Monocular
Model-Based
3D Tracking of
Rigid Objects

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# 1

# Introduction

Tracking an object in a video sequence means continuously identifying its location when either the object or the camera are moving. There are a variety of approaches, depending on the type of object, the degrees of freedom of the object and the camera, and the target application.

2D tracking typically aims at following the image projection of objects or parts of objects whose 3D displacement results in a motion that can be modeled as a 2D transformation. An adaptive model is then required to handle appearance changes due to perspective effects or to deformation. It can provide the object's image position in terms of its centroid and scale or of an affine transformation [141, 26, 62]. Alternatively, more sophisticated models such as splines [16], deformable templates [142], 2D deformable meshes [112], or 2D articulated models [20] can be used. However, none of these methods involves recovering the actual position in space.

By contrast, 3D tracking aims at continuously recovering all six degrees of freedom that define the camera position and orientation relative to the scene, or, equivalently, the 3D displacement of an object relative to the camera.

## 2 Introduction

# 1.1 Focus and Organization of the Survey

The 3D tracking literature is particularly massive both because there are almost as many approaches as target applications and because many different approaches to solving the same problem are possible. Here we focus on online model-based 3D tracking using a single camera. We will describe both marker-based techniques and marker-less natural features-based approaches for camera, scene, and object 3D tracking.

In particular, we will not consider batch methods to camera trajectory recovery: Because these methods can consider image sequence as a whole, they can rely on non-causal strategies that are not appropriate for online camera tracking. Furthermore, an excellent reference text for this topic already exists [54]. We will restrict ourselves to single-camera approaches because multi-camera systems require calibration of the stereo-rig and are therefore less popular. We will consider only rigid objects or scenes, as opposed to deformable [25, 89] or articulated objects such as human bodies [43, 121] that would take us too far afield.

We will first introduce the key mathematical tools required for 3D tracking. We will then present marker-based techniques that use either point fiducials or planar markers to ease the tracking task. Next we will focus on techniques that rely on natural features. Finally, we will discuss recent advances that seek to increase tracking robustness to disappearance and reappearance of the target object by replacing frame-to-frame tracking by detection in each frame individually.

# 1.2 Different Approaches for Different Applications

3D tracking is a very useful tool in many different fields, and we briefly review some of them below.

# 1.2.1 Augmented Reality Applications

Many potential Augmented Reality (AR) applications have been explored, such as medical visualization, maintenance and repair, annotation, entertainment, aircraft navigation and targeting. They all involve superposing computer generated images on real scenes, which must be done at frame-rate in online systems. 3D real-time tracking is

therefore a critical component of most AR applications. The objects in the real and virtual worlds must be properly aligned with respect to each other, and the system latency should also be low, lest the illusion that the two worlds coexist be compromised.

#### 1.2.2 Visual Servoing

Visual servoing involves the use of one or more cameras and a Computer Vision system to control the position of a device such as a robotic arm relative to a part it has to manipulate, which requires detecting, tracking, servoing, and grasping. It therefore spans computer vision, robotics, kinematics, dynamics, control and real-time systems, and is used in a rich variety of applications such as lane tracking for cars, navigation for mobile platforms, and generic object manipulation.

The tracking information is required to measure the error between the current location of the robot and its reference or desired location from eye-in-hand cameras. As a consequence, the tracking algorithm must be robust, accurate, fast, and general.

#### 1.2.3 Man-Machine Interfaces

3D tracking can be integrated into man-machine interfaces. For example, it could be used to continuously update the position of a hand-held object, which would then serve as a 3D pointer. This object would then become an instance of what is known as a Tangible Interface. Such interfaces aim at replacing traditional ones by allowing users to express their wishes by manipulating familiar objects and, thus, to take advantage of their everyday experience.

Eventually, this is expected to lead to more natural and intuitive interfaces. In this context, vision-based tracking is the appropriate technique for seamless interaction with physical objects.

#### 1.3 **Computer Vision-Based 3D Tracking**

Many other technologies besides vision have been tried to achieve 3D tracking, but they all have their weaknesses: Mechanical trackers are accurate enough, although they tether the user to a limited working

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volume. Magnetic trackers are vulnerable to distortions by metal in the environment, which are a common occurrence, and also limit the range of displacements. Ultrasonic trackers suffer from noise and tend to be inaccurate at long ranges because of variations in the ambient temperature. Inertial trackers drift with time.

By contrast, vision has the potential to yield non-invasive, accurate and low-cost solutions to this problem, provided that one is willing to invest the effort required to develop sufficiently robust algorithms. In some cases, it is acceptable to add fiducials, such as LEDs or special markers, to the scene or target object to ease the registration task, as will be discussed in Section 3. Of course, this assumes that one or more fiducials are visible at all times. Otherwise, the registration falls apart. Moreover, it is not always possible to place fiducials. For example, Augmented Reality end-users do not like them because they are visible in the scene and it is not always possible to modify the environment before the application has to run.

It is therefore much more desirable to rely on naturally present features, such as edges, corners, or texture. Of course, this makes tracking far more difficult: Finding and following feature points or edges can be difficult because there are too few of them on many typical objects. Total, or even partial occlusion of the tracked objects typically results in tracking failure. The camera can easily move too fast so that the images are motion blurred; the lighting during a shot can change significantly; reflections and specularities may confuse the tracker. Even more importantly, an object may drastically change its aspect very quickly due to displacement. For example this happens when a camera films a building and goes around the corner, causing one wall to disappear and a new one to appear. In such cases, the features to be followed always change and the tracker must deal with features coming in and out of the picture. Sections 4 and 5 focus on solutions to these difficult problems.

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