Modeling of Radon and Its Short-Lived Decay Products during Showering: Dose to Adult Members of the Public

Rabi Rabi[1]*, Lhoucine Oufni[1], Khamiss Cheikh[2], El-Houcine Youssoufi[1], Hamza Badry[1], Youssef Errami[2]

[1]Department of Physics (LPM), Sultan Moulay Sliman University, Beni-Mellal, Morocco
[2]Department of Physics (LPM), Chouaib Doukkali University, El Jadida, Morocco
Email: *rabiismcm@gmail.com

Abstract

Human exposure to radon inside different parts of the house has become a great concern. In this study, the distribution of radon and its decay inside the shower will be numerically investigated. In fact, the radon concentration in water is measured through the use of AlphaGUARD. They are used as an input for CFD simulation. The numerical results proved that temperature and humidity have significant impacts on both radon content and distribution. Also, the equilibrium factor variations between radon and its progeny with the temperature and relative humidity were carefully looked at. The equivalent doses due to ^{218}Po and ^{214}Po were evaluated in different tissues of the respiratory tract of the members of the public from the inhalation of air inside the shower. The annual effective dose due to radon short lived decay from the inhalation of air inside the shower by the members of the public was also investigated.

Keywords

Radon, Temperature, Shower, Computational Fluid Dynamics (CFD), Effective Dose

1. Introduction

Radon (^{222}Rn), being naturally occurring radioactive, noble gas with a half-life of 3.82 days, is one such important potential health hazard concerning radiation hygiene in modern days. It originates from the radioactive decay of naturally occurring uranium [1] and radium deposits, which is picked up by groundwater passing through rocks and soil containing such radioactive substances and then

enters water supplies, when this water is pumped up a well [2].

The concentration of radon is generally low in the surface water as compared to the underground water because of the presence of granite, sand and gravels [3] [4] [5]. The water soluble radon is an important secondary source for the indoor radon exposure. This soluble radon, degas from the usable water inside the dwellings and becomes airborne [6]. Therefore the indoor radon concentration increases simultaneously with the high radon content in the water. Due to the presence of radon in water, the inhalation and ingestion cause exposure to the lungs and stomach respectively, out of which inhalation is expected to cause much health risk [7].

Computational fluid dynamics (CFD) has been used as a powerful tool in various contexts in different research areas such as aerosol science and technology [8] [9], chemical industries [10] [11] [12]. In recent time, computational fluid dynamics (CFD) has been used for simulating ^{222}Rn and ^{220}Rn characteristics in indoor environments [13] [14] [15] [16]. CFD simulations are being projected as a powerful tool for supplementing ^{222}Rn and ^{220}Rn research in the indoor air [17] [18] [19] [20]. The applicability of CFD for radon related research is still evolving and a lot needs to be done in applying this knowledge for mankind research.

In the current study, a numerical model was applied to investigate radon distribution and its decay in a typical shower. The influence of water temperature, relative humidity on radon distribution and its decay in the shower was analysed. We also determined the annual equivalent doses obtained from inhalation of radon, resulting from the water used in a shower, in various compartments of the human body of adults from the general population.

2. The Numerical Method

2.1. Physical Model

The shower and manikin were modelled with a CFD (Computational Fluid Dynamics) software package for predicting the behavior of radon in the shower. The CFD model of the shower and the position of manikin in the shower are shown in Figure 1. The size of the shower is (1 m × 1 m × 2 m), as well as the manikin had the standard height (1.70 m), and the total surface area (1.81 m^2). A bank of shower heads was located in the center of the chamber, normally at a height of 1.60 m from the floor, and the diameter of the orifice in the shower head is of the order 4 mm.

2.2. The Numerical Approach

In the model, ^{222}Rn was assumed to be emitted from the water of the shower. Once it enters the shower; it mixes with air and disperses in three dimensions. The air flow inside the room was considered as continuous and incompressible in laminar regime. The unsteady-state flow field was established inside the shower using equations of continuity and momentum conservation (Equations (1)-(3)) [20]:
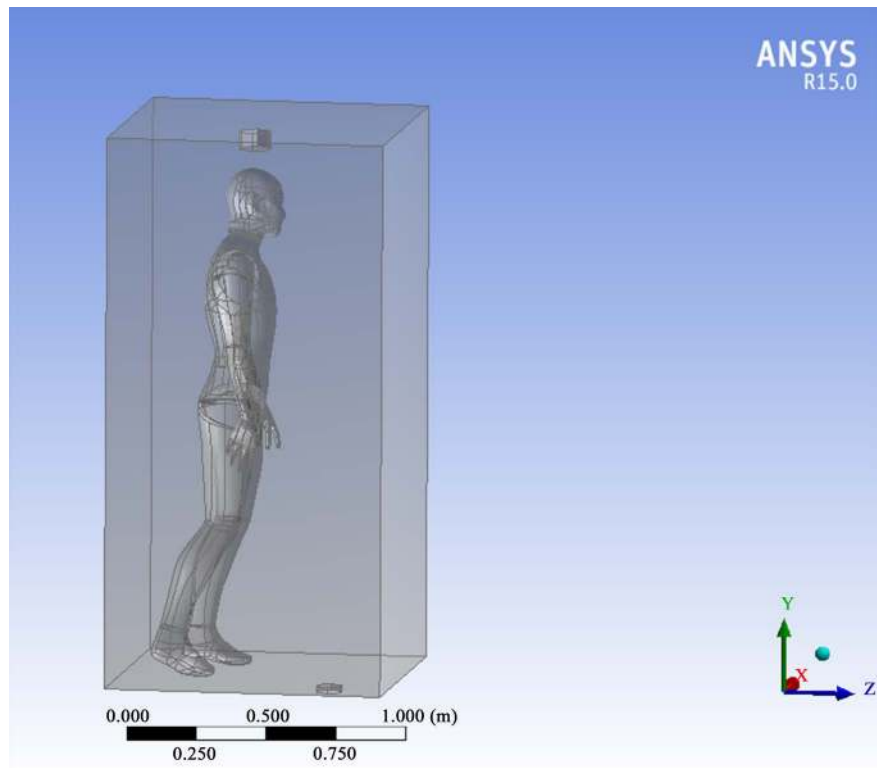
Figure 1. Geometrical of the shower model and position of the manikin.

$$\frac{\partial(\rho U_i)}{\partial X_i} = 0 \tag{1}$$

$$\frac{\partial(\rho U_i)}{\partial t} + \frac{\partial(\rho U_i U_j)}{\partial X_i} = -\frac{\partial P}{\partial X_i} + \frac{\partial}{\partial X_i}\left[\mu\left(\frac{\partial U_i}{\partial X_i} + \frac{\partial U_j}{\partial X_i}\right)\right] + \rho g \tag{2}$$

$$\frac{\partial T}{\partial t} + \frac{\partial(U_i T)}{\partial X_i} = \alpha \frac{\partial^2 T}{\partial X_i^2} \tag{3}$$

where, X is the coordinate axis in the direction ($i = 1, 2, 3$), U_i corresponds to the mean velocity (m·s⁻¹) in the i direction, and ρ is mixture density (Air-²²²Rn) (Kg·m⁻³). Here P is pressure (N·m⁻²), μ is the molecular viscosity (N s·m⁻²), α thermal diffusivity (m²·s⁻¹) and g is the gravitational acceleration (m²·s⁻¹).

The dispersion of radon and its decay were simulated by Equation (4):

$$\frac{\partial C_j}{\partial t} + \frac{\partial(U_i C_j)}{\partial X_i} = D_j \frac{\partial^2 C_j}{\partial X_i^2} - \left(\lambda_j + \lambda_d\right)C_j \tag{4}$$

where, C_j is the concentrations of jth radon decay in the shower (Bq m⁻³), respectively ($j = 0, 1, 2, 3$ and 4 for ²²²Rn, ²¹⁸Po, ²¹⁴Pb, ²¹⁴Bi and ²¹⁴Po), D is the coefficient of Brownian diffusivity (m²·s⁻¹), U are air flow velocity's, λ_j is the radioactive decay constant (h⁻¹) and λ_d is a deposition rate of the radon decay products.

2.3. Numerical Solution and Boundary Conditions

In this paper, CFD modelling was conducted with the Fluent code which is

based on Finite Volume Method to simulate the radon distribution inside the shower. The pressure-velocity coupling was accomplished through an iterative solution method, SIMPLE algorithm. Second-order upwind schemes were used to solve the basic governing equations of the discrete such as momentum, while the standard equation was used for the pressure term. The radon dispersion equation was then coupled with the indoor airflow in order to obtain the dispersion of radon.

The hexahedral grids with an interval size of 0.0005 m were used (**Figure 2**). A sensitivity analysis of the numerical scheme on the grid refinement was also performed by using a finer grid size of 0.00025 m. However, changes to the results were trivial. To confirm numerical convergence on the model, the equation residuals were prevented from changing drastically through iterations, with residuals of conservation equations for [222]Rn set to less than 10^{-5}.

The boundary conditions for the surfaces of the shower and the manikin as well as to the inlet and outlet openings are listed in **Table 1**. In this modelling, inlet boundary condition is taken as a source of radon in the shower. Therefore, an experiment was carried out to measure the radon concentration level in the
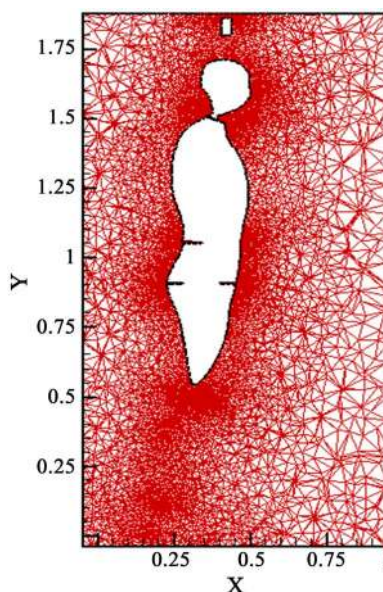
Figure 2. The mesh structure of the shower.

Table 1. Boundary conditions.

Location	Boundary condition
Inflow boundary	$U = W = 0$; $V = V_{inlet}$; $T = T_{inlet}$; $C = C_{inlet}$
Outflow boundary	$\dfrac{\partial (U,V,W,T,C)}{\partial Y} = 0$
Walls	$U = V = W = C = 0$, $\dfrac{\partial T}{\partial X} = \dfrac{\partial T}{\partial Y} = \dfrac{\partial T}{\partial Z} = 0$
Surface manikin	$U = V = W = C = 0$, $T = 306\,\text{K}$

tap water using AlphaGUARD technique [21].

The wall boundary condition of radon decay is simplified as zero normal gradients. That is $\dfrac{\partial C_j}{\partial n} = 0$, where n is the direction normal to the wall [20].

2.4. Numerical Solution and Boundary Conditions

Radon levels in water were determined by using AlphaGUARD technique. All water samples were carefully collected to prevent escape of the radon gas from samples. Water was allowed to run for 5 min, and then a 20 ml sample was taken using vessels connected to detector through the pump.

For the determination of radon concentration in water samples, the following equation was used [21]:

$$C_{\text{water}} = \frac{C_{\text{air}}\left(\dfrac{V_{\text{system}} - V_{\text{sample}}}{V_{\text{sample}}} - k\right) - C_0}{1000} \tag{5}$$

where C_{water} is radon concentration in water sample (Bq·L^{-1}), C_{air} is radon concentration in the measuring set-up after expelling the radon from the water indicated by AlphaGUARD (Bq m^{-3}), C_0 is the background radon concentration measured just before sampling for an empty set-up (Bq·m^{-3}), V_{system} is the interior volume of the measurement set-up (ml), V_{sample} is the volume of the water sample (mL) and k is the partition coefficient which depends on the temperature of the water sample.

The final result is calculated by taking into consideration the value of the diffusion coefficient, which depends on the temperature [21]:

$$k = 0.106 + 0.405\mathrm{e}^{-0.052T} \tag{6}$$

where, k is the diffusion coefficient of radon; T is the temperature of water [˚C].

2.5. Determination of Equilibrium Factor

The equilibrium factors between radon its decay is defined by [22]:

$$F = \frac{0.105 \cdot C_1 + 0.516 \cdot C_2 + 0.379 \cdot C_3}{C_0} \tag{7}$$

where C_j is the concentrations of jth radon decay in the house (Bq·m^{-3}), respectively ($j = 1$, 2 and 3 for ^{218}Po, ^{214}Pb and ^{214}Bi), C_0 is the radon concentration in room (Bq·m^{-3}).

2.6. Determination of Annual Committed Equivalent Doses Due to the Inhalation of Radon Decay Products in the Respiratory Tract of an Adult Member of the Public in the Shower

According to the ICRP Publication 66 [22] [23] (**Figure 3**), the human respiratory tract is divided into two major regions: the thoracic TH and extrathoracic ET regions. The thoracic region is divided into four sub-regions (alveolar interstitium AI, bronchioles bb, bronchi BB and lymphatics LN$_{\text{TH}}$), and the extrathoracic
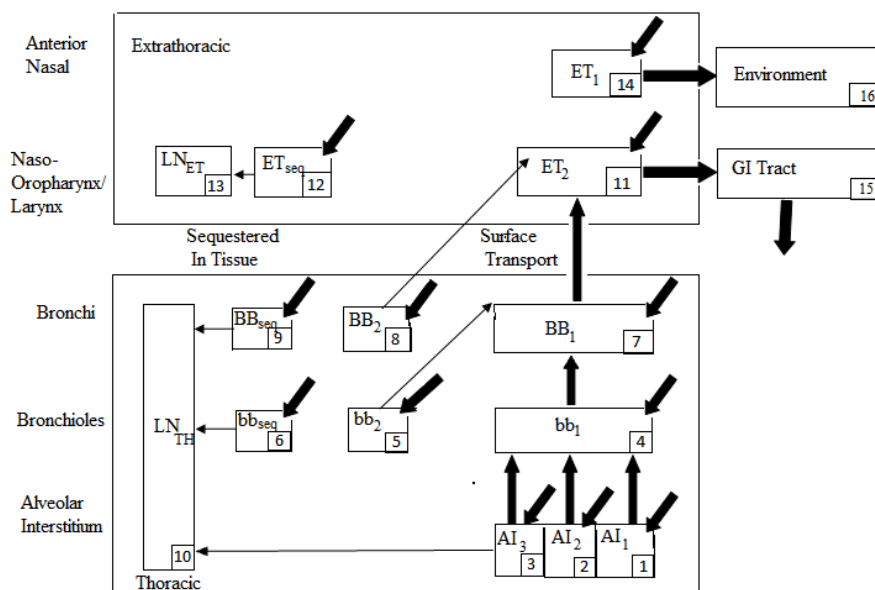
Figure 3. Compartment model showing particle transport from each region.

region is divided into three sub-regions (anterior nasal ET1, posterior nasal passage, larynx, pharynx and mouth ET_2 and lymphatics LN_{ET}). There are ten compartments in the thoracic region of the human respiratory tract numbered from 1 to 10 and, respectively, named AI_1, AI_2, AI_3, bb_1, bb_2, bb_{seq}, BB_1, BB_2, BB_{seq} and LN_{TH}. The extrathoracic region contains four compartments numbered from 11 to 14 and, respectively named ET_2, ET_{seq}, LN_{ET} and ET_1. The thin arrows on **Figure 3** given by the Biokinetic Model of Respiratory Tract denote the mechanical clearance of particles (numerical values shown are the fractional rate per day).

Inhaled radon decay-product radionuclides are assumed to be attached to particles of an activity median aerodynamic diameter of 200 nm. The rate of change of a jth radon decay product alpha-activity in a compartment i of the respiratory tract at any time is given by the following [23]:

$$\frac{dA_c^i(j)}{dt} = F_d(i)I_0(j) + \sum_n \lambda_{n,i} A_c^n(j) - \left(\sum_n \lambda_{i,n} + \lambda_j\right) A_c^i(j) \tag{8}$$

where $F_d(i)$ is the fractional deposition in the compartment i of the respiratory tract of different members of the public (ICRP), $I_0(j) = B \cdot C(j)$; where B is the average breathing rate (1.2 m³·h⁻¹) for the members of the public. $C(j)$ (Bq·m⁻³) is the concentration of the jth radon decay product in the shower air, $\lambda_{n,i} = m_{n,i} + S_s$; where $m_{n,i}$ is the clearance rate from region n to region i due to particle transport and S_s is the clearance rate due to particle absorption into blood (ICRP). The absorption rate of material into blood is the same in all regions of the respiratory tract, except in the anterior nasal passages (ET₁), where no absorption occurs [23]. $\lambda_{i,n} = m_{i,n} + S_s$; where $m_{i,n}$ is the clearance rate from regions i to n due to particle transport and λ_j is the radioactive constant of the jth radon decay product.

Alpha-activities corresponding to the jth radond ecay product in each of the 14 compartments of the respiratory tract as functions of time are obtained by solving Equation (8).

The equivalent dose in the tissue T of the respiratory tract for a radon decay product j^{th} is given by the following:

$$H_T(j) = \int_0^{t'_e} \dot{H}_T(j)(t)\,\mathrm{d}t \tag{9}$$

where t'_e is the exposure time of the tissue T and $\dot{H}_T(j)$ is the alpha-equivalent dose rate (Sv·s^{-1}) in a tissue T of the respiratory tract of an individual due to the inhalation of the jth radon decay given by:

$$\dot{H}_T(j)(t) = A_c^T(j)(t) \cdot Q \cdot k \cdot \frac{K_j R_j S_j}{m_T} \tag{10}$$

where $A^T(j)(t)(\text{Bq})$ is the alpha-activity of the jth radon decay product in the tissue T of the respiratory tract, Q is the quality factor, which is equal to 20 for α-particles (ICRP-66, 1994). m_T is the mass of the target tissue T, K_j is the branching ratio, R_j is the range of the α-particle emitted by the jth radon decay product, S_j is the stopping power of the tissue T for the emitted α-particle and k (1.6×10^{-10}) is a conversion factor. R_j and S_j were calculated by using the SRIM program using the elemental chemical composition of tissues given in the ICRP publication 66 [23].

Regional doses, weighted with factors assigned for the partition of radiation detriment, are summed to give a value of committed equivalent dose for the thoracic $H_{TH}(j)$ and extrathoracic $H_{ET}(j)$ regions. According to the ICRP 66 [23], we have the following equations:

$$H_{TH}(j) = A_{BB}H_{BB}(j) + A_{bb}H_{bb}(j) + A_{AI}H_{AI}(j) \tag{11}$$

and

$$H_{ET}(j) = A_{ET1}H_{ET1}(j) + A_{ET2}H_{ET2}(j) \tag{12}$$

where $H_{BB}(j)$, $H_{bb}(j)$ and $H_{AI}(j)$ are the equivalent doses in the BB, bb and AI tissues of the thoracic region, respectively; $H_{ET1}(j)$ and $H_{ET2}(j)$ are the equivalent doses in the ET$_1$ and ET$_2$ tissues of the extrathoracic region, respectively; $A_{BB} = 0.333$, $A_{bb} = 0.333$ and $A_{AI} = 0.333$ are the weighting factors for the partition of radiation detriment for the BB, bb and AI tissues of the thoracic region, respectively, and $A_{ET1} = 0.001$ and $A_{ET2} = 1$ are the weighting factors for the partition of radiation detriment for the ET$_1$ and ET$_2$ extrathoracic regions [23].

The annual effective dose (mSv·y^{-1}·h^{-1} exposure) due to short-lived radon decay products to the in the shower air was evaluated by using the following equation:

$$E = 0.12\left[H_{TH}\left(^{218}\text{Po}\right) + H_{TH}\left(^{214}\text{Po}\right)\right] + 0.025\left[H_{ET}\left(^{218}\text{Po}\right) + H_{ET}\left(^{214}\text{Po}\right)\right] \tag{13}$$

The annual effective dose (mSv·y^{-1}·h^{-1} of exposure) due to the radon decay to the members of the public was also estimated according to the following formula

[24]:

$$E = A_c \left({}^{222}\text{Rn} \right) \times F \times t \times D \tag{14}$$

where A_c (^{222}Rn) is the radon concentration in the shower air (Bq·m^{-3}), F is the equilibrium factor between radon and its decay in the shower air, $t = 1$ h·y^{-1} and $D = 9.0 \times 10^{-6}$ mSv (Bq·m^{-3}·h)$^{-1}$ is the dose conversion factor.

3. Results and Discussion

3.1. Radon Distribution

The results of measurements of radon concentration in water samples are presented in Table 2. The radon concentration in the water samples varied from 10.47 Bq·L^{-1} to 11.80 Bq·L^{-1}, with an average value of 10.61 Bq·L^{-1}. This value of radon concentration in water is used the key input for simulation; the CFD model was developed for radon dispersion study in shower model.

In order to investigate the spatial and temporal distribution of radon concentrations as well as its decay using CFD model, contours of radon concentrations at the symmetrical plane ($y = 1.5$ m) has been plotted and shown in Figure 4. During early times, it can be seen that the radon concentrations high near shower heads, with the passage of time the radon concentrations dispersed into the shower environment. The distribution of radon concentrations reached steady state from 30 min. Also, we notice that the distribution of ^{218}Po and ^{214}Pb is similar to that of ^{222}Rn, and this was also found in other studies [20].

Table 3 illustrates the ingrowths of the radon decay products by following the equilibrium factor (F). The equilibrium factor is defined as the ratio of the equilibrium equivalent radon concentration and of the radon concentration. By

Table 2. Radon concentration in water in various zones of Beni-Mellal.

Water sample	A_c (^{222}Rn) (Bq·L^{-1})
BM1	10.54
BM2	10.47
BM3	10.61
BM4	10.84

Table 3. Average radon concentration (Bq·m^{-3}) for various times.

Time (min)	A_c (^{222}Rn)	A_c (^{218}Po)	A_c (^{214}Pb)	A_c (^{214}Bi)	A_c (^{214}Po)	F
5	249.35	163.48	92.84	81.35	81.35	0.38
10	417.27	287.18	172.88	151.96	151.96	0.42
20	604.54	432.19	271.72	239.32	239.32	0.45
30	701.18	516.85	336.06	296.40	296.40	0.48
35	713.91	539.64	360.45	318.22	318.22	0.50
40	714.8	555.96	382.54	338.05	338.05	0.53
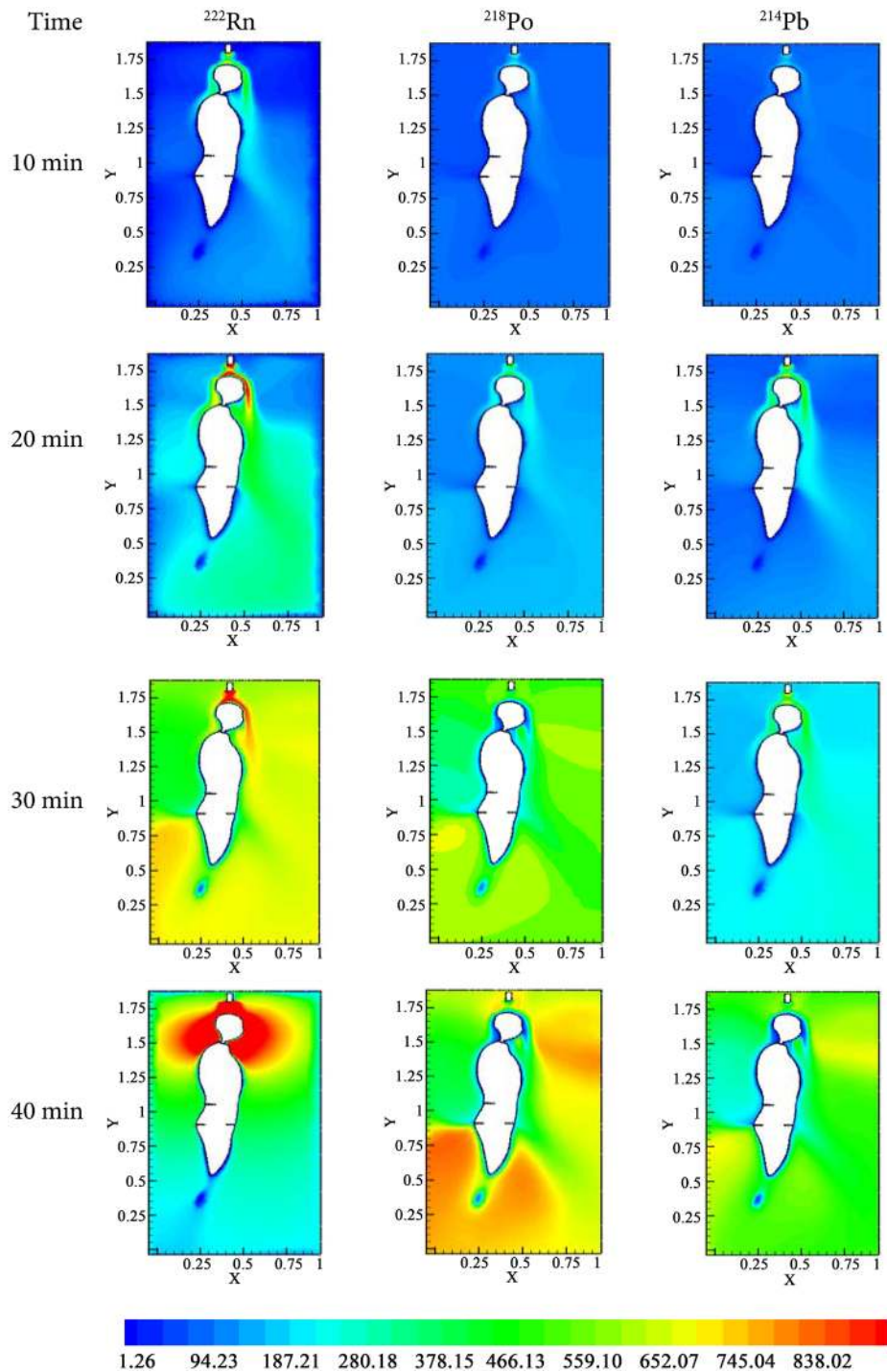
Figure 4. Contours of radon concentration and its decay (Bq·m^{-3}) at various times, in the studied shower at plane (Z = 0.5 m).

increasing the time a significant increase of the equilibrium factor was observed between radon and its decay. The increase of the equilibrium factor can be due also to radon decay products becoming attached to tiny water drops suspended in the air. This fact is in agreement with the earlier work of Chu and Liu [25].

3.2. The Effect of Temperature on Radon Dispersion

Five cases have been considered in order to investigate the effects of temperature changes on radon concentration and its decay inside the shower. The temperature values are 20°C, 25°C, 30°C, 35°C and 40°C. In these cases, the relative humidity has been fixed at 60%. Contours of radon distribution and its decay at different temperatures are illustrated in Figure 5. From the figure, it is also clear that the radon concentration at the centre of the shower to that in the vicinity of the source (*i.e.* shower head), decreases with an increase in temperature. This may be due to the fact that, the radon is soluble in water, and its solubility decreases rapidly with temperature. Increasing the temperature has the same effect on the decay products as it does for the ^{222}Rn. The average values of radon concentration and its decay in this case are summarized in Table 4. It is seen from this table that the equilibrium factor increase when the temperature increase. Then this increase will result in a larger decay product attachment rate.
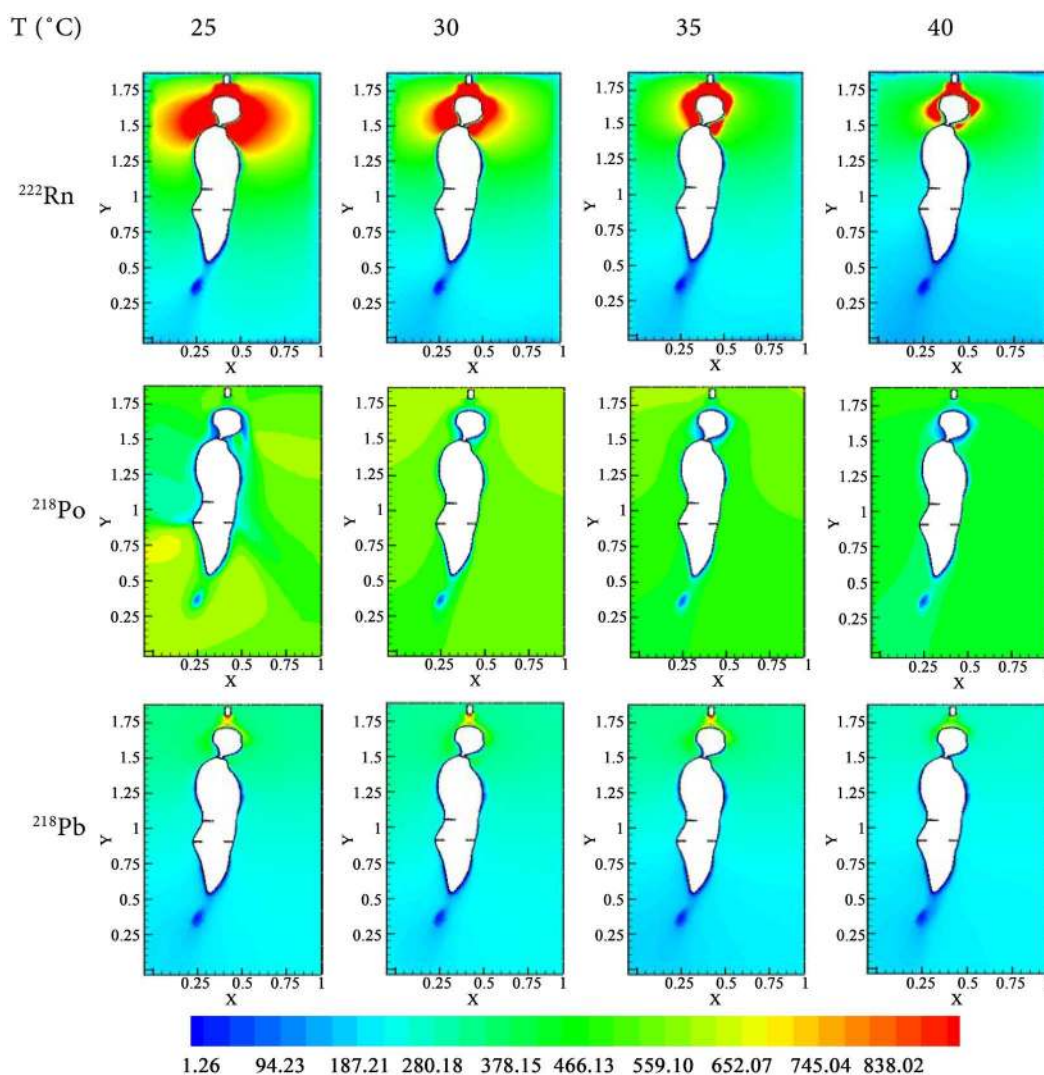

Figure 5. Contours of radon concentration and its decay (Bq·m^{-3}) as a function of temperature, in the studied shower at plane (Z = 0.5 m).

3.3. The Effect of Relative Humidity on Radon Dispersion

In order to investigate the effect of relative humidity on the radon concentration and its decay in the shower, the relative humidity was set at: 50%, 60%, 70%, 80% and 90%. In these cases, the temperature is set at 20˚C. The results of the simulation are shown in **Table 5**. It is seen from this table that the radon decay activity grows with relative humidity, while the radon level is constant. The higher the relative humidity, the higher the aerosol particle concentration, therefore, the higher is the radioactive equilibrium factor and the process of attachment becomes faster than the deposition of unattached particles on the surface [26].

Contours of radon distribution and its decay are plotted in **Figure 6** for different value of relative humidity, it can be seen that there is no increase of the radon concentration of this case. However, the maximum value of the [218]Po and [214]Pb concentration in the shower is increasing with increasing relative humidity.

3.4. Committed Equivalent Doses Due to Radon Short-Lived Alpha-Emitting Decay Products in the Respiratory Tract of Members of the Public

Annual committed equivalent doses per hour of exposure due to the [218]Po (H_T ([218]Po)) and [214]Po (H_T ([214]Po)) have been evaluated in the respiratory tract of different age groups of the members of the general public from the inhalation of air inside the shower. Data obtained for the adult males and females are shown in

Table 4. Average radon concentration (Bq·m⁻³) for various temperatures with $V = 0.2$ L·s⁻¹.

Temperatures of water (˚C)	A_c ([222]Rn)	A_c ([218]Po)	A_c ([214]Pb)	A_c ([214]Bi)	A_c ([214]Po)	F
20	897.67	653.63	419.72	370.00	370.00	0.47
25	714.84	544.51	367.10	324.19	324.19	0.51
30	709.15	541.45	359.24	335.13	335.13	0.53
35	688.76	535.12	348.38	325.81	325.81	0.54
40	418.59	335.95	238.95	211.03	211.03	0.56

Table 5. Average radon concentration (Bq·m⁻³) for various relative humidity with $T = 20$˚C.

RH (%)	A_c ([222]Rn)	A_c ([218]Po)	A_c ([214]Pb)	A_c ([214]Bi)	A_c ([214]Po)	F
40	714.84	491.98	296.17	260.33	260.33	0.42
50	714.84	512.76	323.58	285.04	285.04	0.46
60	714.84	520.89	334.48	294.86	294.86	0.47
70	714.84	545.15	367.53	324.57	324.57	0.51
80	714.84	589.99	430.66	381.17	381.17	0.59
90	714.84	620.77	475.43	421.17	421.17	0.65
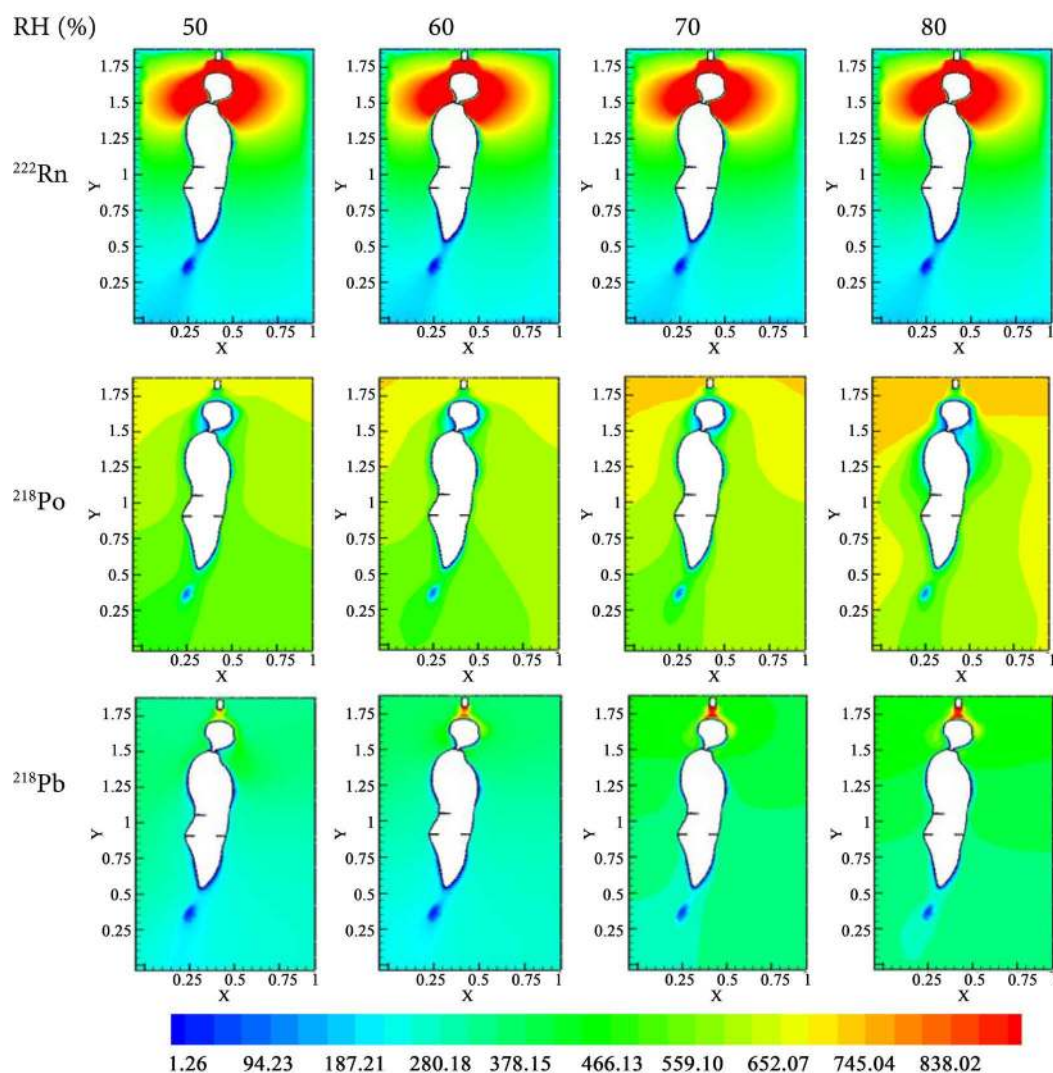
Figure 6. Contours of radon concentration and its decay (Bq·m⁻³) as a function of relative humidity, in the studied shower at plane (Z = 0.5 m).

Table 6 and Table 7. In these tables we can observe that the annual committed equivalent doses due to the ^{214}Po are smaller than those due to ^{218}Po in both the ET and TH regions. This is due to the fact that ^{214}Po has a very short half-life (1.64×10^{-4} s) compared with the exposure time of the tissues: this means that ^{214}Po comes essentially from the disintegration of ^{218}Po present in the ET and TH regions. The results also showed that the equivalent dose the annual committed equivalent dose due to ^{218}Po is higher in the ET region than in the TH region with a factor of 100 (Table 6). Then, the extrathoracic region is more exposed in the respiratory tract.

Annual effective doses due to radon decay from the inhalation of air inside the shower by the members of the general public were evaluated by using the model given here (Equation (13)) and the UNSCEAR formula (Equation (14)) (Table 8). Data obtained for the average effective dose obtained by using the model given here for different age groups of individuals in the shower were found in

Table 6. Data obtained for annual committed equivalent dose (in Sv·y^{-1}·h^{-1} exposure) due to ^{218}Po and ^{214}Po in the compartments of the respiratory tract for adult male from the inhalation of air in the shower.

Time (min)	^{218}Po					^{214}Po				
	Thoracic region			Exthrathoracic region		Thoracic region			Exthrathoracic region	
	AI	bb	BB	ET$_1$	ET$_2$	AI	bb	BB	ET$_1$	ET$_2$
10	1.84×10^{-8}	2.62×10^{-6}	7.61×10^{-6}	8.39×10^{-7}	3.14×10^{-5}	5.24×10^{-15}	7.74×10^{-13}	2.09×10^{-13}	2.36×10^{-13}	1.14×10^{-11}
20	2.73×10^{-8}	3.90×10^{-6}	1.13×10^{-6}	1.24×10^{-6}	4.68×10^{-5}	7.80×10^{-15}	1.15×10^{-12}	3.12×10^{-13}	3.51×10^{-13}	1.69×10^{-11}
30	3.09×10^{-8}	4.40×10^{-6}	$1.27 10^{-6}$	1.41×10^{-6}	5.29×10^{-5}	8.81×10^{-15}	1.30×10^{-12}	3.52×10^{-13}	3.96×10^{-13}	1.91×10^{-11}
40	3.15×10^{-8}	4.49×10^{-6}	$1.30 10^{-6}$	1.43×10^{-6}	5.39×10^{-5}	8.99×10^{-15}	1.32×10^{-12}	3.59×10^{-13}	4.04×10^{-13}	1.95×10^{-11}

Table 7. Data obtained for annual committed equivalent dose (in Sv·y^{-1}·h^{-1} exposure) due to ^{218}Po and ^{214}Po in the compartments of the respiratory tract for adult female from the inhalation of air in the shower.

Time (min)	^{218}Po					^{214}Po				
	Thoracic region			Exthrathoracic region		Thoracic region			Exthrathoracic region	
	AI	bb	BB	ET$_1$	ET$_2$	AI	bb	BB	ET$_1$	ET$_2$
10	1.31×10^{-8}	2.23×10^{-6}	7.08×10^{-7}	6.82×10^{-7}	2.49×10^{-5}	3.80×10^{-15}	6.29×10^{-13}	1.83×10^{-13}	1.96×10^{-13}	9.05×10^{-12}
20	1.95×10^{-8}	3.31×10^{-6}	1.05×10^{-6}	1.01×10^{-6}	3.70×10^{-5}	5.65×10^{-15}	9.36×10^{-13}	2.73×10^{-13}	2.92×10^{-13}	1.34×10^{-11}
30	2.20×10^{-8}	3.74×10^{-6}	1.19×10^{-6}	1.14×10^{-6}	4.18×10^{-5}	6.39×10^{-15}	1.05×10^{-12}	3.08×10^{-13}	3.30×10^{-13}	1.52×10^{-11}
40	2.24×10^{-8}	3.82×10^{-6}	1.21×10^{-6}	1.16×10^{-6}	4.27×10^{-5}	6.51×10^{-15}	1.07×10^{-13}	3.14×10^{-13}	3.37×10^{-13}	1.55×10^{-11}

Table 8. Data obtained for the effective dose (in Sv·y^{-1}·h^{-1} of exposure) due to the short-lived radon decay products from the inhalation of air in the shower by different age groups by using the method here and the UNSCEAR (2000) dose conversion coefficient.

Time (min)	Effective dose (Sv·y^{-1}·h^{-1} of exposure)					
	This method					UNSCEAR
	H-adult	F-adulte	Child 10 y	Child 5 y	Average	
10	1.18×10^{-6}	1.04×10^{-6}	1.57×10^{-6}	2.36×10^{-6}	1.54×10^{-6}	1.50×10^{-6}
20	1.75×10^{-6}	1.56×10^{-6}	2.34×10^{-6}	3.51×10^{-6}	2.29×10^{-6}	2.23×10^{-6}
30	1.98×10^{-6}	1.76×10^{-6}	2.64×10^{-6}	3.96×10^{-6}	2.59×10^{-6}	2.52×10^{-6}
40	2.02×10^{-6}	1.79×10^{-6}	2.69×10^{-6}	4.04×10^{-6}	2.64×10^{-6}	2.57×10^{-6}

good agreement with those obtained by using the UNSCEAR model for the general public.

4. Conclusion

It has been shown in this study that by using CFD modeling one can determine the distribution of radon and its decay inside the air of the shower. The overall results show that the concentrations of radon and its progenies increase when a shower starts as well as when the temperature of water decreases. Annual committed equivalent doses due to ^{218}Po and ^{214}Po were determined in the respiratory tract of adult members of the public from the inhalation of air inside the

shower. It has been shown that committed equivalent doses in the human respiratory tract depend on the human physiological condition (male or female). Owners must, therefore, use water with rationality and good ventilation of the shower to avoid any enhancement of exposure to radiation due to the inhalation of radon and its decay products.

Conflicts of Interest

The authors declare no conflicts of interest regarding the publication of this paper.

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