

Multi-Element High-Lift Configuration Design Optimization Using Viscous Continuous Adjoint Method

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An adjoint-based Navier–Stokes design and optimization method for two-dimensional multi-element high-lift configurations is derived and presented. The compressible Reynolds-averaged Navier–Stokes equations are used as a flow model together with the Spalart–Allmaras turbulence model to account for high Reynolds number effects. When a viscous continuous adjoint formulation is used, the necessary aerodynamic gradient information is obtained with large computational savings over traditional finite difference methods. The high-lift configuration parallel design method uses a point-to-point matched multiblock grid system and the message passing interface standard for communication in both the flow and adjoint calculations. Airfoil shape, element positioning, and angle of attack are used as design variables. The prediction of high-lift flows around a baseline three-element airfoil configuration, denoted as 30P30N, is validated by comparison with available experimental data. Finally, several design results that verify the potential of the method for high-lift system design and optimization are presented. The design examples include a multi-element inverse design problem and the following optimization problems: lift coefficient maximization, lift-to-drag ratio maximization, and the maximum lift coefficient maximization problem for both the RAE2822 single-element airfoil and the 30P30N multi-element airfoil.

Nomenclature

C_d, C_l	=	airfoil coefficients of drag and lift
$C_{l_{\max}}$	=	maximum lift coefficient
C_p	=	pressure coefficient
$C_{p_{\text{crit}}}$	=	critical pressure coefficient
c	=	chord length
D	=	drag
\mathcal{F}	=	boundary shape
\mathcal{G}	=	gradient vector
H	=	total enthalpy
I	=	cost function
L	=	lift
M_∞	=	freestream Mach number
p	=	static pressure
p_d	=	desired target static pressure
R	=	governing equations or residual
Re	=	Reynolds number
S	=	surface area
t/c	=	thickness-to-chord ratio
w	=	conservative flow variables in Cartesian coordinates
x, y	=	Cartesian coordinates
y^+	=	dimensionless wall distance
α	=	angle of attack
$\alpha_{\text{cl max}}$	=	stall angle of attack
δ	=	first variation
λ	=	step size in steepest descent method
ψ	=	Lagrange multiplier, costate or adjoint variables

I. Introduction

AERODYNAMIC shape design has long been a challenging objective in the study of fluid dynamics. Computational fluid dynamics (CFD) has played an important analysis role in the aerodynamic design process since its introduction. However, CFD has been mostly used in the analysis of aerodynamic configurations to aid in the design process rather than to serve as a direct design tool in aerodynamic shape optimization. Although several attempts have been made in the past to use CFD as a direct design tool,^{1–5} it has not been until recently that the focus of CFD applications has shifted to aerodynamic design.^{6–11} This shift has been mainly motivated by the availability of high-performance computing platforms and by the development of new and efficient analysis and design algorithms. In particular, automatic design procedures that use CFD combined with gradient-based optimization techniques have made it possible to remove difficulties in the decision making process faced by the applied aerodynamicist.

In gradient-based optimization methods, finding a fast and accurate way of calculating the necessary gradient information is essential to developing an effective design method because this can be the most time-consuming portion of the design algorithm. Gradient information can be computed using a variety of approaches, such as the finite difference method, the complex-step method,¹² and automatic differentiation.¹³ Unfortunately, except for the case of the reverse mode of automatic differentiation, their computational cost is proportional to the number of design variables in the problem, which can be rather large.

An alternative choice, the control theory approach, has dramatic computational cost and storage advantages when compared to any of these methods. The foundation of control theory for systems governed by partial differential equations was laid by Lions.¹⁴ The control theory approach is often called the adjoint method because the necessary gradients are obtained via the solution of the adjoint equations of the governing equations of interest. The adjoint method is extremely efficient because the computational expense incurred in the calculation of the complete gradient is effectively independent of the number of design variables. The only cost involved is the calculation of one flow solution and one adjoint solution, whose complexity is similar to that of the flow solution. Control theory was applied in this way to shape design for elliptic equations by Pironneau,¹⁵ and it was first used in transonic flow by Jameson.^{6,7,16} Since then, this method has become a popular choice for design problems involving fluid flow.^{9,17–19}

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Most of the early work in the formulation of the adjoint-based design framework used the potential and Euler equations as models of the fluid flow. Aerodynamic design calculations using the Reynolds-averaged Navier–Stokes equations as the flow model have only recently been tackled. In 1997, a continuous adjoint method for aerodynamic shape optimization using the compressible Navier–Stokes equations was formulated, and it has been implemented directly in a three-dimensional wing problem.^{16,20} Because these design calculations were carried out without the benefit of a careful check of the accuracy of the resulting gradient information, a series of numerical experiments in two dimensions were conducted by the authors²¹ to determine the validity of the results. Existing approaches to the adjoint method can be classified into two categories: the continuous adjoint and discrete adjoint methods. If the adjoint equations are directly derived from the governing equations and then discretized, they are termed continuous, whereas if, instead, they are directly derived from the discretized form of the governing equations they are referred to as discrete. In theory, the discrete adjoint method should give gradients that are closer in value to exact finite difference gradients. On the other hand, the continuous adjoint method has the advantage that the adjoint system has a unique form independent of the scheme used to solve the flowfield system. Nadarajah and Jameson²² have recently performed a detailed gradient comparison study of the continuous and discrete adjoint approaches using the Navier–Stokes equations and found that in typical shape optimization problems in transonic flow the differences are small enough that they have no significant effect on the final result. Our work has mainly been based on the continuous adjoint method. In fact, this method has been successfully used for the aerodynamic design of complete aircraft configurations^{8,23} and has been extended to treat aerostructural design.²⁴

The research in this paper addresses the validity of this design methodology for the problem of high-lift design. Traditionally, high-lift designs have been realized by careful wind-tunnel testing. This approach is both expensive and challenging due to the extremely complex nature of the flow interactions that appear. CFD analyses have recently been incorporated to the high-lift design process.^{25–27} Eyi et al.²⁸ have performed design optimizations of a high-lift system configuration with use of a chimera overlaid grid system and the incompressible Navier–Stokes equations. Besnard et al. performed optimizations of high-lift systems using an interactive boundary layer approach.²⁹ All of these earlier works on multi-element airfoil design obtained the necessary gradients by finite difference methods. More recently, discrete adjoint gradients have also been used for the design of multi-element airfoil configurations.^{30–32}

In this work, the continuous viscous adjoint method is applied to two-dimensional high-lift system designs, which removes the limitations on the dimensionality of the design space by making use of the viscous adjoint design methodology. The motivation for our study of high-lift system design is twofold. On the one hand, we would like to improve the takeoff and landing performance of existing high-lift systems using an adjoint formulation, whereas on the other hand, we would like to setup numerical optimization procedures that can be useful to the aerodynamicist in the rapid design and development of high-lift system configurations. In addition to difficulties involved in the prediction of complex flow physics, multi-element airfoils provide an additional challenge to the adjoint method: The effect of the changes in the shape of one element must be felt by the other elements in the system. Whereas preliminary studies of the adjoint method in such a situation have already been carried out,^{19,33,34} this research is designed to validate the adjoint method for complex applications of this type. Emphasis is placed on the validation and not on the creation of realistic designs, which is beyond the scope of this work.

II. Procedure

In this section, we outline the overall design procedure used for a variety of design calculations that will be presented later. After the initial flowchart, each of the elements of the procedure is explained in more detail. In practical implementations of the adjoint method, a design code can be modularized into several components such

as the flow solver, adjoint solver, geometry and mesh modification algorithms, and optimization algorithm. After the configuration of interest is parameterized using a set of design variables and a suitable cost function, which is typically based on aerodynamic performance is defined, the design procedure can be described as follows. First, we solve the flow equations for the flow variables, followed by a solution of the adjoint equations for the costate variables subject to appropriate boundary conditions that will depend on the form of the cost function. Next, we evaluate the gradients and update the aerodynamic shape based on the direction of steepest descent. Finally, we repeat the process to attain an optimum configuration. A summary of the design process and a comparison with the finite difference method are shown in Fig. 1.

A. Continuous Adjoint Method

The progress of a design procedure is measured in terms of a cost function I , which could be, for example, the drag coefficient or the lift-to-drag ratio. For the flow about an airfoil or wing, the aerodynamic properties that define the cost function are functions of both the flowfield variables w and the physical location of the boundary, which may be represented by the function \mathcal{F} . Then,

$$I = I(w, \mathcal{F})$$

and a change in \mathcal{F} results in a change

$$\delta I = \left[\frac{\partial I^T}{\partial w} \right]_I \delta w + \left[\frac{\partial I^T}{\partial \mathcal{F}} \right]_{II} \delta \mathcal{F} \quad (1)$$

in the cost function. Here, the subscripts I and II are used to distinguish the contributions due to the variation δw in the flow solution from the change associated directly with the modification $\delta \mathcal{F}$ in the shape.

With use of the control theory, the governing equations of the flowfield are introduced as a constraint in such a way that the final expression for the gradient does not require multiple flow solutions. This corresponds to eliminating δw from Eq. (1).

Suppose that the governing equation R that expresses the dependence of w and \mathcal{F} within the flowfield domain D can be written as

$$R(w, \mathcal{F}) = 0 \quad (2)$$

Then, δw is determined from the equation

$$\delta R = \left[\frac{\partial R}{\partial w} \right]_I \delta w + \left[\frac{\partial R}{\partial \mathcal{F}} \right]_{II} \delta \mathcal{F} = 0 \quad (3)$$

Next, introducing a Lagrange multiplier ψ , we have

$$\begin{aligned} \delta I &= \left[\frac{\partial I^T}{\partial w} \right]_I \delta w + \left[\frac{\partial I^T}{\partial \mathcal{F}} \right]_{II} \delta \mathcal{F} - \psi^T \left(\left[\frac{\partial R}{\partial w} \right]_I \delta w + \left[\frac{\partial R}{\partial \mathcal{F}} \right]_{II} \delta \mathcal{F} \right) \\ &= \left\{ \frac{\partial I^T}{\partial w} - \psi^T \left[\frac{\partial R}{\partial w} \right]_I \right\} \delta w + \left\{ \frac{\partial I^T}{\partial \mathcal{F}} - \psi^T \left[\frac{\partial R}{\partial \mathcal{F}} \right]_{II} \right\} \delta \mathcal{F} \end{aligned}$$

With the choice of ψ to satisfy the adjoint equation,

$$\left[\frac{\partial R}{\partial w} \right]_I^T \psi = \frac{\partial I}{\partial w} \quad (4)$$

the first term is eliminated, and we find that

$$\delta I = \mathcal{G} \delta \mathcal{F} \quad (5)$$

where

$$\mathcal{G} = \frac{\partial I^T}{\partial \mathcal{F}} - \psi^T \left[\frac{\partial R}{\partial \mathcal{F}} \right]_{II} \quad (6)$$

The advantage is that Eq. (5) is independent of δw , with the result that the gradient of I with respect to an arbitrary number of

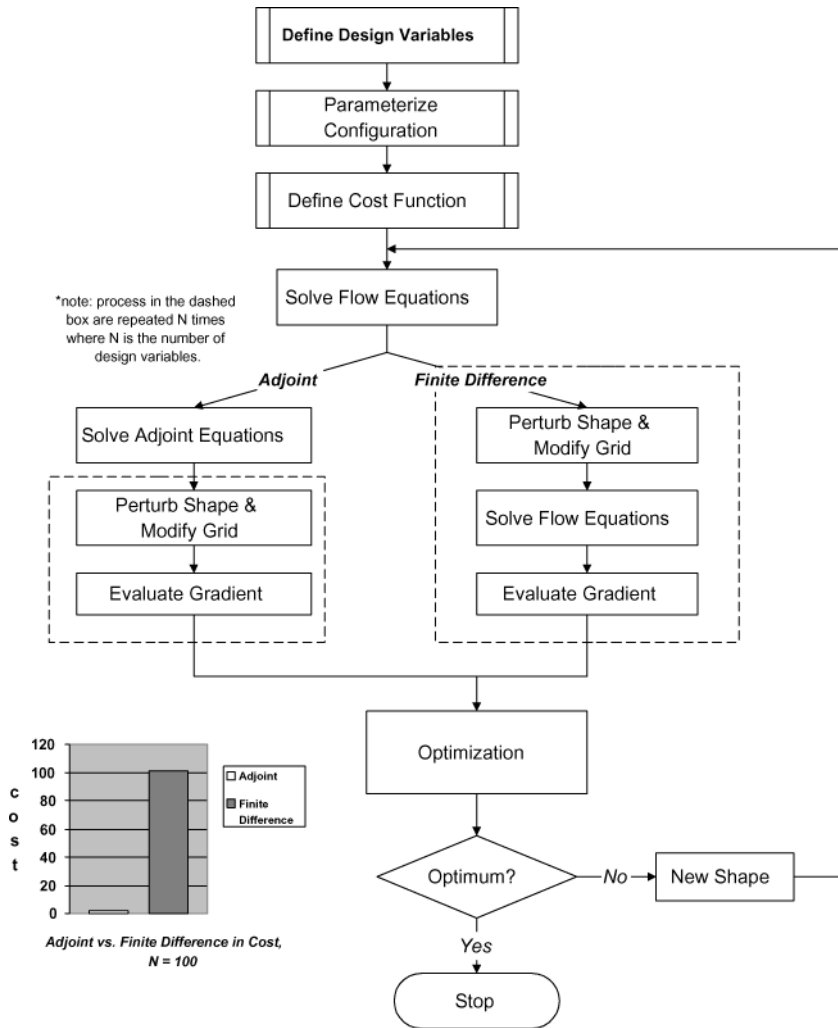


Fig. 1 Flowchart of the design process.

design variables can be determined without the need for additional flow-field evaluations. In the case that Eq. (2) is a partial differential equation, the adjoint equation (4) is also a partial differential equation, and the determination of the appropriate boundary conditions requires careful mathematical treatment.

The formulation of the viscous adjoint equation and the boundary conditions are described in greater detail in previous publications,³⁵ and a detailed gradient accuracy study for the continuous adjoint method has been carried out under the assumption that both the viscosity (laminar plus turbulent) and heat conduction coefficients are essentially independent of the flow and that their variations may be neglected.²¹ This simplification has been successfully used for many aerodynamic problems of interest. However, if the flow variations result in significant changes in the turbulent eddy viscosity, it may be necessary to account for this effect in the calculation.^{36–38}

B. Baseline Configuration

Wind-tunnel measurements have been performed on several three-element airfoil configurations at the NASA Langley Research Center Low Turbulence Pressure Tunnel at various Reynolds and Mach numbers,^{39–42} and the results of many CFD computations for this geometry have been reported using a variety of numerical schemes for the discretization of the Navier–Stokes equations and different turbulence models.^{26,43–45} The three-element configuration used in these studies, denoted as 30P30N, is the starting point for the present design optimization process. Note that the 30P30N configuration had already been highly optimized for $C_{l,max}$. The relative element positioning of the slat, main element, and flap are

described by the rigging quantities. These variables include flap and slat deflection angles, gaps, and overlaps. The meaning of these variables can be easily seen in Fig. 2. The initial deflections of both the slat and the flap are set at 30 deg, the flap gap and overlap are $0.0127c/0.0025c$, whereas for the slat the gap and overlap are $0.0295c/0.025c$. In these measurements, c is the airfoil chord with the slat and flap retracted.

C. Grid Topology

Multiblock viscous and inviscid meshes were generated using either a C (viscous) or O topology (inviscid) before the beginning of the iterative design loop so that the flow and adjoint equations could be suitably discretized. Figure 3 shows a typical viscous multiblock mesh generated around the 30P30N configuration.

One-to-one point connectivity between block faces is employed to ensure conservation across boundaries and to provide for continuity of the grid at block interfaces. Spacing at the wall is set to be less than $2 \times 10^{-6}c$ to obtain $y^+ \approx 1$ based on turbulent flat plate boundary-layer thickness estimates at the Reynolds number in question, $Re = 9 \times 10^6$. The use of a grid with adequately tight wall spacing [$y^+ = \mathcal{O}(1)$] has been reported to be necessary to obtain accurate resolution of the wall boundary layers, wakes, and shear layers present in the problem.^{44,45} Grid lines are also bunched along the expected wake trajectories of each of the elements. Once the initial grid is generated, new grids corresponding to modified airfoil shapes are obtained automatically during the design process by the use of a two-dimensional version of the automatic mesh perturbation scheme (WARP-MB)^{10,11,23,46} that is essentially equivalent to

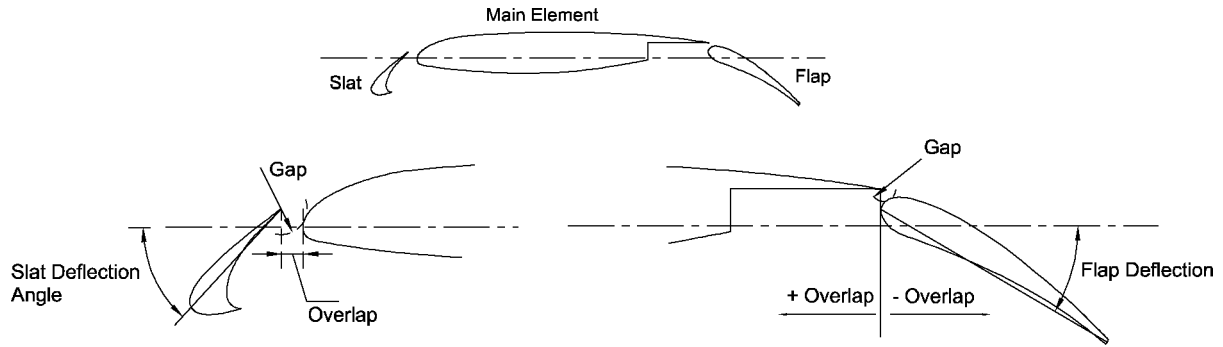


Fig. 2 Definitions of gap, overlap, and deflection angles.

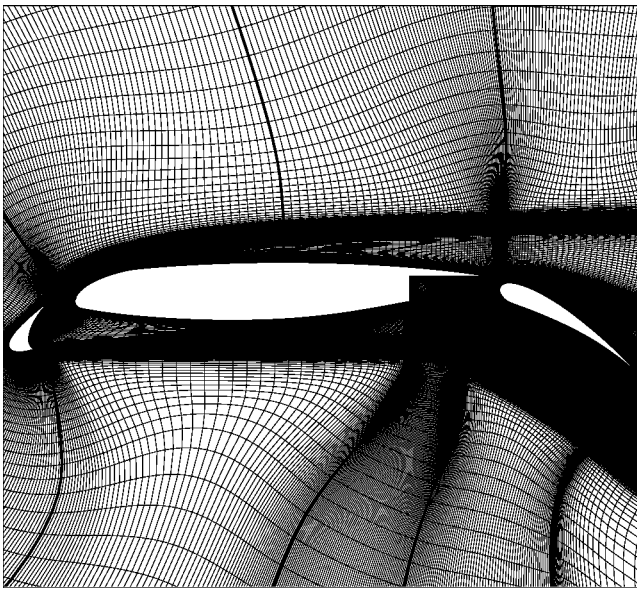


Fig. 3 Grid around the 30P30N multi-element configuration.

shifting grid points along coordinate lines depending on the modifications to the shape of the boundary.

Mesh perturbations are applied only to those blocks that contain a face that is part of the 30P30N baseline configuration surface. Because the block interfaces are modified only by the motion of their endpoints, the initial one-to-one point connectivity between block faces remains valid throughout the complete range of surface deformations. The authors have previously handled the complexity of multiblock mesh perturbation after large baseline geometry changes.⁴⁷

D. Multiblock Flow and Adjoint Solvers

The prediction of high-lift flows poses a particularly difficult challenge for both CFD and turbulence modeling. Even in two dimensions, the physics involved in the flow around a geometrically complex high-lift device are quite sophisticated. In this study FLO103-MB, a multiblock Reynolds averaged Navier–Stokes (RANS) solver derived from the work of Martinelli and Jameson⁴⁸ and similar to the three-dimensional version of Reuther and Alonso,⁹ is used for multi-element airfoil flowfield predictions. FLO103-MB satisfies the requirements of accuracy, convergence, and robustness that are necessary in this work. FLO103-MB solves the steady two-dimensional RANS equations using a modified explicit multistage Runge–Kutta time-stepping scheme. A finite volume technique and second-order central differencing in space are applied to the integral form of the Navier–Stokes equations. The Jameson–Schmidt–Turlak scheme with adaptive coefficients for artificial dissipation is used to prevent odd–even oscillations and to allow for the clean capture of shock waves and contact discontinuities. In addition,

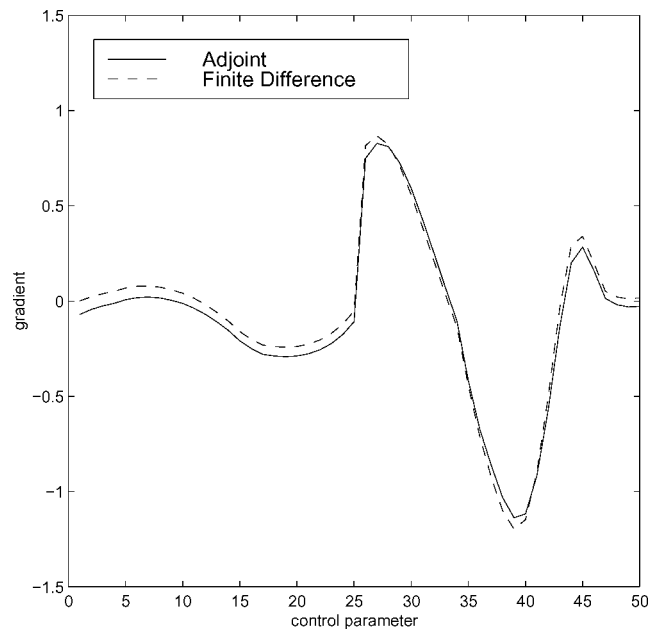


Fig. 4 Navier–Stokes inverse design: comparison of finite difference and adjoint gradients for a 512×64 mesh.

local time stepping, implicit residual smoothing, and the multi-grid method are applied to accelerate convergence to steady-state solutions. The Baldwin–Lomax algebraic model and the Spalart–Allmaras one-equation model are used to account for the Reynolds stresses. The adjoint gradient accuracy study, which was presented in a previous publication,²¹ was based on the Baldwin–Lomax model. This model is also used for the single-element design cases in this paper. Although this algebraic model has some advantages due to its implementational simplicity and robustness, the use of this model must be restricted to design at lower angles of attack and to the design of simpler geometries such as single-element airfoils. For actual high-lift designs such as $C_{l_{\max}}$ maximization, the one-equation Spalart–Allmaras⁴⁹ model gives better predictions of both the $C_{l_{\max}}$ and the flow physics around complex geometries.^{26,43,49}

The solution of the Spalart–Allmaras turbulence model is an adaptation of McNeil’s implementation⁵⁰ embedded in the three-dimensional version of our flow solver. The trip terms are not included in the turbulence model, and fully turbulent flow is assumed. The turbulence equation is solved separately from the flow equations using an alternating direction implicit method, and it is updated at the start of each multistage Runge–Kutta time step on the finest grid of the multigrid cycle only. The adjoint solution is obtained with the exact same numerical techniques used for the laminar flow solution with the assumption of frozen eddy viscosity. The implementation exactly mirrors the flow solution modules inside FLO103-MB, except for the boundary conditions, which are imposed on the costate variables. The parallel implementation uses

a domain decomposition approach, a single program multiple data program structure, and the message passing interface standard for message passing.

E. Design Variables

For the present study, gaps and overlaps are used in an indirect way because the rigging is controlled by the translation of the slat and flap leading edges in the x and y directions. In this way, the element positioning variables can be more easily changed independently of each other. The actual values of overlaps and gaps can be easily recovered from the leading- and trailing-edge locations of the various elements in the airfoil. The shapes of each of the elements are also used as design variables to not rule out the possibility that

the optimum solution may be obtained with a combination of shape and position modifications. In fact, for the drag minimization of a single-element RAE2822 airfoil in transonic flow, the strong shock that appears at transonic flow conditions can only be eliminated using a small change in the shape of the airfoil. The coordinates of mesh nodes on the surface of the airfoil, Hick–Henne “bump” functions, patched polynomials, and frequency-based decompositions can be used to represent each of the elements in the high-lift system. For example, a number of the following Hicks–Henne functions, which have been implemented and used for this study, may be added to the baseline airfoil to modify the shape,

$$b(x) = A[\sin(\pi x^{\log 5 / \log t_1})]^{t_2}, \quad 0 \leq x \leq 1 \quad (7)$$

where A is the maximum bump magnitude, t_1 locates the maximum of the bump at $x = t_1$, and t_2 controls the width of the bump. When this parameterization is used, two options are available for obtaining the optimum $C_{l_{max}}$. First, $C_{l_{max}}$ can be predicted by maximizing C_l at a given angle of attack, then predicting $C_{l_{max}}$ along a C_l vs α line for that configuration, and repeating this procedure iteratively. In this way, the angle of attack α is only considered as a design variable once the intermediate shape of the airfoil has been frozen within each design cycle. Alternatively, $C_{l_{max}}$ may also be maximized directly by including angle of attack as a design variable in the optimization process.

F. Numerical Optimization Method

The search procedure used in this work is a simple steepest descent method in which small steps are taken in the negative gradient direction,

$$\delta \mathcal{F} = -\lambda \mathcal{G}$$

where λ is positive and small enough that the first variation is an accurate estimate of δI . Then

$$\delta I = -\lambda \mathcal{G}^T \mathcal{g} < 0$$

After such a modification is made, the gradient can be recalculated and the process repeated to follow a path of steepest descent until a minimum is reached. To avoid violating constraints, such as a

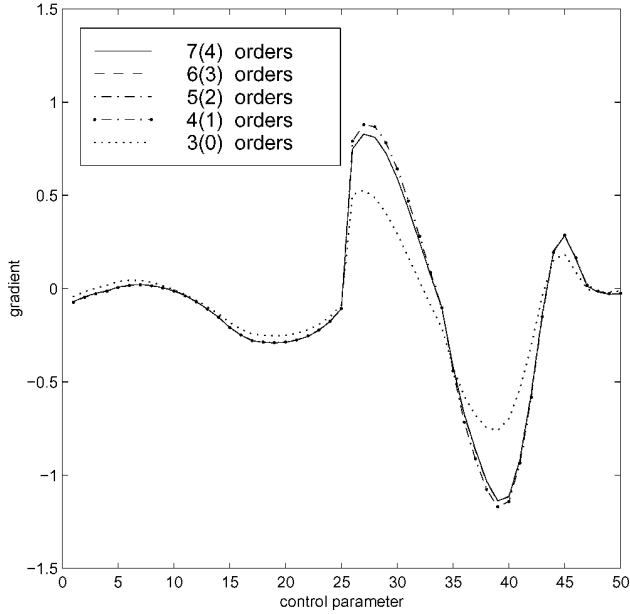


Fig. 5 Navier–Stokes inverse design: adjoint gradients for varying levels of flow solver convergence.

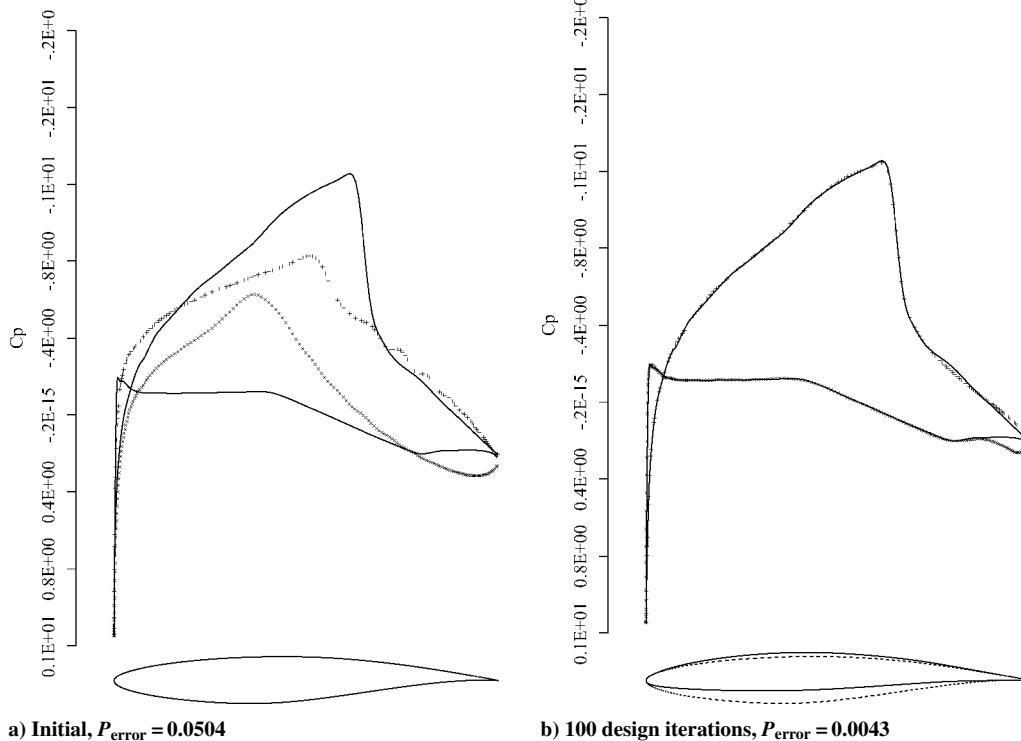


Fig. 6 Typical Navier–Stokes inverse design calculation, RAE 2822 airfoil to NACA64A410, $M_\infty = 0.75$, $\alpha = 0$ deg, and $Re = 6.5 \times 10^6$.

minimum acceptable airfoil thickness, the gradient may be projected into an allowable subspace within which the constraints are satisfied. In this way, procedures can be devised that must necessarily converge at least to a local minimum.

III. Results

A. Validation of the Adjoint Method for Viscous Flows

This section presents the results of a gradient accuracy study for the RANS equations using the Baldwin–Lomax turbulence model, as well as a simple example of the use of the resulting gradient information in a single-element airfoil inverse design case. Gradient accuracy is assessed by comparison with finite difference gradients and by examination of the changes in the magnitude of the gradients for different levels of flow solver convergence. For inverse design, the aerodynamic cost function chosen is given by

$$I = \frac{1}{2} \int_B (p - p_d)^2 dS \quad (8)$$

which is simply the Euclidean norm of the difference between the current pressure distribution and a desired target p_d at a constant angle of attack α . The gradient of the preceding cost function is obtained with respect to variations in 50 Hicks–Henne sine bump functions centered at various locations along the upper and lower surfaces of a baseline airfoil. The locations of these geometry perturbations are numbered sequentially such that they start at the lower surface of the trailing edge, proceed forward to the leading edge, and then back around to the upper surface of the trailing edge. Figure 4 shows a comparison between the most accurate gradients obtained using both the adjoint and finite difference methods. There is a general agreement on all trends, which validates the implementation of the present adjoint method. Some discrepancies exist, which are attributed to several sources. First, there is the issue that the finite difference gradients never achieved step size independence, and therefore, a step size had to be selected for this plot that may not be the correct one. Second, there is the issue of mesh resolution.²¹ Third, the present adjoint equation is obtained without taking into account the dependence of the dissipation coefficients on the flow variables. A detailed study on these issues was presented by Nadarajah and Jameson.²² The source of the discrepancies is believed to be a combination of these influences.

Figure 5 shows the computed adjoint gradients for different levels of flow solver convergence. For Navier–Stokes calculations, the adjoint information is essentially unchanged if the level of convergence in the flow solver is at least four orders of magnitude. This is an additional advantage of using the adjoint method over finite differencing especially for the design of high-lift configurations for which it is difficult to obtain levels of convergence much higher than four orders of magnitude. For viscous flows and finite differencing

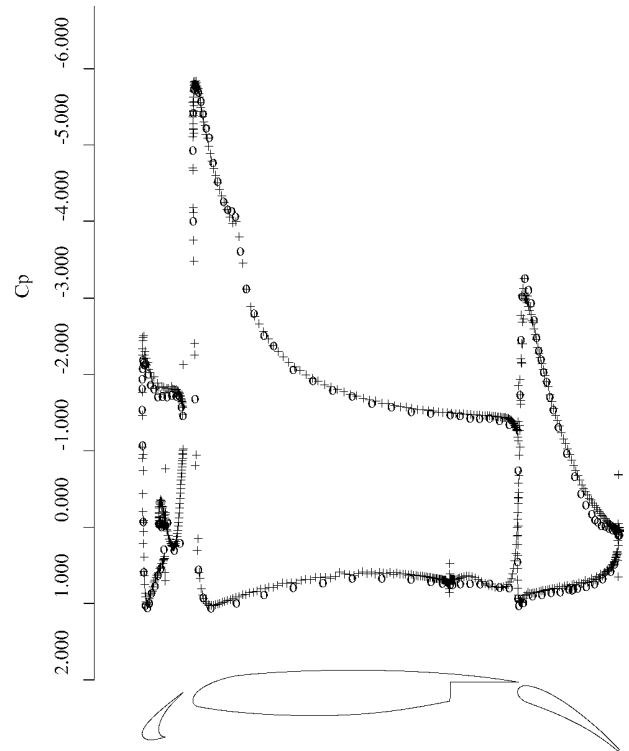
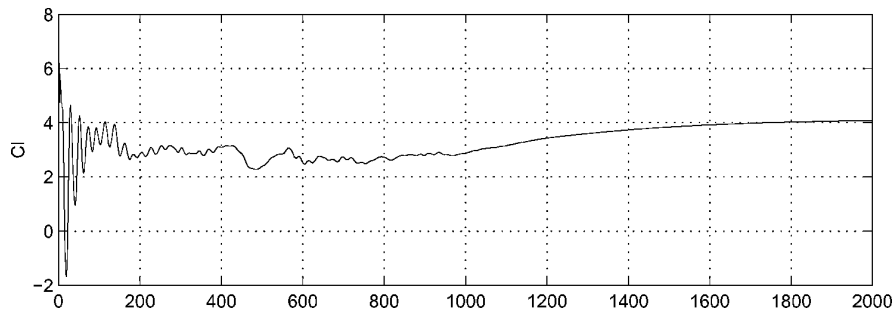
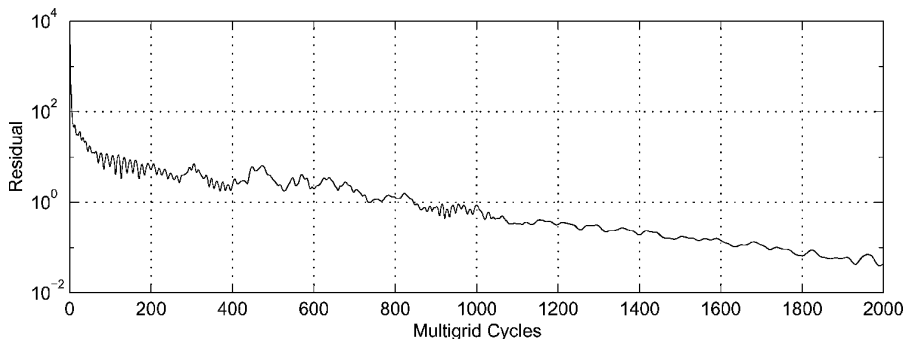


Fig. 8 Comparison of experimental and computational pressure coefficient distributions for the 30P30N multi-element airfoil, $M_\infty = 0.20$, $\alpha = 8$ deg, and $Re = 9 \times 10^6$: +, computational C_p and \circ , experimental C_p .



a) C_l convergence history



b) FLO103MB convergence history

Fig. 7 Convergence history of C_l and density residual for the 30P30N multi-element airfoil using SA turbulence model, $M_\infty = 0.20$, $\alpha = 16.02$ deg, and $Re = 9 \times 10^6$.

it is typical to require that the flow solver converge to about six orders of magnitude so that the gradient information is sufficiently accurate.

An inverse design problem that starts with an RAE2822 airfoil geometry and tries to obtain the shape that generates the pressure distribution around a NACA64A410 airfoil at the same flow conditions is presented next. The mesh used is a Navier–Stokes C mesh with 512×64 cells. The target pressure specified is that of the NACA64A410 airfoil at $M_\infty = 0.75$ and $\alpha = 0$ deg. The Reynolds number of this calculation was set at $Re = 6.5 \times 10^6$. Figure 6 shows the progress of the inverse design calculation. In 100 design iterations, the target pressure was matched almost exactly, including the correct strength and position of the shock. The areas around the trailing edge are very sensitive to small changes in the geometry. The source of the C_p discrepancy in the neighborhood of the trailing edge can be found in the inability of our parameterization to recover exactly the shape of the NACA64A010 airfoil. More geometry control may be required to produce more exactly matched solutions in the areas around the trailing-edge surface. After our design process, the initial RAE2822 airfoil geometry was altered to obtain a shape

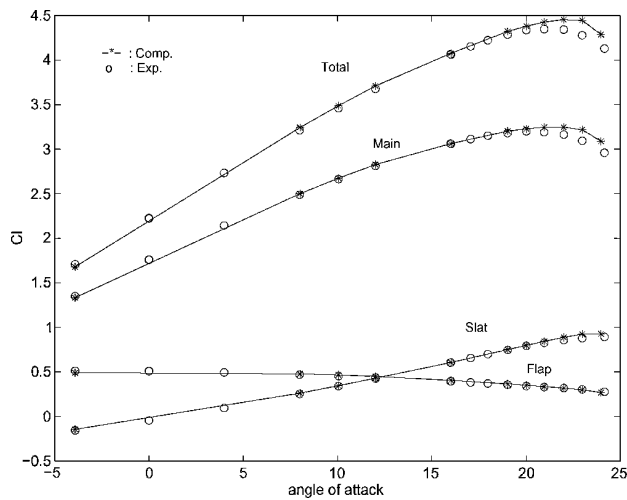


Fig. 9 Comparison of experimental and computational lift coefficient vs angle of attack for the 30P30N multi-element airfoil, $M_\infty = 0.20$ and $Re = 9 \times 10^6$; +, computational C_l and \circ , experimental C_l .

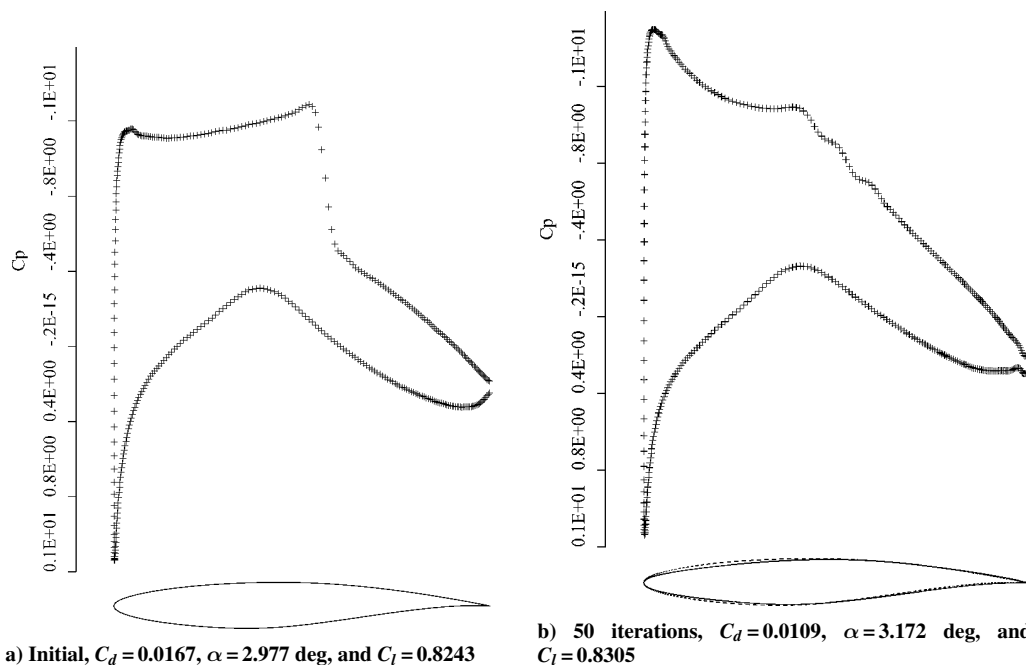


Fig. 10 Typical Navier–Stokes drag minimization calculation at fixed $C_l = 0.83$, $M_\infty = 0.73$, and $Re = 6.5 \times 10^6$; RAE2822 airfoil: ---, initial airfoil and —, current airfoil.

that is quite close to the NACA64A410 airfoil that had produced the target pressure distribution in the first place. Convergence of the design procedure is simply measured by the closeness of the resulting pressure distribution to the specified target. No attempt to satisfy the Kuhn–Tucker conditions was made. The norm of the pressure error decreased over two orders of magnitude from 0.0504 to 0.0043 in 100 design iterations.

B. FLO103-MB with Spalart–Allmaras Model

Before using FLO103-MB with the Spalart–Allmaras (SA) turbulence model for the design of multi-element airfoils, we must demonstrate that the model has been correctly implemented confirming that the solver can accurately predict the flow phenomena involved in this type of problem. In particular it is of primary importance to be able to predict the values of $C_{l_{max}}$, the element pressure distributions, the lift curve slopes for each element, and the details of the shear layers present in the problem.

1. Flow Convergence

Figure 7 shows the convergence history of the averaged density residual for the calculation of the flowfield around the 30P30N high-lift configuration using the flow solver FLO103-MB. The SA one-equation turbulence model is used for this calculation. The solution converges down to somewhere in the range between 10^{-4} and 10^{-5} in about 2000 iterations. Although small oscillations in the residual remain after 2000 iterations, the C_l , one of the cost functions used for subsequent designs, has converged without oscillations. As mentioned earlier, this level of convergence is also sufficient to obtain accurate sensitivity information using the adjoint method.

2. Comparisons with Experimental Data

Comparisons between computational results and experimental data are presented for validation purposes. The code FLO103-MB and the related turbomachinery code TFLO⁵¹ have been extensively validated for a variety of test cases, which range from flat plates and transonic axisymmetric bumps to full three-dimensional configurations.

Figure 8, shows the comparison of the computational and experimental C_p distributions around the 30P30N configuration at $M_\infty = 0.2$, $\alpha = 8$ deg, and $Re = 9 \times 10^6$. The agreement between experimental and computational distributions is very encouraging. Integrated force coefficients also agree quite well.

To validate the ability of the flow solver to predict stall using the SA turbulence model, a comparison of C_l vs angle of attack is shown in Fig. 9. The total coefficient of lift, together with the individual lift from the three components, is plotted in the range of $-5 < \alpha < 25$ deg. The computed results agree quite well with experiment with slightly higher predictions of $C_{l_{max}}$ and angle of attack at $C_{l_{max}}$. Although the results do not agree with the experiment exactly, it has been observed that the choice of turbulence model can have a substantial impact on the numerical values of some of these parameters. The stall prediction capability can be a critical factor for actual design cases, such as $C_{l_{max}}$ maximization. With other turbulence models, these quantities can be overpredicted substantially.

C. Single-Element Airfoil Design

Before the multi-element airfoil design was begun, a study of the use of optimization for single-element airfoils was performed to gain insight into the possibilities for improvements and the behavior of the method. C_d minimization at a fixed C_l and C_l maximization at a fixed C_d were tested to guarantee the improvement of the lift over drag ratio L/D , which is a measure of the aerodynamic efficiency. The design examples presented in this subsection were all carried out using a four-block multiblock mesh around an RAE2822 airfoil with a total number of cells equal to 512×64 . The two designs presented had as a starting point the RAE2822 airfoil, and computations were carried out at a Reynolds number of 6.5×10^6 . The surface of the

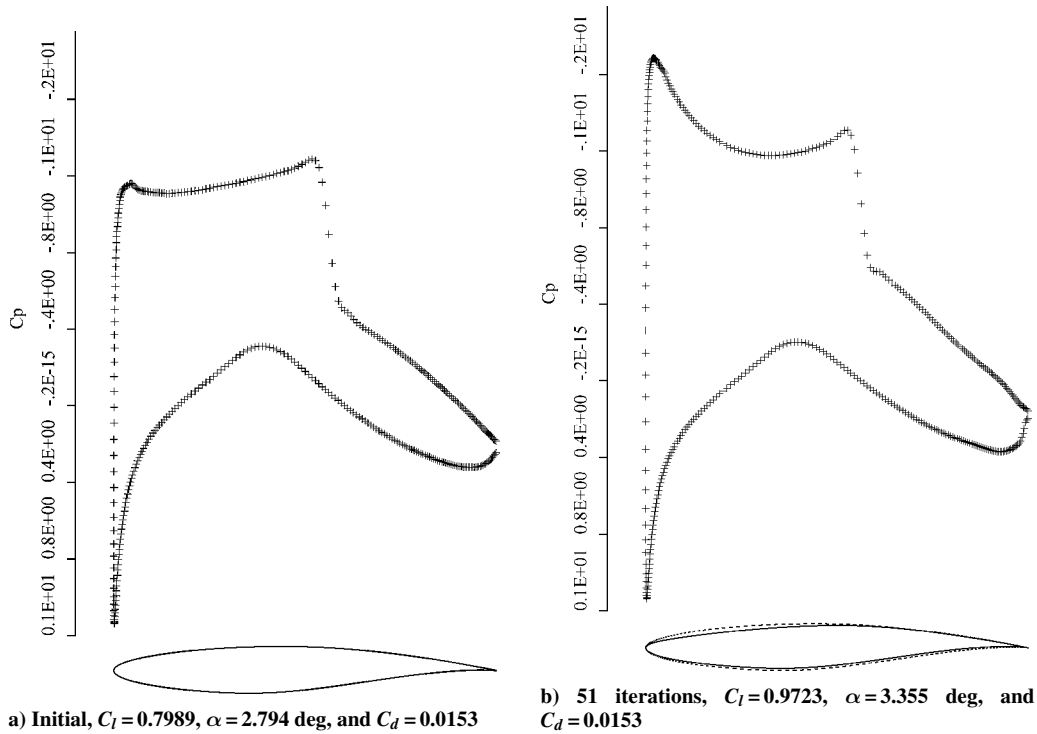


Fig. 11 Typical Navier–Stokes lift maximization calculation at fixed $C_d = 0.0153$, RAE2822 airfoil, $M_\infty = 0.73$, and $Re = 6.5 \times 10^6$: ---, initial airfoil and —, current airfoil.

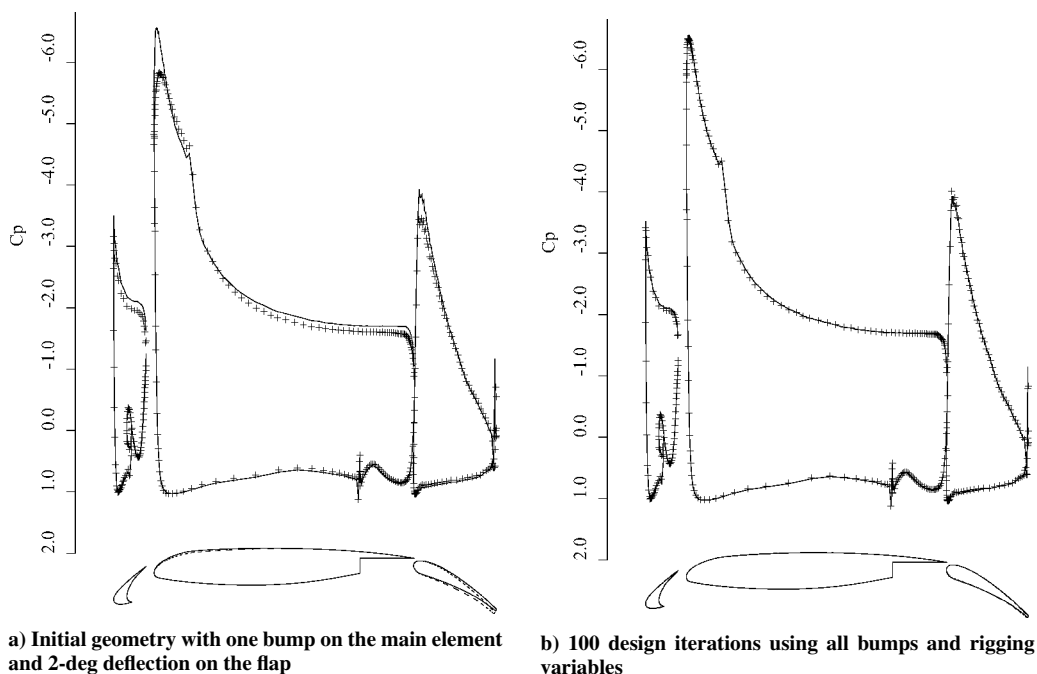


Fig. 12 Example of the 30P30N multi-element Euler inverse design, $M_\infty = 0.2$ and $\alpha = 8.0$ deg: +, actual C_p ; —, target C_p ; ---, initial airfoil; and —, target airfoil.

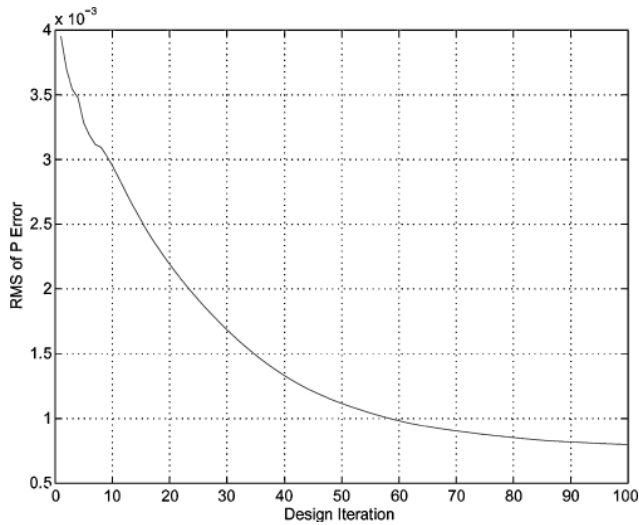


Fig. 13 Convergence history of pressure difference for the 30P30N multi-element Euler inverse design.

airfoil was parameterized using 50 Hicks–Henne bump functions, 25 of which are distributed evenly along the upper surface of the airfoil, whereas the remaining 25 are placed in a similar fashion along the lower surface.

1. C_d Minimization at a Fixed C_l

Figure 10 shows the result of a typical viscous design calculation where the total coefficient of drag of the airfoil is minimized using the parameterization described earlier. The freestream Mach number is 0.73, and the optimization procedure is forced to achieve a near constant $C_l = 0.83$. This constraint is achieved by periodically adjusting the angle of attack during the flow solution portion of the design procedure in what is sometimes called a reduced gradient approach. Figure 10 shows the result of 50 design iterations for this test case. The optimizer is able to eliminate the strong shock wave that existed in the initial design by using the values of the same 50 design variables. Once the design process is completed, the total coefficient of drag has been reduced from 0.0167 to 0.0109, whereas the C_l has increased very slightly from 0.8243 to 0.8305. The L/D has improved by 54.36% from 49.36 to 76.19. This test case also provides a validation of the multiblock design procedure because a similar test case had previously been run using the single-block design code.

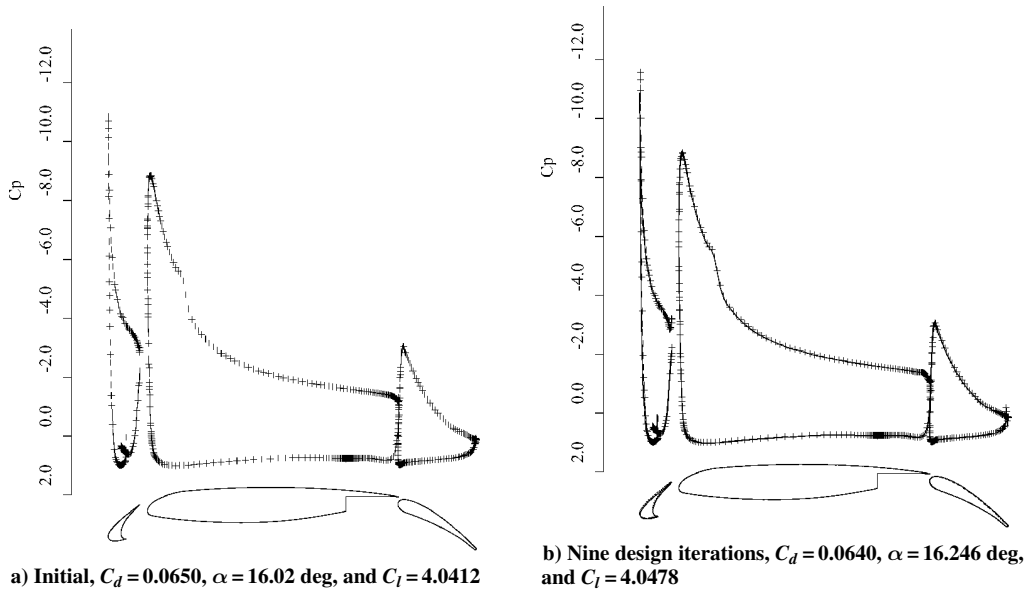


Fig. 14 Multi-element airfoil drag minimization calculation at fixed $C_l = 4.04$, $M_\infty = 0.2$, $Re = 9 \times 10^6$, 30P30N: ---, initial airfoil and —, current airfoil.

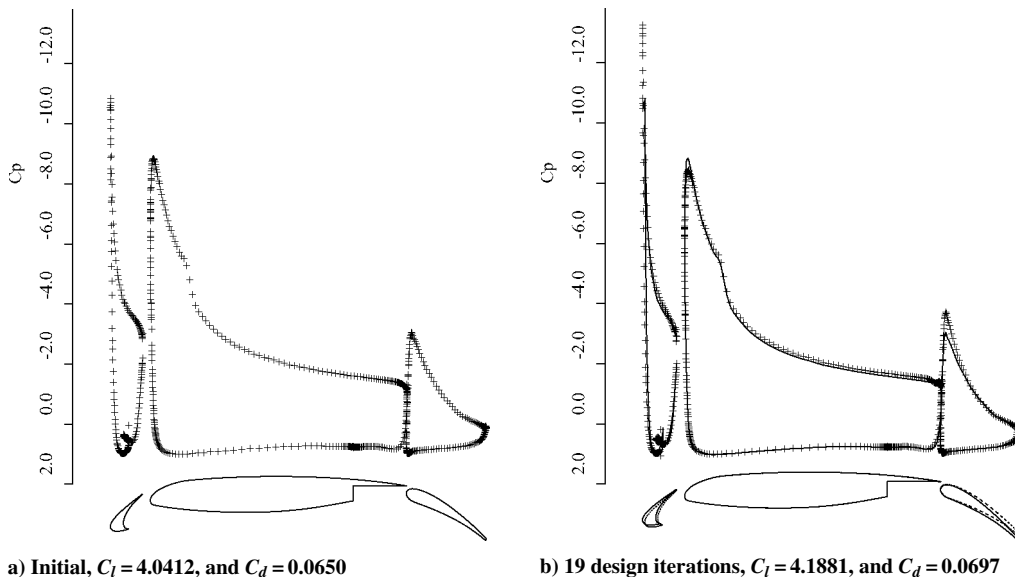


Fig. 15 Multi-element airfoil lift maximization calculation at fixed $\alpha = 16.02$ deg, $M_\infty = 0.2$, $Re = 9 \times 10^6$, 30P30N: +, current C_p ; —, initial C_p ; —, current airfoil; and ---, initial airfoil.

2. C_l Maximization at a Fixed C_d

In this test case, we attempt to maximize the C_l of the RAE2822 airfoil by altering its shape using the same 50 Hicks–Henne design functions while constraining the coefficient of drag to be constant ($C_d = 0.0153$). Figure 11 shows the result of this type of design optimization. The front portion of the upper surface of the configuration is modified considerably to produce a very different pressure distribution that allows for the existence of a shock wave on the upper surface that considerably increases the amount of lift carried by the airfoil. In addition, because the C_d is constrained to be constant (imposed by allowing the angle of attack to float), the resulting angle of attack is also higher, which again leads to the creation of a higher lift coefficient. The numerical results presented show significant improvements in L/D . The resulting L/D increased 21.70% from 52.22 to 63.55.

D. Multi-Element Airfoil Design

Except for the inviscid test case presented in the first subsection to follow, all of the results in this section were computed using multiblock viscous meshes constructed using a C topology. The C-topology mesh has 26 blocks of varying sizes and a total of 204,800 cells. All calculations were carried out at a freestream Mach number

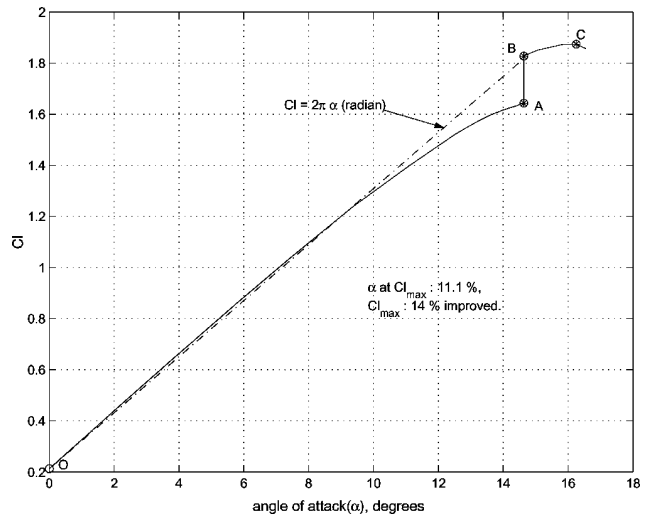


Fig. 18 Design curve of approach 1 for the RAE2822 $C_{l,max}$ maximization, $M_\infty = 0.20$, $Re = 6.5 \times 10^6$: O–A, C_l vs α curve of baseline; A–B, design curve using bumps; and B–C, C_l vs α curve of designed airfoil.

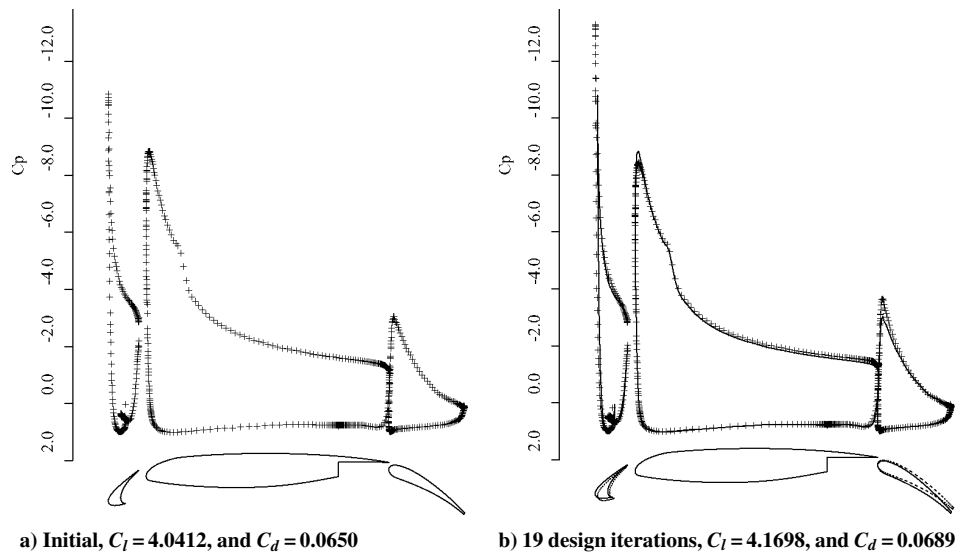


Fig. 16 Multi-element airfoil lift maximization using settings only at fixed $\alpha = 16.02$ deg, $M_\infty = 0.2$, 30P30N: +, current C_p ; —, initial C_p ; —, current airfoil; and ---, initial airfoil.

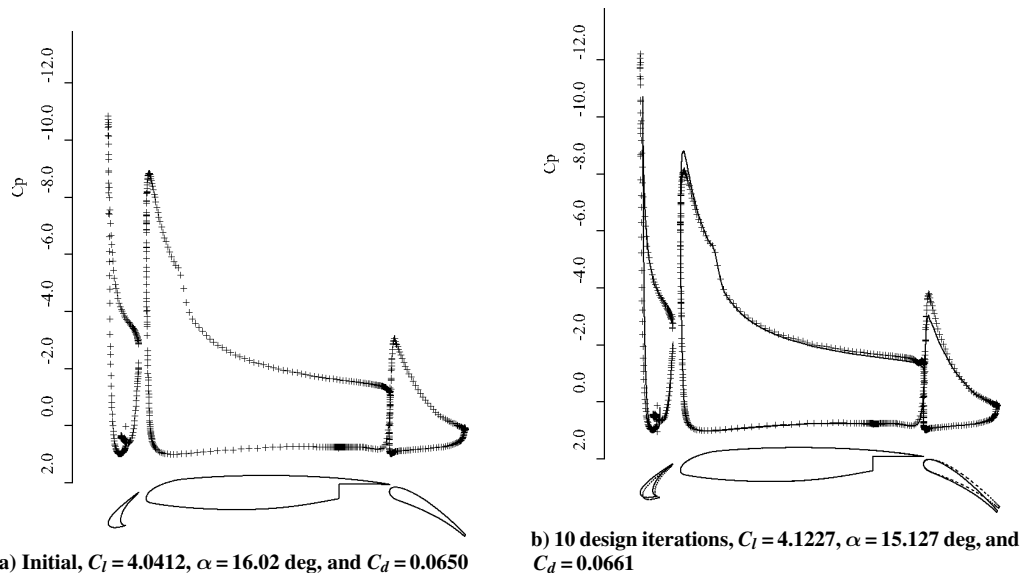


Fig. 17 Multi-element airfoil lift maximization calculation at fixed $C_d = 0.0650$, $M_\infty = 0.2$, 30P30N: +, current C_p ; —, initial C_p ; —, current airfoil; and ---, initial airfoil.

$M_\infty = 0.20$ and a Reynolds number $Re = 9 \times 10^6$. The computation of the Reynolds stress was carried out using the SA turbulence model. Apart from the first inviscid test case, the results in this section mimic those in the single-element airfoil section.

1. Inverse Design Using the Euler Equations

To verify the implementation of our design procedure, we present a simple test case that is aimed at verifying that the multiblock flow and adjoint solvers are capable of producing correct sensitivities to both shape modifications and rigging variables in a multi-element airfoil design environment. For this purpose, a multiblock inviscid grid around the 30P30N configuration was constructed. A perturbed geometry was created by activating a single bump on the upper surface of the main element and by deflecting the flap by an increment of 2 deg. The pressure distribution around the original geometry is used as a target pressure distribution (solid line in Fig. 12) for the perturbed geometry to arrive at through an inverse design process. Because this target pressure distribution is achievable, we can in-

directly measure the correctness of the sensitivity information by observing whether the design evolves toward the known specified target. Notice that the modification of the geometry described earlier influences the pressure distribution in all three elements: slat, main element, and flap.

A total of 156 design variables were used to parameterize the complete configuration, including 50 bump functions in each of the three elements. In addition, both the slat and the flap were allowed to translate in the x and y directions and to rotate about their leading edges. After 100 design iterations where sensitivities with respect to all design variables were calculated, the target pressure distribution was recovered as expected. The original geometry was also recovered, as shown in Fig. 12. Figure 13 shows the convergence history of the objective function. The results of this inviscid test case provide the necessary confidence to tackle some of the more complex viscous cases to be presented.

2. C_d Minimization at a Fixed C_l

In this test case, we attempt to minimize the total drag coefficient of the configuration without changing the lift coefficient. This design task is one of the most interesting problems because decreasing C_d without loss in C_l is the most effective way of increasing the lift over drag ratio of the airfoil at low Mach number (no shock waves) and at high angle-of-attack flight conditions (high initial lift coefficient). However, this case is also the most difficult one because a decrease in C_d usually comes at the expense of a decrease in C_l for the high-lift system configuration design. Notice that, as opposed to the single-element test case, the Mach number of the flow is subsonic throughout ($C_{p_{crit}} = -16.3$ for $M_\infty = 0.2$) and, therefore, no shock waves are present. A total of 9 design iterations were carried out and, as expected, with a slight increase in C_l , a small decrease (10 drag counts) in C_d was achieved as shown in Fig. 14. The resulting L/D increases by 1.73% from 62.17 (baseline L/D at $\alpha = 16.02$ deg) to 63.25. Notice that the resulting α has increased slightly while trying to maintain C_l unchanged.

3. C_l Maximization at Fixed Angle of Attack

We now maximize the C_l of the configuration using all 156 design variables in the problem. In this test case, the angle of attack of the whole configuration remains constant, $\alpha = 16.02$ deg. The optimizer is able to make improvements in C_l after 19 design iterations:

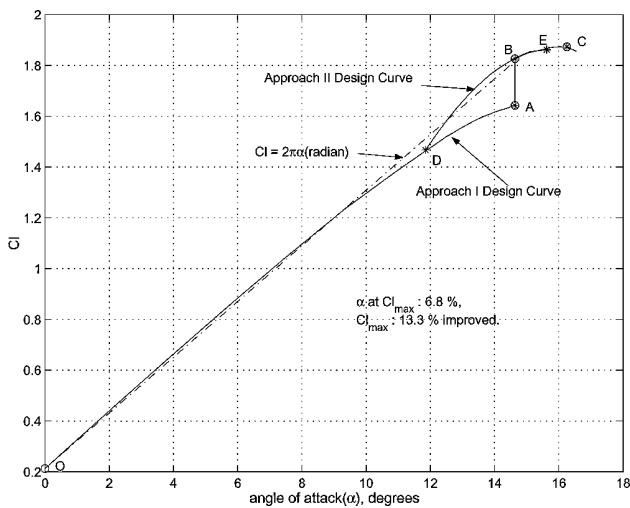


Fig. 19 Design curve of approach 2 for the RAE2822 $C_{l_{max}}$ maximization, $M_\infty = 0.20$, $Re = 6.5 \times 10^6$: D–E, approach 2 design curve.

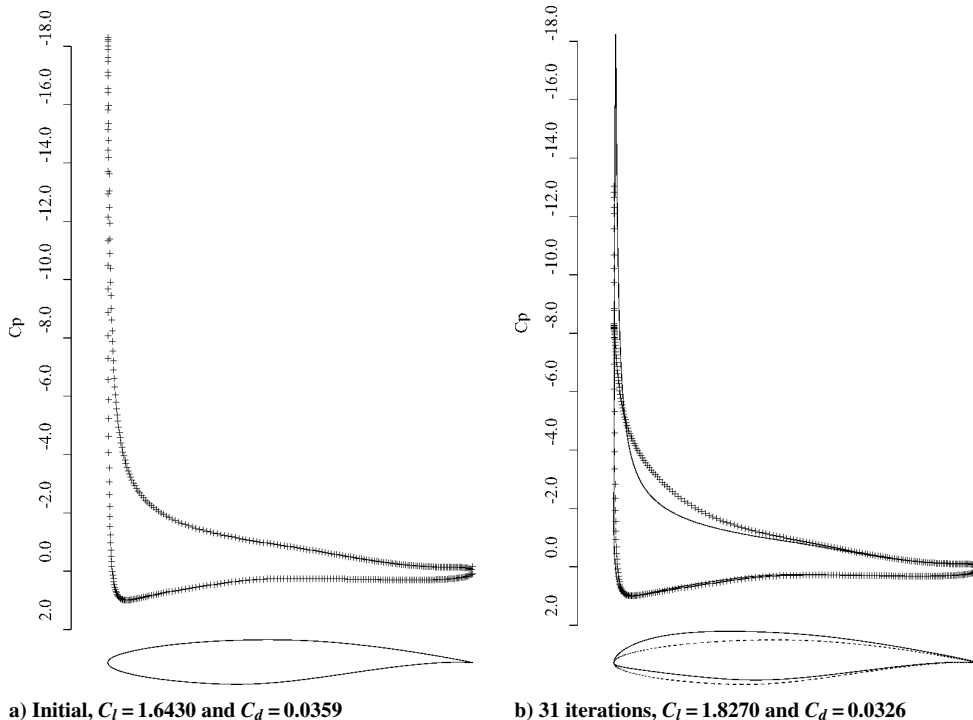


Fig. 20 RAE2822 $C_{l_{max}}$ maximization calculation at a fixed $\alpha = 14.633$ deg, $M_\infty = 0.2$, and $Re = 6.5 \times 10^6$: +, current C_p ; —, initial C_p ; —, current airfoil; and - - -, initial airfoil.

The lift coefficient has increased from 4.0412 to 4.1881, as shown in Fig. 15. Large changes are observed in both the flap and slat deflection angles. The flap deflection angle has increased from 30 to 32.6 deg to allow for larger camber and the slat deflection angle has decreased from 30 to 26.7 deg, which achieves a higher effective angle of attack and, therefore, carries more lift. Changes in gaps and overlaps are small, and the resulting flap gap and overlap are $0.0153c/0.0020c$, whereas for the slat the gap and overlap are $0.0309c/0.0258c$. Figure 16 shows the same design attempt using only the setting parameters as the design variables. After 19 design iterations, the lift coefficient has increased from 4.0412 to 4.1698. From these results, it is evident that a large portion (about 85%) of the increase in C_l is due to the modification of the rigging parameters of each airfoil element. However, notice that very small geometry changes in each element through the bump functions still delivered more than 100 counts (15% of the increase) in lift coefficient.

4. C_l Maximization at a Fixed C_d

We now allow the angle of attack of the configuration to float by fixing the value of C_d to that of the baseline design point at $\alpha = 16.02$ deg. As we can see in Fig. 17, in 10 design iterations, the optimizer has increased the lift by 815 counts from 4.0412 to 4.1227 while reducing the angle of attack from 16.02 to 15.127 deg with small changes in the total coefficient of drag from 0.0650 to 0.0661. This result appears counterintuitive at first but highlights the power of both the adjoint methodology and the careful parameterization of the surface because the procedure still yields a higher C_l , while the angle of attack is forced down to match the prescribed $C_d = 0.0650$.

E. Maximum Lift Maximization

1. Single-Element Airfoil Results

The present adjoint method was also applied to the optimization of an airfoil shape that maximizes the maximum lift coefficient $C_{l_{max}}$. The RAE2822 single-element airfoil and the same four-block mesh used for the earlier single-element airfoil design cases were used for calculations at a design condition of $M_\infty = 0.2$ and $Re = 6.5 \times 10^6$. Bump functions were used as before, and the angle of attack α was included as an additional design variable for the maximization of

maximum lift. Two different approaches were tried. In the first approach, three steps were taken as follows: First when α alone was used as a design variable, $C_{l_{max}}$ and α at $C_{l_{max}}$ ($\alpha_{cl_{max}}$) were predicted along the C_l vs α curve for the baseline configuration. Then, when 50 bump functions were used, a new airfoil configuration was obtained that maximized C_l with $\alpha = \alpha_{cl_{max}}$ fixed. Finally, with this value of α used, the first step was repeated to obtain a new $C_{l_{max}}$ and new $\alpha_{cl_{max}}$ for the updated configuration. Figure 18 shows the design results from this approach. In the first step, $C_{l_{max}}$ was predicted to be 1.6430 at $\alpha_{cl_{max}} = 14.633$ deg (O–A in Fig. 19). Next, as shown in Fig. 20 $C_{l_{max}}$ increased to 1.8270, and the initial airfoil was updated to have more thickness near the leading edge and more camber (A–B in Fig. 19). The final $C_{l_{max}}$ obtained was 1.8732 (point C in Fig. 19) and the overall $C_{l_{max}}$ improved 14% from 1.6430, whereas $\alpha_{cl_{max}}$ increased 11.1% from 14.633 to 16.250 deg. This

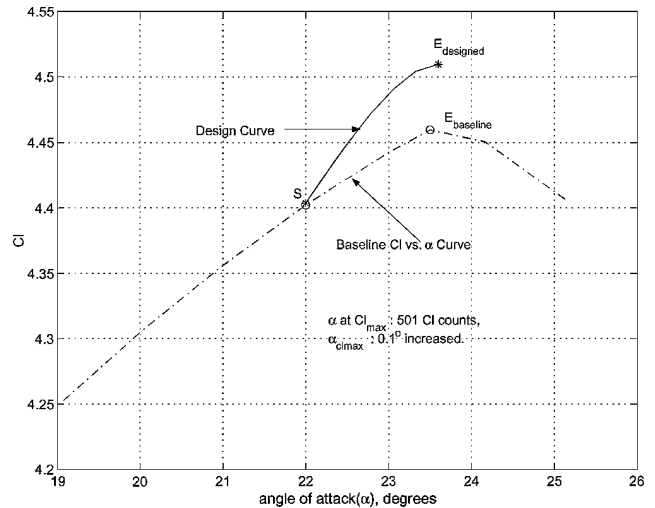


Fig. 22 Design curve of the 30P30N $C_{l_{max}}$ maximization, $M_\infty = 0.20$ and $Re = 9 \times 10^6$.

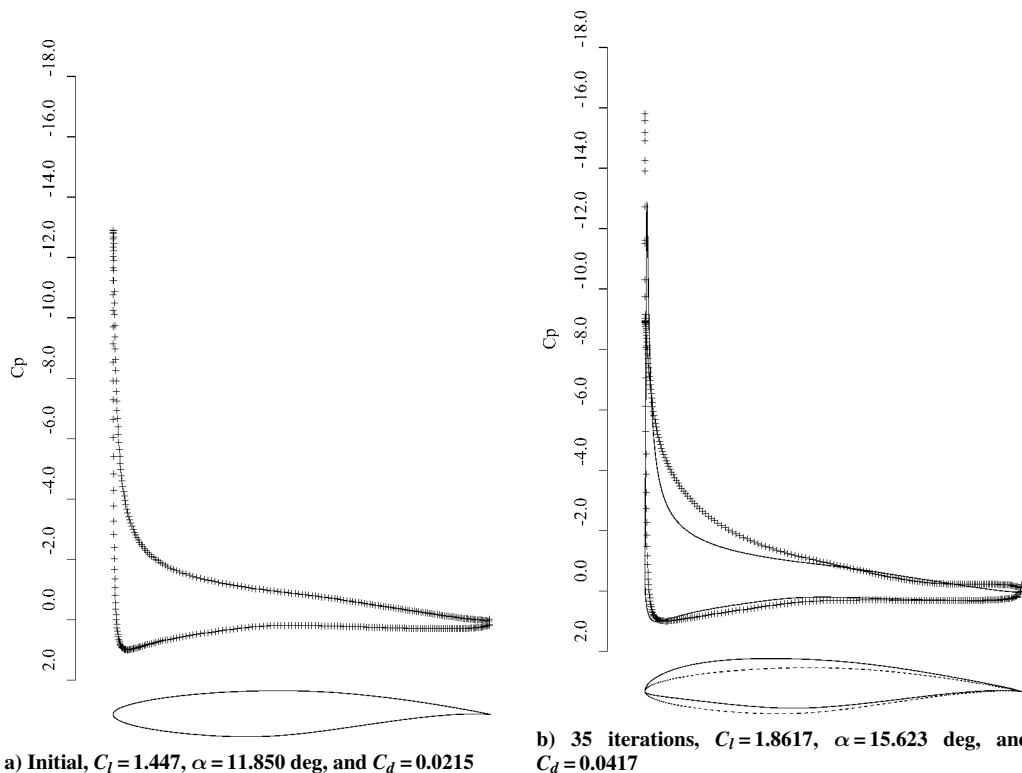


Fig. 21 RAE2822 $C_{l_{max}}$ maximization calculation including α as a design variable, $M_\infty = 0.2$, $Re = 6.5 \times 10^6$: +, current C_p ; —, initial C_p ; —, current airfoil; and - - -, initial airfoil.

design example verifies the design capabilities of the adjoint gradients using α . Although this example represents a single iteration of the overall procedure, this procedure could be repeated iteratively to attain even higher levels of $C_{l_{max}}$. (Note that 31 iterations were used during the A–B step.)

Based on the information gathered from the first approach, both the bumps and the angle of attack were simultaneously used for the design in the second approach (D–E in Fig. 19). As shown in Fig. 21, when the baseline RAE2822 at $\alpha = 11.85$ deg was used, $C_{l_{max}}$ improved by 13.3% to 1.8617 and $\alpha_{cl_{max}}$ changed by 6.8% to 15.623 deg from the $C_{l_{max}}$ and $\alpha_{cl_{max}}$ of the baseline RAE2822 configuration.

2. Multi-Element Airfoil Results

This design example is the culmination of the efforts in this paper. Using the newly developed viscous adjoint procedure, the multi-block flow and adjoint solvers, and the lessons learned in the earlier design examples, we can now attempt to redesign the 30P30N multi-element airfoil to optimize its value of $C_{l_{max}}$. In this case, a total of 157 design variables are used, including 50 Hicks–Henne bump functions on each of the three elements, 3 rigging variables for each the slat and flap components, and the angle of attack α of the complete configuration.

As shown in Fig. 22, the design started at $\alpha = 22$ deg, which is near the $\alpha_{cl_{max}}$ of the baseline 30P30N configuration, and the baseline was modified in the direction of C_l improvement using all of the design variables. As shown in Figs. 22 and 23, $C_{l_{max}}$ improved by 1.12%, 501 counts, increasing from 4.4596 to 4.5097, with a slight change (0.43%) in $\alpha_{cl_{max}}$. Even for highly optimized configuration such as the 30P30N, further small improvements can be achieved by using the viscous adjoint sensitivities that are the central portion of this paper.

F. Results of Design Optimization

In the present design study, all of the optimizations employed the method of steepest descent. Constraints are applied in the optimization by simply projecting the gradient vector onto the subspace of feasible designs, eventually leading to a constrained optimum, which is arrived at by moving along constraint boundaries. No attempt to use an augmented Lagrangian was made, and therefore, the actual optimum design is not measured by the satisfaction of the

Kuhn–Tucker conditions, but, instead, by monitoring the progress of the cost function of interest. Obviously, a nonlinear constrained optimizer could have been used instead (as we have done in some of our previous work^{10,11}). However, we have often found that, in engineering terms, solutions very close to the optimum can be found with the steepest descent method. Although, for gradient-based optimization, convergence to the exact optimum cannot be expected in fewer iterations than the actual number of design variables in the problem, in typical adjoint-based design parameterizations, it is not unusual to have design variables whose gradients are rather small and, therefore, have very little effect on the value of the cost function at the optimum point. For this reason, some of the design calculations were stopped after a given number of design iterations once the function of interest showed no evidence of continued decrease.

Figure 24 shows the convergence history for the C_l maximization of the RAE2822 airfoil when the angle of attack is used as the only design variable. As expected by the theory, C_l converged to the local maximum and the gradient value corresponding to the

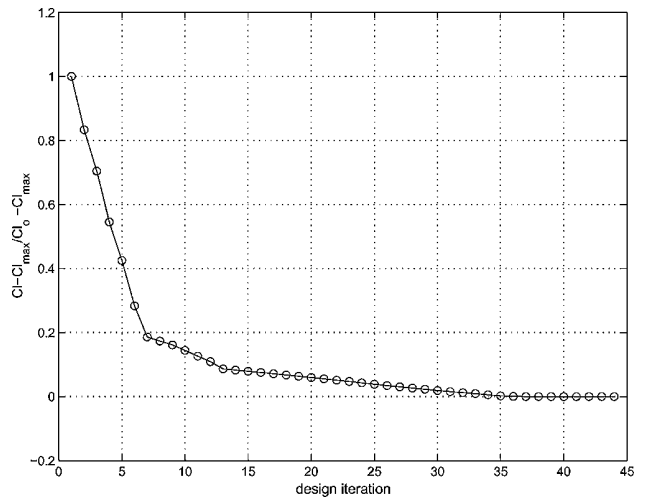


Fig. 24 Convergence history for lift maximization of RAE2822 with angle of attack the only design variable.

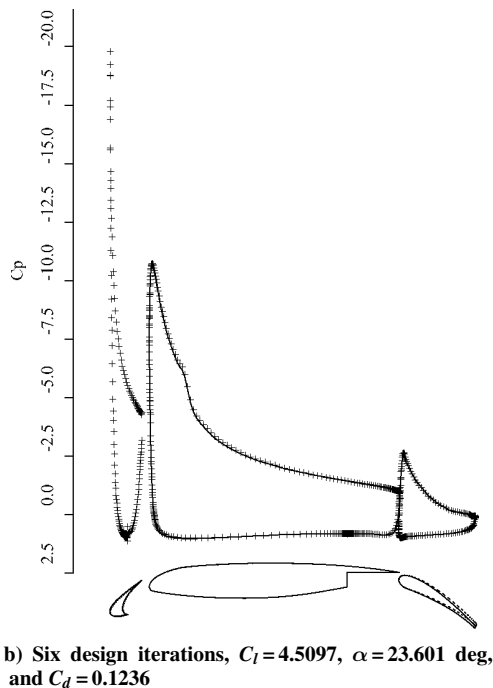
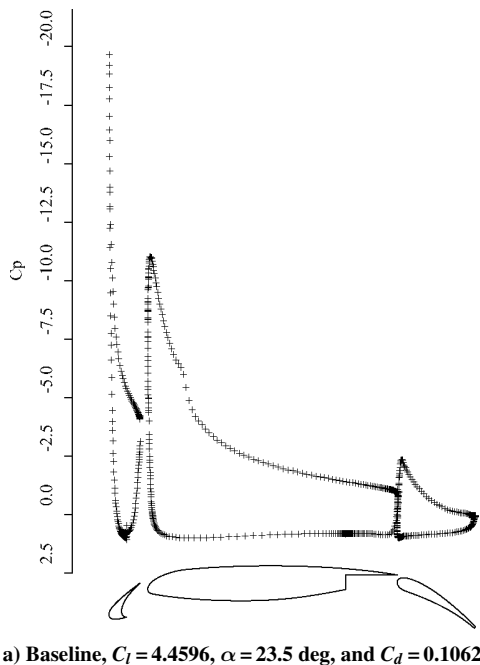


Fig. 23 Multi-element airfoil $C_{l_{max}}$ maximization calculation for the 30P30N, $M_\infty = 0.2$: +, current C_p ; —, initial C_p ; —, current airfoil; and ---, initial airfoil.

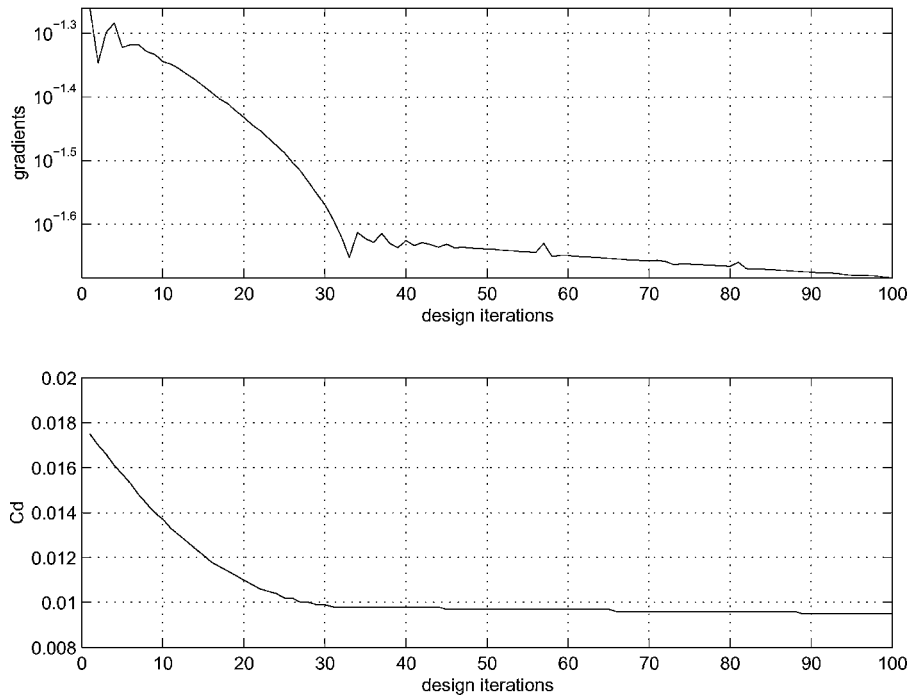


Fig. 25 Convergence History of C_d and L2 norm for drag minimization of RAE2822 at fixed angle of attack.

local optimum became 3.096×10^{-6} of its initial value, 6.506, in 44 design iterations.

Similarly, for the problem of drag minimization of an RAE2822 airfoil at a fixed angle of attack, the local minimum for the specified parameterization was achieved as shown in Fig. 25. However, this minimum may be further improved if a different shape parameterization were to be employed: The present design parameterization did not allow for modifications of the leading- and trailing-edge locations and all of the Hicks–Henne sine bump functions had fixed a , t_1 , and t_2 parameters [in Eq. (7)]; therefore, the numerical optimization procedure was unable to span the complete design space of all possible airfoil shapes. Although no direct constraints were introduced, the use of the present bump functions (with bounds on their possible values) and design parameterization can be considered an indirect way of applying constraints.

In the single-element lift maximization cases using Hicks–Henne bump functions, the designs were run for a prespecified number of design iterations and were not necessarily allowed to converge to the exact local maximum, although inspection of the results reveals that the difference was small. Further improvements can be obtained by reducing the airfoil thickness, and therefore, a more complete treatment of thickness constraints is suggested for more detailed design work.

For the multi-element design cases, the relative improvements were smaller than those of the single-element design cases. The lift increments, however, are of comparable magnitude, although the baseline values for the multi-element cases are much higher. One of the main reasons for this was that the baseline high-lift configuration was already a highly optimized one. Two other possible reasons can also be mentioned. First, the additional design variables, such as the flap and slat deflection angles, gaps, and overlaps, made the multi-element airfoil design space much more complex than that of the single-element airfoil design. For the scalings used in both the bump amplitudes and the flap and slat angle deflections, the magnitudes of the lift and drag sensitivities differ considerably. Typically, for the units chosen in this work, the sensitivities to the bump amplitudes are much larger than those due to angle-of-attack variations, although the cost function improvements that may be derived from angle-of-attack changes may be more substantial after a large number of steepest descent design iterations. Because, due to the cost of the optimization procedure for viscous multi-element

design, we were limited in the total number of design iterations that we could compute, a user-defined scaling was used in the angle-of-attack variables to arrive at the local minimum in a smaller number of iterations. Second, one can expect further improvements by using alternative cost functions and adjoint boundary conditions. Interestingly, for the drag minimization of the multi-element configuration, a significant improvement was observed using pressure drag as the cost function instead of total drag, though the actual numerical result was not included in this paper because a thorough study has not been completed. This may be because most of the drag of the multi-element airfoil is the pressure drag. Although the flow in high-lift systems is dominated by viscous phenomena, the typical ratio of pressure drag to skin-friction drag is of order of 10.

The high-lift system optimizations of the 30P30N configuration were carried out using a multiblock mesh with 26 blocks and a total of 204,800 mesh points. Each design iteration involved the solution of the flow using the SA turbulence model, and it required about 5000 iterations. The adjoint solution is computed in the same mesh, and because it does not need to be converged as far as the flow solution to obtain accurate gradient information, only 700 iterations were required. Each design iteration, consisting of one flow and one adjoint solution and all of the necessary mesh perturbations and gradient calculations, took approximately 1.5 h on 26 processors of an SGI Origin 2000 computer with the 195-MHz R10000 processor.

IV. Conclusions

A numerical optimization procedure using the adjoint method for high-lift system design has been developed and presented. The procedure is based on a multiblock RANS flow solver, FLO103-MB, that uses the SA turbulence model for high Reynolds number flows. FLO103-MB has been implemented in parallel so that the turnaround for design calculations can be even faster.

Multi-element airfoils are parameterized using the well-known Hicks–Henne bump functions and additional design variables that allow the gaps and overlaps, as well as the angle of attack of the slat and flap elements, to be represented. Making use of the large computational savings provided by the adjoint method when large numbers of design variables are involved, we are able to explore high-dimensional design spaces that are necessary for high-lift system design. In this study, the 30P30N multi-element airfoil is used

because experimental data are available for validation purposes. A total of 157 design variables corresponding to 50 Hicks–Henne bump functions on each of the elements of the configuration, the x and y locations and angles of attack of the slat and flap elements, and the overall angle of attack of the configuration are used for C_d minimization and C_l maximization subject to several kinds of constraints. The angle of attack of the high-lift system was used as a design variable for $C_{l_{\max}}$ maximization only.

Results for L/D maximization and $C_{l_{\max}}$ maximization for the RAE2822 single-element airfoil showed significant improvements. For the multi-element design cases, the relative improvements were smaller than those of the single-element design cases. The lift increments, however, are of comparable magnitude, although the baseline values for the multi-element cases are much higher. Of course, one of the main reasons for this was that the baseline high-lift configuration was already a highly optimized one. The results obtained are encouraging and point out that the adjoint method can have great potential for the design of high-lift systems. The design cases in this work are purely academic and meant to validate the sensitivity calculation procedure only. Future work will focus on expanding current results and on utilizing the method described to perform realistic two-dimensional high-lift system designs.

Acknowledgments

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