# Nested Timed Automata

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Feb. 9, 2014

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Joint work with Xiaojuan Cai, Mizuhito Ogawa and Shoji Yuen.

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Hybrid automata extend timed automata with various rates of clocks; We would like to extend timed automata with (time-sensitive) context switches.

- (Recursive) Procedure calls
- Multi-level interrupt handlings

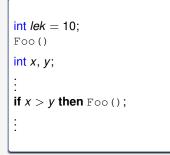
Need to deal with 'local' clocks.

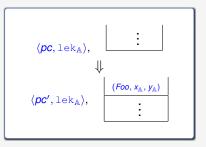
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### A Usual Automata-Based Program Analysis

int lek = 10; Foo() int x, y; i if x > y then Foo();

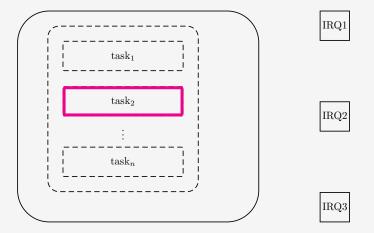
# A Usual Automata-Based Program Analysis

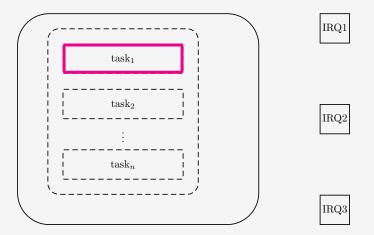




```
Tfoo() {
clock x, y;
   .
reset(y);
if x < 10 && y <= 5 then Tfoo();
else return;
  . . .
```

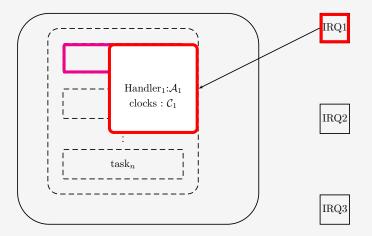
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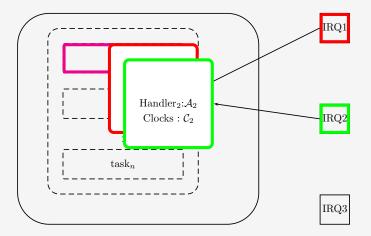
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Interrupt handlers override the behavior by  $A_i$ .



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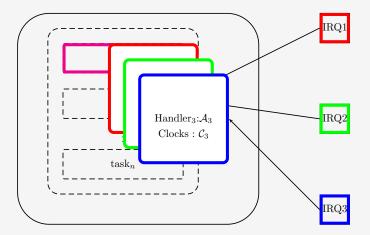
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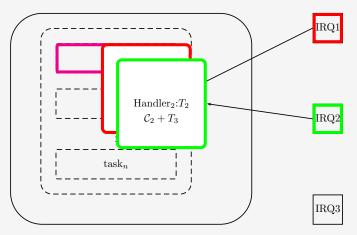


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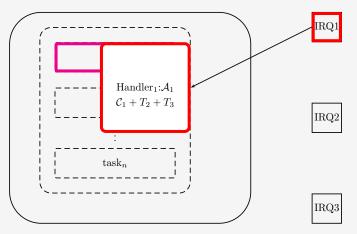
The behavior is resumed after the handlers terminate.

Clock values of  $C_2$  are changed.

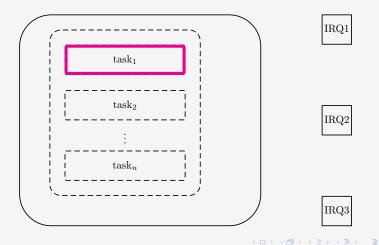


The behavior is resumed after the handlers terminate.

Clock values of  $\mathcal{C}_1$  are changed.



The behavior is resumed after the handlers terminate.



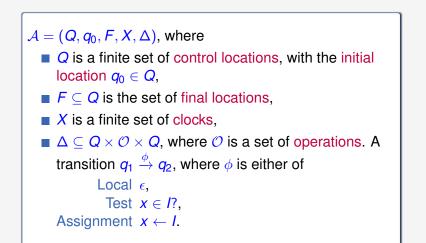
- A nested timed automaton is a pushdown system whose stack symbols are *timed automata*.
- It either behaves as the top TA in the stack, or switches from one TA to another by *pushing*, *popping*, and *altering* the top TA.
- When time passage happens, all clocks of these TAs in the stack elapse uniformly.

#### Timed Automata

- Nested timed automata (NeTA)
- State reachability is decidable via translation into DTPDA (dense timed pushdown automata [Abdulla et.al. LICS2012])
- Correctness of the translation.
- Conclusion

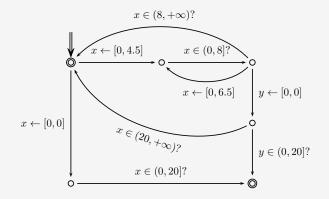
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# Timed Automata (TA)



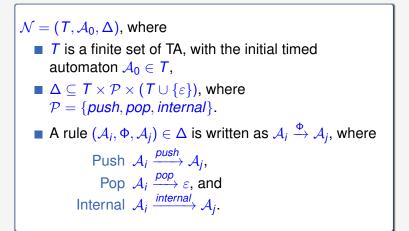
Clock updates, Diagnal-free and convex constraints, No invariants

# Timed Automata (TA) [An Example]



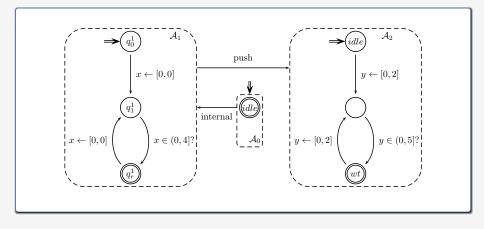
# NESTED TIMED AUTOMATA

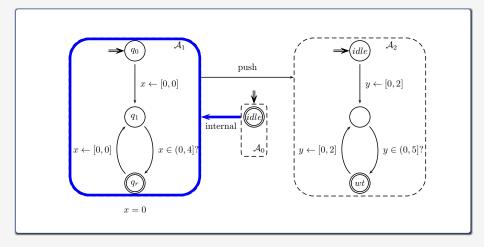
# Nested Timed Automata



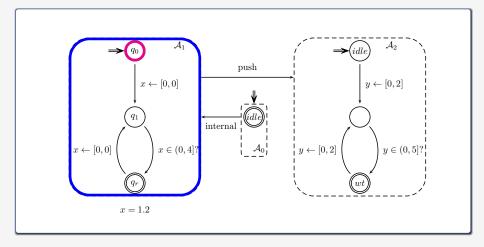
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Given an NeTA ( $T, A_0, \Delta$ ), a configuration is a stack, and the stack alphabet is a tuple  $\langle \mathcal{A}, \boldsymbol{q}, \boldsymbol{\nu} \rangle$ . The transition of NeTA is represented as follows: Progress transitions:  $c \xrightarrow{t} v c + t$ . Discrete transitions:  $c \xrightarrow{\phi} \mathcal{N} c'$ Intra-action  $\langle \mathcal{A}, q, \nu \rangle c \xrightarrow{\phi} \mathcal{A} \langle \mathcal{A}, q', \nu' \rangle c$ **Push**  $\langle \mathcal{A}, q, \nu \rangle c \xrightarrow{\text{push}} \mathcal{N} \langle \mathcal{A}', q_0(\mathcal{A}'), \nu'_0 \rangle \langle \mathcal{A}, q, \nu \rangle c$ **Pop**  $\langle \mathcal{A}, q, \nu \rangle c \xrightarrow{pop}_{\mathcal{N}} c$  if  $q \in F(\mathcal{A})$ . Inter-action  $\langle \mathcal{A}, q, \nu \rangle c \xrightarrow{internal} \mathcal{K} \langle \mathcal{A}', q_0(\mathcal{A}'), \nu'_0 \rangle c$  if  $q \in F(\mathcal{A}).$ 

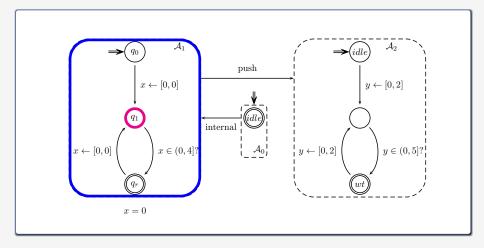




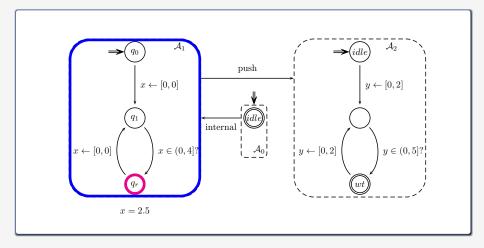
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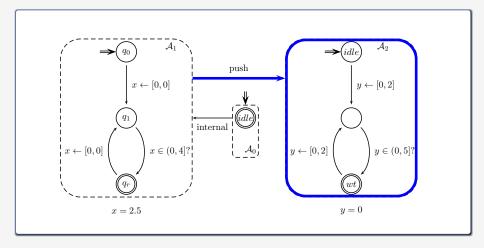
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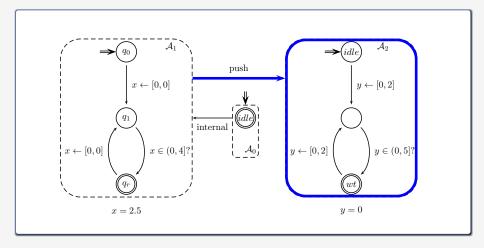
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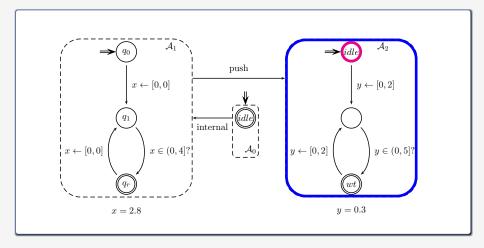
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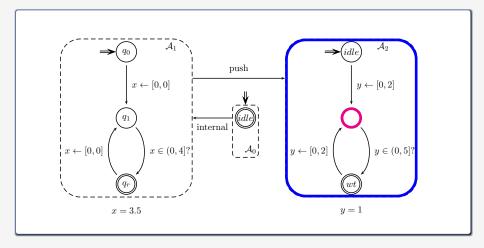
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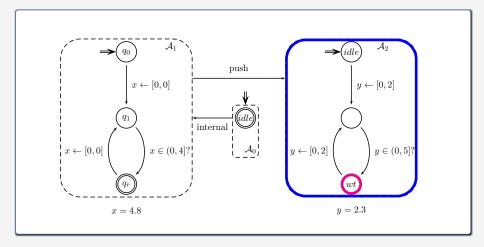
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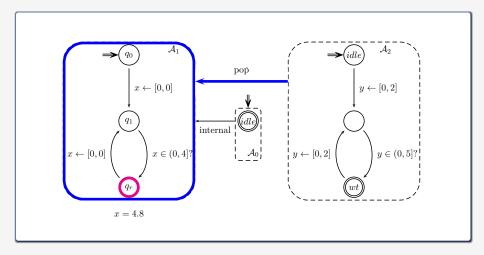
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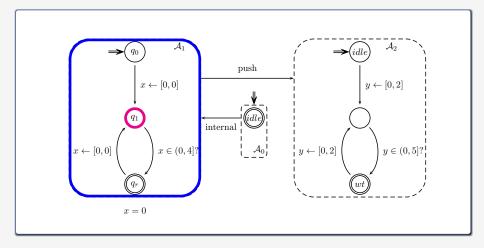
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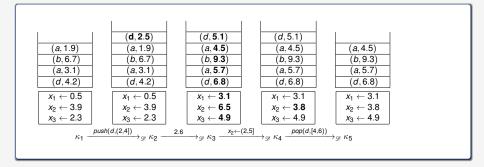
#### **TRANSLATION TO DTPDA**

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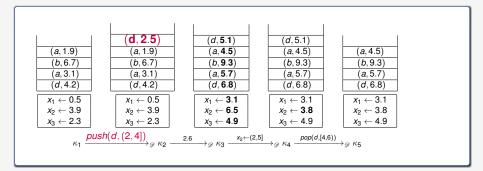
#### Dense Timed PDA [Abdulla et.al. 2012]

- State:  $S = \{\bullet\}$
- clocks:  $C = \{x_1, x_2, x_3\},\$
- Stack symbols:  $\Gamma = \{a, b, d\}$



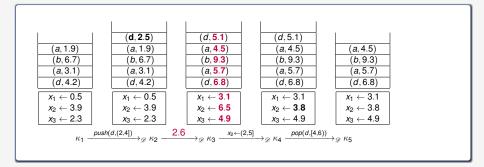
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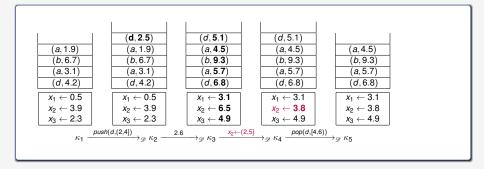
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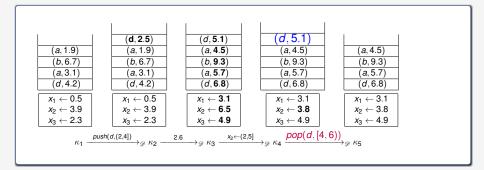
#### Dense Timed PDA [Abdulla et.al. 2012]

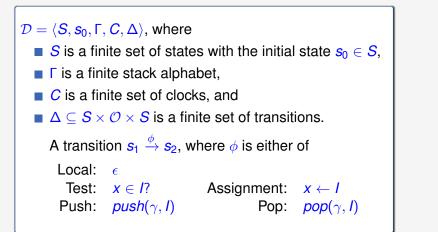
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#### Dense Timed PDA [Abdulla et.al. 2012]

- State:  $S = \{\bullet\}$
- clocks:  $C = \{x_1, x_2, x_3\},\$
- Stack symbols:  $\Gamma = \{a, b, d\}$





# A Variation of DTPDA for Encoding NeTA

Push  $push(\gamma, I)$  pushes  $\gamma$  to the top of the stack, with the age in the interval *I*.

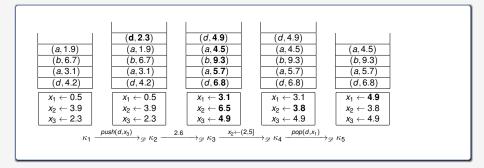
Pop  $pop(\gamma, I)$  pops the top-most stack symbol provided that this symbol is  $\gamma$  and its age belongs to *I*.

Push<sub>A</sub>  $push(\gamma, x)$  pushes  $\gamma$  to the stack associated with a local age with the value of the *x*'s value.

Pop<sub>A</sub>  $pop(\gamma, x)$  pops  $\gamma$  from a stack and assigns value of its local age to the global clock x.

# An Example of the DTPDA Variant

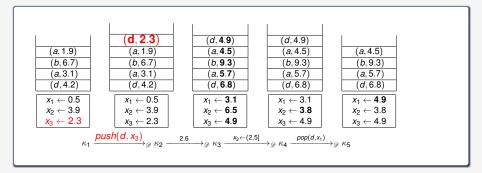
- State:  $S = \{\bullet\}$
- clocks:  $C = \{x_1, x_2, x_3\},\$
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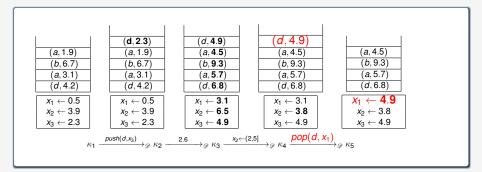
# An Example of the DTPDA Variant

- State: *S* = {•}
- clocks:  $C = \{x_1, x_2, x_3\},\$
- Stack symbols:  $\Gamma = \{a, b, d\}$



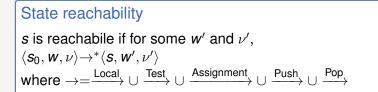
# An Example of the DTPDA Variant

- State: *S* = {•}
- clocks:  $C = \{x_1, x_2, x_3\},\$
- Stack symbols:  $\Gamma = \{a, b, d\}$



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#### State Reachability of DTPDA



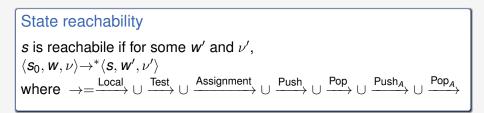
#### Theorem

The state reachability of DTPDA is decidable.

[Abdulla et.al. LICS2012] Region construction by fractional parts of ages Rotation at poping with shadow variables consistency

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# State Reachability of DTPDA Variant



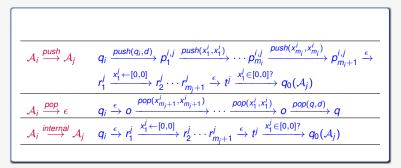
#### Theorem

The state reachability of DTPDA variant is decidable.

Small modification to LICS2012 proof works for the variant.

Another proof idea via WSPDS: [Cai et.al. 2013, 2014]

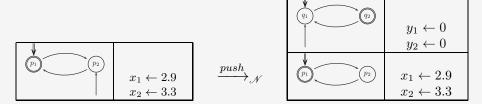
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- The key of the encoding is to synchronize the initial value of clocks, and
- Storing and restoring clocks values simultaneously when timed context switches.

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## Encoding Push of NeTA to DTPDA

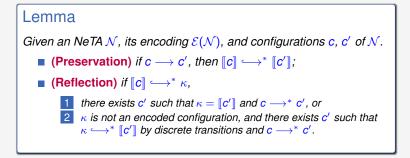


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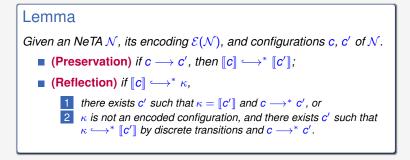
# Encoding Push of NeTA to DTPDA

$p_2 \xrightarrow[y_1 \leftarrow 4.1]{} \underbrace{ \begin{array}{c} x_1 \leftarrow 2.9 \\ x_2 \leftarrow 3.3 \\ y_1 \leftarrow 4.1 \\ y_2 \leftarrow 0.5 \end{array}}_{\mathcal{G}} \underbrace{ \text{push}(p_2, d) }_{\mathcal{G}}$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\xrightarrow{ push(x_1, x_1) } \mathscr{D} \xrightarrow{ push(x_2, x_2) } \mathscr{D}$	$ \begin{array}{c c} y_1 \leftarrow 4.1 \\ \hline y_2 \leftarrow 0.5 \\ \hline x_1 \leftarrow 2.9 \\ \hline x_2 \leftarrow 3.3 \end{array} \begin{array}{ c c } \hline (\mathbf{x_2, 3.3}) \\ \hline (\mathbf{x_1, 2.9}) \\ \hline (p_2, 0) \end{array} $
$\xrightarrow{y_1 \leftarrow [0,0]} \mathscr{D}$	$ \begin{array}{ c c c c c c } r_2^2 & \frac{y_1 \leftarrow 0}{y_2 \leftarrow 0.5} \\ \hline \hline x_1 \leftarrow 2.9 \\ x_2 \leftarrow 3.3 \end{array} & \frac{(x_2, 3.3)}{(x_1, 2.9)} \\ \hline (p_2, 0) \end{array} $
$\underbrace{y_2 \leftarrow [0,0]}{\mathscr{D}}$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\underbrace{y_1 \in [0,0]?}{\mathscr{D}}$	$\begin{array}{ c c c c c c }\hline q_1 & \frac{y_1 \leftarrow 0}{y_2 \leftarrow 0} & \hline (x_2, 3.3) \\ \hline \hline & x_1 \leftarrow 2.9 \\ \hline & x_2 \leftarrow 3.3 & \hline & (x_1, 2.9) \\ \hline & (p_2, 0) & \hline \end{array}$
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#### Correctness



#### Correctness



#### Theorem

The state reachability problem of NeTA is decidable.

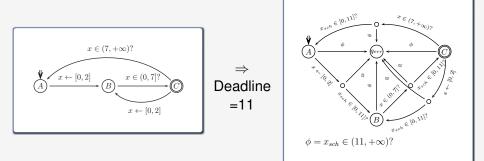
#### DEADLINE ANALYSIS FOR MULTILEVEL INTERRUPT HANDLING

- Interrupt handlers as guarded timed automata.
- Interrupt request as push<sub>A</sub> operation.
- Return from interrupt as *pop<sub>A</sub>* operation.
- Deadline violation as the reachability to *err* state.

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# Timed Automata with Deadline

#### Add a stopwatch to check deadline and an error state



#### Fall into $q_{err}$ when deadline passed.

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 $\begin{array}{rcl} \textit{Handler}_i &: & \texttt{guard}(\mathcal{A}_i, \textit{d}_i) \\ & \texttt{guard}(\mathcal{A}_i, \textit{d}_i) \texttt{ adds the deadline to } \mathcal{A} \end{array}$ 

 $\begin{array}{rcl} \textit{Interrupt} & : & \mathcal{A}_i \xrightarrow{\text{push}} \mathcal{A}_i \\ & A_i \text{ may interrupt } A_j \end{array}$ 

 $\textit{Initial} \quad : \quad \mathcal{A}_0 = \textit{Task}_1 \mid\mid \textit{Task}_2 \mid\mid \cdots \mid\mid \textit{Task}_n$ 

Interrupt fails to be handled if  $q_{err}$  in some  $A_i(i > 0)$  is reachabile.

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- Three kinds of clocks: global clocks, local clocks and stopwatch clocks.
- Reachability problems of pushdown systems under respective kind of clocks are decidable, however:

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  - Under global and local clocks: Decidable [Li et. al., 2014]
  - Under local and stopwatch clocks: ???
- Reachability problem of NeTA with invariant is positive.

- Develop a tool based on a restrictive class such that a pop action occurs only with an integer-valued age.
- This subclass can be encoded into UTPDA (without local age).
- Encode UTPDA to weighted pushdown system to gain the efficiency.

- Timed PDA [Bouajjani et. al.,1994] PDA with Global clocks
- Timed recursive state machines [Benerecetti et.al, 2010] Extended PDA with two stacks for states and clocks
- Recursive timed automata [Trivedi et.al., 2010] Local clocks stop
- Hierarchical timed automata [David et.al., 2001] Static hierarchy

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- An NeTA is a pushdown system with a finite set of TA as stack symbols.
- All clocks in the stack elapse uniformly.
- The state reachability is decidable by encoding to DTPDA with an extension of local clock assignment.

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# Thank you!

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Guoqiang LI Feb. 9, 2014

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