Microwave Fourier Transform Double Resonance Experiment and Theory

H. Dreizler, E. Fliege, H. Mäder, and W. Stahl

Abteilung Chemische Physik im Institut für Physikalische Chemie der Universität Kiel

We present the first experience with a three-level double resonance experiment performed with a microwave Fourier transform spectrometer. The results are described by a theoretical treatment based on three-level Bloch equations.

1. Introduction

Battaglia, Gozzini, and Polacco [1], Shimoda, Yajima [2, 3], and Cox, Flynn, and Wilson [4] supplemented microwave spectroscopy by double resonance and thereby increased the versatility and applicability of this field of spectroscopy. In the course of our efforts to develop microwave Fourier transform spectroscopy (MWFT) of molecular gases in thermal equilibrium [5—8], we tried to test whether double resonance experiments are possible with this technique.

2. Experimental

To perform a double resonance experiment, it is necessary that two radiations interact with the molecular ensemble. A signal radiation detects the changes introduced by a usually strong pump radiation, which is resonant or near resonant to a transition as shown in Figure 1. It is essential that the pump radiation is prevented from reaching the detection system, i.e. the performance of the MWFT spectrometer as described earlier [6] should not be disturbed.

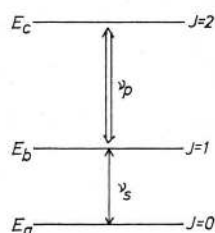These conditions could be fulfilled in the first place by replacing the waveguide to coax transition

Fig. 1. System of three level double resonance, here Carbonylsulfide, OCS, ⇔ pump radiation, ↔ signal radiation, $\nu_{s0} = (E_b - E_a)/h$; $\nu_{p0} = (E_c - E_b)/h$.

9a of Fig. 1 in Ref. [6] by a special tunable transition, on the back side of which an R-band waveguide (26.4—40 GHz, 22 GHz cut off) is introduced. Through this the pump radiation is fed into the sample cell of 23×23 mm cross section (see Figure 2). The pump radiation is supplied by a phase stabilized BWO and is amplified by a TWTA. A maximum of 2 W was available. Secondly we put a band and low pass filter in front of the switch 23 of Fig. 1 in Ref. [6]. Carbonylsulfide, $^{16}O^{12}C^{32}S$, $^{16}O^{12}C^{34}S$, and $^{18}O^{12}C^{32}S$ in natural abundancies were used for this test. As can be seen from Fig. 3—7 a double resonance doublet was observed. The behaviour of the doublet with variation of pump frequency, pump power and gas pressure reminds of the results from
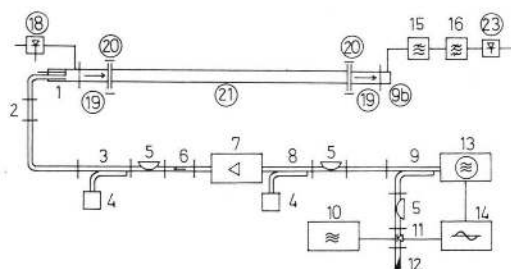
Fig. 2. Changes of the MWFT spectrometer X-band for double resonance experiments. Compare Fig. 1 [6]. Numbers in circles refer to Fig. 1 [6]. 1 Tunable waveguide to coax transition X-band with inserted R-band waveguide (26.4—40 GHz); 2 Transition K- to R-band; 3 Directional coupler 30 dB; 4 Power meter; 5 Attenuator; 6 Waveguide isolator; 7 TWT-amplifier K-band, Hughes 1077 H, 1 W nominal; 8 Directional coupler 20 dB; 9 Directional coupler 10 dB; 10 Frequency standard, Rhode und Schwarz, XUC; 11 Mixer; 12 Termination; 13 Backward wave oscillator, Hewlett Packard 8690 B with 8696 A; 14 Synchronizer, Schomandl FDS 30; 15 Low pass filter, cut off 14 GHz, K & L FLR-14, rejection 20 dB at 15.4 GHz, insertion loss 0.5 dB, VSWR 2:1; 16 Band pass filter, 8—12 GHz, Filtronics F 10021, rejection > 60 dB for 14 to 18 GHz, insertion loss 0.75 dB, VSWR 1.5:1.
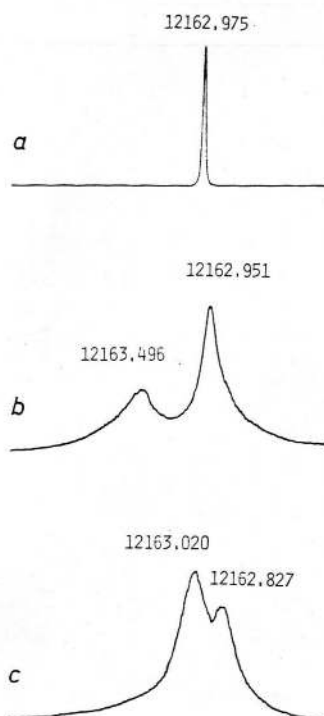
Reprint requests to Prof. Dr. H. Dreizler, Institut für Physikalische Chemie, Olshausenstr. 40—60, D-2300 Kiel.

12162,975

a

12162,951

12163,496

b

12163,020

12162,827

c

Fig. 3. A range of 2.5 MHz out of a 5 MHz scan of the rotational spectrum of OCS, line $J = 1 - 0$ sample interval 50 ns, 1024 data points extended to 4096 by zeros, spectral point distance 5 kHz, signals normalized, frequencies in MHz. a) 500000 averaging cycles, without pump radiation, 0.3 mtorr, $-3\,°C$; b) 1250000 averaging cycles, pump frequency at 24325.501 MHz, 1.8 W at cell entrance, 0.3 mtorr, $-3\,°C$; c) 750000 averaging cycles, pump frequency at 24326.001 MHz, 1.8 W, 0.3 mtorr, $-30\,°C$.

12162,937

12163,035

a

12163,028   12162,930
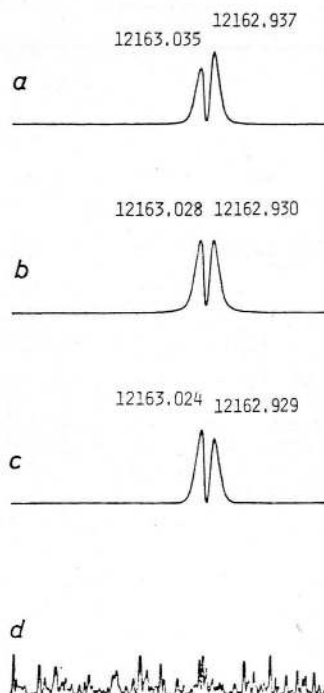
b

12163,024   12162,929

c

d

Fig. 4. Adjustment of the pump frequency (general conditions see Fig. 3) 500000 averaging cycles, 0.3 mtorr, $-59\,°C$, 50 mW at cell entrance. a) pump frequency at 24325.920 MHz; b) pump frequency at 24325.927 MHz; c) pump frequency at 24325.930 MHz; d) 250000 averaging cycles, pump frequency at 24325.901 MHz, 1 W at cell entrance, no substance.

steady-state double resonance experiments. However, the experimental conditions are somewhat different. In MWFT spectroscopy a transient emission following a strong polarizing $\pi/2$-pulse is observed. For further details see the following section.

It may be pointed out that the high resolution of MWFT spectroscopy is very useful for resolving the doublet. Using the symmetry of the doublet we were able to adjust the pump frequency to ± 1 kHz for the transition $J = 2 - 1$ of $^{16}O^{12}C^{32}S$ to 24325.927 MHz. A frequency of 24325.930(20) MHz was reported [9].

3. Theory

A sufficient model to describe the experimental findings given above is that of a three level system with the energy levels $E_a < E_b < E_c$ and the two dipole-allowed transitions between E_a and E_b (sig-

nal transition) and between E_b and E_c (pump transition). The following theoretical treatment is based on the three-level Bloch equations formalism, which has been derived earlier by Feuillade et al. [10]. In contrast to the normal description of steady-state double resonance experiments [11] (assuming high pump and low probe microwave power), transient solutions of the Bloch equations will be considered here to describe the behaviour of the system after a high power signal pulse excitation in the presence of a high power pump radiation.

For our experimental setup the microwave radiation is given by a superposition of pump and signal microwave radiation, plane polarized along the same direction (parallel fields)

$$\varepsilon = 2\,\varepsilon_p \cos \omega_p t + 2\,\varepsilon_s \cos \omega_s t, \qquad (1)$$

where ε_p and ε_s denote the electric field amplitude of the pump and signal radiation with angular frequencies ω_p and ω_s respectively. With (1) and inclusion of intermolecular interaction (relaxation)

11865,662

a

11865,778   11865,547

b

11865,744   11865,580

c

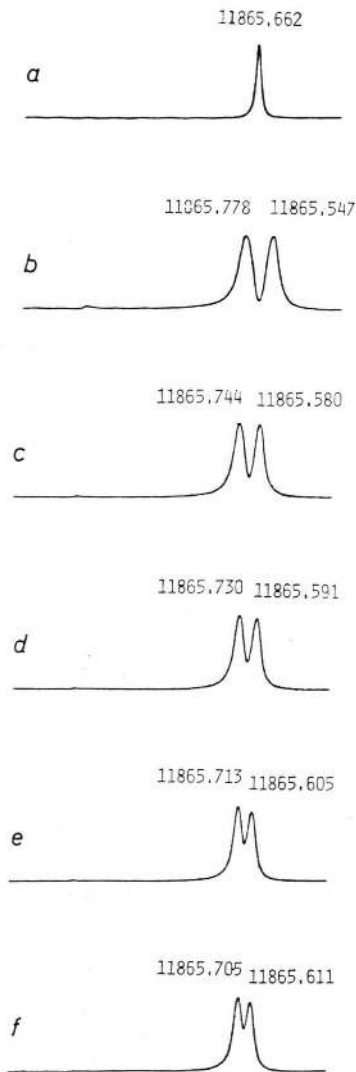11865,730   11865,591

d

11865,713   11865,605

e

11865,705   11865,611

f

Fig. 5. Pump power variation (conditions see Fig. 3) line $J = 1 - 0$ of $^{16}O^{12}C^{34}S$, 250000 averaging cycles, pump frequency at 23731.302 MHz, 3 mtorr, $-59\,°C$; pump power at cell entrance: a) 0 mW; b) 20 mW; c) 10 mW; d) 5 mW; e) 2 mW; f) 1 mW.

under the impact approximation, "three-level Bloch equations" have been derived by considering the equation of motion of the density matrix for the three-level system [10]. The time dependent behaviour of the variables describing the ensemble of three-level systems is then given by a set of coupled differential equations

$$\dot{U}_s = -\Delta\omega_s V_s + (x_p/2) V - (1/T_2^{ab}) U_s,$$
$$\dot{V}_s = \Delta\omega_s U_s - x_s W_s$$
$$\qquad - (x_p/2) U - (1/T_2^{ab}) V_s,$$

11865,705   11865,611

a

11865,711   11865,604

b

Fig. 6. Gas pressure variation (conditions see Fig. 3) line $J = 1 - 0$ of $^{16}O^{12}C^{34}S$, 250000 averaging cycles, pump frequency at 23731.302 MHz, pump power 1 mW at cell entrance, $-59\,°C$: a) 3 mtorr; b) 0.85 mtorr.

11409,708

a

11409,823   11409,596

b
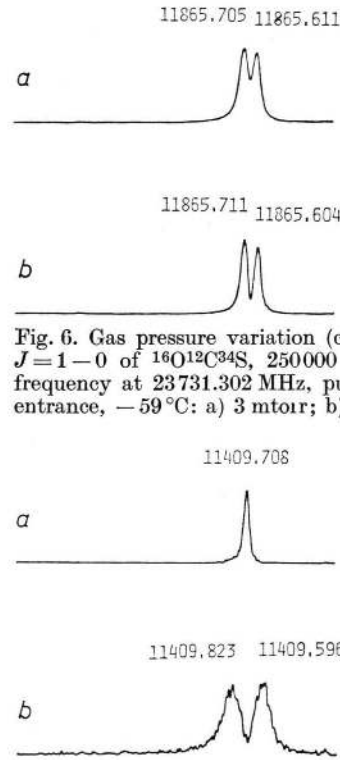
Fig. 7. Double resonance signal of $^{18}O^{12}C^{32}S$, line $J = 1 - 0$ (conditions see Figure 3). 750000 averaging cycles: a) without pump; b) pump frequency at 22819.404 MHz, pump power 20 mW at cell entrance; 3 mtorr; $-59\,°C$.

$$\dot{W}_s = x_s V_s - (x_p/2) V_p$$
$$\qquad - \gamma_y (W_s - W_s^0) - \gamma_z (W_p - W_p^0),$$
$$\dot{U}_p = -\Delta\omega_p V_p - (x_s/2) V - (1/T_2^{bc}) U_p,$$
$$\dot{V}_p = \Delta\omega_p U_p - x_p W_p - (x_s/2) U$$
$$\qquad - (1/T_2^{bc}) V_p,$$
$$\dot{W}_p = x_p V_p - (x_s/2) V_s - \gamma_x (W_p - W_p^0)$$
$$\qquad - \gamma_w (W_s - W_s^0),$$
$$\dot{U} = -\Delta\omega V - (x_s/2) V_p + (x_p/2) V_s$$
$$\qquad - (1/T_2^{ac}) U,$$
$$\dot{V} = \Delta\omega U + (x_s/2) U_p - (x_p/2) U_s$$
$$\qquad - (1/T_2^{ac}) V. \qquad (2a-h)$$

The variables in (2) are related to the elements of the density matrix $\tilde{\varrho}_{ij}$ ($i, j \in \{a, b, c\}$) in the interaction representation as follows.

$$W_s = \tilde{\varrho}_{aa} - \tilde{\varrho}_{bb}, \qquad (3a)$$
$$W_p = \tilde{\varrho}_{bb} - \tilde{\varrho}_{cc}, \qquad (3b)$$

the differences of occupation probabilities between the energy levels of signal and pump transition with

thermal equilibrium values W_s^0 and W_p^0 respectively, and

$$U_s = \tilde{\varrho}_{ab} + \tilde{\varrho}_{ba},$$
$$V_s = i(\tilde{\varrho}_{ba} - \tilde{\varrho}_{ab}),$$
$$U_p = \tilde{\varrho}_{bc} + \tilde{\varrho}_{cb},$$
$$V_p = i(\tilde{\varrho}_{cb} - \tilde{\varrho}_{bc}),$$
$$U = \tilde{\varrho}_{ac} + \tilde{\varrho}_{ca},$$
$$V = i(\tilde{\varrho}_{ca} - \tilde{\varrho}_{ac}), \tag{3c—h}$$

corresponding to a superposition of states for the energy level pairs (E_a, E_b), (E_b, E_c) and (E_a, E_c) respectively. The quantities $U_s(U_p)$ and $V_s(V_p)$ are proportional to the in- and out-of-phase component of the macroscopic polarisation with respect to the external signal (pump) microwave radiation [12], in contrast to U and V which do not correspond to a dipole polarization as the transition dipole matrix element μ_{ac} is assumed to be zero. The other symbols used in (2) are

$$\Delta\omega_s = (E_b - E_a)/\hbar - \omega_s,$$
$$\Delta\omega_p = (E_c - E_b)/\hbar - \omega_p,$$
$$\Delta\omega = \Delta\omega_s + \Delta\omega_p \tag{4a—c}$$

the deviations of the incident radiations from resonance, and

$$x_s = (2\,\mu_{ab}/\hbar)\,\varepsilon_s,$$
$$x_p = (2\,\mu_{bc}/\hbar)\,\varepsilon_p, \tag{4d—e}$$

the Rabi frequencies of signal and pump transition with the dipole matrix elements μ_{ab} and μ_{bc} respectively. To allow for collisional relaxation a set of relaxation parameters for the different elements of the density matrix is introduced into the equations where γ_x, γ_y, γ_z and γ_w concern the relaxation of population (see [10] for definition), and T_2^{ab}, T_2^{bc} and T_2^{ac} are the relaxation times for the superposition of the indicated pairs of levels.

We now proceed and discuss the solutions of (2) as applied to the Fourier transform double resonance experiment described in this paper. According to the experimental procedure the pump microwave radiation is assumed to continuously irradiate the sample gas. The time interval between the signal microwave pulses of duration t_1 is considered to be long with respect to the relaxation times so that it is sufficient to describe the dynamical behaviour of the system by a single pulse excitation. Identi-

fying the start of the signal microwave pulse by $t = 0$ we then have

$$\varepsilon_p \neq 0, \quad \varepsilon_s = 0 \quad \text{for} \quad t \leq 0, \tag{5a}$$
$$\text{(period A)}$$

$$\varepsilon_p \neq 0, \quad \varepsilon_s \neq 0 \quad \text{for} \quad 0 \leq t \leq t_1, \tag{5b}$$
$$\text{(period B)}$$

$$\varepsilon_p \neq 0, \quad \varepsilon_s = 0 \quad \text{for} \quad t \geq t_1. \tag{5c}$$
$$\text{(period C)}$$

To obtain solutions of (2) for the different periods of time, both signal and pump microwave radiation have been assumed to be resonant with the pump and signal transition respectively, giving with (4a—c)

$$\Delta\omega_p = 0, \quad \Delta\omega_s = 0, \quad \Delta\omega = 0. \tag{6a—c}$$

For further simplification some approximations have been made with respect to the relaxation parameters in (2). Firstly, identical coherence decay times ($T_2^{ab} = T_2^{bc} = T_2^{ac}$) have been assumed as was found experimentally for the considered system [13], [14], and [15]. Secondly, cross-relaxation between the variables W_s and W_p representing population differences may be neglected with respect to T_1-relaxation of W_p and W_s itself [10] ($\gamma_w, \gamma_z \ll \gamma_x, \gamma_y$) which is assumed to be described by identical T_1-relaxation times [16] ($\gamma_x = \gamma_y$). Finally, by using the experimental findings of a rather small difference between T_1- and T_2-relaxation times for OCS two level systems [13—15], [16], we may approximate

$$\alpha = 1/T_2^{ij} = \gamma_x = \gamma_y \quad (ij = ab, bc, ac). \tag{7}$$

Although this approximation does not hold rigorously, the result obtained with it presents the most important features of the solutions under consideration.

With the approximations given above, the solutions of (2) are found straightforwardly for the different periods of time. To obtain the initial conditions at the time $t = 0$, we may use the steady-state solutions of (2) for period A (no signal microwave for times $t < 0$ which are long with respect to the relaxation times), giving with (5a), (6) and (7)

$$U_s(0) = V_s(0) = U_p(0) = U(0) = V(0) = 0,$$
$$V_p(0) = -\alpha x_p W_p^0/(\alpha^2 + x_p^2),$$
$$W_p(0) = \alpha^2 W_p^0/(\alpha^2 + x_p^2),$$
$$W_s(0) = W_s^0 + x_p^2 W_p^0/(\alpha^2 + x_p^2). \tag{8a—d}$$

For sufficiently high pump power, $x_p \gg \alpha$, we have

$$V_p(0) \approx 0, \quad W_p(0) \approx 0,$$
$$W_s(0) \approx W_s^0 + W_p^0/2, \qquad (9\,a\text{—}c)$$

i.e. saturation of the pump transition.

For period B ($0 \leqq t \leqq t_1$) we may neglect the collisional damping terms in (2) for a signal pulse duration which is short with respect to the relaxation times ($t_1 \ll 1/\alpha$). We then obtain with the initial conditions (8), (9) at $t = 0$ the following solutions for $0 \leqq t \leqq t_1$

$$U_s(t) = 0,$$
$$V_s(t) = -(x_s/8\Omega^3)\, W_s(0)$$
$$\cdot \{2\,x_p^2 \sin \Omega t + x_s^2 \sin 2\,\Omega t\},$$
$$W_s(t) = (1/8\Omega^4)\, W_s(0)$$
$$\cdot \{x_p^2 x_s^2 \cos \Omega t + (x_p^2 x_s^2/4 + x_s^4/2)$$
$$\cdot \cos 2\,\Omega t + x_p^4/2 - x_p^2 x_s^2/4\},$$
$$U_p(t) = 0,$$
$$V_p(t) = -(x_p x_s^2/8\Omega^3)\, W_s(0) \qquad (10)$$
$$\cdot \{2 \sin \Omega t - \sin 2\,\Omega t\},$$
$$W_p(t) = (x_s^2/8\Omega^4)\, W_s(0)$$
$$\cdot \{x_p^2 \cos \Omega t - (x_p^2/2 + x_s^2/4) \cos 2\,\Omega t$$
$$- x_p^2/2 + x_s^2/4\},$$
$$U(t) = (x_p x_s/8\Omega^4)\, W_s(0)$$
$$\cdot \{(x_p^2 - x_s^2) \cos \Omega t + (x_s^2/2) \cos 2\,\Omega t$$
$$+ x_s^2/2 - x_p^2\},$$
$$V(t) = 0, \quad \text{where} \quad \Omega^2 = (x_p^2 + x_s^2)/4.$$

It may be noted that the transient double resonance solutions (10) for the time dependencies of the polarization components in quadrature to the external MW fields ($\sim V_s$ and $\sim V_p$) and of the population differences ($\sim W_s$ and $\sim W_p$) are more complicated than for the single resonance two-level case. In particular, no simple condition for optimum polarization of the sample gas (such as a $\pi/2$-pulse) may be formulated for the double resonance case. In addition to polarization and population difference, a nonzero coherence between the levels E_a and E_c ($\sim U$) is created which may be ascribed to a transient two-photon double resonance effect.

At the time $t = t_1$ the signal microwave radiation is switched off and transient solutions of (2) for $t \geqq t_1$ (period C) may be obtained for $\varepsilon_s = 0$ and the initial conditions (10) at $t = t_1$. We are interested here only in the solutions for U_s and V_s which are related to the observable quantities in our experi-

ments (see below), given by

$$U_s(t') = 0, \qquad (11\,a)$$
$$V_s(t') = \exp(-\alpha t') \{V_s(t_1) \cos(x_p/2)\,t' \qquad (11\,b)$$
$$- U(t_1) \sin(x_p/2)\,t'\},$$

where $t' = t - t_1$.

To obtain the polarization P of the sample gas which may be observed in the transient and steady-state regime, we used the equation of definition for P

$$P = N \operatorname{Tr}(\mu \varrho), \qquad (12)$$

where N is the number density of molecules, ϱ the density matrix and μ the matrix of the dipole moment operator. Using the real-valuedness of the transition dipole matrix elements, we then obtain, using the transformation of ϱ into the interaction representation [17], and (3 a—d)

$$P(t) = N\mu_{ab}\, U_s(t) \cos \omega_s t - N\mu_{ab}\, V_s(t) \sin \omega_s t$$
$$+ N\mu_{bc}\, U_p(t) \cos \omega_p t$$
$$- N\mu_{bc}\, V_p(t) \sin \omega_p t. \qquad (13)$$

In our experimental arrangement, microwave radiation with frequency components close to ω_p is blocked from reaching the detection system (see Fig. 2) and therefore not observed. Consequently only the first two terms in (13) have to be considered further (slowly varying amplitude functions assumed). The detected microwave field which is emitted by the molecular sample gas at times $t \geqq t_1$ is then proportional to the polarization [18]

$$P(t') = N\mu_{ab} \{U_s(t') \cos \omega_s t'$$
$$- V_s(t') \sin \omega_s t'\} \qquad (14)$$

which may be rewritten with (11)

$$P(t') = -(N\mu_{ab}/2) \exp(-\alpha t')$$
$$\cdot \{V_s(t_1)\,(\sin(\omega_s + x_p/2)\,t'$$
$$+ \sin(\omega_s - x_p/2)\,t')$$
$$+ U(t_1)\,(\cos(\omega_s + x_p/2)\,t'$$
$$- \cos(\omega_s - x_p/2)\,t')\}. \qquad (15)$$

Equation (15) represents the superposition of two decaying signals oscillating at the frequencies $\omega_s + x_p/2$ and $\omega_s - x_p/2$ respectively. With Fourier transformation from the time to the frequency domain we then have a superposition of two Lorentzian lines with center peaks at $\omega_{1/2} = \omega_s \pm x_p/2$ as observed in our experiments. According to (4e) the line splitting is pump power dependent and given by

$$\omega_1 - \omega_2 = (2\mu_{bc}/\hbar)\,\varepsilon_p. \qquad (16)$$

This result is in agreement with the familiar coherence splitting of double resonance lines which have been predicted earlier [11] in a description of steady-state double resonance experiments under the condition of high pump power and low probe microwave power.

Conclusion

In view of the many possible modifications and applications we hope that the Fourier transform double resonance can be developed to an as useful tool as double resonance already is in normal microwave spectroscopy.

[1] A. Battaglia, A. Gozzini, and E. Polacco, Nuovo Cim. **14**, 1076 (1959).
[2] T. Yajima and K. Shimoda, J. Phys. Soc. Japan **15**, 1968 (1960).
[3] T. Yajima, J. Phys. Soc. Japan **16**, 1709 (1961).
[4] A. P. Cox, G. W. Flynn, and E. B. Wilson, J. Chem. Phys. **42**, 3094 (1965).
[5] G. Bestmann, H. Dreizler, H. Mäder, and U. Andresen, Z. Naturforsch. **35a**, 392 (1980).
[6] G. Bestmann and H. Dreizler, Z. Naturforsch. **37a**, 58 (1982).
[7] G. Bestmann and H. Dreizler, Z. Naturforsch. **37a**, 615 (1982).
[8] G. Bestmann, H. Dreizler, E. Fliege, and W. Stahl, to be published.
[9] G. Maki, J. Phys. Ref. Data **3**, 221 (1974).
[10] C. Feuillade, J. G. Baker, and C. Bottcher, Chem. Phys. Lett. **40**, 121 (1976).
[11] A. Javan, Phys. Rev. **107**, 1579 (1957).
[12] W. K. Liu and R. A. Marcus, J. Chem. Phys. **63**, 272 (1975).
[13] S. L. Coy, J. Chem. Phys. **63**, 5145 (1975).
[14] W. E. Hoke, D. R. Bauer, J. Ekkers, and W. H. Flygare, J. Chem. Phys. **64**, 5276 (1976).
[15] H. Bomsdorf and H. Dreizler, Z. Naturforsch. **36a**, 473 (1981).
[16] H. Mäder, Z. Naturforsch. **34a**, 1170 (1979).
[17] W. Schrepp and H. Mäder, Chem. Phys. **63**, 113 (1981).
[18] T. G. Schmalz and W. H. Flygare, Laser and Coherence Spectroscopy, p. 125ff., Plenum Press, New York 1978.