

# Modeling of coherence scanning interferometry using classical Fourier optics

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**Abstract.** We propose a model for coherence scanning interferometry using familiar Fourier optics methods and the spectrum of plane waves for the case where light source spectral bandwidth limits the fringe contrast as a function of optical path length. The model is straightforward to implement, is computationally efficient, and reveals many of the common error sources related to the optical filtering properties of the imaging system. We quantify the limits of applicability of the model related to the geometrical approximations for Fourier optics, particularly for high numerical apertures, and when using the fringe contrast for determining surface heights. These limitations can be overcome using a three-dimensional imaging model. © The Authors. Published by SPIE under a Creative Commons Attribution 4.0 International License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: [10.1117/1.OE.60.10.104106](https://doi.org/10.1117/1.OE.60.10.104106)]

**Keywords:** interferometry; interferometer; metrology; topography; coherence scanning interferometry; Fourier optics.

Paper 20210950 received Aug. 26, 2021; accepted for publication Sep. 29, 2021; published online Oct. 18, 2021.

## 1 Introduction

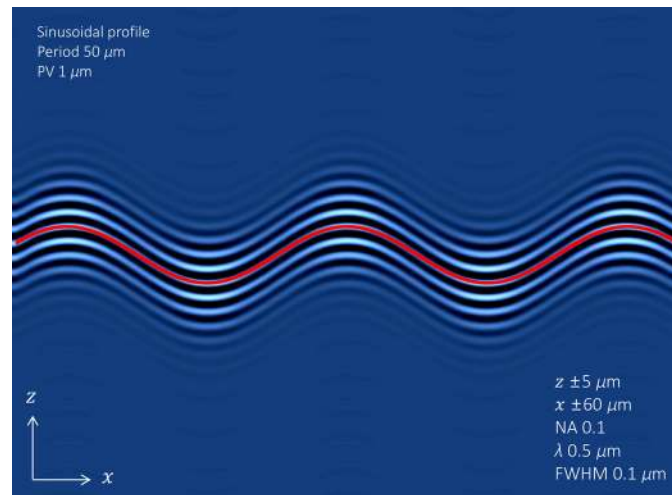
Coherence scanning interferometry (CSI), often thought of as a modern implementation of white light interferometry, is today the most widely used method for surface topography measurement using interference microscopy.<sup>1</sup> The image in Fig. 1 is simulated data from a CSI microscope, showing interference fringes acquired by a camera during an axial scan of the interference objective. Both the shape of the interference fringes and their variation in contrast are suggestive of the surface profile, shown as a solid red line in this figure.

The success of CSI has motivated research into physics-based models to predict the interference signals and measurement results for these instruments.<sup>2–9</sup> These models address surface topographies and materials that vary from simple to complicated, for a wide range of applications for CSI. Modeling predicts performance characteristics such as measurement noise,<sup>10,11</sup> topographic spatial resolution,<sup>12</sup> and measurement errors related to surface structure.<sup>13</sup> In many cases, physical models can be used in place of actual instruments, for analyzing the effects of imaging aberrations<sup>14</sup> or for evaluation of uncertainty using statistical variations in influence factors such as vibrations.<sup>9,15</sup> A further use of instrument models is in defining the optimal measurement configuration for a specific measurement task.<sup>16,17</sup>

In this paper, we propose an approximate model that builds on a classical Fourier optics approach presented in previous papers.<sup>18</sup> The primary interest here is to discover fundamental sources of measurement error related to the imaging properties of the instrument, including wavelength-dependent spatial filtering. The model also provides a means for determining under what circumstances an approximate model of this kind generates meaningful results, and when conversely more accurate diffraction and imaging models are recommended.

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**Fig. 1** Simulated interference signal detected by a camera for a sinusoidal surface topography when using a spectrally broadband light source, as the interference objective is scanned in the  $z$  direction. The central red line represents the object surface profile on the same scale.

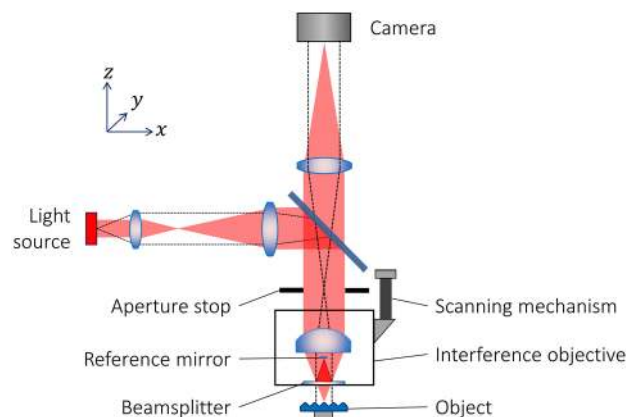
This paper is structured as follows. After a review of the principles of white-light interferometry and data processing methods, we propose the Fourier optics simulator for predicting CSI signals and measurement results. Several examples illustrate the use of the model for understanding error sources and predicting performance characteristics, such as the instrument response as a function of spatial frequency. This is followed by an analysis of the limitations of the model attributable to the geometrical approximations in its development. Finally, we consider approaches to more accurate modeling methods, as well as perspectives on further research in this area.

## 2 Interference Microscopy

Figure 2 shows a common microscope configuration for measurement of surface heights using interferometry.<sup>1</sup> The principle of measurement, at least as a starting concept, relies on the assumption that phases are directly proportional to object surface heights:

$$\theta_o(x) = 2\pi K h_o(x), \quad (1)$$

where the subscript  $o$  refers to the object,  $h_o$  is the local surface height along the orthogonal  $z$  direction, and  $x$  is an abbreviation for the  $x, y$  coordinates in a plane that coincides with the



**Fig. 2** Model of a microscope with a Mirau type interference objective.

surface.<sup>17</sup> The interference fringe frequency  $K$  along the  $z$  axis depends on the illumination geometry as well as the wavelength  $\lambda$ .

A common approximation is to summarize the illumination geometry with an obliquity factor  $\Omega$  that accounts for the illumination numerical aperture (NA) for the objective.<sup>19</sup> The fringe frequency is then

$$K = 2/\lambda\Omega. \quad (2)$$

A value for the obliquity factor for aplanatic imaging and uniform illumination of the objective pupil is

$$\Omega = \frac{3}{2} \left( \frac{1 - \cos^2(\beta)}{1 - \cos^3(\beta)} \right), \quad (3)$$

where the maximum incident angle for the illumination cone in terms of the NA value  $A_N$  is

$$\beta = \sin^{-1}(A_N). \quad (4)$$

After measuring the phase distribution  $\theta_I$  over the surface, for example by phase shifting interferometry (PSI), the calculated topography is

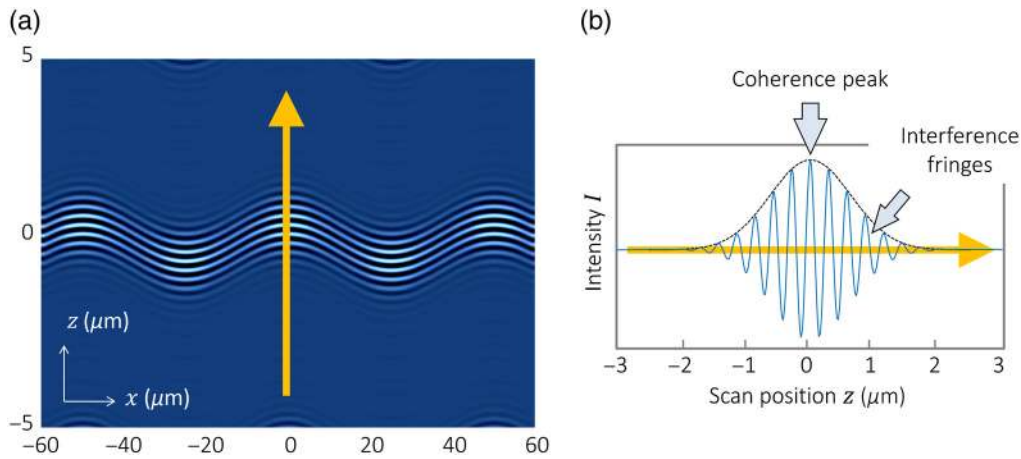
$$h_I(x) = \theta_I(x)/2\pi K, \quad (5)$$

where here the subscript  $I$  refers to a data analysis performed at the optical image plane. A known limitation when using a single wavelength  $\lambda$  is that the interference phase  $\theta_I$  can only be determined within a  $2\pi$  interval. One solution, known since the earliest days of interferometry, is to use a spectrally broadband or “white light” source.<sup>20</sup> The incoherent superposition of interference patterns for multiple wavelengths results in a signal for which the interference fringe contrast reaches a maximum at the stationary phase point, corresponding to a zero group-velocity path difference. The variation in fringe contrast provides a means to determine the interference fringe order or alternatively, to determine surface heights without relying on interference phase at all.<sup>21–23</sup>

The general concepts of white-light interferometry can be extended to any method for which the interference fringe contrast varies with surface height and objective scan position. It is common to equate CSI with white-light interferometry and to assume for example that the width of the coherence envelope is inversely proportional to the spectral bandwidth.<sup>24</sup> However, it is possible to have signals similar to those shown in Fig. 1 without using white light, if the light source is spatially extended and the illumination optics have an NA large enough to limit the  $z$  axis range of high fringe contrast.<sup>25</sup> In practice, in interference microscopy, the fringe contrast effect is a combination of both the broad spectral bandwidth and the focusing effects of high NA values. For this reason, the ISO term for technologies that rely on variations in fringe contrast is CSI rather than the more narrowly defined white light interferometry.<sup>26</sup>

To capture and analyze CSI signals, the interference objective in Fig. 2 is scanned axially while the camera records a sequence of intensity patterns. Setting aside methods for economizing data storage, the result of the acquisition is an  $x, y, z$  cube of intensity values, for which an example  $x, z$  cross section is shown in Fig. 1. The usual approach to analyzing these data is to extract intensity signals  $I$  in the image plane as a function of scan position  $z$  for each image pixel  $x, y$ , as illustrated in Fig. 3. The resulting signal, showing interference fringes and a coherence envelope with defined characteristics such as an envelope peak, is the usual starting point for developing CSI data analysis algorithms.

A common approach to CSI data analysis is to demodulate the signal to obtain the coherence envelope. The location of the peak, centroid or other envelope characteristic is directly a measure of the surface height for the corresponding image pixel. The corresponding surface heights  $h_C$  as a function of  $x$  are often referred to as the coherence profile. By analyzing the interference fringes from the same signal, for example, using a phase-shifting algorithm near the coherence peak, we can also obtain a phase profile  $h_\theta$  that has close to the same value as the result  $h_I$  in Eq. (5).



**Fig. 3** (a) A CSI signal with a gold arrow indicating a column of data points in the scan direction for a single pixel. (b) The corresponding detected intensity signal for the selected column.

The coherence profile is as much as 10× more sensitive to additive noise and signal distortions than the phase profile but has the important advantage of avoiding the  $2\pi$  cycle ambiguity.<sup>1,27</sup>

An alternative to calculating the coherence envelope and fringe phase is to transform the intensity signal  $I$  into the frequency domain.<sup>28</sup> The Fourier transform along the  $z$  direction is

$$q(K') = \frac{1}{\int dz} \int I(z) \exp(-i2\pi K'z) dz, \quad (6)$$

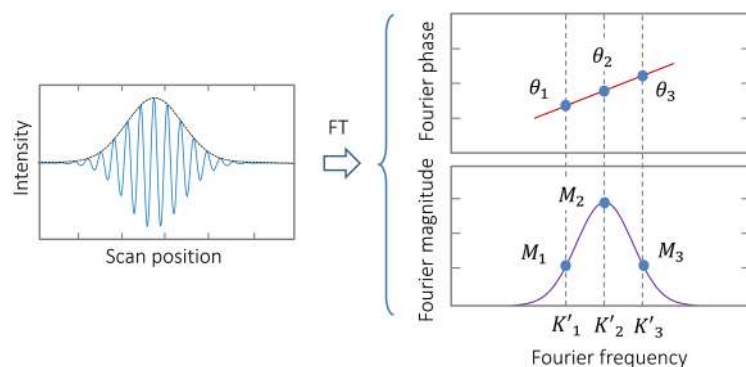
where the definite integral at the Fourier frequency  $K'$  has implied limits corresponding to a scan range encompassing the complete interference signal, and the result is normalized over this same range. These Fourier components have magnitudes and phases given by

$$\theta = \arg\{q(K')\}, \quad (7)$$

$$M = |q(K')|. \quad (8)$$

Figure 4 shows discretely sampled values  $\theta_{1,2,3}$  and  $M_{1,2,3}$  for the Fourier transform of a signal for one image point. After removing integer multiples of  $2\pi$  between neighboring phase values, a linear fit to the phase data weighted by the square of the Fourier magnitudes provides a phase slope and intercept for this image point. The slope of the line is a measure of the location of the signal, corresponding to the coherence profile:

$$h_C(x) = \frac{1}{2\pi} \frac{d\theta(x, K')}{dK'}. \quad (9)$$



**Fig. 4** The FDA method for the CSI signal shown in Fig. 3(b).

This result combines with the intercept  $A$  at  $K' = 0$  to provide a phase value at the strongest frequency  $K'_M$ , which, in Fig. 4, is indicated by the frequency  $K'_2$ :

$$\theta_M(x) = A(x) + 2\pi K'_M h_C(x). \quad (10)$$

The phase translates to a phase profile using

$$h_\theta(x) = \theta_M(x) / 2\pi K'_M. \quad (11)$$

Because the coherence profile  $h_C$  is more sensitive to sources of error than the phase profile  $h_\theta$ , it is common when measuring smooth surfaces to use the coherence profile only as a first estimate of surface height, to resolve the ambiguities in the fringe order for the phase profile  $h_\theta$ .<sup>27</sup>

It is important to note that this frequency-domain analysis (FDA) method is not itself an instrument model; rather, it is one of several ways to analyze CSI signals to extract surface topography information. However, as we shall see, it is a particularly useful method in the context of modeling instrument response, as it will allow for some convenient shortcuts for signal simulations.

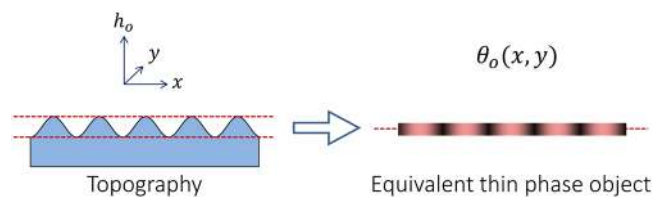
After this brief review of the principles of both monochromatic interference microscopy and CSI, we turn our attention to physical modeling of the interference signal and the resulting measured profiles.

### 3 Elementary Fourier Optics Model

It is understood that the measured interference phases will be altered from the starting values by the imaging optics illustrated in Fig. 2. In previous publications, we have argued that a significant potential contributor to measurement error is the spatial frequency bandwidth of the optical filtering in the imaging system.<sup>17</sup> This basic error mechanism can be examined, within limits of applicability that we will determine later in this paper, using a simplified Fourier optics model that includes geometrical approximations to simplify the calculation.

Imaging systems are frequently characterized in optical engineering using Abbe theory and standardized concepts such as the optical transfer function (OTF) and its modulus, the modulation transfer function (MTF).<sup>29</sup> These methods are most often applied to intensity objects—defined conceptually as perfectly flat surfaces having only a variation in reflectivity. If the illumination is fully incoherent, using the Fourier optics propagation of 2D wavefronts, the diffraction-limited imaging response is determined by linear transfer functions (TFs) in the frequency domain.

The situation is different for 3D surface topography. In principle, for such objects, there does not exist a generalized linear TF for the imaged intensity in partially coherent light, and we cannot readily apply a frequency-domain calculation using the OTF.<sup>30,31</sup> It can be nonetheless constructive to make several approximations that allow us to leverage familiar Fourier optics models. The first of these approximations is to replace the actual surface topography with a flat reflecting aperture function, with the local surface height represented by phase changes in the complex amplitude.<sup>32–34</sup> The main assumption is that the surface topography variations are small relative to the depth of field (DOF). Figure 5 illustrates this approximation, which is a familiar foundational concept in interferometry for topography measurement. Here it serves



**Fig. 5** The thin phase object approximation, assuming that the topography variations are small relative to the DOF. The color density in the equivalent thin object represents phase variations of a complex amplitude reflectivity.

as a starting point for modeling the diffraction problem, in what we refer to as the elementary Fourier optics (EFO) method.

The next approximation in the EFO model for interferometers is to set aside the contribution to the measured intensity of the object surface reflection alone, given the complications of solving this problem in partially coherent light. Instead, we isolate that portion of the signal resulting from the coherent interference of the light reflected from both the object and the reference. This portion contributes the interference fringes shown in Fig. 1, whereas the neglected portion is the background light resulting from conventional, noninterferometric imaging of the object surface, and reference surfaces. This is a significant step, as it allows for modeling the interference signal generation using linear TFs.

The next approximation is not essential to the EFO method, but it provides a path to using familiar TFs such as the OTF in simulations. The most accurate way to calculate the interference signal in partially coherent light is to integrate the image contributions from all illumination incident angles, using a diffraction calculation independently for each of these contributions.<sup>35–37</sup> The problem is significantly simplified, with a penalty to the accuracy of the model at high NA, if we average these effects using the obliquity factor  $\Omega$  defined in Eq. (3).

With this ensemble of approximations in hand and considering for the moment just one wavelength  $\lambda$ , we define the following 2D complex function as a representation of the effect of the object surface on the interference fringe signal:

$$U_o(x) = \exp[-i\theta_o(x)], \quad (12)$$

where the height-dependent phase  $\theta_o$  is defined in Eq. (1). The function  $U_o$  may be thought of conceptually as the light field immediately after reflection from the object surface, assuming uniform illumination and surface reflectivity, although it is more accurately described as the contribution of the object surface reflection to the interference pattern at the camera. Following conventional methods from Fourier optics,<sup>38</sup> the light field immediately after reflection is represented by a spectrum of plane waves:

$$\tilde{U}_0(f_x) = \frac{1}{\int dx} \int U_o(x) \exp(-i2\pi f_x x) dx. \quad (13)$$

The tilde ( $\sim$ ) symbol denotes a frequency-domain representation of the corresponding space-domain quantity, and the definite integrals are over the field of view. The lateral spatial frequency  $f_x$  for each plane wave is

$$f_x = \cos(\alpha_x)/\lambda, \quad (14)$$

where  $\alpha_x$  is the angle between the direction of the plane wave propagation and the  $x$  axis. The effect on the spectrum of plane waves is a multiplication in frequency space:

$$\tilde{U}_I(f_x) = \tilde{O}(f_x) \tilde{U}_o(f_x), \quad (15)$$

where  $\tilde{O}$  is the partially coherent TF for interferometric imaging. A familiar example TF for an interference microscope with Köhler illumination is the autocorrelation of a 2D circular pupil, which has the same form as the OTF for conventional optical imaging with a fully incoherent light source:

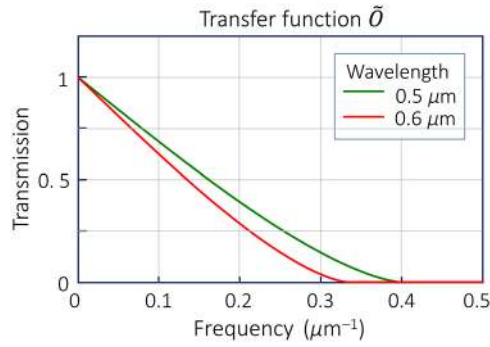
$$\tilde{O}(f_x) = \frac{2}{\pi} \left[ \cos^{-1} \left( \frac{|f_x|}{f_{\max}} \right) - \frac{|f_x|}{f_{\max}} \sqrt{1 - \left( \frac{|f_x|}{f_{\max}} \right)^2} \right] \text{rect} \left\{ \frac{f_x}{2f_{\max}} \right\}, \quad (16)$$

where the maximum detectable lateral spatial frequency is

$$f_{\max} = 2A_N/\lambda. \quad (17)$$

For a 2D pupil, the frequency  $f_x$  is replaced by a radius in the frequency domain. Within the implied limits of the approximations discussed above, the TF can also incorporate overall image





**Fig. 6** The imaging TF calculated from Eq. (16) for wavelengths 0.5 and 0.6  $\mu\text{m}$ .

defocus and optical aberrations.<sup>34</sup> Figure 6 shows example TFs illustrating the wavelength dependence of the response.

At the image plane, the coherent superposition of the filtered plane waves results in an imaged light field given by the inverse Fourier transform

$$U_I(x) = \frac{1}{\int df_x} \int \tilde{U}_I(f_x) \exp(i2\pi f_x x) df_x, \quad (18)$$

where we have reused the object-space coordinates  $x, z$ , equivalent to a system without distortion and with unit magnification. The interference fringe intensities are proportional to the real part of this image function

$$I(x) = \text{Re}[U_I(x)], \quad (19)$$

and the calculation of the topography follows from a determination of the interference phase. In practice, determining the phase interferometrically may proceed by any one of a number of ways. However, for the purposes of mathematically modeling the effect of surface topography, it is often enough to calculate the phase directly from

$$\theta_I(x) = -\arg\{U_I(x)\}. \quad (20)$$

The topography measurement for a single wavelength is then

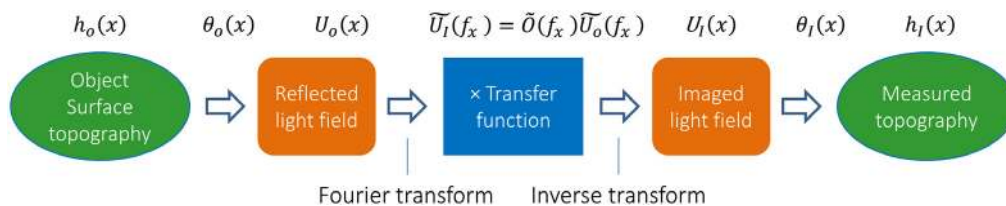
$$h_I(x) = \theta_I(x)/K, \quad (21)$$

and the interference signal strength is proportional to

$$M_I(x) = |U_I(x)|. \quad (22)$$

Figure 7 summarizes the computational steps leading to the topography measurement  $h_I(x)$ .

To extend the EFO model to CSI, an important decision is whether to include both optical spectrum and focus effects in the model. As noted in Sec. 2, the shape of the coherence envelope is a combination of both spectral bandwidth and illumination geometry, implying integrations over multiple incident angles and wavelengths.<sup>39</sup> In what follows, we will assume that the effects



**Fig. 7** The EFO model for a single wavelength.

of the white-light spectrum are dominant. First, we define a light source spectrum that is Gaussian in wavenumber:

$$S(k) = \exp\left[-\frac{1}{2}\left(\frac{k - k_M}{\sigma_k}\right)^2\right]. \quad (23)$$

The mean wavenumber  $k_M$  is the inverse of the central wavelength  $\lambda_M$  of the spectrum, and the standard deviation in wavenumbers  $k$  is given by the approximately equivalent value

$$\sigma_k = \frac{1}{2\sqrt{2 \ln(2)}} \frac{\lambda_\Delta}{\lambda_M^2} \quad (24)$$

for a full-width at half-maximum (FWHM) wavelength bandwidth  $\lambda_\Delta$ . In software simulations, it is often useful to normalize the spectrum  $S$  so that the sum over all  $k$  values is equal to unity.

In the white-light limit of low NA and with a perfectly flat part without tip and tilt, the optical spectrum may be directly associated with the Fourier frequencies using Eq. (14) and by assuming

$$K' = K. \quad (25)$$

The complex values for  $U_I$  of the imaged light field can then be assigned to the Fourier coefficients for FDA:

$$q(x, K) = U_I(x, K). \quad (26)$$

The phases  $\theta$  and magnitudes  $M$  needed for FDA follow from Eqs. (7) and (8). It is therefore feasible in the white-light approximation to model the measured surface profile resulting from an FDA evaluation of a CSI signal, without the need to simulate the signal itself. We call this the direct to FDA method.

The direct to FDA implementation is fast and efficient, but the question remains as to how to simulate the CSI fringe image shown in Fig. 1. This is useful for visualization, but also as a practical matter, for evaluating data processing methods not based on FDA. The signal for each image point follows from the inverse Fourier transform

$$I(z) = \frac{1}{\int dK} \int q(K) \exp(i2\pi Kz) dK. \quad (27)$$

The calculation is simplified by integrating the real value  $q(K)$  over the positive ( $K > 0$ ) frequencies, which is equivalent to summing the interference signal for each of the wavelengths. Table 1 summarized the EFO model for CSI with white light illumination.

The number of wavelengths needed for numerical modeling of the interference signal depends on the range of possible positions of the coherence envelope in the acquired data. Defining this range as  $Z$ , the maximum wavelength spacing to avoid aliasing in the frequency domain is

$$\lambda_\Delta = \Omega \lambda^2 / 2Z. \quad (28)$$

In practice, CSI instruments often store only that portion of the data acquisition scan that includes meaningful interference data while recording the scan offset for each pixel in the image of the object.<sup>27,40</sup> This limits the range  $Z$  in Eq. (28) to  $\sim 5 \mu\text{m}$ , for a maximum wavelength spacing at a mean wavelength of 0.5 of  $0.025 \mu\text{m}$ . For a spectral bandwidth of  $\sim 0.1 \mu\text{m}$ , it is sufficient to use three to five wavelengths near the peak Fourier magnitude for an FDA calculation of surface heights. However, for a signal simulation over a wider range, such as shown in Fig. 1, many more wavelengths may be needed to fully attenuate interference signal contributions outside of the contrast envelope.



**Table 1** Summary of the EFO model for CSI, using FDA for surface profiles.

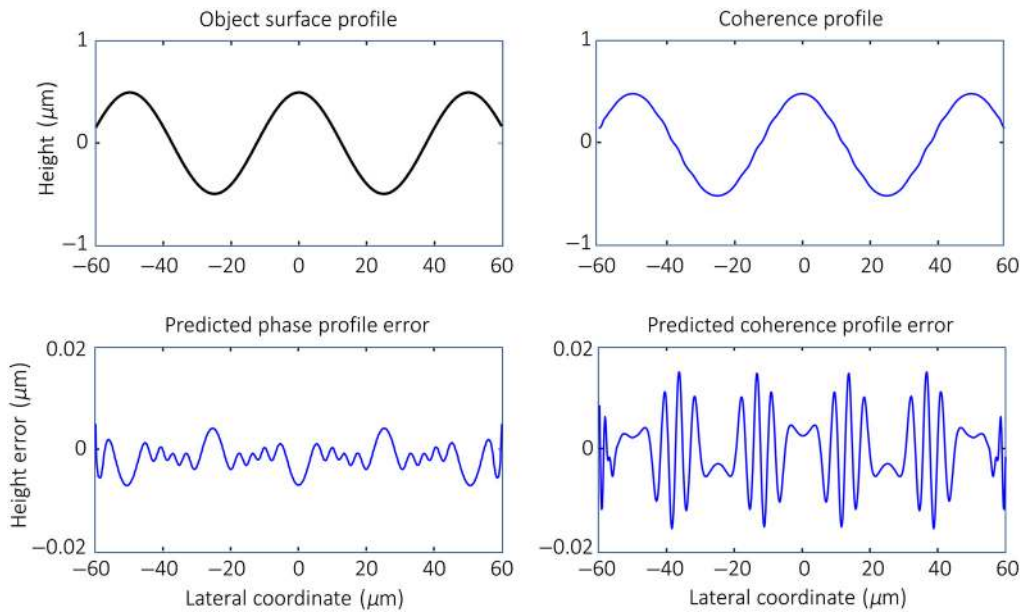
Step	Reference
For each wavelength $\lambda$ in the light source spectrum...	Eq. (23)
Calculate the corresponding fringe frequency $K$ ...	Eq. (2)
Calculate object contribution $U_o$ to the interference effect...	Eq. (12)
Propagate through the optical system using the imaging TF $\tilde{O}$ as a filter...	Eq. (16)
Store complex-valued result $U_l$ as the Fourier coefficient $q$ at this $K$ ...	Eq. (26)
For each imaged pixel $x$ ...	
Extract the phase $\theta$ and magnitude $M$ for the Fourier coefficient $q$ ...	Eqs. (7) and (8)
Unwrap the phase values $\theta$ as a function of $K$ ...	Fig. 4
Perform a weighted least-squares fit to the phase values $\theta$ ...	Fig. 4
Use the phase slope for the coherence profile $h_c$ ...	Eq. (9)
Use the phase offset and slope together from the linear fit for the phase profile $h_\theta$ ...	Eq. (11)
Optional CSI “fringe” signal	
For each imaged pixel $x$ ...	
Inverse transform the Fourier coefficients $q$	Eq. (27)

## 4 Results

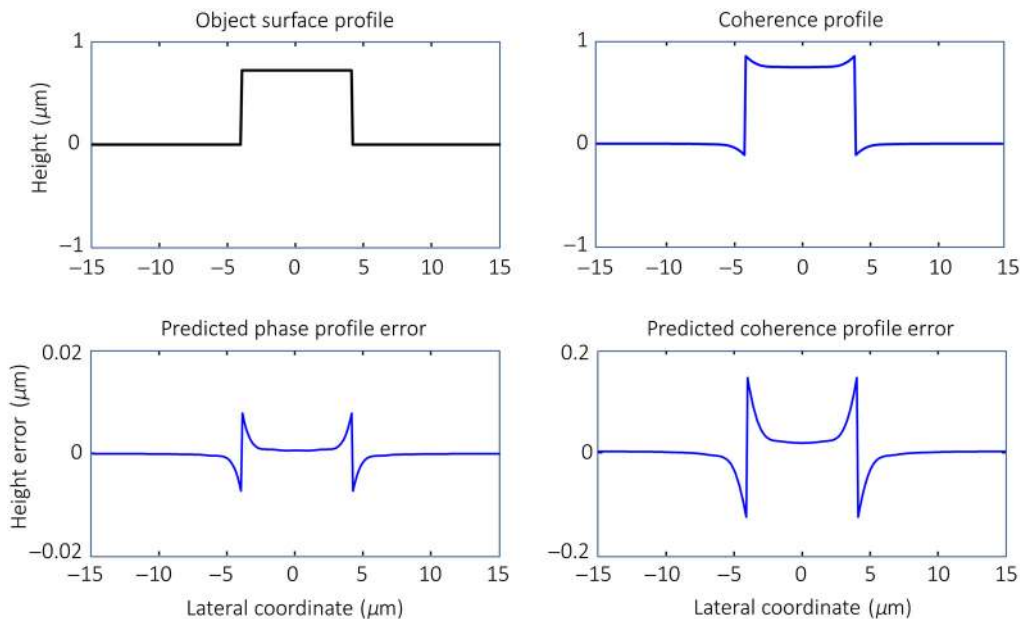
A first example of the modeling is the sinusoidal profile shown in Fig. 1. The simulated results in Fig. 8 show that even in a diffraction limited system, there are small residual errors, particularly for the coherence profile. The example illustrates how a linear diffraction model can be used to predict the kind of nonlinear instrument response often encountered in practice.<sup>9,41,42</sup> These results as well as the other results reported in this section have been confirmed by direct comparison with more advanced models.<sup>9</sup> The errors are a consequence of the bandwidth limits of the imaging TF and are representative of what is observed experimentally.<sup>20,27</sup> For the coherence profile, the larger predicted measurement errors are attributable to the wavelength dependence of TFs.<sup>17,43</sup> This is one of the reasons for preferring the phase profile if the surface is sufficiently smooth.

The difference between the coherence and phase profiles is even more significant when the surface has steep slopes or sharp features that are beyond the specular NA angle limit  $\beta$  of the imaging optics, defined in Eq. (4). Figure 9 shows the predicted behavior for a rectangular surface feature, illustrating the overshoots at sharp edges frequently encountered in CSI.<sup>44</sup> The effect is significantly more pronounced with coherence profiles. This effect is perhaps the most frequently encountered origin of accidental  $2\pi$  errors in the phase profile if the coherence profile is used to determine fringe order. For this reason, software for CSI commonly includes a variety of mitigation strategies, many based on a detailed analysis of the difference between the phase and coherence profiles.<sup>27</sup>

One of the uses of the EFO model is for the evaluation of instrument response as a function of spatial frequencies. This kind of analysis is useful for determining whether an instrument is suitable for measuring the power spectral density of specific surfaces.<sup>45</sup> Figure 10 illustrates such an analysis for an interference microscope measuring sinusoidal surface profiles using phase information. A sequence of simulated profiles is presented to the model, with sinusoidal amplitudes scaled inversely with the spatial frequency, such that the maximum surface slope angle is at 50% of the NA angle limit  $\beta$  for all frequencies. The corresponding amplitudes range from  $12\text{ }\mu\text{m}$  at a frequency of  $0.001\text{ }\mu\text{m}^{-1}$  to  $0.012\text{ }\mu\text{m}$  at  $1\text{ }\mu\text{m}^{-1}$  for an NA of 0.15. Figure 10(a) shows the relative measured amplitude of the sinusoidal input amplitude,



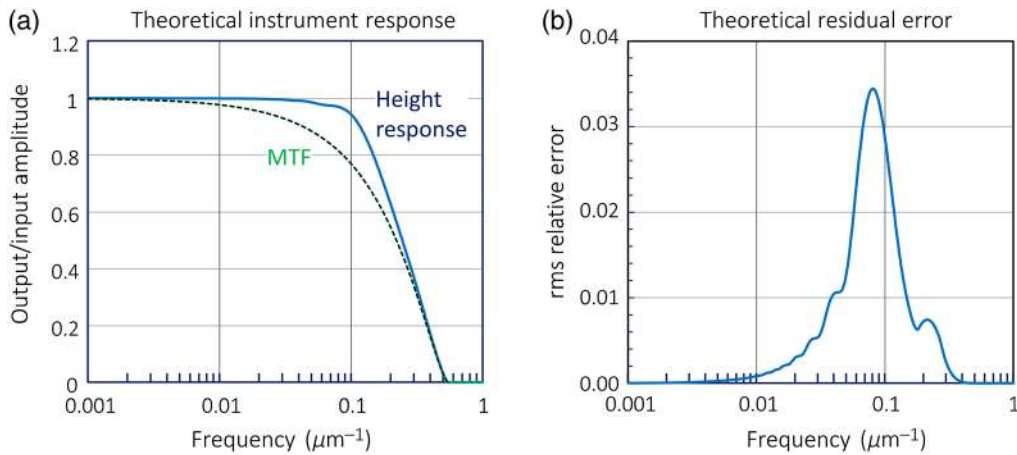
**Fig. 8** Simulated measurement results using the EFO model for the profile of Fig. 1. The sinusoidal period is  $50\ \mu\text{m}$ , and the peak-valley height range is  $1\ \mu\text{m}$ . The mean wavelength is  $0.5\ \mu\text{m}$ , the FWHM bandwidth is  $0.1\ \mu\text{m}$ , and the NA is 0.1.



**Fig. 9** Simulated results using the EFO model for an  $8\text{-}\mu\text{m}$  wide rectangular surface feature with a height of  $0.75\ \mu\text{m}$ . The mean wavelength is  $0.57\ \mu\text{m}$ , the FWHM bandwidth is  $0.12\ \mu\text{m}$ , and the NA is 0.15. Note the  $10\times$  difference in height scale for the predicted errors for the coherence and phase profiles.

whereas Fig. 10(b) shows the rms error in the measured profile at each frequency relative to the input amplitude.

Although not shown in Fig. 10, detailed calculations for other angle limits show that for smaller surface height variations, the response curve approaches that of the MTF for conventional intensity imaging in the same optical system, and the results are almost perfectly linear.<sup>12</sup> Contrarily, for coherence profiles, the height response is nonlinear even for modest slopes and



**Fig. 10** EFO modeling analysis of instrument response as a function of surface spatial frequency for phase profiles, for a constant maximum surface slope equal to 50% of the geometrical NA limit. (a) The results in comparison with the optical imaging MTF and (b) the rms error in the measured profile. The mean wavelength is  $0.57 \mu\text{m}$  and the NA is 0.15.

surface height variations, even though there are many applications involving rough surface textures that are well served by CSI measurement modes based on coherence alone.

Although the results in this section are consistent with what is observed experimentally<sup>27,34</sup> and have been confirmed by comparison with more advanced models,<sup>9</sup> the EFO method has its limits of validity, given the many geometrical approximations built into the model. Quantifying these limits is the topic of the next section.

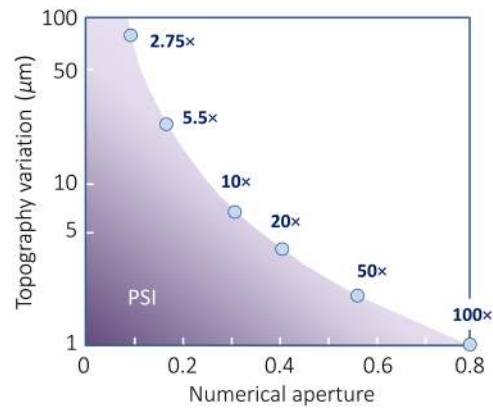
## 5 Limits of Applicability for EFO Modeling

The approximation of a 2D complex-valued aperture function in place of the 3D topography assumes that all surface points in the topography are at the same focus position.<sup>32–34</sup> This gives rise to the DOF limitation for fixed-focus systems, such as PSI microscopes, noted already in Sec. 3. The Rayleigh formula for the DOF is

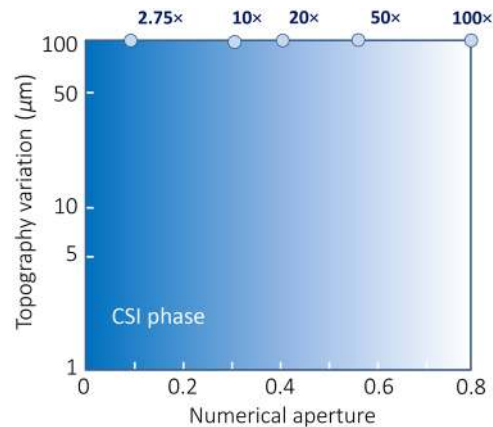
$$D_{\text{field}} = \lambda / A_N^2. \quad (29)$$

This number is one-half the focus range, but for the purpose of specifying an approximate limit for the EFO, we use  $D_{\text{field}}$  as the total allowable range of surface heights. To make this more meaningful in practice, the graph in Fig. 11 shows the DOF as a function of NA with several example magnifications for common interference microscope objectives. It is worth observing that typical 100 mm aperture laser-Fizeau interferometers have an NA of  $<0.01$ . Given the limitations on resolvable fringe density, there is no practical surface height range limit for continuous surfaces below 0.1 NA for use with EFO modeling of laser Fizeau interferometers, provided that the field curvature matches that of the part to within a few millimeters. For this reason, EFO modeling is common for optical design and tolerancing,<sup>46,47</sup> and digital holographic refocusing is possible using 2D propagators.<sup>48</sup>

For CSI, the limitations of EFO modeling are relaxed and at the same time more restricted than for fixed focus monochromatic interferometry. In most implementations of CSI, the focus position and the position of peak fringe contrast are coincident and are scanned together.<sup>1</sup> The measurement principle has the significant benefit that every point on the object surface is measured at the same focus position.<sup>49</sup> This practical benefit also means that the DOF limitation for application of the EFO can be relaxed, at least for measurements based on interference phase. The CSI scan enables a piecewise evaluation across the field of view, equivalent to collapsing the entire surface topography into the thin complex-valued aperture function of the EFO model, even if the surface height range is much larger than the DOF. We have verified this phenomenon by direct comparison with a more advanced 3D model developed in detail in Ref. 50 and that we



**Fig. 11** Limits to the allowable surface height variation for the use of the EFO model for a fixed-focus (nonscanning) system based on the DOF. The graph includes representative magnifications for common interference objectives.



**Fig. 12** Limits to applicability of the EFO model for CSI when using phase information to calculate surface heights.

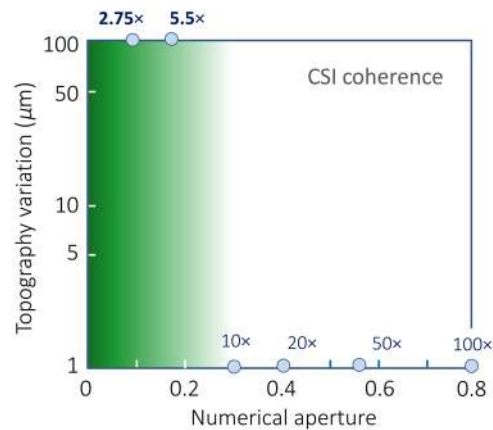
will briefly describe here in Sec. 6. Figure 12 summarizes this finding for phase profiles in CSI, with applicability for the model over all height ranges and NA values. The progressively lighter shading is a qualitative representation of declining confidence in the result at higher NA values, given polarization-dependent material effects at large incident angles, and the use of scalar diffraction theory.

The situation is less encouraging for measurements using coherence. The white-light EFO model for CSI described in this paper assumes that the coherence envelope is shaped uniquely by the broad spectral bandwidth of the light source; whereas it is well known that at high NA values, the envelope changes in width and overall shape as a consequence of the range of illumination angles.<sup>25,39,51</sup> Consequently, a constraint for the extended height range for simple EFO modeling in CSI is that the coherence length of the illumination should be much less than the depth of field  $D_{\text{field}}$ . A comparison of the EFO model presented here with more advanced methods with fewer geometrical approximations shows that “much less” is approximately a factor of five if the intent is to accurately predict residual measurement errors in the coherence profile. This requirement can be written as

$$\sigma_C < D_{\text{field}}/5, \quad (30)$$

where the coherence length is

$$\sigma_C = 1/\sigma_k. \quad (31)$$



**Fig. 13** Limits to applicability of the EFO model for CSI for coherence profiles using common light sources. The white light approximation is limited to low NA values characteristic of objective magnifications below 10 $\times$ .

As a practical example, assuming the coherence length is 2  $\mu\text{m}$  for a 0.57- $\mu\text{m}$  light source with a 0.12- $\mu\text{m}$  FWHM spectral bandwidth and scales inversely with the bandwidth. Figure 13 summarizes this limit, where the shading once again is indicative of declining confidence in the result with increasing NA and corresponding objective magnifications.

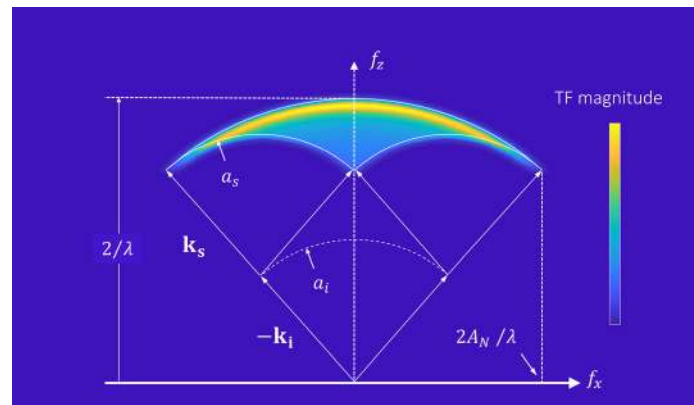
Importantly, the limitations on NA for simulating coherence profiles in CSI are not relaxed in the limit of small surface height variations, as they are for fixed-focus measurements based on interference phase. In essence, above a certain illumination NA value, EFO modeling is simply not suited to the task of simulating the complete CSI signal well enough to predict the coherence profile results, regardless of the range of surface height variations.

The limitations of the EFO model for CSI at high NA can be overcome by abandoning the obliquity factor approximation and considering the diffracted wavefronts as a function of incident angle, using pupil-plane integration.<sup>37</sup> A limit case for this method is the modeling of a monochromatic, high-NA system, for which the Fourier coefficients in the FDA method map to directional cosines, rather than spectral wavenumbers.<sup>25</sup> However, to account for both spectral bandwidth and measurement geometry correctly, the most accurate method is to integrate over the pupil plane the diffracted plane waves for each incident plane wave in the illumination.<sup>34</sup> Although this is a useful approach and can be applied to nonlinear diffraction problems such as optically unresolved surface features,<sup>52</sup> clearly the simplicity and ease of implementation of the EFO model is lost, and it becomes compelling to start fresh with a more realistic 3D imaging solution.

## 6 3D Models

Conventional Fourier optics methods are based on 2D TFs along the lateral spatial  $f_x, f_y$  frequency axes, with propagation and modification of wavefronts expressed in terms of planar representations of light fields. Models based on 3D TFs in  $f_x, f_y$ , and  $f_z$  are common in microscopy,<sup>53</sup> particularly confocal microscopy, and high lateral resolution systems.<sup>54</sup> The formalism for 3D TFs can be equally well applied to holography and interferometry<sup>55</sup> and is of interest in any high-NA system for which focus effects strongly influence the outcome of a measurement, including CSI.<sup>50,56,57</sup>

Linear 3D models have a rigorous foundation in diffraction theory;<sup>50,54</sup> however, for our present purpose, we consider just the geometrical aspects of 3D TFs. Figure 14 shows the  $f_x, f_z$  cross section of a 3D TF for spatially incoherent, monochromatic epi illumination in an interference microscope. The key difference of this figure with respect to the more familiar representation shown in Fig. 6 is the addition of the vertical axis  $f_z$  to the lateral  $f_x$  axis, with the consequence that the TF magnitude is now represented by a color map. The 2D TF shown in



**Fig. 14** Geometrical construction of the cross section of a 3D-TF in monochromatic light with a linear pupil.

Fig. 6 is equivalent to integrating the image shown in Fig. 14 along the  $f_z$  direction for each position along the  $f_x$  axis.

The construction of Fig. 14 starts by defining incident wavevectors  $\mathbf{k}_i$  and scattered wavevectors  $\mathbf{k}_s$ . These wavevectors have a length given by the spectral wavenumber  $k = 1/\lambda$  and are oriented according to their incident and scattered angles. The range of incident angles for  $\mathbf{k}_i$  sweeps out an arc  $a_i$  consistent with the geometry of the illuminating light cone for a system having a pupil filled with spatially incoherent light. For each of these incident wavevectors  $\mathbf{k}_i$ , there is an arc  $a_s$  of scattered wavevectors  $\mathbf{k}_s$  limited by the acceptance cone of the imaging system. The combination of these two arcs defines the range of possible  $f_x, f_z$  values that are detectable using interferometry. By sweeping both the  $\mathbf{k}_i$  and  $\mathbf{k}_s$  vectors through all possible angles, we obtain the 3D TF, with a magnitude distribution proportional to the number of ways in which these vectors can be oriented to reach the same  $f_x, f_z$  point in frequency space.

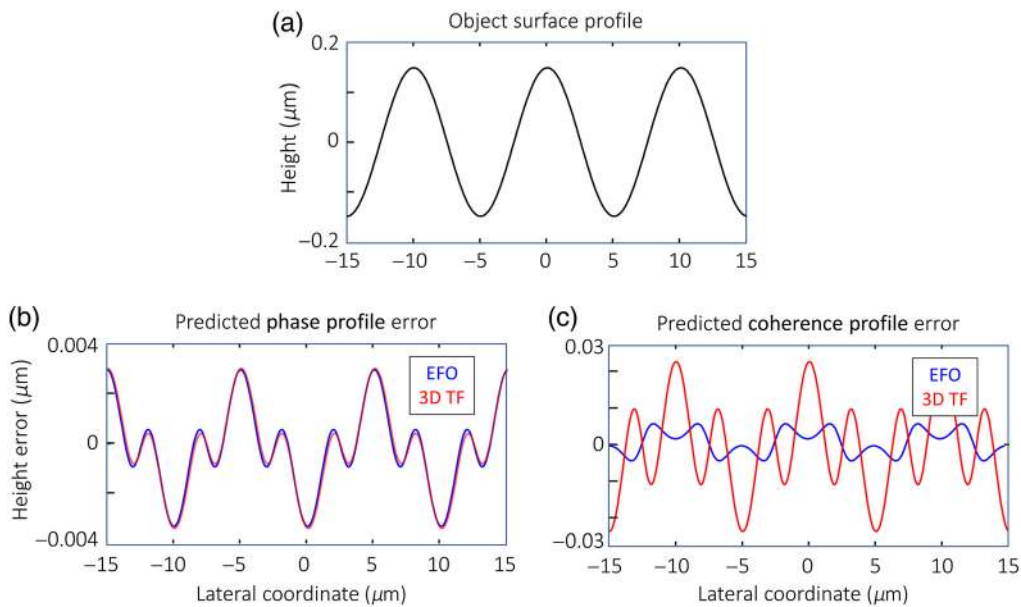
The 3D TF allows us to predict the frequency content of a signal, such as the one shown in Fig. 1, for an object surface modeled as a thin “foil” or point cloud of scattering points in  $x, y, z$ .<sup>32,58</sup> The 3D TF can be measured experimentally by realization of the 3D point spread function using a small sphere, which scatters light in every direction.<sup>56</sup> The resulting detected signal will have a frequency content close to that of the 3D TF. This method has been used to calibrate interferometers and to correct for defocus, aberrations, and tilt-dependent errors.<sup>14,59,60</sup>

An approach to understanding the 3D TF is to observe its frequency limits. Along the lateral  $f_x$  axis, the boundaries are given by the Abbe frequency, exactly as in Eq. (17). Along the vertical  $f_z$  axis, we have a range of possible interference fringe frequencies, with the maximum possible frequency for normal incidence and specular reflection of  $2/\lambda$ . For every other frequency within the boundaries of the 3D TF, there are differing fringe frequency contributions along the  $f_z$  axis and lateral spatial frequencies along the  $f_x$  axis. For white-light illumination, the superposition of wavevector lengths of differing lengths blurs the TF and extends its boundaries along the  $f_z$  direction, without departing from the overall “umbrella” shape shown in Fig. 14.

In the simplest EFO modeling, the use of the obliquity factor  $\Omega$  defined by Eqs. (2) and (3) is equivalent to averaging the frequency projections along the vertical  $f_z$  axis so that we can use linear 2D TFs. In this approximation, we lose all of the detail of the 3D TF regarding the variation in possible  $f_z$  values as a function of  $f_x$ . At low NA values, this is not serious: in the limit of very small NA, the cross section of the 3D TF would appear as a broad line parallel to the lateral  $f_x$  axis shown in Fig. 14, with a magnitude distribution given by the TF shown in Fig. 6. However, at high NA values, the shape of the 3D TF is not well represented by this obliquity factor approximation.

The practical difference in signal simulation between 2D and 3D TFs at high NA is illustrated in the example of Fig. 15, which shows the predicted measurement error for a sinusoidal profile. For the phase profile, the approximations in EFO modeling with an obliquity factor are acceptable; whereas for the coherence profile, which is much more dependent on the signal shape rather than its mean phase, the EFO model underestimates the error. This is consistent with the limits of

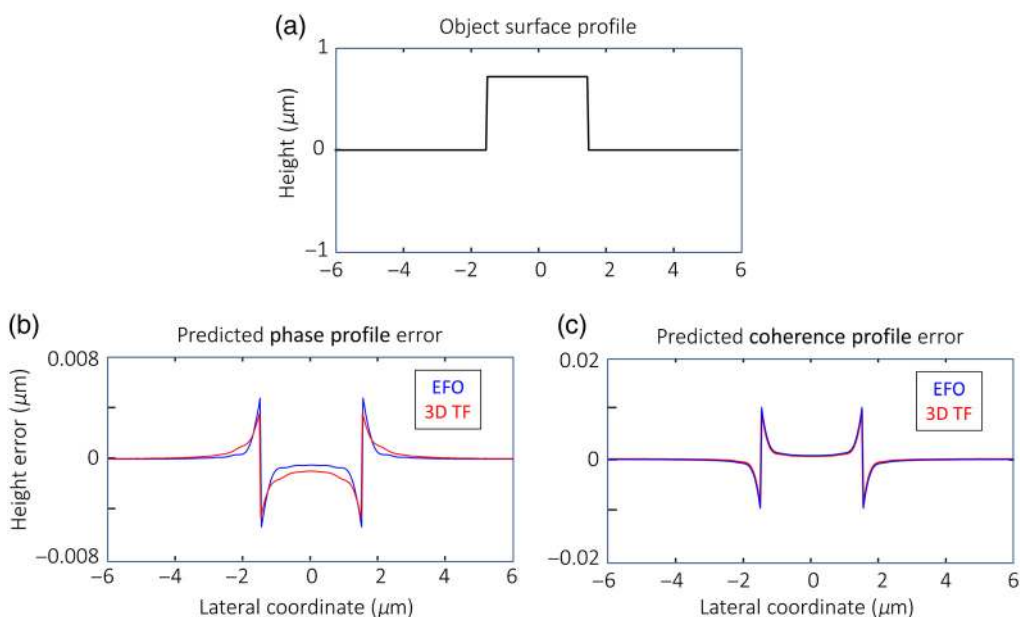




**Fig. 15** (a) Simulations for the EFO and 3D TF models at  $\text{NA} = 0.55$  (50 $\times$  objective) for a sinusoidal profile with an amplitude of  $0.15 \mu\text{m}$ . The mean wavelength is  $0.57 \mu\text{m}$  and the FWHM bandwidth is  $0.08 \mu\text{m}$ . The predicted measurement errors for (b) the phase profile and (c) the coherence profile.

applicability described in Sec. 5, which have been verified by comparison with a virtual CSI model based on 3D TFs.<sup>9</sup>

There are some specific surface structures for which the EFO method provides a good approximation outside the NA guidelines described in Sec. 5. Figure 16 illustrates this with the predicted measurement errors for a rectangular profile. The results show a good match of the predictions of the EFO model to the 3D TF model, even though the NA of 0.55 is larger than the 0.2 limit to the NA indicated by Fig. 13. This illustrates that for rectangular features,



**Fig. 16** (a) Simulations for the EFO and 3D TF models  $\text{NA} = 0.55$  (50 $\times$  objective), for a rectangular profile similar to that shown in Fig. 9, with a width of  $3 \mu\text{m}$  and a height of  $0.75 \mu\text{m}$ . The mean wavelength is  $0.57 \mu\text{m}$  and the bandwidth is  $0.14 \mu\text{m}$ . The predicted measurement errors for (b) the phase profile and (b) the coherence profile.

the dominant source of measurement error is the loss of lateral spatial frequencies because of the bandwidth limits of optical filtering. This mechanism is not as sensitive to the shape of the TF as other structures; however, the results in Fig. 15 show that we cannot rely on this for more general surface topography.

## 7 Summary and Future Work

Modern interference microscopes for surface topography measurement often employ coherence scanning methods with spectrally broadband light sources to extend the measurement range beyond one interference phase cycle. Within well-defined limits, a Fourier optics model, using familiar concepts from conventional imaging systems analysis, can predict the interference signals and measured surface profiles for these instruments. A defining simplification is the modeling of the surface topography as a complex-valued reflecting aperture function for which the surface heights are encoded as phase shifts—a common concept for topography measurement using interferometry. With this approximation in hand, we propose the EFO model summarized by Table 1 for CSI signals and measurement results.

Practical uses for EFO models include evaluating instrument response for the specification of lateral resolution and frequency response.<sup>12</sup> Using the EFO model presented here, we also find that errors in CSI microscopy encountered in practice can often be attributed to the wavelength dependence of the imaging TF, even for diffraction-limited optical systems, particularly when using the fringe contrast envelope to measure surface heights. Software developments since the discovery of CSI three decades ago target these error sources, but it is nonetheless useful to predict their magnitude using simplified data processing, to minimize their influence when setting up the instrument for specific measurement.

We find that the instrument response when using interference phase is adequately represented by the EFO model for the most commonly used interference objectives; however, there are limitations to the accuracy of the model at higher NA values, especially when using the fringe contrast to measure surface heights. In all cases, we find that a full 3D model is more reliable because it has fewer geometrical approximations, with the greatest benefit at NA values above 0.2.

The several additional simplifying assumptions of both 2D and 3D modeling as presented here, including scalar diffraction, optically smooth surfaces (relative to wavelength), neglect of material and polarization effects, and the absence of thin partially transparent surface films, provide opportunities for further work. These developments help with obtaining the most realistic results from existing instruments while generating ideas for new methods and techniques for optical noncontact areal surface topography measurements.

## Acknowledgments

This project was received partial funding from the EMPIR Program (No. 20IND07) co-financed by the Participating States and from the European Union's Horizon 2020 research and innovation program.

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