Nanomechanics of collagen microfibrils

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Summary

Collagen constitutes one third of the human proteome, providing mechanical stability, elasticity and strength to organisms and is thus the prime construction material in biology. Collagen is also the dominating material in the extracellular matrix where its stiffness controls cell differentiation, growth and pathology. We use atomistic-based hierarchical multiscale modeling to describe this complex biological material from the bottom up. This includes the use and development of large-scale computational modeling tools to investigate several aspects related to collagen-based tissues, including source of visco-elasticity and deformation mechanisms at the nanoscale level. The key innovation of this research is that until now, collagen materials have primarily been described at macroscopic scales, without explicitly understanding the mechanical contributions at the molecular and fibrillar levels. The major impact of this research will be the development of fundamental models of collagenous tissues, important to the design of new scaffolding biomaterials for regenerative medicine as well as for the understanding of collagen-related diseases.

KEY WORDS: atomistic simulations, biomechanics, collagen, fibril, nanomechanics.

Introduction

The word collagen originates from the Greek word κόλλα (*kolla,* meaning "glue") due to its ancient use as a glue source – obtained though the boiling of animal skin and collagen-rich tissues from Egyptians about 4,000 years ago[1]. In a broader sense, collagen could be seen as the "glue" of our body, holding it together by providing elasticity and strength to several tissues where a mechanical functions is needed, such as skin, cartilage, tendons and bones[2, 3].

From the structural point of view, collagen-rich tissues are built with the collagen fibril as fundamental building block. These fibrils have a diameter in the range of 30 to 500 nm, a length up to the millimeter range and are assembled in complex hierarchical assemblies, whose structure depend on the particular tissue (Fig. 1).

At the lowest hierarchical level there is the collagen molecule (also called *tropocollagen*), that is a rod-like molecule with a length of about 300 nm and a diameter of about 1.5 nm, made of three separate chains folded in the characteristic triple helical configuration[4, 5]. According to the Hodge-Petruska model[6] a structural model of collagen fibrils proposed in 1964 molecules in a fibril are deposited side by side and parallel but staggered with respect to each oth-
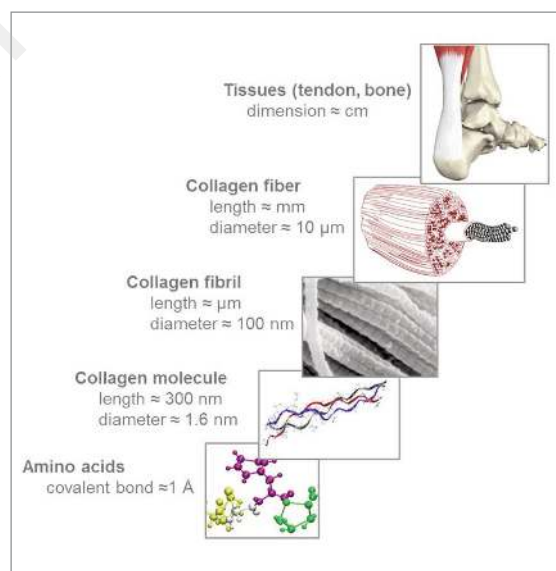

Figure 1. Hierarchical structure of collagen protein materials. Each collagen molecule is made of three peptide chains that form the ≈300 nm long triple helical collagen molecule. Collections of collagen molecules aggregate both in lateral and longitudinal directions to form fibrils. Fibrils in cornea are normally thin (≈30 nm) and uniform in diameter, while tissues such as tendon contain a wide-ranging distribution of diameters (100-500 nm). Fibrils include tiny hydroxyapatite crystals in bone tissue, which provide stiffness and compressive load resistance. In tendons and ligaments multiple fibrils make up collagen fibre, formed with the aid of proteoglycans.
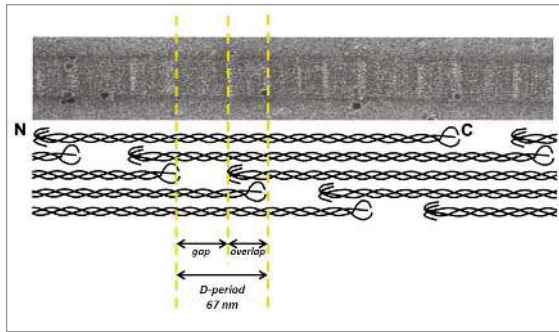
Figure 2. D-period of collagen fibrils. Electron microscope of a collagen fibril (*top panel*) and schematic representation of the axial arrangement of molecules in the D-periodic fibril (*bottom panel*).

er, where the molecular axes are also parallel to the fibril direction. This structure creates an observable periodicity known as the *D*-period whose length is *D*=67 nm, in which two region can be observed, the gap and overlap regions, emerging due to the fact that the length collagen molecule is not a multiple of the *D*-perioditself (Fig. 2). A particularly important feature for the mechanical properties of fibrils is the presence of enzyme-induced covalent cross-linking between molecules, which develops only with maturation of the tissues[7].

At the next level of the hierarchy, the organization of the collagen structure varies greatly depending on the tissue. In tendons and ligaments, multiple fibrils make up the collagen fiber, which are formed with the aid of cross-linking macromolecules such as proteoglycans. In bone, the organic collagen protein matrix alone is not sufficient to provide the stiffness and resistance to compression required for this tissue (which has to carry considerable loads) and additional stiffening is provided by the inclusion of mineral hydroxyapatite crystals into collagen fibrils and particularly in the gap region[8, 9]. Skin and artery walls need to be flexible but arteries also need to resist blood pressure. This implies yet a different arrangement of collagen fibrils in combination with elastomeric molecules, such as elastin.

Due to the biological importance of collagen-based tissues there have been a wealth of investigation concerning the relationship between structure and properties in these complex materials, starting from early works (dated in the 50s) on of the structure of collagen molecules[4]. However, there are still open questions (e.g., concerning the mechanism of load transfer between the hierarchical scale of bone and tendons, or the onset of collagen-related diseases). A very promising technique to complement experiments in addressing these questions is represented by multi-scale modeling. In the following of this Chapter, successful application of atomistic and coarse-grain modeling techniques for the study of collagen materials are presented.

Visco-elastic properties of collagen molecules

In vertebrates, locomotion and movements are achieved through the generation of muscular forces that are then transmitted to joints. The force transmission (mechan-

otransduction), which involves the storage, release and dissipation of energy, is provided by connective tissues such as ligaments and tendons[10, 11]. Thus, in these tissues viscoelasticity is a fundamentally important feature, as both viscous (time-dependent) and elastic (time independent) contributions determine how ligaments and tendons accomplish their function as mechanotransducers. The mechanical behavior of these connective tissues is directly related to their complex hierarchical structure and to their specific macromolecular components[12]. The lowest hierarchical scale of several load-bearing tissues is represented by collagen type I molecules[13, 14].

At the macro-scale (i.e., whole tissues and collagen fibers), the mechanical investigation of collagen-based tissues has been performed for several decades. As a consequence, it is well known that collagen-rich tissue present viscoelastic behavior, as established from a larger number of creep and relaxation tests that have been performed on both tendons and ligaments[15-17]. Based on experimental data, and starting from the pioneering work of Fung[18], several constitutive and structural models have been developed to model the viscoelastic behavior of collagen at the tissues scale[19-24].

On the other hand, fewer studies focused on the viscoelastic properties at smaller scales. At the fibril level, earlier investigations have been performed through small angle X-ray scattering[25] to assess the fibril deformation inside tissue specimens. However, in this set-up the load is not directly applied to single fibril and hence the response is averaged over several fibrils. Direct experimental studies of single fibrils are relatively recent and made possible due to the use of atomic force microscopy or micro-mechanical systems which allowed the study of the elastic[26-30] and viscoelastic properties of collagen fibrils[31, 32].

Ultimately, at the molecular level several studies have been performed using both experimental and computational procedures; however most of these investigations focused solely on the elastic properties[33-42]. For this reasons, despite the abundant investigation of the viscoelastic behavior at the macro-scale and the very recent works on collagen fibril viscoelasticity, relatively little is known about the molecular and fibrillar origin of the time-dependent properties of collagenous tissues. It has been speculated that the elastic behavior of these tissues is due to the stretching of cross-linked collagen molecules and thus fibrils, whereas the energy dissipation (the viscous behavior) is thought to involve sliding of molecules and fibrils by each other during the tissue deformation[12, 43]. However, there is still no clear understanding of the mechanisms behind the viscoelastic behavior of collagenous tissue, and on the role of each hierarchical scale in determining the overall mechanical properties. An important outstanding question is whether or not molecular-level load relaxation effects are important for the viscoelastic properties measured at larger scales.

An approach to investigate the molecular origin of collagen viscoelasticity, is the use of *in silico* tests to study collagen molecules from the level of amino acids upwards. In this way it is possible to obtain quantitative data on the time-dependent mechanical behavior of single collagen mole-
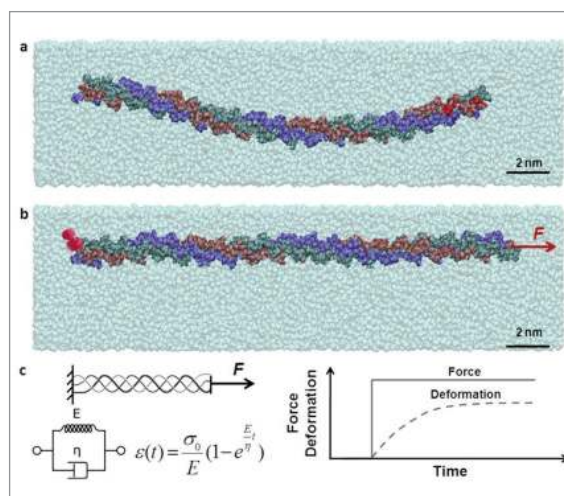
Figure 3. Snapshots of the collagen peptide in water box. Panel a shows the conformation of the full atomistic model of a collagen peptide solvated in water box and equilibrated for 30 ns. After equilibration the molecule is subjected to virtual creep tests: one end of the collagen peptide is held fixed, whereas the other end is pulled with constant force (from 300 pN to 3,000 pN) until end-to-end distance reaches equilibrium (Panel b). Panel c shows a schematic of the creep test; a constant force is applied instantaneously to the molecule and its response (deformation over time) is monitored. The mechanical response of collagen molecule is modeled using a KV model, from which molecular Young's moduls (E) and viscosity (η) are calculated.

cules in order to assess molecular-level viscoelastic properties, and to scale up properties from there to larger tissue levels. In this approach, Steered Molecular Dynamics simulations are used to perform *in silico* creep tests (i.e., constant load tests) of collagen molecules, fitting the deformation response over time with a Kelvin-Voigt (KV) model. The KV model is a simple constitutive model consisting of a spring and a dashpot in parallel (Fig. 3), where this approach allows us to compute the Young's modulus, the viscosity and the characteristic relaxation time of a single collagen molecule.

In order to perform constant force SMD simulations, the three N-terminal C_α atoms are kept fixed whereas the three C-terminal C_α atoms are subject to an instantaneous constant force. This set-up mimics a single molecule creep test, in which an instantaneous load is applied and the strain response in time is observed. The creep test simulations are run until asymptotic deformation and then strain-time curves obtained for collagen molecules during SMD simulations are fitted with the Kelvin-Voigt equation in order to estimate E (Young's modulus) and η (viscosity). The instantaneous stress σ_0 is calculated dividing the applied force by the cross-sectional area of collagen, assuming a round cross-section and a radius of 0.55 nm. The value of the radius is determined from dry collagenous tissue in which the lateral distance between molecules is found to be 1.1 nm[44].

When subjected to creep tests, the engineering strain of the molecule shows an exponential increase until as-
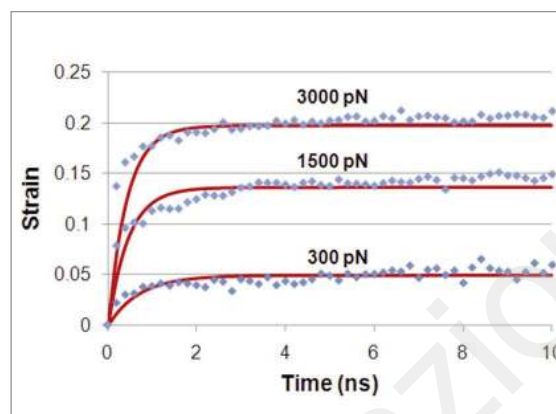

Figure 4. Single molecule creep test. Mechanical response of solvated collagen molecule to creep tests for three cases with increasing value of external force. Dots represent the experimental data, whereas curves represent the fitted curves using a Kelvin-Voigt model.

ymptotic value is reached (Fig. 4). This is the behavior typical of simple viscoelastic materials that can be characterized by a Young's modulus E, responsible for the elastic response, and a viscosity η, responsible for the viscous behavior. These results show that collagen molecule presents a non-linear elastic behavior, since the Young's modulus depends on the external load. In particular, for the loading conditions considered here E ranges from 6 to 16 GPa, a finding that matches several experimental[33, 34, 36, 37] and modeling studies[41, 45-47].

The collagen molecule viscosity has an average value of 3.84.±0.38 Pa·s and it is not significantly affected by the external load. Based on the elastic modulus and the viscosity, the characteristic relaxation time (defined, for a KV model, as η/E) is calculated, obtaining values in the range 0.24-0.64 ns and 0.13-0.27 ns for solvated and dry molecule, respectively. Although the elastic behavior has been previously investigated, no experimental data is available for the viscous component of a single collagen molecule. This could be attributed to the very fast relaxation time (on the order of nanoseconds) of single molecules, which hinders its assessment using available experimental techniques. However, a recent work[48] demonstrated that Atomic Force Microscopy (AFM) can be successfully used to assess the viscoelastic properties of a single polypeptide chain, in this case polystyrene. Within this technique, referred to as "nanofishing" by the authors of that study, an AFM cantilever is mechanically oscillated at its resonant frequency during the stretching process. This enables the estimation of stiffness and viscosity of a single polymer chain with the use of a phenomenological model (the authors used a KV model). The polystyrene viscosity per unit length reported by the authors is 2.6·10-9 Kg/s, which agrees well with the findings for collagen molecules, *i.e.*, ≈ 40·10-9 Kg/s (considering a peptide length of 20 nm). The slightly higher viscosity could be attributed to the fact that the polystyrene chain is a single strand, while the collagen peptide is in a triple helical configuration.

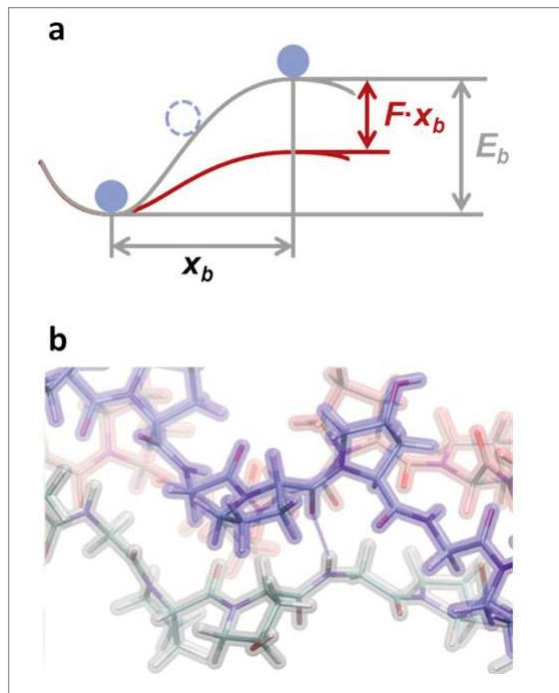It is of great interest to discuss whether the two elements

Figure 5. Statistical theory to predict bond rupture mechanics. The graph depicts the energy as a function of a deformation variable (a), along a particular pathway that leads to bond rupture, where E_b is the energy barrier corresponding to the transition state. Panel b shows an interchain H-bond in collagen.

of the KV model, i.e. the purely elastic spring and the purely viscous dashpot, have an actual physical meaning. A likely explanation would be that the elastic spring corresponds to the protein backbone, while the damping effect could be attributed to the interchain H-bonds. The backbone deformation include dihedral, angle and bond deformation, which are terms expressed by harmonic (or similar) functions in the molecular dynamics force field, and thus result in an elastic response to stretching. On the other hand, the viscous behavior may be due to the breaking and reforming of H-bonds, in particular H-bonds between the three collagen chains. Statistical mechanics based theories, and in particular Bell's model[49], has been applied to study the breaking of H-bonds (see, e.g. reference[50] Fig. 5). It has been shown that the velocity at which a H-bond breaks is a function of the external force:

$$v = \frac{x_b}{\tau_0} e^{-\left[\frac{E_b - F \cdot x_b \cos \theta}{k_b T}\right]}$$

where v is the velocity at which the H-bond breaks, x_b is the distance between the equilibrium state and the transition state, τ_0 is the reciprocal of the bond natural frequency, E_b is the bond energy, F is the applied force, θ is the angle between the direction of the reaction pathway of bond breaking and the direction of applied load F, k_b is the Boltzmann constant and T is the temperature. The equation above shows that the mechanical response of the H-bonds is time-dependent, matching the behavior of the dashpot in the KV model very well (for which the stress is a function of the loading rate). Therefore the time-dependent rupture of H-bonds are likely responsible for the dissipative behavior observed in collagen molecule mechanics.

Atomistic modeling of collagen fibrils

In order to complement experimental approaches, molecular modeling provides a powerful approach to describe the molecular mechanics of collagen. Earlier studies were based on short collagen-like peptides obtained from x-ray crystallography[51-54]. These early molecular simulation studies used these short collagen molecules[38, 39, 41, 46, 55-61] that were typically limited to less than 10 nm length or more than a factor of 30 smaller than actual molecules found in collagen tissues. The resulting elastic modulus of these short collagen peptides was found to be on the order of 4GPa, and thus much greater than the typical Young's moduli measured for macro-scale collagen tissues but in agreement with single molecule studies[33-36, 62]. In order to determine how collagen-based structures confer mechanical properties to tissues like skin, tendon and bone, and to identify how cells interact with the ECM, the understanding of the mechanics at different hierarchical levels and their interplay from a biochemical and molecular level upwards is essential. Earlier work has demonstrated that mechanical strain is distributed over distinct hierarchical levels (molecules, fibrils, fibres)[63-65] and that collagen tissue stretching involves concurrent deformation mechanisms. The significance of defining the material properties of collagenous tissues from the biochemistry level upwards is evident when considering the effect of mutations in collagen, which can result in incorrectly folded collagen protein that cause a variety of severe and sometimes deadly pathologies, such as Ehlers-Danlos syndrome or *osteogenesis imperfecta* (brittle bone disease)[66]. Early collagen microfibril and fibril models represent the supramolecular arrangement in collagenous tissues in a simplified way, using a two-dimensional lattice of mesoscopic beads[67, 68] or extremely short collagen peptides[38, 39, 41, 46, 55-60]. These models do not account for the biochemical details and are much smaller than the typical length-scales of collagen molecules found in collagen microfibrils and fibrils. The reason for these approximations was the lack of crystallographic details of the collagen molecule, which have been obtained only for short collagen-like peptides with lengths below ≈10 nm[51-23], until the work of Orgel and coworkers, that obtained the *in situ* structure of full length collagen type I molecule[69] (Protein Data Bank identification code 3HR2) (Fig. 6). This structure, obtained by employing conventional crystallographic techniques in x-ray fiber diffraction experiments, resolved for the first time the specific three-dimensional arrangement of collagen molecules in naturally occurring fibrils, including the N- and C-telopeptides.
Starting from the structure reported in[69], which includes only backbone alpha carbons and the primary sequence of *rattus norvegicus*, Gautieri et al.[70] used homology modeling to obtain a full-atom structure with the human collagen sequence (Fig. 7). The molecular packing topolo-
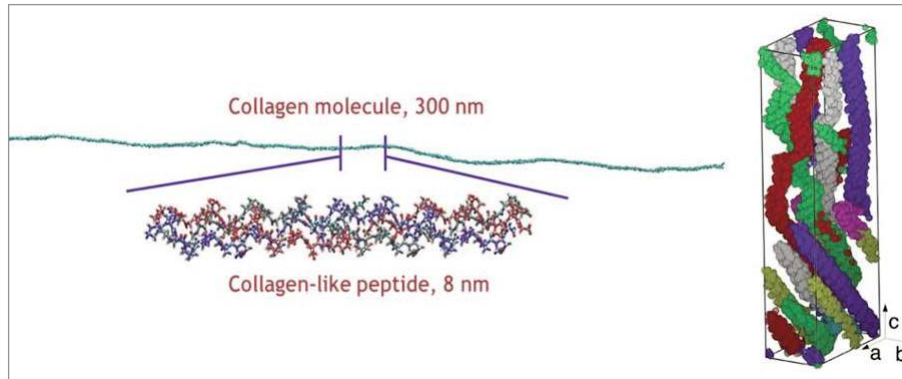
Figure 6. Comparison of collagen-like peptides with the actual collagen molecule (*left*) and unit cell of the low-resolution X-ray crystallography of the collagen microfibil described in (69) (*right*).

gy obtained by the periodic repetition of the unit cell lead to quasi-hexagonally packed collagen molecules which interdigitates with neighboring molecules to form a super twisted right-handed microfibril and to the well-known *D*-banding periodicity seen in AFM images of collagen fibrils. The fibril model is solvated using the solvate plug in of GROMACS by adding SPC water molecules. Since the molecule at physiological pH includes a net charge (positive net charge +34), counterions (Cl⁻) are added in order to keep the system neutral. The fibril model is equilibrated through several ns molecular dynamics simulations at a temperature of 310 K (37°C), and with 1 bar pressure to ensures structural convergence. In order to assess the mechanical properties of the atomistic models, molecular dynamics simulations with increasing constant mechanical stress in tension along the fibril axis has been performed, while maintaining the pressure on the other axes constant at 1 bar. The applied stresses are in the range from 0 to 200 MPa, applied during 20 ns molecular dynamics simulation for each load applied.

The equilibrated collagen microfibril (Fig. 8) has a density of ≈1.19 g/cm³, a value that is halfway between the density of water and the density of dehydrated collagen, which has been estimated at 1.34 g/cm³ [71]. A Ramachandran analysis of the solvated system shows that the collagen microfibrils in a region of the diagram (Psi ≈150°, Phi ≈ -75°) that is characteristic of the polyproline II chain and thus of collagen-like peptides, in good agreement with earlier experimental structural studies [72].

When subjected to mechanical load, collagen microfibrils feature two distinct deformation regimes. In the small-strain regime (<10%) the predicted Young's modulus is ≈300 MPa, while in the large-strain regime (>10%) the microfibril shows a severely increased tangent stiffness, with a Young's modulus of ≈1.2 GPa (Fig. 8). The results of nanomechanical testing of collagen microfibrilare in agreement with experimental results obtained for the small strain regime based on several techniques such as x-ray diffraction [25], Atomic Force Microscopy (AFM) [73, 74] and the use of micro-electro-mechanical systems (MEMS) [28, 29, 75]. For the larger-strain regime there exists less experimental information and available data tend to be more scattered. For example, Shen et al. [28] showed a relatively large variability of collagen fibril behaviors at large
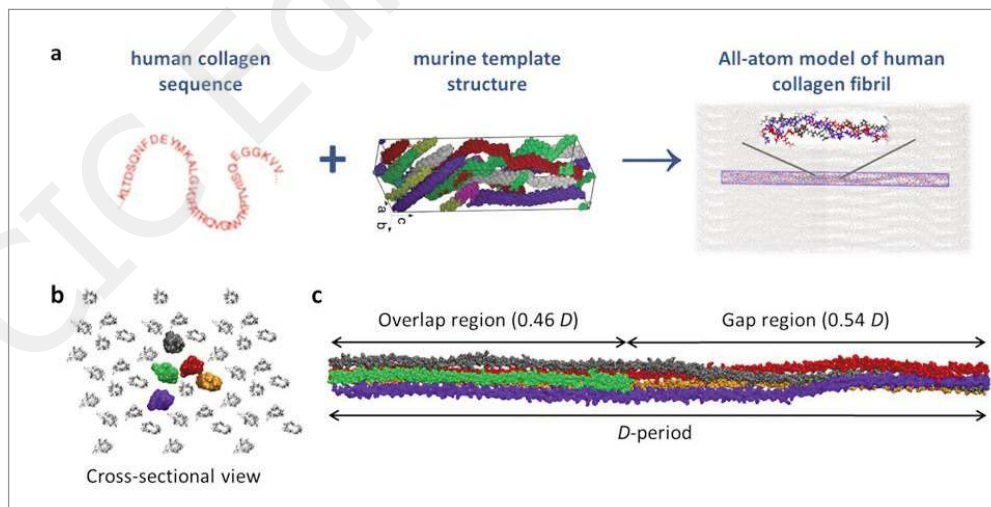

Figure 7. Schematic of the homology modeling process, in which a target sequence is applied to a template structure. The use of the murine template structure is possible thanks to the high sequence homology between human and murine collagen type I (a). Panel b shows the quasi-hexagonal cross-section of the microfibril model and panel c the D-period divided into gap and overlap regions.
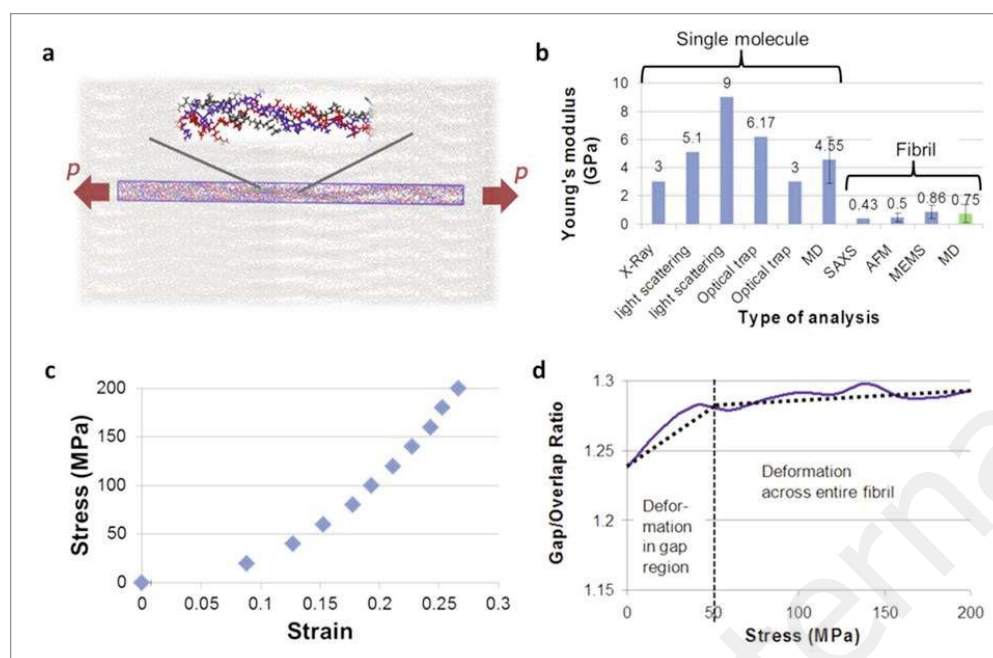
Figure 8. Schematic of the in silico mechanical loading (a) and comparison of modeling results with experimental results at fibril and molecular scale (b). Stress-strain relationship for collagen type I microfibril (c) and analysis of the gap/overlap ratio, showing that for small deformation the gap region is deforming more (d).

deformation, which suggested either strain-hardening or strain-softening depending on the fibril investigated. A direct comparison of the mechanical properties of single collagen molecules versus that of collagen microfibrils suggests that the mechanical properties are strongly scale dependent (Fig 8).

The atomistic model enables to observe atomistic and molecular deformation mechanisms not directly accessible to experimental techniques, and thereby to explain the molecular origin of mechanical properties at different hierarchical levels and levels of strain. It is observed that for small deformation the collagen molecules' end-to-end distance increases linearly until the microfibril strain reaches 10% (corresponding to ≈50 MPa stress), the strain at which the microfibril stiffness increases drastically. Beyond this point the molecular end-to-end still continues to increase but the slope of curve is significantly lower. This can be explained due to the fact that below 10% strain the collagen molecule is straightened within the microfibril and thereby loses its kinked arrangement, while beyond the 10% strain mark the molecule itself is being stretched, resulting in a larger mechanical resistance to deformation. The increase in the gap to overlap ratio in the small-strain regime (Fig. 8) suggests that the initial straightening is concentrated in the gap regions where the molecular packing density is lower and molecules are less organized, with more kinks. This model thereby confirms suggestions made by Fratzl et al.[2, 3, 76]. Once the entire capacity to molecular straightening is exhausted and all collagen molecules assume a straight configuration oriented in the direction of the pulling axis, collagen molecules themselves undergo stretching, leading to significantly increased tangent microfibril stiffness, at strains in excess of 10%. The

combination of these two mechanisms, molecular straightening and molecular stretching, effectively lead to an increase of the *D*-period, in agreement with experimental results[77]. Other mechanisms, such as molecular sliding may take place at larger strains in excess of 30% as described in earlier studies of the deformation mechanisms[25, 76].

Coarse-grain modeling of collagen

As seen in the previous paragraph, the study of collagen fibrils and fibers with full atomistic simulations is currently challenging, which represents an important limitation since this scale in the structural hierarchy of collagen is most relevant for physiological function. Other limitations exist with respect to the accessible time-scale, where most full-atomistic simulations are limited by a few hundred nanoseconds. However, many relevant materials phenomena such as tissue deformation and failure (e.g. under disease conditions) emerge at much longer time-scales.

A promising strategy to overcome these limitations is to decrease the number of degrees of freedom by grouping atoms into pseudo-atoms (or particles) referred to as beads. This represents the basis of the so-called coarse-grained approach[78, 79], where starting at the nanoscale, it is possible to derive parameters for higher hierarchical levels, up to the macroscale by systematically feeding information from smaller, more accurate to larger, more coarse levels[80, 81]. The development of a coarse-grained model provides a powerful path towards reliable modeling of full-length collagen molecules and its higher level hierarchical structures. Specifically, coarse-grained mod-

els allow the study of more complex systems, up to micrometer dimension and millisecond duration[82]. Earlier work of coarse-graining collagen molecules grouped hundreds of atoms into particles[38, 67]. This level of coarse-graining, however, is at a relatively coarse level where information about biochemical features (e.g. amino acid sequence) cannot be represented directly. However, the incorporation of biochemical features is crucial in a computational materiomics approach where material properties are elucidated at multiple scales.

Several other coarse-grained models suitable for proteins have been developed and successfully applied[83]. Particularly, the Martini coarse-grained model[84], developed by Marrink and coworkers, was initially applied to membrane lipids, later extended to proteins[85] and to carbohydrates[86]. It has been successfully applied to gain insights about different biological molecules such as membrane proteins[87, 88], ion channels[89] and liposomes[90].

The Martini model provides a suitable level of coarse-graining as it retains information about the chemistry specific to the amino acid sequence (as side chains are modeled depending on the type of the amino acids). All amino acids in the Martini force field are modeled with a number of beads that varies depending on the steric volume of each amino acid[85]. The general mapping rule is that four heavy atoms (that is, non-hydrogen atoms) are grouped together into one bead. Further, one bead describes the backbone, while others are added to represent the side chain. The number of beads used to model a specific residue therefore varies depending on the dimensions of the side chain of the amino acid. Small amino acids such as glycine or alanine are described by just one bead, while larger amino acids, like phenylalanine, tyrosine and tryptophan are modeled with up to five beads. The model also takes in account the polarity of every bead, described by a letter (P: polar; C: apolar; N: nonpolar; Q: charged) and a number (from 1: low polarity to 5: high polarity). Further, a letter is used to characterize a residue's hydrogen bonding capability (d: donor; a: acceptor; da: donor and acceptor; 0: none). These bead types, which correspond to atom types in the atomistic modeling framework, are used to describe the non-bonded interactions between beads. For each pair of bead types, a set of parameters for electrostatic and van der Waals potentials is defined. The best choice of particle types for amino acids was obtained by the authors of the original Martini force field for proteins by comparing simulation results and experimental measurements of water/oil partitioning coefficients of the amino acid side-chain analogues[85].

However, although the Martini force field is suitable for a wide number of applications and its validity has been proven through several simulations and comparisons both with atomistic and with experimental data, it cannot be applied to model collagen molecules in the original formulation. This is because of two reasons. First, the existing formulations of Martini lack parameters for hydroxyproline (a non-standard amino acid, found solely in collagen and formed through post-translational modification of proline). Second, it lacks parameters to describe the triple helical configuration of a collagen molecule. Thus, recent efforts have been addressed to overcome these limitations and addresses two major points.

In the Martini model, proline is modeled through the use of two beads, one for the backbone (bead type C5) and one for the side-chain (bead type AC2) as shown in Figure 9. Hydroxyproline derives directly from proline via the addition of a hydroxyl group on its side-chain. Therefore, hydroxyproline is also modeled using two beads in the extended MARTINI model. For the backbone bead is represented with the same bead type as for proline. The side chain, however, due to the presence of the hydroxyl group, shows a higher polarity level than proline. This aspect was already demonstrated in the work of Black and Mould[91], who calculated an index that takes into account the hydrophobicity of all amino acid side-chains, including hydroxyproline. Matching the bead types assigned by Marrink and the hydrophobicity values derived from Black and Mould, the hydroxyproline side-chain bead polarity, in the Martini notation, is determined. This parameter ranges from 0 to 1, where 1 is the most hydrophobic amino acid (phenylalanine), while 0 is the most hydrophilic one (arginine). The value reported for hydroxyproline is 0.527, which is found between threonine (0.450) and cysteine (0.680) values. In the Martini force field, threonine side chain is modeled as a P1 bead, while cysteine as a C5 bead. Considering this result, hydroxyproline is assigned a P1 value for the hydroxyproline side-chain, since its hydrophobicity value is closer to the value for threonine. The Martini model also takes into account the secondary structure of a protein, such as alpha-helix, beta-sheet, extended turns, or bends. The characteristic triple helical structure of collagen molecules cannot be described by any of the secondary structure parameters included in original Martini model. Thus, the bond distances, angles and dihedral parameters specific to the collagen triple helix have been assessed. The Martini bond potential forms are maintained, which are described as follows:

$$V_b = \frac{1}{2} K_b (d_{ij} - d_b)^2$$

$$V_a = \frac{1}{2} K_a [\cos(\varphi_{ijk}) - \cos(\varphi_a)]^2$$

$$V_d = K_d [1 + \cos(n\psi_{ijkl} - \psi_d)]$$

Where V_b, V_a and V_d are the potential energy terms of bond stretching, angle deformation and dihedral deformations, respectively. Bonded interactions act between bonded sites i, j, k, l with a distance at the equilibrium of d_b, angle φ_a and dihedral angles ψ_d and with elastic stiffness of K_b, K_a and K_d (for bond, angle and dihedral, respectively).

The triple helical geometrical parameters of the collagen triple helix (that is, d_b, φ_a and ψ_d) are obtained by performing a statistical analysis on a set of five collagen-like molecules available in the Protein Data Bank[92] (identification codes: 2DRT, 1K6F, 1QSU, 1CAG, 1V6Q). The bond lengths between backbone beads, bonding angles and dihedral angles are computed on the basis of these five crystallographic structures, providing a bond reference length (d_b) of 0.365±0.07 nm, a bonding reference angle (φ_a) of 119.2±8.72°, and a dihedral reference angle (ψ_d) of -89.3±9.76°. Figure 9 shows the details of a coarse-grained model of a collagen chain with the angular geometrical parameters.
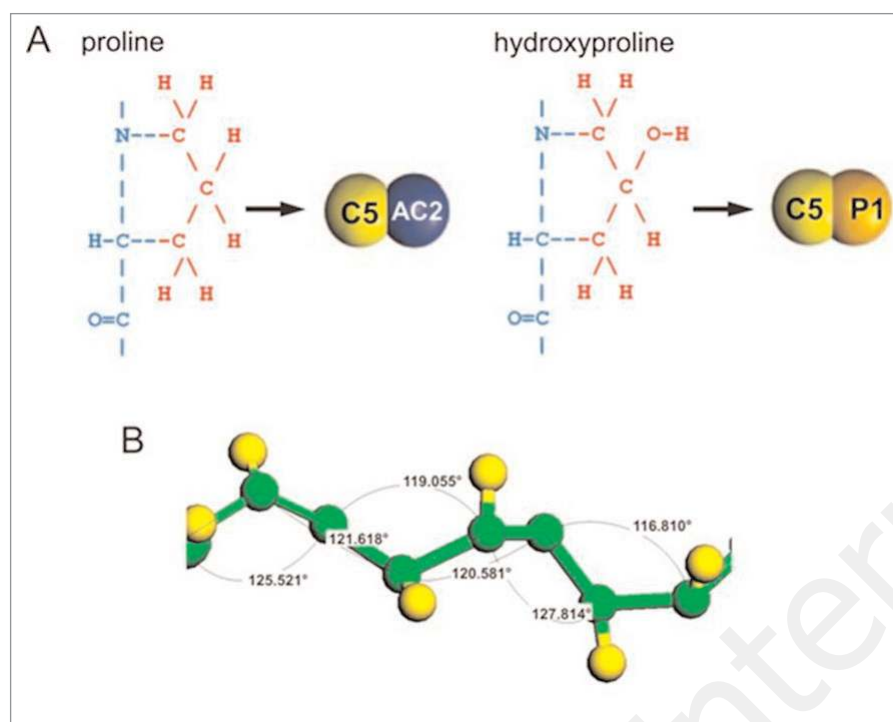
Figure 9. Parameterization of the force field of the MARTINI force field including the hydroxyproline residue (Panel A) and geometrical features (angles) of the coarse-grained collagen triple helix (Panel B).Hydroxyproline directly derives from proline adding a hydroxil group to its side chain, giving rise to an increased polarity level. Atomistic structures of both proline and hydroxyproline are shown on the left side of Panel A, while the bead representation using MARTINI model notation is shown on the right side of Panel A. Panel B shows the analysis of the angle between backbone beads of collagen-like peptides. The statistical analysis is performed on five collagen PDB entry (2DRT, 1K6F, 1QSU, 1CAG, 1V6Q); these collagen-like peptides are coarse-grained and the bond lengths, angles and dihedrals between backbone beads are analyzed.

In order to assess the stiffnesses of bond, angle and dihedrals (respectively, K_b, K_a and K_d), simple atomistic oligopeptides are considered. In order to derive the bonding constant K_b, a glycine-proline structure is chosen. In order to derive the angle elastic constant K_a, a glycine-proline-hydroxyproline oligopeptide is considered. Finally, to obtain the dihedral elastic constants K_d a glycine-proline-hydroxyproline-glycine molecule is studied. These structures are considered both in their atomistic form and in their coarse-grained form, and the parameters of the coarse-grain model (*i.e*, K_b, K_a and K_d) are identified matching force-extension curves obtained from atomistic and coarse-grained steered molecular dynamics simulations. For the coarse-grained models, the spring constants (that is, the parameters K_b, K_a and K_d) are initially set equal to the values adopted in the original Martini force field for an alpha helix secondary structure[85] and then gradually changed in order to best fit the atomistic force-extension curves so that they show the same stiffnesses. The values that best replicate the atomistic behavior are K_b=1250 kJmol^{-1}nm^{-2}, K_a=150 kJmol^{-1} and K_d=100 kJmol^{-1}.

In order to validate the extended MARTINI force field model, an 8 nm long collagen-like molecule (similar to the PDB entry used to assess the geometrical features) is pulled under the same conditions previously described. The chosen molecule is [(glycine-proline-hydroxyproline)$_{10}$]$_3$, which represents an "ideal" reference collagen molecule that was

used in several earlier molecular dynamics works[38, 93]. The equilibrated coarse-grained collagen peptide is pulled using a deformation rate of 1 m/s and the Young's modulus of the coarse-grain collagen molecule is then calculated from the slope of the force-deformation plot. Assuming a cylindrical geometry, and considering a collagen molecular radius of 0.8 nm, the Young's modulus is obtained equal to 4.62±0.41 GPa.

The whole structure of the heterotrimeric type I collagen molecule is investigated in order to derive the persistence length. The full length coarse-grained tropocollagen model is divided into five 60 nm peptide strands to reduce the computational cost. Then, the flexibility of the structures is analyzed from molecular dynamics trajectories of 350 ns each, obtaining the persistence length through the following expression[94]:

$$\log < \cos\theta > = -\frac{s}{L_p}$$

As shown in the inlay in Figure 10, the variable θ denotes the angle between two segments along the molecule separated by contour length s (that is, the sum of the segment lengths), and L_p is the persistence length, which provides information about a molecule's flexibility. In order to evaluate the persistence length, the molecule is divided into several smaller segments. Each segment (as shown in the inlay in Fig. 10), is delimited by the center of mass of the three
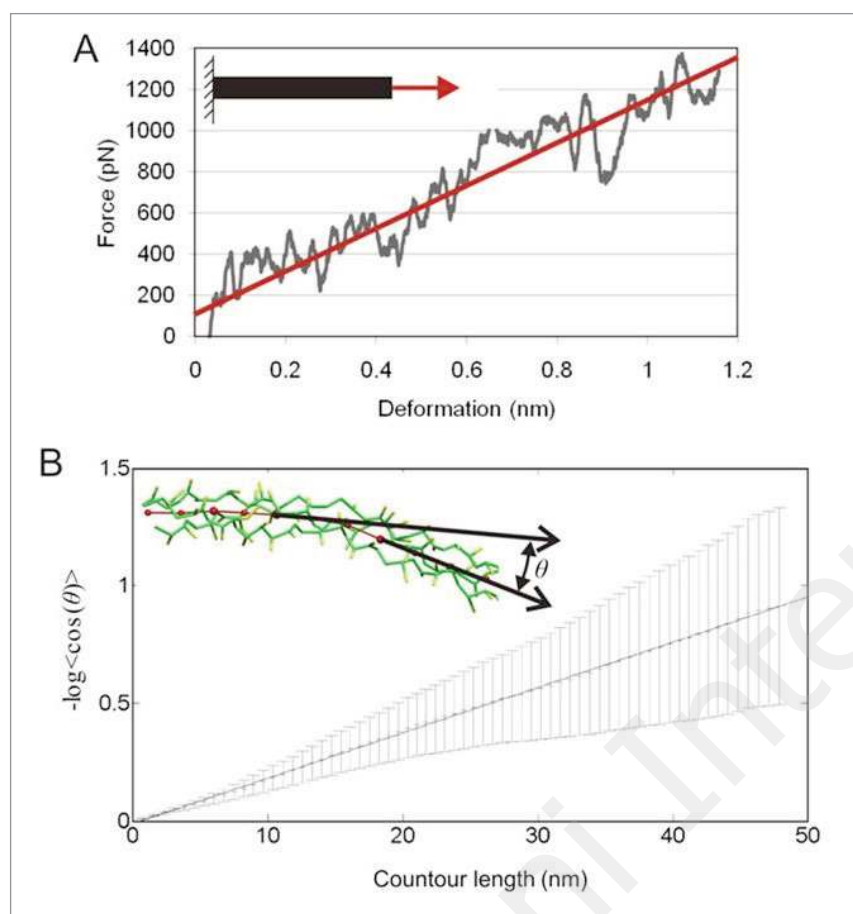
Figure 10. Mechanical analysis of collagen molecules. Panel A: Force-deformation plot up to 15% strain (1.2 nm) for the pulling test of a [(glycine-proline-hydroxyproline)10]₃ collagen-like peptide (*straight line*) and linear regression (*dashed line*) used to obtain the molecular elastic constant. Panel B: Plot of –log<cos(θ)> versus contour length calculated for the coarse-grain model of the first strand (≈ 60 nm) of human collagen type I molecule. The linear regression of the data for the five different strands leads to an average persistence length of ≈ 51.5 nm for human type I collagen.

equivalent glycine residues belonging to the three different collagen chains. The plot of –log<cos(θ)> versus s is obtained, where the average of cos(θ) is calculated over the full molecular dynamics simulations trajectories. Figure 10 shows the plot of –log<cos(θ)> versus the contour length s. The value of the persistence length L_p is then obtained from the inverse of the slope after a linear regression of all data, giving a value of L_p = 51.5±.6.7 nm.

The persistence length found based on the coarse-grained model is close to the value obtained by Hofmann and coworkers[35], who found a value of 57±5 nm for collagen type I molecule through an electron microscopy analysis. On the other hand, a literature analysis shows that great variability in persistence length value can be found considering different kinds of experimental tests. The pioneering work in this analysis is represented by Utiyama and coworkers[95], who considered sedimentation constants and the intrinsic viscosity of purified collagen molecules and calculated a value for the persistence length close to 130 nm. Saito and coworkers[96] considering the hydrodynamic properties of collagen derived the intrinsic viscosity and the sedimentation constant of collagen and,

from these values, the persistence length, equal to 160-180 nm. In another experiment, Nestler and coworkers[97] measured the dynamic viscoelastic properties of dilute solutions of collagen molecules. From the obtained values of intrinsic viscosity and rotational relaxation time, they found a value for the persistence length of about 170 nm. In more recent work, Sun and co-workers[62] used optical tweezers in order to obtain, from force-extension plots fitted to the Marko-Siggia entropic elastic model[98], the collagen persistence length, which was found to be 14.5±7.3 nm. Finally, molecular simulation studies were used to perform bending tests on a collagen-like peptide, predicting the bending stiffness of the collagen molecule and, from this result, evaluate the persistence length of collagen to be in the range of 16-24 nm[99]. The variability that can be found in literature for the collagen persistence length value depends on the used experimental setup, for example electron micrographs or optical tweezers, on the experimental conditions (how the sample is extracted and prepared), on the method applied and the parameters used to fit experimental data with theoretical models. Despite the large variability of experimental values, the val-

ue obtained with the coarse grained model is in good agreement with the consideration of collagen as a semi-flexible molecule with a rod like configuration.

Due to its contour length of 300 nm, all-atom simulations with explicit solvent are prohibitive since they would require excessive computational resources due to the very large number of particles. The reduction by roughly a factor of 10 in the coarse-grained description provides a significant speed-up that facilitates the direct simulation of much longer molecules. Furthermore, the typical time step used in classical molecular dynamics simulations (1-2 fs) allows the modeling only on the nanoseconds time scale. Whereas the coarse-grained model enables to use much longer time-steps, on the order of 20-40 fs. Considering the combined effect of the reduction of the number of particles and the increased time step, the coarse-grained approach leads to a total speed-up of 200-400 with respect to atomistic simulations.

With this significant computational speed-up, the coarse-grained modeling framework opens many possibilities for future studies, particularly at the scale of collagen fibrils and possibly fibers. However, the Martini coarse grain approach is only valid when the phenomena under study do not involve changes of the secondary structure. In the context of collagen, only events that do not involve unfolding of the collagen triple helix can be correctly modeled using the MARTINI force field formulation. While unfolding of molecules is likely to play an important role in large deformation and fracture of collagenous tissues, the mechanical stresses experienced by collagen tissues under small mechanical loads may not lead to unfolding at the molecular level. This is because strain is distributed over several hierarchical levels (i.e., fibers, fibrils, molecules) and involves several concurrent mechanisms (fiber uncrimping, proteoglycan-mediated fibril sliding, molecular slippage and molecular elongation).

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