

# Neural Space-Mapping Optimization for EM-Based Design

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**Abstract**—We propose, for the first time, neural space-mapping (NSM) optimization for electromagnetic-based design. NSM optimization exploits our space-mapping (SM)-based neuromodeling techniques to efficiently approximate the mapping. A novel procedure that does not require troublesome parameter extraction to predict the next point is proposed. The initial mapping is established by performing upfront fine-model analyses at a reduced number of base points. Coarse-model sensitivities are exploited to select those base points. Huber optimization is used to train, without testing points, simple SM-based neuromodels at each NSM iteration. The technique is illustrated by a high-temperature superconducting quarter-wave parallel coupled-line microstrip filter and a bandstop microstrip filter with quarter-wave resonant open stubs.

**Index Terms**—Design automation, EM optimization, microwave circuits, microstrip filters, neural-network applications, neural space mapping, neural modeling, optimization methods, space mapping.

## I. INTRODUCTION

ARTIFICIAL neural networks (ANNs) are suitable models for microwave circuit yield optimization and statistical design [1], [2]. Neuromodels are computationally much more efficient than electromagnetic (EM) or physical models and can be more accurate than empirical physics-based models. Once they are trained with reliable learning data, obtained by either EM simulation or by measurement, the neuromodel can be used for efficient and accurate optimization within the region of training. This has been the conventional approach to optimization of microwave structures using ANNs [3].

The principal drawback of this ANN optimization approach is the cost of generating sufficient learning samples, since the simulations/measurements must be performed for many combinations of different values of geometrical, material, process,

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and input signal parameters over a large region. Additionally, it is well known that the extrapolation ability of neuromodels is poor, making unreliable any solution predicted outside the training region. Introducing knowledge, as in [4], can alleviate these limitations.

A powerful new method for optimization of microwave circuits based on space-mapping (SM) technology and ANNs is presented. An innovative strategy is proposed to exploit the SM-based neuromodeling techniques [5] in an efficient neural space-mapping (NSM) optimization algorithm, including frequency. NSM requires a reduced set of upfront learning base points. A “coarse” or empirical model is used not only as source of knowledge that reduces the amount of learning data and improves the generalization performance of the SM-based neuromodel, but also as a means to select the initial learning base points through sensitivity analysis. A novel procedure that does not require troublesome parameter extraction to predict the next point is presented. Huber optimization is used to train the SM-based neuromodels at each iteration. The SM-based neuromodels are developed without using testing points: their generalization performance is controlled by gradually increasing their complexity starting with a three-layer perceptron with zero hidden neurons. NSM optimization is illustrated by a high-temperature superconducting (HTS) quarter-wave parallel coupled-line microstrip filter and a bandstop microstrip filter with quarter-wave resonant open stubs.

## II. SM CONCEPT INCLUDING FREQUENCY

SM is a powerful concept for circuit design and optimization that combines the computational efficiency of “coarse” models with the accuracy of “fine” models. The coarse models are typically equivalent-circuit models, which are computationally very efficient, but often have a limited validity range for their parameters, beyond which the simulation results may become inaccurate. On the other hand, fine models can be provided by an EM simulator, or even by direct measurements: they are very accurate, but CPU intensive. SM establishes a mathematical link between the coarse and fine models. It directs the bulk of CPU intensive evaluations to the coarse model, while preserving the accuracy and confidence offered by the fine model. The SM technique was originally developed by Bandler *et al.* [6].

In the SM technique with frequency dependence, the operating frequency  $\omega$  is also included in the mapping function. This allows us to simulate the coarse model at a different frequency  $\omega_c$ .

Let the vectors  $\mathbf{x}_c$  and  $\mathbf{x}_f$  represent the design parameters of the coarse and fine models, respectively, and  $\mathbf{R}_c(\mathbf{x}_c, \omega_c)$  and

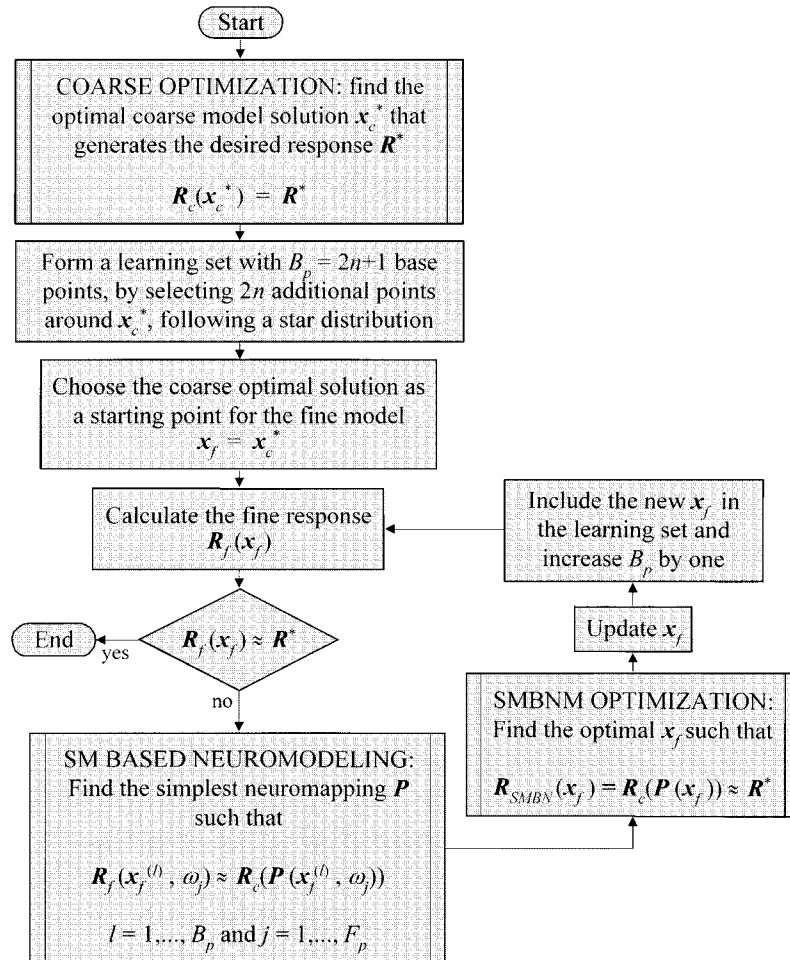


Fig. 1. NSM optimization.

$R_f(\mathbf{x}_f, \omega)$  represent the corresponding model responses (e.g.,  $R_c$  and  $R_f$  might contain the real and imaginary parts of  $S_{21}$ ).  $R_c$  is much faster to calculate, but less accurate than  $R_f$ .

The aim of SM optimization, including frequency, is to find an appropriate mapping  $P$  from the fine-model input space to the coarse-model input space

$$\begin{bmatrix} \mathbf{x}_c \\ \omega_c \end{bmatrix} = P(\mathbf{x}_f, \omega) \quad (1)$$

such that

$$R_c(\mathbf{x}_c, \omega_c) \approx R_f(\mathbf{x}_f, \omega). \quad (2)$$

Once a mapping  $P$  valid in the region of interest is found, the coarse model can be used for fast and accurate simulations in that region.

### III. NSM OPTIMIZATION AN OVERVIEW

Fig. 1 shows the flow diagram of NSM optimization. Here, we explain the overall operation of NSM optimization; a detailed description of the main blocks is presented in the following sections.

We start by finding the optimal solution  $\mathbf{x}_c^*$  that yields the desired response using the coarse model. We select  $2n$  additional points following an  $n$ -dimensional star distribution [5], [7] centered at  $\mathbf{x}_c^*$ , as shown in Fig. 2, where  $n$  is the number of design parameters ( $\mathbf{x}_c, \mathbf{x}_f \in \mathbb{R}^n$ ). The percentage of deviation from  $\mathbf{x}_c^*$  for each design parameter is determined according to the coarse-model sensitivities. The larger the sensitivity of the coarse-model response with respect to a certain parameter, the smaller the percentage of variation of that parameter. We assume that the coarse-model sensitivities are similar to those of the fine model.

The fine-model response  $R_f$  at the optimal coarse-model solution  $\mathbf{x}_c^*$  is then calculated. If  $R_f$  is approximately equal to the desired response, the algorithm ends, otherwise we develop an SM-based neuromodel over the  $2n + 1$  fine-model points.

Once an SM-based neuromodel with small learning errors is available, we use it as an improved coarse model, optimizing its parameters to generate the desired response. The solution to this optimization problem becomes the next point in the fine-model parameter space, and it is included in the learning set.

We calculate the fine-model response at the new point, and compare it with the desired response. If it is still different, we retrain the SM-based neuromodel over the extended set of learning samples and the algorithm continues. If not, the algorithm terminates.

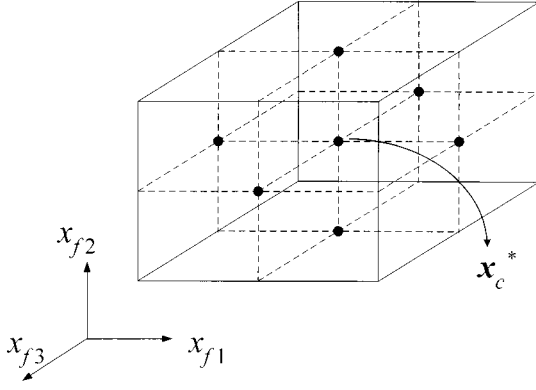


Fig. 2. Three-dimensional star distribution for the initial base points.

#### IV. COARSE OPTIMIZATION

During the coarse optimization phase of NSM optimization, we want to find the optimal coarse-model solution  $\mathbf{x}_c^*$  that generates the desired response over the frequency range of interest. The vector of coarse-model responses  $\mathbf{R}_c$  might contain  $m$  different responses of the circuit

$$\mathbf{R}_c(\mathbf{x}_c) = [\mathbf{R}_c^1(\mathbf{x}_c)^T \dots \mathbf{R}_c^m(\mathbf{x}_c)^T]^T \quad (3)$$

where each individual response has been sampled at  $F_p$  frequency points

$$\mathbf{R}_c^r(\mathbf{x}_c) = [\mathbf{R}_c^r(\mathbf{x}_c, \omega_1) \dots \mathbf{R}_c^r(\mathbf{x}_c, \omega_{F_p})]^T, \quad r = 1, \dots, m \quad (4)$$

The desired response  $\mathbf{R}^*$  is expressed in terms of specifications. The problem of circuit design using the coarse model can be formulated as [8]

$$\mathbf{x}_c^* = \arg \min_{\mathbf{x}_c} U(\mathbf{R}_c(\mathbf{x}_c)) \quad (5)$$

where  $U$  is a suitable objective function. For example,  $U$  could be a minimax objective function expressed in terms of upper and lower specifications for each response and frequency sample. A rich collection of objective functions, for different design constraints, is formulated by Bandler *et al.* in [8].

#### V. TRAINING THE SM-BASED NEUROMODEL DURING NSM OPTIMIZATION

At the  $i$ th iteration, we want to find the simplest neuromapping  $\mathbf{P}^{(i)}$  such that the coarse model using that mapping approximates the fine model at all the learning points. This is realized by solving the optimization problem

$$\mathbf{w}^* = \arg \min_{\mathbf{w}} \left\| [\dots \mathbf{e}_s^T \dots]^T \right\| \quad (6)$$

with

$$\mathbf{e}_s = \mathbf{R}_f(\mathbf{x}_f^{(l)}, \omega_j) - \mathbf{R}_c(\mathbf{x}_{c_j}^{(l)}, \omega_{c_j}) \quad (7a)$$

$$\begin{bmatrix} \mathbf{x}_{c_j}^{(l)} \\ \omega_{c_j} \end{bmatrix} = \mathbf{P}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) \quad (7b)$$

$$j = 1, \dots, F_p \quad (7c)$$

$$l = 1, \dots, 2n + i \quad (7d)$$

$$s = j + F_p(l - 1) \quad (7e)$$

where  $2n + i$  is the number of training base points for the input design parameters and  $F_p$  is the number of frequency points per

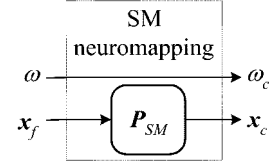


Fig. 3. Space-mapped neuromapping.

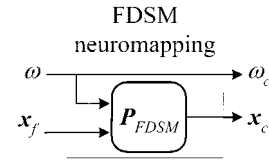


Fig. 4. Frequency-dependent space-mapped neuromapping.

frequency sweep. It is seen that the total number of learning samples at the  $i$ th iteration is  $s = (2n + i)F_p$ .

Equation (7b) is the input–output relationship of the ANN that implements the mapping at the  $i$ th iteration. Vector  $\mathbf{w}$  contains the internal parameters (weights, bias, etc.) of the ANN. The paradigm chosen to implement  $\mathbf{P}$  is a three-layer perceptron.

All the SM-based neuromodeling techniques proposed in [5] can be exploited to efficiently solve (6). In the space-mapped neuromodeling (SMN) approach, only the design parameters are mapped, as illustrated in Fig. 3, and both models use the same frequency

$$\begin{bmatrix} \mathbf{x}_{c_j}^{(l)} \\ \omega_{c_j} \end{bmatrix} = \mathbf{P}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) = \begin{bmatrix} \mathbf{P}_{SM}^{(i)}(\mathbf{x}_f^{(l)}, \mathbf{w}) \\ \omega_j \end{bmatrix}. \quad (8)$$

In the frequency-dependent space mapped neuromodeling (FDSMN) approach, illustrated in Fig. 4, both coarse and fine models are simulated at the same frequency, but the mapping from the fine to the coarse parameter space is dependent on the frequency

$$\begin{bmatrix} \mathbf{x}_{c_j}^{(l)} \\ \omega_{c_j} \end{bmatrix} = \mathbf{P}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) = \begin{bmatrix} \mathbf{P}_{FDSM}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) \\ \omega_j \end{bmatrix}. \quad (9)$$

The frequency space-mapped neuromodeling (FSMN) technique (see Fig. 5) establishes a mapping not only for the design parameters, but also for the frequency variable, such that the coarse model is simulated at a different frequency to match the fine-model response

$$\begin{bmatrix} \mathbf{x}_{c_j}^{(l)} \\ \omega_{c_j} \end{bmatrix} = \mathbf{P}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) = \begin{bmatrix} \mathbf{P}_{FSM}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) \end{bmatrix}. \quad (10)$$

For those cases where the shapes of the fine- and coarse-model responses are nearly identical, but shifted in frequency, the frequency mapped neuromodeling technique (see Fig. 6) simulates the coarse model with the same physical parameters used by the fine model, but at a different frequency to align both responses

$$\begin{bmatrix} \mathbf{x}_{c_j}^{(l)} \\ \omega_{c_j} \end{bmatrix} = \mathbf{P}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) = \begin{bmatrix} \mathbf{x}_f^{(l)} \\ \mathbf{P}_{FM}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) \end{bmatrix}. \quad (11)$$

Finally, the frequency partial-space mapped neuromodeling (FPSMN) technique maps only some of the design parameters

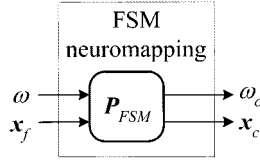


Fig. 5. Frequency space-mapped neuromapping.

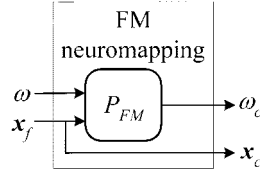


Fig. 6. Frequency-mapped neuromapping.

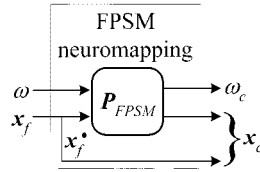


Fig. 7. Frequency partial-space mapped neuromapping.

and the frequency (see Fig. 7), making an even more efficient use of the implicit knowledge in the coarse model

$$\begin{aligned} \begin{bmatrix} \mathbf{x}_{c_j}^{(l)} \\ \omega_{c_j} \end{bmatrix} &= \mathbf{P}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) \\ &= \begin{bmatrix} \mathbf{x}_f^{\bullet(l)} \\ \mathbf{x}_{c_j}^{\bullet(l)} \\ \omega_{c_j} \end{bmatrix} \\ &= \begin{bmatrix} \mathbf{P}_{FPSM}^{(i)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}) \end{bmatrix}. \end{aligned} \quad (12)$$

Note that the “design” parameters of the coarse model do not change with frequency only in the SMN and FM neuromappings.

The starting point for the first training process is a unit mapping, i.e.,  $\mathbf{P}^{(0)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}_u) = [\mathbf{x}_f^{(l)T} \omega_j]^T$ , for  $j = 1, \dots, F_p$  and  $l = 1, \dots, 2n + 1$ , where  $\mathbf{w}_u$  contains the internal parameters of the ANN that give a unit mapping. The SM-based neuromodel is trained in the next iterations using the previous mapping as the starting point.

The complexity of the ANN (the number of hidden neurons and the SM-based neuromodeling technique) is gradually increased according to the learning error  $\varepsilon_L$ , starting with a linear mapping (three-layer perceptron with zero hidden neurons). In other words, we use the simplest ANN that yields an acceptable learning error  $\varepsilon_L$ , defined as

$$\varepsilon_L = \left\| \left[ \dots \mathbf{e}_s^T \dots \right]^T \right\| \quad (13)$$

where  $\mathbf{e}_s$  is obtained from (7) using the current optimal values for the ANN internal parameters  $\mathbf{w}^*$ .

In our implementation, the neuromapping for the first iteration is approximated using the FMN technique so that any possible severe misalignment in frequency between the coarse- and

fine-model responses is first alleviated. The physical parameters are then gradually mapped, following an FPSMN technique.

Linear adaptive frequency-space mapping (LAFSM) is a special case of NSM optimization, corresponding to the situation when the number of hidden neurons of the ANN is zero at all iterations.

## VI. SM-BASED NEUROMODEL OPTIMIZATION

At the  $i$ th iteration of NSM optimization, we use an SM-based neuromodel with small learning error as an improved coarse model, optimizing its parameters to generate the desired response. We denote the SM-based neuromodel response as  $\mathbf{R}_{SMBN}$ , defined as

$$\mathbf{R}_{SMBN}(\mathbf{x}_f) = \left[ \mathbf{R}_{SMBN}^1(\mathbf{x}_f)^T \dots \mathbf{R}_{SMBN}^m(\mathbf{x}_f)^T \right]^T \quad (14)$$

where

$$\mathbf{R}_{SMBN}^r(\mathbf{x}_f) = \left[ R_c^r(\mathbf{x}_{c1}, \omega_{c1}) \dots R_c^r(\mathbf{x}_{cF_p}, \omega_{cF_p}) \right]^T, \quad r = 1, \dots, m \quad (15)$$

with

$$\begin{bmatrix} \mathbf{x}_{c_j} \\ \omega_{c_j} \end{bmatrix} = \mathbf{P}^{(i)}(\mathbf{x}_f, \omega_j, \mathbf{w}^*) \quad (16)$$

$$j = 1, \dots, F_p. \quad (17)$$

The solution to the following optimization problem becomes the next iterate:

$$\mathbf{x}_f^{(2n+i+1)} = \arg \min_{\mathbf{x}_f} U(\mathbf{R}_{SMBN}(\mathbf{x}_f)) \quad (18)$$

with  $U$  defined as in (5). If an SM neuromapping is used to implement  $\mathbf{P}^{(i)}$  (see Fig. 3), the next iterate can be obtained in a simpler manner by solving

$$\mathbf{x}_f^{(2n+i+1)} = \arg \min_{\mathbf{x}_f} \left\| \mathbf{P}_{SM}^{(i)}(\mathbf{x}_f, \mathbf{w}^*) - \mathbf{x}_c \right\|. \quad (19)$$

## VII. NSM ALGORITHM

- Step 0) Find  $\mathbf{x}_c^*$  by solving (5).
- Step 1) Choose  $\mathbf{x}_f^{(1)}, \dots, \mathbf{x}_f^{(2n)}$  following a star distribution around  $\mathbf{x}_c^*$ .
- Step 2) Initialize  $i = 1, \mathbf{x}_f^{(2n+i)} = \mathbf{x}_c^*$ .
- Step 3) Stop if  $\|\mathbf{R}_f(\mathbf{x}_f^{(2n+i)}, \omega_j) - \mathbf{R}_c(\mathbf{x}_c^*, \omega_j)\| \leq \varepsilon_R, j = 1, \dots, F_p$ .
- Step 4) Initialize  $\mathbf{P}^{(i)} = \mathbf{P}^{(i-1)}$ , where

$$\mathbf{P}^{(0)}(\mathbf{x}_f^{(l)}, \omega_j, \mathbf{w}_u) = \begin{bmatrix} \mathbf{x}_f^{(l)} \\ \omega_j \end{bmatrix}, \quad j = 1, \dots, F_p; \quad l = 1, \dots, 2n + i.$$

- Step 5) Find  $\mathbf{w}^*$  by solving (6).
- Step 6) Calculate  $\varepsilon_L$  using (13).
- Step 7) If  $\varepsilon_L > \varepsilon_{\min}$ , increase the complexity of  $\mathbf{P}^{(i)}$  and go to Step 5.
- Step 8) If an SM neuromapping is used to implement  $\mathbf{P}^{(i)}$ , solve (19), otherwise solve (18).
- Step 9) Set  $i = i + 1$ ; go to Step 3.

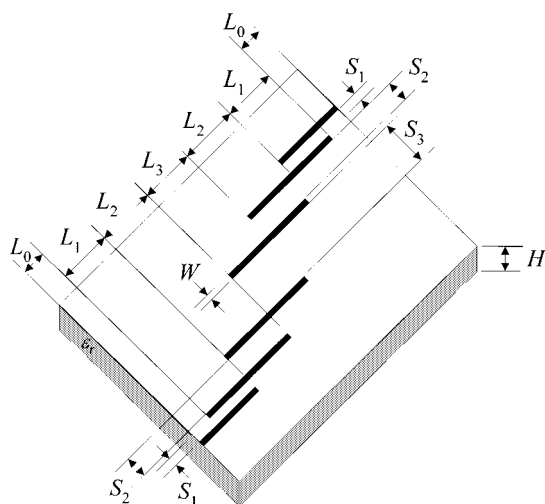


Fig. 8. HTS quarter-wave parallel coupled-line microstrip filter.

### VIII. HTS MICROSTRIP FILTER

We apply NSM optimization to an HTS quarter-wave parallel coupled-line microstrip filter [9], illustrated in Fig. 8.  $L_1$ ,  $L_2$ , and  $L_3$  are the lengths of the parallel coupled-line sections and  $S_1$ ,  $S_2$ , and  $S_3$  are the gaps between the sections. The width  $W$  is the same for all the sections, as well as for the input and output microstrip lines (MSLs), of length  $L_0$ . A lanthanum–aluminate substrate with thickness  $H$  and dielectric constant  $\epsilon_r$  is used.

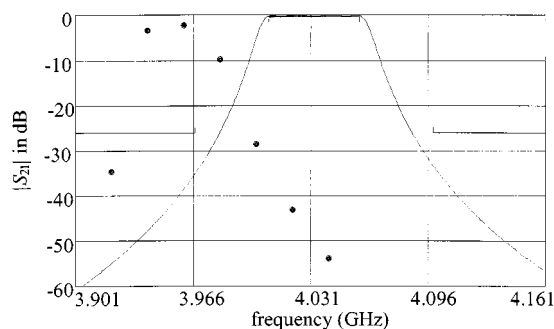
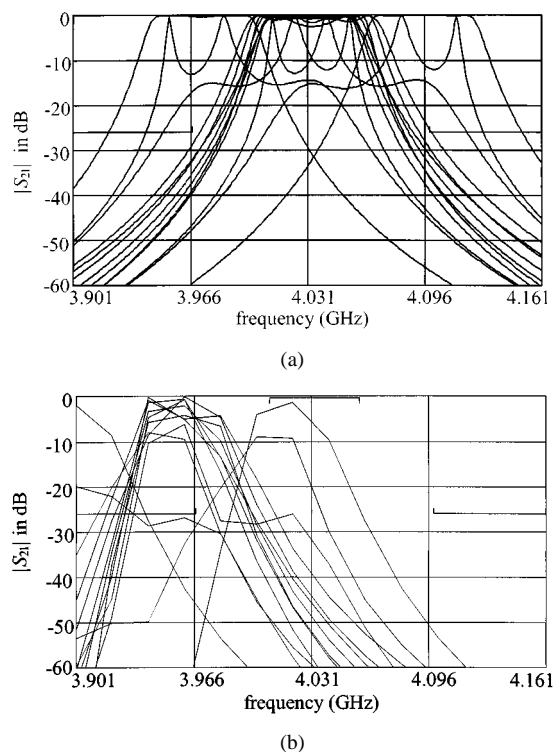
The specifications are  $|S_{21}| \geq 0.95$  in the passband and  $|S_{21}| \leq 0.05$  in the stopband, where the stopband includes frequencies below 3.967 GHz and above 4.099 GHz, and the passband lies in the range (4.008 and 4.058 GHz). The design parameters are  $\mathbf{x}_f = [L_1 \ L_2 \ L_3 \ S_1 \ S_2 \ S_3]^T$ . We take  $L_0 = 50$  mil,  $H = 20$  mil,  $W = 7$  mil, and  $\epsilon_r = 23.425$ , loss tangent =  $3 \times 10^{-5}$ ; the metallization is considered lossless.

Sonnet's *em*<sup>1</sup> driven by Empipe<sup>2</sup> was employed as the fine model, using a high-resolution grid with a 1 mil  $\times$  1 mil cell size. OSA90/hope<sup>3</sup> built-in linear elements MSL, two-conductor symmetrical coupled microstrip lines (MSCLs), and open circuit (OPEN) connected by circuit theory over the same microstrip substrate definition (MSUB) are taken as the “coarse” model.

The following optimal coarse-model solution is found, as in [10]:  $\mathbf{x}_c^* = [188.33 \ 197.98 \ 188.58 \ 21.97 \ 99.12 \ 111.67]^T$  (mils). The coarse- and fine-model responses at the optimal coarse solution are shown in Fig. 9.

The initial  $2n + 1$  points are chosen by performing sensitivity analysis on the coarse model: a 3% deviation from  $\mathbf{x}_c^*$  for  $L_1$ ,  $L_2$ , and  $L_3$  is used, while a 20% is used for  $S_1$ ,  $S_2$ , and  $S_3$ . The corresponding fine and coarse-model responses at these 13 star-distributed learning points are shown in Fig. 10.

Fig. 11 shows the evolution of the learning errors at the  $2n + 1$  points as we increase the complexity of the neuromapping

Fig. 9. Coarse- and fine-model responses at the optimal coarse solution: OSA90/hope (—) and *em* (•).Fig. 10. Coarse- and fine-model responses at the initial  $2n + 1$  base points around the optimal coarse solution. (a) OSA90/hope. (b) *em*.

during the first iteration. All ANNs used in this paper are implemented and trained in OSA90/hope, using Huber optimization, as in [5]. It is seen that mapping the frequency has a dramatic effect on the alignment of the responses, and a simple frequency partial-space mapped neuromapping is needed. The final mapping is implemented with a three-layer perceptron with seven inputs (six design parameters and the frequency), five hidden neurons, and three output neurons ( $\omega$ ,  $L_1$ , and  $S_1$ ).

As indicated in Step 8, we calculate the next point by optimizing the coarse model with the mapping found. The next point predicted is  $\mathbf{x}_f^{(14)} = [185.37 \ 195.01 \ 184.24 \ 21.04 \ 86.36 \ 91.39]^T$  (mils), which matches the desired response with excellent accuracy, as seen in Fig. 12. As a final test, both the FPSMN model and fine model are simulated at the NSM solution  $\mathbf{x}_f^{(14)}$  using a very fine frequency sweep, with a frequency step of 0.005 GHz. The NSM solution satisfies the specifications, as shown in Fig. 13. A detailed illustration of

<sup>1</sup>*em*, version 4.0b, Sonnet Software Inc., Liverpool, NY, 1997.

<sup>2</sup>Empipe, version 4.0, Optimization Systems Associates Inc. (now Agilent EEs of EDA), Dundas, ON, Canada, 1997.

<sup>3</sup>OSA90/hope, version 4.0, Optimization Systems Associates Inc. (now Agilent EEs of EDA), Santa Rosa, CA, 1997.

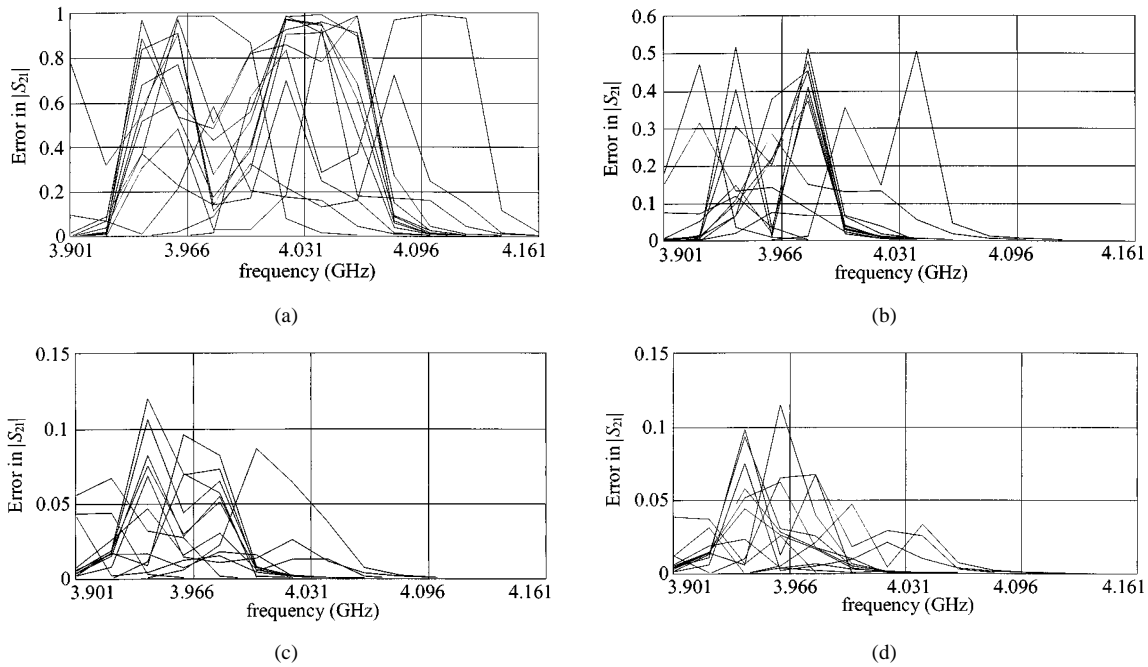


Fig. 11. Learning errors at initial base points. (a) At the starting point. (b) Mapping  $\omega$  with a 3LP:7-3-1. (c) Mapping  $\omega$  and  $L_1$  with a 3LP:7-4-2. (d) Mapping  $\omega$ ,  $L_1$ , and  $S_1$  with a 3LP:7-5-3.

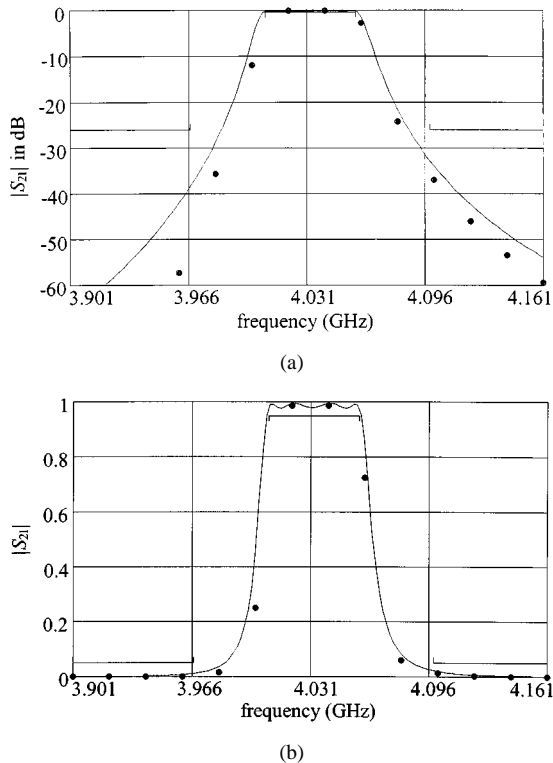


Fig. 12. *em* ( $\bullet$ ) and FPSM 7-5-3 (—) model responses at the next point predicted after the first NSM iteration. (a)  $|S_{21}|$  in decibels. (b)  $|S_{21}|$ .

the passband using an even finer frequency sweep is shown in Fig. 14. The HTS filter is optimized in only one NSM iteration.

#### IX. BANDSTOP MICROSTRIP FILTER WITH OPEN STUBS

NSM optimization is applied to a bandstop microstrip filter with quarter-wave resonant open stubs, illustrated in Fig. 15.  $L_1$  and  $L_2$  are the open stub lengths and  $W_1$  and  $W_2$  are the

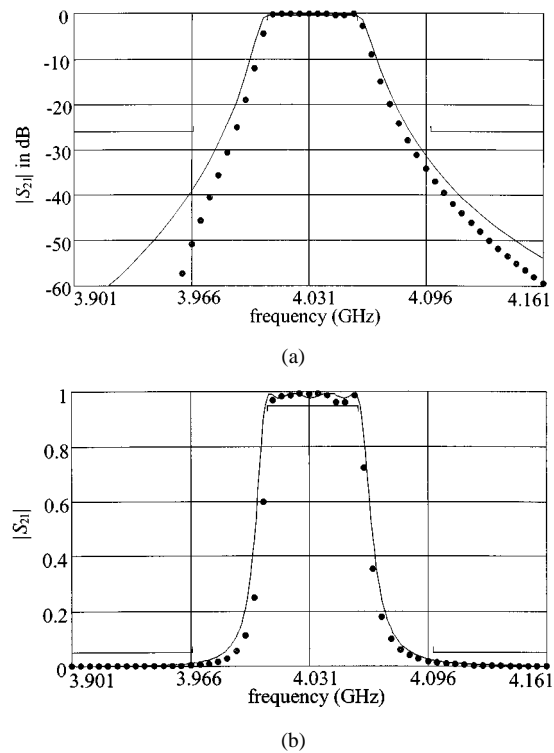


Fig. 13. *em* ( $\bullet$ ) and FPSMN 7-5-3 (—) model responses, using a fine frequency sweep, at the next point predicted after the first NSM iteration. (a)  $|S_{21}|$  in decibels. (b)  $|S_{21}|$ .

corresponding widths. An alumina substrate with thickness  $H = 25$  mil, width  $W_0 = 25$  mil, and dielectric constant  $\epsilon_r = 9.4$  is used for a  $50\text{-}\Omega$  feeding line.

The specifications are  $|S_{21}| \leq 0.05$  in the stopband and  $|S_{21}| \geq 0.9$  in the passband, where the stopband lies between 9.3–10.7 GHz, and the passband includes frequencies below

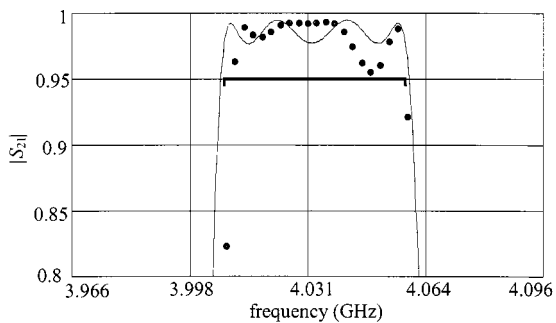


Fig. 14. *em* (•) and FPSMN 7-5-3 (—) model responses in the passband, using a fine frequency sweep, at the next point predicted after the first NSM iteration.

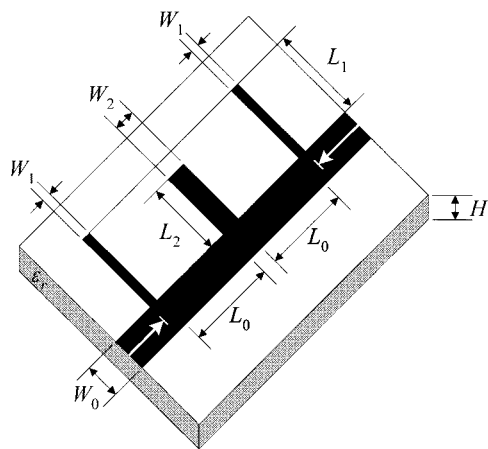


Fig. 15. Bandstop microstrip filter with quarter-wave resonant open stubs.

8 GHz and above 12 GHz. The design parameters are  $\mathbf{x}_f = [W_1 \ W_2 \ L_0 \ L_1 \ L_2]^T$ .

Sonnet's *em* driven by Empipe was employed as the fine model, using a high-resolution grid with a 1 mil  $\times$  1 mil cell size. As a coarse model, we use simple transmission lines for modeling each microstrip section (see Fig. 16) and classical formulas [11] to calculate the characteristic impedance and effective dielectric constant of each transmission line. It is seen that  $L_{c2} = L_2 + W_0/2$ ,  $L_{c1} = L_1 + W_0/2$ , and  $L_{c0} = L_0 + W_1/2 + W_2/2$ . We use OSA90/hope built-in transmission-line elements (TRL).

The following optimal coarse-model solution is found for  $L_0$ ,  $L_1$ , and  $L_2$  of quarter-wave lengths at 10 GHz:  $\mathbf{x}_c^* = [6.00 \ 9.01 \ 106.45 \ 110.15 \ 108.81]^T$  (mils). The coarse- and fine-model responses at the optimal coarse solution are shown in Fig. 17.

The initial  $2n + 1$  points are chosen by performing sensitivity analysis on the coarse model: a 50% deviation from  $\mathbf{x}_c^*$  for  $W_1$ ,  $W_2$ , and  $L_0$  is used, while a 15% deviation is used for  $L_1$  and  $L_2$ . A simple FM neuromapping (see Fig. 6) with two hidden neurons (3LP: 6-2-1,  $\omega$ ) was used to match the responses at the learning base points. The FM neuromodel and fine-model responses at the optimal coarse solution are shown in Fig. 18. Optimizing the FM neuromodel to satisfy the specifications (Step 8 of the NSM algorithm), the next iterate is  $\mathbf{x}_f^{(12)} = [6.54 \ 16.95 \ 91.26 \ 113.30 \ 120.72]^T$  (mils). The coarse- and fine-model responses at this point are shown in Fig. 19.

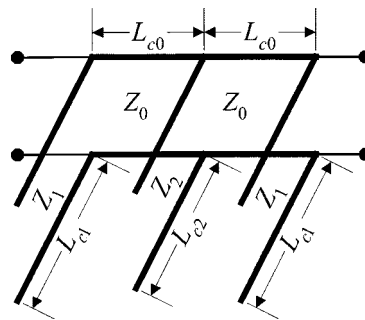


Fig. 16. Coarse model of the bandstop microstrip filter with open stubs.

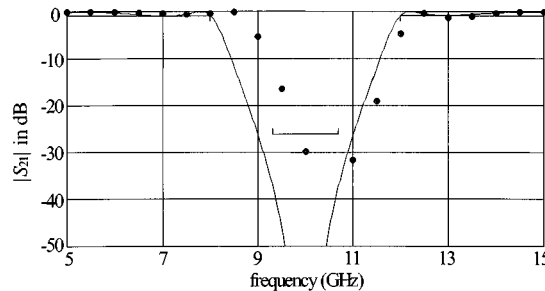


Fig. 17. Coarse- and fine-model responses at the optimal coarse solution: OSA90/hope (—) and *em* (•).

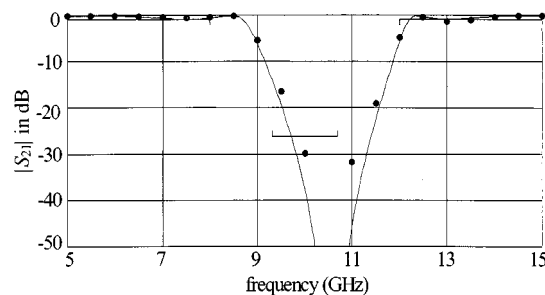


Fig. 18. FM (3LP: 6-2-1,  $\omega$ ) neuromodel (—) and the fine-model (•) responses at the optimal coarse solution.

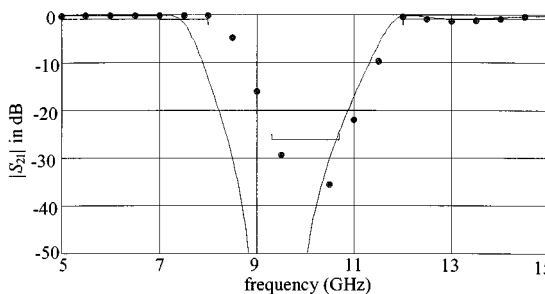


Fig. 19. Coarse- (—) and fine-model (•) responses at the next point predicted by the first NSM iteration.

We performed a second NSM iteration.  $\mathbf{x}_f^{(12)}$  is included in the learning base points. Now, an FPSM neuromapping with three hidden neurons is needed to match the  $2n + 2$  points: only  $\omega$  and  $W_2$  are mapped (3LP: 6-3-2,  $\omega, W_2$ ). Fig. 20 shows the FPSM neuromodel and fine-model responses at  $\mathbf{x}_f^{(12)}$ . Optimizing the FPSM neuromodel, the next iterate is  $\mathbf{x}_f^{(13)} = [5.92 \ 13.54 \ 83.34 \ 114.14 \ 124.81]^T$  (mils). The

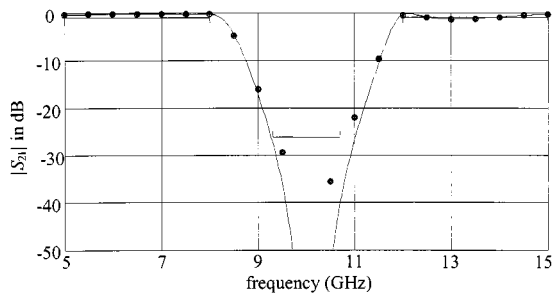


Fig. 20. FPSM (3LP: 6-3-2,  $\omega$ ,  $W_2$ ) neuromodel (—) and the fine-model (•) responses at the point predicted by the first NSM iteration.

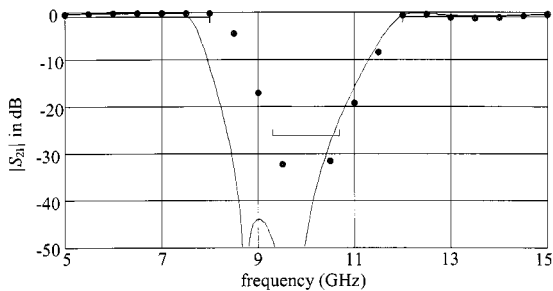


Fig. 21. Coarse- (—) and fine-model (•) responses at the next point predicted by the second NSM iteration.

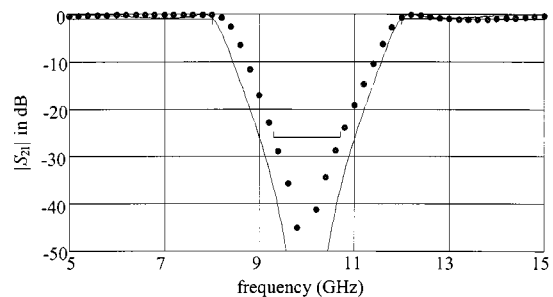


Fig. 22. Fine-model response (•) at the next point predicted by the second NSM iteration and optimal coarse response (—), using a fine frequency sweep.

coarse- and fine-model responses at  $\mathbf{x}_f^{(13)}$  are shown in Fig. 21. As final test, using a fine frequency sweep, we show in Fig. 22 the fine-model response at  $\mathbf{x}_f^{(13)}$  and the optimal coarse response. The bandstop microstrip filter is optimized in two NSM iterations.

## X. CONCLUSION

In this paper, we have presented an innovative algorithm for EM optimization based on SM technology and ANNs. NSM optimization exploits our SM-based neuromodeling techniques to efficiently approximate the mapping from the fine to the coarse input space. NSM does not require parameter extraction to predict the next point. An initial mapping is established by performing upfront fine-model analysis at a reduced number of base points. The coarse-model sensitivities are exploited to select those base points. Huber optimization is used to train simple SM-based neuromodels at each iteration. The SM-based neuromodels are developed without using testing points: their generalization performance is controlled by gradually increasing

their complexity starting with a three-layer perceptron with zero hidden neurons. An HTS quarter-wave parallel coupled-line microstrip filter and a bandstop microstrip filter with quarter-wave resonant open stubs illustrate our optimization technique.

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