Moving Object Detection in Satellite Videos via Spatial-Temporal Tensor Model and Weighted Schatten p-norm Minimization

Qian Yin, Ting Liu, Zaiping Lin, Wei An, Yulan Guo

***Abstract*—Low-rank matrix decomposition approaches have achieved significant progress in small and dim object detection in satellite videos. However, it is still challenging to achieve robust performance and fast processing under complex and highly heterogeneous backgrounds, since satellite video data can neither adequately fit the foreground structure nor the background model in existing matrix decomposition models. In this paper, we propose a novel object detection method based on a spatial-temporal tensor data structure. First, we construct a tensor data structure to exploit the inner spatial and temporal correlation within a satellite video. Second, we extend the decomposition formulation with bounded noise to achieve robust performance under complex backgrounds. This formulation integrates low rank background, structured sparse foreground and their noises into a tensor decomposition problem. For background separation, a weighted Schatten p-norm is incorporated to provide adaptive threshold to obtain the singular value of the background tensor. Finally, the proposed model is solved using the alternative direction method of multipliers (ADMM) scheme. Experimental results on various real scenes demonstrate the superiority of proposed method against the compared approaches.**

***Index Terms*—Moving object detection, satellite video, low-rank tensor recovery, weighted Schatten p-norm.**

I. Introduction

As a new earth observation technology, satellite video is able to provide a period of continuous observation over an area, providing rich dynamic information of an object, such as the moving trajectory, speed and directions. Satellite video is important for numerous applications, such as space-based surveillance [1], traffic monitoring, and disaster rescue.

As an important task based on satellite videos, small and dim moving object detection (MOD) has attracted increasing attention in recent years. However, this task is highly challenging due to several facts. (1) **Low spatial resolution**. Due to the long distance between a target and the imaging platform, the object is extremely small. Besides, the appearance of objects changes significantly between consecutive frames. (2) **Large field of view**. Each frame in a satellite video is typically on the order of several to hundreds of megapixels, resulting in a large searching space and illumination variation. (3) **Heterogeneous backgrounds and complex noise**. Objects are usually immersed and densely packed in highly heterogeneous and complex backgrounds.

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Most state-of-the-art MOD methods for satellite videos follow a motion-based paradigm. That is, the Background Subtraction (BS) technique is used to separate a frame into foreground and background components. Typical BS methods include statistical models [2], [3] and Robust Principal Component Analysis (RPCA) based models [4]–[6]. The RPCA based methods can be categorized into batch-based methods [4], [5] and online methods [6].

Statistical methods (*i.e.*, median (mean) model and statistical model (VIBE) [2]) usually compare each video frame with an adaptive background model (which is free of moving objects). Ahmadi et al. [3] employed a median background model to detect objects and used the nearest neighbor algorithm to produce trajectories. However, these statistical methods do not consider the structure knowledge of an video (*e.g.*, temporal similarity of background and spatial contiguity of foreground). Consequently, their detection performance cannot be further improved, especially in complex and dynamic backgrounds.

To address this limitation, RPCA [4], [5], [7] were introduced to encode the temporal similarities of video backgrounds, and mostly useful foreground prior structures (*e.g.*, sparsity and spatial continuity). Zhang et al. [6], [8] proposed several methods based on the Low-rank and Structured Sparse Decomposition (LSD) framework [5] to achieve moving object detection in satellite videos. However, these matrix RPCA based methods can only convert the videos with a natural 3D structure to a 2D data, which can destroy the structure information and reduce the detection performance. Additionally, these methods cannot achieve robust performance and fast processing speed in complex and highly heterogeneous backgrounds.

Motivated by the work for exploiting spatial-temporal and structural information in [9], [10], we incorporate a spatial-temporal tensor with RPCA (tensor RPCA) and employ the weighted Schatten p-norm minimization (WSNM) [11] to obtain optimal results. In summary, the contributions of this paper can be summarized as follows:

- We introduce a tensor representation to preserve the spatial-temporal information of pixels within a satellite video.
- We propose a tensor RPCA analysis framework with bounded noise and a generalized WSNM to separate objects from the background by estimating the low-rank components. In addition, we adopt tensor singular value decomposition (t-SVD) for efficient inference.

- We employ the alternating direction method of multipliers (ADMM) to solve the low-rank component recovery problem in our tensor RPCA analysis framework. Extensive experiments have demonstrated the superiority of our WSNM-STTN to the state-of-the-art methods.

II. The Proposed Model

A. The Matrix Decomposition Model for Moving Object Detection

The Extended Matrix Decomposition Model (E-LSD) [8] considered foreground detection from a viewpoint of decomposition and optimization problem, which can be defined as:

$$\mathbf{D} = \mathbf{B} + \mathbf{S} + \mathbf{E}. \tag{1}$$

Here, $\mathbf{D} \in \mathbb{R}^{s\times n}$ is an observed video, where s and n represent the number of pixels in a frame and the number of frames in a sequence, respectively. $\mathbf{B} \in \mathbb{R}^{s\times n}$, $\mathbf{S} \in \mathbb{R}^{s\times n}$, and $\mathbf{E} \in \mathbb{R}^{s\times n}$ are the estimated background, foreground, and residuals, respectively.

In E-LSD, an optimization problem is defined as:

$$\begin{aligned}(\mathbf{B}^*, \mathbf{S}^*, \mathbf{E}^*) = \arg\min_{\mathbf{B},\mathbf{S},\mathbf{E}} ||\mathbf{B}||_* + \lambda_1||\mathbf{S}||_{\ell 1/\ell\infty} + \lambda_2||\mathbf{E}||_F^2,\\ s.t.\ \mathbf{D} = \mathbf{B} + \mathbf{S} + \mathbf{E}\end{aligned} \tag{2}$$

where λ_1 >0 and λ_2 >0 are the weights of sparsity term $||\mathbf{S}||_{\ell 1/\ell\infty}$ and the residual term $||\mathbf{E}||_F^2$. $||\mathbf{B}||_*$ means the nuclear norm of matrix $\mathbf{B}$, i.e., the sum of its singular values. $||\cdot||_{\ell 1/\ell\infty}$ is a norm to induce the structural sparsity, $||\cdot||_F$ represents the Frobenius norm.

However, the matrix decomposition model cannot preserve the structural information of the input video. It also cannot make good use of the spatio-temporal correlation prior of the background and spatio-temporal continuity of the foreground. In addition, E-LSD adopts convex nuclear norm minimization (NNM) to characterize the low-rank background, while NNM treats singular values equally. As a result, the accuracy of the estimated low-rank component is reduced in highly noisy scenarios [12], [13], and the low-rank component shrinks too much, which is called the over contraction problem [13].

B. The Spatial-Temporal Tensor Model for Moving Object Detection

Since an satellite video has a 3D structure, a matrix extension of RPCA to Tensor RPCA can be used to address the aforementioned problem. Further, we propose a tensor RPCA analysis framework with bounded noise to preserve the structure information in a satellite video and dig out inter-frame correlations within a satellite video. The problem of MOD in satellite videos can be formulated as:

$$\mathcal{D} = \mathcal{B} + \mathcal{T} + \mathcal{N}, \tag{3}$$

where $\mathcal{D}, \mathcal{B}, \mathcal{T}, \mathcal{N} \in \mathbb{R}^{n_1\times n_2\times n_3}$ represent the original patch-tensor, background tensor, target tensor, and noise tensor, respectively.

In order to recover the low-rank component more accurately and separate the object from background more perfectly, we incorporate WSNM [11] into the low-rank tensor approximation model. This is because, the principle of WSNM is to assign different weights to the ℓ_p norm of singular values, which can adjust the power p to obtain a more suitable value to recover the background. The WSNM for a matrix is defined as:

$$\|\mathcal{X}\|_{w,S_p} = \left(\sum_{i=1}^{\min\{n,m\}} w_i\sigma_i^p\right)^{\frac{1}{p}}, \tag{4}$$

where $\mathcal{X} \in \mathbb{R}^{m\times n}$ represents the input matrix and $w = \left[w_1, \cdots, w_{\min\{n,m\}}\right]$ represents weight values satisfying an non-descending order and the non-negativity requirement. σ_i represents the i-th singular value of $\mathcal{X} \in \mathbb{R}^{m\times n}$ and the value of power p satisfies $0 < p \leq 1$. Both convex Nuclear Norm Minimization (NNM) and Weighted Nuclear Norm Minimization (WNNM) are the special cases of WSNM, when $w = [1, \cdots, 1]$ and $w = \left[w_1, \cdots, w_{\min\{n,m\}}\right]$ with $p = 1$, respectively.

In our model, we generalize the definition of WSNM to tensor $\mathcal{B} \in \mathbb{R}^{n_1\times n_2\times n_3}$, that is:

$$\|\mathcal{B}\|_{\mathcal{W},S_p}^p = \frac{1}{L}\sum_{i=1}^{r}\sum_{j=1}^{n_3}\left(\mathcal{W}(i,i,j)\left(\bar{\mathcal{S}}(i,i,j)\right)^p\right)^{\frac{1}{p}}, \tag{5}$$

$$\mathcal{W}(i,i,j) = \frac{C\sqrt{mn}}{\bar{\mathcal{S}}(i,i,j) + \varepsilon}, \tag{6}$$

where $r = \mathrm{rank_t}(\mathcal{B})$ denotes the tensor tubal rank. $\mathcal{S}(i,i,1)$ is the entries on the diagonal of the first slice of $\mathcal{S}$ ($\mathcal{S} \in \mathbb{R}^{n_1\times n_2\times n_3}$ is a diagonal tensor). The Discrete Fourier Transformation (DFT) of $\mathcal{S}$ is denoted as $\bar{\mathcal{S}} \in \mathbb{R}^{n_1\times n_2\times n_3}$. The entries on the diagonal of $\bar{\mathcal{S}}(:,:,j)$ are the singular values of $\bar{\mathcal{B}}(:,:,j)$. C is a tunning parameter. ε is a positive constant, and $\mathcal{W}$ denotes a weight tensor.

Then, the overall framework can be formulated as:

$$\min_{\mathcal{B},\mathcal{T},\mathcal{N}} \|\mathcal{B}\|_{\mathcal{W},S_p}^p + \lambda\|\mathcal{T}\|_1 + \beta\|\mathcal{N}\|_F^2 \quad s.t.\ \mathcal{D} = \mathcal{B} + \mathcal{T} + \mathcal{N}, \tag{7}$$

where λ and β represent the positive regularization parameters for the target and noise components, respectively.

C. Solution of the proposed model

To solve the proposed model, we adopt ADMM [14] and the Inexact Augmented Lagrangian Multiplier (IALM) [15]. The problem in Eq. 7 can be rewritten by IALM as:

$$\begin{aligned}L(\mathcal{B},\mathcal{T},\mathcal{N},y,\mu) = \|\mathcal{B}\|_{\mathcal{W},S_p}^p + \lambda\|\mathcal{T}\|_1 + \beta\|\mathcal{N}\|_F^2\\ + \langle y, \mathcal{D} - \mathcal{B} - \mathcal{T} - \mathcal{N}\rangle\\ + \tfrac{\mu}{2}\|\mathcal{D} - \mathcal{B} - \mathcal{T} - \mathcal{N}\|_F^2,\end{aligned} \tag{8}$$

where $y \in \mathbb{R}^{n_1\times n_2\times n_3}$ denotes the Lagrangian multiplier tensor. μ represents a penalty factor, and $\langle\cdot\rangle$ denotes the inner product operation. ADMM can decompose the problem in Eq. 8 into three optimization subproblems, including $\mathcal{B}$, $\mathcal{T}$, and $\mathcal{N}$. Since it is hard to optimize all three variables simultaneously, we approximately solve this optimization problem by alternatively minimizing one variable with the others fixed. The detailed process is given below:

1) Updating $\mathcal{B}$ with other variables fixed, and the formulation Eq. 8 can be defined as:

$$\mathcal{B}^{k+1} = \arg\min_{\mathcal{B}} \|\mathcal{B}\|^p_{\mathcal{W},\mathcal{S}_p} + \frac{\mu^k}{2}\left\|\mathcal{D} - \mathcal{B}^k - \mathcal{T}^k - \mathcal{N}^k + \frac{y^k}{\mu^k}\right\|_F^2. \quad (9)$$

To solve the problem in Eq. 9, we incorporate the Generalized Soft-Thresholding (GST) method [11] into tensor singular value thresholding (t-SVT) [16], [17]. Consequently, Eq. 9 can be rewritten as:

$$\mathcal{B}^{k+1} = \mathcal{D}_{\mathcal{W},\mathcal{S}_p(\mu^k)^{-1}}\left(\mathcal{D} - \mathcal{T}^k - \mathcal{N}^k + \frac{y^k}{\mu^k}\right), \quad (10)$$

where $\mathcal{D}_{\mathcal{W},\mathcal{S}_p(\mu^k)^{-1}}(\cdot)$ denotes the ADMM algorithm. It should be noticed that the weights $w = [w_1, \cdots, w_r]$ are in a non-descending order, and the singular values satisfy a non-ascending order: $\sigma_1 \geq \sigma_2 \geq \cdots \geq \sigma_r$.

2): Updating $\mathcal{T}$ with other variables fixed, and the formulation can be defined as:

$$\mathcal{T}^{k+1} = \arg\min_{\mathcal{T}} \lambda\|\mathcal{T}\|_1 + \frac{\mu^k}{2}\left\|\mathcal{D} - \mathcal{B}^{k+1} - \mathcal{T} - \mathcal{N}^k + \frac{y^k}{\mu^k}\right\|_F^2. \quad (11)$$

The problem in Eq. 11 is a typical l_1 regularized minimization problem. Therefore, we can obtain the overall optimal solution through an element-wise shrinkage operation [18]:

$$\mathcal{T}^{k+1} = \mathcal{F}_{\lambda/\mu^k}\left(\mathcal{D} - \mathcal{B}^{k+1} - \mathcal{N}^k + \frac{y^k}{\mu^k}\right), \quad (12)$$

where $\mathcal{F}_{\lambda/\mu^k}(\cdot)$ represents the element-wise shrinkage operator.

3): Updating $\mathcal{N}$ with other variables fixed, and the formulation can be defined as:

$$\mathcal{N}^{k+1} = \arg\min_{\mathcal{N}} \beta\|\mathcal{N}\|_F^2 + \frac{\mu^k}{2}\left\|\mathcal{D} - \mathcal{B}^{k+1} - \mathcal{T}^{k+1} - \mathcal{N} + \frac{y^k}{\mu^k}\right\|_F^2. \quad (13)$$

The solution of the above problem can be obtained by:

$$\mathcal{N}^{k+1} = \frac{\mu\left(\mathcal{D} - \mathcal{B}^{k+1} - \mathcal{T}^{k+1}\right) + y^k}{2\beta + \mu^k}. \quad (14)$$

4): Updating multipliers y with other variables fixed:

$$y^{k+1} = y^k + \mu^k\left(\mathcal{D} - \mathcal{B}^{k+1} - \mathcal{T}^{k+1} - \mathcal{N}^{k+1}\right). \quad (15)$$

5): Updating μ^{k+1} by the following equation:

$$\mu^{k+1} = \min\left(\rho\mu^k, \mu_{\max}\right). \quad (16)$$

Finally, the proposed method is summarized in **Algorithm1**.

Algorithm 1: The process of WSNM-STTN

Input: The image sequence $d_1, \cdots, d_P \in \mathbb{R}^{n_1 \times n_2}$, number of frames L, tunning parameter H, parameters $\lambda, \beta, p, \mu > 0$

Initialize: Transform the image sequence $d_1, \cdots, d_P \in R^{n_1 \times n_2}$ into the tensor $\mathcal{D}, \mathcal{B}^0 = \mathcal{T}^0 = \mathcal{N}^0 = 0 \in R^{n_1 \times n_2 \times n_3}$, $y^0 = 0$, μ_0 = 1e-2, $\mu_{\max} = 1e7$, $k = 0$, $\rho = 1.5$, ζ = 1e-6, $\beta = 100$.

While : not converged do

1 : Update $\mathcal{B}^{k+1}$ according to Eq. 10.

2 : Update $\mathcal{T}^{k+1}$ according to Eq. 11.

3 : Update $\mathcal{N}^{k+1}$ according to Eq. 14.

4 : Update multipliers y according to Eq. 15.

5 : Update μ^{k+1} according to Eq. 16.

6 : Check the convergence conditions $\frac{\|\mathcal{D}-\mathcal{B}^{k+1}-\mathcal{T}^{k+1}-\mathcal{N}^{k+1}\|_F^2}{\|\mathcal{D}\|_F^2} \leq \zeta$.

7 : Update $k = k + 1$.

end While

Output : $\mathcal{B}^{k+1}, \mathcal{T}^{k+1}, \mathcal{N}^{k+1}$.

III. Experimental Results and Analysis

A. Dataset and Metrics

We evaluated the proposed WSNM-STTN on nine satellite video datasets (as listed in Table I). The first two videos (*i.e.*, Video 001 and Video 002) were captured by SkySat[1]. Their spatial resolution is 1.0 meter, while their frame rate is 30 Frame Per Second (FPS). Videos 003-009 are provided by Chang Guang Satellite Technology Co., Ltd [2]. Their spatial resolution is 1.0 meter and their frame rate is 10 FPS. All these datasets mainly cover traffic scenarios of urban areas. Note that, moving object detection in videos 003-009 are challenge due to the complex background. In contrast, the backgrounds of videos 001-002 captured by SkySat are mainly composed of roads, which is relatively easy to achieve good detection performance. In our experiments, moving cars are selected as the targets of interests.

We use three evaluation metrics, including Precision, Recall, F_1 score [19], to evaluate the performance of our WSNM-STTN algorithm.

B. Parameter setting

In the proposed WSNM-STTN algorithm, parameters are properly set to achieve good object detection performance. The regularized parameter λ in Eq. 8 represents the influence of the object tensor. λ is set to $\frac{H}{\sqrt{\max(m,n)\times L}}$, where m and n are the width and the height of the input image, respectively, L represents the number of input frames used to dig out the inter-frame information in the model. We use tunning parameter H to control λ. Figure 1(a)-(c) shows the Recall, Precision, $F1$ curves with respect to the power p, the number of frames L and the tunning parameter H on the test datasets, respectively. Based on the tunning results, we set p = 0.9, L = 8, and H = 4 in the following experiments to obtain the optimal detection performance.

C. Comparison with the state-of-the-art methods

We conduct extensive experiments to demonstrate the robustness of our method to various scenarios in real applications:

[1] https://www.youtube.com/watch?v=lKNAY5ELUZY/

[2] http://www.charmingglobe.com/index.aspx/

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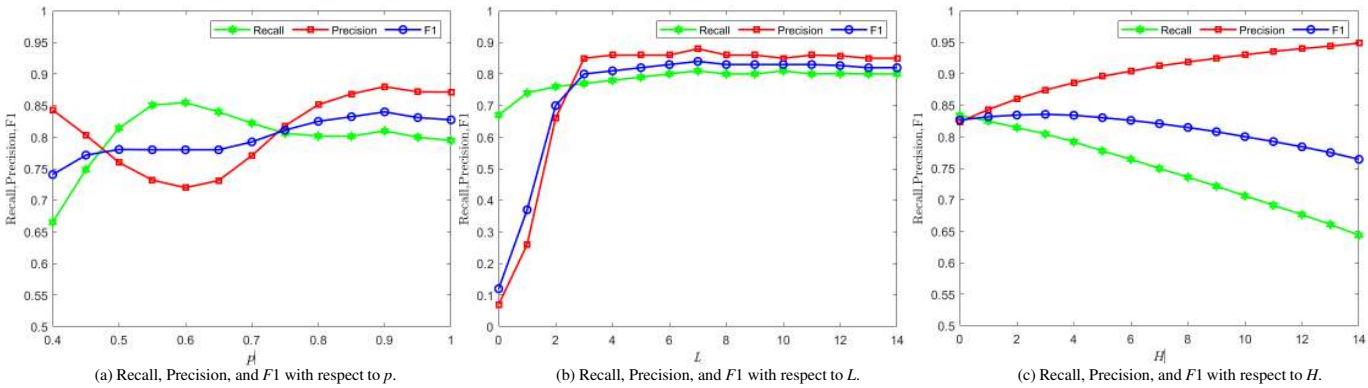

(a) Recall, Precision, and $F1$ with respect to p. (b) Recall, Precision, and $F1$ with respect to L. (c) Recall, Precision, and $F1$ with respect to H.

Figure 1. Recall, Precision, and $F1$ results achieved by our model with different values of L, H, and p.

Table I
THE DETAILS OF NINE SATELLITE VIDEO DATASETS.

Module	Video 001	Video 002	Video 003~009
Image Size	400×400	600×400	1024×1024
Vehicles	27,473	52,807	157,525
Frames	700	700	2,250

Table II
DETECTION PERFORMANCE ACHIEVED BY OUR MODEL AND BATCH-BASED ALGORITHMS ON SKYSAT SATELLITE VIDEOS. THE BEST RESULTS ARE SHOWN IN **RED** AND THE SECOND BEST RESULTS ARE SHOWN IN BLUE (RE: RECALL, PRE: PRECISION).

Method	Video 001			Video 002			Avg(F1)↑
	Re ↑	Pre ↑	$F1$ ↑	Re ↑	Pre↑	$F1$↑	
RPCA [20]	0.94	0.41	0.57	0.90	0.78	0.84	0.70
GoDec [4]	0.95	0.36	0.52	0.90	0.81	0.85	0.69
DECOLOR [7]	0.77	0.59	0.67	0.80	0.81	0.80	0.73
LSD [5]	0.87	0.71	0.78	0.82	0.91	0.86	0.82
E-LSD [8]	0.85	0.79	0.82	0.80	0.94	0.86	0.84
WSNM-STTN	0.94	0.76	0.84	0.95	0.80	0.87	0.86

The SkySat dataset: To test the effectiveness of our WSNM-STTN on Skysat satellite videos, following [6], [8], we compare our method with five batch-based state-of-the-art approaches (*i.e.*, RPCA [20], GoDec [4], DECOLOR [7], LSD [5], and E-LSD [8]) and one state-of-the-art online approaches (*i.e.*, O-LSD [6]). As shown in Tables II and III, the WSNM-STTN method achieves the highest overall performance among these batch methods and online method, with an average $F1$ (Avg-$F1$) of 0.86 being achieved. That is because, the tensor RPCA in our model can dig out inter-frame information in consecutive frames to boost the detection performance. In addition, comparing to the state-of-the-art online approaches O-LSD, WSNM-STTN achieves a comparable detection performance with significantly reduced processing time. That is, the processing time for each frame of WSNM-STTN is thirty times shorter than O-LSD. This is because, the t-SVD operation in our method can speed up the inference process.

The Jilin-1 dataset: To test the effectiveness of our WSNM-STTN method on Jilin-1 satellite videos, we compare our method with three batch RPCA-based state-of-the-art approaches (*i.e.*, GoDec [4], DECOLOR [7], E-LSD [8]), and three statics modeling-based methods (*i.e.*, MDTT [3], VIBE [2], D&T [19]). As shown in Table IV, WSNM-STTN achieves the highest overall performance against other methods, with an average precision of 0.90 and an average $F1$ of 0.83 being reported. Compared to the matrix decomposition method E-LSD, the proposed method even improves the performance by 0.12 and 0.13 in term of average precision and average $F1$, respectively.

In summary, the proposed WSNM-STTN model can achieve robust performance and fast processing in complex and highly heterogeneous backgrounds.

Table III
DETECTION PERFORMANCE ACHIEVED BY OUR MODEL AND THE OTHER METHODS (I.E., E-LSD AND O-LSD) ON SKYSAT SATELLITE VIDEOS.

Method	Video 001				Video 002				Avg(F1)↑
	Re ↑	Pre ↑	$F1$ ↑	FPS ↓	Re ↑	Pre↑	$F1$↑	FPS ↓	
O-LSD [6]	0.65	0.64	0.64	6.57s	0.73	0.90	0.81	10.75s	0.73
E-LSD [8]	0.85	0.79	0.82	17s	0.80	0.94	0.86	33s	0.84
WSNM-STTN	0.94	0.76	0.84	0.23s	0.95	0.80	0.87	0.3s	0.86

D. Ablation Study

We have demonstrated the effectiveness of introducing bounded noises $\mathcal{N}$ in Eq. 8. In this section, we also conduct ablation experiments and visualize the results of WSNM-STTN with noises (i.e., WSNM-STTN w/noises) and without noises (i.e., WSNM-STTN w/o noise) in Fig. 2. It can be observed that our WSNM-STTN method achieves a high detection rate and low false alarms rate by introducing bounded noises.

IV. CONCLUSION

In this paper, we propose a WSNM-STTN model to detect dim and small moving objects in satellite video. With the STTN model, the proposed model can dig out temporal information within a sequence. Besides, we propose an extended tensor RPCA with bounded noise and incorporate WSNM to

Table IV
QUANTITATIVE RESULTS ACHIEVED BY DIFFERENT METHODS ON JILIN-1 SATELLITE VIDEOS. THE BEST RESULTS ARE SHOWN IN **RED** AND THE SECOND BEST RESULTS ARE SHOWN IN BLUE (RE: RECALL, PRE: PRECISION).

Method	Video 003			Video 004			Video 005			Video 006			Video 007			Video 008			Video 009			Average		
	Re↑	Pre ↑	F1 ↑	Re ↑	Pre ↑	F1 ↑	Re ↑	Pre ↑	F1 ↑	Re↑	Pre ↑	F1 ↑	Re ↑	Pre ↑	F1↑	Re ↑	Pre↑	F1 ↑	Re↑	Pre ↑	F1 ↑	Re ↑	Pre ↑	F1↑
VIBE [2]	0.61	0.34	0.44	0.82	0.61	0.70	0.68	0.59	0.63	0.65	0.52	0.58	0.72	0.65	0.69	0.60	0.42	0.49	0.45	0.44	0.44	0.65	0.51	0.57
GoDec [4]	0.92	0.51	0.65	0.73	0.81	0.77	0.93	0.53	0.68	0.72	0.38	0.50	0.72	0.74	0.73	0.81	0.42	0.55	0.93	0.25	0.39	0.82	0.52	0.61
DECOLOR [7]	0.24	0.92	0.38	0.77	0.88	0.82	0.89	0.83	0.86	0.44	0.93	0.60	0.74	0.84	0.79	0.71	0.80	0.75	0.30	0.69	0.42	0.58	0.84	0.66
MTTP [3]	0.74	0.67	0.70	0.67	0.84	0.74	0.71	0.84	0.77	0.64	0.86	0.73	0.62	0.77	0.69	0.55	0.73	0.62	0.25	0.49	0.33	0.60	0.74	0.65
D&T [19]	0.71	0.91	0.80	0.69	0.86	0.76	0.84	0.84	0.84	0.75	0.85	0.80	0.63	0.82	0.71	0.64	0.76	0.70	0.83	0.43	0.56	0.73	0.78	0.74
E-LSD [8]	0.71	0.83	0.77	0.75	0.88	0.81	0.64	0.67	0.65	0.61	0.86	0.72	0.57	0.92	0.70	0.55	0.82	0.66	0.58	0.61	0.60	0.63	0.80	0.70
WSNM-STTN	0.79	0.93	0.85	0.79	0.91	0.84	0.92	0.93	0.92	0.63	0.92	0.75	0.75	0.89	0.81	0.76	0.89	0.82	0.82	0.82	0.82	0.78	0.90	0.83

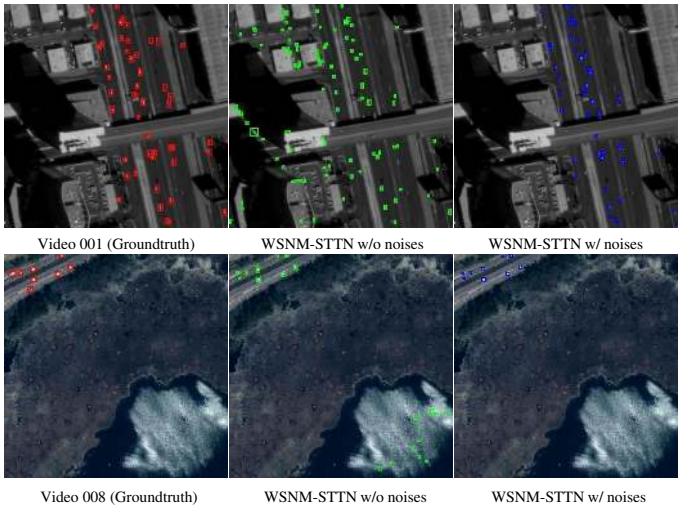

Figure 2. Demonstration on the importance of N in WSNM-STTN.

solve the over-shrink problem in low-rank estimation, which is superior to noiseless modeling methods. Then, we optimize our model by ADMM to detect objects. Extensive experiments show that WSNM-STTN can achieve a high detection rate and a low false alarms rate under complex background with heavy noise. In addition, WSNM-STTN converges faster than the matrix decomposition approach by a large margin.

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