

# Modelling, Simulation and Control of Non-Linear Dynamical Systems

An Intelligent Approach Using Soft Computing  
and Fractal Theory

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