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# **MODERN PORTFOLIO THEORY AND INVESTMENT ANALYSIS**

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EIGHTH EDITION

INTERNATIONAL STUDENT VERSION

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