during spontaneous activity  
208 through self reactivation [3]. Even without self reactivation, when the firing rate of assembly neurons is  
209 below the potentiation threshold for the triplet rule, within assembly weights can still be reinforced during  
210 spontaneous activity if correlation between assembly neurons is high enough, as previously shown in [6]. In  
211 our simulations, stronger correlation between assembly neurons could be achieved with stronger excitatory  
212 weights, but this would possibly also require stronger recurrent weights overall in the network to stabilize  
213 network activity. Alternatively, including other plasticity mechanisms such as plastic excitatory-to-inhibitory  
214 weights could lead to the formation of balanced clusters containing both excitatory and inhibitory neurons.  
215 Embedding such clusters in networks has been shown to allow multistability and faster transitions in assembly  
216 activity between high and low firing rate [26]. In any case, the formation of self reinforcing silent EI assemblies  
217 through increased correlation between assembly neurons would also make assemblies less silent.

218 Silent assemblies have also been shown to form in simulations without inhibitory plasticity [27]. For  
219 example, silent assemblies can be formed with a model of structural plasticity on excitatory synapses [28, 29].  
220 In those studies, stimulation of an assembly led to rewiring of synapses such that the assembly neurons were

221 more likely to be connected, but the total indegree of excitatory neurons remained unchanged. Different to  
222 what we found here, the silent assemblies in that case were formed by rearranging the excitatory connections,  
223 but without increasing total excitatory and inhibitory input currents. Therefore, the mean excitatory and  
224 inhibitory input to assembly neurons was the same before and after the assembly embedding. In that case,  
225 embedding the assembly does not leave a trace on the regularity of firing of assembly neurons. Therefore,  
226 silent assemblies formed in different ways could potentially leave specific markers on neuronal firing patterns,  
227 which could contribute different functional aspects to a more complex circuit.

228 One prediction from our simulations is that neurons belonging to an engram fire with more irregular  
229 spike trains. While not many studies have investigated firing patterns of engram neurons *in vivo*, Tanaka  
230 et al. [30] did find that engram neurons were more likely to fire in bursts. They measured activity of place  
231 cells in hippocampal region CA1 during context discrimination. They found that not all place cells belonged  
232 to an engram, but those that did had higher burst rates and shorter inter-burst intervals. Furthermore,  
233 they found that engram neurons were more likely to fire during, and be phase locked to, fast gamma events.  
234 Since fast gamma oscillations correlate with inputs from entorhinal cortex [31], they have suggested that  
235 engram neurons in CA1 may be more responsive to inputs coming from this region. It remains an open and  
236 interesting question whether there could be any causal relationship between the burst firing of engram cells  
237 and their responsiveness to specific inputs.

238 Burst firing could also have an influence on how input signals are processed and on how signals are  
239 propagated to downstream areas [32]. In our model, the memory encoded in a silent EI assembly would be  
240 reflected in the CV, or level of burstiness of individual neurons. Interestingly, in a recent study, Koren et  
241 al. [33] found that the activity of bursty neurons in monkey primary visual cortex was more informative  
242 for decoding behavior than the activity of non-bursty neurons. Bursts have also been proposed to modulate  
243 the effect of plasticity [14, 13], and shown to implement credit assignment in a model of burst-dependent  
244 synaptic plasticity [34]. This could be relevant in a context of multiplexing, since firing rate and bursts could  
245 convey separate streams of information. In Naud and Sprekeler [25], it was shown that multiplexing could  
246 be implemented in a neuron if single spikes and bursts were considered as two distinct codes. Similarly in  
247 the work we present in this paper, the firing rate and regularity of spike trains, or the CV, could also serve  
248 as two separate streams of information. Different to Naud and Sprekeler [25], however, the CV is modulated  
249 by the amount of inhibitory current, which changes according to the iSTDP rule [2]. Therefore, changes  
250 in CV happen at a slow time scale. In other words, the signal encoded by the CV would have to be a  
251 slow signal. Alternatively, a faster signal could be constructed by gating the activity of different neurons, or  
252 populations of neurons, that fire with constant CV. On the other hand, faster changes in firing rate could still  
253 be propagated without triggering plastic changes through iSTDP and, therefore, without affecting the CV.

254 It remains an open question of how the synaptic increase and the larger CV within an assembly modulate  
255 the output firing of a stimulated neuron.

256 In conclusion, our results show that embedding cell assemblies in a network with excitatory and inhibitory  
257 plasticity can leave a trace in terms of regularity of firing. This means that information about the assembly  
258 can be present in the neuronal activity even when the memory is stored in a silent state. Moreover, we  
259 showed that this information could be readout during spontaneous activity with support of STF, which  
260 suggests the silent memory could potentially modulate other signals in the absence of direct stimulation.  
261 Furthermore, we also showed how this change in regularity contributes to the longevity of memories. Put  
262 together, our results propose a different way in which memories could be encoded in silent EI assemblies.

## 263 Methods

### 264 Neuron model

265 All neurons in our simulations were current-based leaky integrate-and-fire (LIF) with exponential post-  
266 synaptic currents (PSC). The sub-threshold membrane potential  $V_i$  of neuron  $i$  obeyed the following equation:

$$\tau_m \frac{dV_i}{dt} = -V_i + RI(t), \quad (1)$$

267 where  $\tau_m = 20$  ms is the membrane time constant and  $R = 80$  MOhm is the input resistance. The input  
268 current  $I(t)$  consisted of the sum of all excitatory and inhibitory currents coming from pre-synaptic sources.  
269 Unless stated otherwise, the input current from a pre-synaptic neuron  $j$  to a post-synaptic neuron  $i$  evolved  
270 according to:

$$\frac{dI_j(t)}{dt} = -\frac{I_j(t)}{\tau_{\text{syn}}} + W_{ij} \sum_k \delta(t - t_j^k), \quad (2)$$

271 where  $\tau_{\text{syn}} = 1.5$  ms is the synaptic time constant and  $W_{ij}$  represents the synaptic weight between pre-  
272 synaptic neuron  $j$  and post-synaptic neuron  $i$ . The spike train  $\sum_k \delta(t - t_j^k)$  consisted of all spikes produced  
273 by neuron  $j$ . The synaptic weight  $W_{ij}$  was fixed for static synapses. For synapses that obeyed excitatory and  
274 inhibitory plasticity,  $W_{ij} = \bar{w} \times w_{ij}(t)$ , where  $\bar{w}$  is a scaling constant and  $w_{ij}(t)$  is a dimensionless variable  
275 that evolved according to the equations for excitatory and inhibitory plasticity described below.  $\bar{w}_E = 1$  pA  
276 for excitatory synapses and  $\bar{w}_I = -1$  pA for inhibitory synapses. In the following sections, some synaptic  
277 weight parameters are given with respect to a reference value  $J = 30.8$  pA, which was chosen such that the  
278 maximum amplitude of the post-synaptic potential would be 0.15 mV.

279 Every time the membrane potential reached a threshold value  $V_{\text{th}} = 20$  mV, the neuron emitted a spike.  
280 Following a spike, the membrane potential was reset to  $V_{\text{reset}} = 10$  mV and remained there for a refractory  
281 period  $t_{\text{ref}} = 2$  ms.

## 282 Plasticity models

### 283 Inhibitory plasticity

284 Plastic inhibitory-to-excitatory connections followed the inhibitory spike timing-dependent plasticity rule  
285 (iSTDP) by [2]. In this rule, synaptic weights  $w_{ij}$  between pre-synaptic neuron  $j$  and post-synaptic neuron  $i$   
286 are updated whenever there is a pre-synaptic spike ( $t^{\text{pre}}$ ) or post-synaptic spike ( $t^{\text{post}}$ ), respectively, according  
287 to:

$$\begin{aligned} w_{ij}(t) &\rightarrow w_{ij}(t) + \eta(x_i - \alpha) & \text{if } t = t^{\text{pre}}, \\ w_{ij}(t) &\rightarrow w_{ij}(t) + \eta x_j & \text{if } t = t^{\text{post}}, \end{aligned} \quad (3)$$

288 where  $\eta$  is the learning rate,  $\alpha = 2 \times \rho \times \tau_{\text{STDP}}$  is a depression factor and  $\rho$  is a constant parameter that sets  
289 the target firing rate of the post-synaptic neuron [2]. The synaptic trace  $x_i$  increases by 1 whenever neuron  $i$   
290 fires a spike and decays otherwise with time constant  $\tau_{\text{STDP}}$ , according to:

$$\frac{dx_i(t)}{dt} = -\frac{x_i(t)}{\tau_{\text{STDP}}}. \quad (4)$$

291 The parameters used were  $\eta = 0.3$ ,  $\rho = 9$  Hz and  $\tau_{\text{STDP}} = 20$  ms. Weights were bound to a maximum  
292  $W_{I \rightarrow E}^{\text{max}} = 3000$  pA

### 293 Excitatory plasticity

294 Recurrent excitatory-to-excitatory connections in the network simulations were plastic according to the  
295 triplet-based model of spike timing-dependent plasticity by [13]. In this model, synaptic weights  $w_{ij}$  between  
296 pre-synaptic neuron  $j$  and post-synaptic neuron  $i$  are updated whenever there is a pre-synaptic spike ( $t^{\text{pre}}$ )  
297 or post-synaptic spike ( $t^{\text{post}}$ ), respectively, according to:

$$\begin{aligned}
 w_{ij}(t) &\rightarrow w_{ij}(t) - o_1(t - \epsilon)[A_2^- + A_3^- r_2(t - \epsilon)] & \text{if } t = t^{\text{pre}}, \\
 w_{ij}(t) &\rightarrow w_{ij}(t) + r_1(t - \epsilon)[A_2^+ + A_3^+ o_2(t - \epsilon)] & \text{if } t = t^{\text{post}},
 \end{aligned}
 \tag{5}$$

298 where  $A_2^-, A_3^-, A_2^+, A_3^+$  denote amplitude of weight changes and  $r_1, r_2, o_1$  and  $o_2$  are synaptic traces. In the  
 299 original model [13],  $\epsilon$  is a small positive constant to ensure weights are updated before the traces  $o_2$  and  $r_2$ .  
 300 In our simulations,  $\epsilon$  illustrates the fact that weights were always updated before all trace values, including  
 301  $o_1$  and  $r_1$ . The pre-synaptic (post-synaptic) traces  $r_1$  and  $r_2$  ( $o_1$  and  $o_2$ ) are increased by 1 whenever the  
 302 pre-synaptic (post-synaptic) neuron fires, and decay otherwise according to:

$$\begin{aligned}
 \frac{dr_1(t)}{dt} &= -\frac{r_1(t)}{\tau_+}, \\
 \frac{dr_2(t)}{dt} &= -\frac{r_2(t)}{\tau_x}, \\
 \frac{do_1(t)}{dt} &= -\frac{o_1(t)}{\tau_-}, \\
 \frac{do_2(t)}{dt} &= -\frac{o_2(t)}{\tau_y}
 \end{aligned}
 \tag{6}$$

303 Weights were bounded between  $W_{E \rightarrow E}^{\min} = J$  and  $W_{E \rightarrow E}^{\max}$ , which was assigned different values at different  
 304 simulations. The parameters used were taken from [13]:  $A_2^- = 7 \times 10^{-3}$ ,  $A_3^- = 2.3 \times 10^{-4}$ ,  $A_2^+ = 7.5 \times 10^{-10}$ ,  
 305  $A_3^+ = 9.3 \times 10^{-3}$ ,  $\tau_+ = 16.8$  ms,  $\tau_x = 101$  ms,  $\tau_- = 33.7$  ms,  $\tau_y = 125$  ms.

### 306 Short-term plasticity

307 In simulations with short-term plasticity, the model used was the short-term facilitation (STF) by [19]. In  
 308 this model, the total synaptic input to a post-synaptic neuron  $i$  is given by:

$$I(t) = \sum_j A y_j(t),
 \tag{7}$$

309 where  $A$  is the absolute synaptic weight, and  $y_j$  determines the effective contribution of the PSC from neuron  
 310  $j$  to the input current to neuron  $i$ . It evolves according to the system of equations:

$$\begin{aligned}\frac{dx_j}{dt} &= \frac{z_j}{\tau_{\text{rec}}} - u_j x_j \delta(t - t_{\text{pre}}), \\ \frac{dy_j}{dt} &= -\frac{y_j}{\tau_{\text{syn}}} + u_j x_j \delta(t - t_{\text{pre}}), \\ \frac{dz_j}{dt} &= \frac{y_j}{\tau_{\text{syn}}} - \frac{z_j}{\tau_{\text{rec}}},\end{aligned}\tag{8}$$

311 where  $x_j$ ,  $y_j$  and  $z_j$  are the fraction of synaptic resources in the recovered, active and inactive states, respec-  
312 tively, from neuron  $j$ ,  $t_{\text{pre}}$  denotes the timing of a pre-synaptic spike,  $\tau_{\text{syn}}$  is the decay time constant of PSC  
313 and  $\tau_{\text{rec}}$  is the recovery time constant for depression. The variable  $u_j$  describes the effective use of synaptic  
314 resources by each pre-synaptic spike, and it evolves according to:

$$\frac{du_j}{dt} = -\frac{u_j}{\tau_{\text{fac}}} + U(1 - u_j)\delta(t - t_{\text{pre}})\tag{9}$$

315 where  $\tau_{\text{fac}}$  is the time constant for facilitation and the parameter  $U$  determines how much  $u_j$  is increased  
316 with each spike. The absolute synaptic weight used was  $A = 1000$  pA. The remaining parameters were  
317 taken from [25]:  $U = 0.02$ ,  $\tau_{\text{rec}} = 100$  ms,  $\tau_{\text{fac}} = 100$  ms.

## 318 Simulations

319 All simulations were performed using the neural network simulator NEST 2.20.0 [35].

### 320 Single neuron simulation (Figure 1)

#### 321 Spiking simulation

322 A single output neuron received input from an external input, an excitatory and an inhibitory source. The  
323 external input represented a source of feedforward input and it was modeled as a Poisson process with rate  
324  $\nu_{\text{ext}} = 18$  kHz. It connected to the output neuron with a fixed synaptic weight  $W_{\text{ext}} = J/3$ , which did  
325 not change throughout simulations. The excitatory source represented recurrent input received from other  
326 neurons within the same network. It was modeled as a Poisson process with rate  $\nu_{\text{exc}} = 1440$  Hz and it  
327 connected to the output neuron with a fixed synaptic weight  $W_{E \rightarrow E} = J$ , which varied between simulations.  
328 The inhibitory source was modeled as a Poisson process with rate  $\nu_{\text{inh}} = 360$  Hz, and it connected to the  
329 output neuron with a plastic synapse following the iSTDP rule. The choices of parameters were made in  
330 order to match the scenario from Figure 3. After a warm-up period of 200 s of simulation, the excitatory  
331 synaptic weight was increased to a multiple of the original weight  $W_{E \rightarrow E} = 1J, 2J, 3J, 4J, 5J$ . The weight



332 from the external input source remained unaltered. The simulation ran for another 200 s. Mean firing rate  
333 and coefficient of variation of inter-spike intervals of the output neuron were calculated using the last 50 s of  
334 simulation.

### 335 **Subthreshold membrane potential simulation**

336 The mean and variance of the subthreshold membrane potential ( $x$  and  $y$  coordinates of red crosses in  
337 Figure 1E-F and  $x$  coordinates on Figure 1G) were calculated in a new set of simulations. In those simulations,  
338 the spiking threshold of the output neuron was removed, such that the output neuron produced no spikes.  
339 Given that the output neuron produced no spikes, the connection from the inhibitory source was static.  
340 The weight  $W_{I \rightarrow E}$  used was the mean synaptic weight from the spiking simulation, averaged across the last  
341 100 s of simulation. This scenario was simulated for 400 s, and mean and standard deviation of membrane  
342 potential were calculated using the last 200 s of simulation.

### 343 **Single readout simulation (Figure 2)**

344 Two output neurons received input from 160 input sources. Both neurons were the same, except that the  
345 spiking neuron had a spiking threshold  $V_{th} = 20$  mV and the non spiking neuron had none. Input sources  
346 were modeled as Gamma processes. Their spike trains were generated by randomly sampling inter-spike-  
347 intervals from a Gamma distribution with parameters shape  $k = \frac{1}{CV^2}$  and scale  $\theta = \frac{CV^2}{\nu}$ , where CV was the  
348 prescribed coefficient of variation of inter-spike intervals and  $\nu = 9$  Hz was the prescribed mean rate of each  
349 spike train. A different value of CV was used for each simulation, ranging from  $CV = 0.4$  to  $CV = 1.4$  in  
350 intervals of 0.1. Both output neurons also received a constant current  $I = 150$  pA. Each simulation lasted  
351 55 s. Output rate was calculated from the spiking output neuron using the last 50 s of simulation. The mean  
352 and standard deviation of subthreshold membrane potential was calculated from the non spiking output  
353 neuron using the last 50 s of simulation.

354 In the simulations with no plasticity, the input sources were connected to the output neurons with a fixed  
355 synaptic weight  $W_{E \rightarrow E} = J$ . In the simulations with short-term plasticity, the input sources connected to  
356 the output neurons with plastic synapses following STF.

### 357 **Network simulation (Figures 3 and 4)**

358 The recurrent network comprised  $N_E = 1600$  excitatory and  $N_I = 400$  inhibitory neurons. The excitatory  
359 (inhibitory) population formed synapses to randomly selected neurons from both excitatory and inhibitory  
360 populations with an indegree  $C_E = 0.1N_E$  ( $C_I = 0.1N_I$ ). All neurons received a background input in the form

361 of a spike train with Poisson statistics with rate  $\nu_{\text{ext}} = 18$  kHz and weight  $W_{\text{ext}} = J/3$ . Synapses from the  
362 excitatory to the inhibitory population were static with weight  $W_{E \rightarrow I} = J$ . Synapses from the inhibitory  
363 to the inhibitory population were static and stronger by a factor of 10 ( $W_{I \rightarrow I} = -10J$ ). Excitatory-to-  
364 excitatory synapses followed the triplet based STDP rule, and inhibitory-to-excitatory synapses followed the  
365 iSTDP rule.

366 After a warm-up period of 2000 s, a subgroup comprising 10% of the excitatory neurons was stimulated.  
367 Stimulation consisted of increasing the rate of the external input to the stimulated subgroup by a factor 5  
368 for 1 s. Following stimulation, the rate of the external input was set back to its original value  $\nu_{\text{ext}}$ , and the  
369 network was simulated for further 2000 s.

370 Two readout neurons received input from either the stimulated neurons, or a subgroup of excitatory  
371 neurons with the same size as the stimulated subgroup. The synapses connecting excitatory neurons to  
372 readout neurons followed STF.

### 373 Theoretical rate and CV

374 The firing rate  $\nu$  of a leaky integrate-and-fire neuron can be estimated by the following equation (see details  
375 of the derivation in [24, 23]).

$$\nu = \left[ t_{\text{ref}} + \tau_m \sqrt{\pi} \int_{\frac{V_{\text{reset}} - \mu}{\sigma}}^{\frac{V_{\text{th}} - \mu}{\sigma}} e^{u^2} (1 + \text{erf}(u)) du \right]^{-1} \quad (10)$$

376 where  $\mu$  and  $\sigma$  are respectively the mean and standard deviation of the subthreshold membrane potential,  
377  $t_{\text{ref}}$  is the refractory period,  $\tau_m$  is the membrane time constant of the neuron,  $V_{\text{th}}$  is the threshold potential,  
378  $V_{\text{reset}}$  is the reset potential and  $\text{erf}()$  is the error function.

379 The coefficient of variation of inter-spike intervals for a neuron firing with rate  $\nu$  and different combina-  
380 tions of mean  $\mu$  and variance  $\sigma$  of subthreshold membrane potential can be theoretically predicted using the  
381 following equation (see derivation in [23]):

$$\text{CV} = \left[ 2\pi\nu^2 \int_{\frac{V_{\text{reset}} - \mu}{\sigma}}^{\frac{V_{\text{th}} - \mu}{\sigma}} e^{x^2} dx \int_{-\infty}^x e^{y^2} (1 + \text{erf}(y))^2 dy \right]^{\frac{1}{2}} \quad (11)$$

### 382 Data analysis

#### 383 Firing rate

384 Mean firing rates  $r$  were calculated using:

$$r = \frac{S}{N\Delta T}, \quad (12)$$

385 where  $S$  is the number of spikes of all  $N$  neurons during time interval  $\Delta T$ . For single neuron mean rate,  
386  $N = 1$ .  $\Delta T = 50$  s unless stated otherwise.

### 387 CV

388 Coefficient of variation of inter-spike intervals (ISI) were calculated using:

$$CV = \sigma_{\text{ISI}}/\mu_{\text{ISI}}, \quad (13)$$

389 where  $\sigma_{\text{ISI}}$  is the standard deviation and  $\mu_{\text{ISI}}$  is the mean of the ISI of an individual neuron. CVs were  
390 calculated using 50 s of spiking data.

### 391 CC

392 The spike count correlation between a pair of neurons  $i$  and  $j$  was calculated as the Pearson correlation  
393 coefficient

$$R_{ij} = \frac{c_{ij}}{\sqrt{c_{ii}c_{jj}}}, \quad (14)$$

394 where  $c_{ij}$  is the covariance between spike counts extracted from spike trains of neurons  $i$  and  $j$ , and  $c_{ii}$  is the  
395 variance of spike counts extracted from neuron  $i$ . In Figure 4, correlations were calculated from spike trains  
396 comprising the last 1 000 s of activity, using bins of size 10 ms. In Figure 3, correlations were calculated from  
397 spike trains comprising the 10 s of activity shown in the raster plots, using bins of size 10 ms.

### 398 Decay slope

399 The decay slope  $\alpha$  of excitatory weights was calculated by fitting a linear function to the last 1 000 s of the  
400  $W_{E \rightarrow E}(t)$  decay data, and extracting its slope. The fitting was performed using a standard fitting algorithm  
401 from NumPy.

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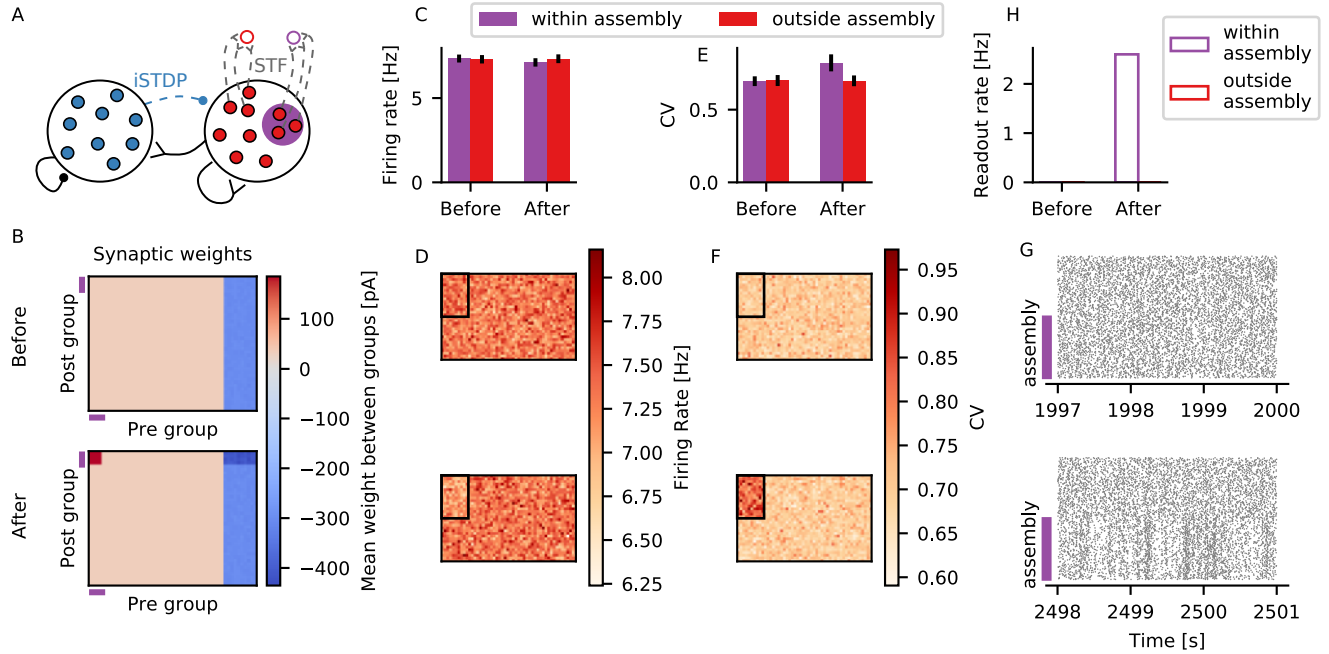
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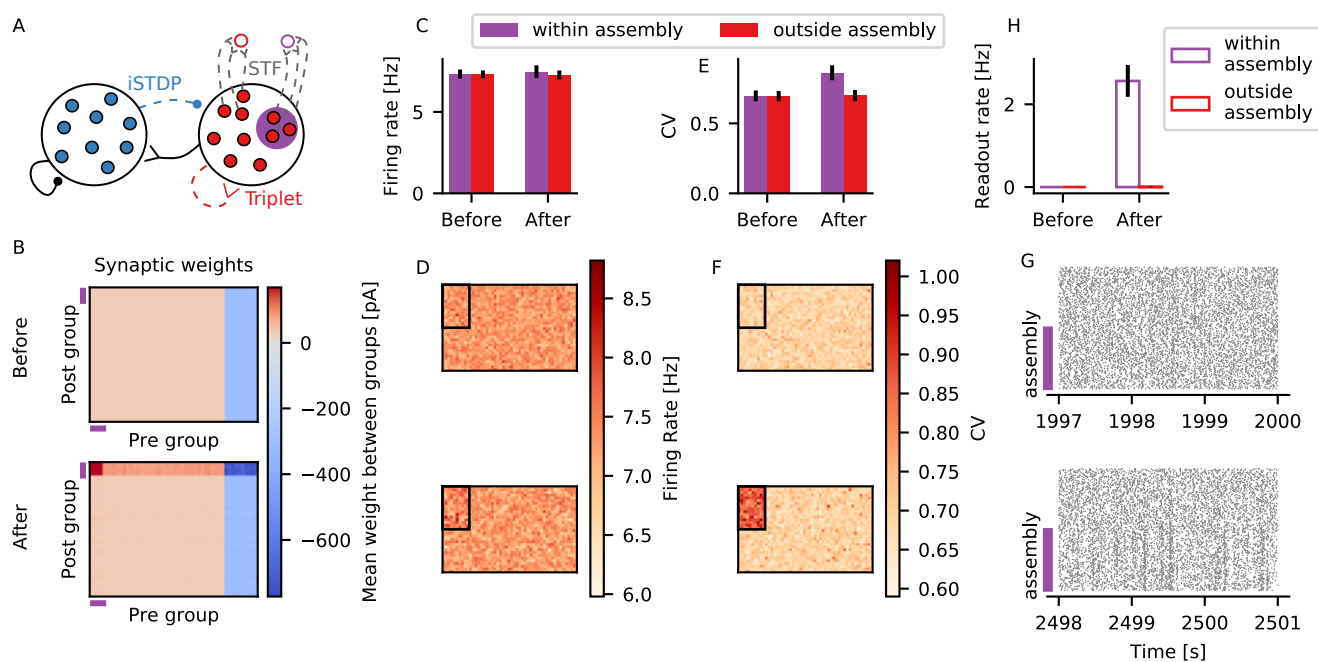
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519 Trust 200790/Z/16/Z, Simons Foundation 564408 and EPSRC EP/R035806/1.

520 **Supplementary Material**

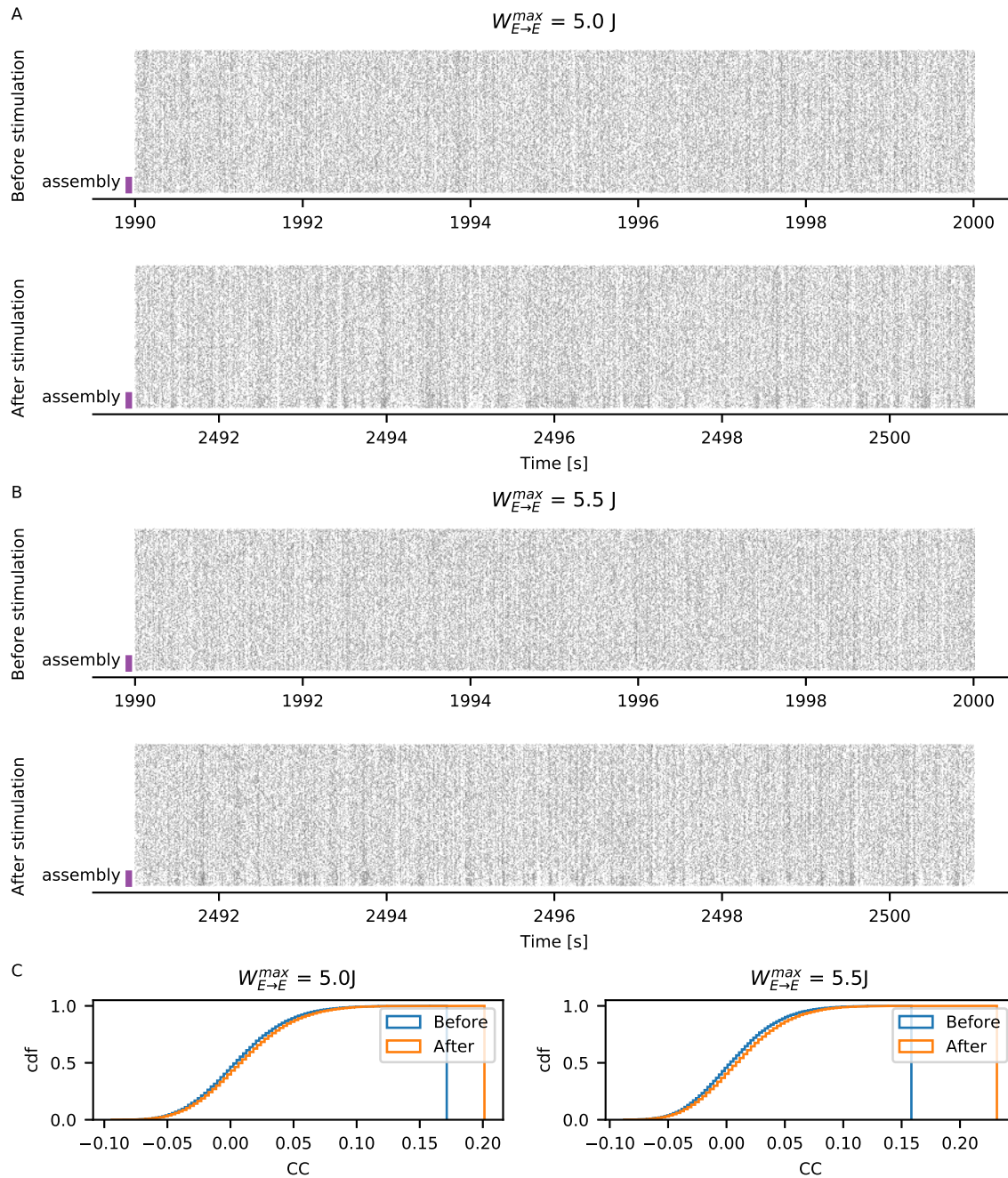


Supplementary Figure 1: Formation of assembly without the triplet rule. Same as Figure 3 from the main text, but excitatory to excitatory connections are static (no triplet rule). The assembly is formed by hardwiring an increase in excitatory weights between assembly neurons by a factor of 6. Please note that in order to achieve a similar effect on CV, the increase by a factor of 6 is larger than  $W_{E \rightarrow E}^{max} = 5$  J on the main figure. This is because the triplet rule leads to potentiation of weights from all excitatory neurons in the network to the assembly neurons, which is not the case for this static scenario (Compare (H) to Figure 3H in the main text).

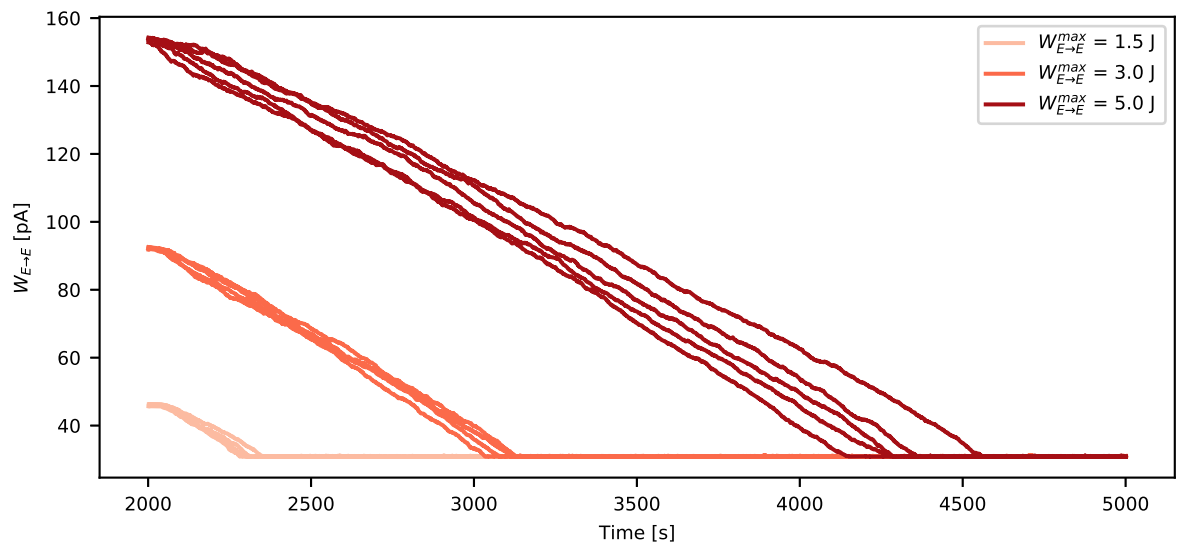




Supplementary Figure 2: Formation of stronger assembly. Same as Figure 3 from the main text, but with  $W_{E \rightarrow E}^{max} = 5.5$  J



Supplementary Figure 3: Whole population raster plot. (A) Raster plot of all assembly neurons (purple) and all other excitatory neurons outside the assembly, during 10s before (*top*), and 500s after (*bottom*) stimulation, for  $W_{E \rightarrow E}^{max} = 5 \text{ J}$  (same simulation as Figure 3 in the main text). (B) Same as (A) for  $W_{E \rightarrow E}^{max} = 5.5 \text{ J}$  (same simulation as Supplementary Figure 2). (C) Cumulative distribution of correlation coefficients between all pairs of assembly neurons (ASB) before (blue) and after (red) stimulation on (A) (*left*) and (B) (*right*).



Supplementary Figure 4: Decay of assembly weights to baseline. Excitatory-to-excitatory weights between assembly neurons as a function of time for different values of  $W_{E \rightarrow E}^{max}$ . For these simulations, plasticity was accelerated by multiplying  $\eta$  from the iSTDP rule, and  $A_2^+$ ,  $A_2^-$ ,  $A_3^+$ ,  $A_3^-$  from the triplet rule by a factor of 10. Shown are the weights between 5 different pairs of pre- and post-synaptic neurons, for each simulation run.