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MINFLUX nanoscopy delivers multicolor nanometer 3D-resolution in (living) cells

Klaus C. Gwosch^{1*}, Jasmin K. Pape^{1*}, Francisco Balzarotti^{1*}, Philipp Hoess², Jan Ellenberg², Jonas Ries², Stefan W. Hell^{1,3#}

1 The ultimate goal of biological superresolution fluorescence microscopy is to provide three-
2 dimensional resolution at the size scale of a fluorescent marker. Here, we show that, by
3 localizing individual switchable fluorophores with a probing doughnut-shaped excitation
4 beam, MINFLUX nanoscopy provides 1–3 nanometer resolution in fixed and living cells. This
5 progress has been facilitated by approaching each fluorophore iteratively with the probing
6 doughnut minimum, making the resolution essentially uniform and isotropic over scalable
7 fields of view. MINFLUX imaging of nuclear pore complexes of a mammalian cell shows that
8 this true nanometer scale resolution is obtained in three dimensions and in two color
9 channels. Relying on fewer detected photons than popular camera-based localization,
10 MINFLUX nanoscopy is poised to open a new chapter in the imaging of protein complexes
11 and distributions in fixed and living cells.

12 While STED^{1, 2} and PALM/STORM^{3, 4} fluorescence microscopy (nanoscopy) can theoretically achieve a
13 resolution at the size of a single fluorophore, in practice they are typically limited to about 20 nm.
14 Owing to a synergistic combination of the specific strengths of these key superresolution concepts,
15 the recently introduced MINFLUX nanoscopy⁵ can attain a spatial resolution of about the size of a
16 molecule, conceptually without constraints from any wavelength or numerical aperture. In MINFLUX
17 imaging, the fluorophores are switched individually like in PALM/STORM, whereas the localization is
18 accomplished by using a movable excitation beam featuring an intensity minimum, such as a
19 doughnut. The minimum ideally is a zero intensity point that is targetable like a probe⁶.

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20 Concomitantly, it serves as a reference coordinate for the unknown position of the fluorophore in
21 the sample, because the closer the minimum is to the fluorophore, the weaker is the emitted
22 fluorescence per unit excitation power. If the excitation zero and the fluorophore coincided in space,
23 no emission would occur. Yet the emitter's position would be known in that case, since it must
24 coincide with the well-controlled position of the zero. For the same reason, the smaller the
25 mismatch between the two coordinates is, the fewer emitted photons are required to measure the
26 emitter's position. Hence, approaching a fluorophore with a position-probing excitation minimum
27 shifts the burden of requiring many photons for localization from the feeble fluorescence to the
28 inherently bright beam of molecular excitation, giving MINFLUX a fundamental edge over popular
29 camera-based localization.

30 While the resolution and speed advantage of MINFLUX nanoscopy have been well documented^{5,7},
31 here we demonstrate that it also allows for three-dimensional (3D) imaging and simultaneous two-
32 color registration, which are critically important for most life science applications. Moreover, we
33 show that, in conjunction with photoactivatable fluorescent proteins, MINFLUX uniquely affords true
34 nanometer resolution in living cells. The first realization of MINFLUX utilized static distances of the
35 intensity zero to the fluorophore, which limited the imaged field to sub-100 nm extents⁵. In this
36 work, we dynamically zoom-in on each fluorophore position, which not only renders the localizations
37 essentially uniform and isotropic, but also facilitates the recording of extended areas and volumes.

38 Results

39 Basics on iterative fluorophore targeting with a local excitation minimum

40 The power of zooming-in on each fluorophore is readily illustrated for a fluorophore located at x_M ,
41 within the interval $x_0 < x_M < x_1$ of size $L = |x_1 - x_0|$. When probing with an intensity zero that is
42 flanked by a quadratic intensity profile, it is sufficient to measure the number of fluorescence
43 photons $n(x_0)$ and $n(x_1)$ with the zero placed at the interval endpoints⁵. With $n(x_0)$ and $n(x_1)$
44 following Poissonian statistics, the minimum standard deviation of the localization, i.e. the Cramer-
45 Rao bound (CRB) within the region L , is given by $\sigma \geq \frac{L}{4\sqrt{N}}$, with $N = n(x_0) + n(x_1)$. Contrasting the
46 linear dependence on the interval size L with the inverse square-root dependence on the number of
47 detected photons N shows that reducing L , i.e. zooming-in on the molecule, outperforms the wait
48 for more photons.

49 This also becomes evident when approaching x_M in successive steps with stepwise reduced L_k , such
50 that L_k is chosen to match three times σ_{k-1} , i.e. the uncertainty of the previous step. Thus, after k
51 iterations we obtain a total of $N_t = k \cdot N$ detected photons and a CRB of

$$\sigma_k \geq \frac{L_k}{4\sqrt{N}} = \frac{3 \cdot \sigma_{k-1}}{4\sqrt{N}} = \frac{3 \cdot L_{k-1}}{(4\sqrt{N})^2} = \dots = \frac{3^{k-1}}{(4\sqrt{N})^k} L_1 \propto k^{k/2} \frac{L_1}{N_t^{k/2}},$$

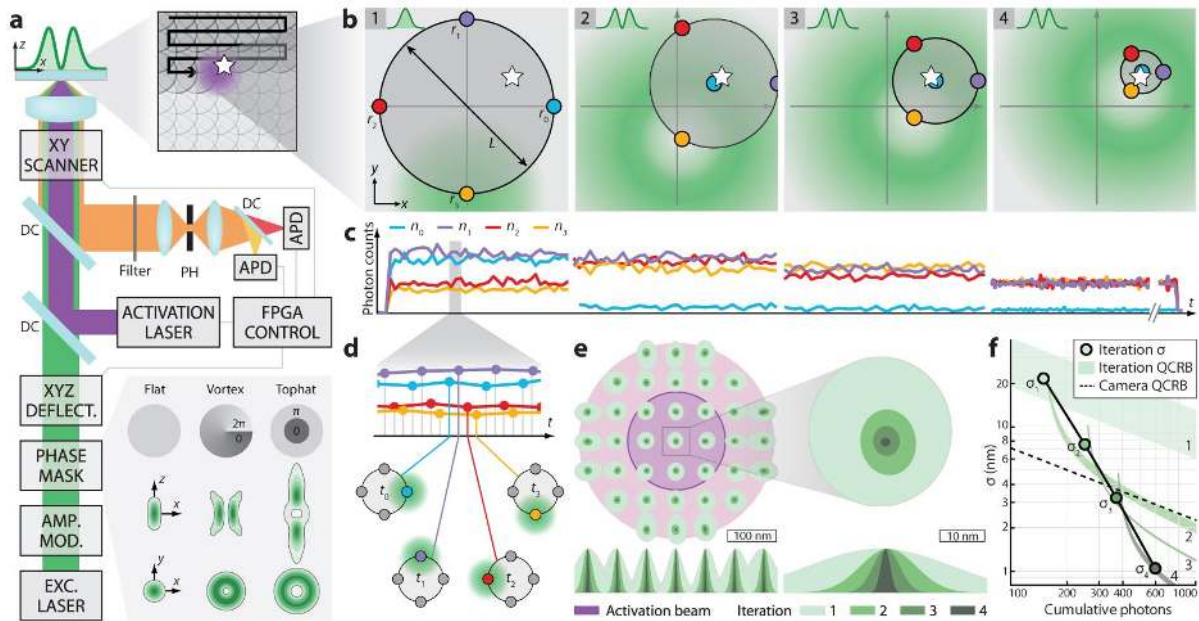
underscoring once more that it is more effective to increase the number k of iterations than that of the photons N per iteration. Already four steps ($k=4$) yield $\sigma_4 \propto 1/N_t^2$, i.e. an inverse quadratic as opposed to an inverse square-root dependence on the total number of detected photons. More iterations yield an even higher order, accounting for the fact that the detected photons become more informative the closer the probing positions are to the molecule. In practice, this procedure is only limited by the background photons, which compromise the information on where to place the zero next.

Realizing iterative MINFLUX and scalable fields of view

Our setup is a beam-scanning confocal fluorescence microscope featuring a visible excitation beam that can enter the objective lens with a flat wavefront, hence being regularly focused, as well as amplitude- and phase-modulated to form a doughnut in the focal region (Fig. 1a, Optical setup, Fig. S1). The excitation beam is co-aligned with a UV beam for activating individual emitters in a ~ 400 nm diameter region in the sample (Fig. 1a,e). Micrometer-range positioning or scanning of these co-aligned beams is performed with a piezo-based mirror, whereas fast microsecond nanometer-range targeting is carried out using an electro-optic beam deflector.

Like all fluorescence nanoscopy concepts, MINFLUX nanoscopy relies on a fluorescence on-off transition for the separation of neighboring emitters⁶. We transiently activated a single fluorophore within the ~ 400 nm diameter activation region, localized it by MINFLUX and finally ensured that it went back to a lasting off-state. The same procedure was applied to the next fluorophore until a representative number of molecules was registered. For each localization, we targeted the zero to a set of coordinates around the anticipated fluorophore position, referred to as the targeted coordinate pattern (TCP). Forming a circle in the focal plane, the diameter L of the TCP is a measure of how well the TCP is zoomed-in on the molecule (Fig. 1b). In the first iteration, the beam was focused regularly, while in the succeeding steps it was modulated to form a 2D- or a 3D-doughnut, depending on whether we localized the fluorophore just in the focal plane (x,y) or in the sample volume (x,y,z). In each iteration, we calculated the newly anticipated fluorophore position based on collecting a defined number of photons in the fluorescence traces (Fig. 1c) produced at each of the targeted coordinates. The four-point TCP used for 2D-localization rendered the position estimator simple and unambiguous⁵. In the next iteration, the TCP was centered on the new position and the diameter L decreased according to the new precision estimate, thus bringing the zeros closer to the molecule. To compensate for the associated reduction in excitation intensity and to maintain the fluorescence flux, we increased the excitation power in each step. The smallest L in the last iteration

85 step, meaning how well we could zoom-in on the fluorophore in practice, was determined by the
 86 concomitantly decreasing signal-to-background ratio.



87 **Fig. 1 | Iterative MINFLUX setup and localization.** **a**, Setup. An excitation beam (green) is amplitude- and phase-
 88 modulated (bottom right inset: flat (regular focus), vortex (2D-doughnut), tophat (3D-doughnut)), electro-
 89 optically deflected in x, y, z , overlapped with a photo-activation beam (purple) and focused into the sample, after
 90 passing a piezo-actuated mirror for coarse x, y -scanning (top right inset, white star: activated molecule position).
 91 Fluorescence is de-scanned, deflected by a dichroic mirror (DC), filtered by a confocal pinhole (PH), split in two
 92 spectral ranges by another DC and detected by photon-counting avalanche photodiodes (APDs), all FPGA-board
 93 controlled. **b**, Iterative xy -localization by targeting the beam to four designated coordinates constituting the
 94 TCP (blue, purple, red, yellow and beam on yellow position in green). Step 1: regular focus, steps 2–4:
 95 2D-doughnut. The TCP is re-centered and zoomed-in on the fluorophore (white star) in steps 2–4. **c**, Typical
 96 fluorescence counts for each iteration with the color indicating the targeted coordinate. **d**, Representation of
 97 the interleaved TCP measurement. **e**, Convergence of iterative localizations for molecules within the activation
 98 area (purple: 200 nm FWHM, 50% single molecule activation probability; pink: 2·FWHM, 95% activation
 99 probability). The covariance of each iteration (green shades) is represented as an ellipse of $e^{-1/2}$ level.
 100 **f**, Progression of the spatially averaged localization precision σ_1 – σ_4 for each iteration (green dots) with the
 101 corresponding CRBs (green shades) and the CRB for camera-based localization (dashed line). Conditions for (e–
 102 f): Photons: $N_1=150$ $N_2=100$, $N_3=120$ and $N_4=230$; total $N_t=600$. TCPs: $L_{1,flat}=300$ nm, $L_{2,vortex}=150$ nm,
 103 $L_{3,vortex}=90$ nm, $L_{4,vortex}=40$ nm.

104

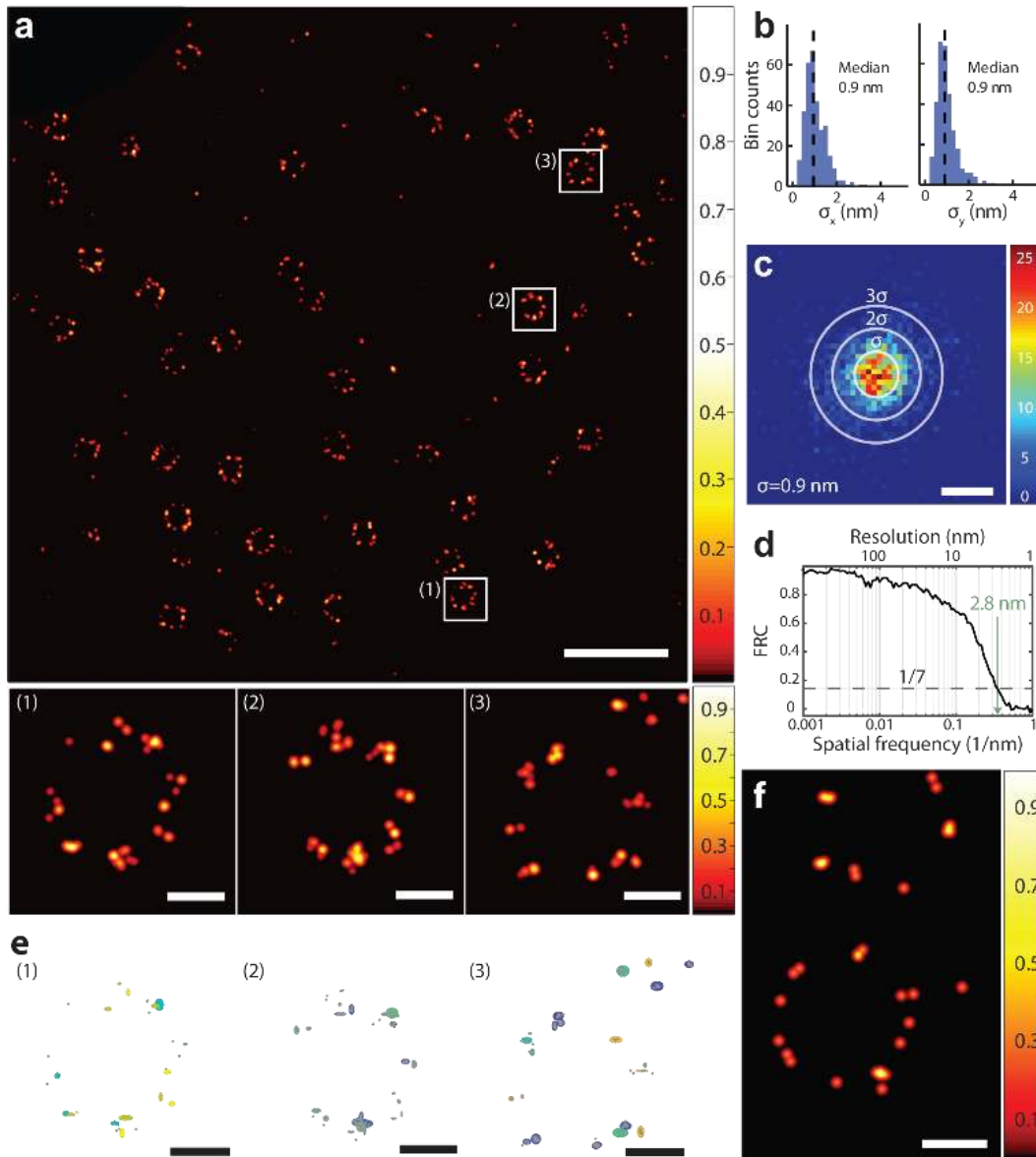
105 We first simulated the procedure by randomly generating multinomial photon counts for different
 106 molecule positions, applying four iteration steps, and zero background (see Simulations and
 107 optimization of iterative strategy). On average, our iteration procedure (Fig. 1b) achieved a
 108 localization precision of $\sigma_{1D} \sim 1$ nm with only $N_t=600$ photons (Fig. 1e). In contrast to static (non-
 109 iterative) MINFLUX localization⁵, the precision obtained here was largely isotropic and independent
 110 of the emitter position within the activation area (Fig. 1e). In our simulation, we selected different
 111 photon numbers in each step according to the required precision, with the last step featuring the
 112 largest photon number. The precision still largely followed the anticipated $1/N_t^2$ behavior. Starting

113 with a lower photon efficiency, our iterative MINFLUX scheme surpassed the quantum CRB (QCRB)⁸
114 of lateral precision for camera-based localization with $N_t \sim 330$ photons (Fig. 1f).

115 For imaging, we defined a state machine on a field-programmable gate array (FPGA) board that
116 recognized single activated fluorophores and localized them iteratively (see Experiment control
117 software). Individual emitters were identified by segmenting their emission trace and their position
118 was obtained by maximum-likelihood estimation (see Data analysis). First, we imaged Nup96, a
119 protein of the nuclear pore complex (NPC), labelled with the organic fluorophore Alexa Fluor 647
120 using SNAP-tag in fixed mammalian (U-2 OS) cells⁹ (Fig. 2a, see U-2 OS NUP96-SNAP/mMaple).
121 Images of several micrometers in size were acquired using MINFLUX with five iteration steps
122 ($N_1=100$, $N_2=100$, $N_3=150$, $N_4=300$, $N_5 \sim 2000$ and $L_{1,flat}=300$ nm, $L_{2,flat}=300$ nm, $L_{3,vortex}=150$ nm,
123 $L_{4,vortex}=100$ nm, $L_{5,vortex}=50$ nm). Based on these parameters and the background, we expected a
124 localization precision below 1 nm in standard deviation. The overall fluorescence rate of typically
125 ~ 50 kHz allowed a complete localization within ~ 40 ms. To ensure a single active fluorophore per
126 activation area, 0.5–5 μ W of UV light was applied in pulses of 5 ms until a fluorescent molecule
127 appeared. After activation and registration of a single Alexa Fluor 647 molecule, the iterative scheme
128 took around 10 ms to reach the final iteration. The photon traces and the TCP re-adjustment were
129 constantly monitored during recording. Altogether, the acquisition of a single NPC required about 1–
130 2 minutes. Our experiments demonstrated that iterative MINFLUX clearly resolved the eightfold
131 symmetry of Nup96 in single NPCs (Fig. 2a), distributed along a ring of 107 nm in diameter^{9,10}. In
132 fact, the localizations typically formed eight clusters of roughly 2–4 localization subclusters,
133 displayed as the sum of Gaussian distributions, one for each localization (see Image rendering),
134 revealing, most likely, individual Nup96 proteins through their individual fluorescent markers. This
135 molecular scale resolution is obtained in various images of the nuclear envelope, demonstrating that
136 iterative MINFLUX nanoscopy can accommodate fields of any size and shape, just like any other
137 scanning confocal microscope.

138 To provide quantitative resolution measures, we applied three different criteria (Fig. 2b–d, see
139 Performance metrics). First, we calculated the standard deviation σ for four and more localizations
140 per fluorophore, where each localization utilized ~ 2000 photons of the last iteration, extracted from
141 over 300 single fluorophore events. The resulting distribution of σ featured a median of ~ 1 nm (Fig.
142 2b). Another resolution assessment was gained by subtracting the mean localized position of an
143 emission train from all of its single localizations (Fig. 2c). Assuming a Gaussian distribution, we
144 obtained a precision error $\sigma_{1D}=0.9$ nm. In the third approach, we calculated the Fourier ring
145 correlation (FRC) curve^{11,12} of the localization data (Fig. 2d), which better captures the influence of
146 setup instabilities on the effective resolution. The threshold value of 1/7 gave $\Delta_{FRC} \sim 3$ nm as a

147 resolution estimate. Simulating localizations at the expected Nup96 positions with a fixed
148 localization standard deviation revealed that this experimental FRC resolution Δ_{FRC} corresponds to a
149 localization precision of roughly 1 nm. To represent the obtained precision in an actual image, we
150 displayed individual localizations with covariance ellipses of 3σ for each emission (Fig. 2e).



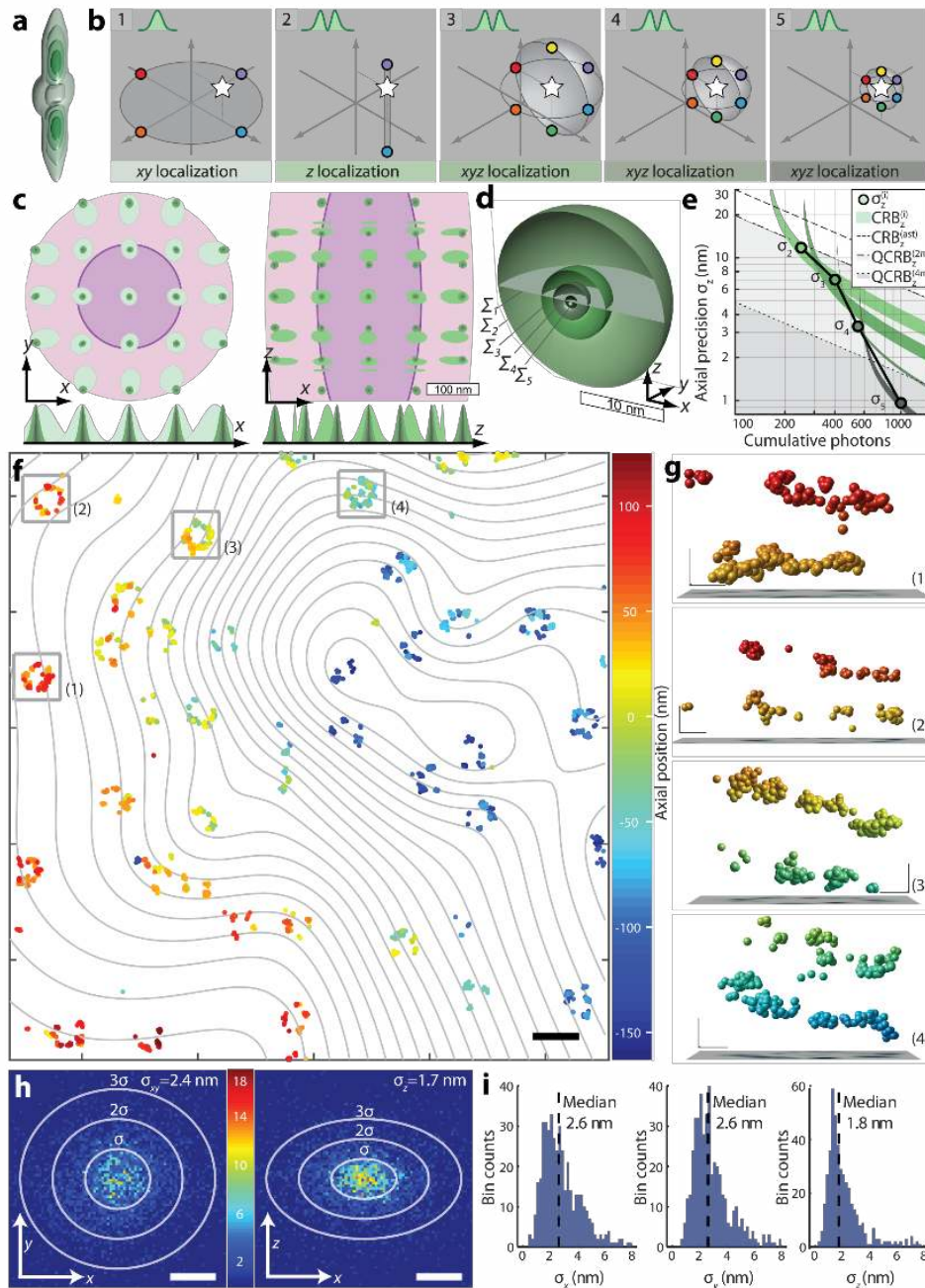
151 **Fig. 2 | MINFLUX nanoscopy in fixed and living cells.** **a**, MINFLUX nanoscopy of a U-2 OS cell expressing
152 Nup96-SNAP labelled with Alexa Fluor 647. Single molecule fluorescence events were split into bunches of
153 2000 photons, yielding localizations that are filtered and displayed according to the methods sections Event
154 filtering, Image rendering and Fig. S2. Zoomed-in excerpts (below) show single nuclear pores, with each dot
155 highlighting groups of localizations representing individual proteins through their fluorescent labels. **b**,
156 Histograms of standard deviations of localizations from single molecules in x and y . Only molecules providing
157 >4 localizations per trace were considered. **c**, Histogram of the distance of a localization to the mean position
158 of a single emitter. The ellipses are displayed with major axes of 2σ , 4σ and 6σ length respectively, with σ
159 being determined in a 1D Gaussian fit. **d**, Fourier ring correlation curve for the image in (a). **e**, Renditions of
160 insets of (a) with 3σ ellipses for each molecule. **f**, MINFLUX image of nuclear pores in living U-2 OS cell
161 expressing NUP96-mMaple; average of ~ 1600 detected photons per localization. Scale bars: 500 nm (a), 50 nm
162 (a (inlets), e, f), 2 nm (c).

163 Since Alexa Fluor 647 imposes a number of restrictions on the sample preparation, most notably
164 incompatibility with living cells, we next demonstrated that MINFLUX nanoscopy is viable with
165 photoactivatable fluorescent proteins. We resolved the eightfold symmetry of Nup96 tagged with
166 the photo-convertible protein mMaple (see U-2 OS Nup96-SNAP/mMaple and Tab. S1) in both fixed
167 and living cells (Fig. 2f). In particular, the live-cell recording proves that imaging of protein complexes
168 in the interior of living cells is possible with nanometer resolution.

169 3D MINFLUX imaging with isotropic resolution

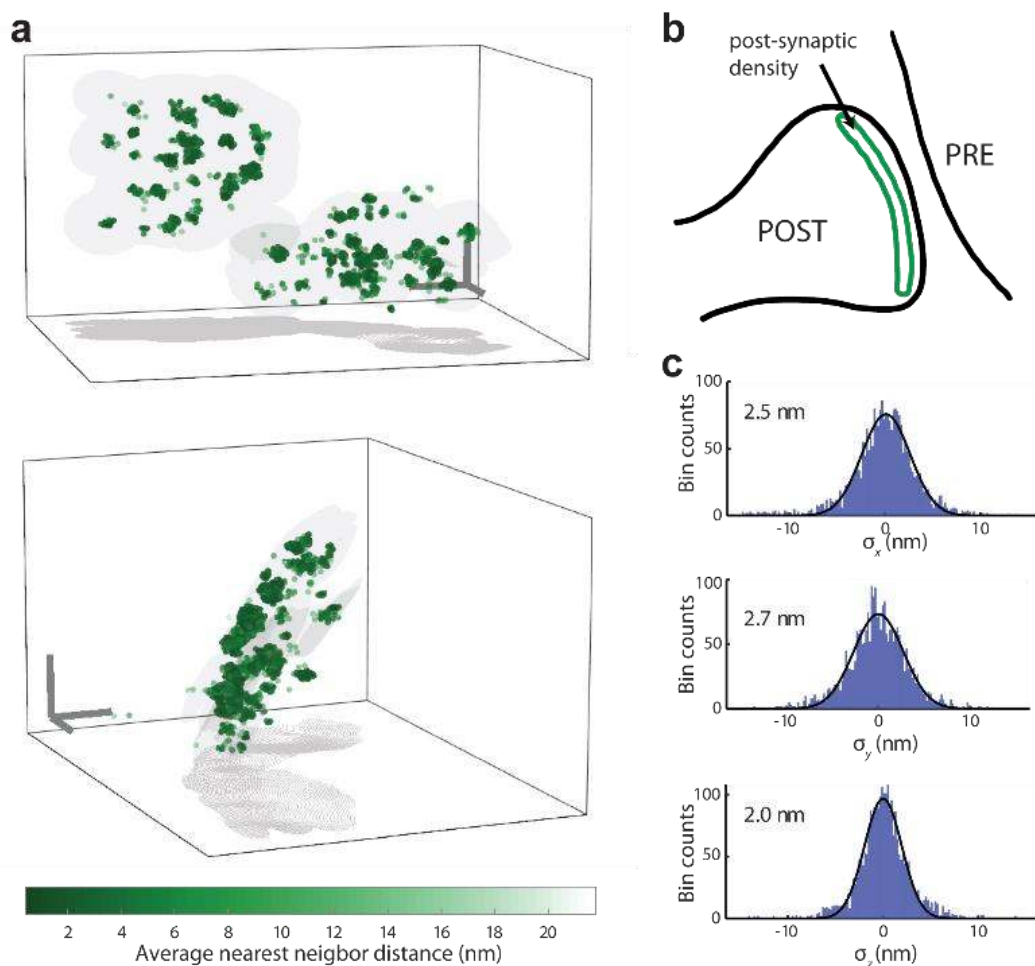
170 Dissection of macromolecular complexes calls for 3D-resolution and hence for usage of the 3D-
171 doughnut (Fig. 3a). In our 3D localization algorithm, we probe the molecule position with three
172 different TCPs. First, the xy -position is probed with a regularly focused beam, so that the central z -
173 axis of the 3D-doughnut is positioned as closely as possible to the fluorophore. Next, the 3D-
174 doughnut is targeted in two positions above and below the anticipated fluorophore position. Last,
175 three coordinate pairs on the x -, y - and z -axis and also the center coordinate of this arrangement
176 are addressed, resulting in a 3D position estimate. A simulation of this 3D-MINFLUX algorithm (Fig.
177 3b) showed that 1000 detected photons were sufficient to cover a ~ 400 nm diameter volume with a
178 largely homogenous and isotropic 3D-precision of ~ 1 nm (Fig. 3c-d). Again, the increase in precision
179 with the total number of detected photons proved to be steeper than $1/\sqrt{N_t}$ (Fig. 3e). Comparing
180 the result with the QCRB for the precision of camera-based localization shows that 3D-MINFLUX can
181 outperform all camera-based approaches, including multiple-objective lens arrangements.

182 In our setup, the axial position of the 3D-doughnut is controlled with an electrically tunable lens,
183 allowing to refocus within 50 μ s. Imaging Nup96-SNAP-Alexa Fluor 647 (Fig. 3f, Fig. S3, Sample
184 preparation, Video S1), 3D-MINFLUX now discerns the cyto- and nucleoplasmic layers of Nup96 in
185 single pore complexes (Fig. 3g). As the cell lies flat on a cover slip, these layers are typically parallel
186 to the focal plane and ~ 50 nm apart in the z -direction⁹. 3D-MINFLUX also recovered the curvature of
187 the nuclear envelope extending ~ 300 nm in depth within the acquired region (Fig. 3f). The
188 localizations featured one-dimensional (1D) standard deviations $\sigma_{xy}=2.4$ nm and $\sigma_z=1.7$ nm (Fig. 3h).
189 Localizations from single events exhibited median standard deviations $\sigma_{xy}=2.6$ nm and $\sigma_z=1.8$ nm
190 respectively (Fig. 3i). Note that the refractive index mismatch at the glass-water interface causes a
191 slight difference between the xy and z localization precision, since L_z of the TCP is slightly
192 compressed due to this mismatch¹³, increasing the MINFLUX localization precision accordingly (see
193 Optical setup).



194 **Fig. 3 | Iterative 3D MINFLUX localization yields isotropic nanometric precision.** **a**, 3D-doughnut with selected
 195 isointensity surfaces. **b**, Iterations. Step 1: *xy*-localization with regularly focused beam (intensity profile top
 196 left). Step 2: *z*-localization with 3D-doughnut. Steps 3–5: *x*-, *y*-, and *z*-localization with 3D-doughnut, shrinking
 197 the TCP each time. **c**, Simulation of localization convergence in *xy* (left) and *xz* (right) for molecules within the
 198 activation region (purple: 200 nm FWHM_{*xy*} and 600 nm FWHM_{*z*} with 29% activation probability, pink: 2 FWHM
 199 with 86% activation probability). The covariance of each iteration (green shades) is represented as an ellipse at
 200 level $e^{-1/2}$. **d**, 3D representation of the step-wise localization precision in the central region in **c**. **e**, Progression
 201 of average *z*-precision in **c** (dots), showing the Cramér-Rao bound (CRB) for camera-based astigmatic
 202 localization, the Quantum CRB (QCRB) for a camera localization in a 2π and 4π -arrangement (dashed lines)
 203 along with MINFLUX CRB in each iteration (green shades). Steps for **c**-**e**: Photons $N_1=150$, $N_2=100$, $N_3=150$,
 204 $N_4=150$, and $N_5=450$; total $N_t=1000$. Step 1: regular focus with $L_{1,flat}=300$ nm. Steps 3–5: 3D-doughnut with
 205 $L_{2,tophat}=400$ nm, $L_{3,tophat}=150$ nm, $L_{4,tophat}=90$ nm, $L_{5,tophat}=40$ nm. **f**, MINFLUX image of nuclear pore
 206 complexes of a fixed cell (Nup96-SNAP-Alexa Fluor 647); *z*-coordinate is color-coded. Contour lines indicate
 207 the nuclear envelope. **g**, *z*-sections of single nuclear pores in **f**. **h**, Localization precision for 3D imaging in *xy*
 208 (left) and *xz* (right). **i**, Histograms of *x*, *y*, *z* standard deviation. Scale bars 200 nm (**f**), 20 nm (**g**), 5 nm (**h**).

209 Next, we imaged the protein PSD-95 in dissected hippocampal neuron cultures from transgenic mice
210 expressing a fusion protein of the Halo-Tag enzyme connected to the protein C-terminus¹⁴ (Fig. 4a–b,
211 Fig. S4, Hippocampal cultured neurons (PSD-95) and Video S2). PSD-95 putatively plays a key role in
212 anchoring and re-arranging glutamate receptors in the post-synaptic membrane^{15, 16}. 3D-MINFLUX
213 nanoscopy suggests that PSD-95 is arranged along a slightly curved surface of 100–400 nm side
214 length. The spots of a high localization density exhibit a standard deviation of ~4–6 nm, with the
215 localization precision being estimated to $\sigma_{1D} \sim 2\text{--}3$ nm (Fig. 4c). The average distance between
216 nearest-neighbor clusters is ~40 nm. While superresolution techniques were repeatedly used to
217 elucidate the organization of post-synaptic proteins¹⁷, virtually all superresolution studies were
218 carried out in 2D. Owing to its isotropic resolution, 3D MINFLUX now opens up entirely new
219 possibilities for studying synaptic protein organization.



220 **Fig. 4 | MINFLUX imaging of the post-synaptic protein PSD-95 with 3D-resolution of ~2–3 nm.** Sample:
221 hippocampal neurons from transgenic mice expressing PSD-95-Halo conjugated to Alexa Fluor 647 after
222 fixation. **a**, 3D-MINFLUX image with color indicating the 3D density of molecular localizations. PSD-95 appears
223 in clusters distributed on a curved surface. **b**, Sketch of PSD-95 occurrence at the postsynaptic site.
224 **c**, Histograms of distances of localizations to the mean molecule position in x , y and z , revealing an isotropic
225 3D localization precision of the individual fluorophores of 2.0–2.7 nm. Scale bar: 100 nm (a).

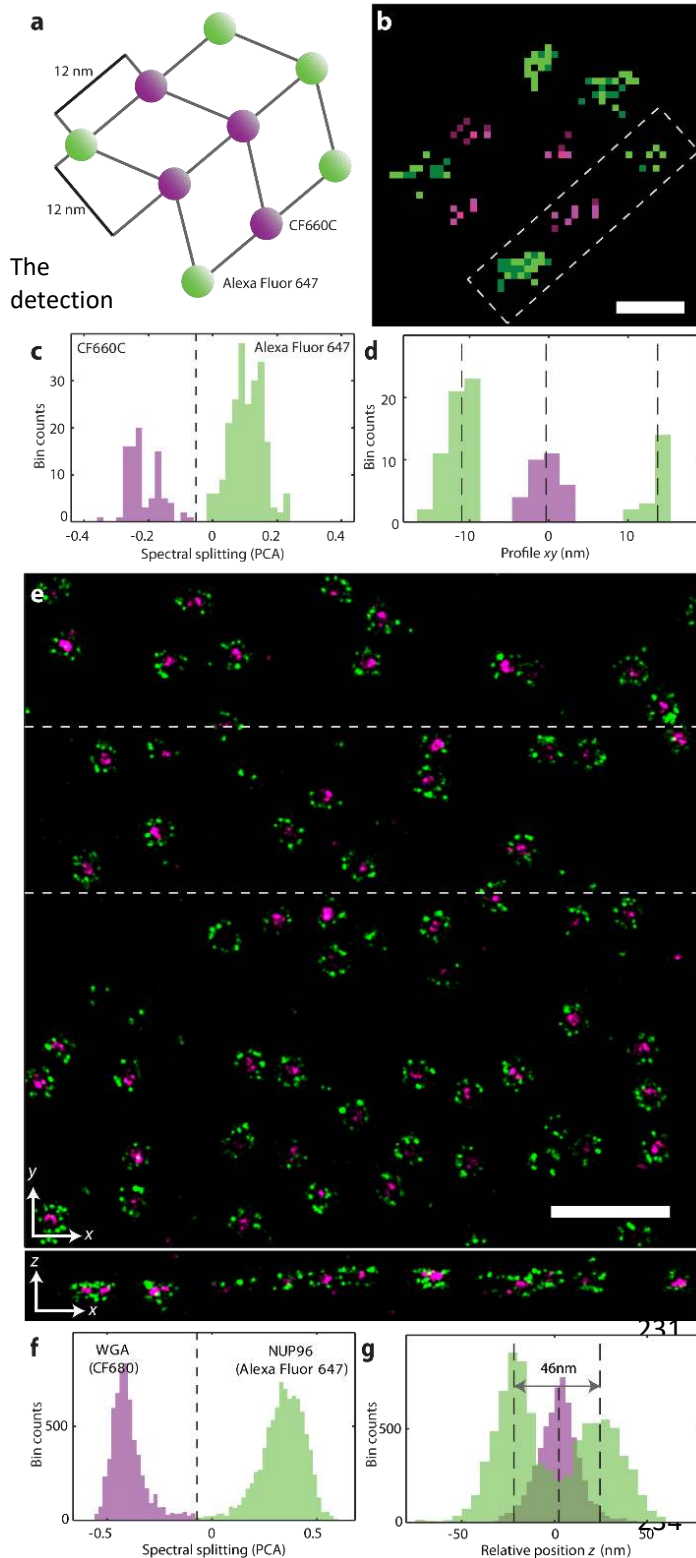


Fig. 5 | Two-color MINFLUX nanoscopy in 2D and 3D. **a**, Scheme of a DNA origami labelled with Alexa Fluor 647 and CF660C with ~ 12 nm intermolecular distances. **b**, Histogram of the localizations acquired with 2D MINFLUX. Alexa Fluor 647 is shown in green, CF660C in magenta. **c**, Spectral separation of the two fluorophore species. abscissa is the principal component of the probability on the spectral channel with $\lambda < 685$ nm for all iterations. The spectral separation (dashed line) minimizes overlap between the two species. **d**, Histogram of localizations along the box in **b**. The positions are well resolved with a distance of the outer fluorophores of ~ 25 nm. **e**, Two-color image of U-2 OS cell expressing NUP96-SNAP. The SNAP-tag was labelled with Alexa Fluor 647. Additionally, wheat germ agglutinin (WGA) conjugated to CF680 stained the center of the NPC. **f**, Spectral distribution of the two fluorophore species with choice of color separation (dashed line). **g**, z-distribution of the two fluorophore species. After considering the nuclear envelope shape (see Fig. 3f) for each nuclear pore position, a distance of 46 nm is found between the cytoplasmic and nucleoplasmic layers of Nup96; WGA is aggregated at the pore center. Scale bars 10 nm (**b**) and 500 nm (**e**).

235

236 Multicolor MINFLUX imaging

237 Fluorophore species sharing the same excitation wavelength but having measurable differences in

238 their emission spectra, such as Alexa Fluor 647, CF660C, and CF680¹⁸ can be separated by spectral

239 classification. Hence, we split the fluorescence at 685 nm into two spectral fractions using a dichroic

240 mirror, and detected both fractions with photon counting detectors. While localization was
241 performed adding up the photons from both detectors, comparing the counts of each spectral
242 fraction enabled fluorophore classification (see Multicolor classification). The classification was
243 refined using a principal component analysis on the spectral fractions from all MINFLUX iterations
244 and selecting a classification threshold based on the distribution of the first principal component.
245 We first tested two-color 2D MINFLUX imaging on a DNA origami labelled with Alexa Fluor 647 and
246 CF660C molecules, arranged at distances of ~ 12 nm (Fig. 5a, Fig. S4, see DNA origami). MINFLUX
247 nanoscopy correctly recovered the labelling sites (Fig. 5b,d) and distinguished the two fluorophore
248 species without overlap (Fig. 5c). Moreover, chromatic distortions between the two color channels
249 are excluded on principle grounds, since the localization is performed by one and the same
250 excitation beam. This is in contrast to camera-based localization, where nanometer multicolor co-
251 localization is affected by chromatic aberrations of the optical system.

252 Finally, we acquired two-color 3D-images of the nuclear pores in the U-2 OS cell by labeling the
253 nuclear pore center with wheat germ agglutinin (WGA) conjugated to CF680 in addition to the
254 Nup96-SNAP Alexa Fluor 647 decoration¹⁹. We indeed observed the CF680 residing inside the Nup96
255 octamer both laterally and axially (Fig. 5e,g, Video S3). Although the emitters featured a broader
256 spectral distribution in the cell than in the origami, we could classify the labels with high fidelity (Fig.
257 5f). We also quantified the distribution of both emitter species along the z-axis by taking into
258 account the nuclear envelope 3D curvature, which was found through a spline interpolation of the
259 pore positions (see Nuclear pore complexes). Thus, we recovered a distance of ~ 46 nm between the
260 Nup96 layers with the WGA distribution centered in between (Fig. 5g), underscoring once more the
261 3D capability of MINFLUX nanoscopy.

262 Discussion and Conclusion

263 We have shown that MINFLUX nanoscopy provides nanometer resolution (1–3 nm in standard
264 deviation) in three dimensions, on arbitrary fields of views, in living cells, and using multiple color
265 channels. Yet, the full potential of this method has not been reached. Ongoing and future
266 developments will cut down the current recording time of tens of minutes per 500 localizations. This
267 can be achieved by optimizing the activation procedure, registering more than just one molecule per
268 localization, and minimizing the fluorophore-to-zero average distance. The latter should be possible
269 through background reduction by time-gated detection and multiphoton excitation. Note that the
270 excitation powers used in this work are on the order of 20–60 μW , so that the intensities are
271 comparable to those in biological confocal microscopy, where the power is confined to an area three
272 times smaller than that of a doughnut beam.

273 Since MINFLUX utilizes a scanning read-out, the recording time of MINFLUX nanoscopy inevitably
274 scales with the imaged area or volume. However, an advantage of scanning is that one can adapt the
275 activation rate to the local fluorophore concentration to save time. Another avenue is to parallelize
276 the scanning process using sets of doughnuts or standing waves. Furthermore, one can utilize
277 different on-off switching processes, such as the transient binding of fluorescent molecules like in
278 PAINT²⁰ or DNA-PAINT²¹. Note that for a PAINT-like sample preparation, the speed and precision
279 advantages provided by MINFLUX persist.

280 With lens-based fluorescence microscopy having finally reached true nanometer resolution, it is
281 important for life scientists to bear in mind that fluorescence microscopes map nothing but the
282 fluorophores; once they have fulfilled this task, they have accomplished their mission. Hence, any
283 conclusion going beyond that, especially at sub-10 nm length scales, has to take the size and
284 orientation of the fluorophore label into account, making the labeling method ever more crucial.
285 MINFLUX offers more flexibility in this regard because, by requiring fewer detected photons than
286 camera-based localization, a larger range of fluorophores and labeling procedures should be viable.
287 For this fundamental reason, as well as its 3D imaging performance, MINFLUX nanoscopy is bound to
288 be a cornerstone, if not the vanguard, of nanometer scale fluorescence microscopy in the years to
289 come.

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298 [Author Contributions](#)

299 K.C.G., J.K.P. and F.B. designed and built hardware, programmed software, performed experiments
300 and data analysis with input from S.W.H. K.C.G, J.K.P and P.H. prepared samples. P.H. and J.R.
301 proposed the Nup96 cell line as resolution test sample. J.E. made the Nup96 cell line. F.B. carried out
302 theoretical analysis of MINFLUX with K.C.G and co-supervised the project. S.W.H. supervised the
303 project and is responsible for its conceptual thrust. K.C.G., J.K.P., F.B. and S.W.H. wrote the
304 manuscript.

305 [Competing interests](#)

306 S.W.H. is a co-founder of the company Abberior Instruments GmbH, which commercializes super-
307 resolution microscopy systems. S.W.H, K.C.G and F.B hold patents on principles, embodiments and
308 procedures of MINFLUX.

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356 Materials and methods

357 Experimental setup

358 Optical setup

359 We used an optical setup (Fig. S1) based on a previously described microscope^{1,2}, having three
360 different illumination modalities provided through separate optical paths: (i) widefield excitation
361 (488 nm, 560 nm, 642 nm), (ii) regularly focused excitation (560 nm or 642 nm) or focused activation
362 (405 nm) and (iii) phase-modulated excitation (560 nm or 642 nm) leading to a 2D- or 3D-doughnut
363 in the focal region. For all excitation beams, we employed an acousto-optic tunable filter (AOTF) for
364 slow power modulation and wavelength selection. Switching between the regularly focused and 2D-
365 /3D-doughnut excitation was performed with electro-optical modulators (EOM). To laterally position
366 the MINFLUX beams within the TCP and to approach the molecules iteratively, we employed electro-
367 optical deflectors (EOD); they were differentially driven with two pairs of identical amplifiers. To
368 image larger fields of views, we scanned the focused activation beam and the TCP across the sample
369 using a piezo-based tip-tilt mirror. An electrooptically actuated varifocal lens (VFL) positioned the
370 3D-doughnut beam axially. The sample was translated using a manual as well as a piezo-driven
371 sample stage. 2D- and 3D-doughnut generation was accomplished with a spatial light modulator
372 (SLM). Applying an achromatic $\lambda/4$ retarder plate for circular beam polarization helped minimizing
373 the intensity at the doughnut minimum. To ensure a deep minimum, we measured the aberrated
374 wavefront using a pupil segmentation based scheme³. A 1.4 numerical aperture oil immersion lens
375 focused the excitation light into the sample and collected the fluorescence light. The tip-tilt mirror
376 de-scanned the emitted light, which subsequently passed through a quad-band dichroic mirror.
377 Electrically driven flip-mirrors allowed the selection between (i) a detection path for acquiring a
378 fluorescence overview image of the sample with an EMCCD camera and selecting a region of
379 interest; (ii) a large-area detector for measuring the point spread function (PSF) of the excitation
380 beam; (iii) a confocal pinhole (multi-mode-fiber) of 500 nm (sample units) for MINFLUX fluorescence
381 acquisitions.

382 An active stabilization system ensured nanometer stability of the sample. For lateral stabilization, we
383 imaged micrometer-sized scattering gold nanorods onto a camera using a spectrally filtered white-
384 light laser source (~950–1000 nm). An infrared laser beam (905 nm) illuminated the sample in total
385 internal reflection mode, so that the axial position was accessible using another camera. A PID
386 controller commanded the piezo-stage to compensate the movements. Since MINFLUX relies on the
387 precise knowledge of the shape and position of the excitation beam, we mapped the applied
388 scanner voltage to a physical position in the sample by calibrating the xy -scanners for both

389 excitation lines¹. Additionally, we calibrated the axial beam displacements (induced by the VFL) by
390 measuring the axial position of the excitation PSF for different input voltages. We also took the
391 refractive index mismatch between the coverglass and the sample into account. To this end, we
392 performed a 3D-MINFLUX measurement to determine the position of two Alexa Fluor 647 molecules
393 on a DNA nanoruler (GATTA-STED 3D 90R – custom, GATTAquant GmbH, Hiltoltstein, Germany).
394 We scaled the estimated z position to match the expected inter-molecule distance. We confirmed
395 the scaling factor of 0.7 in simulations⁴ and applied it in post-processing to correct all estimated z
396 localizations. Fluorescent microspheres (see Fluorescent microsphere sample) were used to re-
397 examine the alignment of the microscope on a daily basis. To this end, we verified the coalignment
398 of the activation beam, the regularly focused and the doughnut-shaped excitation beam. Moreover,
399 we adjusted the confocal detection to coincide with the excitation volume. We measured the PSF of
400 the excitation beams by scanning an area or volume around the doughnut minimum with the EOD or
401 the tip-tilt mirror (xy) and the sample stage (z) respectively.

402 [Experiment control software](#)

403 Similarly to our previously published works^{1,2} we used custom programs written in LabView
404 (National Instruments, Austin, TX, USA) for control of the experimental setup and data acquisition.
405 We implemented the control of hardware components using data acquisition boards (NI PCIe-6353),
406 an FPGA board (NI USB-7856R), and through direct communication with devices (e.g. USB or serial
407 port). The software package consisted of four types of programs: iterative MINFLUX FPGA core,
408 iterative MINFLUX PC host, system stabilization, and auxiliary device control. The iterative MINFLUX
409 FPGA core served the following purposes: control of beam deflectors and amplitude modulators;
410 selection of beam shape and type (activation/excitation); photon registration via avalanche photo
411 diodes (APDs); online data processing; and position scanning for image acquisition. This program
412 performed all tasks and processes described in Data acquisition. The MINFLUX FPGA core and PC
413 host communicated via USB, delivering control commands from the host PC to the FPGA and
414 streaming the acquired data and state information from the FPGA to the host PC.

415 [Live position estimators](#)

416 [Position estimation for doughnut exposures](#)

417 For 1D, 2D and 3D position estimation with a doughnut-shaped excitation beam, we used a modified
418 version of the previously developed modified least mean square estimator (mLMSE)¹. For position
419 estimation in three dimensions, we performed a natural extension of the estimator resulting in the
420 same expression as eq. (S51) in our reference¹ but with the beam positions \vec{r}_{b_i} now being three-
421 dimensional vectors:

$$\hat{r}_{\text{mLMS}}^{(k)}(\hat{p}, \hat{\beta}) = -\frac{1}{1 - \frac{L^2 \log(2)}{\text{FWHM}^2}} \left(\sum_{j=0}^k \beta_j \hat{p}_0^j \right) \sum_{i=0}^{m-1} \hat{p}_i \cdot \bar{r}_{b_i}$$

422 where m is the number of exposures (targeted coordinate positions), k is the estimator order,
423 $\{\beta_j\}$ are the estimator parameters, L is the beam separation, FWHM is the full width at half
424 maximum of a regularly focused beam (FWHM = 360 nm in this work), and $\{\hat{p}_i = n_i/N\}$ are the
425 measured relative photons counts for the different exposures. We used an estimator order of $k = 1$.
426 The estimator parameters β_j were optimized numerically using a typical measured shape of the 2D
427 doughnut or an ideal quadratic function approximating the minimum of the 3D doughnut and
428 assuming a typical experimental signal-to-background ratio. For optimization of $\{\beta_j\}$ we used the
429 Matlab function *fmincon* to minimize the mean bias of the mLMS position estimate in a circular
430 region (for 2D) or spherical volume (for 3D) with a diameter of $0.8 L$, with the beam separation L .
431 We used the obtained position estimator parameters for the live position estimation in the MINFLUX
432 FPGA core as well as for optimization of the iterative MINFLUX strategy.

434 Position estimation for regularly focused exposures

435 Position estimation using a regularly shaped excitation beam was performed using an estimator
436 derived from the previously published estimator for position estimation in 1D using a TCP with a
437 regularly focused beam and two exposures (see eq. (S40) in ¹). We modified the molecule position
438 estimator \hat{x}_m to take into account background signal. The estimator used in this work takes the form

$$\hat{x}_m^G(n_0, N) = \left(1 + \frac{1}{\text{SBR}} \right) \frac{\text{FWHM}^2}{8 \ln(2) L} [\ln(n_0) - \ln(N - n_0)],$$

440 where n_0 is the number of photons in the first exposure, N is the total number of detected photons,
441 L is the beam separation of the two probing positions, FWHM is the full width at half maximum of
442 the excitation beam (FWHM = 300 nm in this study) and SBR is the signal-to-background ratio. We
443 used this estimator for live position estimation in the MINFLUX FPGA core as well as for optimization
444 of the iterative MINFLUX strategy. The SBR was kept fixed for each measurement assuming a typical
445 value for the sample of study.

446 Simulations and optimization of iterative strategy

447 Different iterative MINFLUX schemes were investigated and optimized through numerical
448 simulations using Matlab (MathWorks, Natick, MA, USA). We simulated the complete iterative
449 localization scheme for a set of molecules within the volume covered by the activation beam
450 (360x360x360 nm), with the goal of finding the optimal number of iterations K , size of the TCP L_k
451 and number of photons to use N_k . The simulation replicated the live estimations performed by the

452 FPGA hardware, while the final localization was performed via the MLE, which is used in post-
 453 processing. By minimizing the average localization error for all simulated molecule positions, the
 454 optimal iterative parameters $\{K, L_k, N_k\}$ were found. The simulation used the following beam
 455 shapes:

Type	Function	Variables
Gaussian detection	$f(\vec{x}) = \frac{e\left(\frac{(x-x_0)^2}{2\sigma_{\text{DetXY}}^2}\right) \cdot e\left(\frac{(y-y_0)^2}{2\sigma_{\text{DetXY}}^2}\right) \cdot e\left(\frac{(z-z_0)^2}{2\sigma_{\text{DetZ}}^2}\right)}{(2\pi)^{3/2} \cdot \sigma_{\text{DetXY}}^2 \cdot \sigma_{\text{DetZ}}}$	$\sigma_{\text{DetXY}}: \frac{500 \text{ nm}}{2\sqrt{2\log(2)}}$ $\sigma_{\text{DetZ}}: \frac{1000 \text{ nm}}{2\sqrt{2\log(2)}}$
Focused excitation	$f(\vec{x}) = \frac{e\left(\frac{(x-x_b)^2}{2\sigma_{\text{GaussXY}}^2}\right) \cdot e\left(\frac{(y-y_b)^2}{2\sigma_{\text{GaussXY}}^2}\right) \cdot e\left(\frac{(z-z_b)^2}{2\sigma_{\text{GaussZ}}^2}\right)}{(2\pi)^{3/2} \cdot \sigma_{\text{GaussXY}}^2 \cdot \sigma_{\text{GaussZ}}}$	$\sigma_{\text{GaussXY}}: \frac{330 \text{ nm}}{2\sqrt{2\log(2)}}$ $\sigma_{\text{GaussZ}}: \frac{800 \text{ nm}}{2\sqrt{2\log(2)}}$
Doughnut 2D	$f(\vec{x}) = f_{\text{PSF2d}}(x - x_b, y - y_b) \cdot \frac{e\left(\frac{(z-z_b)^2}{2\sigma_z^2}\right)}{\sqrt{2\pi} \cdot \sigma_z}$	$\sigma_z: \frac{1000 \text{ nm}}{2\sqrt{2\log(2)}}$ $f_{\text{PSF2d}}: \text{experimental 2D PSF}$
Doughnut 3D	$f(\vec{x}) = (x - x_b)^2 + (y - y_b)^2 + (z - z_b)^2$	

456 Data acquisition

457 Before starting a MINFLUX measurement, we selected a region of interest and moved the sample to
 458 the imaging plane based on a widefield fluorescence acquisition. We defined scanning points in the
 459 selected region, located either on a rectangular grid or in a manually defined arrangement. Using a
 460 focused excitation beam with high intensity (100–200 μW entering the back focal plane of the
 461 objective lens), we transferred the fluorescent molecule population into a long-lived non-fluorescent
 462 state. We conditionally applied light of 405 nm wavelength (0.5–5 μW) to photo-activate single
 463 molecules. Subsequently, we probed the presence of an emitting fluorophore by illuminating with
 464 excitation light using the configuration defined for the first iteration (typically 0.1 ms minimal time
 465 until collecting 40–100 photons) and comparing the low-pass filtered photon count rate (filter
 466 constant 1–10 ms) to a pre-defined threshold (5–50 kHz). Upon detection of a fluorescent molecule,
 467 we did not return to the activation step and continued the iterative MINFLUX acquisition scheme.
 468 During the iterations, we applied excitation powers in the range of 20–60 μW in the backfocal plane
 469 comparable to confocal microscopy. The MINFLUX scheme ended (i) upon the photon count rate
 470 falling below a threshold pre-defined for each iteration, meaning the molecule turned off (ii) upon
 471 reaching a certain photon number in the last iteration. In case (i), activation light was applied. In

472 case (ii), we restarted the MINFLUX iterations. After a pre-defined time with no single molecule
473 events (0.3–20 s) or a certain amount of activation pulses (10000–30000 pulses corresponding to
474 50–150 ms of 405 nm light illumination), the tip-tilt mirror moved the illumination beams to the next
475 scan position. We selected the scan positions in a rectangular pattern with distances of 200–250 nm,
476 ensuring a homogenous activation of the whole scan area. As a result, regions covered in
477 neighboring scan positions were overlapping, so that a molecule between the scan positions could
478 be approached starting from any of the neighboring positions.

479 Data analysis

480 PSF evaluation

481 We measured the shape of the excitation point spread function (PSF) with samples of immobilized
482 fluorescent microspheres (FluoSpheres®, 0.02 µm, dark red fluorescent; Thermo Fischer Scientific Inc.,
483 Waltham, MA, USA). For measurements in two dimensions, data acquisition and processing of the
484 PSF followed a previously published protocol¹. For measurement in three dimensions, we assumed
485 the PSF to take the form $I(x, y, z) = a \cdot (x^2 + y^2 + z^2)$, with a denoting a constant.

486 Trace segmentation

487 In the photon count trace segments, we distinguished single molecule emissions from background
488 using a Hidden-Markov model¹. We only considered trace sections for which the MINFLUX
489 acquisition was running in its final iteration. We obtained a first estimate for the emission rates in
490 the Hidden Markov model by calculating the mean emission after artificially splitting the median
491 filtered photon counts at a manually chosen threshold in the range 1.1–3.6. We used a Poissonian
492 distribution with the obtained mean emission values as initial emission probabilities in the Hidden-
493 Markov model. Using the Matlab implementation of the Viterbi algorithm, we estimated the
494 emission states from a three-state Hidden Markov model (1: on, 2: off, 3: blinking) with the sampling
495 time $t_s=0.1$ ms, $t_{\text{off}}=0.1$ s, and $t_{\text{on}}=0.5$ s being the estimated on and off-times of the molecule and
496 $t_{\text{blink,on}}=1$ ms and $t_{\text{blink,off}}=0.1$ ms the estimated blinking on and off times. We applied the Viterbi
497 algorithm twice, using the same transition probability matrix, but applying the improved emission
498 rate distribution from the previous run. We merged successive emissions in states 1 or 3. We split
499 events at a pre-defined photon number of $N=2000$ to obtain several localizations per molecule for
500 an experimental assessment of the localization precision. We assigned a molecule identification
501 number to each localization assuming that emissions with several iteration rounds (no activation
502 applied in between) originated from the same molecule.

503 Position estimation

504 As previously reported, we used a maximum likelihood estimator implemented in a grid search
505 optimization algorithm to retrieve the molecule positions from the photon count traces ¹. For the
506 3D-MINFLUX scheme, we wrote the trivial extension of the p -functions to three dimensions using
507 the presented TCP. Unlike before, we could not obtain the background counts directly from the
508 measurement as the background depended on (i) the position in the scan and (ii) the position of the
509 iterative TCP in the confocal volume, so that the background varied even for successive events of the
510 same molecule. We circumvented this issue by estimating the signal-to-background ratio with the
511 molecule position in the maximum likelihood estimator.

512 Event filtering

513 During the iterative MINFLUX measurement, we chose a fixed threshold value to decide on the
514 presence of a molecule emission. This approach led to two types of false positives: (i) reaction to
515 background, as we chose a low threshold value to avoid missing faint emission events; and (ii)
516 reaction to thermally activated molecules outside the iterative MINFLUX region, which were still
517 detected, despite the live estimators not reaching them.

518 We applied three filters in post-processing to select true emission events only. These are the central
519 doughnut fraction p_0 , the estimated location of the molecule with respect to the center of the TCP
520 r_{rel} and the photon number in the last iteration N . We show the distribution of the filtering variables
521 together with the selected threshold values in figure Fig. S2–4 for all presented datasets.

522 Molecules far outside the TCP and background events are expected to produce equal mean counts in
523 all m exposures, delivering $p_0^{(b)} \sim 1/m$, with $p_0 = n_0 / \sum_{i=0}^{m-1} n_i$ describing the probability to detect a
524 photon in the central exposure. True emission events will yield $p_0 < 1/m$ when successfully
525 approaching the molecule in the iterations. The overlap of the two distributions becomes stronger
526 with decreasing SBR, so that a classification based on p_0 is not sufficient in a cellular context. We
527 achieved a better classification by using the distance of the estimated position with respect to the
528 center of the TCP in the last iteration $r_{\text{rel}} = (x_{\text{rel}}^2 + y_{\text{rel}}^2 + z_{\text{rel}}^2)^{1/2}$, a measure that does not directly
529 depend on the SBR. We note that further restricting both filter variables can improve the overall
530 localization precision at the expense of discarding valid localizations. For measurements with a
531 population of events with low photon number, we additionally applied a lower threshold on the
532 photon number N in the last iteration to avoid a bias in the position estimation.

533 Multicolor classification

534 For each localization, we obtained photon numbers for both spectral channels in all iterations. We
535 used the probability of detecting a photon in the blue-shifted spectral channel in the i -th iteration

$$536 \quad p_{\text{blue}}^{(i)} = \frac{N_{\text{blue}}^{(i)}}{N_{\text{blue}}^{(i)} + N_{\text{red}}^{(i)}}$$

537 as a measure of the spectral properties of the dye. In the last iteration, we obtained mean values of
538 0.2, 0.4 and 0.55 for CF680, CF660C and Alexa Fluor 647 respectively. Photons from all MINFLUX
539 iterations carry information about the spectral properties of the dye, but with different signal-to-
540 background ratio values. To reduce the classification error by using all available information, we
541 performed a principal component analysis based on $p_{\text{blue}}^{(i=0 \dots \max(\text{iter}))}$ and manually chose a splitting
542 threshold to classify the dye species based on the distribution of the first principal component.

543 Image rendering

544 In datasets with a low number of events per molecule, we replaced each localization with a Gaussian
545 distribution, summing up pixel entries for overlapping Gaussians. We normalized the image,
546 resulting in $0 \leq I_{ij} \leq 1$ with I_{ij} being the value of the ij th pixel. For images displaying a micrometer
547 sized image region (Fig. 2a, Fig. 5e), we chose a pixel size of 0.5 nm and a large width of the Gaussian
548 kernel ($\sigma=4$ nm) for visibility. For images displaying single or few nuclear pores (Fig. 2a, f) we chose
549 $\sigma=2$ nm and a pixel size of 0.2 nm. We used a non-linear color distribution to compensate for the
550 unequal number of events per fluorescent molecule. For the multicolor data (Fig. 5e), we
551 independently convolved the localization of each dye species with a Gaussian kernel and displayed
552 the normalized images as RGB images with $\alpha=7$ in the red channel and $\alpha=5$ in the green channel
553 using the components

$$554 \quad I_{ij}^{(\text{red})} = \alpha \cdot I_{ij}^{(\text{CF660C,CF680})}$$

$$555 \quad I_{ij}^{(\text{green})} = \alpha \cdot I_{ij}^{(\text{Alexa Fluor 647})}$$

$$556 \quad I_{ij}^{(\text{blue})} = 0.7 \cdot I_{ij}^{(\text{CF660C,CF680})}.$$

557 For the DNA origami image (Fig. 5b), we displayed a simple 2D histogram of the localization data
558 with 1 nm pixel size, with the RGB value for each pixel determined with $\alpha=0.5$. Where we displayed
559 localization data as scatter plots, the size of the scatter points/spheres was unrelated to the
560 estimated localization precision. An exception is Fig. 2e, where we displayed scatter points together
561 with an ellipse, with the principal axes lengths related to the localization precision.

562 Surface fitting

563 *Nuclear pore complexes*

564 To obtain a model of the nuclear envelope in the 3D measurements of nuclear pore complexes (Fig.
565 3f and Fig. 5e), we first determined the nuclear pore centers by clustering localization in the same
566 nuclear pore. We employed the Matlab implementation *linkage* to generate an agglomerative
567 hierarchical cluster tree using the median as a distance measure between clusters. We chose
568 clusters using Matlab's *cluster* function based on the manually determined number of clusters in the
569 data. Based on the mean position of all clusters in the dataset we approximated the shape of the
570 nuclear envelope based on thin-plate smoothing spline interpolation using a smoothing parameter
571 of 0.999 (Matlab function *tpaps*).

572 *PSD-95*

573 Localizations were assigned to two domains using a *kmeans* clustering algorithm. To determine the
574 average position of the volumes of high localization density within each domain, we employed the
575 Matlab implementation of the density-based clustering algorithm *dbscan* (epsilon=8 nm, minPts=10).
576 We determined a surface using the Matlab function *tpaps* with a smoothing parameter 0.996.

577 Performance metrics

578 *Localization precision based on clustering*

579 We assessed the localization precision in the acquired MINFLUX images based on a clustering of
580 localizations according to their molecule identification number (see Trace segmentation). This
581 included grouping localizations from single iteration cycles, obtained by splitting the photon
582 numbers in time, as well as grouping localizations from subsequent iterations that were triggered by
583 exceeding a pre-defined photon number in the last iteration. We filtered for molecules with more
584 than four localizations. We calculated the standard deviation of single clusters and obtained the
585 median standard deviation for all molecules (Fig. 2b, Fig. 3i). To achieve a more general assessment
586 (Fig. 2c, Fig. 3h, Fig. 4c), we subtracted the mean cluster position from all localizations and displayed
587 the obtained distances in 1D histograms for all three dimensions. We assumed a Gaussian
588 distribution of the distances to determine their spread in a fit. We note that the calculation of the
589 mean cluster position is biased for a low number of samples, which leads to a slight bias towards
590 lower values in the localization precision that we obtain.

591 *Fourier ring correlation*

592 We used a Fourier ring correlation (FRC) analysis to assess the resolution in the image independently
593 of any localization clustering. We randomly split the localizations in two groups and determined the
594 FRC curve directly from the localization coordinates as previously described in ⁵. We chose a

595 correlation threshold of 1/7 to determine the spatial frequency transition from signal-to-background
596 (Nieuwenhuizen et al. 2013). To reduce noise in the determination of the cut-off frequency, we
597 interpolated the data using the 'nearest' method of the Matlab function *interp1*.

598 Sample preparation

599 Sample mounting and imaging buffers

600 To stabilize the sample during the MINFLUX acquisition, we treated all coverslips with gold nanorods
601 (A12-25-980-CTAB-DIH-1-25, Nanopartz Inc., Loveland, CO, USA). We diluted the nanorods 1:3 in
602 single molecule clean phosphate-buffered saline (PBS, P4417 Sigma-Aldrich, St. Louis, MO, USA),
603 sonicated them for 5–10 min, and incubated the sample with the nanorod solution for 5–10 min at
604 room temperature. To avoid floating nanorods, we washed the sample 3–4 times in PBS after
605 removing the nanorod solution.

606 For MINFLUX imaging of samples labelled with Alexa Fluor 647, CF660C or CF680, we used a STORM
607 blinking buffer containing 0.4 mg/mL glucose oxidase (Sigma, G2133), 64 µg/mL catalase (Sigma
608 C100-50MG), 50 mM TRIS/HCl pH 8.0/8.5, 10 mM NaCl, 10–30 mM MEA (Cysteamine hydrochloride,
609 Sigma M6500) and 10% (w/v) glucose. When measuring DNA origami samples, we added 10 mM
610 MgCl₂ to the blinking buffer to avoid dehybridization of DNA strands. We imaged U-2 OS cells
611 endogenously tagged with mMaple in 50 mM Tris buffer (pH 8) in 95% D₂O to reduce the short time
612 blinking and increase the photon count of mMaple⁶. We sealed the samples with picodent twinsil®
613 speed 22 (picodent® Dental-Produktions- und Vertriebs-GmbH, Wipperfürth, Germany).

614 Fluorescent microsphere sample

615 We used samples with poly-L-lysine-immobilized fluorescent microspheres (FluoSpheres®, 0.02 µm,
616 dark red fluorescent; Thermo Fischer Scientific Inc., Waltham, MA, USA) to examine the setup
617 performance on a daily basis, to measure the PSF of the optical setup and to calibrate the axial beam
618 positioning with the VFL. The samples were prepared as previously described¹.

619 DNA origami

620 We pre-annealed the unlabeled DNA origami template based on 10-fold excess of the staple strands
621 (containing biotinylated strands for immobilization) compared to the scaffold strands (M13mp18,
622 N4040S, New England Biolabs Inc., Ipswich, MA, USA) in folding buffer containing TAE 1x (1:5), MgCl₂
623 27 mM heating first to 85 °C for 3 min, cooling down at a speed of 0.5 °C/min until reaching 42 °C
624 and storing at 4 °C. The sequences of the DNA staple strands are listed in the supplementary
625 material (Tab. S2). After annealing, we purified the DNA origami templates by adding 15% PEG in
626 TAE 1x containing 0.5 mM NaCl and 16 mM MgCl₂. After mixing the solutions, we centrifuged for

627 30 min, keeping the sample at 4 °C. After removing excess, we repeated the procedure three times
628 before storing the template in TAE 1x containing 10 mM MgCl₂. Prior to experiments, we annealed
629 the template with the complementary strands 5'-labelled with a fluorescent molecule. In a first step,
630 we used a 25x excess of the labelled strands and kept the mixed solutions overnight at room
631 temperature. After purifying as described above, we repeated annealing and purification with a 250x
632 excess of labelled strands. On the day of the experiment, we prepared the samples with immobilized
633 DNA origamis as previously described¹.

634 U-2 OS Nup96-SNAP/mMaple

635 We handled the cells as previously described⁷. Briefly, cells were cultured in DMEM without phenol
636 red (Cat#1180-02, ThermoFisher Scientific, Waltham, MA, USA) supplemented with 1x MEM NEAA
637 (Cat#11140-035, ThermoFisher Scientific), ZellShield (Cat#13-0050, Minerva Biolabs, Berlin,
638 Germany), 1x GlutaMAX (Cat#35050-038, ThermoFisher Scientific) and 10% [v/v] fetal bovine serum
639 (Cat#10270-106, ThermoFisher Scientific) at 37 °C, 5% CO₂ and 100% humidity. Seeded coverslips
640 were pre-fixed (2.4% [w/v] formaldehyde [FA] in PBS) after two days of growth for 30 sec,
641 permeabilized (0.4% [v/v] Triton X-100 in PBS) for 3 min and fixed (2.4% [w/v] FA in PBS) for 30 min.
642 The sample was quenched by incubating it for 5 min in 100 mM NH₄Cl and subsequently washed
643 twice for 5 min in PBS. Samples of NUP96-mMaple were ready for imaging and mounted as
644 described above. NUP96-SNAP samples were blocked for 30 min with Image-iT FX Signal Enhancer
645 (ThermoFisher Scientific) and stained with staining solution (1 μM BG-AF647 [Cat#S9136S, New
646 England Biolabs, Ipswich, MA, USA], 1 mM DTT in 0.5% [w/v] BSA) for 50 min. After washing 3 times
647 in PBS for 5 min each to remove unbound dye, the samples were mounted as described above. For
648 cells with an additional labelling for the center of the pore, we applied wheat germ agglutinin CF680
649 conjugate (29029, Biotium, Inc., Fremont, CA, USA) diluted to 0.02 μg/mL in PBS with an addition of
650 1% BSA in the final solution. We incubated the cells at room temperature for 5 min before washing
651 three times in PBS. The cell lines are available via Cell Line Services (CLS, clsgmbh.de, Nup96-SNAP
652 #300444, Nup96-mMaple #300461).

653 Hippocampal cultured neurons (PSD-95)

654 We prepared hippocampal neurons from transgenic PSD-95-HaloTag mice⁸ in accordance with the
655 regulations of the German Animal Welfare Act and under the approval of the local veterinary service
656 as previously described⁹. After 35 days in vitro we fixed the neurons in PFA (4% in PBS, pH 7.4) at
657 room temperature for 15 min. After washing in PBS, we treated the neurons with Ammonium
658 chloride (100 mM) for 10 min to reduce background due to autofluorescence. We permeabilized
659 using 0.1% Triton X-100 in PBS for 10 min and subsequently stained with Alexa Fluor 647-HaloTag

660 ligand (1 μ M, synthesized in house) for 30 min at room temperature. After several short washing
661 steps in PBS, we mounted the coverslips for imaging (see Sample mounting and imaging buffers).

662 [Data Availability](#)

663 The data that support the findings of this study are available from the corresponding author upon
664 reasonable request.

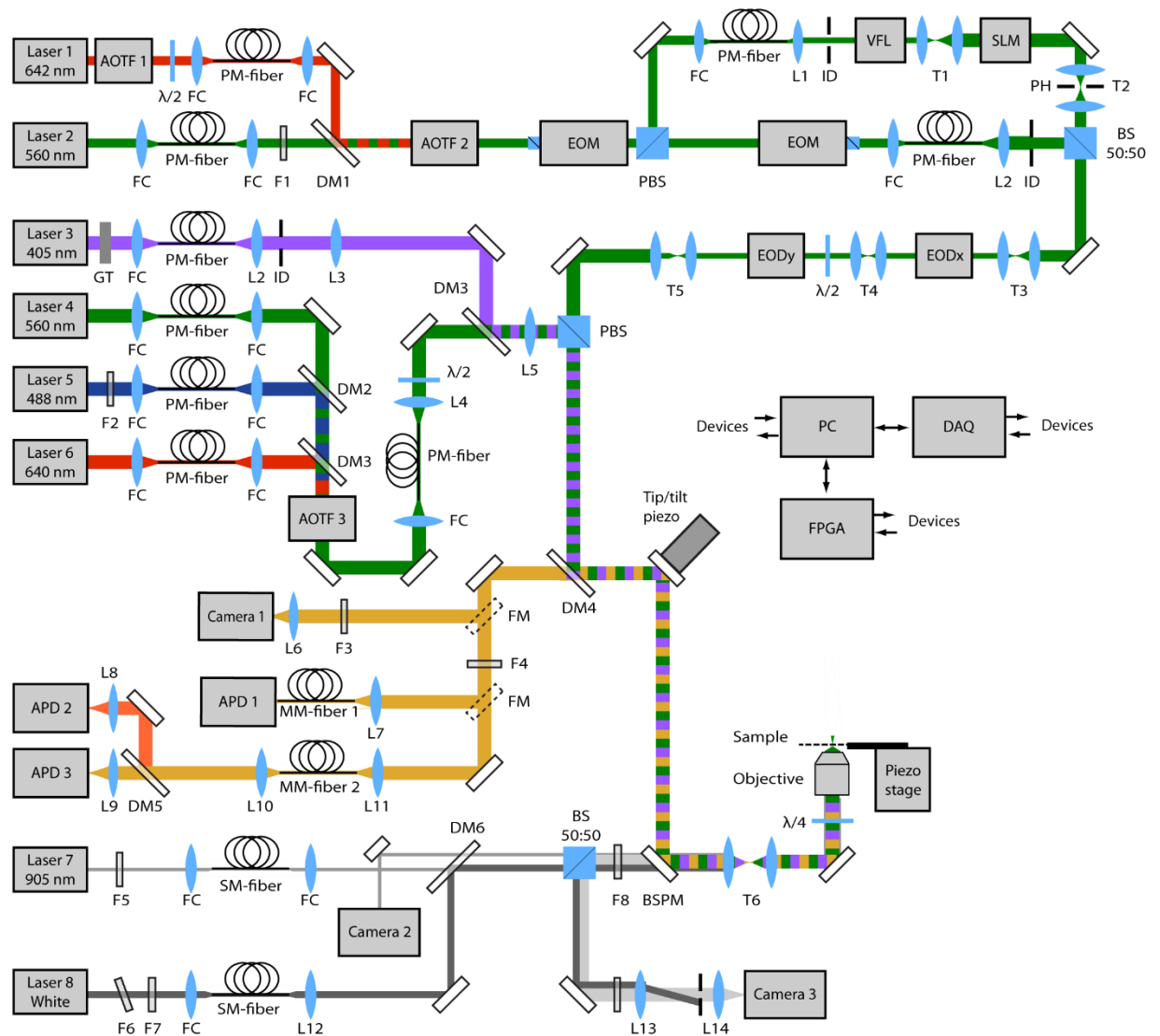
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688

689 Supplementary information

690 Supplementary figures



691 **Fig. S1 | Schematic drawing of the optical setup.**

692 Lasers :

693 Laser 1: VFL-P-1500-642 (MPB Communications Inc., Pointe-Claire, Quebec, Canada),

694 Laser 2: Cobolt Jive™ 150-561 (Cobolt AB, Solna, Sweden),

695 Laser 3: 405-50-COL-004 (Oxxius, Lannion, France),

696 Laser 4: Cobolt Jive™ 25-561 (Cobolt AB, Solna, Sweden),

697 Laser 5: LDH-D-C-485 (PicoQuant, Berlin, Germany),

698 Laser 6: LDH-D-C-640 (PicoQuant, Berlin, Germany),

699 Laser 7: LuxX® 905-150 (Omicron-Laserage Laserprodukte GmbH, Rodgau-Dudenhofen,

700 Germany),

701 Laser 8: Koheras SuperK Extreme (NKT Photonics, Birkerød, Denmark)

702 Beam modulation:

703 AOTF1: AOTFnC VIS-TN (AA Sa, Orsay, France),

704 AOTF2: AOTFnC VIS-TN (AA Sa, Orsay, France),

705 AOTF3: AOTFnC 400.650-TN (AA Sa, Orsay, France),

706 EOM: LM 0202 P 5W + LIV 20 (Qioptiq Photonics GmbH & Co. KG, Göttingen, Germany),

707 SLM: LCOS-SLM X13267-06 (Hamamatsu Photonics Deutschland GmbH, Herrsching am Ammersee,
708 Germany),

709 Scanning:
710 EODx and EODy: M-311-A (Conoptics Inc., Danbury, CT, USA) + WMA-300 (Falco Systems BV,
711 Amsterdam, The Netherlands),
712 VFL: KLMS2D0700 -00 KTN varifocal lens module (NTT Advanced Technology Corporation, Omiya-
713 cho Saiwai-ku, Kawasaki-shi, Japan) + AMPS-2B200-03 (Matsusada Precision Inc., Aojicho Kusatsu,
714 Japan),
715 Tip/tilt piezo: PSH-10/2 + EVD300 (both piezosystem jena GmbH, Jena, Germany),
716 Piezo stage: P-733.3-DD + E725 (both Physik Instrumente (PI) GmbH & Co. KG, Karlsruhe,
717 Germany),

718 Polarization and beam transport:
719 GT: Glan-Thompson polarizer (B. Halle Nachfl. GmbH, Berlin, Germany),
720 PBS: polarizing beam splitter cube (B. Halle Nachfl. GmbH, Berlin, Germany),
721 BS: beam splitter cube 50:50,
722 FC: fiber collimator 60FC-* (Schäfter+Kirchhoff, Hamburg, Germany),
723 $\lambda/2$: half wave plate (B. Halle Nachfl. GmbH, Berlin, Germany or Thorlabs Inc., Newton, NJ, USA),
724 $\lambda/4$: achromatic quarter wave plate (Thorlabs Inc., Newton, NJ, USA),
725 PM-fiber: polarization maintaining single mode fiber (Thorlabs Inc., Newton, NJ, USA or
726 Schäfter+Kirchhoff, Hamburg, Germany),
727 MM-fiber 1: multimode fiber M31L01 (Thorlabs Inc., Newton, NJ, USA),
728 MM-fiber 2: multimode fiber M42L02 (Thorlabs Inc., Newton, NJ, USA),

729 Lenses and mirrors
730 Objective: HC PL APO 100x/1.40 Oil CS2 (Leica Microsystems GmbH, Wetzlar, Germany),
731 L1-L14: achromatic lens with VIS or NIR AR coating (Thorlabs Inc., Newton, NJ, USA or Qioptiq
732 Photonics GmbH & Co. KG, Göttingen, Germany),
733 T1-T6: telescope,
734 ID: iris diaphragm,
735 FM: mirror on motorized flip mount,
736 PH: pinhole,
737 BSPM: back side polished mirror (Thorlabs Inc., Newton, NJ, USA),

738 Dichroic mirrors and filters
739 DM1: H 568 LPXR superflat (AHF Analysetechnik GmbH, Tübingen, Germany),
740 DM2: Z500-RDC-XT (Chroma Technology Corp., Bellows Falls, VT, USA),
741 DM3: Z620SPRDC (Chroma Technology Corp., Bellows Falls, VT, USA),
742 DM4: ZT405/488/561/640rpc (AHF Analysetechnik GmbH, Tübingen, Germany),
743 DM5: FF685-DiO2 (Semrock Inc., Rochester, NY, USA),
744 DM6: FF925-DiO1 (Semrock Inc., Rochester, NY, USA),
745 F1: ZET561/10x (Chroma Technology Corp., Bellows Falls, VT, USA),
746 F2: 488/6 BrighLine HC (Semrock Inc., Rochester, NY, USA),
747 F3: FF01-842/SP-25 (Semrock Inc., Rochester, NY, USA) and Quad-Band 446/523/600/677 HC
748 (Semrock Inc., Rochester, NY, USA),
749 F4: FF01-775/SP-25 (Semrock Inc., Rochester, NY, USA) and Quad-Notch 405/488/560/635
750 (Semrock Inc., Rochester, NY, USA) and ET700/75m (Chroma Technology Corp., Bellows Falls, VT,
751 USA) or BLP02-561R-25 (Semrock Inc., Rochester, NY, USA),
752 F5: FL905/10 (Dynasil, Littleton, MA, USA),
753 F6: FELH0950 (Thorlabs Inc., Newton, NJ, USA),
754 F7: FESH1000 (Thorlabs Inc., Newton, NJ, USA),
755 F8: 66-230 long pass filter 950 (Edmund Optics®, Barrington, NJ; USA),
756

757 Detectors

758 APD 1: SPCM-AQR-13-FC (Excelitas Technologies, Waltham, MA, USA),

759 APD 2,3: SPCM-AQRH-13-TR (Excelitas Technologies, Waltham, MA, USA),

760 Camera 1: Ixon EMCCD DU897-BV, (Andor Technology Ltd., Belfast, UK),

761 Camera 2: DMK 22BUC03 (The Imaging Source Europe GmbH, Bremen, Germany),

762 Camera 3: DMK 23UP1300 (The Imaging Source Europe GmbH, Bremen, Germany),

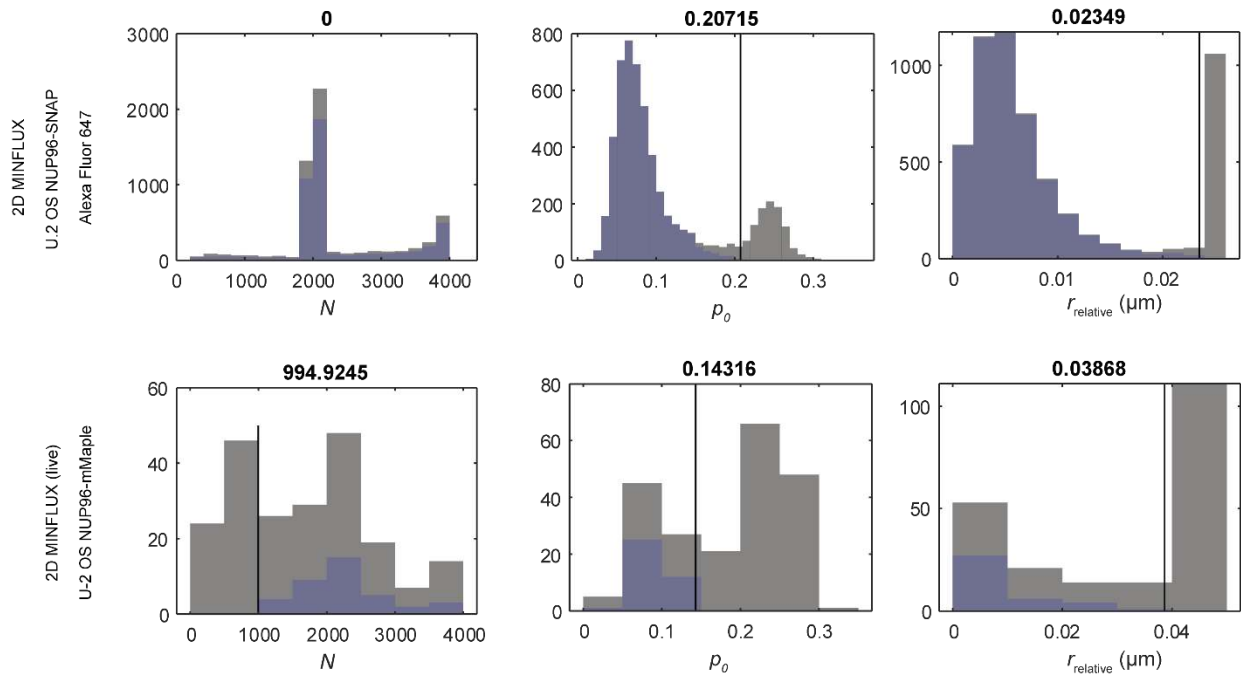
763 Computer

764 PC: 3 personal computers running Windows 7 (Microsoft Corp., Redmond, WA, USA) and LabView
765 2016 (National Instruments, Austin, TX, USA),

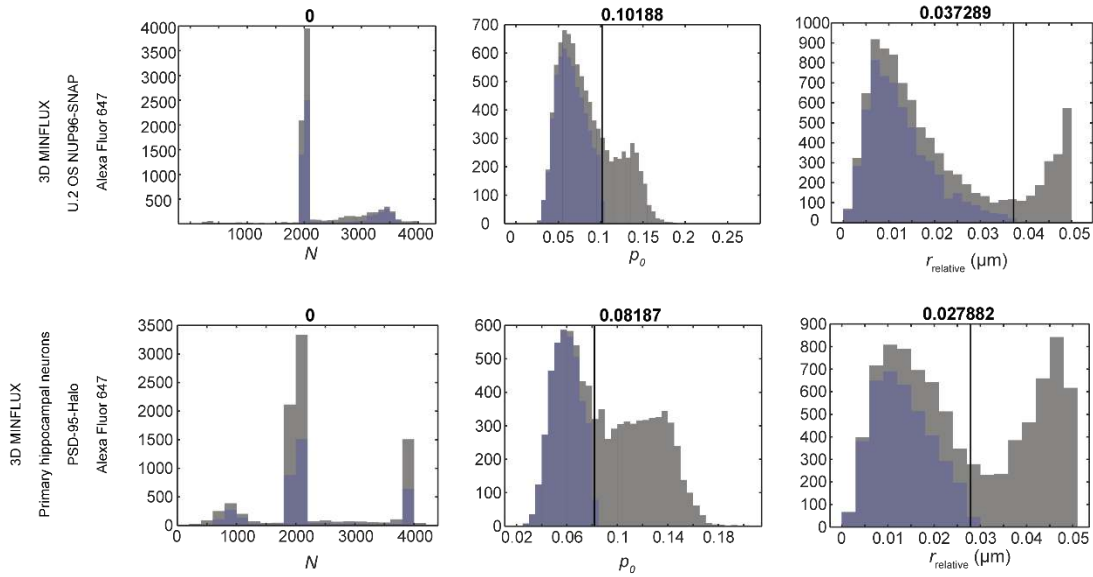
766 DAQ: NI PCIe-6353 + NI PCI-6259 (both National Instruments, Austin, TX, USA) + USB-3133

767 (Measurement Computing Corporation, Norton, MA, USA),

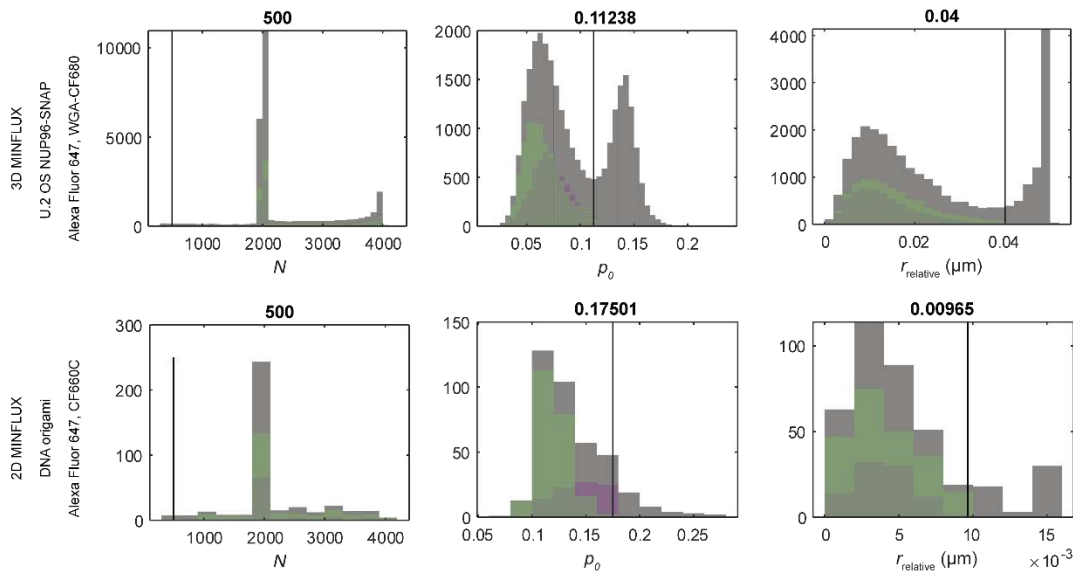
768 FPGA: NI USB-7856R (National Instruments, Austin, TX, USA)



769 **Fig. S2 | Filtering of 2D imaging data.** The histogram of photon number N , the relative photon count
 770 number in the central exposure p_0 and distance of the estimated position relative to the center of
 771 the last excitation beam pattern r_{relative} are displayed for each localization. Before filtering (gray) at
 772 a manually defined position (black line, number above), p_0 and r_{relative} show two populations. The
 773 population that is assigned to background events is discarded, leading to a new filtered distribution
 774 (blue). Top row: data displayed in Fig. 2a. Bottom row: data displayed in Fig. 2f.



775 **Fig. S3 | Filtering of 3D imaging data.** The histogram of photon number N , the relative photon count
776 number in the central exposure p_0 and distance of the estimated position relative to the center of
777 the last excitation beam pattern r_{relative} are displayed for each localization. Before filtering (gray) at
778 a manually defined position (black line, number above), p_0 and r_{relative} show two populations. The
779 population that is assigned to background events is discarded, leading to a new filtered distribution
780 (blue). Top row: data displayed in Fig. 3f. Bottom row: data displayed in Fig. 4a.



781 **Fig. S4 | Filtering of multicolor imaging data.** The histogram of photon number N , the relative
782 photon count number in the central exposure p_0 and distance of the estimated position relative to
783 the center of the last excitation beam pattern r_{relative} are displayed for each localization. Before
784 filtering (gray) at a manually defined position (black line, number above), p_0 and r_{relative} show two
785 populations. The population that is assigned to background events is discarded, leading to a new
786 filtered distribution for each molecule species (green: Alexa Fluor 647, magenta: CF dye). Top row:
787 data displayed in Fig. 5e. Bottom row: data displayed in Fig. 5c.

788 Supplementary videos

789 **Video S1 | 3D MINFLUX nanoscopy of Nup96 in a mammalian cell.** U-2 OS cell expressing Nup96-
790 SNAP labelled with Alexa Fluor 647 after fixation as displayed in Fig. 3. The color indicates the z-
791 position of the localization.

792 **Video S2 | 3D MINFLUX nanoscopy of the synaptic protein PSD-95.** Primary hippocampal neurons
793 from transgenic mice expressing PSD-95-Halo conjugated to Alexa Fluor 647 after fixation as
794 displayed in Fig. 4. The color indicates the 3D localization density.

795 **Video S3 | 3D two-color MINFLUX nanoscopy of the nuclear pore complex in a mammalian cell.** U-
796 2 OS cell expressing Nup96-SNAP labelled with Alexa Fluor 647 (green) and wheat germ agglutinin
797 conjugated to CF680 (magenta) after fixation as displayed in Fig. 5. The colors indicate the molecular
798 species assigned in the two-color classification.

Supplementary tables

Tab. S1 | Iterative MINFLUX strategies

		Beam shape	L (nm)	N_k	Estimator scaling factor	Estimator β_0	Estimator β_1		
2D iterative MINFLUX imaging									
Simulations	Fig. 1	G	300	150	0.8	Optimal			
		D	150	100					
		D	90	120					
		D	40	230					
U-2 OS-NUP96-SNAP-AlexaFluor647 (2D)	Fig. 2a	G	300	100	0.8	-	-		
		G	300	100	0.8	-	-		
		D	150	150		0.89	7.18		
		D	100	300		0.57	10.8		
U-2 OS-NUP96-mMaple, live (2D)	Fig. 2f	G	300	100	0.8	-	-		
		G	300	100	0.8	-	-		
		D	150	150		0.099	6.1		
		D	100	300		0.77	8.7		
U-2 OS-NUP96-mMaple, live (2D)	Fig. 2f	D	100	10000		0.77	8.7		
		3D iterative MINFLUX imaging							
		Simulations	Fig 3	G	300	150	0.8	Optimal	
				Z	400	100			
$D7$	150			150					
$D7$	90			150					
U-2 OS-NUP96-SNAP-AlexaFluor647 (3D)	Fig. 3f	$D7$	40	450					
		G	300	100	0.8	-	-		
		G	300	100	0.8	-	-		
		Z	300	100		0.55	-		
HPN-PSD95-HaloTag-AlexaFluor647 (3D)	Fig. 4a	Z	200	100		0.55	-		
		$D7$	150	150		0.88	23.5		
		$D7$	100	200		0.58	31.5		
		$D7$	100	10000		0.58	31.3		
HPN-PSD95-HaloTag-AlexaFluor647 (3D)	Fig. 4a	G	300	100	0.8	-	-		
		G	300	100	0.8	-	-		
		Z	300	100		0.55	-		
		Z	200	100		0.55	-		
HPN-PSD95-HaloTag-AlexaFluor647 (3D)	Fig. 4a	$D7$	150	150		0.88	23.5		
		$D7$	100	200		0.58	31.5		
		$D7$	100	10000		0.58	31.3		
		Multicolor MINFLUX imaging							
U-2 OS-NUP96-SNAP-AlexaFluor647, WGA CF680 (3D)	Fig. 5e	G	300	100	0.8	-	-		
		G	300	100	0.8	-	-		
		Z	300	100		0.55	-		
		Z	200	100		0.55	-		
DNA origami, AlexaFluor647, CF660C (2D)	Fig. 5c	$D7$	150	150		0.88	23.5		
		$D7$	100	200		0.58	31.5		
		$D7$	100	10000		0.58	31.3		
		G	300	40	1	-	-		
DNA origami, AlexaFluor647, CF660C (2D)	Fig. 5c	G	300	60	1	-	-		
		D	150	100		1.16	8		
		D	100	100		0.95	8.8		
		D	50	100		0.58	11.6		
DNA origami, AlexaFluor647, CF660C (2D)	Fig. 5c	D	30	Inf		0.4	13.5		

Tab. S2 | DNA origami strands.

Biotinylated

Biotin conjugated to 5' end, HPLC purified

47	CTTTGAAAAGAAGCTGGCTCATTATTTAATAAA
54	CCGGAAACACACCACGGAAATAAGTAAGACTCC
103	CGAGTAGAACTAATAGTAGTAGCAAACCTCA
106	GGTATTAAGAACAAGAAAAATAATTAAAGCCA
173	CTTGCATGCATTAATGAATCGGCCCGCCAGGG
180	CGGAATTATTGAAAGGAATTGAGGTGAAAAAT

For Alexa Fluor 647 labelling sites

39	TTATTCCTGTAGTATATGGCAATGAAATTATGCTCCATGAGAGGCTTTGAGGACTAGGGAGTT
41	TTATTCCTGTAGTATATGGCAATGAAATTATGCGAAACATGCCACTACGAAGGCATGCGCCGA
111	TTATTCCTGTAGTATATGGCAATGAAATTATCAAAATTAAGTACGGTGTCTGGAAGAGGTCA
113	TTATTCCTGTAGTATATGGCAATGAAATTATTCAATTCTTTTAGTTTGACCATTACCAGACCG
130	TTATTCCTGTAGTATATGGCAATGAAATTATGGTAGCTAGGATAAAAAATTTTAGTTAACATC

For CF660C labelling sites

58	ACTAGCGGCAACGGCCCAACTATCCATTTTTTCAACTATAGGCTGGCTGACCTTGTATCAT
75	ACTAGCGGCAACGGCCCAACTATCCATTTTACTGGATAACGGAAACAACATTATTACCTTATG
77	ACTAGCGGCAACGGCCCAACTATCCATTTTCCAAAATATAATGCAGATACATAAACACCAGA
94	ACTAGCGGCAACGGCCCAACTATCCATTTTACCTTTAAGGTCTTTACCCTGACAAAGAAGT

Marker strands

Dye conjugated to 5' end, PAGE purified

Alexa Fluor 647	TAATTTCAATTGCCATATACTACAGGAATAA
CF660C	AAATGGATAGTTGGGCCGTTGCCGCTAGT

Staple strands

2	ACGTTAGTAAATGAATTTTCTGTAAGCGGAGT	23	CAATGACACTCCAAAAGGAGCCTTACAACGCC
3	CGTAACGATCTAAAGTTTGTGCGTGAATTGCG	24	CTTAAACATCAGCTTGCTTTTCGAGAAACAGTT
4	TGTAGCATTCACAGACAGCCCTCATCTCCAA	25	TGCCTTGACTGCCTATTTTCGGAACAGGGATAG
5	TGAGTTTCGTCACCAGTACAACTTAATTGTA	26	AGTGTACTTGAAAGTATTAAGAGGCCGCCACC
6	CAAGCCCAATAGGAACCCATGTACCGTAACAC	27	TAAGCGTGAAGGATTAGGATTAGTACCGCCA
7	CTCAGAGCCACCACCCTCATTTTCTATTATT	28	GGAAAGCGACCAGGCGGATAAGTGAATAGGTG
8	CCCTCAGAACC GCCACCCTCAGA ACTGAGACT	29	ACGGCTACTTACTTAGCCGGAACGCTGACCAA
9	TATCACCGTACTCAGGAGGTTTAGCGGGGTTT	30	TTTCATGAAAATTGTGTGAAATCTGTACAGA
11	GAGAATAGCTTTTGC GGATCGTCGGGTAGCA	31	ATACGTAAAAGTACAACGGAGATTTTCATCAAG
12	AATAATAAGGTCGCTGAGGCTTGCAAAGACTT	32	AAACGAAATGACCCCAGCGATTATTCATTAC
13	AAAAAAGGACAACCATCGCCCACGCGGGTAAA	33	GAGCCGCCCCACCACCGGAACCGCCTAAAACA
14	TCGGTTTAGCTTGATACCGATAGTCCAACCTA	34	GCCACCACTCTTTTCATAATCAAACCGTCACC
15	AATGCCCCGTAACAGTGCCCGTATGTGAATTT	35	CACCAGAGTTCGGTCATAGCCCCCGCCAGCAA
16	CTGAAACAGGTAATAAGTTTAAACCCCTCAGA	36	TGAGGCAGGCGTCAGACTGTAGCGTAGCAAGG
17	CCTCAAGAATACATGGCTTTTGATAGAACCAC	39	Modified > Alexa Fluor 647
18	TGCTCAGTCAGTCTCTGAATTTACCAGGAGGT	40	CGCCTGATGGAAGTTTCCATTAACATAACCG
21	AAAGGCCGAAAGGAACA ACTAAAGCTTTCCAG	41	Modified > Alexa Fluor 647
22	ATATATTC TTTTTT CACGTTGAAAATAGTTAG	42	CTCATCTTGAGGCAAAGAATACACTCCCTCA

MINFLUX nanoscopy delivers multicolor nanometer 3D-resolution in (living) cells

43	AACCAGAGACCCTCAGAACCGCCAGGGGTCAG
44	GTTTGGCCACCTCAGAGCCGCCACCGATACAGG
45	TCGGCATTCCGCCGCCAGCATTGACGTTCCAG
46	TGCCTTTAGTCAGACGATTGGCCTGCCAGAAT
47	Modified > Biotin
48	CCAGGGCGCTTAATCATTGTGAATTACAGGTAG
49	AGTAATCTTAAATTGGGCTTGAGAGAATACCA
50	CCAAATCACTTGCCCTGACGAGAACGCCAAAA
51	TTATTCATAGGGAAGGTAAATATTCATTCACT
52	GACTTGAGAGACAAAAGGGCGACAAGTTACCA
53	AATCACCAAATAGAAAATTCATATATAACGGA
54	Modified > Biotin
57	CGATTTTAGAGGACAGATGAACGGCGCGACCT
58	Modified > CF660C
59	ACGAGTAGTGACAAGAACCGGATATACCAAGC
60	GAATAAGGACGTAACAAAGCTGCTGACGGAAA
61	ATTGAGGGTAAAGGTGAATTATCAATCACCGG
62	AGCGCCAACCATTTGGGAATTAGATTATTAGC
63	TCACAATCGTAGCACCATTACCATCGTTTTCA
64	ACGCAAAGGTCACCAATGAAACCAATCAAGTT
65	ACGAACTAGCGTCCAATACTGCGGAATGCTTT
66	AAAGATTCAGGGGGTAATAGTAAACCATAAAT
67	CATTCAACGCGAGAGGCTTTTGCATATTATAG
68	GGAATTACTCGTTTACCAGACGACAAAAGATT
69	AAAAGTAATATCTTACCGAAGCCCAACTAT
70	GAAGGAAAATAAGAGCAAGAAACAACAGCCAT
71	ATACCCAAGATAACCCACAAGAATAAACGATT
72	TTATTACGGTCAGAGGGTAATTGAATAGCAGC
75	Modified > CF660C
76	TTTGCCAGATCAGTTGAGATTTAGTGGTTTAA
77	Modified > CF660C
78	CATAACCCGAGGCATAGTAAGAGCTTTTTAAG
79	GCAATAGCGCAGATAGCCGAACAATTCAACCG
80	GCCCAATACCGAGGAAACGCAATAGGTTTACC
81	ATCAGAGAAAGAAGTGGCATGATTTTATTTTG
82	TGAACAAACAGTATGTTAGCAAATAAAAGAA
83	AAACAGTTGATGGCTTAGAGCTTATTTAAATA
84	CAAAAATCATGCTCCTTTTGATAAGTTTCAT
85	TCAGAAGCCTCCAACAGGTCAGGATCTGCGAA
86	AAGAGGAACGAGCTTCAAAGCGAAGATACATT
87	CCTAATTTACGCTAACGAGCGTCTATATCGCG
88	ATTATTTAACCCAGCTACAATTTTCAAGAACG

89	TTTTGTTTAAGCCTTAAATCAAGAATCGAGAA
90	CTTTACAGTTAGCGAACCTCCCAGCTAGGAA
93	TTTTTGCAGAGAAAACGAGAATGAATGTTTAG
94	Modified > CF660C
95	GAAGCAAAAAAGCGGATTGCATCAGATAAAAA
96	TTTTAATTGCCCGAAAGACTTCAATTCAGAG
97	TCTTACCAGCCAGTTACAAAATAAATGAAATA
98	TATTTTGCTCCCAATCCAAATAAGTGAGTTAA
99	AGGTTTTGAACGTCAAAAATGAAAGCGCTAAT
100	GAGGCGTTAGAGAATAACATAAAAAGAACCCC
101	TGCAACTAAGCAATAAAGCCTCAGTTATGACC
102	TCCATATACATACAGGCAAGGCAACTTTATTT
103	Modified > Biotin
104	TCGCAAATGGGGCGCGAGCTGAAATAATGTGT
105	ATCGGCTGCGAGCATGTAGAAACCAGCTATAT
106	Modified > Biotin
107	CAAGCAAGACGCGCCTGTTTATCAAGAATCGC
108	TCATTACCCGACAATAAACAACATATTTAGGC
109	TATAGAAGCGACAAAAGGTAAAGTAGAGAATA
110	GCTAAATCCTGTAGCTCAACATGTATTGCTGA
111	Modified > Alexa Fluor 647
112	CAATAAATACAGTTGATTCCCAATTTAGAGAG
113	Modified > Alexa Fluor 647
114	TTTCATTTGGTCAATAACCTGTTTAAATCAATA
115	CTAATTTATCTTTTCTTATCATTATCCTGAA
116	TAAGTCTTACCAAGTACCGCACTCTTAGTTGC
117	AATGCAGACCGTTTTTTATTTTTCATCTTGCGGG
118	CCAGACGAGCGCCCAATAGCAAGCAAGAACGC
119	CTGTAATATTGCCCTGAGAGTCTGGAAAAC TAG
120	CAACGCAATTTTTGAGAGATCTACTGATAATC
121	TATATTTTAGCTGATAAATTAATGTTGTATAA
122	AGGTAAAGAAATCACCATCAATATAATATTTT
123	GCGTTATAGAAAAAGCCTGTTTAGAAGGCCGG
124	ACGCTCAAAAATAAGAATAAACACCGTGAATTT
125	CATATTTAGAAATACCGACCGTGTACCTTTT
126	AGAGGCATAATTTTCATCTTCTGACTATAACTA
129	TCAGGTCACTTTTGCGGGAGAAGCAGAATTAG
130	Modified > Alexa Fluor 647
131	ACCGTTCTAAATGCAATGCCTGAGAGGTGGCA
132	AGACAGTCATTCAAAGGGTGAGATATCATAT
133	AATTAATACTAAATCTTACCAGTAATCCCATC
134	AGGCGTTACAGTAGGGCTTAATTGACAATAGA

MINFLUX nanoscopy delivers multicolor nanometer 3D-resolution in (living) cells

135	AATGGTTTACAACGCCAACATGTAGTTCAGCT
136	TTTTAGTTTTTCGAGCCAGTAATAAATTCTGT
137	CATGTCAAGATTCTCCGTGGGAACCGTTGGTG
138	AGAAAAGCAACATTTAAATGTGAGCATCTGCCA
139	GCAAATATCGCGTCTGGCCTTCTGGCCTCAG
140	GTTAAAATTTTAACCAATAGGAACCCGGCACC
141	TTAAGACGTTGAAAACATAGCGATTTAAATCA
142	ATCAAAATCGTCGCTATTAATTAACGGATTCTG
143	TAACCTCCATATGTGAGTGAATAAACAAAATC
144	TATGTAAACCTTTTTTAATGGAAAAATTACCT
147	ACCCGTCGTCATATGTACCCCGGTAAAGGCTA
148	CTTTCATCCCCAAAAACAGGAAGACCGGAGAG
149	AAATAATTTTAAATTGTAAACGTTGATATTCA
150	GCTCATTTTTCGCATTAATTTTTTGAGCTTAGA
151	TAGAATCCCTGAGAAGAGTCAATAGGAATCAT
152	CTGTAAATCATAGGTCTGAGAGACGATAAATA
153	AAATCAATGGCTTAGGTTGGGTTACTAAATTT
154	TTGAATTATGCTGATGCAAATCCACAAATATA
155	TAGATGGGGGTAACGCCAGGGTTGTGCCAAG
156	GTTTGAGGAAAGGGGATGTGCTAGAGGATC
157	GAAGATCGGTGCGGGCCTCTTCGCAATCATGG
158	GCTTCTGGTCAGGCTGCGCAACTGTGTTATCC
159	CTTTTACACAGATGAATATACAGTAAGCGCCA
160	CCTGATTGAAAGAAATTGCGTAGACCCGAACG
161	GCGCAGAGATATCAAAATTATTTGACATTATC
162	GAGCAAAAACCTCTGAATAATGGAAGAAGGAG
165	ATTAAGTTCGCATCGTAACCGTGCGAGTAACA
166	CAGCTGGCGGACGACGACAGTATCGTAGCCAG
167	GGCGATCGCACTCCAGCCAGCTTTGCCATCAA
168	TTCCGCAATTGCCGAAACCAGGCAAACAGTAC
169	TTTAACGTTTCGGGAGAAACAATAATTTTCCCT
170	ACAGAAATCTTTGAATACCAAGTTCCTTGCTT
171	AACCTACCGCAATTATTCATTTCCAGTACAT
172	TGGATTATGAAGATGATGAAACAAAATTTTCAT
173	Modified > Biotin
174	CCCGGGTACTTTCCAGTCGGGAAACGGGCAAC
175	TCATAGCTACTCACATTAATTGCGCCCTGAGA
176	GCTCACAATGTAAAGCCTGGGGTGGGTTTGCC
177	CGACAATAAGTATTAGACTTTACAGCCGGAA
178	TTATTAATGCCGTCAATAGATAATCAGAGGTG
179	ATTTTGCCTTTTAGGAGCACTAAGCAACAGT
180	Modified > Biotin

183	GCCAGCTGCCTGCAGGTCGACTCTGCAAGGCG
184	ACTGCCCCGCCGAGCTCGAATTCGTTATTACGC
185	GTGAGCTAGTTTCCCTGTGTGAAATTTGGGAAG
186	GCATAAAGTTCACACACAACATACGAAACAATT
187	GGATTTAGCGTATTAATCCTTTGTTTTTCAGG
188	AGATTAGATTTAAAAGTTTGAGTACACGTAAA
189	CTAAAATAGAACAAAGAAACCACCAGGGTTAG
190	ATCAACAGTCATCATATTCCTGATTGATTGTT
191	TGGTTTTTAACGTCAAAGGGCGAAGAACCATC
192	AGCTGATTACAAGAGTCCACTATTGAGGTGCC
193	GAGTTGCACGAGATAGGGTTGAGTAAGGGAGC
194	CCAGCAGGGGCAAAATCCCTTATAAAGCCGGC
195	ACGAACCAAAACATCGCCATTAATGGTGGT
196	AGGCGGTCATTAGTCTTTAATGCGCAATATTA
197	GCCACGCTATACGTGGCACAGACAACGCTCAT
198	CTAAAGCAAGATAGAACCCTTCTGAATCGTCT
201	TGGACTCCCTTTTACCAGTGAGACCTGTCTGT
202	AGTTTGGAGCCCTTACCAGCCTGGTTGCGCTC
203	GAATAGCCGCAAGCGGTCCACGCTCCTAATGA
204	CCGAAATCCGAAATCCTGTTTGAAATACCGA
205	TAGCCCTACCAGCAGAAGATAAAAAACATTTGA
206	GAATGGCTAGTATTAACACCGCCTCAACTAAT
207	GCGTAAGAGAGAGCCAGCAGCAAAAAGGTTAT
208	GCCAACAGTCACCTTGCTGAACCTGTTGGCAA
210	ACCCAAATCAAGTTTTTTGGGGTCAAAGAACG
211	GTAAGCACTAAATCGGAACCCTAGTTGTTCC
212	CCCCGATTTAGAGCTTGACGGGAAATCAAAA
213	GAACGTGGCGAGAAAGGAAGGAAACAACTAT
214	CGGCTTGCTGGTAATATCCAGAACGAAGTGA
215	CCGCCAGCCATTGCAACAGGAAAAATATTTTT
216	GGAAATACCTACATTTTGACGCTCACCTGAAA
217	GAAATGGATTATTTACATTTGGCAGACATTTCTG