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Nature of the constant factor in the relation between radial breathing mode frequency and tube diameter for single-wall carbon nanotubes

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Resonance Raman scattering is used to determine the radial breathing mode (RBM) frequency (ω_{RBM}) dependence on tube diameter (d_t) for single-wall carbon nanotubes (SWNTs). We establish experimentally the $\omega_{\text{RBM}}=227.0/d_t$ as the fundamental relation for pristine SWNTs. All the other RBM values found in the literature can be explained by an upshift in frequency due mostly to van der Waals interaction between SWNTs and environment.

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The radial breathing mode (RBM) provides the spectroscopic signature of single-wall carbon nanotubes (SWNTs).^{1,2} The RBM frequency (ω_{RBM}) depends on the SWNT diameter (d_t), which is related to their (n, m) structural indices by $d_t=0.142\sqrt{3(n^2+mn+m^2)}/\pi$.² The experimental results in the literature have been fitted with the relation $\omega_{\text{RBM}}=\mathbf{A}/d_t+\mathbf{B}$, with values for \mathbf{A} and \mathbf{B} varying from paper to paper.³⁻¹² The empirical constant factor \mathbf{B} prevents the expected limit of a graphene sheet from being achieved, where the ω_{RBM} should go to zero when d_t approaches infinity. Therefore, \mathbf{B} is supposedly associated with an environmental effect on ω_{RBM} , rather than an intrinsic property of SWNTs. Environmental effect here means the effect of the surrounding medium, such as bundling, molecules adsorbed from the air, surfactant used for SWNT bundle dispersion, and substrates where the tubes are sitting.

Here we use resonance Raman scattering to measure the RBMs of SWNTs grown by the water-assisted chemical vapor deposition (CVD) method.¹³⁻¹⁶ These SWNTs follow a simple linear relation between ω_{RBM} and d_t , with the proportionality constant $\mathbf{A}=227.0\text{ cm}^{-1}\text{ nm}$, in agreement with the elastic property of graphite, and with a negligible environmental effect ($\mathbf{B}\approx\mathbf{0}$). All the observed ω_{RBM} reported in the literature are upshifted from this fundamental relation.³⁻¹² The upshift exhibits a d_t dependence in quantitative agreement with recent predictions considering the van der Waals interaction between SWNTs and environment.¹⁷

This water-assisted CVD process has been called “super-growth” and generates millimeter-long isolated and high-purity SWNTs.¹³⁻¹⁶ The super-growth SWNTs exhibit a broad d_t distribution (d_t from 1 to 4 nm) and all tube chiralities ($0^\circ\leq\theta\leq 30^\circ$). The SWNTs are vertically aligned from a silicon substrate to form a very sparse material, where SWNTs represent only 3.6% of the total volume.¹⁵ Two triple-monochromator Raman spectrometers (a Dilor XY in the visible and a SPEX in the near-infrared) with charge

coupled device (CCD) detectors are used to acquire the spectra. In both cases a backscattering geometry is applied. An Ar-Kr laser and two quasicontinuous (dye and Ti:sapphire) lasers are used to tune the excitation laser wavelength. The laser power density is maintained constant, low enough to avoid heating effects (1 mW focused with an 80 \times objective in the visible, and 25 mW focused with a 10 cm focal length in the infrared).

In Fig. 1 we compared similar ω_{RBM} Raman spectra of two different samples. The gray lines show ω_{RBM} spectra for the super-growth SWNTs and they are being compared to the black lines ω_{RBM} spectra obtained from a SWNT sample grown by the alcohol-assisted CVD method.¹² Looking at Figs. 1(a) and 1(b) it is clear that the super-growth ω_{RBM} frequencies are downshifted from the ω_{RBM} values for the other sample. The differences in the low frequency region

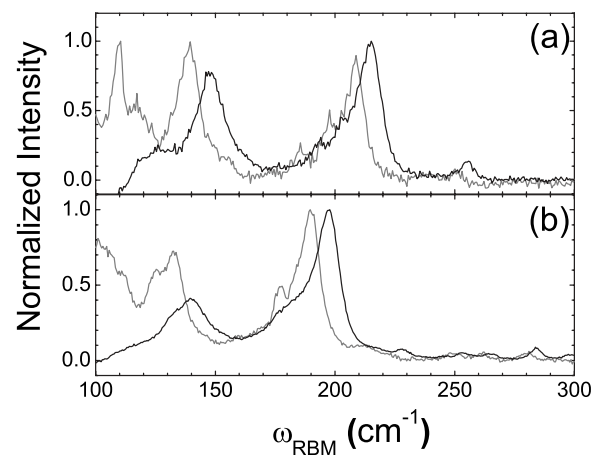


FIG. 1. The ω_{RBM} spectra for the super-growth SWNTs (gray) and for the “alcohol CVD” SWNTs (black). The spectra are obtained using different laser lines: (a) 590 nm (gray) and 600 nm (black); (b) 636 nm (gray) and 650 nm (black).

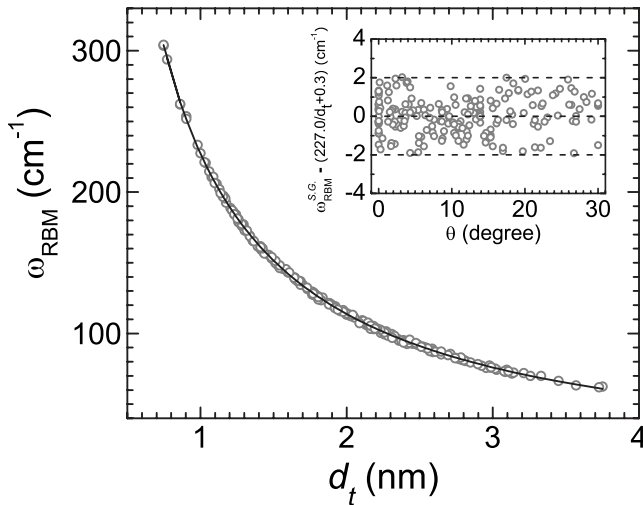
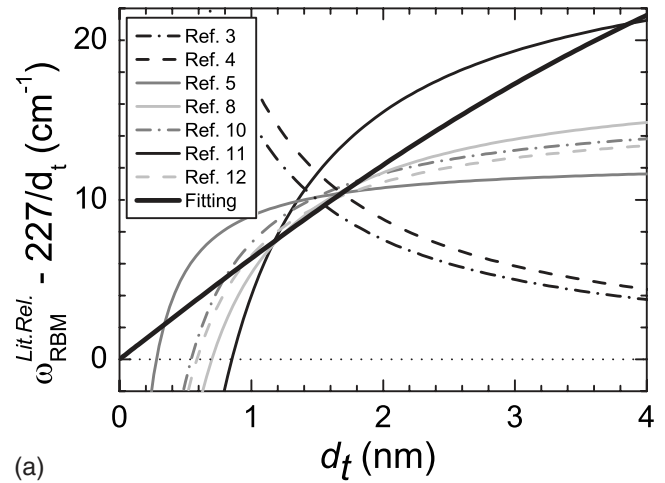


FIG. 2. Experimental radial breathing mode frequency (ω_{RBM}) as a function of tube diameter (d_t). The open circles represent the SWNT data assigned in this work and the solid line is a fitting to the data given by $\omega_{\text{RBM}}=227.0/d_t+0.3$. The inset plots the difference between the experimental ω_{RBM} and $227.0/d_t+0.3$ as a function of SWNT chiral angle (θ).

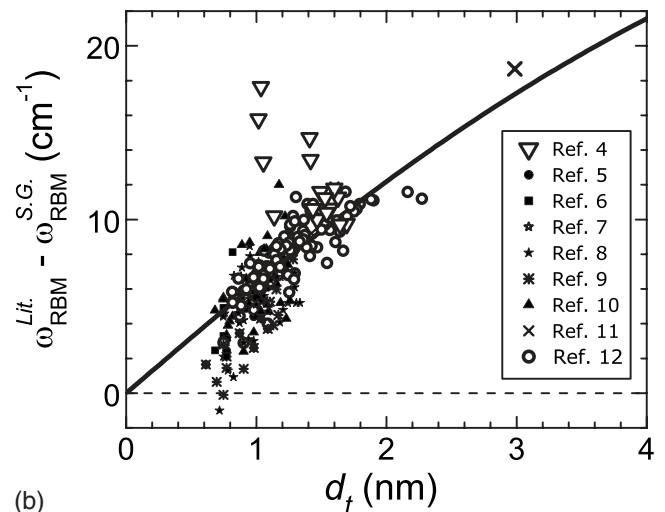
(below $\sim 120 \text{ cm}^{-1}$) are due to different d_t distributions in the samples.

With the super-growth sample, 125 Raman spectra, each at a different E_{laser} excitation, are used to assign the (n,m) structure of 197 different SWNTs (of which 73 are metallic and 124 are semiconducting).² As a short explanation, each RBM spectrum exhibits bands that are composed of a convolution of Lorentzian peaks. Each Lorentzian corresponds to the RBM Stokes spectrum of one specific (n,m) SWNT. The SWNTs observed are the ones having an optical transition energy (usually called E_{ij} , $i=1,2,\dots$) in resonance with the excitation laser energy. The (n,m) assignment is a complex but reliable procedure, and has already been extensively discussed in the literature (see Refs. 8–10 and especially Ref. 12). This analysis is important because all the 197 (n,m) tubes assigned in this work have their optical transition energies (E_{ij}) upshifted from others in the literature.^{5,6,8–10,12,18–21} To compare the ω_{RBM} for the same set of resonant (n,m) SWNTs in the two samples, the two spectra in either Fig. 1(a) or Fig. 1(b) have to be obtained with different laser excitations (see caption to Fig. 1). While the alcohol-assisted CVD sample has a specific set of SWNT species in resonance at a given laser excitation energy, the super-growth sample has the same species resonant for a higher ($\Delta E \sim 40 \text{ meV}$) laser energy.

Using all the 197 (n,m) SWNTs assigned and the relation $d_t=0.142\sqrt{3(n^2+mn+m^2)}/\pi$, the experimental ω_{RBM} can be plotted as a function of d_t , as shown in Fig. 2. Fitting the data shown in Fig. 2 using the relation $\omega_{\text{RBM}}=\mathbf{A}/d_t+\mathbf{B}$ we obtain $\mathbf{A}=(227.0 \pm 0.3) \text{ cm}^{-1} \text{ nm}$ and $\mathbf{B}=(0.3 \pm 0.2) \text{ cm}^{-1}$. This result is unexpected for being different from all results in the literature,^{3–12} and it is remarkable because a pristine-like relation between ω_{RBM} and d_t with a negligible environmental effect ($\mathbf{B} \approx 0$) has been obtained, so that $\omega_{\text{RBM}} \rightarrow 0$ as $d_t \rightarrow \infty$. Furthermore, the value of the constant



(a)



(b)

FIG. 3. (a) Difference between ω_{RBM} relations from the literature ($\omega_{\text{RBM}}^{\text{Lit.Rel.}}$) and $\omega_{\text{RBM}}=227.0/d_t$ as a function of tube diameter (d_t). (b) Difference between ω_{RBM} data from the literature ($\omega_{\text{RBM}}^{\text{Lit.}}$) and ω_{RBM} data from this work ($\omega_{\text{RBM}}^{\text{S.G.}}$) as a function of d_t . Each symbol represents data from a different reference (see legends). The thick solid line is a fit to the data in (b), as discussed in the text, and it is also shown in (a).

$\mathbf{A}=227.0 \text{ cm}^{-1} \text{ nm}$ that accounts for the vibrational characteristics of SWNTs exactly matches the value predicted by elasticity theory^{22,23} and is in excellent accordance with the value predicted by recent tight-binding method calculations for isolated SWNTs.²⁴ Both the theoretical methods are parameterized by the speed of sound in graphite. Therefore, this result directly connects one-dimensional carbon nanotubes and their two-dimensional counterpart graphene.

To understand why the ω_{RBM} dependence with d_t in super-growth SWNTs is unique, the results obtained here are compared with the results in the literature. Figure 3(a) shows the difference between several $\omega_{\text{RBM}}=\mathbf{A}/d_t+\mathbf{B}$ found in the literature^{3–5,8,10–12} and the $\omega_{\text{RBM}}=227.0/d_t$ established here. All the curves in the literature converge within the 1 to 2 nm d_t range, that is where most of the experimental data were actually obtained. Figure 3(b) shows the difference between the ω_{RBM} experimental values from the literature ($\omega_{\text{RBM}}^{\text{Lit.}}$)

(Refs. 4–12) and from this work ($\omega_{\text{RBM}}^{\text{S.G.}}$, S.G. stands for super-growth) as a function of d_t . All the published results for $\omega_{\text{RBM}}^{\text{Lit.}}$ are grouped in Fig. 3(b) on a d_t dependent upshifted trend for $\Delta\omega_{\text{RBM}} = \omega_{\text{RBM}}^{\text{Lit.}} - \omega_{\text{RBM}}^{\text{S.G.}}$. The down-triangles in Fig. 3(b) that spread out from the general trend are related to the $\omega_{\text{RBM}} = 248/d_t$ relation [dashed dark-gray curve from Ref. 4 in Fig. 3(a)] proposed in 2001⁴ by imposing the $\mathbf{B}=0$ condition on the basis of $\omega_{\text{RBM}} \rightarrow 0$ as $d_t \rightarrow \infty$. The $\omega_{\text{RBM}} = 248/d_t$ relation was obtained with an E_{ii} vs d_t relation that did not consider nanotube curvature effects (the first-neighbor tight-binding model), which are important for small d_t tubes (below $d_t = 1.2$ nm).² Therefore, the scatter in the data from the general trend in Fig. 3(b) might be due to a wrong (n, m) assignment below $d_t = 1.2$ nm. It is likely that the same argument is valid for the ω_{RBM} vs d_t relation obtained in Ref. 3 [black dashed-dotted line in Fig. 3(a)], since it is also based on the first-neighbor tight-binding model. Therefore, we demonstrated here that the d_t dependence of the difference between the experimental data in the literature and the fundamental relation $\omega_{\text{RBM}} = 227.0/d_t$ is always the same.

A recent molecular dynamics calculation considering van der Waals interactions between SWNTs and a shell of adsorbed fluid¹⁷ is now applied to explain the result shown in Fig. 3(b). Longhurst and Quirke¹⁷ considered SWNTs within the 1.03 to 1.73 nm diameter range surrounded by water at 300 K and showed a d_t dependent upshift on ω_{RBM} as compared to the tube in vacuum, ranging from 4 to 10 cm^{-1} , in perfect agreement with our observation in Fig. 3(b). The shifts were explained by the interaction of the RBM with the adsorbed shell of fluid surrounding the nanotube via Lennard-Jones potential, plus a small contribution of static pressure difference at the nanotube surface (10%–20% of the total effect). Then they proposed a model that fits their calculations, considering the RBM of a coupled system SWNT/environment composed of two spring constants: one coming from the C-C bond strength and the other coming from the interaction strength between the SWNT and its surroundings. The problem of addressing the environmental effect on ω_{RBM} is now reduced to solving a simple harmonic oscillator for a cylindrical shell subjected to an inwards pressure [$p(x)$] given by

$$\frac{2x(t)}{d_t} + \frac{\rho h}{Eh}(1-\nu^2)\frac{\partial^2 x(t)}{\partial t^2} = -\frac{(1-\nu^2)}{Eh}p(x), \quad (1)$$

where $x(t)$ is the displacement in the radial direction, $p(x) = (24K/s_0^2)x(t)$, K (in $\text{eV}/\text{\AA}^2$) gives the van der Waals interaction strength, s_0 is the equilibrium separation between the SWNT wall and the environment shell, E is the Young's modulus, ρ is the mass density per unit volume, ν is the Poisson's ratio, and h represents the thickness of the shell. If $p(x)$ is null, Eq. (1) gives the fundamental ω_{RBM}^0 for a pristine SWNT,

$$\omega_{\text{RBM}}^0 = \left\{ \frac{1}{\pi c} \left[\frac{Eh}{\rho h(1-\nu^2)} \right]^{1/2} \right\} \frac{1}{d_t}, \quad (2)$$

where the term inside the curly bracket is established here as 227.0 $\text{cm}^{-1} \text{nm}$. For $p(x)$ non-null we have

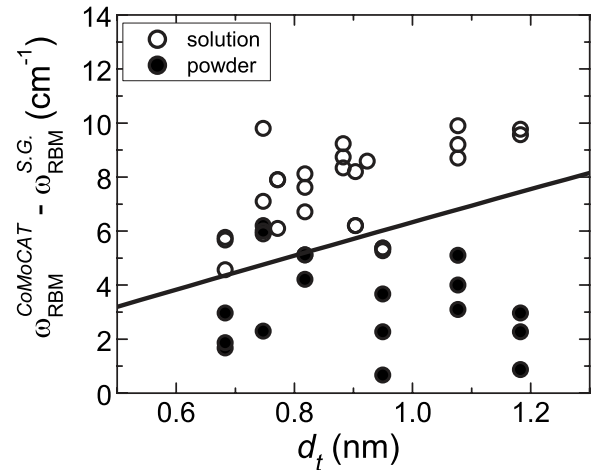


FIG. 4. Difference between CoMoCAT SWNT RBM frequencies ($\omega_{\text{RBM}}^{\text{CoMoCAT}}$) and $\omega_{\text{RBM}}^{\text{S.G.}}$ as a function of d_t . The open circles stand for SWNTs in solution and filled circles stand for SWNTs in powder. The thick solid line represents the fitting shown in Fig. 3(b).

$$\omega'_{\text{RBM}} = 227.0 \left[\frac{1}{d_t^2} + \frac{6(1-\nu^2)K}{Eh s_0^2} \right]^{1/2}, \quad (3)$$

where $[6(1-\nu^2)/Eh] = 26.3 \text{ \AA}^2/\text{eV}$. The shift in ω'_{RBM} due to the environment is given by $\Delta\omega_{\text{RBM}} = \omega'_{\text{RBM}} - \omega_{\text{RBM}}^0$. The data in Fig. 3(b) are fitted (see black thick solid line) by considering K/s_0^2 in Eq. (3) as an adjustable parameter. The best fit is obtained with $K/s_0^2 = (2.2 \pm 0.1) \text{ meV}/\text{\AA}^4$. The d_t dependent behavior of the environmental effect in ω_{RBM} is then established up to $d_t = 3$ nm. A similar environmental effect is obtained for SWNTs in bundles,^{3,12} surrounded by different surfactants,^{5–10} in air suspended by posts¹¹ or sitting on a SiO_2 substrate,⁴ but absent in the super-growth SWNTs.

In fact, indication for environmental dependent effects is observed in the lower d_t range,²⁵ as shown by the large spread of data in Fig. 3(b) for $d_t < 1.2$ nm. Notice that 1.2 nm is also the limit where curvature effects become important.^{2,26} Therefore, to complete our ω_{RBM} analysis, Raman spectroscopy experiments in low d_t CoMoCAT SWNT samples are performed in two different environments, (i) as-grown powder and (ii) dispersed in D_2O using CTAB (cetyltrimethylammoniumbromide) as the surfactant.²⁷ Figure 4 shows the result of the same analysis as presented in Fig. 3(b). Again, all the $\Delta\omega_{\text{RBM}}$ are positive, going up to +10 cm^{-1} , and a clear environment dependence is observed. The ω_{RBM} for SWNTs in solution (open circles) are clearly upshifted from the ω_{RBM} for SWNTs in powder (full black circles). Three different sets of SWNTs in solution and powder were measured and the results were reproducible.

In summary, super-growth SWNTs exhibit a relation $\omega_{\text{RBM}} = 227.0/d_t$ that gives the fundamental spectroscopic signature of the SWNT d_t . This relation is in agreement with calculations using the velocity of sound in graphite and has $\omega_{\text{RBM}} \rightarrow 0$ as $d_t \rightarrow \infty$, recovering the 2D graphene. The energies $E_{ii}^{\text{S.G.}}$ measured in the super-growth SWNTs are generally blueshifted from the $E_{ii}^{\text{Lit.}}$ in the literature

($\Delta E \sim 40$ meV), suggesting smaller environment dielectric constant (close to 1). All the ω_{RBM} results in the literature are upshifted from the pristine values due to van der Waals interaction with the environment, and can be generally described by

$$\omega_{\text{RBM}}^{\text{Lit.}} = \frac{227}{d_t} \sqrt{1 + C * d_t^2}, \quad (4)$$

where $C = [6(1 - \nu^2)/Eh][K/s_0^2] = 0.05786 \text{ nm}^{-2}$. For $d_t < 1.2$ nm, where the curvature effects become important, the environment effect depends more critically on the specific sample, the observed environmental-induced upshifts ranging from 1 to 10 cm^{-1} . The super-growth SWNTs discussed here are shielded from the environment by their own struc-

ture, that is a dense forest. We propose that all SWNT property measurements, such as exciton binding energy, temperature, doping, pressure dependent responses, etc. be revisited with similar samples, to provide what could be a solid baseline for the properties of pristine SWNTs. Furthermore, having established the fundamental d_t dependence, the ω_{RBM} can now be used as a probe for understanding surface tension, wetting on an attractive substrate, and the interaction potential for different liquids with respect to graphite and carbon nanotubes.¹⁷

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