

# Multi-Swarm Whale Optimization Algorithm for Data Clustering Problems using Multiple Cooperative Strategies

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Abstract-Computational Intelligence (CI) is an as of emerging area in addressing complex real world problems. The WOA has taken its root from the collective intelligent foraging behavior of humpback whales (Megaptera Novaeangliae). The standard WOA is suffers from the selection of best agent while whales searching and encircling prey. This research paper deals with the multi-swarm cooperative strategies for finding the best agents which balances the two phase's exploration and exploitation. The performance of invoked Multi-Swarm cooperative strategies into standard WOA i.e, MsWOA is first benchmarked on a set of 23 standard mathematical benchmark function problems which includes 7 Uni-Modal, 6 Multi-modal and 10 fixed dimension multimodal functions. The obtained graphical and statistical results have been portrayed along with the previously established techniques. The obtained results depicts that cooperative strategies for the proposed WOA outperforms in solving optimization problems of standard benchmark functions. This paper also studies the numerical efficiency of proposed techniques on the problem of data clustering where 10 real data clustering problems have been taken from data repository https://archive.ics.uci.edu.data. Statistical results for the obtained cluster centroids, intra-cluster distances and inter-cluster distances confirms that the cooperative strategies for best whale agent selection improves the performance WOA for function optimization problems as well as data clustering problems.

*Index Terms*—Nature Inspired Algorithms, Metaheuristic optimization techniques, WOA, Cooperative Strategies, Data Cluster Problems.

# I. INTRODUCTION

Computational Intelligence is the fast growing area in tending to this real world and complex problems. The majority of the computational Intelligence algorithms are inspired by nature [1]. Researchers now conceded the way that the most ideal approach to discover answers for this real world and complex problems by studying the nature, this unveiling the micro secrets in nature to produce new optimization algorithms. Population based meta-heuristic algorithms are ending up noticeably more well known in solving complex real world problems with use of no single gradient function. Modern problems are for the most part with various complex variables that are should have been utilized as a part of finding optimal solutions. The last two decades have witnessed many real world complex problems are addressed by the field of meta-heuristics. The main objective of these algorithms is enabling the optimization process in giving the best possible solution in any situation where there are an extensive number of possible solutions.

In Data Mining, cluster analysis identifies the patterns which are recognized from each other through their features, by finding the partitions that have similar characteristics. Partitioning is a collection of objects into clusters all together that items in one cluster ought to have a minimization of intra-cluster similarity and the maximization of inter cluster likeness. Finding optimal clusters or optimal structures of data is a difficult task when it comes to complex data. Many classical algorithms have been developed for discovering clusters of data however finding optimal structures of data is as yet a big challenging task. There are two main problems in clustering. The first is choice of initial number of centroids and the second one is distance function optimization problem. Numerous data researchers have demonstrated that k-Means clustering technique is the absolute best answer for discovering hidden patterns by clustering the entire dataset. Clustering also called unsupervised learning in some traditional fields, for example, machine learning.

Authors [2-6] used nature inspired algorithms to find the optimized structures by applying them to cluster techniques. For instance, in *k*-Means clustering similarity function should be minimizing centroid distance to obtain optimized clusters. *i.e.* minimization of sum of squared Euclidean distance of objects from respective cluster means shown in Eq. (1).

$$d_{min} = \sum_{j=1}^{K} \sum_{Z_i \in C_i} \|Z_i - \mu_j\|^2$$
(1)

where  $\mu_i$  is the mean of  $C_i$ .

Let's consider an optimization problem. We have given an undertaking to distinguish the natural product sort. Each organic product has recognized three particular components they are contour, color, size. X is a dataset which has the above three components. Initial number of clusters and cluster centroids are chosen. I now need to cluster up the natural products into clusters in which it definitely has a place with. The clustering component is said to be good only if clustering method acquires two conditions, one is intra-cluster minimization and the other is inter-cluster maximization. Numerous classical clustering algorithms have the optimization problem, failed to deal with non-linear dataset and insensitive to the noisy or anomaly data. We assumed that, we have an optimization function that measures how "good" clustering. By clustering up the organic products, and after that calling an optimization function on each group to measure its goodness, and afterward summing up the goodness of each group, at that point we can quantify how "good" a certain set of groups is. At the point when there is an increase in the aggregate number of natural product sort and components, at that point the problem has all the earmarks of being a NP-Complete, so it can be solved with agreeing to a parallel meta-heuristic algorithm. Nature inspired meta-heuristic algorithm can optimize the non-linear functions in an efficient manner.

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Table 1.a. List of Uni and Multi modal benchmark functions ( $F_1$  to  $F_{13}$ ). where  $V_{no} = 30$ ,  $f_{min} = 0$ 

F_Name	Objective Function	Range
Sphere function	$F_1(x) = \sum_{i=1}^n x_i^2$	[-100, 100]
Schwefel 2.22 function	$F_{2}(x) = \sum_{i=1}^{n}  x_{i}  + \prod_{i=1}^{n}  x_{i} $	[-10, 10]
Schwefel 1.2 function	$F_{3}(x) = \sum_{i=1}^{n} \left( \sum_{j=1}^{i} x_{j} \right)^{2}$	[-100, 100]
Rotated Schwefel 2.21 function	$F_4(x) = \max_i \{  x_i , 1 \le i \le n \}$	[-100, 100]
Rosenbrock's function	$F_{5}(x) = \sum_{i=1}^{n-1} [100(x_{i+1} - x_{i}^{2})^{2} + (x_{i} - 1)^{2}]$	[-30, 30]
	$F_6(x) = \sum_{i=1}^n ([x_i - 0.5])^2$	[-100, 100]
Quartic function	$F_7(x) = \sum_{i=1}^n i x_i^4 + random[0,1)$	[-1.28, 1.28]
Schwefel function	$F_8(x) = \sum_{i=1}^n -x_i^2 \sin(\sqrt{ x_i })$ (Note: $f_{min} = -418.9829*5$ )	[-500, 500]
Rotated Rastrigin's function	$F_9(x) = \sum_{i=1}^{n} [x_i^2 - 10\cos(2\pi x_i) + 10]$	[-5.12, 5.12]
Ackley function	$F_{10}(x) = -20e^{\left(-0.2\sqrt{\frac{1}{n}\sum_{i=1}^{n}x_{i}^{2}}\right)} - e^{\left(\frac{1}{n}\sum_{i=1}^{n}\cos(2\pi x_{i})\right)} + 20 + e^{\left(\frac{1}{n}\sum_{i=1}^{n}\cos(2\pi x_{i})\right)} + 20 + e^{\left(\frac{1}{n}\sum_{i=1}^{n}x_{i}^{2}\right)} - e^{\left(\frac{1}{n}\sum_{i=1}^{n}x_{i}^{2}\right)} - e^{\left(\frac{1}{n}\sum_{i=1}^{n}x_{i}^{2}\right)} + e^{\left$	[-32, 32]
Griewank function	$F_{11}(x) = \frac{1}{4000} \sum_{i=1}^{n} x_i^2 - \prod_{i=1}^{n} \cos(\frac{x_i}{\sqrt{i}}) + 1$	[-600, 600]
Penalized 1 function	$F_{12}(x) = \frac{\pi}{n} \{ 10\sin(\pi y_1) + \sum_{i=1}^{n-1} (y_i - 1)^2 [1 + 10\sin\pi y_{i+1}^2] + (y_n - 1)^2 \} + \sum_{i=1}^{n} u(x_i, 10, 100, 4) \}$	[-50, 50]
	$y_{i} = 1 + \frac{x_{i} + 1}{4}u(x_{i}, a, k, m) = \begin{cases} k(x_{i} - a)^{m} & x_{i} > a \\ 0 & -a < x_{i} < a \\ k(-x_{i} - a)^{m} & x_{i} < -a \end{cases}$	
Penalized 2 function	F <sub>13</sub> (x)	[-50, 50]
	$= 0.1\{\sin(3\pi x_1)^2 +$	
	$\sum_{i=1}^{n} \frac{(x_i - 1)^2 [1 + \sin(3\pi x_i + 1)^2] + (x_n - 1)^2 [1 + \sin 2\pi x_n)^2]}{\sum_{i=1}^{n} u(x_i, 5, 100, 4)}$	

**Problem statement** the problem of optimized structures of a dataset for clustering is formalized as takes after. Let consider a dataset  $D_T$ , where T denotes the total number of data instances and N be the dataset dimensions (variables) that are considered. Let the input N-dimensional dataset. Consider a dataset D featured by P attributes:

$$D_{T} = [\{x_{1T}, x_{2T}, \dots, x_{PT}\}]^{T}$$
(2)

Assume dataset  $D_T$  with N dimensions is partitioned into  $C_i$  clusters, where i = 1 to k, so that for each  $D_T$ Similarity measured by distance d then,

$$d(D_T | C_i(\{x_{1T}, x_{2T}, \dots, x_{PT})) = max \left\{ d(D_T | C_l(x_{1T}, x_{2T}, \dots, x_{PT})) \right\}$$
(3)

*d* is the distance between  $D_T$  and  $C_i$ .  $C_i$  Should meet the following conditions:

$$C_i \neq \emptyset$$
,  $C_i \cap C_s = \emptyset$  and  $\bigcup_{i=1}^k C_i = D_T$  where *i*,  $s = 1 \dots k$ 

We utilize the term compactness to quality of a given cluster in light of intra and inter cluster minimization, maximization similarities respectively. The clustering problem minimizing in a simple manner is portrayed as takes after.

$$d(D_T, Z) = \sum_{i=1}^{N} \sum_{j=1}^{k} || D_{Tij} - Z_j ||^2$$
(4)

where *k* denotes the number of clusters, *N* the number of dimensions,  $D_{Tij}$  is the location of *i*<sup>th</sup> dimension of cluster *j*.

$$\frac{1}{N_j} \sum_{i=1}^N D_{Tij} \tag{5}$$

 $N_i$  is the number of dimensions in the  $j^{th}$  cluster.

F_Name	Objective Function	Range	V_no	$\mathbf{f}_{\min}$
De jong function 5	$F_{14}(x) = \left(\frac{1}{500} \sum_{j=1}^{25} \frac{1}{j + \sum_{i=1}^{2} (x_i - a_{ij})^6}\right)^{-1}$	[-65,65]	2	1
Kowalik function	$F_{15}(x) = \sum_{i=1}^{11} \left[ a_i - \frac{x_1(b_i^2 + b_i x_2)}{b_i^2 + b_i x_3 + x_4} \right]^2$	[-5, 5]	4	0.00030
Six-Hump Camel Back function	$F_{16}(x) = 4x_1^2 - 2.1x_1^4 + \frac{1}{3}x_1^6 + x_1x_2 - 4x_2^2 + 4x_2^4$	[-5, 5]	2	1.0316
Branin RCOS function	$F_{17}(x) = \left(x_2 - \frac{5.1}{4\pi^2} x_1^2 + \frac{5}{\pi} x_1 - 6\right)^2 + 10\left(1 - \frac{1}{8\pi}\right)\cos x_1 + 10$	[-5, 5]	2	0.398
Goldstein–Price function	$F_{18}(x) = \begin{bmatrix} 1 + (x_1 + x_2 + 1)^2 \begin{pmatrix} 19 - 14x_1 + 3x_1^2 - 14x_2 + \\ 6x_1x_2 \end{pmatrix} + \\ 3x_2^2 \\ [30 + (2x_1 - 3x_2)^2 * (18 - 32x_1 + 12x_1^2 + \\ 48x_2 - 36x_1x_2 + 27x_2^2)] \end{bmatrix} *$	[-2, 2]	2	3
Hartmann function 3	$F_{19}(\mathbf{x}) = -\sum_{i=1}^{4} c_i e^{(-\sum_{j=1}^{3} a_{ij}(x_j - p_{ij})^2)}$	[1, 3]	3	-3.86
Hartmann function 6	$F_{20}(x) = -\sum_{i=1}^{4} c_i e^{(-\sum_{j=1}^{6} a_{ij}(x_j - p_{ij})^2)}$	[0, 1]	6	-3.32
Shekel function 5	$F_{21}(x) = -\sum_{i=1}^{5} [(X - a_i)(X - a_i)^T + c_i]^{-1}$	[0, 10]	4	-10.1532
Shekel function 7	$\mathbf{F}_{22}(\mathbf{x}) = -\sum_{i=1}^{7} [(X - a_i)(X - a_i)^T + c_i]^{-1}$	[0, 10]	4	-10.4028
Shekel function 10	$F_{23}(x) = -\sum_{i=1}^{10} [(X - a_i)(X - a_i)^T + c_i]^{-1}$	[0, 10]	4	-10.5363

Table 1.b. List of fixed-dimension multimodal benchmark functions ( $F_{14}$  to  $F_{23}$ ).

#### II. RELATED WORK

The most recent two decades have seen an exceptional change in the area of computational intelligence for growing popular and efficient optimization techniques which are generally inspired by the nature; these are well known in tackling complex np-hard problems by exploring and mimicking different phenomena of the nature. The absolute most well-known optimization algorithms are comprehensively listed below.

Darwin's theory of evolution has inspired towards the development of GA (Genetic Algorithms) [7]. These algorithms are adaptive heuristic search algorithms intended to imitate the processes in natural system. The basic idea behind the development of GA is the evolution of new chromosomes from the combinations of initial chromosome populations making an expectation that recently evolved ones are better to the old set of chromosomes. The searching capability of GA is exploited, keeping in mind the end goal to search for proper cluster centers in the feature space to such an extent that a similarity metric of the resulting cluster is optimized.

The chromosomes that which are represented as strings of real numbers, encode the centers of a fixed number of clusters [8]. The ACO [9] is probabilistic based method and was planned in view of the natural phenomenon of real ant colonies. It is a populace based MHO calculation motivated by the ant behavior that is used to determine discrete- optimization problems. Many researchers [10], [11] used ACO as tool for finding k optimal clusters of N data objects. This algorithm has been devised and used on several artificial and real datasets. DE [12] is a population of candidate solutions based optimization technique has paved the path by storn and price and it is used to optimize real parameter, real valued functions. It is the one of the quick, robust and efficient global search heuristics of current intrigue. Many authors utilized DE for finding optimized clusters of large unlabeled datasets. As opposed to the vast majority of the current clustering techniques, the DE requires no prior knowledge of the data for finding optimal clusters [13], [14]. The behavioral aspect of many birds flocking and fish schooling patterns has prompted the development of PSO [15] by Russell Eberhart and J. Kennedy. The key idea has been created from a flock of birds where every individual in the flock determines its closest neighbor and replaces their velocity with that neighbor. Among the numerous nature-inspired algorithms, clustering using PSO technique has identified as robust and efficient in

solving clustering problems [16]. PSO can be utilized to discover centroids of a user indicated number of clusters. It is suitable for clustering complex and linearly nonseparable datasets [17]. Keeping in mind the end goal to enhance the efficiency of PSO technique, many researchers have proposed distinctive variations of the PSO algorithm furthermore, have grown new thoughts. for example, adaptive heuristics, different fitness functions, kernel-induced similarity measures, and evolution of swarm generations and so on [18-24]. Newton's law of gravity has given rise to an optimization algorithm named as GSA [25]. It is a stochastic population based MHO algorithm was developed based on the gravity and mass interactions. Variants of GSA also developed based on the concept of antigravity. In GSA randomly created candidate solutions for data clustering problem then the interaction have been made to each and other via Newton's gravitation law to search problem space [26], [27]. The WOA (Whale Optimization Algorithm) [28] has been devised based on the foraging strategy of hump back whales. The strategy of searching for prey, encircling strategy and the mass net searching towards getting the prey was considered in building up this algorithm. The performance comparisons have been made by testing on 23 standard mathematical benchmark functions. Found that WOA perform efficient than many state-of-the-art optimization algorithms including PSO [28]. Authors in [29] improved the optimization performance by introducing new convergence factor in both exploration and exploitation phase. Authors [30] proposed a new parallel metaheuristic optimization algorithm (NPMOA) which was formulated by hybridizing WOA with CSA. The above variants of WOA (IWAO, CSAWOA) were tested and applied to data clustering problems [31], [32].

In this paper we use the multi-swarm cooperative strategies for enhancing the performance of standard WOA and applying it to data clustering problems. The paper focuses on ring, master-slave and hybrid cooperative strategies for finding the best agent vector  $\vec{X}^*$ . As earlier said this paper comprises two parts where in the first part we use each multi-swarm cooperative strategy and find the performance. In second part applying the swarm cooperative strategies based WOA for data clustering problems.

The structural organization of this paper is done as follows. The section III presents the Standard Whale Optimization Algorithm. In the Section IV, we have described the swarm cooperative strategies where in A, B and C we presented Ring, Master-Slave and Hybrid cooperative strategies respectively. The performance comparisons of swarm cooperative strategies based WOA with GSA, DE, PSO, WOA and variants of WOA have been made in Section V whereas Section A and B outlines the performance comparisons on 23 standard benchmark functions that are listed in Table 1. a) and b) and data clustering problems that are described in Table 6 respectively. The last section concludes the whole paper and points out the future scope.

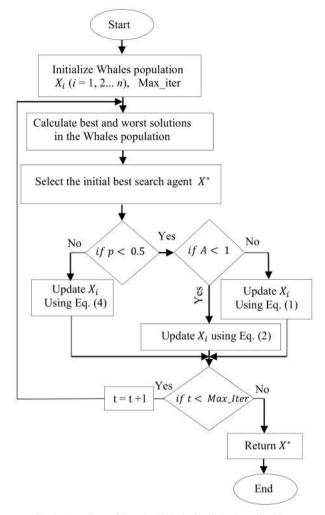


Fig.1. Flowchart of Standard Whale Optimization algorithm

#### III. STANDARD WOA

The Whale optimization Algorithm in short WAO was first coined by S. Mirjalili and A. Lewis. The special hunting behavior of humpback whales has paved the path for developing this algorithm [25]. The specialty of whales in hunting prey is they release bubbles in either 'circular' manner or '9' shaped path to move prey to the surface of the ocean. The mathematical model of this behavior is explained in two phases. The first phase is explained as hunting behavior. In this phase observed that whales show two maneuvers. They are shrinking encircling mechanism and Spiral updating position. Eq. (6) and (7) specifies the equations for the whales updating position in circular and spiral path respectively.

$$\vec{X}_{t+1} = \begin{cases} \overline{X^{*}}_{t} - \vec{A}.\vec{D}, & p < 0.5 & (6) \\ \overline{D^{'}}.e^{bl}.cos(2\pi l) + \overline{X^{*}}_{t} & p \ge 0.5 & (7) \end{cases}$$

where  $\overrightarrow{D'} = |\overrightarrow{X^*}_t - X^*_t|$ ,  $p = (-1) \times rand(0,1)$ . In Eq. (6)  $\overrightarrow{a}$  is decreased to achieve to shrinking the encircling mechanism. Then  $\overrightarrow{A} = (-2a) \cdot rand(1,1) + a$ . where, 'a' is an integer and coefficient  $\overrightarrow{A}$  is decreased by  $\overrightarrow{a}$ .

In Eq. (2) constant *b* is used in defining the shape of the logarithmic spiral, l = (-2) \* rand(1, 1) + 1, and '.' is a dot product operator. WOA assumes probability of 50% to choose between either these two approaches. If p < 0.5 whales updates their position in *shrinking encircling mechanism* else if  $p \ge 0.5$ , they move in *Spiral updating position*. The second phase is presented as searching phase. In this phase, WOA assumed that whales search for prey in two different possible ways. If  $\vec{A} \ge 1$  then the updated position of whale using Eq. (8).

$$\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$$
(8)

where,  $\vec{D} = |\vec{A}.\vec{X}_{rand} - \vec{X}|$ ,

 $\vec{X}_{rand}$  is a random position vector.

Else if  $\vec{A} < 1$  new updated position becomes the Eq. (9).

$$\vec{X}_{t+1} \leftarrow \vec{X^*}_t - \vec{A}.\vec{D} \tag{9}$$

where,  $\vec{D} = |\vec{C}.\vec{X^*}_t - \vec{X}_t|\vec{A}$  and  $\vec{C}$  are internal parameters, the subscript 't' specifies the current iteration,  $\vec{X}$  is the position vector,  $\vec{X^*}$  is the new position vector. '| |', '.' are absolute value and element-by-element multiplication respectively. Both  $\vec{A}$  and  $\vec{C}$  are coefficient vectors where,  $\vec{A} = 2\vec{a}.\vec{r} - \vec{a}$ ,  $\vec{C} = 2.\vec{r}$ . Here,  $\vec{a}$  straightaway decreases from 2 to 0 during the course of maneuver (in both phases: exploration and exploitation) and  $\vec{r} = (-1).*$ rand(0,1). The flowchart and pseudo code of WOA is given in Fig. 1 and Table 2 respectively.

Table 2. Pseudo code of Standard WOA

1 Initialize population  $X_i$  (i = 1, 2, ..., n)Find the fitness of each search agent 2 3  $\mathbf{X}^*$  is the best search agent obtained 4 Update a, A, C, 1 and p every search agent if1 p< 0.5 5 if2 |**A**|< 1 6 Update position using Eq. (9) 7 8 else if2  $A \ge 1$ Select a random search agent 9 Xrand 10 Update the position using Eq. (8) end if2 11 else ifl p  $\geq$  0.5 12 Update the topography using Eq. (7) 13 end if1 14 15 Check is any search agent goes beyond space and amend it the search Calculate the fitness of each search 16 agent Update  $X^*$  if there is a better solution 17 18 Go to Step 4 t times and return  $\boldsymbol{X}^{\ast}$ 

## IV. MULTI-SWARM COOPERATIVE STRATEGIES

This section presents the multi-swarm cooperative strategies for enhancing the performance of standard WOA by invoking the Ring, Master-Slave and Hybrid strategies individually for finding the best whale population vector. The main objective of invoking these three cooperative strategies is maintaining the balancing between exploration and exploitation phases. According to the standard WOA all the whales are attracted by the best whale position. If the whales in each sub population converge at the best whale position then within a few iteration they will move near to the surface. In invoking Cooperative Strategies into Standard WOA, The whole population is grouped into multiple-cooperative swarms, we named it as sub-swarms. These sub-swarms perform different searching behavior for finding the best whale position vector  $Best_Sub_Pop_k^*$ . This phenomenon in each whale sub-population leads to the similar updating behavior and the loss of diversity in whales. The fallowing section 4.1, 4.2 and 4.3 describes the Ring, Master-Slave and Hybrid cooperative strategies with neat flowchart and pseudo code.

#### A. Ring Cooperative Strategy

This Strategy is a heterogeneous search strategy based on k-sub-swarms. The basic idea behind this strategy was inspired from ring topology. It is one of the network topology called ring network or ring topology. Many cooperative algorithms used this cooperative strategy to improve the performance of algorithm. In this cooperative strategy each sub-population of k subpopulation evolves in parallel to find best whale position. Each whale sub-population interchanges its best whale position with the other whale sub-population. Each subpopulation replaces its best whale position only if gets the better whale position than the present best whale position. The interchange of best whale position happens continuously. In the optimal model structures of whale population, each sub-swarm can learn from the best whale position given by other sub-swarm and enhance their foraging direction i.e., bringing the prey closer to the surface which is optimal place to catch the prey. The pseudo code and flowchart is given in Table 3 and Fig. 2.

## B. Master Slave Cooperative Strategy

This section presents the improved strategy of ring strategy. We mentioned "improved strategy of ring strategy" because the best whale position is interchanged like the ring cooperative strategy. But the difference is instead of interchanging best whale position between each other sub whale population, one sub whale population acts as master and all remaining are as slaves. it also called as multi-population collaborative strategy. In this cooperative strategy each slave sub-population of k-1 sub-population, evolves in parallel to obtain best whale position and share this information to the master. Master sub populations find the best among the received and share the same to the slaves. Master-Slave strategy balances the exploration and exploitation phases. The pseudo code and flowchart is given in Table 4 and Fig. 3.

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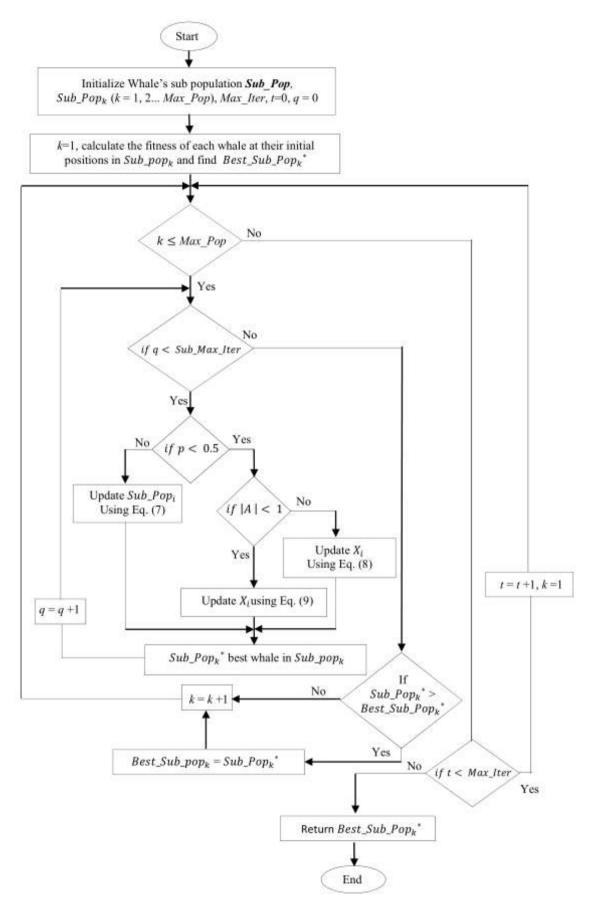


Fig.2. WOA invoking ring cooperative strategy

<b>T</b> (	
Input	$Sub_Pop_k$ (k = 1, 2 $Max_Pop$ ), $Sub_Max_iter$ , $Max_Iter$ , $t=0$ , $q=0$
-	Best solution, best optimal values of objective function
1.	Initialize Whale sub population $Sub_Pop$ , $Sub_Pop_k$ ( $k = 1, 2 Max_Pop$ ), $Max_Iter$ , $k = 1, t = 0$ and $q = 0$
2.	calculate the fitness of each whale at their initial positions in $Sub\_pop_k$ and find $Best\_Sub\_Pop_k^*$ ( $Best\_Sub\_Pop_1^*$ is the best search agent obtained at k = 1)
3.	Update <i>a</i> , <i>A</i> , <i>C</i> , <i>l</i> and <i>p</i> every search agent
4.	if $k \leq Max_Pop$
5.	<b>if</b> $p < 0.5$
6.	if  A  < 1
7.	Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X^*}_t - \vec{A}.\vec{D}$
8.	else if $ A  \ge 1$
9.	Select a random search agent $X_{rand}$ update the topography using
9.	$\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$
10.	end if
11.	else if $p \ge 0.5$
12.	Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'} \cdot e^{bl} \cdot \cos(2\pi l) + \vec{X}_t^*$ Check is any search agent goes beyond the search space and amend it
13.	end if
14.	repeat Sub_Max_Iter times
15.	if Sub_Pop <sub>k</sub> * > Best_Sub_Pop <sub>k</sub> *
16.	$Best_Sub_pop_k = Sub_Pop_k^*$
17.	k = k + 1
18.	<b>else if</b> $k = k + 1$
19.	end if
20.	end if
21.	repeat Max_Iter times
22.	return $Best_Sub_Pop_k^*$

Table 3. Pseudo code for WOA invoking ring cooperative strategy

## C. Hybrid Cooperative Strategy

This section gives the detailed description of a new hybrid cooperative strategy. The discussed cooperative strategies in earlier sections 4.1 and 4.2 are combined and form a new hybrid cooperative strategy. The key objective of this hybridization is infusion of swarm cooperative mechanism of ring cooperative strategy between the slave populations into the Master-Slave cooperative strategy. In this, a duplicate set of the best whale position of each slave sub-swarm population is shared to the master sub-swarm population. Moreover, if after Max\_iter (a maximum number of iterations) there is no improvement in the obtained solution, each slave subswarm population shares its best whale position obtained with its neighbors. Finally, the general best whale position is detected by the master sub-population.

The cooperation and communication model within the ring cooperative strategy are injected into the master and slave sub-populations and interchanging the individual best whale position of each slave sub-population with master sub-population reduces the possibility of moving outwards from the optimal solution. This hybridization process goes for maximizing the possibility of finding the best position within a low solution cost and the diversification of search can be achieved through the same. On the other hand, as the swarms are searching independently and in real parallelism, comprehensively the algorithm must be more effective than the previous ones. The pseudo code and flowchart of this cooperative strategy are given in Table 5 and Fig. 4 respectively.

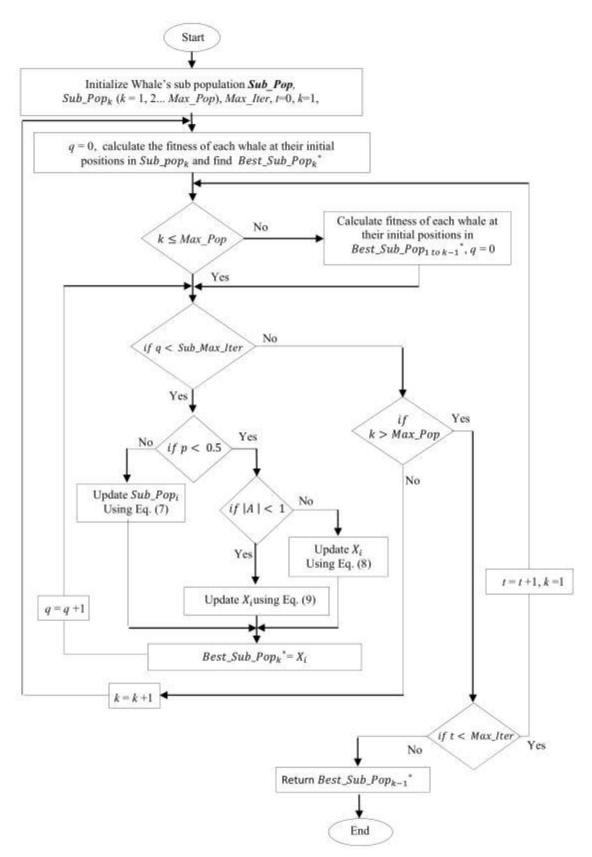


Fig.3. WOA invoking master-slave cooperative strategy

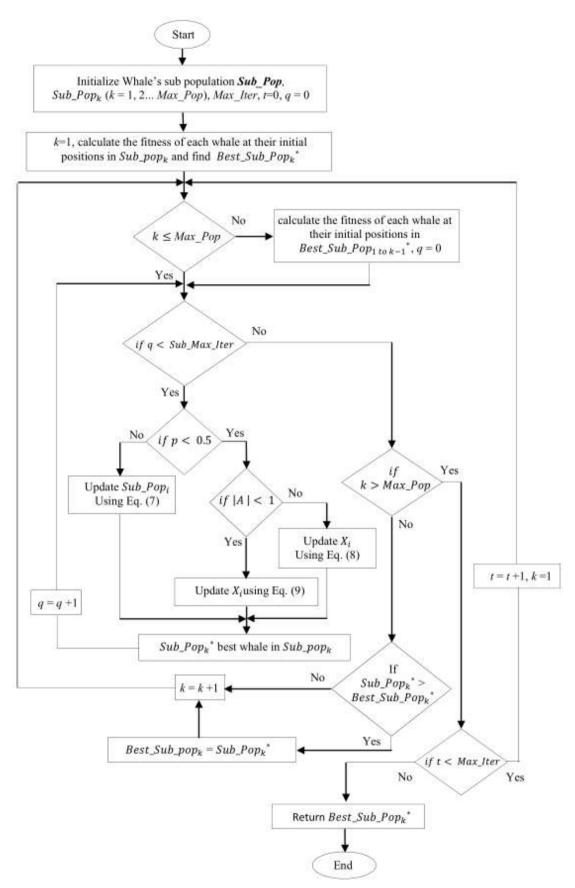


Fig.4. WOA invoking Hybrid cooperative strategy

Table 4. Pseudo code for WOA invoking Master - Slave cooperative strategy

Input	$Sub\_Pop_k$ (k = 1, 2 $Max\_Pop$ ), $Sub\_Max\_iter$ , $Max\_Iter$ , t=0, q = 0
Output	Best solution, best optimal values of objective function
1.	Initialize Whale sub population <i>Sub_Pop</i> , <i>Sub_Pop</i> <sub>k</sub> ( $k = 1, 2 Max_Pop$ ), <i>Max_Iter</i> , $k = 1, t = 0$ and $q = 0$
2.	calculate the fitness of each whale at their initial positions in $Sub_pop_k$ and find $Best_Sub_pop_k^*$ ( $Best_Sub_pop_1^*$ is the best
	search agent obtained at $k = 1$ )
3.	Update <i>a</i> , <i>A</i> , <i>C</i> , <i>l</i> and <i>p</i> every search agent
4.	if $k \leq Max_Pop$
5.	<b>if</b> $p < 0.5$
6.	$\mathbf{if}  A  \leq 1$
7.	Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_t^* - \vec{A} \cdot \vec{D}$
8.	else if $ A  \ge 1$
9.	Select a random search agent $X_{rand}$ update the topography using
	$\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$
10.	end if
11.	else if $p \ge 0.5$
12.	Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'} \cdot e^{bl} \cdot \cos(2\pi l) + \vec{X}_t^*$ Check is any search agent goes beyond the search space and
	amend it
13.	end if
14.	else if
15.	calculate the fitness of each whale at their initial positions in $Best_Sub_Pop_{1 to k-1}^*$ , $q = 0$
16.	if $k > Max_Pop$
17.	goto step 21
18.	else if $k = k + 1$
19.	goto step 2
20.	end if
21.	repeat step 5 to 20 Sub_Max_Iter times
22.	end if
23.	repeat Sub_Max_Iter times
24.	repeat step 4 to 23 Max_Pop times
25.	repeat 4 to 24 Max_Iter
26.	return $Best_Sub_Pop_k^*$

#### V. EXPERIMENTAL RESULTS AND DISCUSSION

In the current work, the performance of the proposed multi-swarm cooperative strategies (MsWOA) is compared with GSA, DE, PSO, WOA and variants of WOA in solving 23 standard mathematical benchmark functions and data clustering problems. We considered 10 real datasets for addressing the data clustering problems of which are taken from https://archive.ics.uci.edu. The detailed description of these datasets is listed in Table 6. In all the experiments, we have taken whales population of 30 and maximum of 500 iterations for both standard mathematical benchmark functions optimization problems and data clustering problems. All the conducted experiments and investigations have been made on an Intel(R) Core(TM)-i5-2400 CPU with a clock rate of 3.10 GHz, 8 GB RAM and proposed multi-swarm cooperative strategies for enhancing standard WOA is described earlier sections has been implemented using MATLAB-R2016a.

## A. Experiment 1: mathematical benchmark functions

Like the other state-of-the-art and popular population based meta-heuristic optimization techniques such as GSA, DE [12], PSO [15], WOA [25] and advanced variants IWOA [26] and NPMOA [27] of WOA, makes use of a population to investigate the problem space. Population based mechanism bring into play the probability of obtaining optimal solution and abscond from local optima increases.

In this section, the proposed multi-swarm cooperative strategies for enhancing the optimization performance of standard WOA and compared the obtained results with GSA, DE, PSO, WOA, IWOA and NPMOA based on the optimal solutions obtained on 23 standard mathematical benchmark functions. We presented the comprehensive description of these benchmark functions in Table 1 a) and Table 1 b). Note that the Table 1 a) indicates the comprehensive descriptions of 13 standard mathematical benchmark functions which include 7 Uni-modal and 6 Multimodal functions and Table 1 b) presents the description of 10 fixed dimension multimodal standard mathematical benchmark functions. The performance comparison have been made in terms of fitness convergence of GSA, DE, PSO, WOA and advanced variants IWOA and NPMOA of WOA and MsWOA for first four benchmark functions in graphical manner as given in Fig 5. The statistical analysis of obtained solution costs for MsWOA along with GSA, DE, PSO, WOA and variants of WOA is presented in a tabular form as given in Table 7. Hence, it is clear that the MsWOA is good at optimizes the most of the benchmark functions within a low cost solution than the other compared algorithms. Note that we used MsWOA for indicating all Ring (RWOA), Master-Slave (MSWOA) and Hybrid (HWOA) cooperative strategies in a single term.

 Table 5. Pseudo code for WOA invoking Hybrid cooperative strategy

 Image: Sub Box (k = 1, 2, Max Bax) Sub Max iten Max to 0, a = 0

12. space and amend it	
2. calculate the fitness of each whale at their initial positions in $Sub\_pop_k$ and find $Best\_Sub\_Pop_k^*$ ( $Best\_Sub\_Pop_k^*$ ) search agent obtained at $k = 1$ ) 3. Update $a, A, C, l$ and $p$ every search agent 4. if $k \le Max\_Pop$ 5. if $p < 0.5$ 6. if $ A  < 1$ 7. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X^*}_t - \vec{A}.\vec{D}$ 8. else if $ A  \ge 1$ 9. Select a random search agent $X_{rand}$ update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. end if 11. else if $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D^*}.e^{bl}.\cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyon space and amend it	
2. search agent obtained at k = 1) 3. Update <i>a</i> , <i>A</i> , <i>C</i> , <i>l</i> and <i>p</i> every search agent 4. <b>if</b> $k \le Max\_Pop$ 5. <b>if</b> $p < 0.5$ 6. <b>if</b> $ A  < 1$ 7. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{t}^{*} - \vec{A}.\vec{D}$ 8. <b>else if</b> $ A  \ge 1$ 9. Select a random search agent $X_{rand}$ update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. <b>end if</b> 11. <b>else if</b> $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D}^{*}.e^{bl}.\cos(2\pi l) + \vec{X}_{t}^{*}$ Check is any search agent goes beyond	
4. <b>if</b> $k \le Max\_Pop$ 5. <b>if</b> $p < 0.5$ 6. <b>if</b> $ A  < 1$ 7. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}^*_t - \vec{A}.\vec{D}$ 8. <b>else if</b> $ A  \ge 1$ 9. Select a random search agent $X_{rand}$ update the topography using 9. $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. <b>end if</b> 11. <b>else if</b> $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D}^t.e^{bl}.\cos(2\pi l) + \vec{X}^*_t$ Check is any search agent goes beyond space and amend it	$p_1^*$ is the best
5. <b>if</b> $p < 0.5$ 6. <b>if</b> $ A  < 1$ 7. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X^*}_t - \vec{A}.\vec{D}$ 8. <b>else if</b> $ A  \ge 1$ 9. Select a random search agent $X_{rand}$ update the topography using 9. $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. <b>end if</b> 11. <b>else if</b> $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D^*}.e^{bl}.\cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyond space and amend it	
6. if $ A  < 1$ 7. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{t}^* - \vec{A} \cdot \vec{D}$ 8. else if $ A  \ge 1$ 9. Select a random search agent $X_{rand}$ update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A} \cdot \vec{D}$ 10. end if 11. else if $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D}^{\dagger} \cdot e^{bl} \cdot \cos(2\pi l) + \vec{X}_{t}^*$ Check is any search agent goes beyond space and amend it	
7.       Update the topography using $\vec{X}_{t+1} \leftarrow \vec{X^*}_t - \vec{A}.\vec{D}$ 8.       else if $ A  \ge 1$ 9.       Select a random search agent $X_{rand}$ update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10.       end if         11.       else if $p \ge 0.5$ 12.       Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'}.e^{bl}.\cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyon space and amend it	
8. else if $ A  \ge 1$ 9. Select a random search agent $X_{rand}$ update the topography using 10. end if 11. else if $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D^{\prime}} \cdot e^{bl} \cdot \cos(2\pi l) + \vec{X^{*}}_{t}$ Check is any search agent goes beyon space and amend it	
9. Select a random search agent $X_{rand}$ update the topography using $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. end if 11. else if $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'}.e^{bl}.\cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyon space and amend it	
9. $\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. end if 11. else if $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'}.e^{bl}.\cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyon space and amend it	
$\vec{X}_{t+1} \leftarrow \vec{X}_{rand} - \vec{A}.\vec{D}$ 10. end if 11. else if $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'}.e^{bl}.\cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyon space and amend it	
11. <b>else if</b> $p \ge 0.5$ 12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'} \cdot e^{bl} \cdot \cos(2\pi l) + \vec{X^*}_t$ Check is any search agent goes beyon space and amend it	
12. Update the topography using $\vec{X}_{t+1} \leftarrow \vec{D'} \cdot e^{bl} \cdot \cos(2\pi l) + \vec{X}_t^*$ Check is any search agent goes beyon space and amend it	
12. space and amend it	
	nd the search
13. end if	
14. else if	
15. calculate the fitness of each whale at their initial positions in $Best_Sub_Pop_{1 to k-1}^*, q = 0$	
16. <b>if</b> $k > Max_Pop$	
17. goto step 21	
18. else if $k = k + 1$	
19.goto step 2	
20. <b>end if</b>	
21. repeat step 5 to 20 Sub_Max_Iter times	
22. end if	
23. <b>repeat</b> Sub_ <i>Max_Iter</i> times	
24. <b>repeat</b> step 4 to 23 <i>Max_Pop</i> times	
25. <b>repeat</b> 4 to 24 <i>Max_Iter</i>	
26. return $Best\_Sub\_Pop_k^*$	

#### B. Experiment 2: Data clustering problems

To test the efficiency of MsWOA on data clustering problems, we examined 10 real datasets. The comprehensive descriptions of these datasets are displayed in Table 6. This section for the most part

algorithm is said to be good, it should return optimal clusters in which the clustering strategy should indulge in minimization and maximization of intra cluster and inter cluster detachment respectively. The experimental and

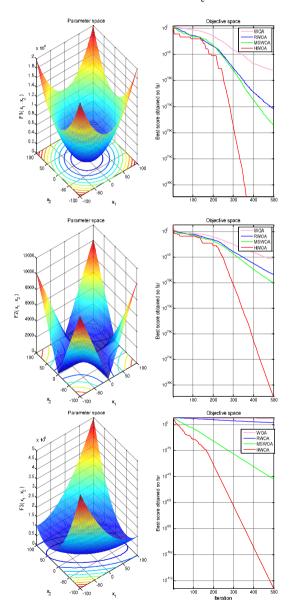
centered around data clustering using the proposed

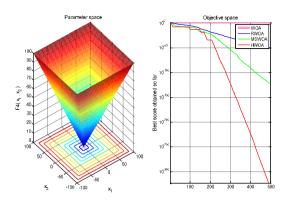
technique. At the point when a partitional clustering

evidentical comparisons have been made with previously established algorithms. We used the fallowing three criteria to measure the clustering performance of each clustering technique. They are,

- Finding quantization error using Eq. (10)
- Intra-cluster minimization, i.e. where the key objective is to minimize the distance between data objects within a cluster.
- Inter-cluster maximization, i.e. where the key objective is to maximize the distance between the centroids of the clusters.

Quantization error  $J_e = \frac{\sum_{j=1}^{N_c} \left[ \sum_{\forall Z_p \in C_{i,j}} d(Z_p, m_j) / |C_{i,j}| \right]}{N_c}$  (10)





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Fig.5. Fitness convergence of first four Uni-modal functions

Table 6. Description of datasets

S. No	Dataset	size	dimension	k
1	Iris	150	4	3
2	Glass	214	9	6
3	Wine	178	13	3
4	Breast	683	9	2
5	Pima Indian diabetes	68	8	2
6	Haberman's survival	306	3	2
7	Hayes-Roth	160	4	3
8	E. Coli	336	7	8
9	Zoo	101	16	7
10	Vowel	462	10	11

In order to evaluate the MsWOA clustering performance, this algorithm is run on every benchmark dataset. From the obtained results the statistical analysis has been made. The convergence characteristics of data clustering problems are presented in a graphical manner in Fig.6. The mean and standard deviation are calculated for each test. The obtained solution cost, Intra-Cluster and Intra-Cluster distances for MsWOA are summarized in Table 8 along with previously established algorithms GSA, DE, PSO, WOA, IWOA, CSAWOA. In most of the cases the hybrid cooperative strategy improved the performance of WOA. From all the experiment results obtained for data clustering problems, we can testify that MsWOA works well in solving data clustering problems. Note that for all the data cluster problems, k-Means partitional clustering algorithm along with the standard Euclidean distance measuring technique is used.

Table 7. Statistical analysis of obtained solution cost for $F_1$ to $F_{23}$										
Alg.			F <sub>1</sub>					F <sub>2</sub>		
	Average	Median	Std. Dev	Best	Worst	Average	Median	Std. Dev	Best	Worst
GSA	121.248e+01 132.328e+01	1.1549e-27 1.4728e-27	8.1245e+03 8.0715e+03	1.1845e-51 1.0548e-55	6.7843e+04 6.9825e+04	5.1532e+07 5.4537e+07	2.1562e-09 2.5416e-09	8.4238e+08 8.4751e+08	3.4525e-47 3.9816e-47	7.2637e+11 7.3519e+09
DE PSO	132.328e+01 115.452e+01	1.4728e-27 1.4528e-29	8.0282e+03	1.0348e-33 1.2457e-87	6.8354e+04	4.2193e+07	2.3410e-09 2.2023e-09	8.7425e+08	3.5812e-47	7.2581e+10
WOA	976.0925	1.4934e-29	6.0966e+03	1.0730e-81	6.2422e+04	2.9207e+07	1.7031e-18	4.6134e+08	3.4225e-52	7.3017e+09
IWOA	141.0601	1.6987e-69	2.8017e+03	8.5331e-315	6.2234e+04	2.6816e+08	1.1694e-32	5.9961e+09	2.1158e-159	1.3408e+11
CSAWOA	143.4836	1.2152e-78	3.2060e+03	0	7.1689e+04	1.0502e+06	3.8957e-42	2.3483e+07	1.1054e-202	5.2510e+08
RWOA	278.4197	3.5175e-53	3.4636e+03	3.0772e-155	6.5930e+04	1.1445e+09	9.0683e-30	2.5592e+10	7.6042e-92	5.7226e+11
MSWOA	148.2499	1.0370e-55	2.1034e+03	3.6666e-186	4.2005e+04	6.2541e+08	2.8133e-31	1.3984e+10	8.5322e-102	3.1270e+11
HWOA	133.7060	3.1538e-94	2.9709e+03	0	6.6431e+04	4.1330e+06	1.0576e-49	9.2418e+07	5.5813e-318	2.0665e+09
Alg.	Avenage	Median	F <sub>3</sub> Std. Dev	Dect	Worst	Avenage	Median	F <sub>4</sub> Std. Dev	Dest	Worst
GSA	Average 5.2318e+05	5.4532e+04	3.8421e+05	Best 2.5136e+03	1.3428e+05	Average 1.7672	2.4365e-36	5.6827	Best 6.4162e-26	112.3518
DE	4.9845e+05	4.1429e+04	3.5432e+05	2.3684e+04	1.3428e+05	1.7516	2.6842e-36	5.6845	6.6273e-26	110.438
PSO	4.7536e+05	4.2137e+04	3.1452e+05	2.2531e+04	1.3549e+05	1.2461	2.6821e-36	5.3245	6.5736e-49	100.2456
WOA	5.7966e+04	5.2965e+04	3.4381e+04	1.6992e+04	1.2689e+05	1.4157	2.2081e-35	5.2690	6.3572e-38	90.7160
IWOA	1.2377e+03	2.4741e-60	1.6451e+04	9.7553e-270	2.5731e+05	0.2815	1.1628e-36	4.2173	4.6036e-149	87.9804
CSAWOA	676.4248	7.3566e-74	9.4417e+03	0.784 e-270	1.6777e+05	0.2573	3.1044e-38	4.2628	1.9567e-208	86.0427
RWOA	2.6761e+04	2.0174e+03	5.0740e+04	30.4146	2.4953e+05	0.8732	6.0729e-24	6.7354	2.3219e-50	92.1388
MSWOA	2.3047e+03	2.8134e-18	1.7782e+04	1.1087e-42	2.1653e+05	0.3378	1.8580e-37	4.3973	1.5083e-123	85.7551
HWOA	635.1985	2.6796e-47	8.1064e+03	9.0514e-127	1.5907e+05	0.2516	1.4527e-76	4.1991	0	87.8658
Alg.	- <u></u>		F5					<b>F</b> <sub>6</sub>		
-	Average	Median 28.5925	Std. Dev 1.7486e+08	Best 29.8465	Worst 2.7165e+08	Average 648.9124	Median	<b>Std. Dev</b> 4.8462e+03	Best 0.4934	Worst 6.7168e+04
GSA	2.9438e+06						0.4864		0.4934 0.4271	
DE PSO	2.7268e+06 2.8436e+06	28.3516 28.2816	1.7345e+08 1.7519e+08	29.5438 29.1575	2.7465e+08 2.6427e+08	650.4671 635.9215	0.45311 0.3843	4.8513e+03 4.7364e+03	0.4271 0.4637	6.4625e+04 5.4928e+04
WOA	2.6080e+06	27.9527	1.9373e+07	27.9516	2.5396e+08	629.8011	0.3204	4.7976e+03	0.3204	5.5280e+04
IWOA	4.0073e+05	27.8797	8.7116e+06	27.8797	1.9476e+08	168.6582	0.1528	3.2574e+03	0.1528	7.2028e+04
CSAWOA	5.6167e+05	28.6617	1.2501e+07	28.6617	2.7952e+08	135.4935	0.2798	2.8557e+03	0.2798	6.3775e+04
RWOA	6.4358e+05	27.5877	1.0019e+07	27.5877	2.1035e+08	739.3369	0.3262	6.0110e+03	0.3262	7.2705e+04
MSWOA	5.9859e+05	27.9460	1.2597e+07	27.9460	2.8119e+08	607.4678	0.1720	4.6416e+03	0.1720	6.1839e+04
HWOA	5.6736e+05	28.4372	1.2686e+07	28.4371	2.8366e+08	158.9282	0.1634	2.7791e+03	0.1633	6.0336e+04
			$\mathbf{F}_7$					F <sub>8</sub>		
Alg.	Average	Median	Std. Dev	Best	Worst	Average	Median	Std. Dev	Best	Worst
GSA	2.6218	0.02(1	12.9861	0.2907	150 ( 465	-1.2942e+04	-1.5429e+04	1.8435e+03	-1.8415e+04	
		0.9261	12.9601	0.2897	150.6465		-1.54296+04	1.04556+05	-1.8415e+04	-3.4791e+03
DE	2.6284	0.8649	12.8534	0.2785	150.6481	-1.2942e+04	-1.6354e+04	1.7926e+03	-1.7816e+04	-3.4627e+03
DE PSO	1.6845	0.8649 0.8634	12.8534 12.6521	0.2785 0.0654	150.6481 148.5281	-1.2648e+04 -1.2549e+04	-1.6354e+04 -1.4215e+04	1.7926e+03 1.7924e+03	-1.7816e+04 -1.8195e+04	-3.4627e+03 -3.4996e+03
PSO WOA	1.6845 1.3233	0.8649 0.8634 0.0057	12.8534 12.6521 11.1443	0.2785 0.0654 0.0052	150.6481 148.5281 139.6725	-1.2648e+04 -1.2549e+04 -1.1491e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04	1.7926e+03 1.7924e+03 1.7492e+03	-1.7816e+04 -1.8195e+04 -1.2347e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03
PSO WOA IWOA	1.6845 1.3233 0.2960	0.8649 0.8634 0.0057 2.3889e-04	12.8534 12.6521 11.1443 6.2970	0.2785 0.0654 0.0052 4.0297e-05	150.6481 148.5281 139.6725 140.7692	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04	1.7926e+03 1.7924e+03 1.7492e+03 897.0959	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03
PSO WOA IWOA CSAWOA	1.6845 1.3233 0.2960 0.2358	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04	12.8534 12.6521 11.1443 6.2970 5.2301	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05	150.6481 148.5281 139.6725 140.7692 116.9492	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03
PSO WOA IWOA CSAWOA RWOA	1.6845 1.3233 0.2960 0.2358 0.2866	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03
PSO WOA IWOA CSAWOA RWOA MSWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03
PSO WOA IWOA CSAWOA RWOA MSWOA	1.6845 1.3233 0.2960 0.2358 0.2866	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03
PSO WOA IWOA CSAWOA RWOA MSWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub>	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04 -1.2201e+04	$\begin{array}{c} 1.7926e{+}03\\ 1.7924e{+}03\\ 1.7492e{+}03\\ 897.0959\\ 1.3604e{+}03\\ 1.4897e{+}03\\ 1.5558e{+}03\\ 1.3690e{+}03\\ \hline \mathbf{F_{10}}\end{array}$	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg.	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 Median	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub> <b>Std. Dev</b>	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 Worst	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b>	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04 -1.2201e+04 Median	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>F</b> <sub>10</sub> <b>Std. Dev</b>	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 Best	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 Median 0.2241	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub> <b>Std. Dev</b> 87.2954	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 Worst 490.8134	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04 -1.2201e+04 Median 6.8435e-14	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>F</b> <sub>10</sub> <b>Std. Dev</b> 2.9043	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 Best 4.6205e-15	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 Median 0.2241 0.2168	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495 0.0413	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3690e+03 <b>Fi</b> <b>5td. Dev</b> 2.9043 3.0483	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 Best 4.6205e-15 3.9352e-15	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 Median 0.2241	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub> <b>Std. Dev</b> 87.2954	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 Worst 490.8134	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04 -1.2201e+04 Median 6.8435e-14	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>F</b> <sub>10</sub> <b>Std. Dev</b> 2.9043	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 Best 4.6205e-15	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO WOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 Median 0.2241 0.2168 0.1762	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495 0.0413 0.0361	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2430e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>F10</b> <b>Std. Dev</b> 2.9043 3.0483 3.0201	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 3.9352e-15 4.6205e-15	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 <b>Worst</b> 20.6019 20.7294 20.6903
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO WOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495 0.0413 0.0361 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 -1.2201e+04 Median 6.8435e-14 6.5269e-15 6.6024e-15 6.2172e-15	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>F10</b> <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 Best 4.6205e-15 3.9352e-15 4.6205e-15 4.4409e-15	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO WOA IWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495 0.0413 0.0361 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.2172e-15 8.8818e-16	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>F10</b> <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 3.9352e-15 4.6205e-15 4.4409e-15 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 <b>Worst</b> 20.6019 20.7294 20.6903 20.4593 20.8727
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 <b>Median</b> 0.2241 0.2168 0.1762 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.2172e-15 8.8818e-16 8.8818e-16	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 Best 4.6205e-15 3.9352e-15 4.6205e-15 4.4409e-15 8.8818e-16 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 <b>Worst</b> 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 <b>Median</b> 0.2241 0.2168 0.1762 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.2172e-15 8.8818e-16 8.8818e-16 4.4409e-15	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.9570 0.9380 0.9233	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 3.9352e-15 4.6205e-15 4.4409e-15 8.8818e-16 4.4409e-15	-3.4627e+03 -3.4996c+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 <b>Worst</b> 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 <b>Median</b> 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> <b>87</b> .2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F</b> <sub>11</sub>	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 -1.220	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F</b> 12	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 3.9352e-15 4.6205e-15 4.4409e-15 8.8818e-16 8.8818e-16 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA RWOA HWOA Alg.	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 <b>Median</b> 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F11</b> <b>Std. Dev</b>	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b>	-1.2648e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b>	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 <b>Median</b>	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F</b> 12 <b>Std. Dev</b>	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA RWOA MSWOA HWOA Alg. GSA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 <b>Median</b> 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F11</b> <b>Std. Dev</b> 49.2604	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.8218e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F12</b> <b>Std. Dev</b> 5.7261e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 <b>Median</b> 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F11</b> <b>Std. Dev</b> 49.2604 49.1806	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.0681e+06	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.2172e-15 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16	1.7926e+03 1.7924e+03 1.7492e+03 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F12</b> <b>Std. Dev</b> 5.7261e+07 5.8216e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.6205e-15 4.6205e-15 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518 6.9046	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 0 0 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F11</b> <b>Std. Dev</b> 49.2604 49.1806 40.6608	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409 614.7406	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.6207e+06 7.6207e+06 6.8106e+06	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.2172e-15 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16	1.7926e+03 1.7924e+03 1.7492e+03 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F12</b> <b>Std. Dev</b> 5.7261e+07 5.8216e+07 5.8216e+07 5.8216e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16	-3.4627e+03 -3.4996c+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08 7.8265e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA <b>Alg.</b> GSA DE PSO WOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518 6.9046 6.8496	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 0 0 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub> <b>Std. Dev</b> <b>87</b> .2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F</b> <sub>11</sub> <b>Std. Dev</b> 49.2604 49.1806 40.6608 51.1150	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409 614.7406 573.1051	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.1393e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.0681e+06 6.8106e+06 6.5367e+06	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.6024e-15 8.8818e-16 8.8818	1.7926e+03 1.7924e+03 1.7492e+03 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F12</b> <b>Std. Dev</b> 5.7261e+07 5.8216e+07 5.6152e+07 5.6152e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16	-3.4627e+03 -3.4996c+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08 7.8265e+08 7.4401e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA HWOA GSA DE PSO WOA IB. GSA DE PSO WOA IWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518 6.9046 6.8496 2.5364	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 0 0 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub> <b>Std. Dev</b> <b>87</b> .2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F</b> <sub>11</sub> <b>Std. Dev</b> 49.2604 49.1806 40.6608 51.1150 37.8199	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409 614.7406 573.1051 605.3266	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.1683e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.0681e+06 6.8106e+06 6.5367e+06 1.7024e+06	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.6024e-15 8.8818e-16 8.8818	1.7926e+03 1.7924e+03 1.7492e+03 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F12</b> <b>Std. Dev</b> 5.7261e+07 5.8216e+07 5.6152e+07 5.613e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08 7.8265e+08 7.4401e+08 6.8750e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA HWOA GSA DE PSO WOA IWOA CSAWOA IWOA CSAWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518 6.9046 6.8496 2.5364 1.3268	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 0 0 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F</b> <sub>9</sub> <b>Std. Dev</b> <b>87</b> .2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F</b> <sub>11</sub> <b>Std. Dev</b> 49.2604 49.1806 40.6608 51.1150	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 <b>Best</b> 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409 614.7406 573.1051	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.1393e+04 -1.1949e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.0681e+06 6.8106e+06 6.5367e+06	-1.6354e+04 -1.2337e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 Median 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.2172e-15 8.8818e-16	1.7926e+03 1.7924e+03 1.7492e+03 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.2812 1.2812 1.2812 1.2812 5.7261e+07 5.7261e+07 5.6152e+07 5.6152e+07 5.6132e+07 3.1591e+07 3.2097e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16	-3.4627e+03 -3.4996c+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08 7.8265e+08 7.4401e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA RWOA HWOA GSA DE PSO SA DE PSO WOA IWOA IWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518 6.9046 6.8496 2.5364	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 0 0 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F11</b> <b>Std. Dev</b> 49.2604 49.1806 40.6608 51.1150 37.8199 29.4677	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409 614.7406 573.1051 605.3266 658.9239	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1731e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.6207e+06 7.6207e+06 1.7024e+06 1.4370e+06	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.6024e-15 8.8818e-16 8.8818	1.7926e+03 1.7924e+03 1.7492e+03 1.3604e+03 1.4897e+03 1.3558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.2812 1.9570 0.9380 0.9233 <b>F12</b> <b>Std. Dev</b> 5.7261e+07 5.8216e+07 5.6152e+07 5.613e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 4.6205e-15 4.6205e-15 4.4409e-15 8.8818e-16 8.8	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08 7.8265e+08 7.4401e+08 6.8750e+08 7.1770e+08
PSO WOA IWOA CSAWOA RWOA MSWOA HWOA GSA DE PSO WOA IWOA CSAWOA HWOA GSA DE PSO WOA IWOA GSA DE PSO WOA IWOA CSAWOA RWOA	1.6845 1.3233 0.2960 0.2358 0.2866 0.3021 0.1892 Average 30.6527 30.5468 30.2458 27.1213 2.8204 1.6330 4.6452 0.9208 1.4091 Average 7.1582 7.3518 6.9046 6.8496 2.5364 1.3268 2.5074	0.8649 0.8634 0.0057 2.3889e-04 8.3541e-04 4.1339e-05 4.5624e-04 1.3918e-04 Median 0.2241 0.2168 0.1762 0 0 0 0 0 0 0 0 0 0 0 0 0	12.8534 12.6521 11.1443 6.2970 5.2301 6.3802 6.7172 4.2067 <b>F9</b> <b>Std. Dev</b> 87.2954 86.6218 86.1954 76.7544 28.9688 24.0741 35.8709 20.5897 22.7304 <b>F11</b> <b>Std. Dev</b> 49.2604 49.1806 40.6608 51.1150 37.8199 29.4677 31.0664	0.2785 0.0654 0.0052 4.0297e-05 9.0942e-05 4.1339e-05 7.0342e-05 1.3918e-04 Best 0.0495 0.0413 0.0361 0 0 0 0 0 0 0 0 0 0 0 0 0	150.6481 148.5281 139.6725 140.7692 116.9492 142.6656 150.2019 94.0648 <b>Worst</b> 490.8134 490.6218 485.1668 450.6246 467.2299 447.3239 426.5025 460.3999 425.1632 <b>Worst</b> 615.1082 615.1082 615.3409 614.7406 573.1051 605.3266 658.9239 610.5245	-1.2648e+04 -1.2549e+04 -1.2549e+04 -1.1491e+04 -1.2393e+04 -1.1683e+04 -1.1731e+04 -1.1731e+04 -1.1711e+04 <b>Average</b> 1.2816 1.1956 0.6583 0.4300 0.1190 0.1025 0.2884 0.0420 0.0448 <b>Average</b> 7.6207e+06 7.0681e+06 6.8106e+06 6.5367e+06 1.7024e+06 1.4370e+06 9.9647e+05	-1.6354e+04 -1.4215e+04 -1.2337e+04 -1.2560e+04 -1.2494e+04 -1.2569e+04 -1.2201e+04 <b>Median</b> 6.8435e-14 6.5269e-15 6.6024e-15 6.6024e-15 6.6024e-15 8.8818e-16 8.8818	1.7926e+03 1.7924e+03 1.7492e+03 897.0959 1.3604e+03 1.4897e+03 1.5558e+03 1.3690e+03 <b>Std. Dev</b> 2.9043 3.0483 3.0201 2.5248 1.2921 1.2812 1.2812 1.2812 1.2812 1.2812 1.2812 1.2812 1.2812 5.7261e+07 5.7261e+07 5.6152e+07 5.6152e+07 5.6132e+07 3.1591e+07 3.2097e+07 1.7356e+07	-1.7816e+04 -1.8195e+04 -1.2347e+04 -1.2569e+04 -1.2569e+04 -1.2569e+04 -1.2532e+04 -1.2201e+04 <b>Best</b> 4.6205e-15 3.9352e-15 4.6205e-15 4.4409e-15 8.8818e-16 8.8818e-16 8.8818e-16 8.8818e-16 <b>Best</b> 0.0486 0.0482 0.0465 0.0472 0.0101 0.0073 0.0126	-3.4627e+03 -3.4996e+03 -2.4467e+03 -1.7542e+03 -3.4988e+03 -2.2332e+03 -2.2201e+03 -1.5414e+03 Worst 20.6019 20.7294 20.6903 20.4593 20.8727 20.6321 20.7436 20.9750 20.5905 Worst 7.4182e+08 7.9208e+08 7.8265e+08 7.4401e+08 6.8750e+08 7.1770e+08 3.7500e+08

Table 7. Statistical analysis of obtained solution cost for F<sub>1</sub> to F<sub>23</sub>

				Table	7. Continued					
			<b>F</b> <sub>13</sub>					F <sub>14</sub>		
Alg.	Average	Median	Std. Dev	Best	Worst	Average	Median	Std. Dev	Best	Worst
CEA	-		8.2696e+07			-				
GSA	8.8435e+06	0.4261		0.4261	3.4791e+08	3.9406	2.9143	2.5492	2.9143	304.6271
DE	9.4926e+06	0.3158	8.8716e+07	0.3158	3.4627e+08	3.9603	2.9084	2.5834	2.9084	304.6419
PSO	9.5109e+06	0.3151	8.3418e+07	0.3151	3.4996e+08	3.5038	2.9864	2.5681	2.9864	201.1934
WOA	9.6103e+06	0.2720	8.2630e+07	0.2720	9.5398e+08	3.4340	2.9821	2.6263	2.9821	43.0259
IWOA	2.5621e+06	0.3602	5.6061e+07	0.3602	1.2533e+09	1.8742	0.9980	18.6189	0.9980	416.9956
CSAWOA	1.2597e+06	0.1022	2.8129e+07	0.1020	6.2899e+08	1.3906	0.9980	5.3740	0.9980	115.8909
RWOA	3.9986e+06	0.2009	6.7180e+07	0.2008	1.4467e+09	1.3106	0.9980	4.8911	0.9980	78.4131
MSWOA	3.4805e+06	0.2839	7.7827e+07	0.2838	1.7403e+09	1.2186	0.9980	2.2341	0.9980	46.0861
HWOA	2.1650e+06	0.2324	4.8411e+07	0.2323	1.0825e+09	1.2154	0.9921	1.0419	0.9921	5.6662
			F <sub>15</sub>					F <sub>16</sub>		
Alg.	Average	Median	Std. Dev	Best	Worst	Average	Median	Std. Dev	Best	Worst
GSA	0.0072	0.0089	0.0348	0.0089	0.6428	-1.0364	-1.0316	0.2487	-1.0316	0.1791
DE	0.0086	0.0075	0.0365	0.0075	0.6612	-1.0363	-1.0316	0.2674	-1.0316	0.1772
PSO	0.0065	0.0081	0.0349	0.0081	0.5241	-1.0316	-1.0316	0.1642	-1.0316	0.1541
WOA	0.0015	3.2965e-04	0.0205	3.2964e-04	0.4502	-1.0305	-1.0316	0.0089	-1.0316	-0.8963
IWOA	9.7449e-04	4.6921e-04	0.0038	4.6921e-04	0.0746	-1.0198	-1.0316	0.1012	-1.0316	0.1630
CSAWOA	7.6984e-04	3.1298e-04	0.0056	3.1298e-04	0.1238	-1.0188	-1.0316	0.1130	-1.0316	1.0587
RWOA	0.0016	4.9407e-04	0.0030	4.9407e-04	0.1238	-0.9916	-0.9999	0.1416	-0.9999	2.1355
MSWOA	6.6054e-04		0.0210	4.9407e-04 4.3257e-04	0.0485	-0.9910	-0.9999	0.1410	-0.9999	3.4022
		4.3257e-04								
HWOA	6.0123e-04	3.7381e-04	0.0028	3.7258e-04	0.0599	-0.9931	-1.0000	0.0350	-1.0000	-0.7368
Alg.	· .		F <sub>17</sub>		***			F <sub>18</sub>	<b>D</b> (	
	Average	Median	Std. Dev	Best	Worst	Average	Median	Std. Dev	Best	
GSA	0.5247	0.3971	0.1736	0.3979	1.3601	3.4518	3.0000	3.0814	3.0000	34.4201
DE	0.5716	0.3969	0.1705	0.3979	1.4608	3.5806	3.0000	3.0514	3.0000	34.1089
PSO	0.4975	0.3951	0.1674	0.3979	2.3072	3.4841	3.0000	3.2153	3.0000	34.0045
WOA	0.4256	0.3982	0.1260	0.3979	1.2673	3.5112	3.0000	3.5737	3.0000	34.9664
IWOA	0.4115	0.3979	0.1003	0.3979	1.2713	3.3809	3.0000	3.0850	3.0000	33.3362
CSAWOA	0.4000	0.3979	0.0155	0.3979	0.5795	3.0159	3.0000	0.1765	3.0000	5.7108
RWOA	0.4324	0.3983	0.5675	0.3979	12.8981	3.1832	3.0184	1.3085	3.0183	22.4620
MSWOA	0.4195	0.4024	0.0932	0.3985	1.0922	3.2130	3.0027	0.8532	3.0022	8.7739
HWOA	0.4236	0.4001	0.1144	0.3999	1 ( 400	0.7100	2 0000	5.2395	3.0000	70.2(10
			0.1144	0.5999	1.6499	3.7103	3.0000	5.2395	5.0000	79.2618
	011200	0.1001		0.3999	1.0499	3.7103	3.0000		3.0000	/9.2018
Alg.		Median	<b>F</b> <sub>19</sub>	Best	Worst		Median	5.2395 F <sub>20</sub> Std. Dev	Best	Worst
	Average	Median	F <sub>19</sub> Std. Dev	Best	Worst	Average	Median	F <sub>20</sub> Std. Dev	Best	Worst
GSA	Average -3.8514	<b>Median</b> -3.8567	<b>F</b> <sub>19</sub> <b>Std. Dev</b> 0.0721	Best -3.8587	Worst -3.4802	<b>Average</b> -3.2142	<b>Median</b> -2.0701	<b>F</b> <sub>20</sub> <b>Std. Dev</b> 0.0618	Best -3.1014	Worst -1.7692
GSA DE	Average -3.8514 -3.8587	Median -3.8567 -3.8712	F19           Std. Dev           0.0721           0.0506	Best -3.8587 -3.8654	Worst -3.4802 -2.9634	Average -3.2142 -2.8401	Median -2.0701 -2.4602	F20           Std. Dev           0.0618           0.0681	Best -3.1014 -3.0285	Worst -1.7692 -1.5593
GSA DE PSO	Average -3.8514 -3.8587 -3.8297	Median -3.8567 -3.8712 -3.8409	F19           Std. Dev           0.0721           0.0506           0.0501	Best -3.8587 -3.8654 -3.8542	Worst -3.4802 -2.9634 -3.2409	Average -3.2142 -2.8401 -3.2406	Median -2.0701 -2.4602 -3.0019	F <sub>20</sub> Std. Dev 0.0618 0.0681 0.0605	<b>Best</b> -3.1014 -3.0285 -1.4018	Worst -1.7692 -1.5593 -1.4608
GSA DE PSO WOA	Average           -3.8514           -3.8587           -3.8297           -3.8218	Median -3.8567 -3.8712 -3.8409 -3.8560	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616	Best -3.8587 -3.8654 -3.8542 -3.8565	Worst -3.4802 -2.9634 -3.2409 -3.4609	Average -3.2142 -2.8401 -3.2406 -2.9480	Median -2.0701 -2.4602 -3.0019 -2.9899	F20 Std. Dev 0.0618 0.0681 0.0605 0.0695	Best -3.1014 -3.0285 -1.4018 -2.9900	Worst -1.7692 -1.5593 -1.4608 -2.3866
GSA DE PSO WOA IWOA	Average -3.8514 -3.8587 -3.8297 -3.8218 -3.8585	Median -3.8567 -3.8712 -3.8409 -3.8560 -3.8613	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014	F20           Std. Dev           0.0618           0.0681           0.0605           0.0695           0.1696	Best -3.1014 -3.0285 -1.4018 -2.9900 -3.3015	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692
GSA DE PSO WOA IWOA CSAWOA	Average -3.8514 -3.8587 -3.8297 -3.8218 -3.8585 -3.8290	Median -3.8567 -3.8712 -3.8409 -3.8560 -3.8613 -3.8549	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634 -3.2802	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017	F20           Std. Dev           0.0618           0.0681           0.0605           0.0695           0.1696           0.1452	<b>Best</b> -3.1014 -3.0285 -1.4018 -2.9900 -3.3015 -3.0235	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593
GSA DE PSO WOA IWOA CSAWOA RWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960	Median -3.8567 -3.8712 -3.8409 -3.8560 -3.8613 -3.8549 -3.8249	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634 -3.2802 -3.3592	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143	$\begin{array}{c} F_{20} \\ \hline Std. \ Dev \\ 0.0618 \\ 0.0608 \\ 0.0605 \\ 0.0695 \\ 0.1696 \\ 0.1452 \\ 0.1464 \end{array}$	Best -3.1014 -3.0285 -1.4018 -2.9900 -3.3015 -3.0235 -3.3143	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA	Average -3.8514 -3.8587 -3.8297 -3.8218 -3.8585 -3.8290 -3.7960 -3.8128	Median -3.8567 -3.8712 -3.8409 -3.8560 -3.8613 -3.8549 -3.8249 -3.8249 -3.8612	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260 -3.8612	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634 -3.2802 -3.3592 -3.5227	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2733	Best -3.1014 -3.0285 -1.4018 -2.9900 -3.3015 -3.0235 -3.3143 -2.6756	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171 -0.8829
GSA DE PSO WOA IWOA CSAWOA RWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960	Median -3.8567 -3.8712 -3.8409 -3.8560 -3.8613 -3.8549 -3.8249	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634 -3.2802 -3.3592	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143	$\begin{array}{c} F_{20} \\ \hline Std. \ Dev \\ 0.0618 \\ 0.0608 \\ 0.0605 \\ 0.0695 \\ 0.1696 \\ 0.1452 \\ 0.1464 \end{array}$	Best -3.1014 -3.0285 -1.4018 -2.9900 -3.3015 -3.0235 -3.3143	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA	Average -3.8514 -3.8587 -3.8297 -3.8218 -3.8585 -3.8290 -3.7960 -3.8128	Median -3.8567 -3.8712 -3.8409 -3.8560 -3.8613 -3.8549 -3.8249 -3.8249 -3.8612	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260 -3.8612	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634 -3.2802 -3.3592 -3.5227	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2733	Best -3.1014 -3.0285 -1.4018 -2.9900 -3.3015 -3.0235 -3.3143 -2.6756	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171 -0.8829 -1.4009
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg.	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057	Median           -3.8567           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260 -3.8612 -3.8612 -3.8553 Best	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 Median	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2353           F22           Std. Dev	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171 -0.8829 -1.4009 Worst
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057	Median           -3.8567           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260 -3.8612 -3.8553	Worst -3.4802 -2.9634 -3.2409 -3.4609 -2.9634 -3.2802 -3.3592 -3.5227 -3.0619	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2733           0.2353           F22	Best -3.1014 -3.0285 -1.4018 -2.9900 -3.3015 -3.0235 -3.3143 -2.6756 -3.1437	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171 -0.8829 -1.4009
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg.	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057	Median           -3.8567           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev	Best -3.8587 -3.8654 -3.8542 -3.8565 -3.8614 -3.8549 -3.8260 -3.8612 -3.8612 -3.8553 Best	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 Median	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2353           F22           Std. Dev	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best	Worst -1.7692 -1.5593 -1.4608 -2.3866 -1.7692 -1.5593 -1.5171 -0.8829 -1.4009 Worst
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA HWOA Alg. GSA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021	Median           -3.8567           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154	Best           -3.8587           -3.8654           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8553           Best           -3.1408	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           Median           -3.8560	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2353           F22           Std. Dev           0.3144	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA HWOA Alg. GSA DE	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407           -4.3518	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8553           Best           -3.1408           -3.9215	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           Median           -3.8560           -3.0417	F20           Std. Dev           0.0618           0.0605           0.0695           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4935	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA HWOA Alg. GSA DE PSO	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           Median           -3.8560           -3.0417           -3.8409	F20           Std. Dev           0.0618           0.0605           0.0695           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4935           0.2954	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142
GSA DE PSO WOA IWOA CSAWOA RWOA MSWOA HWOA Alg. GSA DE PSO WOA IWOA	Average           -3.8514           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           Median           -3.8560           -3.0417           -3.8409           -3.7213           -6.8573	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4935           0.2954           0.3054           0.8925	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9900           -3.7213           -6.8695	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA HWOA GSA DE PSO WOA IWOA CSAWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8612           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           Median           -3.8560           -3.0417           -3.8409           -3.7213           -6.8573           -9.4109	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4935           0.2954           0.3054           0.8925           1.9301	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9900           -3.7213           -6.8695           -9.4130	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           -2.6756           -3.1437           -3.8560           -3.0417           -3.8409           -3.7213           -6.8573           -9.4109           -10.3475	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4935           0.2954           0.3054           0.8925           1.9301           1.9994	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8614           -3.8549           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501	Median           -2.0701           -2.4602           -3.0019           -2.9899           -3.3014           -3.0017           -3.3143           -2.6756           -3.1437           -2.6756           -3.1437           -3.8560           -3.0417           -3.8409           -3.7213           -6.8573           -9.4109           -10.3475	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4935           0.2954           0.3054           0.8925           1.9301           1.9994	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA	Average           -3.8514           -3.8514           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8612           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23	Best           -3.8587           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA RWOA HWOA HWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA RWOA HWOA HWOA HWOA	Average           -3.8514           -3.8587           -3.8297           -3.8218           -3.8218           -3.8585           -3.8200           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA HWOA HWOA HWOA HWOA	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408	Median           -3.8567           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8249           -3.8612           -3.8553           Median           -4.5407           -4.5407           -4.5407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.4554	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8565           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA HWOA HWOA HWOA B	Average           -3.8514           -3.8587           -3.8587           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.4554           0.4171	Best           -3.8587           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8614           -3.8549           -3.8612           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541           -0.1630	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA HWOA HWOA CSAWOA RWOA BSO BSO BSO BSO BSO BSO BSO BSO BSO BSO	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8297           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831           -5.0517	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8513           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593           -5.1273	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.4554           0.4171           0.3852	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8612           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541           -0.1630           -5.1273	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593           -1.3220	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA RWOA RWOA HWOA HWOA Alg. GSA DE PSO WOA IWOA HWOA I	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8218           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831           -5.0517           -2.3074	Median           -3.8567           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593           -5.1273           -2.4192	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.4554           0.4171           0.3852           0.3146	Best           -3.8587           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8614           -3.8549           -3.8612           -3.8612           -3.8612           -3.8612           -3.8612           -3.8260           -3.8612           -3.8612           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8612           -3.8553           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.1541           -0.1630           -5.1	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593           -1.3220           -0.6555	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA HWOA HWOA CSA BE PSO WOA IWOA CSAWOA IDE	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8297           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831           -5.0517           -2.3074           -5.5784	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593           -5.1273           -2.4192           -5.1016	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.454           0.4171           0.3852           0.3146           1.5542	Best           -3.8587           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8614           -3.8549           -3.8260           -3.8612           -3.8612           -3.8612           -3.8612           -3.8553           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541           -0.1630           -5.1273           -2.4192           -9.0782	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593           -1.3220           -0.6555           -0.8072	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA RWOA HWOA HWOA CSAWOA RWOA BAL BC BC BC BC BC BC BC BC BC BC BC BC BC	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8218           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831           -5.0517           -2.3074	Median           -3.8567           -3.8712           -3.8409           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593           -5.1273           -2.4192	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.4554           0.4171           0.3852           0.3146	Best           -3.8587           -3.8654           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8612           -3.8612           -3.8612           -3.8612           -3.8260           -3.8612           -3.8612           -3.8260           -3.8612           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8260           -3.8612           -3.820           -4.2831           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541           -0.1630           -5.1273           -2.4192	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593           -1.3220           -0.6555	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA HWOA HWOA CSA BE PSO WOA IWOA CSAWOA IE	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8297           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831           -5.0517           -2.3074           -5.5784	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593           -5.1273           -2.4192           -5.1016	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.454           0.4171           0.3852           0.3146           1.5542	Best           -3.8587           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8612           -3.8612           -3.8612           -3.8612           -3.8260           -3.8260           -3.8612           -3.8253           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541           -0.1630           -5.1273           -2.4192           -9.0782	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593           -1.3220           -0.6555           -0.8072	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594
GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA RWOA HWOA Alg. GSA DE PSO WOA IWOA CSAWOA HWOA CSAWOA RWOA IWOA CSAWOA RWOA	Average           -3.8514           -3.8587           -3.8297           -3.8297           -3.8297           -3.8297           -3.8218           -3.8585           -3.8290           -3.7960           -3.8128           -3.8057           Average           -3.9021           -3.7463           -4.4026           -4.9423           -9.9569           -6.9943           -5.0086           -4.5664           -4.4230           Average           -1.9215           -1.1408           -1.2831           -5.0517           -2.3074           -5.5784           -2.3955	Median           -3.8567           -3.8712           -3.8712           -3.8409           -3.8560           -3.8560           -3.8613           -3.8549           -3.8549           -3.8549           -3.8553           Median           -4.5407           -4.3518           -4.0407           -5.0547           -10.0979           -5.0521           -5.0528           -4.6989           -4.5876           Median           -4.0019           -3.4602           -4.5593           -5.1273           -2.4192           -5.1016           -2.4244	F19           Std. Dev           0.0721           0.0506           0.0501           0.0616           0.0411           0.0429           0.0552           0.0725           0.1308           F21           Std. Dev           2.0154           2.4106           0.3109           0.4996           0.8079           2.5053           0.3067           0.2979           0.4779           F23           Std. Dev           0.4512           0.454           0.4171           0.3852           0.3146           1.5542           0.1182	Best           -3.8587           -3.8654           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8542           -3.8612           -3.8612           -3.8612           -3.8612           -3.8260           -3.8260           -3.8612           -3.8253           Best           -3.1408           -3.9215           -4.2831           -5.0547           -10.1128           -9.9571           -5.0529           -4.6989           -4.5876           Best           -0.8963           -0.1541           -0.1630           -5.1273           -2.4192           -9.0782           -2.4251	Worst           -3.4802           -2.9634           -3.2409           -3.4609           -2.9634           -3.2802           -3.3592           -3.5227           -3.0619           Worst           -0.9154           -0.9425           -9.7106           -0.5249           -2.0944           -0.4070           -0.4786           -0.4279           -0.3629           Worst           -0.9142           -1.5893           -1.5593           -1.3220           -0.6555           -0.8072           -0.7247	Average -3.2142 -2.8401 -3.2406 -2.9480 -3.2169 -2.9522 -3.2815 -2.6257 -3.0471 Average -2.1008 -3.1473 -3.4083 -3.4083 -3.6383 -6.3471 -8.1818 -9.3501 -3.3935	Median -2.0701 -2.4602 -3.0019 -2.9899 -3.3014 -3.0017 -3.3143 -2.6756 -3.1437 -3.8409 -3.8560 -3.0417 -3.8409 -3.7213 -6.8573 -9.4109 -10.3475 -3.8828	F20           Std. Dev           0.0618           0.0605           0.1696           0.1452           0.1464           0.2733           0.2353           F22           Std. Dev           0.3144           0.4955           0.3054           0.3054           0.8925           1.9301           1.9994           0.8519	Best           -3.1014           -3.0285           -1.4018           -2.9900           -3.3015           -3.0235           -3.3143           -2.6756           -3.1437           Best           -3.0019           -2.9480           -2.9900           -3.7213           -6.8695           -9.4130           -10.3630           -3.8828	Worst           -1.7692           -1.5593           -1.4608           -2.3866           -1.7692           -1.5593           -1.5171           -0.8829           -1.4009           Worst           -0.4102           -0.5657           -0.9142           -0.5457           -1.0269           -0.5524           -0.7678           -0.4594

Table 7. Continued

		Iris	over 30 independent run	Glass					
Alg.	Solution cost	Intra-cluster	Inter-cluster	Solution cost	Intra-cluster	Inter-cluster			
GSA	0.2791±0.0157	$2.4925 \pm 0.3709$	$1.9247 \pm 0.2746$	0.0565±0.0049	$5.2019 \pm 0.8524$	$5.2634 \pm 6.4387$			
DE	0.2787±0.0151	$2.2405 \pm 0.3918$	$1.9219 \pm 0.2778$	0.0584±0.0027	$5.2113 \pm 0.8509$	$4.7738 \pm 9.2009$			
PSO	0.2787±0.0152	$2.4703 \pm 0.3725$	$1.9701 \pm 0.2784$	0.0428±0.0047	$5.0216 \pm 0.7034$	$6.0021 \pm 7.3475$			
WOA	0.2672±0.0141	$2.3902 \pm 0.3562$	$1.9291 \pm 0.2789$	0.0443±0.0042	$5.0199 \pm 0.7014$	$4.7812 \pm 9.2109$			
IWOA	0.2765±0.0042	$2.2258 \pm 0.3601$	$1.9121 \pm 0.2821$	0.0436±0.0027	$4.9542 \pm 0.5987$	$5.2514 \pm 6.4521$			
CSAWOA	0.2681±0.0071	$2.2258 \pm 0.3429$	$1.9623 \pm 0.2731$	0.0435±0.0029	$4.8781 \pm 0.8924$	$6.0081 \pm 7.3125$			
RWOA	0.2689±9.5741e-004	$2.1222 \pm 0.3522$	$1.9802 \pm 0.2189$	0.0433±0.0017	$4.8745 \pm 0.8957$	$6.4189 \pm 6.9702$			
MSWOA	0.2655±0.0067	$2.0641 \pm 0.3434$	$1.9291 \pm 0.2789$	0.0429±0.0031	$4.0934 \pm 0.7134$	$6.7204 \pm 9.0704$			
HWOA	0.2645±0.0064	$2.0176 \pm 0.3427$	$1.9802 \pm 0.2189$	0.0414±0.0014	$4.3705 \pm 0.7447$	$6.7612 \pm 6.4308$			
		Wine			Breast				
Alg.	Solution cost	Intra-cluster	Inter-cluster	Solution cost	Intra-cluster	Inter-cluster			
GSA	360.8613±1.8143	364.6584 ± 8.6347	328.5411 ± 3.4305	0.0672±0.0214	17.1289 ± 3.7189e-015	13.4628 ± 0			
DE	359.4155±11.1054	362.0013 ± 9.8672	359.8273 ± 54.4602	0.0621±0.0275	16.9721 ± 7.46e-15	$13.4654 \pm 0$			
PSO	343.8378±3.5681	350.1967 ± 7.5448	349.7465 ± 46.7305	0.0563±0.0361	17.0346 ± 8.01e-15	$13.5438 \pm 0$			
WOA	340.1125±10.9298	350.1951 ± 7.5439	329.2461 ± 71.9199	0.0561±0.0285	17.0246 ± 7.95e-15	$13.4529 \pm 0$			
IWOA	340.8713±1.7802	341.7484 ± 8.6213	329.2701 ± 72.4532	0.0552±0.0128	17.0238 ± 8.01e-15	$13.4536 \pm 0$			
CSAWOA	342.8378±3.6219	$341.0013 \pm 9.8928$	$363.7845 \pm 46.7197$	0.0546±0.0341	17.0238 ± 7.89e-15	$13.4523 \pm 0$			
RWOA	341.7219±6.8014e-014	332.7921 ± 2.2318	359.8712 ± 52.3245	0.0551±6.7872e-004	16.9804 ± 7.45e-15	$13.5521 \pm 0$			
MSWOA	341.6293±1.6702	330.1041 ± 7.4414	345.2121 ± 47.3042	0.0547±0.1385	16.0426 ± 7.75e-15	$13.4521 \pm 0$			
HWOA	339.6378±1.6716	330.1181 ± 7.4034	329.2711 ± 47.9159	0.0534±0.0234	16.4036 ± 7.71e-15	$13.4520 \pm 0$			
		Diabetes			Haberman				
Alg.	Solution cost	Intra-cluster	Inter-cluster	Solution cost	Intra-cluster	Inter-cluster			
GSA	14.5400±0.1048	730.0298 ± 0.1502	$30.4512 \pm 0.4152$	$5.4800 \pm 0.3273$	40.3214 ± 2.1089e-014	5.2185 ± 8.8425e-016			
DE	14.5701±0.1814	$713.6642 \pm 74.3624$	36.2192 ± 12.2457	$5.5629 \pm 0.2713$	35.1085 ± 3.5591	8.7361 ± 10.8134			
PSO	14.4416±0.0548	$713.6502 \pm 74.3512$	$36.2192 \pm 12.2401$	$5.7000 \pm 0.3045$	$35.3451 \pm 3.6982$	$7.3547 \pm 9.8732$			
WOA	14.2800±0.1654	$708.0127 \pm 74.4521$	$36.2301 \pm 14.7728$	$5.7700 \pm 0.2845$	$35.3026 \pm 3.6534$	$7.6424 \pm 9.8043$			
IWOA	13.8000±0.0954	$707.0087 \pm 74.6214$	$36.2354 \pm 14.7602$	$5.7800 \pm 0.3215$	$35.2445 \pm 3.784$	$7.9401 \pm 9.9731$			
CSAWOA	13.8524±0.0459	$705.9815 \pm 74.3714$	$36.8004 \pm 14.4543$	$5.3300 \pm 0.3545$	$35.2064 \pm 3.0475$	$7.9821 \pm 9.9801$			
RWOA	$13.7689 \pm 0.0025$	$705.9802 \pm 74.3512$	$36.8425 \pm 14.4512$	5.5689±3.6142e-006	$34.9885 \pm 3.6875$	$8.1285 \pm 10.4219$			
MSWOA	13.7741±0.0454	$705.0164 \pm 74.6151$	$36.3051 \pm 14.3508$	$5.3655 \pm 0.3065$	$34.3721 \pm 3.5504$	$7.3047 \pm 9.8042$			
HWOA	13.7453±0.0656	$705.0045 \pm 74.3402$	$36.3801 \pm 14.3461$	5.2814±0.3061	$34.3125 \pm 3.5530$	$7.3607 \pm 9.8342$			
Ala		Hayes-Roth		E. Coli					
Alg.	Solution cost	Intra-cluster	Inter-cluster	Solution cost	Intra-cluster	Inter-cluster			
GSA	$0.3279 \pm 0.0324$	$3.5643 \pm 0.4428$	$1.3915 \pm 0.3541$	$0.0672 \pm 0.0373$	$0.6648 \pm 0.0834$	$0.2445 \pm 0.0598$			
DE	$0.3928 \pm 0.0346$	$3.518 \pm 0.2735$	$1.8519 \pm 0.7531$	$0.0663 \pm 0.0032$	$0.6643 \pm 0.0735$	$0.3637 \pm 0.1341$			
PSO	$0.3507 \pm 0.0254$	$3.5081 \pm 0.4318$	$1.4189 \pm 0.6078$	$0.0671 \pm 0.0030$	$0.6312 \pm 0.0726$	$0.3145 \pm 0.1028$			
WOA	$0.3672 \pm 0.0284$	$3.5492 \pm 0.4865$	$1.4256 \pm 0.6845$	$0.0641 \pm 0.0028$	$0.6745 \pm 0.0825$	$0.3176 \pm 0.1517$			
IWOA	$0.3765 \pm 0.0251$	$3.5489 \pm 0.4812$	$1.4364 \pm 0.6704$	$0.0672 \pm 0.0028$	$0.6545 \pm 0.0754$	$0.3522 \pm 0.1102$			
CSAWOA	$0.2681 \pm 0.0248$	$3.5413 \pm 0.4716$	$1.7012 \pm 0.6146$	$0.0666 \pm 0.0030$	$0.6245 \pm 0.0689$	$0.4540 \pm 0.1056$			
RWOA	$0.2689 \pm 0.0129$	$3.2508 \pm 0.3512$	$1.8251 \pm 0.6702$	$0.0641 \pm 0.0012$	$0.6012 \pm 0.0542$	$0.4643 \pm 0.1728$			
MSWOA	0.2655±0.0105	$3.3415 \pm 0.4181$	$1.4046 \pm 0.6451$	0.0637±0.00124	$0.6015 \pm 0.0621$	$0.3206 \pm 0.1410$			
HWOA	0.2645±0.0108	$3.5472 \pm 0.4160$	$1.4053 \pm 0.6415$	0.0624±0.00113	$0.6018 \pm 0.0721$	$0.3603 \pm 0.1421$			
Alg.		Zoo			Vowel				
	Solution cost	Intra-cluster	Inter-cluster	Solution cost	Intra-cluster	Inter-cluster			
GSA	$0.0202 \pm 0.0026$	1.6378 ± 1.1528e-15	$2.2315 \pm 5.0214e-016$	$41.9500 \pm 1.3465$	$901.3251 \pm 108.8745$	348.3268 ± 230.3519			
DE	$0.0220 \pm 0.0024$	$1.6512 \pm 1.1324e-15$	$2.6502 \pm 2.278e-15$	$39.2800 \pm 2.2481$	$898.617 \pm 102.9459$	$353.3712 \pm 218.2482$			
PSO	$0.0130 \pm 0.0018$	1.6396 ± 1.1244e-15	2.6421 ± 2.256e-15	$38.4700 \pm 2.3618$	$899.254 \pm 101.8954$	$350.3465 \pm 215.7135$			
WOA	$0.0120 \pm 0.0022$	$1.6401 \pm 1.1312e-15$	2.6471 ± 2.274e-15	$38.4012 \pm 2.2314$	$899.246 \pm 101.8705$	$350.3548 \pm 215.6548$			
IWOA	$0.0110 \pm 0.0021$	1.6391 ± 1.1268e-15	$2.6484 \pm 2.25e-15$	$37.6824 \pm 1.3545$	$899.238 \pm 102.3254$	$350.7091 \pm 215.9805$			
CSAWOA	$0.0090 \pm 0.0019$	1.6381 ± 1.1254e-15	$2.6487 \pm 2.258e-15$	$36.8140 \pm 2.3456$	$899.228 \pm 102.3815$	$350.8086 \pm 215.9501$			
RWOA	$0.0094 \pm 8.3665 - 04$	$1.5254 \pm 4.5498e-016$	$2.6502 \pm 2.256e-15$	$35.8941 \pm 2.2145$	$898.145 \pm 102.9821$	353.3282 ± 218.2545			
MSWOA	0.0100±0.0012	$1.5332 \pm 1.1268e-14$	$2.6451 \pm 2.264e-15$	$34.1553 \pm 2.2645$	$898.224 \pm 102.3142$	$350.7301 \pm 215.9611$			
HWOA	0.00534±0.0024	1.4301 ± 1.1341e-14	2.6432 ± 2.261e-15	$32.4501 \pm 2.2416$	898.138 ± 102.3107	$350.6126 \pm 215.9411$			

Table 8. Mean and std. dev. over 30 independent runs for 500 iterations for 10 real datasets

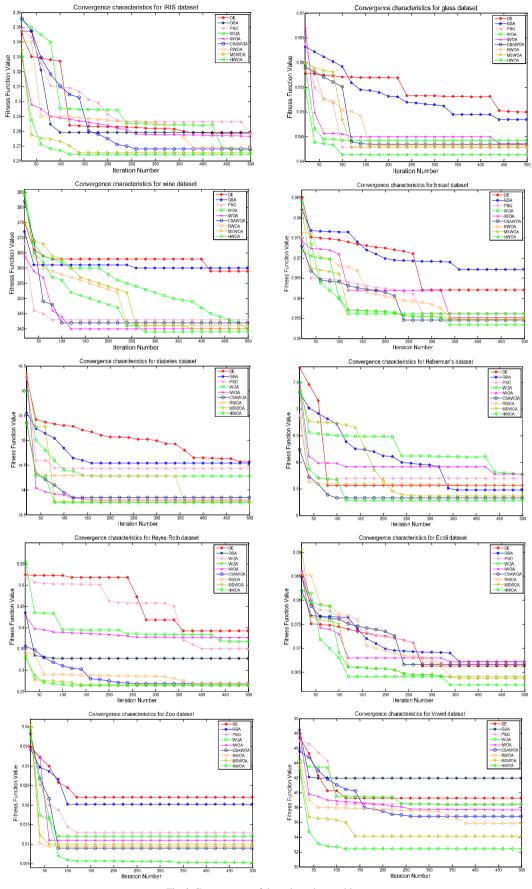


Fig.6. Convergence of data clustering problems

#### VI. CONCLUSIONS AND FUTURE WORK

In this work we presented multi-swarm cooperative strategies for addressing two problems. They are solving standard mathematical benchmark functions problems and solving the data clustering problems. In this process we have used the standard whale optimization algorithm. We utilized three cooperative strategies namely the Ring, Master-Slave and Hybrid cooperative strategies to enhance the performance of standard WOA. Several experiments have been conducted and the performance of each cooperative strategy is compared with previously established techniques GSA, DE, PSO, WOA and also variants of WOA. The results established the multi-swarm cooperative strategies outperform in solving benchmark functions as well as the data clustering problems compared GSA, DE, PSO, WOA and variants of WOA for 10 different real databases. All the obtained graphical and statistical results are reported respective figures and tables. The reported values were averaged over 40 simulations to specify the algorithms convergence range. In most cases, the proposed multi-swarm cooperative strategies realized lower quantization errors. Generally, the proposed multi-swarm cooperative strategies establish their efficiency in finding optimizing benchmark functions as well as the data clustering problems.

This explore run may be extended for further research in the shadowing dimensions: In this research work, the show on multiple swarm based cooperative strategies proposed for enhancing the numerical optimization performance of WOA and these are compared with other-state-of-the-art algorithms and variants of WOA for its action judgement on 23 standard benchmark functions. As a future line, added new versions of WOA could also be tried to key the unexceeded type in achieving test suite improvement. This research work concentrate on standard WOA optimization. In the future we go through the new based meta-heuristic optimization population algorithms which are also inspired by the nature.

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