

Multiple superionic states in helium-water compounds

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Superionic states are phases of matter that can simultaneously exhibit some of the properties of a liquid and of a solid. For example, in superionic ice, hydrogen atoms can move freely while oxygen atoms are fixed in their sublattice. “Superionicity” has attracted much attention both in fundamental science and applications. Helium is the most inert element in nature and it is generally considered to be unreactive. Here we use *ab initio* calculations to show that He and H₂O can form stable compounds within a large pressure range which can exist even close to ambient pressure. Surprisingly, we find that they can form two previously unknown types of superionic states. In the first of these phases the helium atoms exhibit liquid behavior within a fixed ice-lattice framework. In the second of these phases, both helium and hydrogen atoms move in a liquid-like fashion within a fixed oxygen sublattice. Because the He-O interaction is weaker than the H-O interaction, the helium atoms in these superionic states have larger diffusion coefficients and lower “melting” temperatures than that of hydrogen, although helium is heavier than hydrogen. The insertion of helium atoms substantially decreases the pressure at which superionic states may be formed, compared to those in pure ice.

The pioneering work of Demontis *et al.* [1] and Cavazoni *et al.* [2] led to studies of the “hot ice” layer between the rocky core and gaseous atmosphere in Uranus and Neptune, and proposed a surprising new phase between the solid and the fluid. This is a “superionic” state which is characterized by a fixed sublattice of oxygen or nitrogen atoms, while the hydrogen atoms diffuse almost freely throughout the sublattice. Since then, many theoretical and experimental studies have been devoted to investigating this important state of matter [3–20]. For instance, experimental electrical conductivity measurements [3, 4] and Raman signals [5] of water under compression indicate the existence of superionic states. The superionic water seems to be adjacent to the ordered ice VII and ice X, and significant ionic conductivity is found. [10] Very recently, Millot *et al.* [19, 20] investigated water ice under shock compression conditions and showed that ice melts near 5000 K at 190 GPa, which is close to the conditions found in the interiors of planets, and may have connections to superionic states.

Theoretical simulations were used to investigate the phase diagram of superionic water under conditions that may be found in planetary interiors.[7, 8] Recent simulations suggested that the oxygen sublattice in superionic water experiences a complicated evolution under

compression, with phases such as bcc, fcc, closed-packed and $P2_1/c$, etc. [11, 12]. To study these transformations, thermodynamic potentials and entropies for superionic water were calculated. [14] Phases of superionic water (VII' and VII'') were proposed, and [15, 18] superionic states in ammonia and ammonia-water mixtures have also been investigated [9, 13, 16, 17]. For instance, Bethkenhagen *et al.* [13, 16] studied equations of state of mixtures of water, ammonia, and methane, and developed a new model of the interior structure of Uranus. Jiang *et al.* [17] found an ionic phase in ammonia dihydrate, which transforms into a superionic phase under high temperature and pressure. Due to the chemical similarity of hydrogen and lithium, the mechanism of hydrogen diffusion in the superionic state has been used to explore ionic conductivity in electrodes and electrolyte materials, especially in lithium-based battery materials [21–23]. It seems that superionic states also have connections with the recently discovered copper-based thermoelectric materials [24, 25].

Knowledge of the behavior of helium at different temperatures and pressures is key to understanding the nature of celestial bodies, as it is the second most abundant element in the universe after hydrogen and it is also present in large quantities in the atmospheres of giant planets such as Uranus and Neptune. Helium, as the most inert element in the periodic table, is generally considered to be unreactive due to its stable closed-shell electronic configuration with filled s valence orbitals. Pres-

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sure is often used to explore new states of matter. Even a material as inert as helium can react with some elements and compounds under high pressure. For instance, a mixture with other inert gases [26, 27], such as nitrogen [28, 29], reacts with sodium [30], iron [31] or iron peroxide [32], alkali oxides or sulfide compounds [33] and alkaline earth fluorides [34]. The addition of helium can also reduce the pressure at which polymerization of nitrogen may occur. [35]. It has been reported that helium can react with water to form $\text{He}(\text{H}_2\text{O})_2$ at very high pressures (297 GPa) [36]. Teeratchanan and Hermann [37] recently found that helium can fill the voids in ice clathrates at very low pressures.

However, there is still a gap between the pressure of a few GPa and that of 300 GPa which has not been explored in the helium-water system, although this turns out to be the pressure range in which superionic states can emerge in ice. On the other hand, helium compounds are not easily formed and superionicity in helium-based structures has not so far been reported. Moreover, the diffusive motions of helium in these compounds are also unknown. Beyond the “hot ice” layer in Uranus and Neptune, helium is gaseous, which motivates exploration of the relationship between helium and water at low and medium pressures.

Results

Crystal structures. We have used first-principles crystal-structure searching techniques to determine the most stable phases of various compositions of He- H_2O . This has led us to predict two different stable stoichiometries, HeH_2O and $\text{He}_2\text{H}_2\text{O}$, which have lower formation enthalpies than mixtures of H_2O and He at 2–8 and 8–92 GPa, respectively, as shown in the convex hulls and the phase diagram of the pressure-components in Fig. 1 (a) and (b). These new phases adopt the tetragonal $I4_1md$ HeH_2O structure and the cubic $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$ structures, the symmetry of the system changes from $I4_1md$ to $Fd\bar{3}m$ at around 55 GPa. At low pressures the HeH_2O and $\text{He}(\text{H}_2\text{O})_2$ compositions become energetically favorable. Our calculations suggest that the $I4_1md$ HeH_2O phase and the previously proposed clathrate structure $Cmc2_1$ phase $\text{He}(\text{H}_2\text{O})_2$ [37] are stable even close to ambient pressure. We also note that vdW effects play a dominant role in the stability of He- H_2O compounds under pressure, and the effects of volume reduction is also a key element, especially in $\text{He}_2\text{H}_2\text{O}$.

Our searches also provide other candidate structures that have enthalpies that are very close (less than 1 meV/atom) to the lowest enthalpy structures presented in the main text. For instance, the energy of $P4_32_12$ HeH_2O is very close to that of $I4_1md$ HeH_2O ; the $Cmc2_1$ $\text{He}_2\text{H}_2\text{O}$ structure has a similar enthalpy to that of $I4_1md$ $\text{He}_2\text{H}_2\text{O}$; while the enthalpy of a $P6_3/mmc$ $\text{He}_2\text{H}_2\text{O}$ phase is similar to that of $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$. The relevant structures are listed in Table I in the Supplemen-

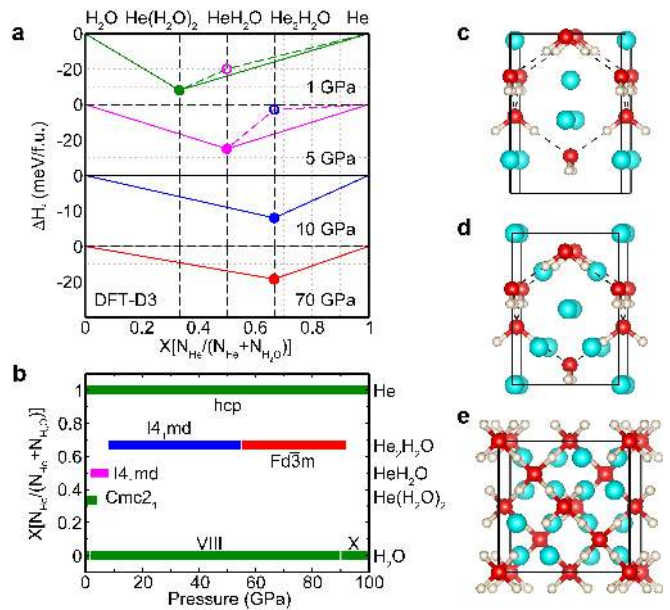


FIG. 1. **Thermodynamics of the He- H_2O system and crystal structures of the stable compounds.** (a) Convex hull for formation enthalpies (ΔH_f , with respect to He and H_2O) at different pressures, calculated with the DFT-D3 functional. (b) Pressure-composition phase diagram of the He- H_2O phases (magenta, blue and red lines) discovered in this work, together with the previously known phases (green lines) below 100 GPa. (c-e) Crystal structures of three new phases: (c) $I4_1md$ HeH_2O , (d) $I4_1md$ $\text{He}_2\text{H}_2\text{O}$ and (e) $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$.

tary Information. It is interesting that the ice framework of $P6_3/mmc$ $\text{He}_2\text{H}_2\text{O}$ is close to that of hexagonal ice, while the ice framework in $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$ appears similar to cubic ice.

As shown in Fig. 1 (d) and (e), the H_2O molecule sublattice in $I4_1md$ and $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$ are similar to those of ice VIII and ice X, respectively. As recently shown by Bronstein *et al.*[38], O–H–O bond symmetrization occurs at around 90–100 GPa when the protons are considered as classical particles, and 60–65 GPa for quantum protons. Therefore the presence of helium significantly decreases the pressure at which hydrogen-bond symmetrization occurs in the helium-water system.

Diffusion of atoms. To study the dynamical properties of the predicted water-helium compounds we have performed extensive *ab initio* molecular dynamics (AIMD) simulations within the pressure range 10–120 GPa and the temperature range 200–2600 K. Diffusion coefficients were calculated for the oxygen, hydrogen and helium atoms from their mean-square displacements (MSD). Superionic water is usually classified as one of three phases in terms of the diffusion coefficient of the H and O atoms: the solid phase ($D_O = 0$ and $D_H = 0$), the superionic (SI) phase ($D_O = 0$ and $D_H > 0$) and the fluid phase

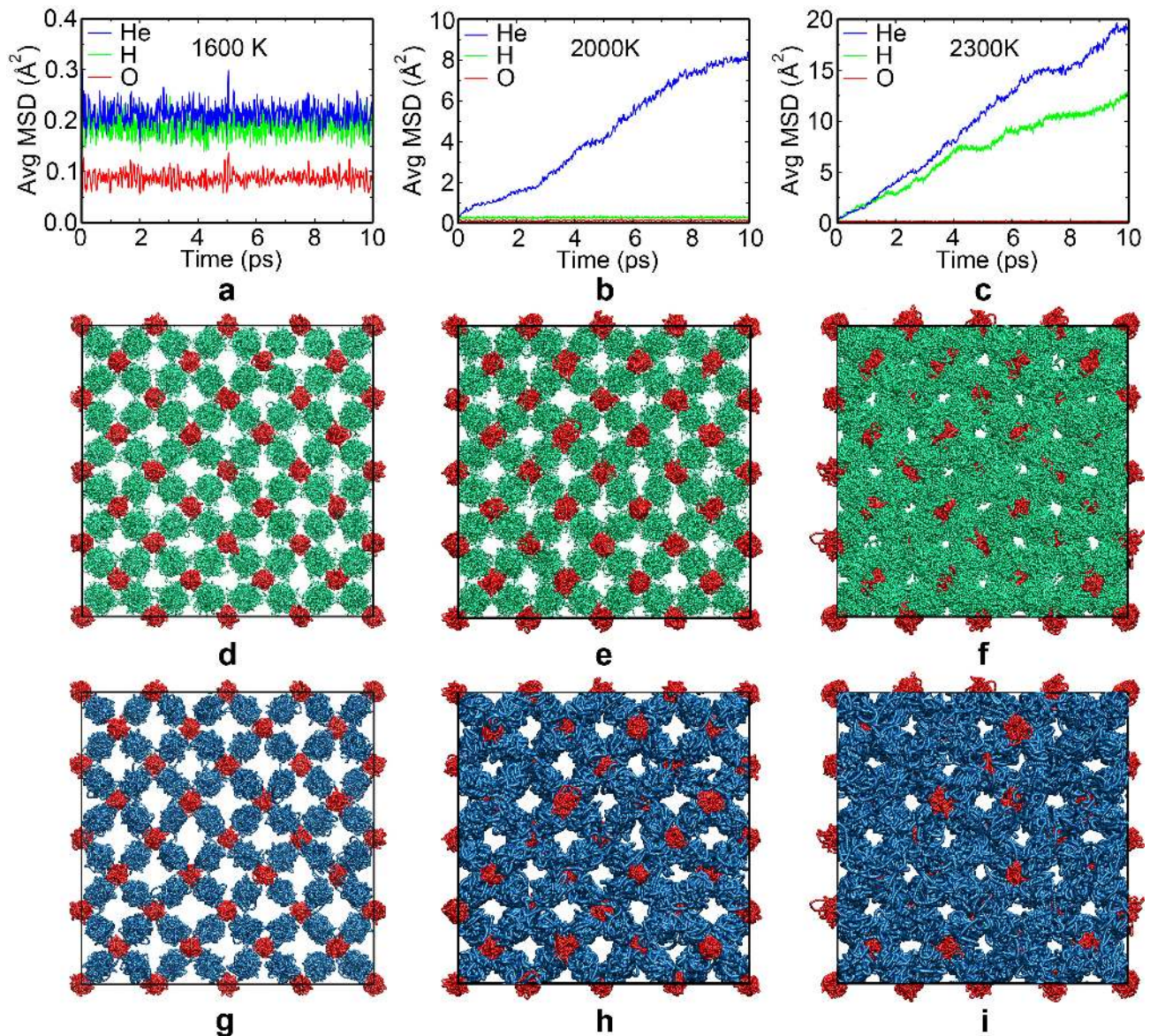


FIG. 2. Behavior of H (green) and He atoms (blue) compared to O atoms (red) in $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$ from AIMD simulations at 1600 K, 2000 K and 2300 K. (a-c) The averaged mean squared displacements (MSD) for the H, He and O atoms from AIMD simulations at different temperatures. (d-i) Representation of atomic trajectories in one supercell from the simulations from the last 5 ps run representing the three distinct phases: the solid phase (1600 K), the superionic He phase (2000 K), *SI-I*, and superionic He and H phase (2300 K), *SI-II*.

($D_O > 0$ and $D_H > 0$). Surprisingly, in our hydrated helium system we found a region of superionicity with a new diffusive helium phase ($D_O = 0$, $D_H = 0$ and $D_{He} > 0$) that we have named as *SI-I*, and a coexisting diffusive helium and hydrogen phase ($D_O = 0$, $D_H > 0$ and $D_{He} > 0$) named *SI-II*, as shown in Fig. 2 (a-c). We have also confirmed our results for the radial distribution functions of the averaged structures, as shown in Supplementary Fig. S1. To confirm the superionic features we have distinguished the two superionic phases (*SI-I* and *SI-II*) by comparing their atomic trajectories from sim-

ulations at around 90 GPa, as shown in Fig. 2 (d-i).

The Hydrogen and Helium trajectories overlap with one another, and for clarity we show them in separate plots. Therefore in Fig. 2 (d-f) only the oxygen and hydrogen atoms are plotted, while in Fig. 2 (g-i), only the oxygen and helium atoms are plotted. At around 90 GPa and a starting temperature below 1600 K, the atoms are tethered at their starting positions and vibrate around them. From the diffusion constants of the atoms ($D_O = 0$, $D_H = 0$ and $D_{He} = 0$) one finds that helium hydride maintains the solid phase under these conditions.

However, when the temperature is increased to 2000 K, although the oxygen and hydrogen atoms vibrate on their original sublattices, the helium atoms vibrate much more strongly and even jump to neighboring sites which results in a non-zero diffusion constant $D_{He} = 0.14 \times 10^{-8} \text{ m}^2/\text{s}$. At 2300 K both hydrogen and helium atoms are delocalized from their initial sites and their diffusion coefficients are both non-zero ($D_H = 0.21 \times 10^{-8} \text{ m}^2/\text{s}$ and $D_{He} = 0.33 \times 10^{-8} \text{ m}^2/\text{s}$). The diffusion coefficients calculated from the velocity autocorrelation functions are very similar to those obtained from the MSD, as shown in Table II of the Supplementary Information. Both helium and hydrogen atoms have larger diffusivities and therefore larger probabilities of moving into the interstitial spaces of the oxygen sublattice. Finally, increasing the temperature beyond 2400 K leads to melting of the helium hydrate and the atoms diffuse freely (not shown here).

Our simulations show that the three atomic species in helium hydrate: oxygen, hydrogen and helium, have different “melting” temperatures above which diffusion occurs $T_{He} < T_H < T_O$. The law of equipartition states that in equilibrium the energy should be equally distributed among the degrees of freedom. Therefore with the same kinetic energy, the lighter atoms should move faster in non-interacting systems. Within our helium-water system the helium atoms have a higher mobility and a lower “melting” temperature than hydrogen atoms, although helium is heavier than hydrogen.

To investigate the reasons for this abnormal diffusive behavior we calculated the electron localization function (ELF) of the hydrate $Fd\bar{3}m$ phase at 0 K, as shown in Supplementary Fig. S2. We plotted an ELF isosurface (isovalue = 0.7) in the conventional unit cell and a cross-section along the $\langle 011 \rangle$ plane. This demonstrates that electrons localize along the bonds between the oxygen and hydrogen atoms and are isolated in the helium atoms. This shows that the O–H interactions arise from strong covalent bonds while the helium atoms have weak vdW interactions with the H_2O framework. This results in a higher diffusion barrier for hydrogen atoms than for helium in the finite temperature superionic phases.

Phase diagram. Inspired by the temperature-induced features in helium hydrate discussed above, we expanded the pressure range studied to explore the superionic region from ambient pressure up to about 100 GPa with pressure steps of 20 GPa. In superionic water the two different “melting” temperatures of hydrogen and oxygen in ice divide its phase diagram into three regions: solid, superionic, and liquid. As shown in Fig. 3, the three “melting” temperatures of helium, hydrogen and oxygen divide the phase diagram of helium hydrate into four distinct regions: the solid, superionic helium ($SI-I$), superionic helium + hydrogen ($SI-II$), and fluid phases. As expected, the superionicity is enhanced with increasing

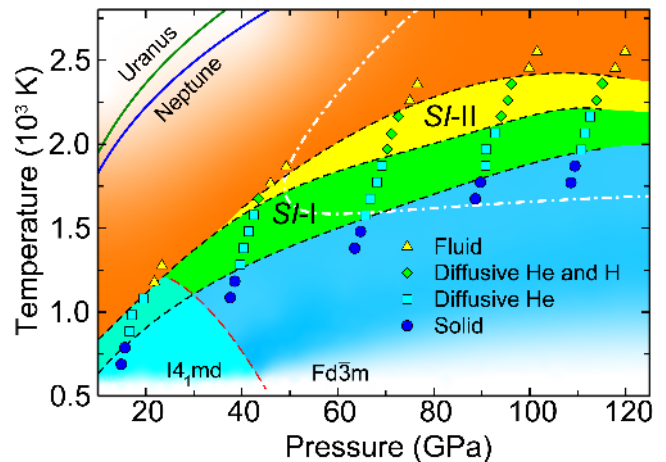


FIG. 3. **Proposed phase diagram of the helium-water system at high pressures obtained from our structure searches and AIMD simulations.** Symbols represent four distinct thermodynamic states sampled in our simulations: circle, solid state; square, He diffusive state ($SI-I$); diamond, both He and H diffusive state ($SI-II$); and triangle, fluid state. Black dashed lines were fitted to the phase transition boundaries. Red dashed lines distinguish the two predicted solid phases: $I4_1md$ and $Fd\bar{3}m$, as well as two types of H_2O sublattice ($I4_1md$ and $Fd\bar{3}m$) in the $SI-I$ region. Isentropes for Uranus and Neptune (Dark green and blue solid lines) and phase boundary for superionic pure water (white dash-dotted line) are taken from Ref. [8].

pressure and the superionic helium region ($SI-I$) exists over the entire pressure range studied, while the superionic helium + hydrogen phase ($SI-II$) is stable only above 40 GPa. The pressure-induced transition from $I4_1md$ to $Fd\bar{3}m$ is in fact a continuous second-order phase transition, as shown in Supplementary Fig. S3. The temperature may therefore have a critical influence on the transition pressure between these two phases at high pressure.

Sun *et al.* [12] recently reported that the sublattice of the oxygen atoms in superionic water shows a complicated sequence of phase transitions. Examination of the trajectories in the superionic region obtained by averaging atomic positions shows that the oxygen sublattices in both $SI-I$ and $SI-II$ retain an FCC arrangement in helium hydrate, which has the same oxygen sublattices in solid $I4_1md$ and $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$. Moreover, we have calculated radial distribution functions for these averaged structures and compared them with the initial zero-temperature structure. At 30 GPa the H_2O sublattice maintains its original positions as in the $I4_1md$ phase at low temperatures and then transforms into a sublattice of the $Fd\bar{3}m$ phase with increasing temperature, as shown in Supplementary Fig. S4.

Discussion

We have also studied superionicity in the low pressure phase by gradually increasing the temperature in

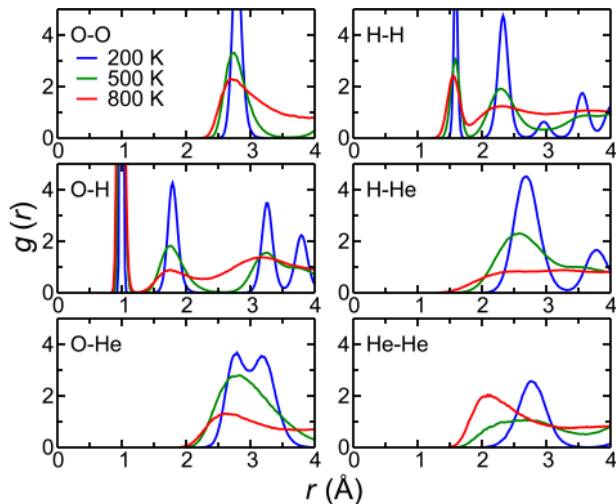


FIG. 4. **Radial distribution functions $g(r)$ of the $141md$ HeH_2O phase.** The *AIMD* simulations are performed at around 3 GPa and heating to around 200 K (blue lines), 500 K (green lines) and 800 K (red lines), corresponding to the solid phase, diffusive helium phase (*SI-I*) and fluid phase, respectively.

the *AIMD* simulations. The RDFs in Fig. 4 obtained from simulations at three different temperatures clearly indicate the presence of three states: the solid at 200 K, superionic helium at 500 K, and a fluid phase at 800 K. HeH_2O maintains its crystalline form at 200 K, and almost all of the atomic pairs maintain their isolated peaks in the RDF, except for the combination of the first two peaks in the oxygen-helium RDF which exhibit large thermal fluctuations. The thermal fluctuations increase rapidly with heating and the peaks in the oxygen-oxygen, oxygen-hydrogen, and hydrogen-hydrogen RDFs are slightly broadened, but still show the characteristic peaks of a sublattice of H_2O undergoing large amplitude vibrations.

In the superionic helium (*SI-I*) phase at 500 K the thermal fluctuations increase rapidly and the peaks in the oxygen-oxygen, oxygen-hydrogen, and hydrogen-hydrogen RDFs are slightly broadened, but they still show the characteristic peaks of a sublattice of H_2O undergoing large amplitude vibrations. The RDF involving helium atoms shows only one maximum and then converges to a constant intensity, which represents the behavior of a liquid or a glass. Finally, at 800 K in the fluid phase the H_2O sublattice distorts from the hydrogen-hydrogen RDF. We find that the first peak still exists at the same position even in the fluid, and the O-H distance in the superionic state remains similar to that in ice.

Previous work [14] shows that the quantum correction to the internal energy in MD simulations is affected by the pressure and temperature in water ice. Our results

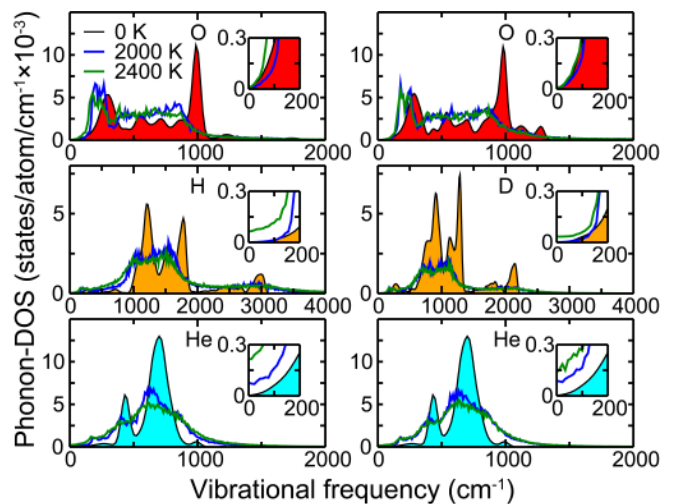


FIG. 5. **Vibrational density of states of $Fd\bar{3}m$ phase $\text{He}_2\text{H}_2\text{O}$ (left) and $\text{He}_2\text{D}_2\text{O}$ (right).** Colored areas under black curves give the Phonon-DOS of O (red), H/D (orange) and He (cyan) from static phonon calculations at 0 K. The blue and dark green lines represent the vibrational DOS of each atomic species in the *SI-I* phase at 2000 K and *SI-II* phase at 2400 K, respectively, calculated from the Fourier transform of the velocity autocorrelation function. The low frequency regions are enlarged in the insets and the zero/non-zero vibrational DOS at zero frequency shows the fixed/diffusive behavior of O, H/D, and He at different temperatures.

(Supplementary Table II) show that the nuclear quantum corrections u_{qc} for helium-water compounds are on a similar scale to those found in the literature for ice [14]. This is relatively small compared with the internal energy u_{md} , and therefore it does not greatly affect the occurrence of superionic phases in helium-water compounds.

In addition, Hermann *et al.* [39] studied zero-point energies of water ice at megabar pressures by replacing hydrogen atoms with its isotopes, deuterium and tritium. The isotope effect can also emerge in the dynamical properties such as the diffusion coefficient and vibrational spectra. Here, we estimate the influence of nuclear quantum effects in the *SI-I* phase (at 2000 K) and *SI-II* phase (at 2400 K) by comparing the vibrational density of states in $\text{He}_2\text{H}_2\text{O}$ and $\text{He}_2\text{D}_2\text{O}$. As shown in Fig. 5, with increasing mass, in the zero temperature phonon DOS, the high frequency phonon peak decreases from about 3000 cm^{-1} for hydrogen, to about 2100 cm^{-1} for deuterium. At 2000 K, both H and D are fixed in their sublattices and have very similar vibrational frequencies to their corresponding zero temperature phonon frequencies. As shown in the insets, He atoms have a non-zero diffusive coefficient at zero frequency, which represents the *SI-I* phase. At 2400 K, the H and D, as well as the He atoms have non-zero diffusive coefficients at zero frequency, while only the oxygen atoms are fixed, which cor-

responds to the *SI-II* phase. These results indicate that nuclear quantum effects do not significantly affect the existence of the superionic states in helium-water compounds.

In summary, we have used a combination of *ab initio* crystal structure searches and *AIMD* simulations based on DFT to perform our calculations. We have systematically explored the helium-water phase diagram below 100 GPa and found three thermodynamically stable solid phases: the tetragonal $I4_1md$ HeH_2O , the $I4_1md$ $\text{He}_2\text{H}_2\text{O}$ and the cubic $Fd\bar{3}m$ $\text{He}_2\text{H}_2\text{O}$ phases. The pressure at which hydrogen-bond symmetrization occurs is reduced to around 55 GPa by introducing helium. More interestingly, we find a superionic helium region in the helium hydrate phase diagram with highly mobile helium atoms and a fixed sublattice of ice at relatively low temperatures. Further heating leads to a superionic phase in which the motions of hydrogen and helium atoms give rise to superionicity, while the oxygen atoms vibrate around the original sublattice. These three atomic types in the helium hydrate exhibit abnormal “melting” properties ($T_{\text{He}} < T_{\text{H}} < T_{\text{O}}$) marked by a change in diffusion rates, molecular dynamics trajectories and radial distribution functions. These properties divide the phase diagram into four distinguishable regions: solid, superionic helium, superionic helium + hydrogen and fluid. At relatively low pressures (below 40 GPa), the superionic helium + hydrogen region is absent and the superionic helium region remains close to ambient pressure. The insertion of helium substantially reduces the pressures at which superionic states can be formed compared to pure ice which may be more easily accessed in future experiments. Although the pressures and temperatures in this work are somewhat lower than those in the isentropes of Uranus or Neptune, the insertion of helium could alter the superionicity of pure water, which may still exist in Uranus or Neptune. Meanwhile, as the second most abundant element, helium may exist in planets or moons with different masses, compositions and distances from their own main stars. These planets and moons may have different isentropic conditions which could allow the formation of superionic He- H_2O compounds.

Online content

Any methods, additional references, Nature Research reporting summaries, source data, statements of code and data availability and associated accession codes are available at <https://xxx.xxx-xxxxx>

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Authors contribution

J.S. conceived the project. J.S. and H.T.W. led the project. C.L., H.G., Y.W. C.J.P performed the calculations. C.L., H.G., C.J.P and J.S. analyze the data. C.L., J.S., R.J.N, H.T.W. and D.X. wrote the manuscript. All authors discussed the results and commented on the manuscript.

C. L. and H. G. contributed equally to this work.

Competing financial interests. CJP is an author of the CASTEP code, and receives royalty payments from its commercial sales by Dassault Systemes.

Additional information

Supplementary Information accompanies this paper is available at <http://xxx.xxx.xxx>

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Method

We performed variable-composition structure predictions implemented in a machine-learning accelerated crystal structure search method[1]. The crystal structures obtained were cross-checked with results from the *ab initio* random structure searching approach (AIRSS) [2, 3], which gave very similar results. The density functional theory (DFT) calculations were performed using the Vienna *ab initio* simulation package (VASP) [4] and the projector augmented-wave method and the generalized gradient approximation (GGA) and the Perdew-Burke-Ernzerhof exchange correlation functional (PBE). [5]. We employed a plane wave cutoff energy of 720 eV and a dense Monkhorst-Pack Brillouin zone integration grid with a resolution of $2\pi \times 0.025 \text{ \AA}^{-1}$. The relaxed ionic positions and cell parameters provided forces that are smaller than 10^{-5} eV and $eV/\text{\AA}$, respectively. The CASTEP code was used for the AIRSS searches, similar convergence parameters as used in VASP were employed [6]. To account for the vdW interactions we used the DFT-D3 [7], optB88-vdW [8] and rev-vdW-DF2 [9] functionals to cross check the quality of the energy minimization and the calculated zero-point energy. The results obtained with different functionals are very similar, see Supplementary Fig. S5. Phonon calculations show that the newly predicted structures are dynamically stable, as can be seen in Supplementary Fig. S6. Phonon spectra of the $I4_1md$ HeH₂O phases at 0 GPa do not exhibit imaginary vibrational frequencies, which indicates that it may be quenchable even to ambient pressure. Results for the zero point energy (ZPE), finite temperature Gibbs free energy, and tests of the dynamical stability of the He-H₂O compounds are available in Fig. S7 and S8 in the Supplementary Information. Phonon calculations were performed using the phonopy package [10]. *Ab initio* molecular dynamics (AIMD) simulations were performed in $4 \times 4 \times 4$ supercells (with 256 atoms for HeH₂O and 320 atoms for He₂H₂O, respectively) with Γ -centred k -point sampling. The results of convergence tests for the k -point mesh and the finite size effects are shown in Table III of the Supplementary Information. A

Nose-Hoover thermostat was used to perform the *NVT* simulations. Runs with 7000 steps were carried out with a time step of 1 fs, the initial 2 ps were used for thermalization and the final 5000 steps of each trajectory were used to extract the statistical quantities. Some trajectories were extended to 12 ps to check the stability of the simulations.

Data Availability

The data that support the plots within this paper and other findings of this study are available from the corresponding authors upon reasonable request.

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