

## Motives associated to graphs<sup>\*</sup>

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**Abstract.** A report on recent results and outstanding problems concerning motives associated to graphs.

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