

Multiferroic oxide thin films and heterostructures

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APPLIED PHYSICS REVIEWS

Multiferroic oxide thin films and heterostructures

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Multiferroic materials promise a tantalizing perspective of novel applications in next-generation electronic, memory, and energy harvesting technologies, and at the same time they also represent a grand scientific challenge on understanding complex solid state systems with strong correlations between multiple degrees of freedom. In this review, we highlight the opportunities and obstacles in growing multiferroic thin films with chemical and structural integrity and integrating them in functional devices. Besides the magnetoelectric effect, multiferroics exhibit excellent resistant switching and photovoltaic properties, and there are plenty opportunities for them to integrate with other ferromagnetic and superconducting materials. The challenges include, but not limited, defect-related leakage in thin films, weak magnetism, and poor control on interface coupling. Although our focuses are Bi-based perovskites and rare earth manganites, the insights are also applicable to other multiferroic materials. We will also review some examples of multiferroic applications in spintronics, memory, and photovoltaic devices. © 2015 AIP Publishing LLC.

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II. MULTIFERROIC OXIDE THIN FILMS	4	I. INTRODUCTION	
A. Bi-containing multiferroic thin films	4	A. General overview of multiferroic materials	
1. BiFeO ₃	4	The terminology of multiferroics refers to materials where two or more ferroic orders such as ferroelectricity, (anti-)ferromagnetism, and ferroelasticity co-exist. More importantly, the strong coupling between multiple ferroic orders can produce additional functionalities, in particular, the magnetoelectric (ME) effect, which enables the control of electric polarization by a magnetic field and the control of magnetization by an electric field. Therefore, the enthusiastic endeavors on multiferroics have been motivated by not only the rich physics underlying the intricate spin-charge ordering in these materials but also their promising potential applications for future multifunctional computing and memory devices. ¹⁻⁴	
2. BiMnO ₃ (BMO)	4	Research on the magnetoelectric effect can be traced back to the work by Dzyaloshinskii on Cr ₂ O ₃ in 1960s. ⁵ Within the next decade, there were some studies on the bulk composites of magnetostrictive ferrites and piezoelectric barium titanate. ⁶ However, the research was halted for a number of years because the observed ME coupling was quite weak. Since 2003, the discoveries of spin-dependent multiferroicity and strong ME effect in TbMnO ₃ (TMO) ⁷ and the	
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coexistence of magnetism and excellent ferroelectricity in BiFeO₃ (BFO)⁸ have boosted great interest in multiferroic materials. Up to date, over ten different multiferroic material families have been extensively investigated, including the rare-earth manganates and the well-known BFO. Broadly speaking, these materials can be divided into single phase multiferroics with widely separated ferroelectric and magnetic ordering temperatures (type I multiferroic), single phase multiferroics having a magnetic transition with concurrent ferroelectric ordering (type II multiferroic), and composite multiferroics formed by distinct but coupled ferromagnetic (FM) and ferroelectric (FE) components.⁹ However, most of the single-phase multiferroics reported so far are antiferromagnets without spontaneous magnetization, and generally their Curie or Néel temperatures are far below the room temperature, diminishing their chance of practical applications.

The scarcity of multiferroic materials stems from the fact that magnetism requires unpaired d^n cations, while ferroelectricity exists almost exclusively in d^0 compounds.¹⁰ This intrinsic constraint has invited lots of efforts on searching new multiferroics as well as on developing relevant theoretical models. This research thrust has witnessed many synergetic collaborations between experimentalist and theorists, and in many cases the modern advancements of first-principles calculations help to shed light on the physics of multiferroics.¹¹

B. Synthesis of multiferroic thin films and strain engineering

It is not an exaggeration to say, that the research on multiferroic thin films was enabled by the developments of state-of-the-art thin film deposition tools. With careful tuning of synthesis conditions, the multiferroic properties of thin films could be enhanced compared to those of the bulk counterparts. For example, BFO was extensively investigated in 1960s, but its spontaneous polarization was revealed to be just few micro-Coulombs per square centimeter, owing to the leakage problems associated with the low crystal quality.^{12–14} This issue was eventually solved by high-quality thin film growth using pulsed laser deposition (PLD) in 2003, which is one of the milestones in the field of multiferroics.⁸

Successful thin film growth is the foundation of almost all device applications, but it introduces extrinsic complications such as substrate strain, surface states, impurity phases, structural defects, and so on. For example, excessive leakage current may compromise the measurement of ferroelectricity; surfaces and interfaces may introduce spin canting, which compromises magnetism. Thus, it is important to secure strategies of retaining or even improving the multiferroic properties in thin films.

Various state-of-art physical deposition techniques, such as PLD, molecular beam epitaxy (MBE), and sputtering, and chemical synthesis routes, such as sol gel spin coating and metal-organic chemical vapor deposition (MOCVD), have been utilized to prepare multiferroic thin films. PLD is a physical vapor deposition method that is widely used in the research community, particularly for investigating new

materials and novel heterostructures. An intrinsic advantage of PLD technique is that the growth process takes place far from equilibrium and hence it is good at preserving complex stoichiometry, which is especially important for the growth of multi-element compounds. Moreover, being equipped with *in-situ* reflection high-energy electron diffraction (RHEED), PLD enables the precise control of film thickness on the unit cell level,¹⁵ which is critical for the synthesis of high-quality epitaxial thin films. In contrast to PLD, MBE involves the generation of thermal atomic beams with very low energy (~ 1 eV), which is quite suitable to prepare extremely pure and defect free thin films of multiferroics and other complex oxides.¹⁶ Although PLD and MBE are capable to produce high quality films, such processes are challenging to scale up to large-area wafers. Sputtering, on the other hand, is a widely used deposition techniques for large-scale production, including magnetron sputtering, ion-beam sputtering, and off-axis sputtering.¹⁷ Precise control of reactive gas, especially the O₂ or Ar/O₂ mixtures, is crucial for synthesizing high-quality oxide thin films with desired oxygen stoichiometry. Different from the vapor-based methods, sol gel spin coating is a convenient and inexpensive chemical process to fabricate thin films with large areas and low costs. However, the obtained films are usually in the polycrystal or textured structures, and it is often hard to tune the sample thickness and morphology. Finally, MOCVD has been routinely used in the electronics industry, which offers promising potential for the deposition of multiferroic films due to several advantages, such as excellent film uniformity over large areas, relatively high deposition rates, and compatibility with modern integrated circuit technologies,¹⁸ but there are limited metal-organic sources for growing complex oxides. More information on the growth of ferroelectric and multiferroic oxide thin films can be found in a few recent reviews.^{18,19}

Selecting suitable substrates is often the first step for the thin film synthesis. The crystal structure and lattice parameters of several widely studied multiferroic materials and some typical substrates are listed in Table I. On the one hand, good lattice match between film and substrate is a prerequisite for growing smooth films with controlled low-density structural defects. On the other hand, strain (either tensile or compressive) engineering is an effective tool to induce lattice distortion and to optimize physical properties.²⁰

Strain engineering, in fact, is a general strategy often employed in semiconductor industry to increase the carrier mobility in the transistor channel and to enhance device performance. For example, capping layers of CVD silicon nitride are used to induce either compressive strain or tensile strain to improve the channel transport. Other methods like growing epitaxial silicon on silicon-germanium underlayer are also adapted to modulate the channel strain. It has been reported for ferroelectric oxides that strain engineering can lead to sizable increases of spontaneous polarization and Curie temperature.²¹ Similarly, the properties of epitaxial multiferroic thin films can be engineered by substrate-induced strain. Strain engineering has been extensively exploited for BFO thin films. One of the most notable examples is the strain induced tetragonal BFO phase which possesses giant c/a ratio (> 1.25) and

TABLE I. Lattice parameters and crystal structure of several typical multiferroics and substrates.^{29–36}

Compound	Crystal structure	Lattice parameters
BiFeO ₃	Rhombohedral	$a = 3.965 \text{ \AA}$
BiMnO ₃	Triclinic	$a = b = 3.935 \text{ \AA}, c = 3.989 \text{ \AA}$
BiCrO ₃	Triclinic	$a = b = 3.90 \text{ \AA}, c = 3.87 \text{ \AA}$
YMnO ₃	Hexagonal	$a = 6.13 \text{ \AA}, c = 11.4 \text{ \AA}$
TbMnO ₃	Orthorhombic	$a = 5.2418 \text{ \AA}, b = 5.8029 \text{ \AA}, c = 7.3643 \text{ \AA}$
DyMnO ₃	Orthorhombic	$a = 5.2931 \text{ \AA}, b = 5.8384 \text{ \AA}, c = 7.4025 \text{ \AA}$
LuMnO ₃	Orthorhombic	$a = 5.2785 \text{ \AA}, b = 5.8337 \text{ \AA}, c = 7.3778 \text{ \AA}$
LuMnO ₃	Orthorhombic	$a = 5.1984 \text{ \AA}, b = 5.7845 \text{ \AA}, c = 7.2994 \text{ \AA}$
Substrate		
SrTiO ₃	Cubic	$a = 3.905 \text{ \AA}$
LaAlO ₃	Pseudocubic	$a = 3.792 \text{ \AA}$
(LaAlO ₃) _{0.3} (LaSr ₂ TaO ₆) _{0.7}	Tetragonal	$a = 3.868 \text{ \AA}$
LaSrAlO ₄	Tetragonal	$a = 3.754 \text{ \AA}, c = 11.263 \text{ \AA}$
LaSrGaO ₄	Tetragonal	$a = 3.84 \text{ \AA}, c = 12.676 \text{ \AA}$
NdScO ₃	Orthorhombic	$a = 5.777 \text{ \AA}, b = 5.577 \text{ \AA}, c = 8.005 \text{ \AA}$
YAlO ₃	Orthorhombic	$a = 5.18 \text{ \AA}, b = 5.33 \text{ \AA}, c = 7.37 \text{ \AA}$
NdGaO ₃	Orthorhombic	$a = 5.417 \text{ \AA}, b = 5.499 \text{ \AA}, c = 7.717 \text{ \AA}$
DyScO ₃	Orthorhombic	$a = 5.54 \text{ \AA}, b = 5.71 \text{ \AA}, c = 7.89 \text{ \AA}$

spontaneous polarization up to $150 \mu\text{C}/\text{cm}$.^{2,22–25} Since the tetragonal BFO was identified in 2009,²² significant progresses have been achieved on the related research.²⁶ One impressive feature of this tetragonal phase BFO is the reversible control of its crystalline structure between rhombohedra and tetragonal using an electric field, which provides the possibility of making nanoscale shape-memory devices.²⁷ While tetragonal BFO has been intensively addressed, orthorhombic BFO has also attracted lots of interest due to its interesting physical properties.²⁸

Strain can significantly alter the phase diagrams of oxides with strong correlations between multiple degrees of freedom. For example, in systems with strong spin-phonon coupling, if the lowest-frequency polar phonon is softer for ferromagnetic ordering than for antiferromagnetic (AFM) ordering, then strain may induce a polar instability and trigger transition from the antiferromagnetic-paraelectric state to the ferromagnetic-ferroelectric state. This strain-induced multiferroic state was proposed for SrMnO₃ based on the results of first-principle calculations, encouraging experimental efforts to explore thin films of materials with strong spin-phonon coupling.³⁷

C. Structure of the review

In Sec. I, we have given a general overview of multiferroics and briefly reviewed the aspects of thin film growth and strain engineering. The main aim of this review is to discuss the most recent works on multiferroic thin films and devices, with a focus on the perspective of novel applications. In spite of recent progresses, growing thin films with retained or improved multiferroic functionalities remains as a challenge and presents opportunities of breakthroughs at the same time.^{38–40} We should note that this review is constraint to the research related to multiferroic thin films. Significant progresses have been made on the front of multiferroic bulk samples in the form of single crystals, ceramics,

and multi-component thick layers.⁴¹ There are also interesting works on non-oxide multiferroics such as CuCl₂.⁴² Our aim here is not to exhaust the fascinating physics in the broad field of multiferroics, but to give the readers a glimpse of recent discoveries on multiferroic oxide thin films, and to offer a perspective of possible future research directions.

In Sec. II, we will review the research progresses made on a few prototypical multiferroic oxides, particularly Bi-containing compounds and rare-earth manganites. We should note here that BFO is probably the most investigated multiferroic material, and there have been several comprehensive reviews in the literature.^{39,43–45} This review will not duplicate the existing ones, and we will give more attention to other multiferroic oxides. It is a consensus in the community that more efforts are needed to improve the materials synthesis and to elucidate the physical properties of many multiferroic compounds. This section also includes a brief discussion on the magnetism of multiferroic oxide thin films. Although the conventional antiferromagnetic order in some well-studied multiferroics does not give rise to sizable magnetism in bulk samples, a few works reported some weak magnetic signals in thin films. Such a size effect is particularly important for nanoscale and interface-based devices, and the underlying mechanisms will be discussed.

In Sec. III, we will review several device prototypes involving multiferroic thin films. The most straightforward one in terms of device fabrication and characterization is the resistive switching devices, where the memory functionality hinges on the toggles between high and low resistance states. A related device concept, but involving the ferroelectricity in ultrathin multiferroic thin films, is the ferroelectric tunneling junctions (FTJs). In the third device application, researchers take advantage of the interfacial coupling between multiple ferroic orders to realize new ME controls in multiferroic/ferromagnetic heterostructures. Although much less investigated, multiferroic/superconducting heterostructures

constitute one particular type of fascinating multiferroic thin film device. Last but not least, we will briefly discuss the photovoltaic (PV) devices involving multiferroic thin films, and open questions remain regarding the transport physics of such oxide films with domain walls under the light stimulation. Although time is still too early to unambiguously predict the killer applications of multiferroic materials, their fascinating properties continue inviting research efforts from both theoretical and experimental communities.

This review ends with a summary and outlooks in Sec. IV.

II. MULTIFERROIC OXIDE THIN FILMS

A. Bi-containing multiferroic thin films

1. BiFeO₃

In the arena of multiferroic research, one of the most successful stories is BiFeO₃, which exhibits room temperature ferroelectric and magnetic orders ($T_C = 830^\circ\text{C}$ and $T_N = 370^\circ\text{C}$). The ordering of highly polarizable Bi lone pairs drives the emergence of ferroelectric polarization, while the super-exchange between neighboring Fe and O ions leads to the G-type antiferromagnetic order. Bulk BFO has a rhombohedral lattice structure (space group: $R3c$) with lattice parameters of $a_{\text{hex}} = 5.58 \text{ \AA}$ and $c_{\text{hex}} = 13.90 \text{ \AA}$. It perovskite-type unit cell has a lattice parameter, $a = 3.965 \text{ \AA}$.^{8,29,44}

BFO thin films present complex and fascinating domain physics. The ferroelectric domain structure of BFO films can be characterized by analyzing the in-plane (IP) and out-of-plane (OOP) piezoelectric force microscopy (PFM) images. Three types of domain walls can be identified, e.g., 71° , 109° , and 180° , as illustrated in Figure 1(a).⁴³ At present, people can successfully control the domain configurations during or after the growth of BFO films (Figures 1(b)–1(d)).^{46–50} Some interesting domain-related physics have been revealed in BFO films with carefully controlled ferroelectric domains,

such as the high conductivity in domain wall⁵¹ and above-bandgap photovoltage.^{52,53}

2. BiMnO₃ (BMO)

BMO is a unique multiferroic material, possessing ferromagnetic ($T_{\text{FM}} = 105 \text{ K}$) and ferroelectric ($T_{\text{FE}} = 770 \text{ K}$) ground state with a spontaneous polarization ($P \sim 16 \mu\text{C}/\text{cm}^2$) and magnetization ($M \sim 3.6 \mu_B/\text{Mn}$).^{30,54–58} Similar to BFO, the ferroelectric state in BMO is caused by the stereochemical activity of Bi $6s^2$ lone pairs, while the ferromagnetism originates from the ferromagnetic super-exchange interaction between Mn^{3+} . High pressure is required for the synthesis of bulk BMO single crystals, but this difficulty can be overcome by epitaxial stabilization in thin films. Epitaxial BMO thin films have been successfully grown using PLD by a few groups, and the growth window appears to be very narrow.^{31,59–64} The magnetic property of BMO film is very sensitive to the growth parameters, which can be associated with the Bi vacancy and the substrate strain effect.^{31,61,62} To avoid these shortcomings, Gajek *et al.* partially replaced Bi^{3+} with isovalent La^{3+} while retaining the good FE-FM property. They found a broader growth window, and the magnetism is more stable than the case of pure BMO thin films.⁶⁵

In terms of devices, a four-state resistive system was realized in a $\text{La}_{0.1}\text{Bi}_{0.9}\text{MnO}_3$ (LBMO)/ $\text{La}_{2/3}\text{Sr}_{1/3}\text{MnO}_3$ heterostructure (Figure 2).⁶⁶ The junction transport depends on not only the relative magnetic orientations like in the conventional magnetic tunneling junctions but also the polarization direction of the thin LBMO layer. It represents a significant breakthrough in the quest for the next-generation memory devices.

3. BiCrO₃ (BCO)

BCO is another typical perovskite multiferroic material with large A-site Bi^{3+} , in which antiferroelectricity and

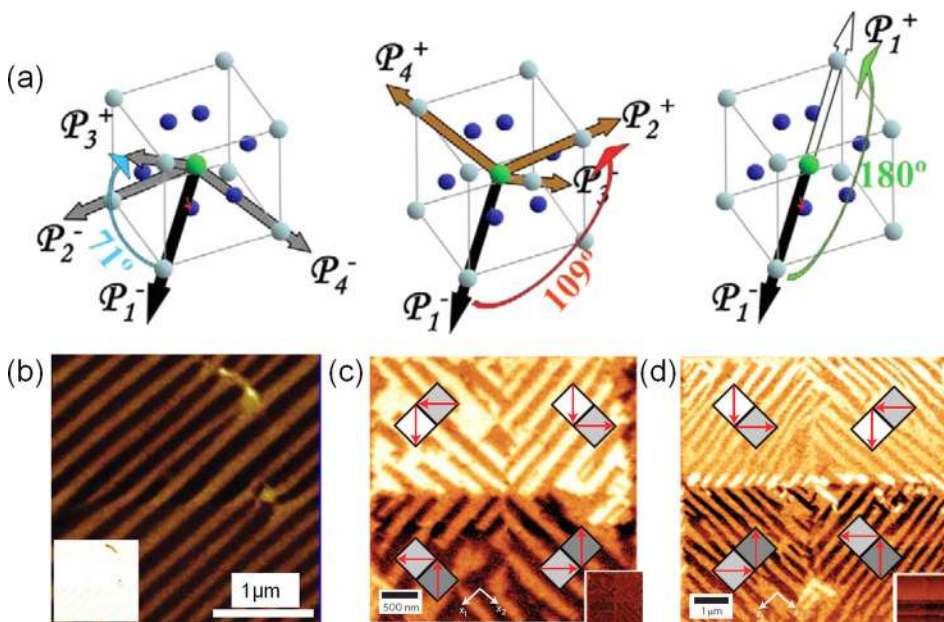


FIG. 1. (a) Three possible mechanisms for switching the polarization in BiFeO₃. Reprinted with permission Chu *et al.*, *Mater. Today* **10**, 16 (2007). Copyright 2007 Elsevier. (b) In-plane PFM image reveals clear stripe domains which are formed during the film deposition. The inset shows the out-of-plane PFM image of BFO thin film, in which no evident contrast can be observed. Reprinted with permission from Chu *et al.*, *Nano Lett.* **9**, 1726 (2009). Copyright 2009 American Chemical Society. (c) and (d) In-plane PFM images of artificial stripe patterns with different configurations for BiFeO₃ thin films grown on SrTiO₃ (001) substrates with $\text{La}_{0.7}\text{Sr}_{0.3}\text{MnO}_3$ buffer layers. The insets show the corresponding out-of-plane PFM images. Reprinted with permission from Balke *et al.*, *Nat. Nanotechnol.* **4**, 868 (2009). Copyright 2009 Nature Publishing Group.

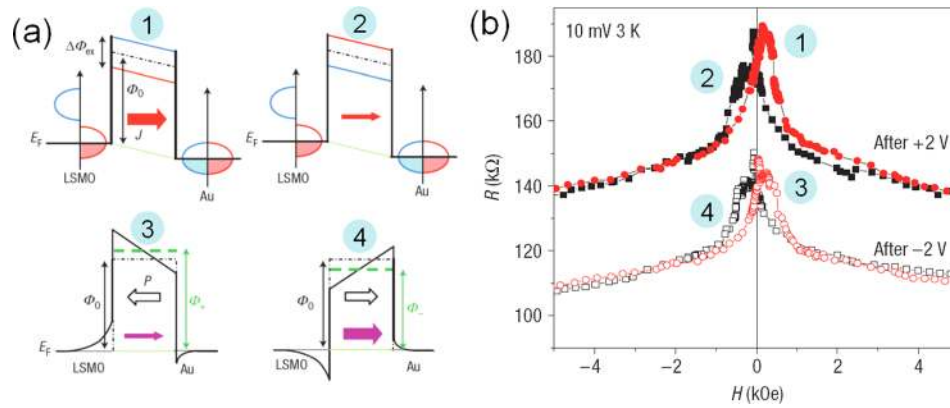


FIG. 2. (a) Schematic drawing of the tunnel barrier potential profiles and tunnel currents in the LSMO/LBMO/Au heterostructure. Upper figures indicate spin-dependent tunneling for parallel (left) or antiparallel (right) configuration of the LBMO and LSMO magnetization. Bottom figures indicate polarization dependent tunneling for electric field parallel (left) or antiparallel (right) to the polarization; (b) tunnel magnetoresistance of the junction measured at 3 K at 10 mV after applying a positive (2 V) or negative (−2 V) voltage across the junction. Reprinted with permission from Gajek *et al.*, Nat. Mater. 6, 296 (2007). Copyright 2007 Nature Publishing Group.

weak parasitic ferromagnetism were evidenced.^{32,67} Unlike BFO, only a few studies on BCO thin films have been reported. Hill first theoretically predicted in BCO a G-type antiferromagnetic ground state with antiferroelectric structure distortion.^{68,69} Murakami *et al.*³² reported piezoelectric response and tunable dielectric constant in BCO epitaxial thin film grown on LaAlO₃ (LAO) substrate, while weak ferromagnetism arises at low temperatures. Similar weak ferromagnetism was revealed by Kim *et al.*⁶⁷ in BCO thin films grown on SrTiO₃ (STO) (001) substrates, while double hysteresis loops were observed in both $\epsilon(E)$ and $P(E)$, indicating the antiferroelectricity within the film, as shown in Figure 3. There remain open questions regarding the antiferroelectricity and weak ferromagnetism in BCO thin films, while multi-phase coexistence may help to understand these features.⁷⁰

4. Bi-based ordered double perovskites

For the Bi-based transition metal perovskites BiMO₃ (M = Fe, Mn, Cr, ...), ordered double perovskites (such as BiFe_{0.5}Cr_{0.5}O₃ and BiFe_{0.5}Mn_{0.5}O₃) were theoretically predicted to be promising multiferroic candidates, in which large spontaneous polarization and ferromagnetism could be realized simultaneously.^{69,71} Indeed, very large polarization ($P \sim 60 \mu\text{C}/\text{cm}^2$) was experimentally evidenced in

BiFe_{0.5}Cr_{0.5}O₃ thin film, but the magnetism is weak (Figures 4(a) and 4(b)).⁷²

A notably large magnetization of $\sim 90 \text{ emu}/\text{cc}$ was reported in BiFe_{0.5}Mn_{0.5}O₃ thin films (Figure 4(c)).⁷³ In a different approach, Nechache *et al.* fabricated BFO/BCO heterostructures using PLD and revealed significant enhancement of magnetism.⁷⁴

B. Multiferroic rare-earth manganites

An intriguing class of compounds is rare-earth (R) manganites that show either a hexagonal structure when the R ionic radius is small ($P63cm$, from Y, Sc, and Ho to Lu) or an orthorhombic structure when the ions are large ($Pnma$, from Dy to La). The crossover is around Y/Ho (Figure 5).³⁸ Recent studies demonstrated that the hexagonal manganites with small R ionic radius can be transformed into the orthorhombic phase through soft chemical synthesis, thin film growth, or high pressure treatment. Intriguing physical properties were revealed in these newly synthesized orthorhombic phases.^{33,75,76} Reversely, the orthorhombic phase can also be transformed to the hexagonal one through exploiting the epitaxial strain, and the associated physical properties can be modified correspondingly.^{34,77}

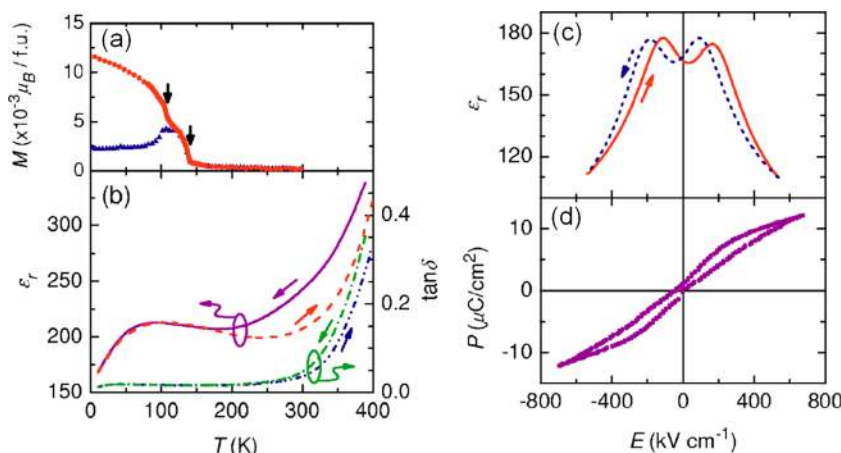


FIG. 3. (a) Temperature dependent magnetization of BCO film on STO substrate with a SrRuO₃ bottom layer measured at 2 kOe under field cooling (red circles) and zero field cooling (blue triangles) conditions. (b) Dielectric constant and loss tangent data as a function of temperature measured during cooling or warming processes. Dielectric constant (c) and polarization (d) as a function of electric field measured at a frequency of 10 kHz. Reprinted with permission from Appl. Phys. Lett. 89, 162904 (2006). Copyright 2006 AIP Publishing LLC.

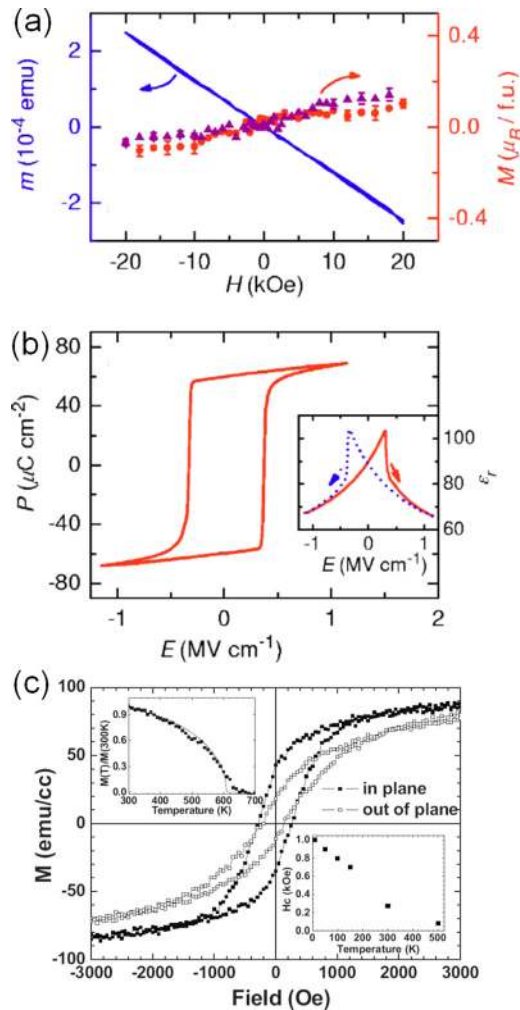


FIG. 4. (a) Magnetic field dependent magnetization for the $\text{BiFe}_{0.5}\text{Cr}_{0.5}\text{O}_3$ film grown on SrTiO_3 (001) substrate with a SrRuO_3 bottom layer. The blue line is the original data, and the red circles (increasing field) and purple triangles (decreasing field) are the data after subtracting the diamagnetism from the substrate. (b) Ferroelectric hysteresis loop measured at $T = 77.3$ K with a frequency of 1 kHz. The inset shows the electric field dependent dielectric constant with a measuring frequency of 10 kHz at $T = 77.3$ K. Reprinted with permission from Appl. Phys. Lett. **91**, 042906 (2007). Copyright 2007 AIP Publishing LLC. (c) Room temperature magnetic hysteresis loop for a $\text{BiFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ film grown on SrTiO_3 (001) substrate. Reprinted with permission from Appl. Phys. Lett. **98**, 012509 (2011). Copyright 2011 AIP Publishing LLC.

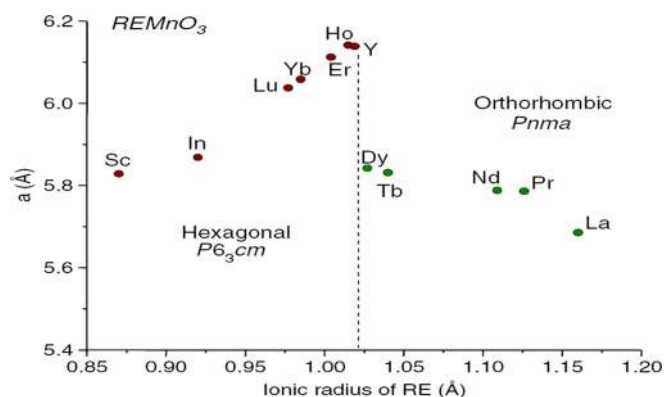


FIG. 5. Structural evolution of RMnO_3 as a function of the radius of A-site rare earth ions. Adapted with permission from Prellier *et al.*, J. Phys.: Condens. Matter **17**, R803 (2005). Copyright 2005 Institute of Physics.

1. Antiferromagnetic RMnO_3

The most studied hexagonal RMnO_3 is YMnO_3 (YMO), in which layers of MnO_5 trigonal bipyramids (different from the MnO_6 octahedron in the perovskites) and layers of Y^{3+} alternatively packed along the c axis. The lattice parameters of YMO are $a = 6.13$ Å and $c = 11.4$ Å.⁷⁸ One obvious advantage of YMO is that it does not contain volatile elements such as Bi and Pb. The spin configuration of hexagonal YMO is frustrated as a result of the geometric constraint. In the layer of MnO_5 bipyramids (ab plane), the spins of Mn^{3+} are mediated by strong in-plane antiferromagnetic superexchange interaction and restricted within the plane. Along the c axis, the inter-plane exchange between Mn spins is about two orders of magnitude lower than that within the ab plane, giving rise to a strong anisotropy and an easy ab plane. The long range antiferromagnetic order of Mn spins arises at $T_N \sim 70$ K with a 120° configuration, which is typically observed in triangular antiferromagnets. Bulk single crystals of YMO possess a remnant polarization of $5.5 \mu\text{C/cm}^2$. In early works in the 1960s, the ferroelectricity ($T_C \sim 950$ K) in hexagonal YMO was ascribed to an off-center distortion of Mn^{3+} towards one of the apical oxygen ions.^{79,80} However, recent detailed single crystal x-ray diffraction experiments revealed that the Mn ions remain very close to the centre of the oxygen bipyramids, and the ferroelectric phase should be ascribed to the buckling of the layered MnO_5 bipyramids accompanied by the displacements of the Y ions.⁷⁸ The mechanism of the ferroelectricity in hexagonal YMO is associated with the strong hybridization between Y $4d$ and O $2p$ states.⁸¹

Since both ferroic orders are associated with the crystal structure, the ME coupling should be strong in YMO. Indeed, coupled magnetic and ferroelectric domains were directly mapped using the optical second harmonic generation (SHG) technique, as shown in Figure 6.^{82,83} Recently, Choi *et al.* reported very interesting interlocked ferroelectric and structural antiphase domain walls in hexagonal YMO single crystals using transmission electron microscopy (TEM) and conductive atomic force microscopy.⁸⁴ At the isostructural transition in hexagonal manganites, giant

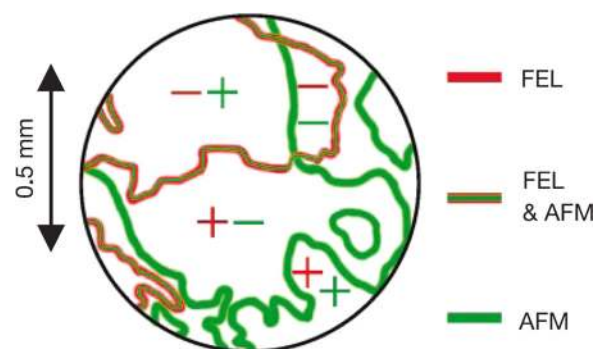


FIG. 6. Coupled magnetic and ferroelectric domain structures observed in YMnO_3 . YMnO_3 has four types of 180° domains denoted by $(+P, +I)$, $(+P, -I)$, $(-P, -I)$, and $(-P, +I)$, respectively, where $\pm P$ and $\pm I$ are the independent components of the ferroelectric and antiferromagnetic order parameters. Reprinted with permission from Fiebig *et al.*, Nature **419**, 818 (2002). Copyright 2002 Nature Publishing Group.

magneto-elastic coupling was observed and the atomic displacement is nearly 0.1 Å.⁸⁵

YMO thin films have been grown on various substrates including SrTiO₃, MgO, ZnO, GaN, and Si, in which the physical properties are qualitatively similar to the bulk counterpart.^{86–92} In ultrathin YMO films grown on yttria-stabilized zirconia (111) substrates, strain can induce in-plane trigonality and four stable polarization states.⁹³ The crystal structure of YMO can be dramatically changed to orthorhombic when it is grown on YAlO₃ (010) or SrTiO₃ substrate. In the orthorhombic-YMO (*o*-YMO), the super-exchange interaction mediated long-range E-type anti-ferromagnetic order can directly generate ferroelectricity ($P \sim 0.8 \mu\text{C}/\text{cm}^2$) due to the effect of exchange striction.⁷⁶

In another E-type antiferromagnetic ferroelectric material TmMnO₃, the spontaneous polarization was reported to be $0.45 \mu\text{C}/\text{cm}^2$.⁹⁴ Hexagonal HoMnO₃ shows a higher polarization of $5.6 \mu\text{C}/\text{cm}^2$ below $T_C \sim 875$ K. The orderings of Mn and Ho ions occur at 75 K and 4.6 K, respectively. Furthermore, the ferromagnetic ordering in HoMnO₃ can be switched by an applied electric field *via* ME interactions.⁹⁵ Recently, theoretical calculation predicts a huge electronic contribution to the ferroelectricity in HoMnO₃ thin films with large strain, but so far it has not been confirmed experimentally.⁹⁶ Actually, in this E-type AFM state, the magnetically driven spontaneous polarization was theoretically predicted to be as large as the values observed in the conventional perovskite ferroelectrics.^{97,98}

2. Orthorhombic RMnO₃ with spiral spin order (SSO)

The magnetic control of ferroelectricity in TMO was first reported in 2003 by Kimura *et al.*⁷ TMO has a perovskite crystal structure with lattice parameters of $a = 5.2931 \text{ \AA}$, $b = 5.8384 \text{ \AA}$, and $c = 7.4025 \text{ \AA}$.⁷⁵ In this material, the breaking of spatial-inversion and time-reversal symmetries simultaneously occurs, and the ferroelectricity is induced by the inherent magnetic configuration, i.e., SSO. So far, dozens of magnetically driven multiferroic materials have been identified, and two types of SSO were revealed to be responsible for producing spontaneous polarization, as schematically illustrated in Figures 7(a) and 7(b).^{99,100} The corresponding mechanism of the multiferroicity can be generally understood using the inverse effect of the Dzyaloshinskii-Moriya (DM) interaction, $\mathbf{P} \propto -\mathbf{e}_{i,j} \times (\mathbf{S}_i \times \mathbf{S}_j)$, where $\mathbf{e}_{i,j}$ is the unit vector connecting the nearest-neighboring (NN) spins \mathbf{S}_i and \mathbf{S}_j .¹⁰¹

Typical materials with cycloidal spin ordering are TMO and DyMnO₃ (DMO), in which a collinear sinusoidal antiferromagnetic spin ordering arises ($T_N = 41$ K for TMO and 39 K for DMO), and further cooling causes a *bc*-plane cycloidal (transverse-spiral) spin ordering with magnetically induced spontaneous polarization along the *c* axis ($T_C = 28$ K for TMO and 19 K for DMO).¹⁰² A schematic drawing of the spin configuration and the temperature-dependent evolution of physical properties in TMO are presented in Figures 7(c)–7(e).⁷ For the physics of bulk SSO multiferroic materials, three reviews are recommended.^{4,99,100}

TMO thin films were synthesized and interesting ferromagnetic tendency was revealed.^{103–108} Detailed

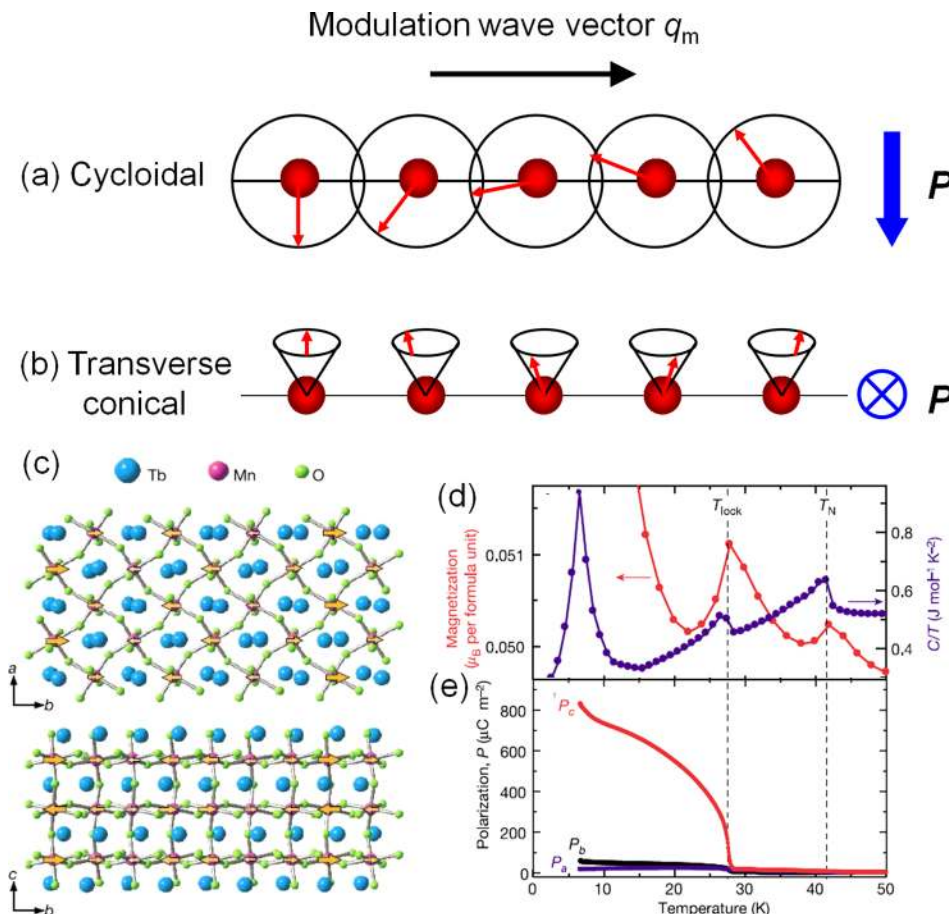


FIG. 7. Schematic drawings of (a) cycloidal and (b) transverse conical spin ordering. (c) Collinear sinusoidal spin ordering as $T_C < T < T_N$ (up), and spiral-spin-ordering as $T < T_C$ in multiferroic TbMnO₃. Temperature dependent magnetization and specific heat (d), and spontaneous polarization (e) along different axes in TbMnO₃. Reprinted with permission from Kimura *et al.*, Nature **426**, 55 (2003). Copyright 2003 Nature Publishing Group.

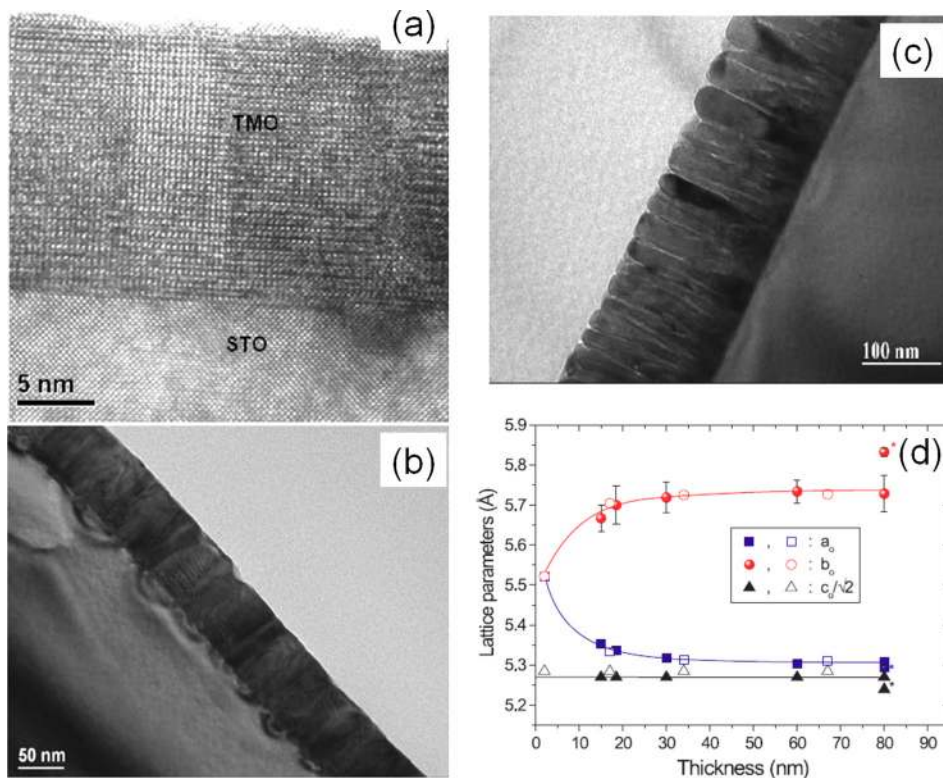


FIG. 8. Bright-field cross-section TEM images of TMO/SrTiO₃ thin films with different thicknesses (a) 17 nm; (b) 67 nm; and (c) 140 nm. Reprinted with permission from Venkatesan *et al.*, Phys. Rev. B **80**, 214111 (2009). Copyright 2009 American Physical Society. (d) Evolution of lattice parameters with thickness. Adapted with permission from Daumont *et al.*, J. Phys.: Condens. Matter **21**, 182001 (2009). Copyright 2009 Institute of Physics.

magnetometry, x-ray, and neutron scattering investigations confirmed that the emergent ferromagnetism in TMO thin films is an intrinsic property.¹⁰⁶ Two possible mechanisms were proposed to be responsible for the emerged ferromagnetism: (i) strain-induced modulation of the competition between antiferromagnetic and ferromagnetic exchange interactions,¹⁰⁸ and (ii) magnetic contribution from the domain walls.¹⁰³ By combining x-ray photoemission measurements and *Ab initio* calculations, Rubi *et al.* revealed that the Mn 3s splitting in TMO thin films is 0.3 eV larger than that of the bulk counterpart.¹⁰⁴ Detailed structural characterizations were also carried out on TMO/SrTiO₃ thin films.^{103,105,109} Very clear nanoscale domains were observed, and the crystalline structure transforms from the tetragonal phase to the orthorhombic one *via* a twinning process. The evolution of crystal structure with film thickness characterized using TEM and high-resolution x-ray diffraction is shown in Figure 8.

Although interesting ferromagnetism has been reported in TMO thin films, measuring the small spontaneous polarization in this type of spiral multiferroic materials remains challenging. Recently, the magnetically induced ferroelectric state was confirmed in TMO thin films grown on YAlO₃ (001) substrates by using the second harmonic generate method, and the ferroelectricity can even exist in films as thin as 1.6 nm.¹¹⁰ In DMO (Figure 9) and GdMnO₃ thin films grown on SrTiO₃ (001), the ferroelectric polarization was clearly demonstrated by both pyroelectric current method and hysteresis measurement, and large magnetic anisotropy and magnetic field induced polarization enhancement were also identified.^{111,112} In particular, large spontaneous polarization was reported in GdMnO₃ thin films, which is probably due to a self-assembled nano-twinning domain

structure.¹¹² This result indicates that finely tuning the competing balance of multiple interactions is a promising route to explore novel spin-dictated multiferroicity in classic multiferroics. In addition, while the ground state of bulk orthorhombic YMO is E-type antiferromagnetic, a strain induced spiral spin ordering phase accompanied by spontaneous polarization was recently reported in thin films, and an intriguing memory effect was evidenced.^{113,114} The recent progresses of directly measuring the spontaneous polarization in these spiral multiferroic thin films open the possibility of integrating them into functional devices. Furthermore, a few recent works reported gigantic magnetically induced ferroelectric polarization and ME coupling in bulk crystals of

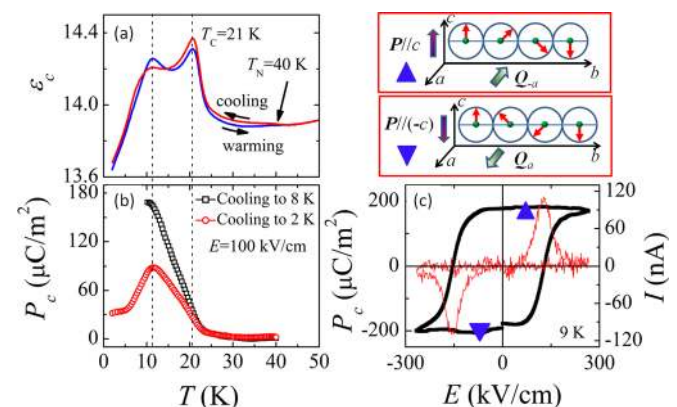


FIG. 9. Dielectric and ferroelectric properties of DyMnO₃ thin films. Temperature dependence of ϵ_c (a) and P_c (b). (c) Ferroelectric hysteresis loop measured at $T = 9$ K without magnetic field during the cooling process. A sketch of the clockwise (Q_{-a}) and counterclockwise (Q_a) spiral spin orders is also presented. Adapted with permission from Lu *et al.*, Sci. Rep. **3**, 3374 (2013). Copyright 2013 Nature Publishing Group.

$\text{CaMn}_7\text{O}_{12}$,¹¹⁵ $\text{CaBaCo}_4\text{O}_7$,¹¹⁶ and TbMnO_3 under pressure,¹¹⁷ which may motivate more thin film research.

C. Other multiferroic thin films

The search for more multiferroic materials with high performances has been fruitful, and along the process new physics was revealed. However, it is unrealistic to exhaust here all the related works in literature because of the space constraint. Instead, we focus here on one example: delafossite-type CuMO_2 ($M = \text{Cr, Mn, Fe, or Co}$). This class of materials has a two-dimensional (2D) triangular crystal structure, in which the M oxide magnetic layers and the cuprous oxide layers are alternately packed along the c axis. These 2D triangular antiferromagnets have received lots of interest due to the inherent multiferroicity caused by the frustrated spin configuration.^{118,119} It was demonstrated for CuCrO_2 that ferroelectric polarization reversal could be finely tuned by both magnetic and electric fields.¹²⁰ Recently, a few works on multiferroic CuMO_2 thin films were reported, and measurements of optical absorption spectra were performed on these multiferroic thin films.^{121,122} Two optical transitions were identified and associated with $\text{Cu}3d+O2p \rightarrow \text{Cu}3d_z^2+4s$ and $\text{Cu}3d+O2p \rightarrow M3d$, as shown in Figure 10. These results indicate that epitaxial thin films of 2D triangular ferromagnets involving magnetic and excitonic features are promising to realize some novel functionalities.

D. Magnetism in multiferroic thin films

In most well-studied multiferroic materials such as BFO and TMO, the antiferromagnetic spin order, which coexists

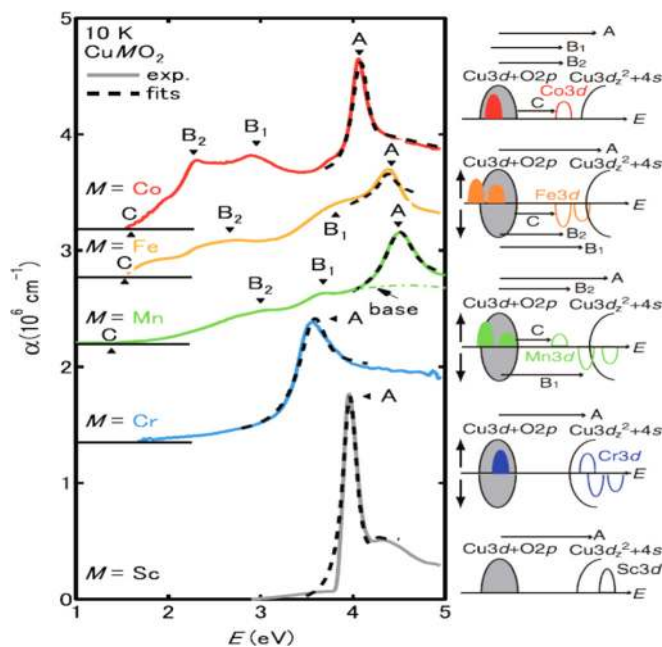


FIG. 10. Absorption spectra (solid lines) of CuMO_2 ($M = \text{Sc, Cr, Mn, Fe, and Co}$) thin films. The right panel represents a schematic drawing of the energy diagrams derived from first-principles calculations. Arrows indicate transitions corresponding to the observed absorption peaks. Reprinted with permission from Hiraga *et al.*, Phys. Rev. B **84**, 041411 (2011). Copyright 2011 American Physical Society.

with ferroelectricity, does not give rise to any macroscopic magnetic moment. Canting of the AFM aligned spins by the DM interaction can give rise to weak FM.¹⁰¹ For multiferroic device applications, it is beneficial to enhance the magnetism in these materials and to achieve sizable spontaneous magnetism. In literature, there are several reported approaches of enhancing the magnetism in multiferroic oxide thin films. It is not a surprise that most of such works have focused on BFO.

Combining the angle and temperature dependent dichroic measurements and spectroscopy, Holcomb *et al.* observed that the antiferromagnetic phase in BFO epitaxial thin films is sensitive to the thickness and strain.¹²³ Similar magnetic modulation was observed in BFO/ LaAlO_3 thin films with large compressive strain, in which the saturated magnetism and coercivity of the highly strained phase are about six times larger than those of the relaxed one (Figure 11).¹²⁴ A weak but definite spin-glass (SG) transition was evidenced in BFO/ LaAlO_3 thin films.^{124,125} Overall, strain can exert significant effects on the magnetic property of BFO thin films. But it should be noted that such glassy magnetism in thin BFO films would be too weak to be integrated into functional devices.

In another approach, magnetism in BFO was enhanced through structural and compositional modulations.^{126–130} When Bi^{3+} is substituted by a larger radius ion (such as Ba^{2+}), the net magnetization can be notably enhanced due to the suppression of the long range spiral-spin-ordering in BFO.¹²⁶ Furthermore, rare-earth doping is an effective way to enhance the magnetism in BFO, which can be associated

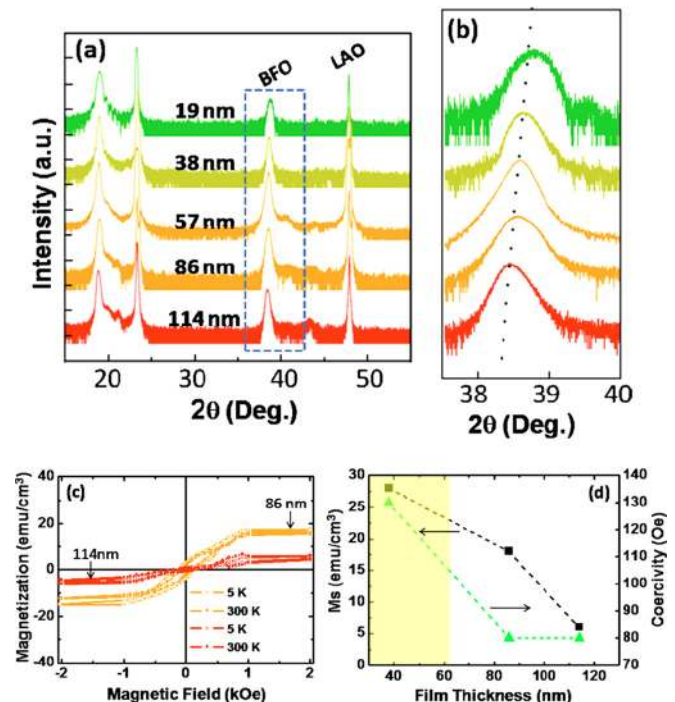


FIG. 11. (a) and (b) X-ray diffraction spectra of quasi-tetragonal phase BFO/ LaO films with various thicknesses. (c) Magnetic field dependence of magnetization for samples with different thicknesses measured under 300 and 5 K. (d) Thickness dependence of room temperature saturated magnetization and coercivity. Reprinted with permission from Appl. Phys. Lett. **98**, 242502 (2011). Copyright 2011 AIP Publishing LLC.

with the crystal structure modulation as well as the magnetic coupling between rare-earth ions and Fe^{3+} .^{127,128}

Regarding the size effect, the period of spiral-spin-ordering in bulk BFO is about 62–64 nm, so it would be of interest to see the magnetic variation as the size of BFO samples is scaled down into the nanometer regime. Indeed, a few groups reported ferromagnetism in nano-sized BFO, which was ascribed to the breakdown of the long-range spin order.^{129,130} These results also bear relevance to thin film and nanoscale device research, and new physics may emerge when the sample dimensions scale down to the characteristic length of spin order in BFO.

As aforementioned, interesting strain-engineered ferromagnetism has been observed in TMO thin films.^{104,106,107} In fact, similar modulation in magnetism was identified in YMO thin films as well.^{108,131} A large magnetic moment of $\sim 330 \text{ emu/cm}^3 = 2.2 \mu_B/\text{Mn}$ at 15 K was observed in BiMnO_3 films grown on SrTiO_3 and the coercivity is $\sim 500 \text{ Oe}$.⁶² A later work found that the magnetic moment of BiMnO_3 films can further increase to $\sim 3.2 \mu_B/\text{Mn}$ by growing on SrTiO_3 .⁶⁴ However, the magnetism usually appears quite weak in most multiferroic oxides. For example, a magnetic moment of only $\sim 0.075 \mu_B/\text{Mn}$ was found for YMO films grown on YAlO_3 (001) substrates.⁷⁶ It is worth of mentioning that a large ferromagnetic moment of $\sim 0.5 \mu_B/\text{Mn}$ with intrinsic exchange bias was evidenced in orthorhombic $\text{LuMnO}_3/\text{YAlO}_3$ (110) thin films. Combining the polarized neutron reflectometry technique, a possible ferromagnetic interlayer close to the substrate in the film was proposed to be the origin.¹³² These findings suggest that the multiferroic manganites can be promising candidates for new functional devices.

III. DEVICES BASED ON MULTIFERROIC THIN FILMS

A. Resistive switching devices

We start the discussion on multiferroic devices with resistive switching memories because of their simple two-terminal configuration and relatively straightforward operation mechanism. Since most multiferroic materials are excellent insulators, they can be directly applied in resistive switching devices for nonvolatile memory applications. Such devices usually show advantages of high density, high speed, and low power, and thus they are promising for next generation nonvolatile memory technology. Different from the switching operation of conventional dielectric materials

where only the resistance can be switched between two states, namely, the high resistance state and the low resistance state, the resistive switching actions in multiferroic thin films could be accompanied by the concurrent modulation of the magnetic and ferroelectric properties, which, although has not been extensively explored so far, would drastically functionalize the devices.

Interesting switching effects were realized in BFO thin films: Wang *et al.*¹³³ observed polarization-modulated conduction behaviors, including switchable diode effect and ferroelectric resistive switching, as shown in Figure 12. These interesting properties were attributed to the polarization-induced variations of Schottky barrier. In addition, a novel ferroelectric-resistive non-volatile random access memory (RAM) consisting of BFO epitaxial thin films was reported. This device showed promising properties like excellent retention and high ON/OFF ratios.¹³⁴

There are mainly two barrier-related mechanisms proposed to be responsible for the resistance switching observed in such multiferroic thin films. One is the polarization induced interface barrier, and the other is the charge injection induced interface barrier change, especially the electromigration of oxygen vacancies under the high electric field. However, which mechanism is dominant during a particular switching process is still under active debate.^{134–136} This is partially due to the diverse electric behaviours of BFO films which depend sensitively on the deposition conditions.

The well studied multiferroic materials YMO, TMO, and DMO were also used in memory devices, which show quite high ON/OFF ratios ($>10^4$) and good retention ($>10^5 \text{ s}$). The ferroelectricity in such films is much weaker than that of BFO. The mechanism of resistive switching in these thin films was ascribed to the rupture and formation of conductive filaments.^{137–139} For example, at the ON state, the carriers such as oxygen vacancies would be driven to form a certain pathway throughout the device, resulting a highly conductive path in the device and thereby a smaller resistance. On the other hand, for the OFF state, all those carriers are distributed randomly within the device, and there is no conductive channel, giving rise to a high resistance state.

B. Ferroelectric/multiferroic tunnel junctions

The above mentioned resistive-switching behaviour is often observed in oxide films with thickness of hundreds of

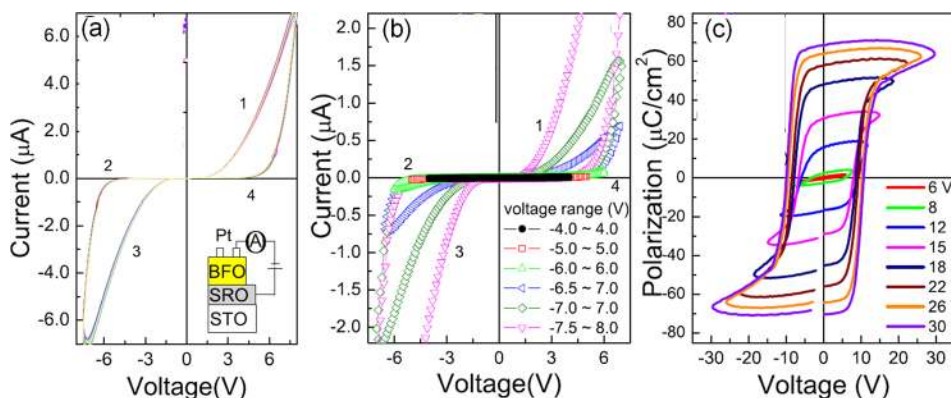


FIG. 12. (a) I - V curves for BFO thin film. The schematic of the device structure is plotted in the inset. (b) I - V curves measured on a virgin BFO thin film with different voltage sweeping ranges. The resistive switching behavior appears when the sweeping voltage is larger than 6 V. (c) Ferroelectric hysteresis loops measured under different voltage ranges. Reprinted with permission from Appl. Phys. Lett. 98, 192901 (2011). Copyright 2011 AIP Publishing LLC.

nanometers. In this thickness range, both the interface barrier and the ferroelectric itself contribute to the transport. However, when the ferroelectric layer thickness goes down to several nanometers, where electric tunnelling occurs, the polarization controlled interface barrier will become the dominant factor due to the large depolarization field. Based on this idea, the device concept of FTJ was proposed,¹⁴⁰ which is composed of an ultra-thin FE layer sandwiched between two metal electrodes (M/FE/M).

Figure 13 shows the schematic band diagram of a FTJ device.¹⁴⁰ Due to the charge screening effect, the reversal of polarization will change the charge distribution on the ferroelectric-metal interface and thus modify the tunnel barrier height the tunnelling electrons experience. Tunnelling electroresistance (TER) is thus defined as the ratio of resistance values corresponding to different barriers. Other effects such as the chemical bonding at the interface and the piezo-induced strain effect (Figure 13, right) could also contribute to TER.

The maintenance of the ferroelectricity in the ultrathin films is the main challenge of fabricating functional FTJs. Benefitting from the improvement of thin film deposition technology in recent years, ferroelectricity in ultrathin films¹⁴¹ and the related FTJs have been demonstrated in BaTiO₃, PbZr_{0.2}Ti_{0.8}O₃, and BFO ultrathin films.¹⁴²⁻¹⁴⁴ Different with the magnetic tunnel junctions, where the writing is accomplished through the current induced magnetic field, the states of a FTJ are set using an electric field. This all electronic operation means low energy consumption in FTJs, which is one of the main advantages of using FTJ as a non-volatile memory device. Other advantages include the fast writing speed as a result of the fast domain switching and the multi-level resistance states.^{142,145} However, the drawbacks are also obvious, including the poor retention and

endurance performance of the device, which are a result of the unstable ferroelectric polarization in ultrathin films due to the size effect. These issues have been partially resolved by Wen *et al.* recently, who extended the common M/FE/M FTJs to M/FE/S(semiconductor) FTJs such as Pt/BaTiO₃/Nb-SrTiO₃ as shown in Figure 14.¹⁴⁶ It was found that by replacing the metal electrode with a semiconductor, TER could be greatly enhanced by two orders of magnitude, together with the improvement of the device retention and endurance. It was claimed that the simultaneous modulation of barrier height and barrier width by the polarization is responsible for this TER enhancement, and this breakthrough will surely inspire more future efforts in this research direction.

Recently, the rare-earth manganite TMO in hexagonal structure was also used as tunnel barrier, and giant ON/OFF ratio of resistance (30 000%) due to the switching of TMO polarization was observed.¹⁴⁷ This value is comparable with those in classic ferroelectric tunnel junctions and, moreover, TMO is a magnetic material. This work might inspire more interests in exploring superior properties in multiferroic tunnel junctions with rare-earth manganite barriers.

C. Multiferroic/ferromagnetic heterostructures

Although multiple ferroic-orders with intimate cross coupling coexist in some single-phase multiferroic material, the net magnetization is small, in general. To overcome this disadvantage, constructing heterostructures of multiferroic/ferromagnetic materials is promising to realize advanced spintronic devices. Recently, several groups successfully combined the multiferroic materials with ferromagnetic ones in thin film heterostructures, and very interesting phenomena were observed.¹⁴⁸ For example, exchange bias and uniaxial magnetic anisotropy were studied in BFO, YMO, and TMO

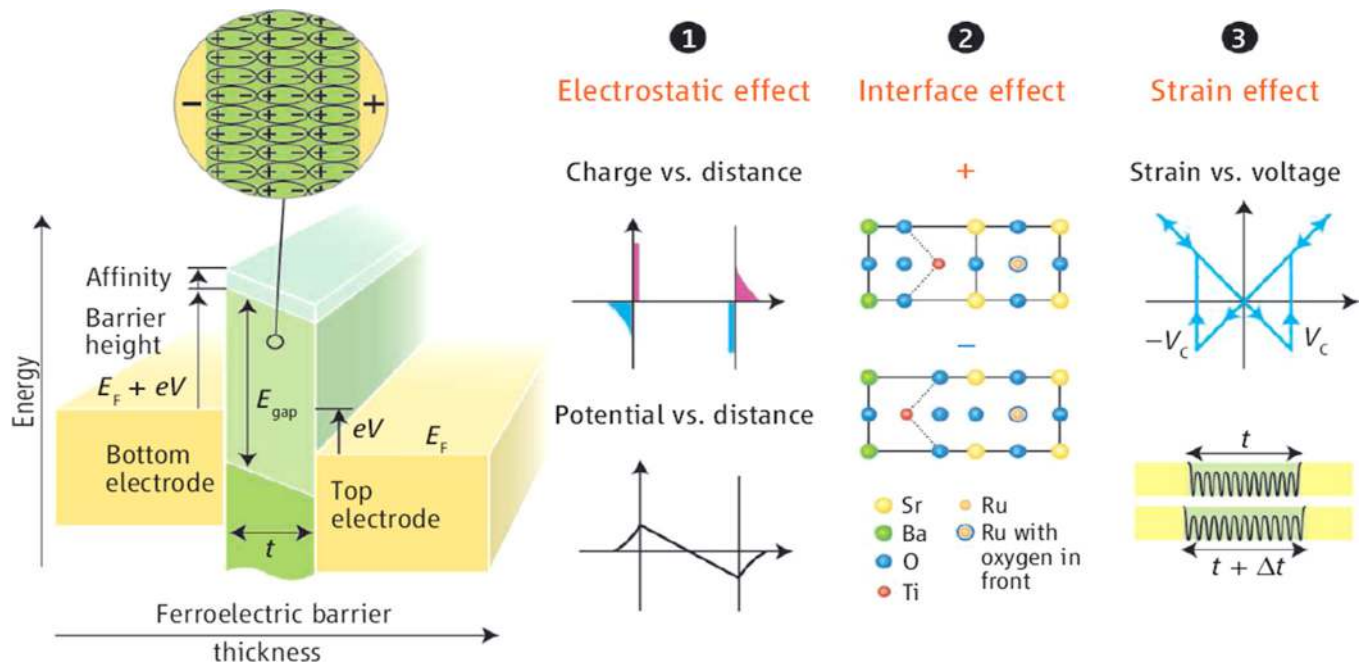


FIG. 13. Schematic diagram of a ferroelectric tunnel junction, which consists of two electrodes separated by a nanometer-thick ferroelectric barrier layer. (E_{gap} is the energy gap, E_F is the Fermi energy, V is the applied voltage, V_c is the coercive voltage, t is the barrier thickness, and δt is the thickness variation under an applied field.) Reprinted with permission from E. Y. Tsymlal and H. Kohlstedt, *Science* **313**, 181 (2006). Copyright 2006 AAAS.

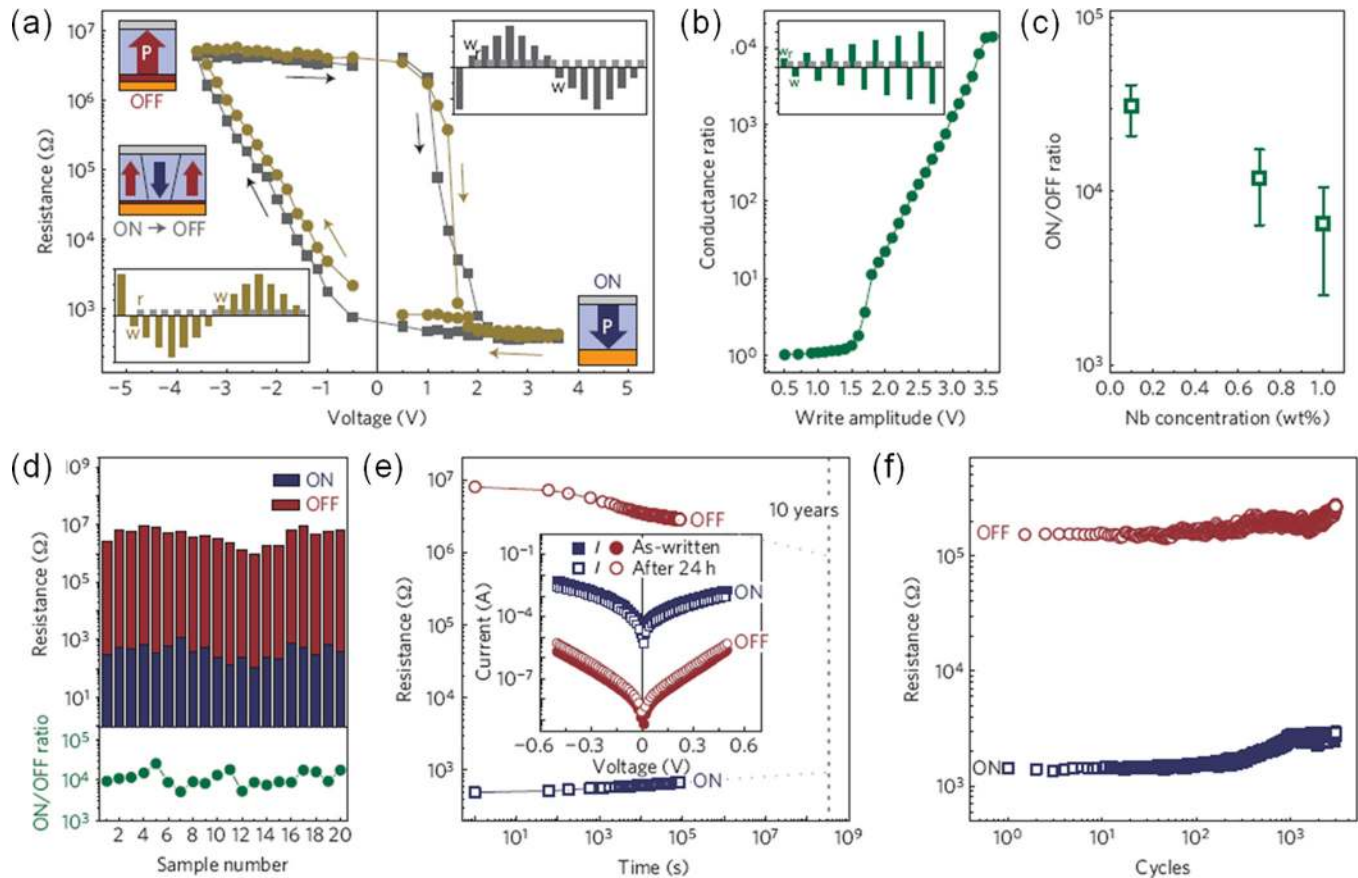


FIG. 14. (a) Resistance hysteresis loops measured on the Pt/BaTiO₃/Nb-SrTiO₃ heterostructure. The corresponding domain evolution is shown schematically in the bottom-right, top-left, and middle-left insets for the ON, OFF, and intermediate states, respectively. The testing pulse train is composed of write pulses (w) following a triangular profile between +3.6 and -3.6 V and read pulses (r) of +0.1 V following each write pulse. (b) Conductance ratio as a function of write amplitude. (c) ON/OFF ratio read at +0.1 V as a function of Nb doping concentration in Nb:SrTiO₃. (d) ON and OFF state resistances (upper panel) and the corresponding ON/OFF ratios (bottom panel) of 20 different devices. (e) Retention properties. The inset shows current-voltage curves collected before and after the retention measurement. (f) Bipolar resistance switching properties. Reprinted with permission from Wen *et al.*, *Nat. Mater.* **12**, 617 (2013). Copyright 2013 Macmillan Publishers Limited.

based heterostructures.^{149–163} As a milestone in the research on electric field control of magnetism, Zhao and coworkers demonstrated that the antiferromagnetic domains of BFO can be switched simultaneously with the ferroelectric domains using an electric field.¹⁶⁴ Ferromagnetic domains of the top Co_{0.9}Fe_{0.1} layer can be electrically switched when it was deposited on the BFO thin film, which indicates a strong magnetic interaction at the interface between the AFM order in BFO and the FM order in CoFe (Figure 15).^{152,163} Recently, Allibe *et al.* reported interesting electrical control of giant magnetoresistance (GMR) in spin valves exchange-biased with BFO, which represents another important progress in the field.¹⁶⁵

The first observation of the electric field control of exchange bias effect was reported in a Py/YMO heterostructure at a very low temperature of 2 K.¹⁶¹ Exchange bias effects were later obtained in multiferroic BiFeO₃/La_{0.7}Sr_{0.3}MnO₃ (LSMO) heterostructures without the need of heating to the Néel temperature of BFO, which can be further modulated by a gate electric field.^{156,157} A model was proposed to take into account the field-induced ionic displacements in BFO, and the modulation of the interatomic distance between the Fe and Mn ions presumably leads to the observed switching of exchange bias. Intriguingly, a

recent structural investigation revealed that the field effect should be ascribed to the motions of oxygen ions at the interface.¹⁶⁶

The magnetoelectric effect may enable the construction of novel device concepts like magnetoelectric RAMs (MeRAMs) which combines the magnetoelectric coupling with the interfacial exchange coupling between multiferroic and ferromagnetic layers.¹⁶⁷ In MeRAM, a voltage is used to switch the exchange coupling across the interface and in turn the magnetization of the ferromagnetic layer. This voltage mode of operation supposedly consumes much less energy than the current mode used in devices like MRAMs (magnetic RAMs). The mechanism of the exchange bias effects in such multiferroic/ferromagnetic heterostructures is still controversial.^{168–170} We would refer the readers to a few recent reviews dedicated to this topic of magnetoelectric effects.^{4,41,45} Nevertheless, these phenomena pave the way for integrating multiferroics into modern memory devices with potential high performances.

D. Multiferroic/superconducting heterostructures

Multiferroic/superconducting heterostructures, such as BFO-YBa₂Cu₃O₇ (YBCO) heterostructures, are interesting

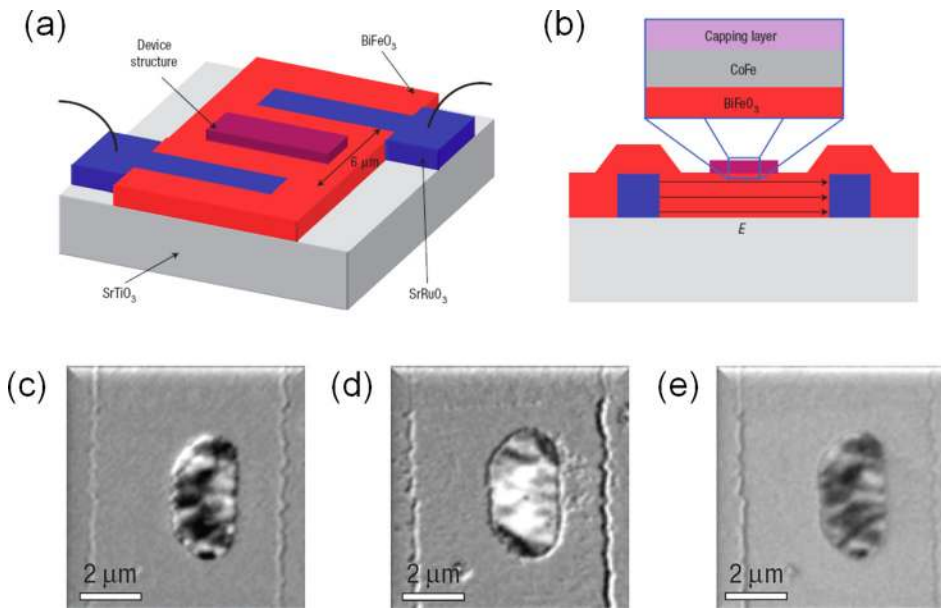


FIG. 15. (a) and (b) Schematics of the multiferroic-ferromagnetic device structure. Magnetic state of the CoFe layer was obtained using the x-ray magnetic circular dichroism (XMCD)-photoemission electron microscopy (PEEM) (white and black correspond to different magnetic polarities). (c) Original state; (d) domain state after the bottom layer of BFO was electrically switched; and (e) the BFO layer was switched back to the original state. Reprinted with permission from Chu *et al.*, Nat. Mater. 7, 478 (2008). Copyright 2008 Nature Publishing Group.

in considering the possible interactions between the superconducting order with the multiple ferroic orders at the interface. Indeed, a variety of fascinating properties have been evidenced in YBCO-based junctions.^{171–175} Epitaxial growth of BFO/YBCO heterostructure can be realized due to the compatible lattice structure in the two materials with a lattice mismatch of $\sim 3\%$. Interfacial couplings in such heterostructures may drastically upset the delicate balance of the competing interactions among charges, spins, orbitals, and lattice, which can potentially present a wide range of emergent phenomena.

Recently, high-quality BFO/YBCO heterostructure and its transport properties were reported. Interestingly, an enhancement of the interface barrier induced by the superconducting gap of YBCO was observed (Figure 16).¹⁷⁶ Moreover, the multiferroic field effect was reported in similar BFO/YBCO heterostructures, in which the superconducting condensate was modulated at nanoscale *via* the field effect.¹⁷⁷ We should note here that there has been no report on any theoretical framework which can guide the experiments on such multiferroic/superconducting heterostructures,

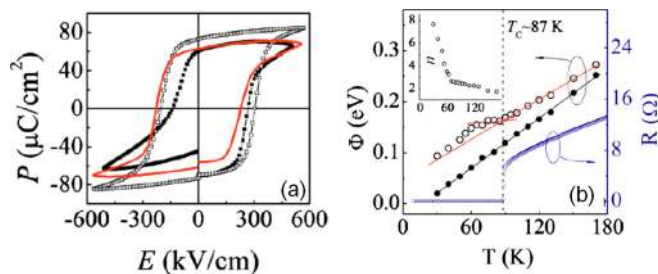


FIG. 16. (a) Ferroelectric hysteresis loops for the BFO/YBCO heterostructure measured at 77 K (open squares) and 300 K (solid squares). (b) Temperature dependence of the Schottky barrier height and resistance for the BFO/YBCO heterostructure. The inset shows the T -dependent refractive index n . For a comparison, the P - E loop (red line in (a)) and $\Phi(T)$ (solid dots in (b)) of a BiFeO₃/SrRuO₃ heterostructure were also presented. Reprinted with permission from Appl. Phys. Lett. 97, 252905 (2010). Copyright 2010 AIP Publishing LLC.

and data interpretation remains challenging. More future efforts are needed in order to elucidate the interface physics in such multiferroic/superconducting heterostructures.

E. Photovoltaic effect in multiferroic thin films

Recently, interesting PV effects were observed in BFO thin films with striped domains, and the produced voltage was significantly higher than the bandgap (Figure 17).⁵³ To understand this novel PV effect in BFO thin films, a ferroelectric-domain-wall-based model was proposed.^{52,53} In the ferroelectric domain walls, the built-in potential steps caused by the component of polarization can efficiently separate the photo-generated electrons and holes. The accumulation of the electrons/holes in the domain walls would build up a net electric voltage across the sample, leading to the observed open circuit photovoltage. This model can well explain the PV effect in BFO thin films with periodic domain structures.

On the other hand, a few groups reported PV effects in BFO thin films without striped domain and even in bulk monodomain BFO single crystals.^{63,135,178–180} Furthermore, PV effects were also observed in traditional ferroelectrics without a regular domain configuration.^{181–183} Concerning the role of domain walls on the abnormal PV effect in BFO thin films, Bhatnagar *et al.* performed temperature dependent PV effect measurements, proved that the bulk PV effect is the origin,¹⁸⁴ and revealed an interesting persistent PV effect in strained BFO.¹⁸⁵ After comparing with the traditional PV effects in p - n /Schottky junctions, Yuan and Wang proposed a model based on the ferroelectric polarization modified depletion region to explain the PV effects evidenced in ferroelectric materials.¹⁸⁶ In this model, the depletion region is modified when the polarization is switched, and thus the directional dependence of PV voltage and current on the polarization can be understood.

It is generally observed that the bulk photovoltaic effect is switchable with the polarization reversal,¹³⁵ which is proposed to be due to the polarization induced transition between Schottky and Ohmic contacts and the electromigration of

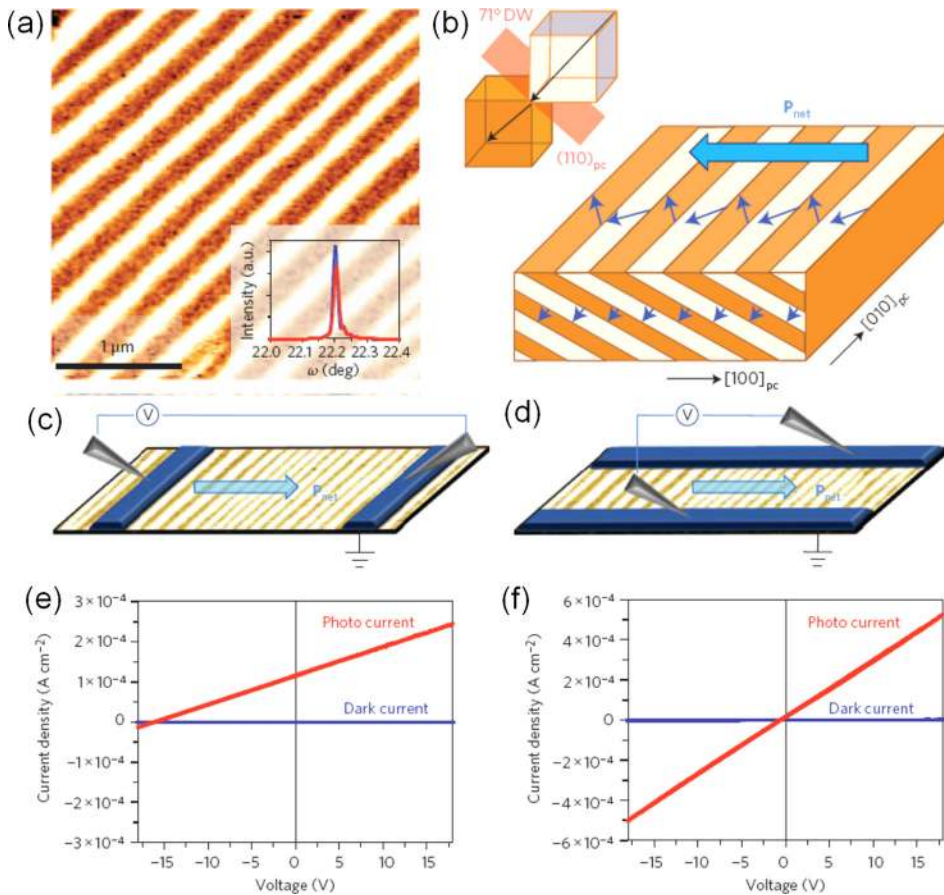


FIG. 17. (a) PFM image for periodic arrays of 71° domain walls. The inset shows the X-ray rocking curves along two orthogonal crystal axes. (b) Schematic drawing of the 71° domain arrays. The arrows indicate different components of ferroelectric polarization. The large arrow indicates the net polarization. Also shown are the schematic drawings of two different measurement configurations: parallel to the domain walls (c) and perpendicular to the domain walls (d), as well as the corresponding I - V curves measured perpendicular (e) or parallel (f) to the domain walls. Reprinted with permission from Yang *et al.*, Nat. Nanotechnol. 5, 143 (2010). Copyright 2010 Macmillan Publishers Limited.

defects such as oxygen vacancies.¹⁸⁷ Based on this phenomenon, a new type of non-destructive FeRAM device has been proposed recently by Guo *et al.*¹⁸⁸ The basic idea is to use the short circuit current (I_{sc}) or open circuit voltage (V_{oc}) to sense the direction of the polarization. Figure 18 shows the prototype device structure, where a positive (negative) V_{oc} corresponds to the up (down) polarization. V_{oc} as well as the polarization state could be read once there is light illumination on the device. This is a non-destructive operation process without any electric energy consumption, which represents an advantage compared with the traditional FeRAM devices.

Regarding to the light-induced effect, Kundys *et al.* recently reported an interesting phenomenon that the size of BFO crystal can be modulated by light illumination.¹⁸⁹ In this experiment, a bulk mono-domain BFO crystal was used, and a positive size change was observed when the sample was illuminated by light. The observation of photostriction indicates the possibility of realizing mechanical, magnetic,

electric, and optical functionalities in monolithic multifunctional devices.

IV. FINAL REMARKS AND OUTLOOKS

In Secs. I–III, we used several material systems to highlight not only the groundbreaking achievements but also some grand challenges in applying multiferroic materials in thin-film-based technologies. These challenges are related to issues such as excessive leakage current, weak magnetism, and elusive coupling mechanism between various ferroic orders. Complementary experimental and theoretical efforts are needed to address the materials challenges on composition and defect controls, substrate and strain engineering, as well as post-growth processing and patterning. In order to guide the thin film growth, advanced structural characterization and spectroscopic tools should be developed to enable nanoscale imaging and measurements.

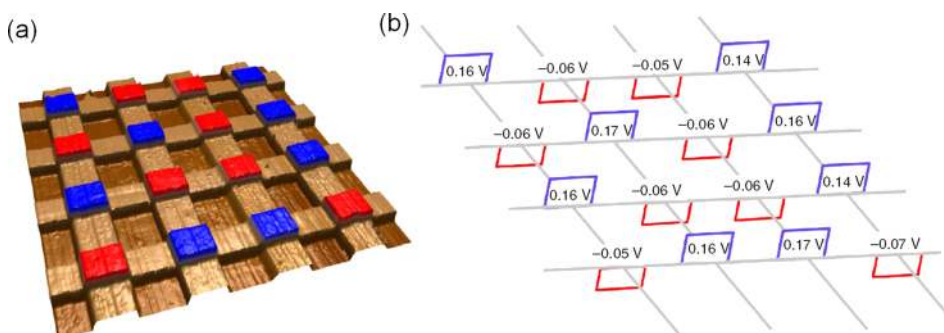


FIG. 18. Performance of a prototype 16-cell ferroelectric memory with the cross-bar architecture. (a) Topography of the device with preset polarization direction. Blue: polarization up, red: polarization down. (b) V_{oc} of all 16 cells are indicated. These were measured under 20 mW/cm^2 light illumination. Adapted with permission from Guo *et al.*, Nat. Commun. 4, 1990 (2013). Copyright 2013 Nature Publishing Group.

Discovering new multiferroic materials remains as the top priority in defining the future research directions. On the one hand, in Bi-based multiferroic materials, both ferroelectric and magnetic phase transitions can be higher than room temperature, and the polarization can reach the values found in classic ferroelectric materials. However, the magnetoelectric coupling is often very weak in these materials. On the other hand, in the multiferroics with spin origin, strong magnetoelectric effects have been observed due to the strong coupling between the ferroelectric and magnetic orders. But these materials generally show very low T_C , and the spontaneous polarization is about four orders of magnitude smaller than those of classic ferroelectrics. These drawbacks observed in the existing multiferroic materials plague the potential applications, which in turn motivate researchers to look for new high-performance materials.

In recent years, much research attention has been focused on multiferroic thin films and heterostructures, and indeed significant progresses have been made, and new device concepts were proposed and realized. Nevertheless, more efforts are desired to effectively bridge the fundamental research and technical applications. For instance, although combining ferroelectricity and spintronics in ME devices provides the possibility of nonvolatile memories with ultralow energy consumption, there has been no demonstration of reliable exchange-coupled multiferroic heterostructure operating at room temperature with high endurance and retention. Furthermore, more attempts are needed to advance domain engineering to either make mono-domain films to reproduce/improve the bulk-like physical properties or control domain structures to render novel functionalities in sensing and photovoltaic devices. Continuously improving the switching capability of ultrathin multiferroic films and elucidate the mechanism on the nanoscale are critical for device applications like ferroelectric/multiferroic tunneling junctions and nonvolatile memories. The dimensions of modern memory devices are often within the regime of tens of nm, but little is known how the multiferroic materials will behave at such small scales. Another important research front is compositional and structural interface/surface engineering on the atomic scale, which again is very challenging and remains largely unexplored for many multiferroics-based heterostructures. We believe that more significant breakthroughs in the field of multiferroic thin films and heterostructure devices will be witnessed in the near future.

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