

Modeling of phase volume diffractive gratings, part 2: reflecting sinusoidal uniform gratings, Bragg mirrors

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Abstract. A detailed model of diffraction of plane and Gaussian beams on plane uniform phase Bragg gratings based on a Kogelnik's theory of coupled waves is presented. The model describes reflecting gratings (Bragg mirrors) with arbitrary orientation in a plane-parallel plate having no material losses. It takes into account spectral width and angular divergence of laser beams. The results of modeling are compared with experimental data for Bragg mirrors in a photo-thermo-refractive glass. © 2012 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: [10.1117/1.OE.51.5.058001](https://doi.org/10.1117/1.OE.51.5.058001)]

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1 Introduction

A detailed model of diffraction of plane and Gaussian beams on plane uniform phase Bragg gratings based on a Kogelnik's theory of coupled waves is presented. The model describes reflecting gratings (Bragg mirrors) with arbitrary orientation in a plane-parallel plate having no material losses. It takes into account spectral width and angular divergence of laser beams. The results of modeling are compared with experimental data for Bragg mirrors in a photo-thermo-refractive (PTR) glass.

Wide applications of volume Bragg gratings (VBG) in optics and photonics require comprehensive practical knowledge of such optical elements. In spite of Kogelnik's theory of coupled waves¹ developed about 40 years ago, no reduction to practical formulae enabling precise design of VBGs has been provided up to today. VBGs in the case of a monochromatic plane wave were also treated in detail in Ref. 2, which considers Fresnel reflections and the added effects of composite VBGs such as using two VBGs to form a Fabry-Perot cavity, but also does not address a reduction to practical formulae for designers.

A detailed modeling of the diffraction of plane monochromatic waves along with divergent and polychromatic beams

on transmitting volume gratings on the basis of Kogelnik's theory¹ was published in Ref. 3. The effect of finite divergence on thick grating performance has been previously described in Refs. 4 and 5. This paper extends the results of the previous works to a modeling of the diffraction on reflecting volume gratings (Bragg mirrors) describing simultaneously divergent and polychromatic beams where Kogelnik's theory is reduced to practical formulae which are necessary for design of diffractive optical elements based on VBGs.

A uniform phase grating is a structure produced by periodical distribution of the refractive index modulation inside the volume of a photosensitive medium, as shown in Fig. 1. Each structure recorded inside a slab with plane-parallel surfaces could be considered as either transmitting or reflecting Bragg grating depending on the orientation of a readout beam in regard to the front surface. Dotted and dashed arrows in Fig. 1 correspond to a beam tracing for transmitting and reflecting grating geometry; solid arrows are the wave vectors of beams and the grating vectors. As was noted in Ref. 3, uniform sinusoidal VBGs could be entirely described by the following set of parameters: the grating thickness t , the average refractive index of a medium n_{av} , the amplitude of refractive index modulation δn , the grating period Λ (or spatial frequency $f = 1/\Lambda$), and the grating inclination angle φ between the normal to the grating front surface \mathbf{N}_f and the grating vector \mathbf{K}_G .

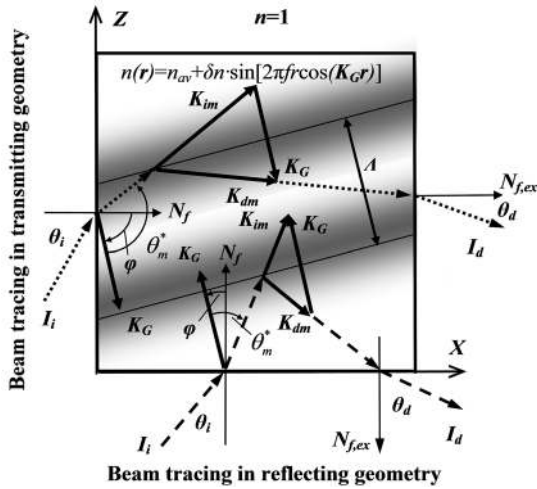


Fig. 1 Propagation of optical rays through a volume Bragg grating in transmitting (dotted lines) and reflecting (dashed lines) geometry. \mathbf{N}_f and $\mathbf{N}_{f,ex}$ = normal to the front surface for incident (I_i) and diffracted (I_d) beams; $\mathbf{K}_{im}, \mathbf{K}_{dm}$ = wave vectors of incident and diffracted beams inside the grating medium; \mathbf{K}_G = Grating vector; φ = grating inclination; θ_i, θ_d = incident and diffraction angles; θ_m^* = incident Bragg angle.

The grating vector \mathbf{K}_G is normal to the planes of a constant refractive index, has a module $|\mathbf{K}_G| = 2\pi f$, and is directed inside a medium.¹ It is important to emphasize that a sinusoidal volume grating itself has a double degeneration of grating vector directions due to its symmetry. Therefore, the definition of a grating vector in a diffractive optical element is based on its orientation with respect to the front surface of the element, though the process of diffraction does not depend on what surface was crossed by an incident beam. This feature of sinusoidal gratings results in different orientation of grating vector depending on what surface of a photosensitive plate was chosen as a front one. For example,

according to the definition given above (introduced by Kogelnik¹), the volume grating depicted in Fig. 1 is a transmitting grating for short-wavelength radiation (large wave vector) which crosses the left vertical surface (front surface for this beam). The vector of this grating for this beam is directed down to the bottom of this figure. The same grating is a reflecting one for long-wavelength radiation (small wave vector) which crosses the bottom surface (front surface for this beam). The vector of this grating for this beam is directed to the top of the figure. An inclination angle of grating φ is the angle between the normal to the front surface \mathbf{N}_f and the grating vector \mathbf{K}_G . It is positive in a counter-clockwise direction and can vary from $-\pi/2$ to $+\pi/2$. Therefore, a transmitting grating excited through the left vertical side has a negative inclination. The same grating excited through the bottom horizontal side is a reflective one and has a positive inclination.

Following the approach proposed in Refs. 1 and 3, we use the incident Bragg angle in a medium θ_m^* , which is the angle between a grating vector \mathbf{K}_G and a wave vector \mathbf{K}_{im} of an incident beam inside the medium. Let us note again that incident Bragg angle θ_m^* differs from a conventional Bragg angle in the media θ_m , and the relationship between these parameters is $\sin \theta_m = |\cos \theta_m^*|$. While there are two orders of Bragg diffraction in an infinite sinusoidal grating,¹ there are four possible orders of Bragg diffraction in sinusoidal grating recorded in a plane parallel plate.³ The positive orders of Bragg diffraction are for incident Bragg angle $0 < \theta_m^* < +\pi$, while the negative orders are for $-\pi < \theta_m^* < 0$. The forward orders of Bragg diffraction are for a module of an incident Bragg angle $|\theta_m^*| < \pi/2$, while the backward orders are for $|\theta_m^*| > \pi/2$. For transmitting geometry (dotted arrows) shown in Fig. 1, an incident Bragg angle is positive and $|\theta_m^*| > \pi/2$. This means that this is a positive backward Bragg order. For the same grating that is used in a reflecting geometry (dashed arrows) for longer wavelengths, an incident Bragg angle for a beam coming

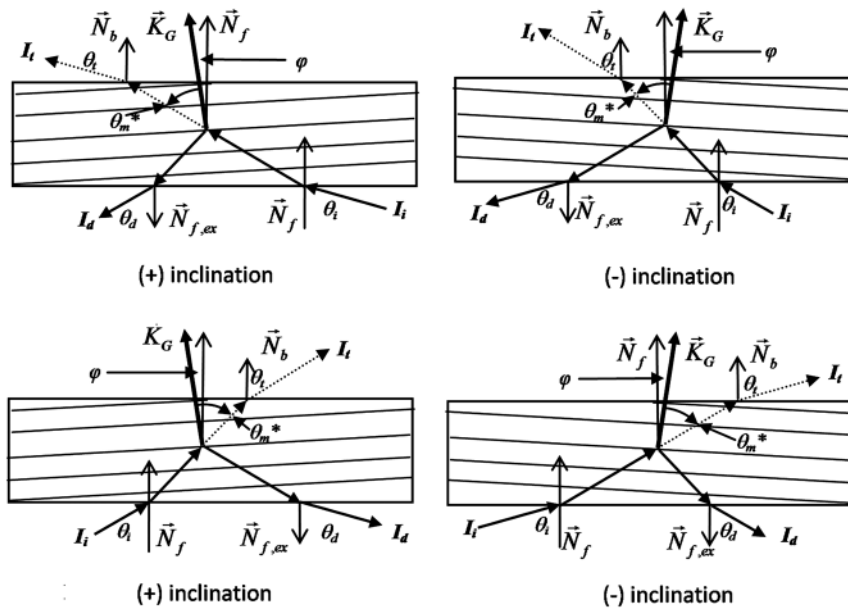


Fig. 2 Possible orders of Bragg diffraction for reflecting gratings with different angles of inclination. $I_i, I_t,$ and I_d = incident, transmitted, and diffracted beams; \mathbf{K}_G = grating vector; φ = grating inclination; $\theta_i, \theta_t,$ and θ_d = angles of incidence, transmission, and diffraction; θ_m^* = incident Bragg angle.

from approximately the same direction is negative and $|\theta_m^*| < \pi/2$; this is a negative forward Bragg order. It is important to note that for forward orders of diffraction, the wave vector of a diffracted beam \mathbf{K}_{dm} is the difference between the wave vector of an incident beam \mathbf{K}_{im} and the grating vector \mathbf{K}_G , while for backward orders the wave vector of a diffracted beam \mathbf{K}_{dm} is the sum of the wave vector of an incident beam \mathbf{K}_{im} and the grating vector \mathbf{K}_G .³

Figure 2 shows the Bragg diffraction for reflecting VBGs (Bragg mirrors) with different inclination angles φ . One can see that scanning of the incident angle results in switching between plus and minus orders only. This is the opposite of transmitting gratings, where scanning of an incident angle results in switching between forward and backward orders.³ Similar to conventional mirrors, a positive sign of the incident angle corresponds to a negative sign of the exit diffraction angles for reflecting VBGs. Also, a change of the sign of the Bragg mirror inclination does not change the sign of a Bragg order.

Regardless of the VBG geometry, the basic relationship between Bragg wavelength λ_0 and incident Bragg angle θ_m^* is determined by the Bragg condition as

$$\frac{\lambda_0}{n_{av} |\cos \theta_m^*|} = 2\Lambda. \quad (1)$$

Contrary to transmitting gratings, where $|\theta_m^*|$ is close to $\pi/2$ and the wavelength of reading radiation is significantly less in comparison to the grating period, for reflecting gratings θ_m^* is close to zero and the wavelength of reading radiation is comparable to the grating period. For each grating period, there is the maximum wavelength λ_0^{\max} , which corresponds to normal beam incidence on a reflecting Bragg grating, that is, at $\theta_m^* = 0$,

$$\lambda_0^{\max} = 2n_{av}\Lambda. \quad (2)$$

Radiation with wavelength exceeding λ_0^{\max} cannot be diffracted by this particular grating at any conditions of excitation. Radiation with shorter wavelengths can be reflected by a Bragg mirror at larger angles of incidence.

2 Diffraction of Plane Monochromatic Waves on a Transmitting Bragg Grating

Diffraction efficiency (DE) of a reflecting Bragg grating that has no material losses is described by the following formula if ξ and S are considered to be real positive numbers and $\xi > S$ (Ref. 1). This equation also appears in the theory for fiber Bragg gratings.^{6,7}

$$\eta = \frac{\sin^2 \sqrt{\xi^2 - S^2}}{\xi^2/S^2 - \cos^2 \sqrt{\xi^2 - S^2}}. \quad (3)$$

Here S and ξ are the same phase incursion, also called grating strength, at Bragg condition and dephasing parameter at certain detuning from Bragg condition as they were described in Ref. 3 for transmitting gratings. However, there is a distinctive feature between transmitting and reflecting gratings: the inclination factor, $F_\varphi = [-\cos(\varphi - \theta_m^*) \cos(\varphi + \theta_m^*)]^{1/2}$, is a real number for transmitting gratings and an imaginary number for reflecting ones because the incident Bragg angle θ_m^* is close to $\pi/2$ and to zero, respectively. Therefore, in order to

maintain the phase incursion S as a real-valued parameter, it should be redefined for reflecting VBGs as:

$$S = \frac{i\pi t \delta n}{\lambda_0 F_\varphi}. \quad (4)$$

For unslanted reflecting grating $\varphi = 0$, and the phase incursion S becomes:

$$S_0 = \frac{\pi t \delta n}{\lambda_0 |\cos \theta_m^*|} = \frac{2\pi n_{av} t \delta n}{\lambda_0^2 f}. \quad (5)$$

Similarly, when small angular deviations $\Delta\theta_m$ from an incident Bragg angle θ_m^* and/or small deviations $\Delta\lambda$ from central wavelength λ_0 occurred, dephasing parameter ξ for reflecting gratings should be redefined for keeping it positive by changing of the sign in Eq. (6).³ The resulting dephasing parameter becomes:

$$\xi = \frac{\pi f t \cos(\theta_m^*)}{\cos(\varphi - \theta_m^*) - \frac{f\lambda_0}{n_{av}} \cos(\varphi)} \left[\Delta\theta_m \frac{\sin(\theta_m^*)}{\cos(\theta_m^*)} + \frac{\Delta\theta_m^2}{2} + \frac{\Delta\lambda}{\lambda_0} \right]. \quad (6)$$

Kogelnik's dephasing parameter, $-\Delta\theta_m \sin(\theta_m^*) + \frac{f}{2n_{av}} \Delta\lambda$, is the result of a first-order Taylor series approximation of $\cos(\theta_m^* + \Delta\theta_m) + \frac{f}{2n_{av}} (\lambda_0 + \Delta\lambda)$. However, this approximation will not be valid if the Bragg angle is set to near normal incidence, as $\sin(\theta_m^*) \approx 0$ in this case. Therefore, one has to use the second term in the approximation.

Let us assume that for unslanted ($\varphi = 0$) reflecting VBGs the incident beam corresponds to the angular Bragg condition (i.e., $\Delta\theta_m = 0$), but there is some spectral deviation $\Delta\lambda$ from exact Bragg wavelength λ_0 . In this case, one can write a formula for dephasing parameter ξ from Eq. (6) by considering the Bragg condition [Eq. (1)]:

$$\xi_0 = \frac{2\pi n_{av} t \Delta\lambda}{\lambda_0^2 |\cos \theta_m^*|} = \frac{\pi f t \Delta\lambda}{\lambda_0}. \quad (7)$$

Spectral selectivity of such unslanted grating could be derived by substitution of Eqs. (5) and (7) to Eq. (3)

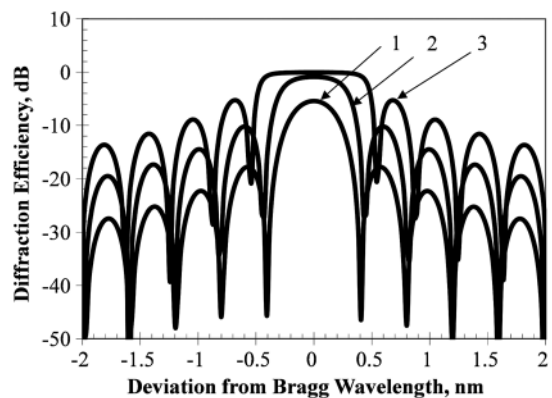


Fig. 3 Dependence of diffraction efficiency of a reflecting VBG on deviation from resonant wavelength $\lambda_0 = 1085$ nm. Normal incidence, thickness 1 mm, average refractive index $n_{av} = 1.4867$. Refractive index modulation, ppm: 1 = 200, 2 = 500, 3 = 1000.

when the mismatching from the exact Bragg wavelength λ_0 of $\Delta\lambda$ occurs. The selectivity could be described in the terms of Bragg grating parameters:

$$\eta = \frac{\sin^2 \sqrt{\left(\frac{2\pi n_{av} t \delta n}{\lambda_0^2 f}\right)^2 - \left(\frac{\pi f t \Delta\lambda}{\lambda_0}\right)^2}}{\left(\frac{\lambda_0^2 \Delta\lambda}{2n_{av} \delta n}\right)^2 - \cos^2 \sqrt{\left(\frac{2\pi n_{av} t \delta n}{\lambda_0^2 f}\right)^2 - \left(\frac{\pi f t \Delta\lambda}{\lambda_0}\right)^2}}. \quad (8)$$

Figure 3 shows the dependence of diffraction efficiency (reflection coefficient) on spectral detuning from Bragg wavelength for 1-mm-thick reflecting Bragg grating for three different values of refractive index modulation δn . If δn is decreasing, the spectral selectivity is narrowing and the maximal DE decreases. A reflecting VBG at Bragg condition ($\Delta\theta_m = \Delta\lambda = 0$) has a dephasing parameter $\xi = 0$, and the maximal DE can be simplified from Eq. (3):

$$\eta_0 = \tanh^2 S_0 = \tanh^2 \frac{\pi t \delta n}{\lambda_0 |\cos \theta_m^*|}. \quad (9)$$

Following the hyperbolic tangent function, diffraction efficiency η_0 asymptotically approaches the 100% value by increasing of grating thickness and/or refractive index modulation.

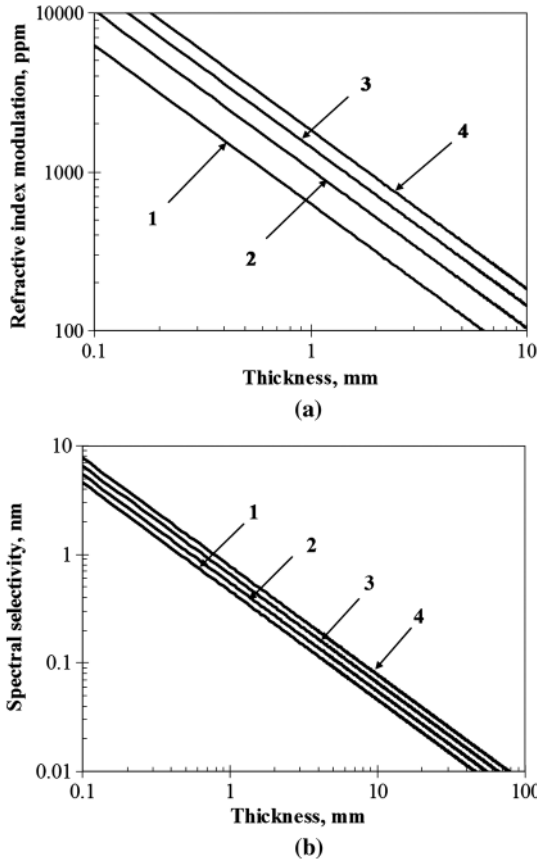


Fig. 4 Interrelationship between grating parameters and spectral selectivity for predetermined diffraction efficiency of VBG: 1 = 90%, 2 = 99%, 3 = 99.9%, 4 = 99.99%. Normal incidence, $\lambda_0 = 1085$ nm, $n_{av} = 1.4867$. (a) Refractive index modulation versus thickness. (b) Spectral selectivity at HWFZ versus thickness.

Let us note that if the desired diffraction efficiency η_0 could be predetermined at a certain level, it would serve as one of the basic parameters for a design of a reflecting VBG. To achieve this specified diffraction efficiency, interrelationships between thickness, refractive index modulation, and incident Bragg angle θ_m^* could be derived from Eq. (9):

$$\delta n = \frac{\lambda_0 |\cos \theta_m^*| \operatorname{atanh} \sqrt{\eta_0}}{\pi t_0}. \quad (10)$$

Figure 4(a) illustrates this interrelation [Eq. (10)] for four DE values: 90%, which corresponds to 10 dB of attenuation of a transmitted beam; 99% (20 dB); 99.9% (30 dB); and 99.99% (40 dB), at $\lambda_0 = 1085$ nm for $\theta_m^* = 0$ (normal incidence). It can be noted that refractive index modulation δn becomes less than 1000 ppm for securing the diffraction efficiency level of $\eta_0 = 99\%$ (20 dB attenuation) only when a VBG thickness is more than 1 mm. Therefore, reflecting VBGs should be thick enough to achieve efficient reflection at relatively low values of refractive index modulation.

One can conclude that unslanted reflecting VBGs can be fully described by a combination of any two out of three grating parameters: thickness, refractive index modulation, and diffraction efficiency that should be predetermined for a particular incident Bragg angle θ_m^* at a wavelength λ_0 .

To determine spectral selectivity, Eq. (3) should be equaled to zero. Because $\xi \neq S$ (otherwise we have a function singularity at this point), diffraction efficiency reaches its zero value at multiple points:

$$(\xi^2 - S^2)^{1/2} = j\pi, \quad \text{where } j = 1, 2, \dots, n, \dots \quad (11)$$

Generally, spectral selectivity at a half width at first zero (HWFZ) level, $\delta\lambda^{\text{HWFZ}}$, is defined by substitution of Eqs. (4) and (6) into Eq. (11) at $j = 1$. However, the general result can be simplified for unslanted reflecting VBGs with maximal DE η_0 by substitution of S_0 and ξ_0 from Eqs. (7) and (9) to Eq. (11):

$$\begin{aligned} \delta\lambda^{\text{HWFZ}} &= \frac{\lambda_0^2 \left[(\operatorname{atanh} \sqrt{\eta_0})^2 + \pi^2 \right]^{1/2}}{2\pi n_{av} t |\cos \theta_m^*|} \\ &= \frac{\lambda_0 \left[(\operatorname{atanh} \sqrt{\eta_0})^2 + \pi^2 \right]^{1/2}}{\pi f t}. \end{aligned} \quad (12)$$

Assessment of typical values of spectral selectivity $\delta\lambda^{\text{HWFZ}}$ for $\eta_0 = 99.0\%$, $\lambda_0 = 1085$ nm, $n_{av} = 1.485$, and $\theta_m^* = 0$ gives the following formula:

$$\delta\lambda^{\text{HWFZ}} [\text{nm}] \cong \frac{0.55}{t [\text{mm}]}. \quad (13)$$

It is clear that this simple expression can be easily derived for any particular wavelength. It is necessary to point out that refractive index modulation δn has to follow any changing of thickness for securing the diffraction efficiency value of η_0 . Figure 4(b) illustrates the interrelation between spectral selectivity $\delta\lambda^{\text{HWFZ}}$ and grating thickness t that is necessary to achieve for different diffraction efficiency values: the

thicker the grating, the narrower the spectral selectivity. One can see that a spectral selectivity $\delta\lambda^{\text{HWFZ}} \sim 0.1$ nm could be achieved for a 5.5-mm-thick VBG, and $\delta\lambda^{\text{HWFZ}} \sim 0.5$ nm corresponds to a 1.1-mm-thick grating at $\eta_0 = 99\%$. The coefficient in Eq. (13) slightly increases for higher DE values.

Let us derive the basic interrelation between angular and spectral parameters for a reflecting VBG. Similarly to the procedure described in Refs. 1 and 2 for transmitting Bragg gratings, we suppose that small angular deviation $\Delta\theta$ from θ_m^* inside the grating medium leads to corresponding change $\Delta\lambda$ in resonant wavelength λ_0 . In this case, Bragg condition, Eq. (1), can be expressed in its differential form:

$$\frac{\lambda_0 - \Delta\lambda}{\lambda_0} = \left| \frac{\cos(\theta_m^* - \Delta\theta)}{\cos \theta_m^*} \right|. \quad (14)$$

Because deviation $\Delta\theta$ from θ_m^* is small, $\cos \Delta\theta = 1 - 2 \sin^2 \frac{\Delta\theta}{2} \approx 1 - \frac{\Delta\theta^2}{2}$, and Eq. (14) becomes

$$\Delta\theta^2 - 2 \tan \theta_m^* \Delta\theta - \frac{2\Delta\lambda}{\lambda_0} = 0. \quad (15)$$

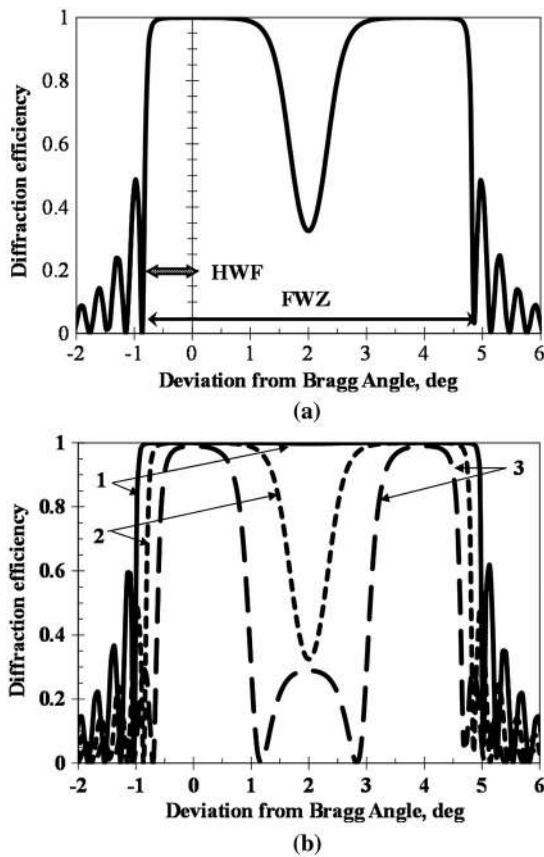


Fig. 5 Angular selectivity of 1-mm-thick reflecting VBG at $\theta_m^* = 2^\circ$. $\lambda_0 = 1085$ nm, $n_{\text{av}} = 1.4867$. (a) Definition of angular selectivity at HWFZ (solid arrow) and FWZ (dashed arrow) levels. (b) Dependence of angular selectivity shape on refractive index modulation: 1 = 2000 ppm (solid line), 2 = 1500 ppm (dotted line), 3 = 1000 ppm (dashed line).

Equation (15) has two solutions:

$$\Delta\theta_{1,2} = \pm \left(\tan^2 \theta_m^* + \frac{2\Delta\lambda}{\lambda_0} \right)^{1/2} + \tan \theta_m^*. \quad (16)$$

If one would like to consider angular selectivity between the first zeros of the DE, it is necessary to substitute $\delta\lambda^{\text{HWFZ}}$ from Eq. (12) to Eq. (16). However, Eq. (15) has two different solutions and we have to introduce two different definitions for angular selectivity. Figure 5(a) shows the simulation results for angular selectivity of a 1-mm-thick VBG with 1500 ppm refractive index modulation and an incident Bragg angle of 2 deg at 1085 nm. The first definition is for full (wider) angular selectivity at full width at zero (FWZ) level, $\delta\theta_m^{\text{FWZ}}$, i.e., for the distance between two first zeros in angular selectivity as they are determined by both solutions of Eq. (15):

$$\delta\theta_m^{\text{FWZ}} = \Delta\theta_2 - \Delta\theta_1 = 2 \left(\tan^2 \theta_m^* + \frac{2\delta\lambda^{\text{HWFZ}}}{\lambda_0} \right)^{1/2}. \quad (17)$$

Full angular selectivity $\delta\theta_m^{\text{FWZ}}$ of reflecting VBGs with predetermined DE η_0 and incident Bragg angle θ_m^* could be written in the following form by substitution of the spectral selectivity value from Eq. (12):

$$\delta\theta_m^{\text{FWZ}} = 2 \left[\tan^2 \theta_m^* + \frac{2\sqrt{(\text{atanh}\sqrt{\eta_0})^2 + \pi^2}}{\pi f t} \right]^{1/2}. \quad (18)$$

Let us note that full angular selectivity $\delta\theta_m^{\text{FWZ}}$ should be the primary consideration when incident Bragg angles θ_m^* are small enough. In this case, an overlapping of the two different selectivity curves has occurred due to their proximity, and a divergent incident beam can interact with both of them. Angular selectivity $\delta\theta_m^{\text{FWZ}}$ can be affected by changing of refractive index modulation, especially for overdeveloped VBGs. Figure 5(b) shows this phenomenon for 1-mm-thick grating at $\theta_m^* = 2^\circ$ incident Bragg angle. One can see that slight overall widening of $\delta\theta_m^{\text{FWZ}}$ is accompanied with dramatically changing of angular selectivity shape. The shape is changing from total overlapping of diffraction peaks at more than 99.99% diffraction efficiency (which corresponds to refractive index modulation $\delta n = 2000$ ppm) to partial peak separating at $\eta_0 \approx 99\%$ ($\delta n = 1500$ ppm) and their full dividing at $\eta_0 \approx 99\%$ ($\delta n = 1000$ ppm). This peculiarity of reflecting VBGs should be considered for $\delta\theta_m^{\text{FWZ}}$ assessment when gratings' DE is near the 100% diffraction efficiency limit.

The second definition of VBG angular selectivity is for the distance between the Bragg angle and the first zero closest to it [Fig. 5(a)]. Let us call this reduced angular selectivity the HWFZ, $\delta\theta_m^{\text{HWFZ}}$; this is similar to the definition for transmitting VBGs introduced in Ref. 3. The HWFZ angular selectivity considers the negative solution of Eq. (15) and assumes that it has more universal nature and can be used for reflecting Bragg gratings with any diffraction efficiency and/or incident Bragg angle θ_m^* , especially when the selectivity curves corresponding two different diffraction orders do not overlap. The analytical formula for the HWFZ selectivity is

$$\delta\theta_m^{\text{HWFZ}} = |\Delta\theta_1| = \left(\tan^2 \theta_m^* + \frac{2\delta\lambda^{\text{HWFZ}}}{\lambda_0} \right)^{1/2} - \tan \theta_m^*. \quad (19)$$

For unslanted gratings $\theta_m^* = 0$, and the interrelation between both definitions of angular selectivity can be significantly simplified:

$$\delta\theta_m^{\text{FWZ}} = 2\delta\theta_m^{\text{HWFZ}} = \left(\frac{8\delta\lambda^{\text{HWFZ}}}{\lambda_0} \right)^{1/2}. \quad (20)$$

Because there are two different definitions of Bragg grating angular selectivity, we should determine the applicability range for both definitions. Let us estimate at what incident Bragg angle θ_m^* one should consider the FWZ angular selectivity rather than the doubled HWFZ value. This problem is very close to the problem of separation of two functions with two maxima located near each other. Historically, three main criteria for such separation were developed by Lord Rayleigh (1879), C. M. Sparrow (1916), and W. V. Houston (1926). The Rayleigh criterion states that the separation arises when the peak of one function falls on the first zero point of the other function (so-called null first derivative criterion); the Sparrow criterion defines separation as when the saddle point of the summed function first develops (so-called null second derivative criterion); the Houston criterion states that the intersection of two identical functions at their half maximum level is a suitable definition for their effective separation.

Let us apply the classical Rayleigh criterion, because the Sparrow criterion is too strict and Houston's does not work well for functions which have varying core to wing ratios.⁸

Let us call the incident Bragg angle that defines the fulfillment of Rayleigh's criterion as the threshold incident Bragg angle θ_0 . To determine it, the following procedure should be applied. Actually, θ_{0m} is the angle inside the VBG medium at which full FWZ angular selectivity is three times wider than HWFZ selectivity: $\delta\theta_m^{\text{FWZ}} = 3\delta\theta_m^{\text{HWFZ}}$. Combining of Eqs. (18) and (19) together with Eq. (12) gives a result

$$\tan^2 \theta_0 = \frac{\delta\lambda^{\text{HWFZ}}}{4\lambda_0} = \frac{\lambda_0 \left[(a \tanh \sqrt{\eta_0})^2 + \pi^2 \right]^{1/2}}{8\pi n_{av} t |\cos \theta_0|}. \quad (21)$$

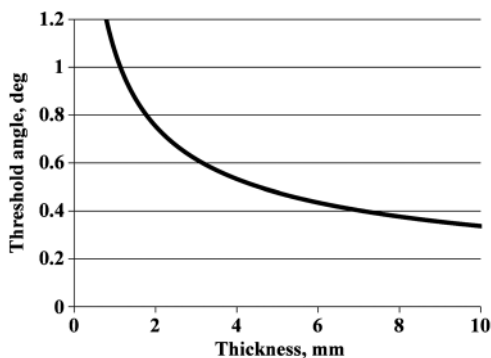


Fig. 6 Dependence of threshold incident angle in air on thickness of reflecting VBG with 99.9% diffraction efficiency at resonant wavelength of $\lambda_0 = 1085$ nm.

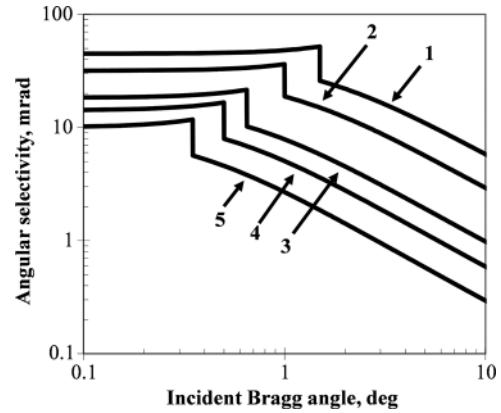


Fig. 7 Angular selectivity of reflecting VBG with 99% diffraction efficiency at wavelength $\lambda_0 = 1085$ nm versus incident Bragg angle in the medium at different grating thickness, mm: 1 = 0.5; 2 = 1; 3 = 3; 4 = 5; 5 = 10.

One can easily calculate the θ_0 angle as an angle outside the VBG (i.e., in air). As an example, it is about 1 deg for $t = 1$ mm and $\eta_0 = 99.9\%$ for $\lambda_0 = 1085$ nm. The dependence of the threshold angle in air on VBG thickness is shown in Fig. 6. The thinner the grating, the bigger the threshold angle is. However, differences in diffraction efficiency of relatively strong reflecting VBGs have almost no influence on the shape of this curve and the values of threshold angles.

Hence, at $\theta_m^* < \theta_0$ one should define the angular selectivity of reflecting VBG as its FWZ value, $\delta\theta_m^{\text{FWZ}}$; otherwise, a doubled value of the HWFZ selectivity, $\delta\theta_m^{\text{HWFZ}}$, should be taken into consideration at $\theta_m^* > \theta_0$.

Figure 7 shows the dependence of angular selectivity on VBG thickness at different incident angles for a 99% efficient grating. As one can see, the thicker the grating (still in the assumption that all gratings are 99% efficient by respective choosing of their refractive index modulations), the wider the angular selectivity is. At normal incidence ($\theta_m^* = 0$), angular selectivity is 20 mrad for 10-mm-thick, 28 mrad for 5-mm-thick, and 65 mrad for 1-mm-thick gratings with a 1085 nm resonant wavelength. When incident angles are small ($\theta_m^* < \theta_0$), angular selectivity is slightly wider due to the appearance of two separated diffraction maxima and their partial overlapping. The relative amount of this widening is higher for thicker gratings. In these conditions, reflecting VBGs work well for spectral narrowing and mode-locking of diode lasers,^{9,10} as a coupling element in laser resonators.^{11,12}

Due to separation of two maxima of angular selectivity according to Rayleigh criterion at $\theta_m^* = \theta_0$, the FWZ definition of angular selectivity of reflecting VBG should be replaced by its HWFZ definition. Figure 7 shows the corresponding drop in VBG selectivity at this point that was determined from Eq. (21). Then, the angular selectivity dramatically narrows with increasing of incident angle at $\theta_m^* > \theta_0$; however, even at high angles of incidence angular selectivity of reflecting VBGs is still much wider in comparison with typical transmitting VBGs. Possible applications of VBGs in non-retroreflecting condition are coherent and spectral beam combining, deflecting, splitting, and attenuating of laser beams, etc.¹³⁻¹⁵

Hence, despite its spectral selectivity being unambiguously specified, the angular selectivity of a reflecting

Bragg grating has two different definitions due to partial (or full) overlapping of positive and negative orders of Bragg diffraction. This phenomenon is inherent to reflecting Bragg gratings and it could be used for design of high-selective spectral filters with relatively wide angular selectivity.

3 Diffraction of Gaussian Beams by Reflecting VBGs

3.1 Polychromatic Planar Waves

Similarly to diffraction of Gaussian beams on transmitting Bragg gratings described in Ref. 1, we will consider the Bragg diffraction by comparing of grating spectral selectivity with the beam spectrum:

$$G_1(\Delta\lambda, w) = e^{-2\left(\frac{\Delta\lambda - \lambda_0}{w}\right)^2}, \quad (22)$$

where parameter w is the half width at e^{-2} of the maximum ($HWe^{-2}M$) spectral width and λ_0 is a central wavelength of a

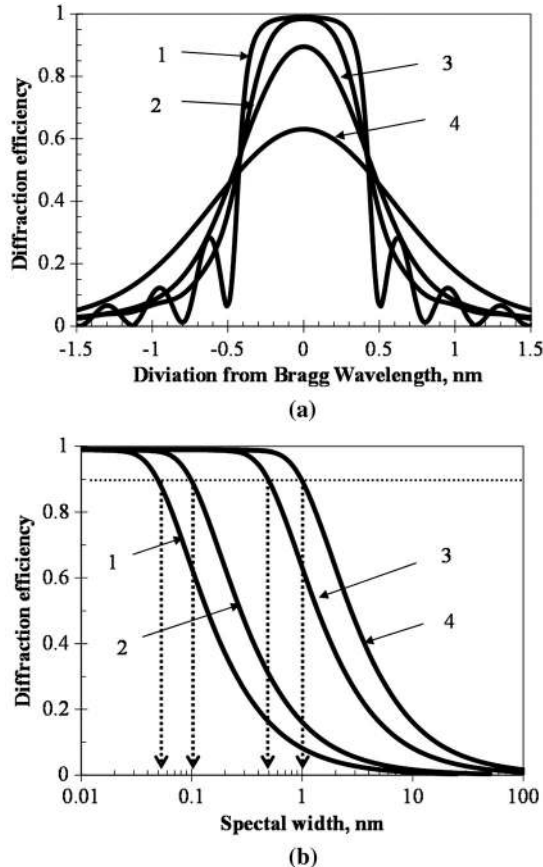


Fig. 8 Spectral selectivity of 99% efficient reflecting VBG for polychromatic plane waves at normal incidence. The calculated VBG is 1.1 mm thick with approximately 1000 ppm refractive index modulation. (a) Dependence of diffraction efficiency on deviation from Bragg wavelength. Spectral width of a beam ($HWe^{-2}M$), nm: 1 = 0.05, 2 = 0.25, 3 = 0.5, 4 = 1.0; grating spectral selectivity (HWFZ) is 0.5 nm. (b) Dependence of grating DE on spectral width of the beam. Spectral selectivity of gratings (HWFZ), nm: 1 = 0.05, 2 = 0.1, 3 = 0.5, 4 = 1.0; shown by dotted arrows. Dotted line corresponds to diffraction efficiency for a beam with spectral width which is equal to the grating selectivity.

beam emission. In this case, grating diffraction efficiency spectrum could be calculated from a convolution of the grating DE for monochromatic wave, Eq. (8), with the Gaussian spectral distribution, Eq. (22). The convolution is normalized with the integral of the Gaussian bandwidth profile. This gives us the adjusted value of diffraction efficiency $\eta_\lambda(w)$ as a function of wavelength.

$$\eta_\lambda(\Delta\lambda, w) = \frac{[\eta * G_1](\Delta\lambda)}{\int G_1(\Delta\lambda, w)d\Delta\lambda} = \frac{\int \eta(\lambda_c)G_1(\Delta\lambda - \lambda_c)d\lambda_c}{\int G_1(\Delta\lambda, w)d\Delta\lambda}. \quad (23)$$

Results of numerical calculations of Bragg diffraction on reflecting gratings are shown in Fig. 8. Figure 8(a) shows how different polychromatic beams diffract on a 1.1-mm-thick grating which has 99% diffraction efficiency at normal beam incidence. According to Eq. (12), this VBG has 0.5 nm of HWFZ spectral selectivity. One can see that diffraction efficiency drops down as the beam spectrum widens; this grating has diffraction efficiency of about 60% when $w = 2\delta\lambda^{HWFZ}$. In comparison with the same dependence of spectral selectivity for transmitting gratings described in Ref. 1, when 60% DE occurs at $w = \delta\lambda^{HWFZ}$, one can conclude that spectral width of incident beams is half as restrictive of a parameter for reflecting VBGs in comparison with transmitting ones. Also, the side lobes in the spectral selectivity curves begin to disappear when the beam spectral width is approximately half the grating spectral selectivity ($2w \geq \delta\lambda^{HWFZ}$); total flattening of the DE curve occurs when these values become equal to each other and for further increasing of the beam spectral linewidth ($w \geq \delta\lambda^{HWFZ}$).

Figure 8(b) shows the dependence of peak diffraction efficiency $\eta_\lambda(\Delta\lambda = 0, w)$ on the beam spectral bandwidth w for a set of VBGs with different spectral selectivity. These gratings have thickness of 10.9, 5.5, 1.1, and 0.55 mm, and all are 99% efficient for monochromatic wave. Their HWFZ spectral selectivity is determined from Eq. (13) as 0.05, 0.1, 0.5, and 1.0 nm, respectively. One can see that 99% efficient reflecting VBGs exhibit losses of about 10% for beams having a spectral width equal to the spectral selectivity of a corresponding grating. It is important to note that a reflecting VBG has fewer losses in comparison with a transmitting VBG having the same spectral selectivity when a beam bandwidth is equal to the spectral selectivity of the grating.³ For reflecting VBGs, decreasing DE from 99% to 98% occurs when the beam width, w , becomes approximately half the grating's spectral selectivity. This parameter for 1% efficiency decreasing ratio is about four times less restrictive in comparison with the same parameter for transmitting VBG as it was determined in Ref. 3.

It is important to note that the general shape of the curves showed in Fig. 8 does not change when the beam incidence is not normal (i.e., incident Bragg angle $\theta_m^* \neq 0$) when the beam wavelength obeys the relation $\lambda_0 = \lambda_0^{\max} |\cos \theta_m^*|$. Thus, one can use the criterion described above for the determination of diffraction losses resulting from spectral widening of diffracted beams for all values of incident Bragg angles θ_m^* .

3.2 Divergent Monochromatic Beams

Similar to the description for transmitting VBGs in Ref. 3, monochromatic beams that have a certain divergence could be approximated by a Gaussian function with $\text{HWE}^{-2}M$ divergence b :

$$G_2(\Delta\theta_m, b) = e^{-2\left(\frac{\Delta\theta_m - \theta_m^*}{b}\right)^2}. \quad (24)$$

Diffraction of divergent beams on reflecting VBG could be described by a convolution of the grating diffraction efficiency, $\eta(\Delta\theta)$, given by Eqs. (6) and (3), and the angular distribution of the beam. In this case, wavelength is taken to be a constant, $\Delta\lambda = 0$.

$$\begin{aligned} \eta_\theta(\Delta\theta, b) &= \frac{[\eta * G_2](\Delta\theta_m)}{\int G_2(\Delta\theta_m, b) d\Delta\theta_m} \\ &= \frac{\int \eta(\theta_c) G_2[(\Delta\theta_m - \theta_c), b] d\theta_c}{\int G_2(\Delta\theta_m, b) d\Delta\theta_m}. \end{aligned} \quad (25)$$

Although the general shape of the angular selectivity for reflecting VBGs at normal incidence is the same as its spectral selectivity shown in Fig. 8(a), splitting of angular selectivity curves described above results in more complex interrelations between angular selectivity of a grating, divergence of a beam, and the resulting diffraction efficiency. Let us consider a set of Bragg gratings similar to those which were described above in Sec. 3.1. Gratings with thickness 10.8, 5.4, 1.08, and 0.54 mm each have a corresponding HWFZ angular selectivity of 0.26, 0.53, 2.6, 5.2 mrad at an incident Bragg angle in the medium of $\theta_m^* = 10$ deg. A 1.1-mm-thick reflecting VBG has angular selectivity of 30.3, 22.8, 17.5, 5.1, and 2.6 mrad for corresponding Bragg angles of 0, 0.5, 1, 5, and 10 deg. FWZ angular selectivity for this grating is 30.3, 31.6, and 35.1 mrad for incident Bragg angles of 0, 0.5, and 1.0 deg, respectively. Figure 9(a) shows the results of numerical modeling of diffraction efficiency $\eta_\theta(\Delta\theta, b)$ versus beam divergence b . One can see a rather complex dependence of diffraction efficiency on divergence of an incident beam for incident Bragg angles between the normal and threshold angle θ_0 [see Fig. 9(b)]. Despite the fact that angular selectivity decreases considerably while the Bragg angle increases [Fig. 9(b)], diffraction efficiency reaches its maximum at $\theta_m^* = \theta_0$ due to overlapping of the positive and negative diffraction orders. Further increasing of incident Bragg angle results in a weak decreasing of this DE value down to a level of about 90%; it is in good correlation with the data shown in Fig. 8(b). Moreover, when an incident Bragg angle well exceeds the threshold angle of $\theta_0 \approx 1^\circ$, the incident beam interacts with only one diffraction order of the grating and, therefore, there is no difference between angular and spectral parameters of the grating as they are shown in Figs. 8(b) and 9(c).

It should be noticed again that DE is about 90% when beam divergence b equals the angular selectivity of the grating (HWZ), and these results are similar to the those for spectral characterization of reflecting VBGs as it was discussed in Sec. 3.1. Decreasing of grating DE from 99% to 98% occurs when the beam divergence b is equal to half the angular selectivity of the grating (HWM) ($2b = \delta\theta_m$). In comparison with diffraction of divergent beams on transmitting gratings described in Ref. 3, this 1% loss

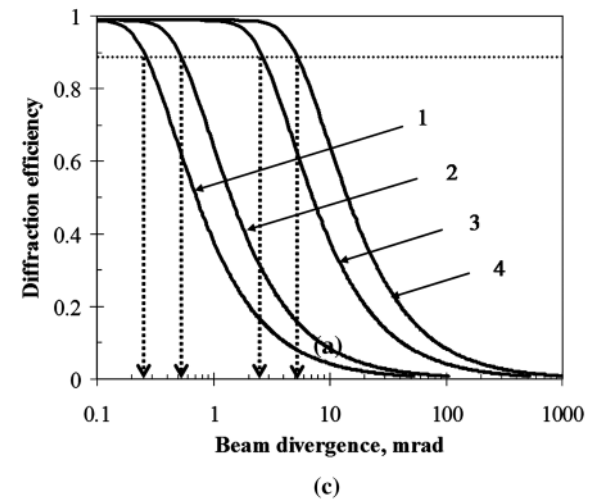
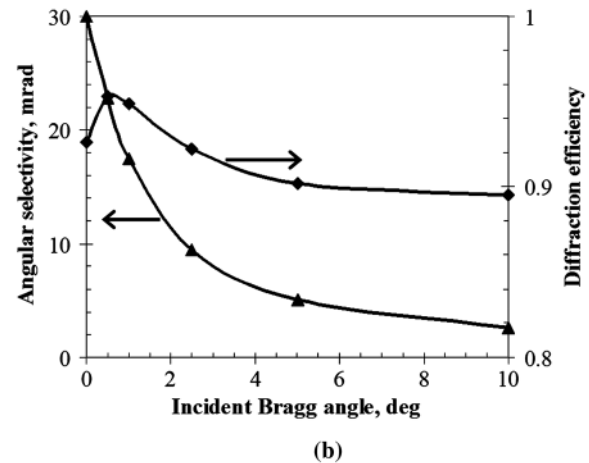
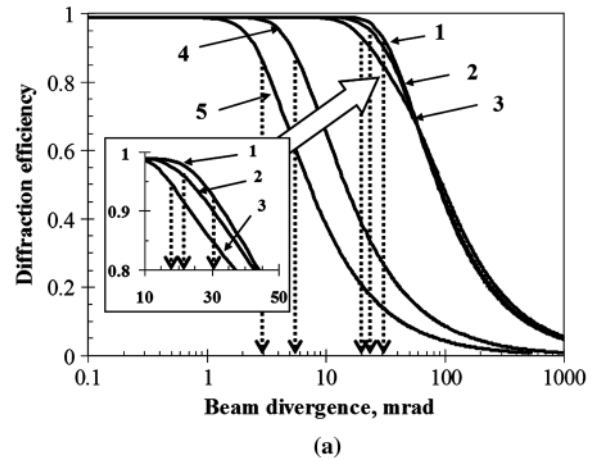


Fig. 9 Effect of divergence of incident beam on parameters of 1.1-mm-thick reflecting VBG. Diffraction efficiency of the grating for plane monochromatic wave is 99%. (a) Dependence of diffraction efficiency on beam divergence for different incident Bragg angles in medium θ_m , deg: 1 = 0; 2 = 0.5; 3 = 1.0; 4 = 5.0; 5 = 10.0. HWFZ angular selectivity of grating for corresponding incident Bragg angles, mrad: 1 = 30.3, 2 = 22.8, 3 = 17.5, 4 = 5.1, 5 = 2.6; shown by dotted arrows. (b) Dependence of angular selectivity (HWFZ) and diffraction efficiency on incident Bragg angle in a medium. Divergence of a beam is chosen equal to the grating selectivity at corresponding incident Bragg angles. (c) Dependence of diffraction efficiency on beam divergence for incident Bragg angle $\theta_m^* = 10^\circ$. HWFZ angular selectivity of gratings, mrad: 1 = 0.26, 2 = 0.53, 3 = 2.6, 4 = 5.2; shown by dotted arrows. Grating thickness, mm: 1 = 10.8, 2 = 5.4, 3 = 1.08, 4 = 0.54. Dotted line corresponds to diffraction efficiency for a beam with the same beam divergence as the grating selectivity.

requirement is much less restrictive for reflecting VBGs and is absolutely the same as was described in Sec. 3.1 for interrelations between spectral parameters of the beam and reflecting grating. Generally, reflecting VBGs are less restrictive for achieving high DE in comparison with transmitting VBGs, especially for divergent beams, but they have narrower spectral selectivity which could considerably restrict efficient Bragg diffraction of wide-spectrum beams.

If considering diffraction of divergent polychromatic beams from reflecting VBGs, the total peak DE after the Bragg grating is a product of $\eta_\lambda(\Delta\lambda = 0, w)$ and $\eta_\theta(\Delta\theta = 0, b)$ which is calculated from Eqs. (23) and (25):

$$\eta(w, b) = \eta_\lambda(\Delta\lambda = 0, w)\eta_\theta(\Delta\theta = 0, b). \quad (26)$$

For instance, if a beam is characterized by both angular divergence and spectral bandwidth which is equal to the angular and spectral selectivity of a reflecting VBG, its diffraction efficiency will be about only 80% compared with 99% DE for the same grating in plane monochromatic wave.

In some cases it is desirable to calculate diffraction efficiency as a function of wavelength or angle while considering effects of a divergent beam and laser bandwidth simultaneously. In this case, simply multiplying Eqs. (23) and (25) will not be effective; instead, a double convolution must be performed. Equation (27) gives the resulting expression.

$$\eta_\theta(\Delta\theta, b) = \frac{[\eta * G_2](\Delta\lambda, \Delta\theta_m)}{\int G_1(\Delta\lambda, w)d\Delta\lambda \int G_2(\Delta\theta_m, b)d\Delta\theta_m} = \frac{\iint \eta(\lambda_c, \theta_c) G_1[(\Delta\lambda - \lambda_c), w] G_2[(\Delta\theta_m - \theta_c), b] d\theta_c d\lambda_c}{\int G_1(\Delta\lambda, w)d\Delta\lambda \int G_2(\Delta\theta_m, b)d\Delta\theta_m}. \quad (27)$$

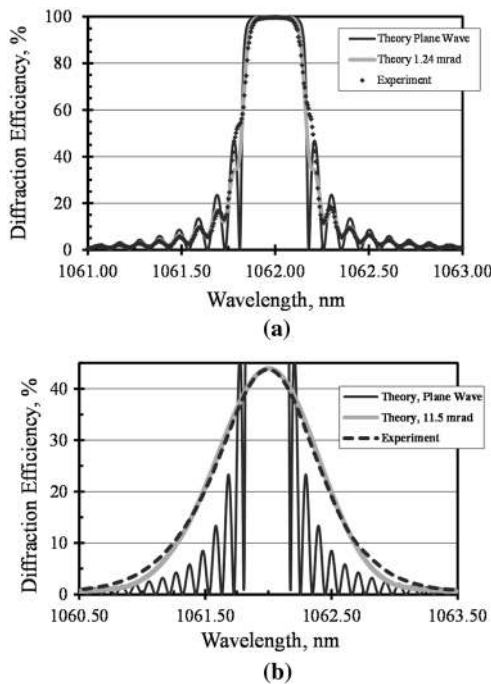


Fig. 10 Comparison of Modeling with experimental data. The VBG used is 3.5 mm thick with a refractive index modulation of 420 ppm, and has a spectral selectivity of 0.186 nm (HWFZ) and an angular selectivity of 3.67 mrad (full angle at 5.4 deg Bragg angle in glass). (a) 1.24 mrad beam divergence; (b) 23 mrad beam divergence.

4 Comparison of Modeling and Measurements

When comparing experimental data with ideal VBGs modeled above, there are usually multiple contributors that deteriorate the diffraction efficiency. Effects of spectral width and angular divergence of laser beams have been discussed above. Effects of losses and nonuniformity of real VBGs requires additional modeling that will be a subject of future researches. However, it is clear that material losses would decrease diffraction efficiency while inhomogeneity in the VBG, which result in variations in Bragg wavelength and diffraction efficiency across the aperture, will contribute to the diffraction efficiency in much the same way as does spectral or angular divergence of laser beams.

Figure 10(a) shows the measured and modeled spectra of diffraction efficiency of a reflecting VBG at normal incidence. This grating is 3.5 mm thick and has a spectral selectivity HWFZ of 0.186 nm and angular selectivity of 3.67 mrad (full-angle). The two curves match well when 1.24 mrad beam divergence (full-angle) is assumed. To remove any ambiguity about which effect we are measuring, another experiment was performed in which the beam was focused onto a very small spot on the grating. In this way, we can reduce the effect from VBG inhomogeneity to be negligible. Figure 10(b) shows the measured and calculated data resulting from this experiment. The beam divergence was measured to be approximately 23 mrad (full-angle), and calculations made by using this beam divergence match very well with the experimental data. In this high-divergence case, one can see that the side lobes have been completely washed out. This behavior was predicted above for cases in which the divergence, spectral or angular, exceeds the selectivity of the VBG. Spectrally divergent beams behave similarly.

5 Conclusions

Mathematical modeling based on Kogelnik's coupled wave theory has been produced for diffraction of beams with a wide range of spectral and angular parameters on reflecting volume Bragg gratings. This model is particularly important for most practical applications when spectral width and angular divergence of diffracted beams are comparable with spectral and angular selectivity of reflecting Bragg gratings. Contrary to fiber Bragg gratings described in numerous publications, free space VBGs allow for an additional design dimension where the interacting beams are not confined to a waveguide. This additional dimension allows for angular tuning of the Bragg resonance, and highly divergent (nonguided) beam interaction. The proposed model allows fast analytical calculation of angular and spectral dependencies of diffraction efficiency for normal and slanted gratings and could be used for the design of different devices based on reflecting Bragg gratings as well as testing tools for Bragg grating certification. This theoretical model was compared with and found very close to experimental data observed in Bragg mirrors recorded in photo-thermo-refractive (PTR) glass. This model can be applied for all other thick Bragg gratings with sinusoidal refractive index modulation recorded in different phase photosensitive materials.

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References

1. H. Kogelnik, "Coupled wave theory for thick hologram gratings," *Bell Syst. Tech. J.* **48**(9), 2909–2945 (1969).
2. L. B. Glebov et al., "Reflection of light by composite volume holograms: Fresnel corrections and Fabry-Perot spectral filtering," *JOSA A* **25**(3), 751–764 (2008).
3. I. V. Ciapurin, L. B. Glebov, and V. I. Smirnov, "Modeling of phase volume diffractive gratings, part 1: transmitting sinusoidal uniform gratings," *Opt. Eng.* **45**(1), 015802 (2006).
4. M. G. Moharam, T. K. Gaylord, and R. Magnusson, "Bragg diffraction of finite beams by thick gratings," *JOSA* **70**(3), 300–304 (1980).
5. J. Hellstrom and B. Jacobsson, "Finite beams in reflective volume Bragg gratings: theory and experiments," *IEEE J. Quant. Electron.* **44**(1), 81–89 (2008).
6. R. Kashyap, "Theory of fiber Bragg gratings," Chapter 4 in *Fiber Bragg Gratings*, pp. 119–188, Academic Press, Burlington, MA (2010).
7. T. Erdogan, "Fiber grating spectra," *J. Lightwave Tech.* **15**(8), 1277–1294 (1997).
8. A. W. Jones, J. Bland-Hawthorn, and P. L. Shopbell, "Towards a general definition for spectroscopic resolution," in *Astronomical Data Analysis Software and Systems IV*, Astronomy Society of the Pacific Conference Series, Vol. **77**, pp. 503–506 (1995).
9. B. L. Volodin et al., "Wavelength stabilization and spectrum narrowing of high-power multimode laser diodes and arrays by use of volume Bragg gratings," *Opt. Lett.* **29**(16), 1891–1893 (2004).
10. G. B. Venus et al., "Stable coherent coupling of laser diodes by a volume Bragg grating in photothermorefractive glass," *Opt. Lett.* **31**(10), 1453–1455 (2006).
11. P. Jelger and F. Laurell, "Efficient narrow-linewidth volume-Bragg grating-locked Nd: fiber laser," *Opt. Express* **15**(18), 11336–11340 (2007).
12. O. Andrusyak et al., "Spectral combining and coherent coupling of lasers by volume Bragg gratings," *IEEE J. Sel. Top. Quant.* **15**(2), 344–353 (2009).
13. O. Andrusyak et al., "Fiber laser system with kW-level spectrally-combined output," in *21st Solid State and Diode Laser Technology Review Proc.*, Directed Energy Professional Society, pp. 3–7 (2008).
14. A. Jain et al., "Coherent and spectral beam combining of fiber lasers using volume Bragg gratings," in *Proc. SPIE* **7686**, 768615 (2010).
15. I. Divliansky et al., "Volume bragg lasers," *Proc. SPIE* **7751**, 77510Z (2010).



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