



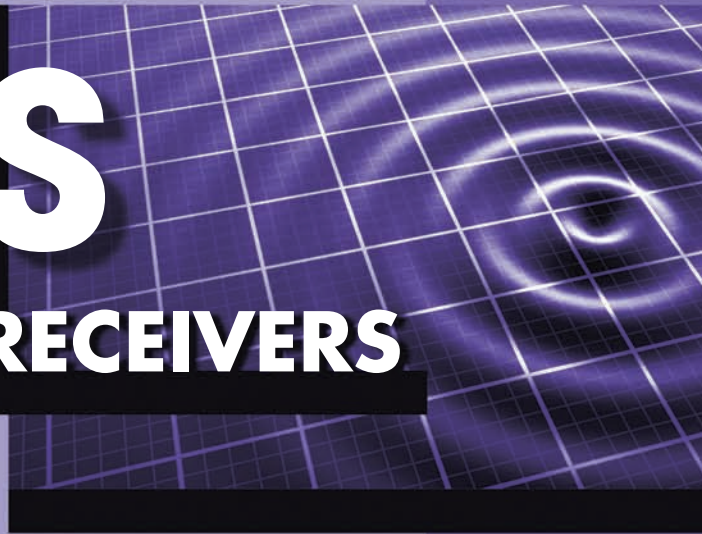
TECHNOLOGY AND APPLICATIONS SERIES

THOMAS PANY

**Navigation
Signal
Processing** for

GNSS

SOFTWARE RECEIVERS



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