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Multiagent Based Reactive Power Sharing and Control Model for Islanded Microgrids

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Abstract—In islanded microgrids (MGs), the reactive power cannot be shared proportionally among distributed generators (DGs) with conventional droop control, due to the mismatch in feeder impedances. For the purpose of proportional reactive power sharing, a multiagent system (MAS) based distributed control model for droop-controlled MGs is proposed. The proposed control model consists of two layers, where the bottom layer is the electrical distribution MG, while the top layer is a communication network composed of agents. Moreover, agents on the communication network exchange the information acquired from DGs with neighbors, and calculate set points for DGs they connect to, according to the control laws. Further, a theorem is demonstrated, which yields a systematic method to derive the control laws from a given communication network. Finally, three cases are carried out to test the performance of the control model, in which the uncertainty of intermittent DGs, variations in load demands, as well as impacts of time delays are considered. The simulation results demonstrate the effectiveness of the control model in proportional reactive power sharing, and the plug and play capability of the control model is also verified.

Index Terms—Microgrids (MGs), multiagent system (MAS), distributed control, reactive power sharing, plug and play.

I. Introduction

Nowadays, world consumption of mineral resources is constantly increasing, so that the proven mineral resources reserves are progressively decreasing and even exhausted. To address these concerns, the share of renewable energy in energy consumption has been steadily growing, in the last few years [1]. And it is worth noting that the increasing trend toward renewable energy has brought forward the microgrid (MG), which facilitates the effective integration of distributed generators (DGs) into the main grid. An MG is able to operate in both islanded and grid-connected modes, as well as to transfer between these two modes seamlessly. However, the control and management of inverter-based

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MGs pose significant challenges, due to their low inertia, bidirectional power flows, and the uncertainty of intermittent DGs, etc [2], [3].

A popular control approach, termed centralized control, has been widely employed in MG control, and it requires all DGs to communicate with the MG central controller (MGCC), and then control decisions are broadcasted back to DGs. Therefore, the centralized control highly depends on the MGCC to process significant amounts of data, and it requires an extensive communication network to collect information globally. Moreover, there is an intrinsic disadvantage of single-point failure in centralized control, because any failures of the MGCC or its associated communication links result in the failure of the MG. On the contrary, in decentralized and distributed control, the decision making is performed based on local information, eliminating the requirement of the MGCC and extensive communication network. Therefore, the decentralized and distributed control are better suited for a large sized MG than centralized control, and the main difference between the decentralized and distributed control lies in the fact that neither interactions nor local communication network among DGs is considered in decentralized control [4], [5].

Considering the high variability of photovoltaic generators (PVs), cooperative control has been studied for distributed control of PVs [6]–[8], which has robustness against intermittency and latency on the communication network. For example, cooperative control was utilized to allow PVs to operate at the same active power utilization ratio with respect to their respective capacities [6]. And further work was carried out, which required no direct measurement of output of each PV [7]. For the case that multiple energy storage systems were organized as an MG, Xin *et al.* [8] developed an "N-1" redundant control network based on cooperative control, which satisfied both energy balance and fair utilization among energy storage systems with local measurements.

Furthermore, the multiagent system (MAS) has also been recently introduced to the area of distributed control of DGs [9]–[15]. For instance, an MAS based frequency control strategy was developed in [9], where agents exchanged information locally using an average consensus algorithm. Additionally, based on the stability of frequency, an adaptive distributed load shedding approach was investigated [10]. By combining MAS with cooperative control, Bidram *et al.* [11], [12] considered the secondary control of a droop-controlled MG as a tracking synchronization problem. Focusing on

distributed energy storages in an MG, an MAS based dynamic control strategy was demonstrated in [13], which allowed energy storages operate at a common energy level. In addition, a hierarchical MAS based energy management was developed to manage and optimize the MG operations [14]. And in our recent work [15], an agent-based control model for islanded MGs was proposed, which guaranteed the demand and supply balance, as well as the stability of frequency and voltage.

Moreover, the droop control has long been applied to decentralized control of islanded MGs, which requires no intercommunication among DGs. As is known, the accurate active power sharing is obtained easily by droop control, but due to the mismatch in feeder impedances between DGs, the conventional droop control achieves poor reactive power sharing among DGs, even with proportional droop coefficients [16], [17]. In other words, conventional droop control cannot distribute generation responsibility among DGs with respect to their respective power ratings, which may possibly result in a number of DGs being overload. Consequently, with the aim of proportional reactive power sharing, Guerrero et al. [18], [19] formulated the adaptive virtual output impedance. Further, the strategy based on static droop characteristics and transient droop function was developed [20]. Additionally, the method of optimum droop parameter settings for reactive power sharing was provided [21]. And based on current sensing and adaptive virtual impedance, Zhu et al. [22] developed a wireless reactive power sharing strategy.

It is worth noting that the introduction of communication network to droop control enhances the accuracy of reactive power sharing [23]–[34]. In [23], [24], a distributed strategy for secondary control and proportional reactive power sharing was investigated, where each DG required information of all other DGs in the MG. Further, the improvements were carried out in [25], [26], where each DG required information exchange with only a few neighboring DGs. Based on the work carried out in [11], [12], further work was performed to achieve power sharing among DGs [27]. In addition, the application of distributed finite-time control to distributed secondary control and power sharing was explored [28]. Considering the conflicting goals of voltage regulation and reactive power sharing, a distributed averaging proportional integral controller for secondary control was presented in [29]. With the consideration of dynamical models of PVs, battery energy storage systems, and plug-in hybrid vehicles, a nonlinear distributed controller for power sharing was developed [30]. Moreover, a distributed voltage control and reactive power sharing strategy was presented in [31], which was based on weighted average consensus protocol, and corresponding rigorous mathematical analysis was given. And Han et al. [32] improved the sharing accuracy by means of sharing error reduction and voltage recovery. In [33], a consensus-based power sharing method was developed, which was effective for alleviating the effects of non-ideal line impedances. Moreover, a distributed reactive power sharing approach was formulated in [34], where consensus control was utilized to adaptively adjust the virtual impedances.

On the other hand, DC MGs are emerging and they have attracted much attention, for DC MGs have several potential advantages over AC MGs, including simpler models and reduced conversion losses, etc [35]. With regard to distributed voltage control and power sharing in DC MGs, several distributed approaches based on information of average voltage and current of neighboring DGs were explored [36]–[39]. In [36], the control loop based on the average total current was developed for power sharing. Nasirian et al. [37] focused on a distributed primary and secondary controller for DC MGs, which employed a sparse communication network for data exchange among DGs. Based on dynamic consensus algorithm, a distributed hierarchical control approach for accurate current sharing and voltage restoration was proposed [38]. Additionally, an MAS based supervisory control was developed for power sharing and optimal power dispatch [39], where the average consensus algorithm was adopted for synchronous communication.

It is worth noting that in the existing methods [23]–[26], [29], [36]–[39], with the aim of power sharing, each DG collects the information i.e., the voltages, currents and power outputs of neighboring DGs using local communication network, and then the averages are calculated and used for adjusting the operation states of DGs, termed here the average methods. Motivated by the average methods discussed in the literature, in this paper, a two-layer MAS based reactive power sharing and control model is presented for a droop-controlled MG, where the bottom layer is the electrical distribution MG, while the top layer is an MAS communication network composed of agents. Moreover, the agents can collect the information of corresponding DGs, i.e., reactive power outputs, by means of communication links between two layers, and then they exchange the information acquired with their neighboring agents on the communication network. Furthermore, a theorem is proved, which provides a systematic method to derive the control laws from a given communication network. And in terms of acquired information and the control laws, the average reactive power outputs of neighboring controllable DGs can be calculated, i.e., the reference reactive power outputs. After that, the references are sent to DGs, to adjust their reactive power outputs. Finally, simulation cases are performed to verify the feasibility, as well as plug and play capability of the control model. According to the results, it can be found that the proportional power sharing is achieved, when the control laws are used, moreover, the plug out and plug in of the DG and agent do not affect the performance of the control model.

Furthermore, compared to existing methods, the salient features of the proposed control model are (i) a theorem is proved, which yields a systematic method for deriving the control laws from a given communication network, and then the reactive power references can be calculated conveniently in terms of the control laws, therefore making it more suitable for practical applications; (ii) the proposed control model has the capability of plug and play, which is not extensively discussed in the existing methods; (iii) the proposed control model is fully distributed, and each unit simply requires the information of reactive power outputs of its neighboring DGs, by means of a sparse communication network, which reduces
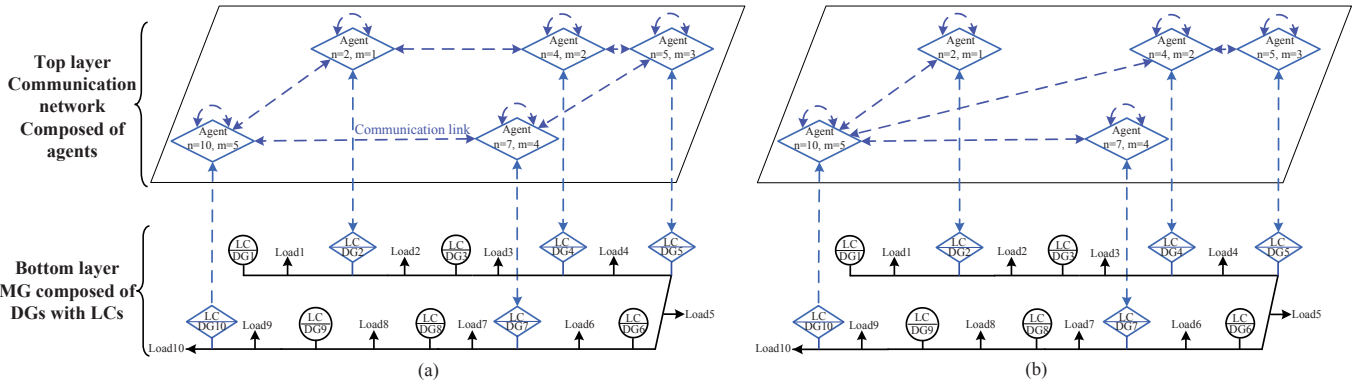
Fig. 1. The two-layer control model for islanded MGs. (a) Network 1: the ring communication network. (b) Network 2: the radial communication network. For the same MG, two different communication networks are established and used.

the communication cost.

The rest of the paper is organized as follows. In Section II, the MAS based control model for islanded MGs is formulated and described in detail. And in Section III, a theorem is demonstrated for deriving the control laws from a given communication network. Later, the structure and parameters of the islanded MG are introduced and listed in Section IV. In Section V, three cases with different settings are carried out to test the performance of the control model. Finally, Section VI concludes the paper.

II. Control Model for Islanded MGs

A. Control Model

In this paper, a two-layer control model is established, where the bottom layer is the electrical distribution MG, which consists of DGs, local controllers (LCs) and loads, while the top layer is an MAS communication network composed of agents, as shown in Fig. 1. Generally speaking, there are two types of DGs in an MG, i.e., *intermittent* and *controllable*, according to the characteristics of the output power [40]. For clarity, in the proposed control model, the intermittent DGs are indicated by circles, while controllable DGs and corresponding agents are illustrated by diamonds, as shown in Fig. 1. And it can be found in Fig. 1 that there exist bidirectional communication links between two layers and among agents, and agents have self loops. Further, the arrows on dashed lines on the communication network, and between two layers indicate the information transfer directions.

Therefore, by means of communication links, agents can collect the information of controllable DGs they connect to, i.e., the reactive power output, and then agents exchange the information acquired with their neighbors on the communication network. After that, the set points of controllable DGs can be calculated by agents, in terms of acquired information and control laws. Thereafter, the set points are sent to controllable DGs to adjust their reactive power outputs.

B. MAS Based Communication Network

In this paper, the MAS communication network is modeled by a directed graph $G(V, E)$, where V is the set of nodes or agents, and E is the set of edges or communication links. In order to describe the relationships between m agents, an $m \times m$ adjacency matrix A is used, where the entry $a_{ij} = 1$ means there is a communication link from Agent$_i$ to Agent$_j$, otherwise $a_{ij} = 0$. Also, an $m \times m$ and diagonal outdegree matrix D is employed to count the number of outgoing communication links of an agent, known as the outdegree d_{ii} of Agent$_i$. Moreover, the parameter k is defined as $k = \max(d_{11}, \cdots, d_{ii}, \cdots, d_{mm})$. Finally, $(k \cdot I)^{-1}$ is the inverse matrix of $k \cdot I$, and I is an $m \times m$ identity matrix.

It is should be emphasized that the topology of the MAS communication network is independent of the structure of the MG. In other words, it is not required that the topology of the communication network is identical to that of the MG. Therefore, many possible communication networks can be considered for a given MG, but each communication network possesses a set of control laws. In this paper, two communication networks with different topologies, network 1 and 2, are designed for the same MG, as shown in Fig. 1. Moreover, the communication network must be connected, i.e., there are no isolated agents on the communication network, for connected communication network allows communication among agents.

Furthermore, if the topology of the communication network is identical to that of the MG, the power line communication is a feasible manner to transmit information among agents. In the case that the topology of the communication network is different from that of the MG, other mature communication technologies are available, e.g., TCP/IP communication, optical fiber communication.

III. Distributed Control Laws for Reactive Power Sharing

For the purpose of reactive power sharing, in this section, a theorem is proved for deriving the control laws from a given communication network. And then in terms of the control laws, agents regulate the reactive power outputs of controllable DGs to which they connect, to realize the proportional power sharing.

First, the ratios of outputs of controllable DGs to their respective power ratings are defined. And suppose for the ith controllable DG, the active and reactive power ratios can be
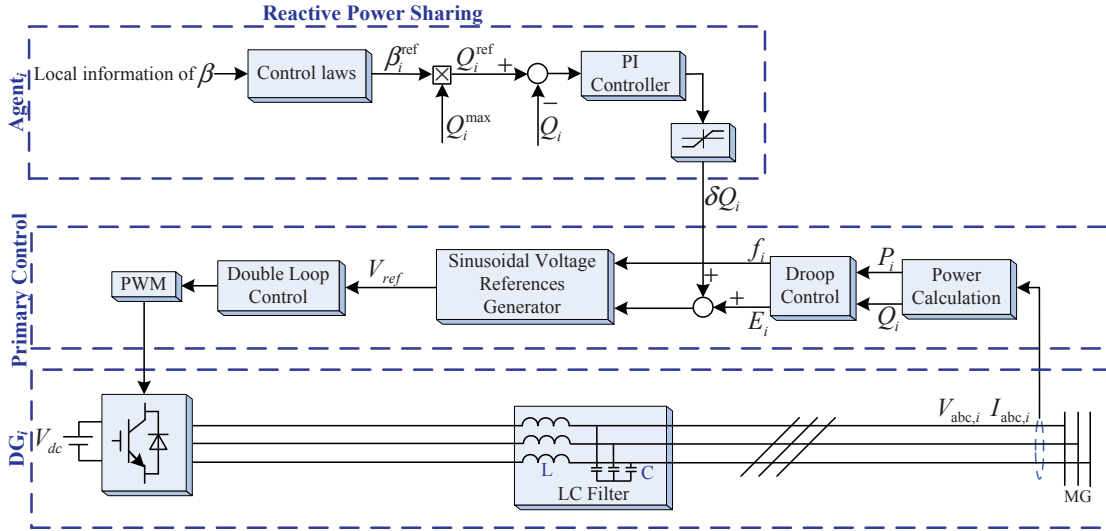
Fig. 2. Schematic of distributed reactive power sharing.

calculated

$$\begin{cases} \alpha_i = P_i/P_i^{\max}, \\ \beta_i = Q_i/Q_i^{\max}, \end{cases} \quad (1)$$

where α_i and β_i denote active and reactive power ratios, P_i, Q_i are active and reactive power outputs of controllable DG$_i$, and $P_i^{\max}$, $Q_i^{\max}$ are active and reactive power ratings of DG$_i$, respectively.

As discussed in Section II, agents can collect the information of reactive power outputs of controllable DGs they connect to. Therefore, receiving the information, the reactive power ratios can be calculated by agents in terms of (1), and then agents exchange the information of reactive power ratios with their neighbors on the communication network. Thereafter, in terms of the control laws and acquired information, the average reactive power ratios of neighboring controllable DGs can be calculated, i.e., the reference reactive power ratios, as illustrated in Fig. 2. Consequently, a theorem is proved, which provides a systemic method to derive the control laws for a given communication network.

Theorem: Let $G(V, E)$ be a directed communication network with m agents, if agents calculate the reference reactive power ratios in terms of (2), and apply the results to regulate reactive power outputs of controllable DGs to which they connect, then the proportional reactive power sharing among controllable DGs is guaranteed, namely, $\beta_1 = \cdots = \beta_i \cdots = \beta_m$,

$$\beta^{\text{ref}} = (k \cdot I)^{-1} \cdot [A + (k \cdot I - D)] \cdot \beta, \quad (2)$$

where $\beta^{\text{ref}} = (\beta_i^{\text{ref}})_{m \times 1}$, $\beta = (\beta_i)_{m \times 1}$.

Proof: First, $k \cdot I - D$ is calculated

$$k \cdot I - D = \begin{bmatrix} k - d_{11} & & & & \\ & \ddots & & & \\ & & k - d_{ii} & & \\ & & & \ddots & \\ & & & & k - d_{mm} \end{bmatrix}. \quad (3)$$

Therefore, $A + (k \cdot I - D)$

$$= \begin{bmatrix} a_{11} + k - d_{11} & \cdots & a_{1i} & \cdots & a_{1m} \\ \vdots & \ddots & \vdots & \vdots & \vdots \\ a_{i1} & \cdots & a_{ii} + k - d_{ii} & \cdots & a_{im} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{m1} & \cdots & a_{mi} & \cdots & a_{mm} + k - d_{mm} \end{bmatrix}. \quad (4)$$

Then, in terms of (2), we can obtain the reference reactive power ratios

$$\begin{aligned} \beta^{\text{ref}} &= (k \cdot I)^{-1} \cdot [A + (k \cdot I - D)] \cdot \beta \\ &= \frac{1}{k} \begin{bmatrix} 1 & & & & \\ & \ddots & & & \\ & & 1 & & \\ & & & \ddots & \\ & & & & 1 \end{bmatrix} \\ &\cdot \begin{bmatrix} a_{11} + k - d_{11} & \cdots & a_{1i} & \cdots & a_{1m} \\ \vdots & \ddots & \vdots & \vdots & \vdots \\ a_{i1} & \cdots & a_{ii} + k - d_{ii} & \cdots & a_{im} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_{m1} & \cdots & a_{mi} & \cdots & a_{mm} + k - d_{mm} \end{bmatrix} \begin{bmatrix} \beta_1 \\ \vdots \\ \beta_i \\ \vdots \\ \beta_m \end{bmatrix}. \end{aligned} \quad (5)$$

According to (5), the concrete formulas for calculating reference reactive power ratios can be obtained

$$\begin{cases} \beta_1^{\text{ref}} = \frac{1}{k}[\beta_1 \cdot (a_{11} + k - d_{11}) + \cdots + \beta_i \cdot a_{1i} + \cdots + \beta_m \cdot a_{1m}], \\ \vdots \\ \beta_i^{\text{ref}} = \frac{1}{k}[\beta_1 \cdot a_{i1} + \cdots + \beta_i \cdot (a_{ii} + k - d_{ii}) + \cdots + \beta_m \cdot a_{im}], \\ \vdots \\ \beta_m^{\text{ref}} = \frac{1}{k}[\beta_1 \cdot a_{m1} + \cdots + \beta_i \cdot a_{mi} + \cdots + \beta_m \cdot (a_{mm} + k - d_{mm})]. \end{cases} \quad (6)$$

Consequently, the reference reactive power outputs $Q^{\text{ref}} =$

$(Q_i^{\text{ref}})_{m \times 1}$ for controllable DGs can be calculated

$$
\begin{cases}
Q_1^{\text{ref}} = \beta_1^{\text{ref}} \cdot Q_1^{\max}, \\
\vdots \\
Q_i^{\text{ref}} = \beta_i^{\text{ref}} \cdot Q_i^{\max}, \\
\vdots \\
Q_m^{\text{ref}} = \beta_m^{\text{ref}} \cdot Q_m^{\max}.
\end{cases}
\tag{7}
$$

It is worth noting that the proportional reactive power sharing is based on reactive power balance, which is ensured by primary droop control. And in this paper, we employ PI controllers to drive reactive power outputs of controllable DGs, $Q = (Q_i)_{m \times 1}$ converges to $Q^{\text{ref}} = (Q_i^{\text{ref}})_{m \times 1}$ gradually [23]. Meanwhile, the reactive power ratios, $\beta = (\beta_i)_{m \times 1}$ also approaches $\beta^{\text{ref}} = (\beta_i^{\text{ref}})_{m \times 1}$. Therefore, in the steady state, from the reactive power sharing schematic in Fig. 2, we have the following expressions

$$
\begin{cases}
\sum_{i=1}^{m} \delta Q_i = \sum_{i=1}^{m} (Q_i^{\text{ref}} - Q_i) = 0, \\
\sum_{i=1}^{m} Q_i^{\text{ref}} = \sum_{i=1}^{m} Q_i, \\
\sum_{i=1}^{m} Q_i^{\max} \cdot \beta_i^{\text{ref}} = \sum_{i=1}^{m} Q_i^{\max} \cdot \beta_i.
\end{cases}
\tag{8}
$$

According to (8), the equations in (9) are satisfied in the steady state

$$
\begin{cases}
\beta_1^{\text{ref}} = \beta_1, \\
\vdots \\
\beta_i^{\text{ref}} = \beta_i, \\
\vdots \\
\beta_m^{\text{ref}} = \beta_m.
\end{cases}
\tag{9}
$$

Therefore, applying conditions (9) to (6), we have the following equation set

$$
\begin{cases}
\frac{1}{k}[\beta_1 \cdot (a_{11} + k - d_{11}) + \cdots + \beta_i \cdot a_{1i} + \cdots + \beta_m \cdot a_{1m}] = \beta_1, \\
\vdots \\
\frac{1}{k}[\beta_1 \cdot a_{i1} + \cdots + \beta_i \cdot (a_{ii} + k - d_{ii}) + \cdots + \beta_m \cdot a_{im}] = \beta_i, \\
\vdots \\
\frac{1}{k}[\beta_1 \cdot a_{m1} + \cdots + \beta_i \cdot a_{mi} + \cdots + \beta_m \cdot (a_{mm} + k - d_{mm})] = \beta_m.
\end{cases}
\tag{10}
$$

Moreover, the expressions in (10) can be simplified as

$$
\begin{cases}
\beta_1 \cdot (a_{11} - d_{11}) + \cdots + \beta_i \cdot a_{1i} + \cdots + \beta_m \cdot a_{1m} = 0, \\
\vdots \\
\beta_1 \cdot a_{i1} + \cdots + \beta_i \cdot (a_{ii} - d_{ii}) + \cdots + \beta_m \cdot a_{im} = 0, \\
\vdots \\
\beta_1 \cdot a_{m1} + \cdots + \beta_i \cdot a_{mi} + \cdots + \beta_m \cdot (a_{mm} - d_{mm}) = 0.
\end{cases}
\tag{11}
$$

And the determinant for the coefficient matrix B of (11) is obtained as follows,

$$
|B| =
\begin{vmatrix}
a_{11} - d_{11} & \cdots & a_{1i} & \cdots & a_{1m} \\
\vdots & \ddots & \vdots & \vdots & \vdots \\
a_{i1} & \cdots & a_{ii} - d_{ii} & \cdots & a_{im} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
a_{m1} & \cdots & a_{mi} & \cdots & a_{mm} - d_{mm}
\end{vmatrix}.
\tag{12}
$$

Furthermore, according to graph theory, for the i-th row of the adjacency matrix A, the sum of all elements in the row vector equals the outdegree of Agent$_i$, therefore, the following equation is obtained

$$
\sum_{j=1}^{m} a_{ij} = d_{ii}.
\tag{13}
$$

Applying condition (13) to (12), it yields the following equation

$$
|B| = 0.
\tag{14}
$$

In terms of (14), there exist non-zero solutions for the equation set in (11). In order to obtain non-zero solutions for (11), the rank of the coefficient matrix B is calculated first, which is equal to that of B^T. In other words, we have

$$
R(B) = R(B^T) = R
\begin{bmatrix}
a_{11} - d_{11} & \cdots & a_{i1} & \cdots & a_{m1} \\
\vdots & \ddots & \vdots & \vdots & \vdots \\
a_{1i} & \cdots & a_{ii} - d_{ii} & \cdots & a_{mi} \\
\vdots & \vdots & \vdots & \ddots & \vdots \\
a_{1m} & \cdots & a_{im} & \cdots & a_{mm} - d_{mm}
\end{bmatrix}.
\tag{15}
$$

Applying condition (13) to (15), the rank of the coefficient matrix B is obtained

$$
R(B) = R(B^T) = m - 1.
\tag{16}
$$

And the equation (16) denotes that the basic solutions for (11) simply have one solution vector. Moreover, we know that $m \times 1$ unit column vector is one of non-zero solutions for (11), therefore, the $m \times 1$ unit column vector is the basic solution for (11). Finally, we obtain general solutions for equation set in (11) as follows,

$$
\begin{bmatrix} \beta_1 \\ \vdots \\ \beta_i \\ \vdots \\ \beta_m \end{bmatrix} = k \cdot \begin{bmatrix} 1 \\ \vdots \\ 1 \\ \vdots \\ 1 \end{bmatrix}.
\tag{17}
$$

where $0 \le k \le 1$.

Therefore,

$$
\beta_1 = \cdots = \beta_i \cdots = \beta_m = k.
\tag{18}
$$

That is, the theorem is proved. ∎

IV. MICROGRID SYSTEM ARCHITECTURE

In this section, the setup of the islanded MG under test is introduced first. Later, in terms of the theorem, two sets of control laws are derived from two different communication networks shown in Fig. 1.

A. MG Structure

Fig. 3 illustrates the single-line diagram of the MG test system, which is established in MATLAB/Simulink, and used to verify the effectiveness of the proposed control model. The MG is composed of 10 DGs, namely $n = 10$, and the specifications of loads and capacities of DGs are listed in Fig. 3. Here, DG_1 and DG_3 are PVs, while DG_6, DG_8 and DG_9 are permanent magnet synchronous generator (PMSG) based wind turbines, all of which work in maximum power point tracking (MPPT) control mode, and they produce no reactive power, that is $Q_1 = Q_3 = Q_6 = Q_8 = Q_9 = 0$. Additionally, the dc-links of controllable DGs, e.g., micro gas turbine, are modeled as constant dc voltage sources V_{dc}, and we assume that the voltage variations of dc-links are well regulated. Furthermore, controllable DGs are all operate in the manner of droop control.
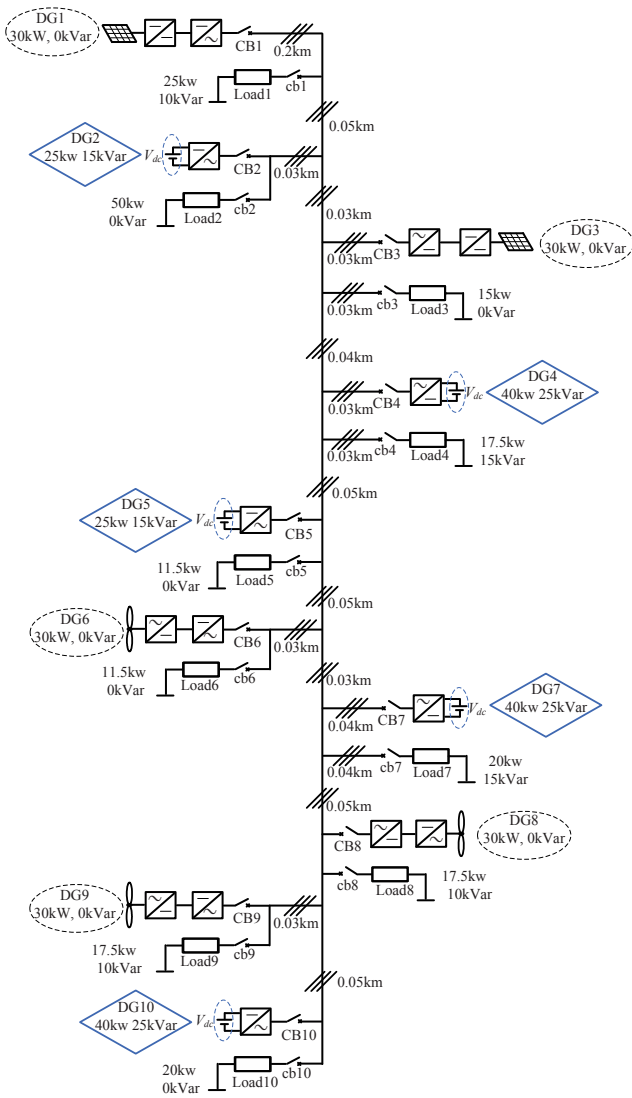

Fig. 3. Schematic diagram of an islanded MG with radial structure.

As discussed in Section III, PI controllers are adopted to drive reactive power outputs of controllable DGs to references. Therefore, according to critical ratio method, the proportional gains of PI controllers are reasonably chosen so that controllers

	MG Setup	
V_{dc}	DC voltage	800 V
C	Filter capacitance	4 mH
L	Filter inductance	8 μF
	Primary droop Control	
$m2$, $m5$	$P - \omega$ coefficients for DG_2, DG_5	1.01e-4 W/rd.s
$m4$, $m7$, $m10$	$P - \omega$ coefficients for DG_4, DG_7, DG_{10}	6.28e-5 W/rd.s
$n2$, $n5$	$Q - E$ coefficients for DG_2, DG_5	9.42e-4 VAr/V
$n4$, $n7$, $n10$	$Q - E$ coefficients for DG_4, DG_7, DG_{10}	5.65e-4 VAr/V
	Reactive Power Sharing	
k_{PQ}	Proportional gain	0.000002 VAr/V
k_{iQ}	Integral gain	0.005 VAr/Vs
upper, lower	Saturation limits of PI controllers	5, -5

respond quickly to changes, while the stability of the MG is guaranteed. The integral gains, on the other hand, ought to be set high enough to eliminate steady state errors, and avoid excessive overshoots. Moreover, the saturation limits of PI controllers ensure that the reactive power correction term δQ does not affect the stability of the MG. In addition, specifications of the control model are summarized in Table I.

Furthermore, in order to remove deviations in voltage and frequency, the distributed secondary control is carried out to recover voltage and frequency to their nominal values of 380 V and 50 Hz [41], respectively. And the distributed secondary control is elaborated in [23], hence it is not discussed further here. In the MG, the line impedance is also considered, which is set at $0.642 + j0.083$ Ω/km.

Meanwhile, the MG system initially works in a balanced state, and sample time is 1ms. And it is worth noting that the proposed control model can also be implemented with asynchronous communication, where no communication is needed, if the data remains unchanged. However, if updated data is received, agents will recalculate the set points for controllable DGs. In this manner, the sample time can be longer.

B. Control Laws from Given Communication Networks

According to the theorem, a set of control laws can be derived from communication network 1 and network 2, respectively, named here the control laws I and II. In order to obtain control laws I, the adjacency matrix A_1, outdegree matrix D_1, and the parameter k_1 for communication network 1 can be obtained as follows,

$$A_1 = \begin{bmatrix} 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 & 1 \end{bmatrix}, D_1 = k_1 \cdot I = \begin{bmatrix} 3 & 0 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 & 0 \\ 0 & 0 & 3 & 0 & 0 \\ 0 & 0 & 0 & 3 & 0 \\ 0 & 0 & 0 & 0 & 3 \end{bmatrix}. \tag{19}$$

Therefore,

$$(k_1 \cdot I)^{-1} \cdot [A_1 + (k_1 \cdot I - D_1)] = \frac{1}{3} \begin{bmatrix} 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 & 1 \end{bmatrix}. \tag{20}$$

And then in terms of the theorem, we can obtain the control laws I for calculating reference reactive power ratios, which take the following forms,

$$\beta_1^{\mathrm{ref}} = \frac{1}{3}\beta_1 + \frac{1}{3}\beta_2 + \frac{1}{3}\beta_5, \tag{21}$$

$$\beta_2^{\mathrm{ref}} = \frac{1}{3}\beta_1 + \frac{1}{3}\beta_2 + \frac{1}{3}\beta_3, \tag{22}$$

$$\beta_3^{\mathrm{ref}} = \frac{1}{3}\beta_2 + \frac{1}{3}\beta_3 + \frac{1}{3}\beta_4, \tag{23}$$

$$\beta_4^{\mathrm{ref}} = \frac{1}{3}\beta_3 + \frac{1}{3}\beta_4 + \frac{1}{3}\beta_5, \tag{24}$$

$$\beta_5^{\mathrm{ref}} = \frac{1}{3}\beta_1 + \frac{1}{3}\beta_4 + \frac{1}{3}\beta_5. \tag{25}$$

Consequently, the reference reactive power outputs for controllable DGs, DG_2, DG_4, DG_5, DG_7, DG_{10} can be calculated

$$Q_2^{\mathrm{ref}} = \beta_1^{\mathrm{ref}} \cdot Q_2^{\mathrm{max}}, \tag{26}$$

$$Q_4^{\mathrm{ref}} = \beta_2^{\mathrm{ref}} \cdot Q_4^{\mathrm{max}}, \tag{27}$$

$$Q_5^{\mathrm{ref}} = \beta_3^{\mathrm{ref}} \cdot Q_5^{\mathrm{max}}, \tag{28}$$

$$Q_7^{\mathrm{ref}} = \beta_4^{\mathrm{ref}} \cdot Q_7^{\mathrm{max}}, \tag{29}$$

$$Q_{10}^{\mathrm{ref}} = \beta_5^{\mathrm{ref}} \cdot Q_{10}^{\mathrm{max}}. \tag{30}$$

Similarly, the control laws II for communication network 2 are obtained, after A_2, D_2, and $k_2 \cdot I$ are calculated

$$A_2 = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 \end{bmatrix}, D_2 = \begin{bmatrix} 2 & 0 & 0 & 0 & 0 \\ 0 & 3 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 0 & 4 \end{bmatrix}, \tag{31}$$

$$k_2 \cdot I = \begin{bmatrix} 4 & 0 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 & 0 \\ 0 & 0 & 4 & 0 & 0 \\ 0 & 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 0 & 4 \end{bmatrix}. \tag{32}$$

Hence, in terms of the theorem, the control laws II for calculating reference reactive power ratios are obtained

$$\beta_1^{\mathrm{ref}} = \frac{3}{4}\beta_1 + \frac{1}{4}\beta_5, \tag{33}$$

$$\beta_2^{\mathrm{ref}} = \frac{1}{2}\beta_2 + \frac{1}{4}\beta_3 + \frac{1}{4}\beta_5, \tag{34}$$

$$\beta_3^{\mathrm{ref}} = \frac{1}{4}\beta_2 + \frac{3}{4}\beta_3, \tag{35}$$

$$\beta_4^{\mathrm{ref}} = \frac{3}{4}\beta_4 + \frac{1}{4}\beta_5, \tag{36}$$

$$\beta_5^{\mathrm{ref}} = \frac{1}{4}\beta_1 + \frac{1}{4}\beta_2 + \frac{1}{4}\beta_4 + \frac{1}{4}\beta_5. \tag{37}$$
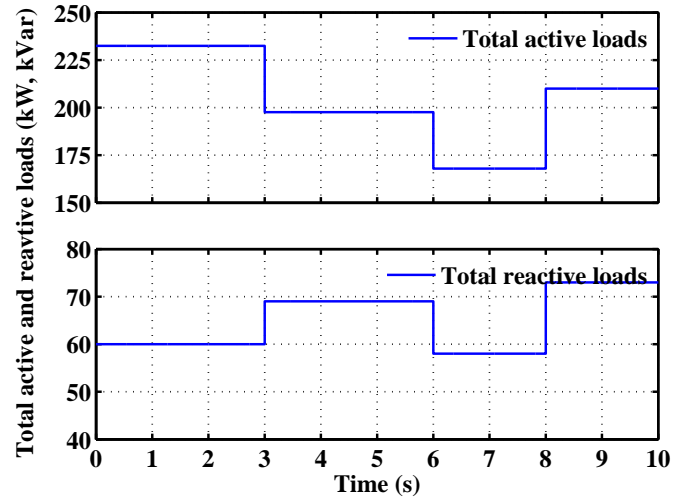
V. Results

In this section, three cases are designed to evaluate the performance of the control model, when both active power outputs of intermittent DGs and load demands change at the same time. Case 1 focuses on the effectiveness of the control model in reactive power sharing. Further, the impacts of time delays on reactive power sharing are investigated in case 2.
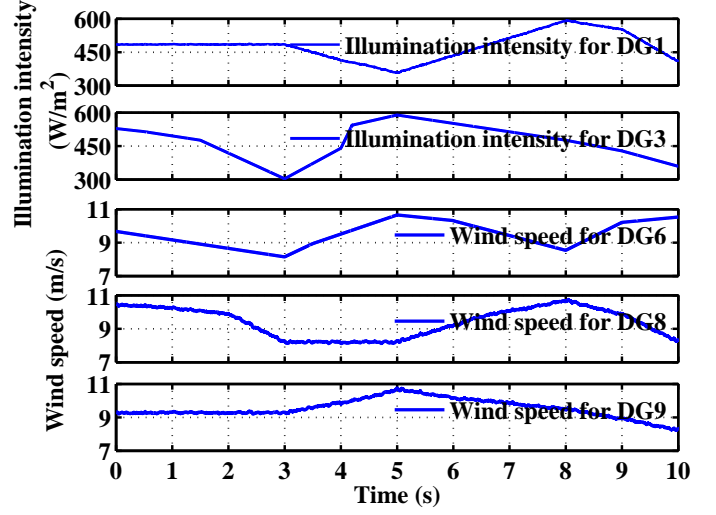
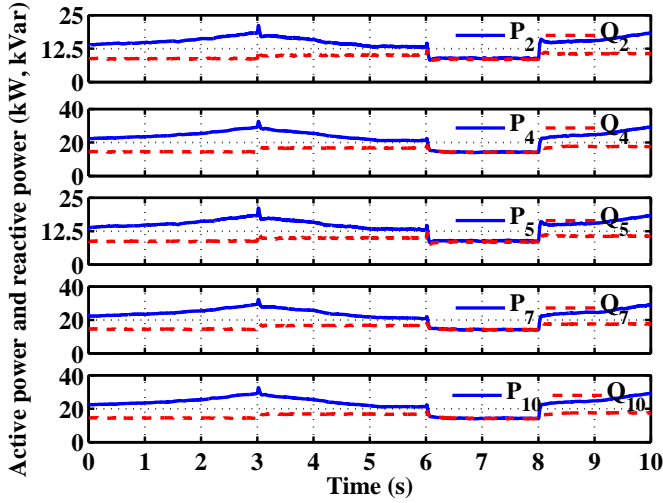(a) the illumination intensity and wind speed.
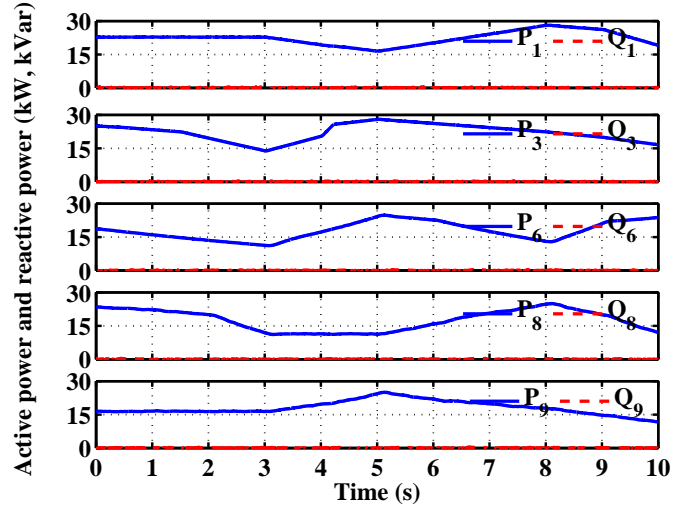
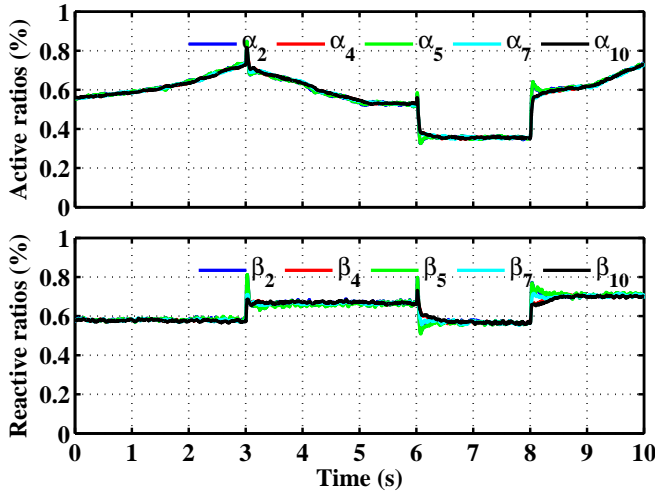(b) power outputs of intermittent DGs.

(c) load changes over time.

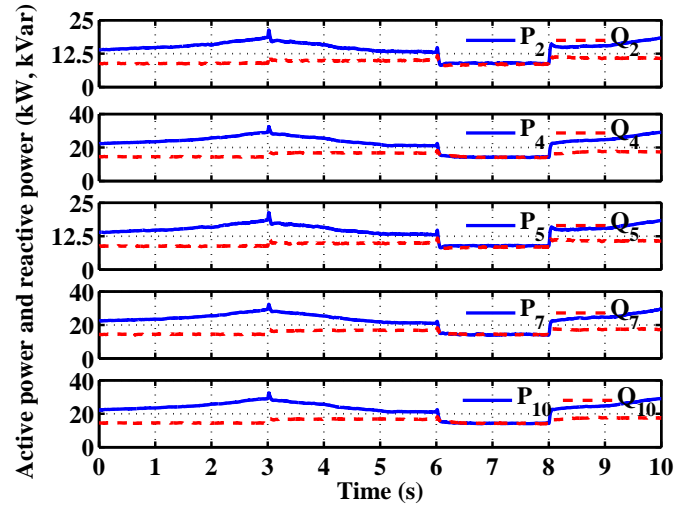Fig. 4. Power outputs of intermittent DGs and load demands in the MG.
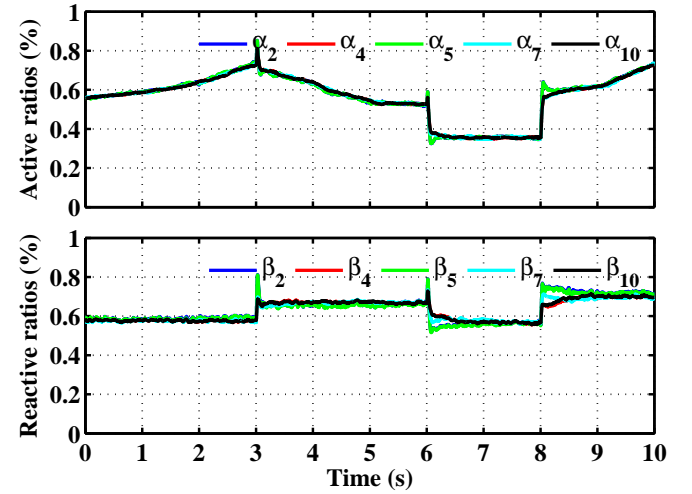
(a) power outputs of controllable DGs.

(b) power ratios of controllable DGs.

Fig. 5. Case 1: Simulation results under the control laws I, when both the environmental conditions and load demands change simultaneously.

(a) power outputs of controllable DGs.

(b) power ratios of controllable DGs.

Fig. 6. Case 1: Simulation results under the control laws II, when both the environmental conditions and load demands change simultaneously.

Later, in case 3, the capability of plug and play is verified. Finally, the results are discussed and explained in detail.

For these three cases, the active power outputs of intermittent DG_1, DG_3, DG_6, DG_8 and DG_9 change between 10 kW to 30 kW, due to the fluctuations of illumination intensity for DG_1, DG_3, and wind speed for DG_6, DG_8 and DG_9, as shown in Fig. 4(a), while the active power outputs of DG_1, DG_3, DG_6, DG_8 and DG_9 are illustrated in Fig. 4(b).

Furthermore, the load demands also change over time and are scheduled as follows,

- $t = 3$ s: active loads decrease by 15% and reactive loads increase by 15%;
- $t = 6$ s: both active and reactive loads decrease by 15%;
- $t = 8$ s: both active and reactive loads increase by 25%,

where the fluctuations of total active and reactive loads are illustrated in Fig. 4(c).

A. Case 1: Reactive Power Sharing

In this case, the control laws I and laws II are used respectively, to investigate whether the control model achieves the proportional power sharing among controllable DGs, when both environmental conditions and the load demands change at the same time.

First, the control laws I are utilized, according to the topology of communication network 1 shown in Fig. 1, $Agent_1$, $Agent_2$, $Agent_3$, $Agent_4$ and $Agent_5$ collect the information of reactive power outputs of controllable DGs to which they connect, $Q_i, i = 2, 4, 5, 7, 10$, respectively. After that, the reactive power ratios can be calculated and are exchanged among neighboring agents. Receiving the information of neighbors, the reference reactive power ratios, $\beta_i^{ref}, i = 1, 2, 3, 4, 5$ are calculated according to control laws from (21) to (25), respectively. Thereafter, the reference reactive power outputs for controllable DGs, $Q_i^{ref}, i = 2, 4, 5, 7, 10$ are obtained in terms of equations
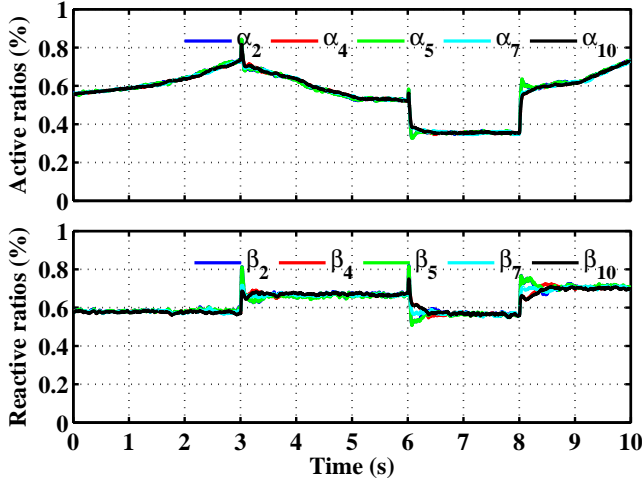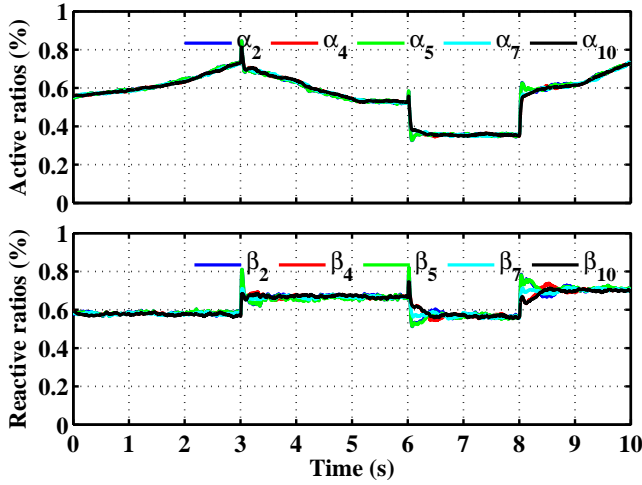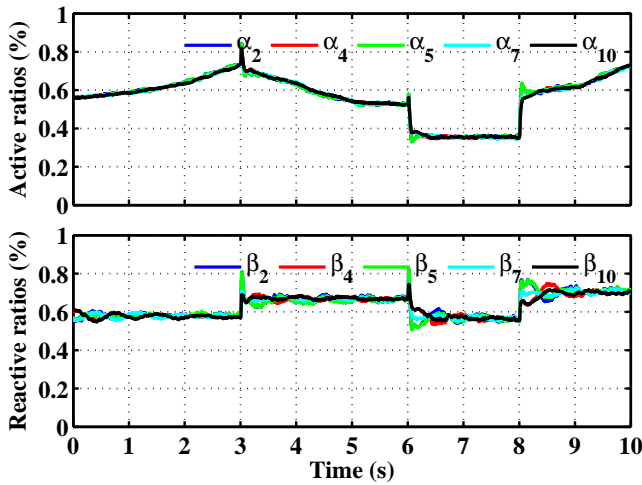
(a) $t_d = 0.08$ s.

(b) $t_d = 0.1$ s.

(c) $t_d = 0.12$ s.

Fig. 7. Case 2: Simulation results under the control laws I when time delays t_d are involved, and both the environmental conditions and load demands change over time.

from (26) to (30), respectively.

Consequently, the reference reactive power outputs are compared with measured values, respectively. Moreover, the errors between references and measured values are fed to PI controllers, and the produced reactive power correction terms, $\delta Q_i, i = 1, 2, 3, 4, 5$ are sent to controllable DGs to regulate their reactive power outputs, allowing reactive power outputs converge to references gradually. Meanwhile, the reactive power ratios also approach references, respectively. Therefore, it can be found in Fig. 5(a) and Fig. 5(b) that the load demands are shared proportionately among controllable DGs, and power ratios stay the same regardless of variations in load demands.

In addition, it can be found in Fig. 1 that each agent exchanges the information with two neighbors in network 1. However, in network 2, Agent$_1$, Agent$_3$ and Agent$_4$ simply have one neighbor, and Agent$_5$ exchanges the information with three neighbors. On the other hand, according to the discussion in Section II B, many possible communication networks can be considered for a given MG, and each communication network possesses a set of control laws, moreover, the control laws derived from different communication networks are supposed to have the similar performance. In order to verify the feasibility of the communication network 2, the control laws II derived from communication network 2 are used, and the simulation results are drawn in Fig. 6, which are similar to those that obtained under the control laws I. Therefore, the simulation results are consistent with the discussion. However, how the topology affects the performance of the control model requires further investigation.

B. Case 2: Impacts of Time Delays

As is known, the time delays on the communication network may possibly result in performance deterioration or even instability of the MG system. Therefore, in order to examine the impacts of time delays, the control laws I are adopted, and fixed time delays are taken into account on the communication among agents at each sample time, when both active power outputs of intermittent DGs and load demands fluctuate simultaneously.

Furthermore, Fig. 7 displays the effects of communication delays on reactive power sharing performance, when three fixed time delays t_d are employed, namely $t_d = 0.08$, 0.1 and 0.12 s, respectively. From Fig. 7(a) and Fig. 7(b), it can be seen that the control model is robust with time delays of $t_d = 0.08$ and 0.1 s. However, comparing with Fig. 7(a) and Fig. 7(c), it can be observed that the system dynamic has slowed down, when longer time delays are involved, because the control laws are calculated using lagged information from neighboring agents, when time delays are involved.

C. Case 3: Plug and Play Capability

In this case, both the active power outputs of intermittent DGs and load demands change at the same time, and the control laws II for communication network 2 are utilized. Note that controllable DGs have already reached the steady states before the plug out of controllable DG$_5$. At $t = 4$ s, the controllable DG$_5$ is disconnected from the MG, and
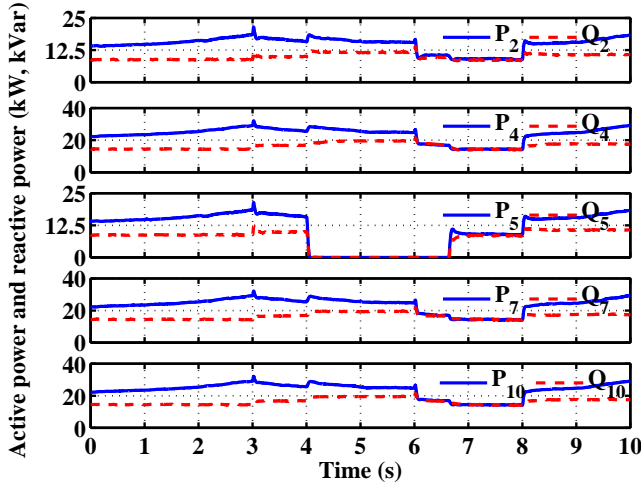
(a) power outputs of controllable DGs.
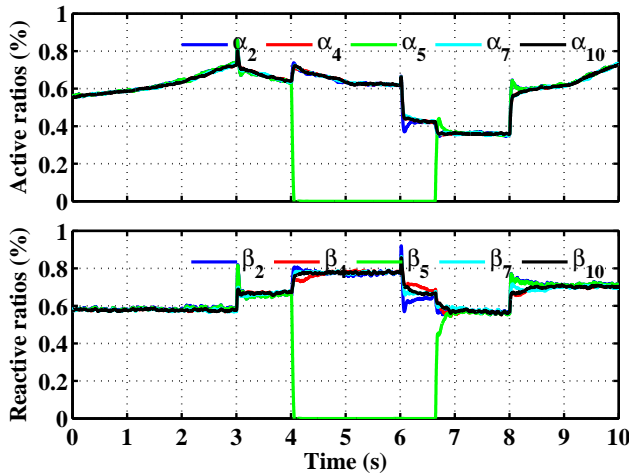
(b) power ratios of controllable DGs.
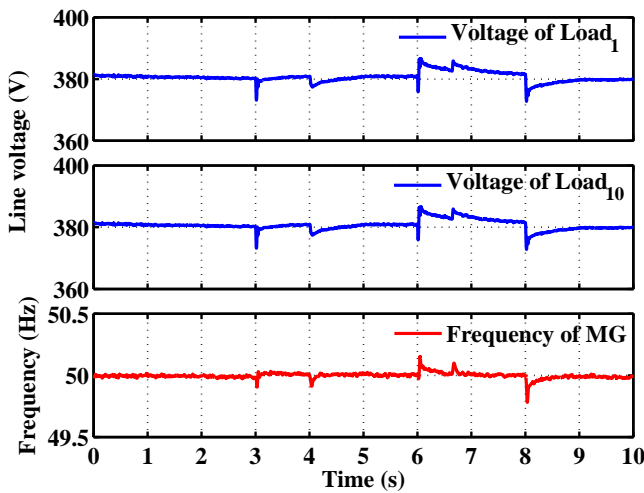
(c) frequency and line voltages in the MG.

Fig. 8. Case 3: Simulation results under the plug and play of DG$_5$, when the control laws II are used, and the active power outputs of intermittent DGs and load demands fluctuate simultaneously.

corresponding Agent$_3$, and associated communication links are excluded from the communication network, as shown in Fig. 9. With the consideration of power mismatch under new situations, the remaining controllable DGs produce more power to compensate for the amount of power previously generated by DG$_5$, as shown in Fig. 8(a). Therefore, there are increases in power ratios with increasing power outputs, while those of DG$_5$ drop to zero during the plug out, as illustrated in Fig. 8(b), because the information of DG$_5$ is not available to the agents.

Moreover, it can be found from Fig. 9 that the plug out of Agent$_3$ does not hinder the graphical connectivity of the communication network. In other words, there are no isolated agents on the communication network, and the remaining communication network allows communication among agents, which is identified as an essential ingredient for reactive power sharing. Therefore, after the plug out of DG$_5$ and Agent$_3$, agents calculate reference reactive power ratios, in terms of concrete formulas of control laws in (6), which take the following forms

$$\beta_1^{\text{ref}} = \frac{3}{4}\beta_1 + \frac{1}{4}\beta_5, \tag{38}$$

$$\beta_2^{\text{ref}} = \frac{3}{4}\beta_2 + \frac{1}{4}\beta_5, \tag{39}$$

$$\beta_3^{\text{ref}} = \beta_3, \tag{40}$$

$$\beta_4^{\text{ref}} = \frac{3}{4}\beta_4 + \frac{1}{4}\beta_5, \tag{41}$$

$$\beta_5^{\text{ref}} = \frac{1}{4}\beta_1 + \frac{1}{4}\beta_2 + \frac{1}{4}\beta_4 + \frac{1}{4}\beta_5. \tag{42}$$

Thereafter, the reference reactive power outputs for controllable DGs can be calculated, in terms of the equations from (26) to (30). Finally, according to the references, agents adjust the reactive power outputs of controllable DGs, for the purpose of proportional reactive power sharing, and the power ratios are illustrated in Fig. 8(b).

Furthermore, at $t = 6$ s, the synchronization strategy is activated and the seamless plug in of DG$_5$ into the MG is achieved at $t = 6.5$ s, and the corresponding Agent$_3$ is reconnected to the communication network simultaneously. Similarly, in terms of (6), the control laws under the new situations are derived and implemented, which are identical to the control laws II. Moreover, it can be seen in Fig. 8(b) that despite plug out and plug in operations of DG$_5$ and Agent$_3$, the control laws quickly drive the power ratios to equal values. That is, the capability of the control model to meet the requirement of plug and play operation is verified.

On the other hand, Fig. 8(c) shows that frequency stays around nominal value, namely 50 Hz, in all situations, and line voltages at the head and the tail of the bus, which are represented by voltages of Load$_1$ and Load$_{10}$ respectively, are still in a normal range, as shown in Fig. 8(c), even if large fluctuations in load demands occur at $t = 3$ s, 6 s and 8 s, which satisfy IEEE Standard 1547 requirements [42].

VI. CONCLUSION

Regarding to reactive power sharing in an islanded droop-controlled MG, an MAS based two-layer control model is
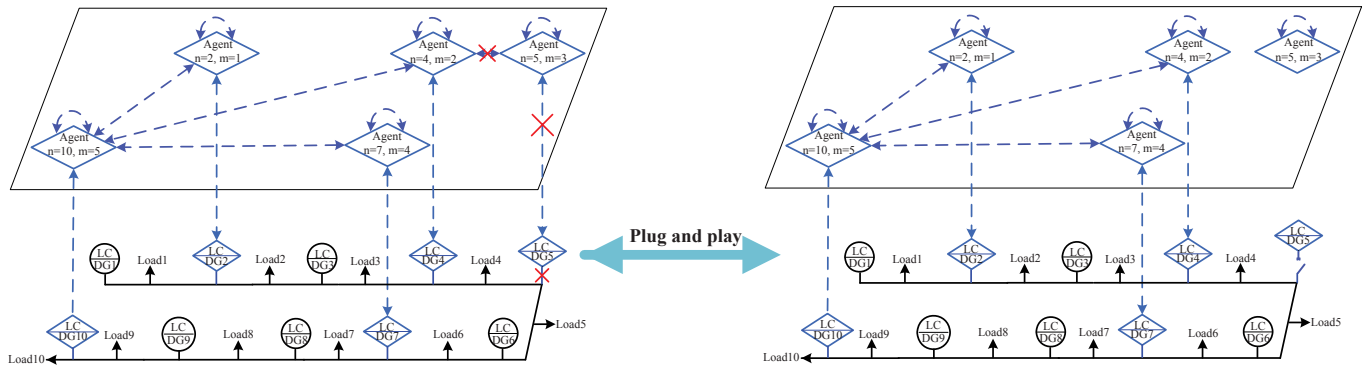
Fig. 9. The plug and play of DG_5 and $Agent_3$.

proposed in this paper. The bottom layer of the control model is the electrical distribution MG, while the top layer is a communication network composed of agents. In the control model, agents collect the information of reactive power ratios locally, and then agents process the acquired information in terms of the control laws. Moreover, a theorem is demonstrated for deriving the distributed control laws from a given communication network. Therefore, the reference reactive power outputs for controllable DGs can be calculated conveniently. Thereafter, agents send references to controllable DGs they connect to, to regulate their reactive power outputs, with the aim of proportional power sharing.

In order to evaluate the performance of the control model, three simulations cases are carried out and the results show that all controllable DGs have almost the same reactive power ratios, when the control laws are utilized, i.e., the proportional power sharing is achieved. Furthermore, the plug out and plug in behaviors of the controllable DG almost do not affect the power sharing performance, due to the plug and play capability of the control model.

For our future work, how the package loss, failure and topology affect the performance of the control model is also an open question for further investigation.

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