

Neutral Density and Crosswind Determination from Arbitrarily Oriented Multiaxis Accelerometers on Satellites

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An iterative algorithm for determining density and crosswind from multiaxis accelerometer measurements on satellites is presented, which works independently of the orientation of the instrument in space. The performance of the algorithm is compared with previously published algorithms using simulated data for the challenging minisatellite payload. Without external error sources, the algorithm reduces rms density errors from 0.7 to 0.03% and rms wind errors from 38 to 1 m/s in this test. However, the effects of the errors in the instrument calibration and the external models that are used in the density and wind retrieval are dominant for the challenging minisatellite payload. These lead to mostly systematic density errors of the order of ~10–15%. The accuracy of the wind results when using the new algorithm is almost fully determined by the sensitivity of the cross-track acceleration component to the calibration and radiation pressure modeling errors. The applicability of the iterative algorithm and the accuracy of its results are demonstrated by presenting challenging minisatellite payload data from a period in which the satellite was commanded to fly sideways and by comparing the density and wind results with those from adjacent days for which the satellite was in its nominal attitude mode. These investigations result in recommendations for the design of future satellite accelerometer missions for thermosphere research.

I. Introduction

ACCCELEROMETERS carried by low-Earth orbiters, such as the Challenging Minisatellite Payload (CHAMP), the Gravity Recovery and Climate Experiment (GRACE), the Gravity Field and Steady-State Ocean Circulation Explorer (GOCE), and the future Swarm satellites provide important data for improving our understanding of thermospheric density and winds. The CHAMP and GRACE missions were not designed for studies of the thermosphere; they carry accelerometers in order to allow for the removal of nongravitational signals from measured orbit perturbations due to inhomogeneities in the Earth's gravity field. Nevertheless, their application to thermosphere studies has resulted in density and wind data sets containing information at unprecedented levels of detail and coverage.

Analyses of accelerometer-derived density data sets resulted in the publication of a large number of scientific papers on topics including the response to drivers, such as solar EUV variability [1,2], geomagnetic storms [3–5], Joule heating [6], solar flares [7], and solar wind streams [8]; and on phenomena such as the equatorial mass density anomaly [9,10], upwelling in the cusp region [11,12], travelling atmospheric disturbances [13], and solar terminator waves [14,15]. These investigations made use of density data, processed using algorithms published by Bruinsma and Biancale [16], Bruinsma et al. [17], Sutton et al. [4,18], Liu et al. [9], and Rentz and Lühr [12].

Investigations of wind results from the CHAMP mission have started to appear in recent years as well. These papers can be classified by their focus on either the low and midlatitudes [14,19–22] or the polar regions [23,24]. An important early paper on wind derivation from accelerometer data is that by Marcos and Forbes [25], who analyzed measurements from the satellite electrostatic triaxial accelerometer instrument flown on several spacecraft in the early 1980s. Recent publications on the derivation of winds from CHAMP data are provided by Liu et al. [19] and Sutton et al. [18] and their respective coauthors.

The current paper contributes to this research topic by presenting an improved, more generally applicable iterative density and wind derivation algorithm. The basic problem to be solved by such an algorithm is that the accelerometer delivers, at most, three orthogonal acceleration observations. However, there are at least four unknowns: density and three orthogonal wind velocity components. The solution to this problem lies in the fact that the orbital velocity of the satellite is much greater than the wind velocity. The error in the total relative velocity, and therefore in the density, can be kept limited by assuming that the in-track wind speed is zero or by applying an in-track wind value from an empirical model. Eliminating this unknown from the equation enables the determination of reasonably accurate density values, as well as wind speed components orthogonal to the in-track direction.

Section II describes the relative velocity components in more detail and discusses the relationship between models and observations of the aerodynamic acceleration. In Sec. III, the previously published algorithms are reviewed, then the new algorithm is presented. Section IV provides an evaluation of the algorithm. Section V contains recommendations for future missions, and Sec. VI summarizes the main conclusions from this work.

II. Accelerations and Velocities

Figure 1 provides a simple schematic view of the three vectors of importance for a density and wind retrieval algorithm: the observed and modeled aerodynamic accelerations \mathbf{a}_{obs} and \mathbf{a}_{mod} are shown

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originating in the center of mass of the satellite. In addition, the velocity \mathbf{v}_r of the atmosphere, relative to the spacecraft, is shown. This quantity is partly observed and partly modeled, as will be explained next. Note that, due to the asymmetrical shape of the satellite with respect to the flow, the acceleration is (in general) not exactly aligned with the relative velocity, as indicated by the dashed guide line.

Due mainly to the approximate character of the modeled density and wind speed, the modeled and observed aerodynamic acceleration vectors initially do not match in magnitude and direction. It is the purpose of the new algorithm to find those density and wind values that, when replacing the original values, make these accelerations match.

Before more detailed descriptions of the previous and new algorithms are provided, the relationship between the parameters in Fig. 1 and the way in which they can be obtained from satellite observation data sets and models will be described. The description in the following sections will refer to the instruments and data products of the current generation of accelerometer missions (CHAMP and GRACE) and to the external models (atmospheric models, force models, etc.) that are currently available. However, the new algorithm is not limited by the use of these data sets and models. It can just as well be applied to equivalent data from historical or future accelerometer missions and benefit from future improvements of external models.

A. Relative Velocity

The relative velocity of the atmosphere with respect to the spacecraft is the sum of the contributions from the inertial velocity of the spacecraft in its orbit \mathbf{v}_o , the velocity caused by the corotating atmosphere \mathbf{v}_c , and the velocity of the winds \mathbf{v}_w with respect to an Earth-fixed atmosphere:

$$\mathbf{v}_r = \mathbf{v}_o + \mathbf{v}_c + \mathbf{v}_w = -R\mathbf{v}_i + R(\boldsymbol{\omega}_\oplus \times \mathbf{r}_i) + \mathbf{v}_w \quad (1)$$

The rotation matrix R from the inertial to the satellite body-fixed (SBF) frame is obtained from star camera observations; the inertial satellite position and velocity, \mathbf{r}_i and \mathbf{v}_i , are obtained by precise orbit determination, using tracking observations made by the satellite's global positioning system (GPS) receiver; $\boldsymbol{\omega}_\oplus$ is the Earth's angular velocity vector. These first two contributors to \mathbf{v}_r are known at a much higher accuracy than the wind velocity \mathbf{v}_w . If model values for \mathbf{v}_w are required, these can be obtained from the horizontal wind model HWM07 [26], for example, and subsequently transformed to the SBF frame.

This paper will use the notation $\mathbf{v}_{r,0}$ or $\mathbf{v}_{r,i=0}$ to indicate an initial guess of the relative velocity, by either neglecting winds or using a wind model. The notation $\mathbf{v}_{r,i}$ will designate a relative velocity that already includes an accelerometer-derived wind component. The index i is an iteration counter.

B. Observed Aerodynamic Acceleration

The observed aerodynamic acceleration \mathbf{a}_{obs} is obtained from the raw accelerometer data after calibration and removal of non-aerodynamic acceleration signals.

Calibration is performed by multiplying the raw acceleration vector with a 3×3 diagonal scale factor matrix and adding a bias vector:

$$\mathbf{a}_{\text{cal}} = S\mathbf{a}_{\text{raw}} + \mathbf{a}_{\text{bias}} \quad (2)$$

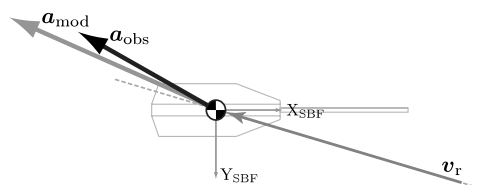


Fig. 1 Relative velocity, modeled and observed accelerations in the CHAMP SBF X–Y plane. CHAMP is viewed from the top.

The scale factors can often be considered (nearly) constant [27], whereas the bias is known to vary on timescales of days and more under the influence of aging effects and temperature variations. Changes to the satellite software or switches between the redundant onboard electronic parts can cause abrupt changes in the calibration parameters. The determination of the calibration parameters used in this study for the in-track accelerometer observations is described by van Helleputte et al. [28], who made use of observations by the satellite's GPS receiver. This method was found to not be sufficiently accurate for the cross-track accelerometer observations, for which an alternative method was applied, as discussed at the end of Sec. IV.A.

Various nonaerodynamic signals should be removed from the accelerometer data, including accelerations due to activity of cold gas thrusters for attitude control. If a set of two opposing thrusters is not perfectly balanced, as is often the case, they introduce a residual signal in the linear acceleration in addition to the intended angular acceleration. Data around the activation times of these thrusters should therefore be removed. A less obvious example of accelerations that should be removed from the data are those due to mechanical forces caused by electrical current changes on the satellite [29].

Finally, modeled accelerations due to radiation pressure from the sun \mathbf{a}_{srp} , the Earth's albedo \mathbf{a}_{alb} , and the Earth's infrared radiation \mathbf{a}_{IR} are computed and removed from the calibrated and edited accelerometer data \mathbf{a}_{cal} to arrive at the observed aerodynamic acceleration vector \mathbf{a}_{obs} :

$$\mathbf{a}_{\text{obs}} = \mathbf{a}_{\text{cal}} - \mathbf{a}_{\text{srp}} - \mathbf{a}_{\text{alb}} - \mathbf{a}_{\text{IR}} \quad (3)$$

The modeling of these radiation pressure forces comprises several nontrivial components: modeling of eclipse and semishadow conditions for solar radiation pressure [30–32], values for the reflectivity and infrared emissivity of Earth surface elements [31,33], and models of the geometry and optical properties of the satellite surfaces. Simple panelized models (of limited accuracy) are available in literature for CHAMP [16] and GRACE [34]. These provide areas A_k and unit normal vectors $\hat{\mathbf{n}}_k$ for 8 to 15 panels. But these models do not provide information on the shape and relative position of each panel. More accurate geometry models, with an arbitrary number of precisely positioned and shaped panels, can be created in specialized software, such as ANGARA [31], based on CAD drawings of the satellites.

The modeled radiation pressure accelerations can then be calculated by either evaluating analytical equations [16,18] or applying a Monte Carlo test particle method [31] on the panelized representation of the satellite. The advantage of the latter approach is that the contributions of multiple reflections of photons and the shadowing of parts of the satellite by other parts are automatically taken into account.

C. Modeled Aerodynamic Acceleration

The modeled aerodynamic acceleration vector \mathbf{a}_{mod} is a function of a large number of parameters. Because the aerodynamic acceleration is found to be proportional to the density ρ and the square of the relative velocity v_r^2 , it is expressed in vector form as

$$\mathbf{a}_{\text{mod}} = C_a \frac{A_{\text{ref}}}{m} \frac{1}{2} \rho v_r^2 \quad (4)$$

If the aerodynamic force components perpendicular to the velocity direction (lift and sideways forces) are omitted, the aerodynamic acceleration reduces to just a drag acceleration, which is (by definition) in the direction of the velocity of the atmospheric particles relative to the spacecraft. Equation (4) then reduces to an equation containing the scalar drag coefficient C_D instead of the force coefficient vector C_a :

$$\mathbf{a}_D = C_D \frac{A_{\text{ref}}}{m} \frac{1}{2} \rho v_r^2 \hat{\mathbf{v}}_r \quad (5)$$

Ignoring the much smaller lift and sideways force components (both perpendicular to drag) is standard practice in applications such

as orbit determination [35], but it introduces errors in the density and wind derivation from accelerometer data. Therefore, we will continue here by using the more general vector equation (4).

The aerodynamic force coefficient vector C_a is a function of the satellite shape, its orientation with respect to the flow, and the nature of the aerodynamic interaction with the atmospheric particles. These aspects will be discussed further in the next paragraphs. The area A_{ref} is a fixed reference value used to make C_a dimensionless. The mass m is obtained by subtracting the used amount of cold gas, which is logged in the satellite's housekeeping data, from the satellite launch mass.

The computation of C_a is, for a large part, analogous to the computation of radiation pressure accelerations, referred to previously. Similar computational techniques can be used, including an evaluation of analytical expressions of the forces acting on a panelized representation of the satellite outer surfaces [16,18,36] or applying a Monte Carlo test particle computation [31].

The description of the interaction of the atmospheric particles with each surface element can be split into two distinct contributions: that of the incident particle flux and that of the reflected or reemitted particle flux. Both contribute to the drag; however, lift and sideways aerodynamic forces are mainly generated by the reflected particle flux.

An exact description of the acceleration contribution by the incident particle flux is possible, but it requires knowledge on the magnitude and direction of the relative velocity \mathbf{v}_r , with respect to the surface element, the atmospheric temperature T , and the relative concentrations c_j of the different particle species ($j = \text{O}_2, \text{N}_2, \text{O}, \text{He}, \text{H}$) with different molecular masses m_j . These latter parameters determine the velocity of the random motion of the molecules and the atoms, which is to be superimposed on the bulk velocity \mathbf{v}_r of the atmosphere with respect to the satellite surface.

Earlier analyses of the CHAMP and GRACE data [4,16–18] used aerodynamic expressions by Cook [37], simplified for compact satellite shapes, which ignored the influence of the random thermal motion of the atoms and the molecules on the aerodynamic force [38]. This resulted in lower drag coefficients and higher densities with larger fluctuations for CHAMP and GRACE. Sutton recently made an update of his aerodynamic model [39] that resulted in a much improved fidelity of the density data [40], a difference which we have been able to confirm in our own processing.

Contrary to previous analyses [16], we do not use a mean molecular mass but calculate C_a as the concentration-weighted sum of contributions from the various constituents j , because the dependence of these contributions on the molecular mass is highly nonlinear. When a small concentration of lightweight constituents (such as helium) is present, this does not affect the mean molecular mass by much. However, these lightweight particles, because of their high thermal velocity, will have a higher collision rate with the satellite's side panels (which are oriented nearly parallel to the stream) than with the heavier constituents (such as oxygen or nitrogen). This will result in significantly larger values of C_a , especially for the elongated satellite shapes of the current accelerometer missions.

A description of the reflected particle flux requires a model of the gas–surface interaction, which specifies the angular distribution and energy flux of the reflected particles. Unfortunately, experimental data on gas–surface interaction [41,42] are limited to only a subset of the range of conditions under which current space accelerometers are making measurements. This puts an exact physical representation of this contribution to the aerodynamic force out of reach.

Ideally, information on the gas–surface interaction, as well as in situ observations of aerodynamic model parameters (like the temperature T and concentrations c_j) should be measured by independent instruments on the accelerometer-carrying satellite. Because the current and planned accelerometer missions lack the required instrumentation, we have to rely on empirical atmosphere models, such as NRLMSISE-00 [43], simplified gas–surface interaction models, and some educated guesses.

Such simplified gas–surface interaction models contain parameters like the energy flux accommodation coefficient α [44], which determines whether the particles retain their mean kinetic energy (for $\alpha = 0$) or acquire the temperature of the spacecraft

surface T_{wall} (for $\alpha = 1$). Another possible parameter is the Maxwell coefficient σ , which determines the fraction of particles that leaves the surface in either a completely diffuse ($\sigma = 1$) or completely specular ($\sigma = 0$) angular distribution.

With these caveats in mind, the rarefied aerodynamic equations for flat panels, derived by Sentman [45], are currently seen as an appropriate choice for use in the processing of the CHAMP and GRACE data. Sentman's equations take into account the random thermal motion of the incident particles and assume a completely diffuse distribution of the reflected particle flux. This is reasonably consistent with the limited data from in-orbit gas–surface interaction experiments [41,46], which suggest that (over the altitude range of CHAMP and GRACE) the angular distribution is likely within a few percent of complete diffuse reemission ($\sigma \gtrsim 0.95$), and that the energy flux accommodation is quite high ($\alpha \gtrsim 0.8$). Moe et al. [44] introduced the energy flux accommodation coefficient α as a parameter in Sentman's equations [45]. Our implementation of this modification of Sentman's equations for accelerometer data processing is similar to the one recently published by Sutton [39]; therefore, we shall not repeat the equations here.

For the purposes of this paper, it is sufficient to keep in mind that C_a is an intricate function of the relative velocity and parameters related to the spacecraft and the surrounding atmosphere:

$$C_a = C_a(\mathbf{v}_r, c_j, T, A_k, \hat{\mathbf{n}}_k, T_{\text{wall},k}, \alpha, \dots) \quad (6)$$

III. Processing Algorithms

A. Direct Algorithms for CHAMP and GRACE

Previously published algorithms made use of assumptions about the orientation of the accelerometer in space. For CHAMP and GRACE, the accelerometer instruments are carefully mounted near the satellite center of mass and oriented so that their three axes can be considered perfectly aligned with the SBF axes. The spacecraft are under active attitude control, which keeps these axes within a few degrees of the orbit-fixed along-track, cross-track, and radial directions (see Fig. 2). The relative orientation of these axes can be expressed in roll, pitch, and yaw Euler angles.

Because these Euler angles are relatively small, the inertial orbital velocity of the satellite is kept closely aligned with the X_{SBF} axis. It is known from orbital mechanics that accelerations in the velocity direction are the most effective in changing the orbital energy and, therefore, have a much larger effect on the orbit than accelerations of similar magnitude in perpendicular directions. This means that the X_{SBF} axis of the accelerometer can be more accurately calibrated using positioning data from the GPS instrument [28] than the Y_{SBF} and Z_{SBF} axes, even without taking into account the larger measured signal. This consideration leads to an approach for density determination [16–18], for which only the projection of the aerodynamic acceleration on the X_{SBF} axis is used, as shown schematically in Fig. 3. The density can be solved directly from the X component of the vector equation (4):

$$\rho = \frac{2m}{A_{\text{ref}} v_{r,0}^2} \frac{a_{\text{obs},x}}{C_{a,x}} \quad (7)$$

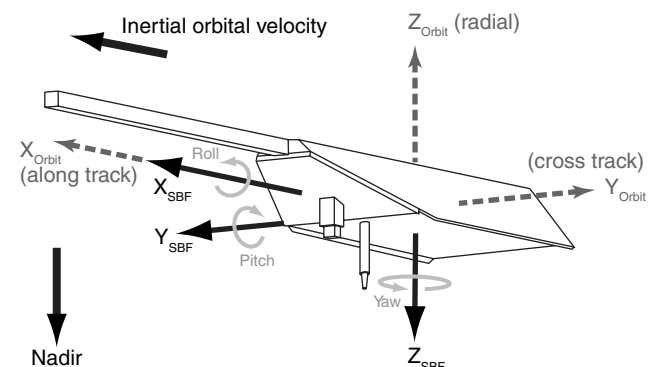


Fig. 2 Definition of SBF axes for CHAMP and their relative orientation with respect to the orbit-fixed axes in the satellite's nominal attitude.

Information from the acceleration component in the Y_{SBF} direction, closely aligned with the cross-track direction, can be used to derive data on the wind speed in that direction. Sutton et al. [18] describe two approaches. In the first approach, C_a in Eq. (4) is expanded using analytical equations and evaluated by summation over a 13-panel satellite model, which incorporates the computation of both the drag and lift on each two-dimensional panel. The resulting equation is quadratic with respect to $v_{w,y}$, which can then be solved, resulting in an expression depending on $a_{\text{obs},y}$ and ρ . Sutton named this approach the single-axis method, even though information from both the X and Y axes is required if ρ is to be substituted from Eq. (7).

The second approach was named the dual-axis method by Sutton et al. [18] and can be found in an earlier paper by Liu et al. [19] as well. The method requires that the lift and sideways forces are negligible or are modeled and removed from the acceleration beforehand, so that only the observed acceleration due to drag $\mathbf{a}_{\text{obs},D}$ remains. The authors do not specify exactly how the lift and sideways forces should be modeled, but we have adopted the following approach: a new modeled aerodynamic acceleration is computed according to Eq. (4), with the density from Eq. (7) and the a priori relative velocity $\mathbf{v}_{r,0}$ as inputs. This acceleration vector \mathbf{a}_{mod} can then be decomposed into a drag component, by projection on the relative velocity direction and a perpendicular lift plus sideways force component, by subtraction of that drag component from the original modeled acceleration. In equations,

$$\mathbf{a}_{\text{mod},D} = (\mathbf{a}_{\text{mod}} \cdot \hat{\mathbf{v}}_{r,0})\hat{\mathbf{v}}_{r,0}; \quad \mathbf{a}_{\text{mod},L} = \mathbf{a}_{\text{mod}} - \mathbf{a}_{\text{mod},D} \quad (8)$$

The modeled lift plus sideways aerodynamic force $\mathbf{a}_{\text{mod},L}$ is then subtracted from the observed aerodynamic acceleration to arrive at the observed drag:

$$\mathbf{a}_{\text{obs},D} = \mathbf{a}_{\text{obs}} - \mathbf{a}_{\text{mod},L} \quad (9)$$

The velocity and drag acceleration are (by definition) in the same direction, so that the wind can be determined from a simple geometrical consideration (see Fig. 4). Expressed in the form of an equation, ρ and C_D disappear when the Y component of Eq. (5) is divided by the X component, and $v_{w,y}$ is solved for after the substitution of Eq. (1), resulting in

$$v_{w,y} = \frac{a_{\text{obs},D,y}}{a_{\text{obs},D,x}} v_{r,0,x} - v_{r,0,y} \quad (10)$$

A similar wind determination could, in principle, be performed for the Z_{SBF} axis. However, the aerodynamic acceleration in this direction is, in general, too small when compared with errors in the instrument calibration, the radiation pressure model, and the lift force model. In addition, on the CHAMP accelerometer, this Z_{SBF} component suffers from a malfunction that prevents the acquisition of accurate data [47].

B. Discussion of the Direct Algorithms

The schematic representations in Figs. 3 and 4 clearly show that when the angle between the relative velocity and the X_{SBF} axis gets larger, the errors in the density and wind increase. For the extreme case in which this angle approaches 90 deg, density values will approach zero, whereas the wind speed will go to infinity. Of course, the angles in these figures are exaggerated for clarity, in the case of CHAMP and GRACE under nominal attitude control. The

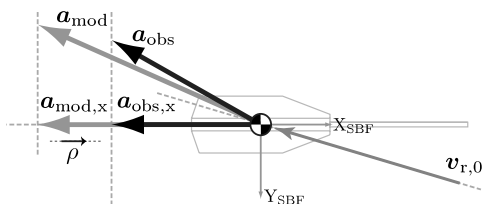


Fig. 3 Schematic representation of the direct determination of density from the projection of accelerations on the X_{SBF} axis.

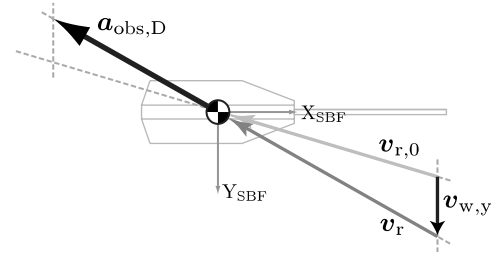


Fig. 4 Schematic representation of the direct determination of wind from the accelerometer Y_{SBF} axis.

roll, pitch, and yaw Euler angles are kept within ± 1 deg for GRACE and ± 2 deg for CHAMP. For the future Swarm mission, the attitude will likely be somewhat more loosely controlled, probably to within ± 4 deg.

These attitude angles only determine the alignment of the body-fixed frame with the inertial velocity vector. The contributions to the relative velocity vector by the corotation of the atmosphere and the thermosphere winds can be equally important. The atmospheric corotation velocity over the equator depends on the altitude, ranging from 483–502 m/s at 250–500 km. This increases the maximum angle between the relative velocity and the X_{SBF} axis by 3.6–3.8 deg. The wind speed, which under most conditions is within the range of about 0–200 m/s, can reach peak velocities in the polar regions of up to 500–1000 m/s [23,24], causing the incidence angle to reach peak values of 8–10 deg. In principle, the accuracy of the derived density and the wind speed should be independent of these angles.

Another limiting factor of the direct algorithm results from the dependence of C_a on \mathbf{v}_r . The methods use an initial value $\mathbf{v}_{r,0}$, composed of the orbit and corotation velocity, and neglect to model the in-track wind velocity. After the derivation of the cross-track wind $v_{w,y}$, however, there is a better estimate of the relative velocity

$$\mathbf{v}_{r,i=1} = \mathbf{v}_{r,0} + \mathbf{v}_{w,y} \quad (11)$$

where the index i is an iteration counter. This new relative velocity leads to a new value of C_a [according to Eq. (6)] and, therefore, to a new value of ρ . The change in C_a also leads to a change in the lift and sideways components of the aerodynamic acceleration, which are to be removed from \mathbf{a}_{obs} to arrive at $\mathbf{a}_{\text{obs},D}$, yielding a new value for $v_{w,y}$. This chain of dependencies indicates that an iterative algorithm is more suitable to determine the density and the wind speed with high accuracy.

C. Iterative Algorithm

This section presents an iterative algorithm, which avoids the restrictions and sources of error discussed in the previous section. Figure 5 schematically illustrates the principle of the algorithm in two steps. The goal of the algorithm is to make the modeled aerodynamic acceleration \mathbf{a}_{mod} match the direction (top panel) and, subsequently, the magnitude (bottom panel) of the aerodynamic acceleration observed by the accelerometer \mathbf{a}_{obs} . This is achieved by first modifying the direction of the relative velocity vector \mathbf{v}_r , without modifying its magnitude, until the modeled acceleration direction matches that of the observed acceleration. Subsequently, the density ρ is modified, so that the magnitude of the accelerations matches.

The adjustment to the orientation is made by a rotation of the relative velocity about the local vertical direction, indicated by the unit vector $\hat{\mathbf{u}}_{\text{up}}$. The acceleration components projected on this direction will be set to zero. To simplify the notation, a prime is added to indicate this modification of the acceleration vectors, which is applied repeatedly:

$$\mathbf{a}' = \mathbf{a} - (\mathbf{a} \cdot \hat{\mathbf{u}}_{\text{up}})\hat{\mathbf{u}}_{\text{up}} \quad (12)$$

We will use the sum of the orbital and corotation velocities as our a priori relative velocity for now:

$$\mathbf{v}_{r,i=0} = \mathbf{v}_o + \mathbf{v}_c \quad (13)$$

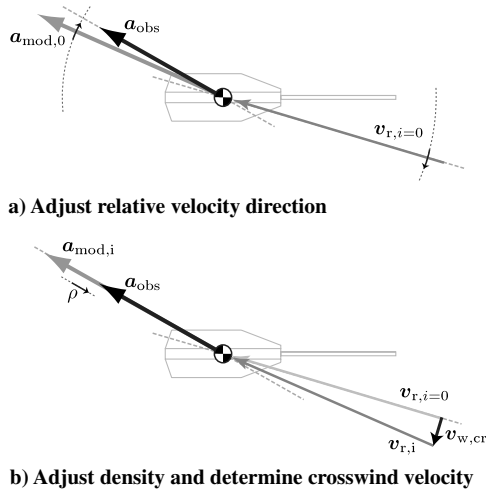


Fig. 5 Schematic representation of the iterative wind and density derivation.

The possibility of including modeled in-track and vertical wind velocities in the algorithm computation will be discussed in Sec. III.D.

While modifying the direction of the velocity and the modeled acceleration vectors, the magnitude of the acceleration is not of importance. We therefore make use of the unit vectors \hat{a}'_{obs} and \hat{a}'_{mod} and, according to Eq. (4), substitute \hat{C}'_a for the latter. We can now define our measure of the acceleration direction residual:

$$\mathbf{d} = \hat{a}'_{\text{obs}} - \hat{a}'_{\text{mod},i} = \hat{a}'_{\text{obs}} - \hat{C}'_a(\mathbf{v}_{r,i}, \dots) \quad (14)$$

In practice, if the magnitude of \mathbf{d} is below a certain predefined threshold ϵ , convergence has been reached. Otherwise, another iteration is required. The convergence criterium is thus

$$d = \|\mathbf{d}\| < \epsilon \quad (15)$$

The unit vector representing the direction of the velocity adjustment for the current iteration is defined to be perpendicular to both the relative velocity and the rotation axis:

$$\hat{\mathbf{v}}_{\text{adj},i} = \frac{\mathbf{v}_{r,i} \times \hat{\mathbf{u}}_{\text{up}}}{\|\mathbf{v}_{r,i} \times \hat{\mathbf{u}}_{\text{up}}\|} \quad (16)$$

Next, to start our numerical differentiation, two relative velocity vectors are formed, which keep the magnitude of the unadjusted relative velocity but are rotated slightly in both directions with respect to the relative velocity of the current iteration:

$$\mathbf{v}_r^+ = \|\mathbf{v}_{r,i}\| \frac{\mathbf{v}_{r,i} + \delta \hat{\mathbf{v}}_{\text{adj},i}}{\|\mathbf{v}_{r,i} + \delta \hat{\mathbf{v}}_{\text{adj},i}\|}; \quad \mathbf{v}_r^- = \|\mathbf{v}_{r,i}\| \frac{\mathbf{v}_{r,i} - \delta \hat{\mathbf{v}}_{\text{adj},i}}{\|\mathbf{v}_{r,i} - \delta \hat{\mathbf{v}}_{\text{adj},i}\|} \quad (17)$$

These modified relative velocities will result in modified modeled acceleration directions, for which we will apply the model of Eq. (6). The results from both rotation directions are substituted into Eq. (14):

$$\mathbf{d}^+ = \hat{a}'_{\text{obs}} - \hat{C}'_a(\mathbf{v}_r^+, \dots); \quad \mathbf{d}^- = \hat{a}'_{\text{obs}} - \hat{C}'_a(\mathbf{v}_r^-, \dots) \quad (18)$$

The vector difference between the two velocity vectors is

$$\Delta \mathbf{v}_r = \mathbf{v}_r^+ - \mathbf{v}_r^- \quad (19)$$

and the effect of this velocity rotation on the acceleration direction residual is

$$\Delta d = \|\mathbf{d}^+\| - \|\mathbf{d}^-\| \quad (20)$$

Now, all the elements are in place to compute the next iteration of the relative velocity, which keeps the magnitude of the original velocity but changes the direction:

$$\mathbf{v}_{r,i+1} = \|\mathbf{v}_{r,i}\| \frac{\mathbf{v}_{r,i} - d(\Delta \mathbf{v}_r / \Delta d)}{\|\mathbf{v}_{r,i} - d(\Delta \mathbf{v}_r / \Delta d)\|} \quad (21)$$

At this point, Eqs. (14) and (15) are reevaluated. If the convergence criterium of Eq. (15) is met, we can proceed computing the crosswind speed and mass density:

$$\mathbf{v}_{w,\text{cr}} = \mathbf{v}_{r,i} - \mathbf{v}_{r,i=0} \quad (22)$$

$$\rho = \frac{2m}{A_{\text{ref}} v_{r,i}^2} \frac{\|\mathbf{a}'_{\text{obs}}\|}{\|\mathbf{C}'_{a,i}\|} \quad (23)$$

D. Modeling of In-Track and Vertical Winds

In the previously mentioned descriptions of the algorithms, we have not discussed the possible effect on the aerodynamics of the wind components, other than the cross-track component. Because we are interested in retrieving the crosswind $\mathbf{v}_{w,\text{cr}}$ from the accelerometer data, a model value for this component should not be included in the a priori relative velocity of Eq. (13). However, a model value for the in-track wind $\mathbf{v}_{w,\text{it}}$ and the wind in the direction of the rotation axis $\mathbf{v}_{w,\text{up}}$ could be applied in that equation. These can be computed by projecting the full model wind on the unit vectors in these directions:

$$\mathbf{v}_{w,\text{it}} = (\mathbf{v}_{w,\text{mod}} \cdot \hat{\mathbf{v}}_r) \hat{\mathbf{v}}_r \quad (24)$$

$$\mathbf{v}_{w,\text{up}} = (\mathbf{v}_{w,\text{mod}} \cdot \hat{\mathbf{u}}_{\text{up}}) \hat{\mathbf{u}}_{\text{up}} \quad (25)$$

Because $\hat{\mathbf{v}}_r$ changes its direction during the iterative process described in the previous section, Eq. (24) will have to be reevaluated, and \mathbf{v}_r [in Eqs. (17) and (21)] will have to be updated after each iteration step.

IV. Algorithm Tests

A. Error Assessment Using Simulated Accelerometer Data

The direct and iterative algorithms were tested using simulated aerodynamic acceleration data in order to verify their correct implementation and assess the accuracy of their results, both in the absence and presence of errors in the input data and the models.

The simulated aerodynamic acceleration data were generated by applying Eq. (4) and by using modeled density ρ_m and wind $\mathbf{v}_{w,m}$ values from the NRLMSISE-00 density model [43] and the HWM07 wind model [26]. The real CHAMP attitude and orbit data were used, both in the generation of this simulated acceleration data and in the application of the retrieval algorithms. The accuracy of the algorithm results, comprising the density ρ and the crosswind $v_{w,y}$ or $v_{w,\text{cr}}$, can then be tested by examining the density and wind residuals r_ρ and r_v .

The density residuals are expressed as percentages relative to the simulated density signal:

$$r_\rho = \frac{\rho - \rho_m}{\rho_m} \cdot 100\% \quad (26)$$

The wind residuals are defined as the differences between the retrieved wind speed and the modeled wind speed's projection on the direction of the retrieved wind speed:

$$r_v = v_{w,y} - v_{w,m} \cdot \hat{\mathbf{v}}_{w,y} \quad (27)$$

or

$$r_v = v_{w,\text{cr}} - v_{w,m} \cdot \hat{\mathbf{v}}_{w,\text{cr}}$$

Six cases for simulated errors are defined. In the first case, labeled identical input, the exact same models and input data were used in the

retrieval algorithm that had been originally applied in the creation of the simulated accelerations. This allows for an assessment of the errors that are purely inherent in the algorithm.

However, it is also important to evaluate the algorithms under the influence of the uncertainties in the input data and the models. In two further cases, named X_{SBF} offset and Y_{SBF} offset, a value of 10 nm/s^2 was added to the simulated acceleration data in either direction before applying the algorithms. For each single measurement, such an offset could be the result of an error in the instrument calibration or due to errors in the removal of radiation pressure and attitude thruster accelerations. Each of these error sources comes with its own temporal variation of the acceleration error, and their effects can either add up or (partly) cancel each other out. Therefore, the constant 10 nm/s^2 offset introduced here should be viewed as just a crude approximation, which should nevertheless give some idea of the sensitivity of the density and wind derivation algorithms. In the fourth test case, named in-track wind, the HWM07-modeled wind in the in-track direction was neglected in the density and crosswind derivation algorithms.

Two further test cases are used to assess the effect of force model errors. The simulated aerodynamic accelerations were generated with a value of $\alpha = 0.93$ for the energy flux accommodation parameter in the aerodynamic model. In the energy accommodation case, this value was changed to $\alpha = 0.88$ for the density and wind retrieval. This 5% difference can be used to represent one aspect of the inherent uncertainty in the gas-surface interaction modeling. The final test case, named panel model, is used to represent the uncertainty in the satellite geometry model for complexly shaped satellites, such as CHAMP. Our own adjusted panelized geometrical model of the CHAMP satellite [48], used in the simulated data generation, was replaced by an alternative one [16] in the density and wind retrieval. This replacement amounts to a reduction in the frontal area of around 14% when the satellite is viewed along the X_{SBF} axis (front) and of 8% when viewed along the Y_{SBF} axis (side).

The statistics of the density retrieval residuals over the complete year of 2004 (~ 3.15 million measurements) are presented in Table 1. During this year, CHAMP flew only in its nominal attitude mode, for which the direct algorithm is applicable. The data in the table show that the iterative algorithm leads to lower density residuals than the direct approach in the identical input case. With the 10 nm/s^2 Y_{SBF} acceleration offset, this ranking is shifted, because the iterative algorithm is sensitive to this acceleration component, whereas the direct algorithm is not. Both algorithms show an equal sensitivity to in-track wind errors. However, the direct algorithm seems slightly more sensitive to the force-model-related errors if judged by the standard deviations. Note that, for the force-model-related errors, the mean values are generally larger than the standard deviations, indicating that these accelerometer-derived density data are affected by mostly systematic errors. The data will therefore be more suitable to studies of relative changes in density than for use in modeling approaches that require absolute density values.

Table 1 Statistics of the density retrieval residuals in percentages of the density signal

	Min	Mean	Max	RMS	Std
Direct algorithm					
Identical input	-3.3	0.0	5.5	0.7	0.7
X_{SBF} offset	-17.4	-2.7	3.8	3.1	1.5
Y_{SBF} offset	-3.3	0.0	5.5	0.7	0.7
In-track wind	-10.8	0.2	14.3	2.2	2.1
Energy accomm	-4.8	-1.7	3.7	1.9	0.7
Panel model	3.5	7.8	14.0	7.9	0.9
Iterative algorithm					
Identical input	-0.5	-0.0	0.0	0.0	0.0
X_{SBF} offset	-17.4	-2.9	0.5	3.2	1.4
Y_{SBF} offset	-12.3	-0.3	4.5	1.6	1.6
In-track wind	-10.9	0.2	13.6	2.0	2.0
Energy accomm	-2.1	-1.6	-0.7	1.6	0.2
Panel model	5.7	8.1	9.0	8.1	0.3

In the wind residual statistics, presented in Table 2, the advantage of the iterative algorithm over the direct approach is evident, certainly for the identical input case. For both algorithms, the 10 nm/s^2 error introduced in the Y_{SBF} direction of the accelerations has a very large detrimental effect on the accuracy of the crosswind speed, leading to maximum errors of 915 m/s (iterative) and 1283 m/s (direct). Such very large wind errors will occur in the real data processing when the aerodynamic acceleration signal in the Y_{SBF} direction is small when compared with the instrument calibration, the instrument noise, and the radiation pressure errors for that direction. These large wind errors are, therefore, prevalent at conditions of low density, such as at higher orbital altitudes and lower solar activity levels. For this reason, it is not currently possible to acquire an accurate crosswind derivation from the GRACE satellites, which are at a higher altitude than CHAMP. A related important factor in this respect is the magnitude of cross-track radiation pressure accelerations and related acceleration errors. These occur when the satellite's orbital plane is near-perpendicular to the sun-Earth vector (dawn-dusk orbit). We have also encountered particularly extreme wind errors around eclipse transitions. A small discrepancy between the modeled and the true eclipse geometry will lead to short periods with an incorrect application or removal of the full modeled radiation pressure acceleration, which has a maximum magnitude of around 40 nm/s^2 for CHAMP, leading to wind errors far exceeding 1000 m/s .

The results in Table 2 show that the crosswind derivation is practically insensitive to errors in the along-track wind. The other error sources also have only minor effects in comparison with the Y_{SBF} offset.

It should be clear that a large aerodynamic signal strength, a careful calibration of the accelerometer in the crosswind direction, and an accurate modeling of cross-track radiation pressure accelerations are a necessity for the derivation of accurate crosswind results.

The Y_{SBF} (cross-track) calibration for the CHAMP and GRACE satellites using GPS data is problematic [28], because of the relatively low acceleration signal and the limited capability of accelerations in this direction to perturb the orbit, when compared with along-track accelerations. Both limitations are the result of fundamental orbital dynamics in combination with the tight attitude control of the spacecraft, as discussed at the start of Sec. III.A. Therefore, we adopted an alternative approach to calibrate CHAMP's Y_{SBF} accelerometer data, analogous to Sutton et al. [18]. We took density observations, derived using the direct method from the X_{SBF} data, and combined these with the aerodynamic satellite model to arrive at simulated observations for the Y_{SBF} data. The accelerometer data for this direction were then calibrated by estimating the biases that minimize the difference between the data and these simulated observations. We have checked the reliability of these biases by comparing the local time variation of the zonal wind from ascending arcs with those from descending arcs and found no systematic difference. An error in the Y_{SBF} biases would influence the ascending and descending wind profiles in opposite directions.

Table 2 Statistics of the wind retrieval residuals in m/s

	Min	Mean	Max	RMS	Std
Direct algorithm					
Identical input	-225	-1	202	38	38
X_{SBF} offset	-226	-2	210	44	44
Y_{SBF} offset	-173	209	1285	236	110
In-track wind	-228	-2	205	38	38
Energy accomm	-258	-1	222	52	52
Panel model	-262	-2	224	54	54
Iterative algorithm					
Identical input	-9	-0	10	1	1
X_{SBF} offset	-44	3	81	12	12
Y_{SBF} offset	-242	81	915	140	114
In-track wind	-9	-0	10	1	1
Energy accomm	-55	-0	51	21	21
Panel model	-52	0	49	22	22

Users of accelerometer-derived density and wind data should be aware of the level and nature of errors inherent in these data, as presented in this section.

B. CHAMP Accelerometer Data for Different Satellite Attitude Modes

The CHAMP mission provides an interesting possibility for further assessment of the capabilities of the iterative algorithm. There have been two periods (7–8 October 2001 and 6 November 2002) when CHAMP was commanded to fly sideways, with respect to its nominal altitude, for about seven orbital revolutions (~ 11 h). Figure 6 shows the CHAMP calibrated accelerometer data with the modeled radiation pressure accelerations removed for three days surrounding the sideways-flying attitude period on November 6, 09:00–20:00 coordinated universal time (UTC). The shaded areas correspond to three orbits of data, starting at 12:00 UTC each day, and lasting about 1.5 h, which will be used in the next analysis. The three small drawings at the top of Fig. 6 give an indication of the CHAMP satellite geometry, as viewed from the nominal orbital velocity direction.

Notice that the drag acceleration is in the Y_{SBF} direction during the sideways-flying period, and it is approximately three times larger than the drag in the X_{SBF} direction during the surrounding nominal (forward-flying) period. This higher drag acceleration in the sideways-flying period is the result of the larger frontal area, but this is offset to some extent by a lower drag coefficient.

Basically, these two attitude modes present us with two completely different aerodynamic shapes with respect to the flow. In the forward-flying configuration, CHAMP is a long and slender shape, with only a small frontal area, but with its large solar panel and bottom surfaces oriented parallel to the stream. A considerable fraction of the aerodynamic acceleration on the shape in this orientation is due to collisions with these parallel surfaces, which cause an increase in the drag coefficient. In the sideways-flying configuration, CHAMP is a wide and short object, with most of the aerodynamic force caused by near-frontal collisions and only a relatively small contribution by surfaces parallel to the stream.

Unfortunately, the satellite was not designed to operate in the sideways-flying mode for extended periods of time. Both the attitude

control actuation and the thermal environment of the accelerometer instrument will have been quite different than during nominal operations on the surrounding days. The different orientation of the instrument also has consequences for the accuracy of the instrument calibration (see the discussion at the end of Sec. IV.A). These considerations are important to keep in mind in the interpretation of this data.

Figure 7 shows the density and wind retrieval results, using the iterative algorithm for the three orbits indicated with background shading in Fig. 6. The black, light gray, and dark gray solid lines represent the accelerometer-derived density and wind results for the sideways-flying day and the nominal previous and next days, respectively. These shades also correspond to the model results for these orbits, plotted with open circles in the same figure.

The local solar time at the equator crossings for these orbits was approximately 09:40 (ascending) and 21:40 (descending) during this period. The shaded background indicates where the satellite was in eclipse. The 24-h interval between the three orbits was chosen so that each of the orbits crosses the auroral zones at approximately the same magnetic local time, thus reducing variability by keeping the sampling characteristics as similar as possible. Because proxies of solar EUV radiation and geomagnetic activity also show little variation during this period, the NRLMSISE-00 and HWM07 model curves for the orbits on the three different days show largely the same magnitudes and patterns. The large scale density patterns are determined by variations in orbital altitude, between 396/400 km at the evening/morning equator crossings and 417 km over the poles, and by thermospheric features, such as the diurnal density bulge, causing the absolute maximum in density around the morning equator crossing.

The density retrieved by CHAMP resembles this behavior but is, in general, around 15–25% lower than the model values. It is unlikely that such a large offset can be fully attributed to systematic errors in the accelerometer-derived data alone, so it should be at least partly due to the density model error as well. Such offsets between the model and the observed density values are seen in other data sets and at other times in our CHAMP data set as well, but a further analysis must be delegated to a future paper. Another significant difference between the density model data and the CHAMP results are the sharp spikes at high latitudes, especially in the southern hemisphere evening sector, which could be related to upwelling in the polar cusp

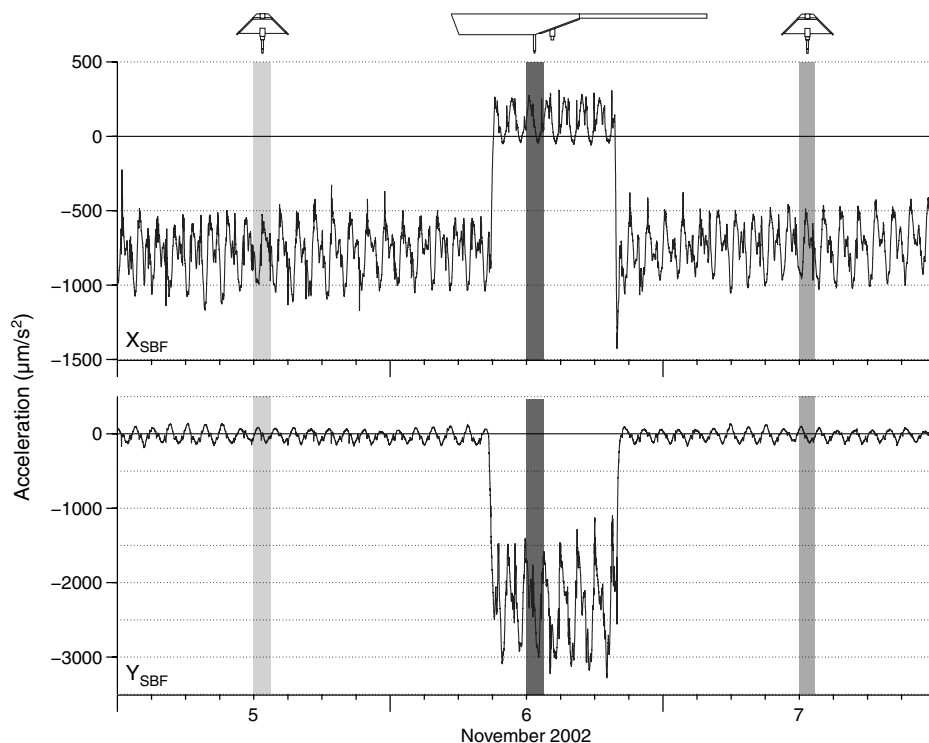


Fig. 6 Calibrated CHAMP accelerometer data, with modeled radiation pressure removed, for three days surrounding the 6 November 2002 sideways-flying period.

region [11,12] and/or errors due to poorly modeled in-track wind variations.

The CHAMP density data from the sideways-flying period show largely the same features as the data for the two surrounding days, but they are (on average) slightly higher. This difference could be due to different errors in the satellite geometry and the aerodynamic interaction modeling for the two attitude modes, but it is not possible to distinguish such an effect from the natural density variability over these days.

We shall now turn our attention to the zonal wind data in Fig. 7. The model zonal winds at low and midlatitudes are at around 100 m/s, eastward in the evening and westward in the morning, away from the subsolar density bulge. The modeled winds at high latitudes show a complex behavior with much shorter wavelengths, related to geomagnetic energy inputs, with peaks of around 300 m/s eastward in the southern hemisphere and around 200 m/s westward in the northern hemisphere. The most obvious feature in the CHAMP-derived data is this northern hemisphere peak, which reaches an amplitude of over 700 m/s, nearly three times the model prediction. These strong westward winds, blowing from the day to the night side across the prenoon sector, are common in the auroral region [23,24]. The smaller southern hemisphere peak shows a better consistency between the HWM07 model and the CHAMP-derived data than this northern hemisphere peak.

At low- and midlatitudes, the HWM07 model predictions for the three consecutive days overlap to a large extent. It is, therefore,

interesting to see that the CHAMP-derived zonal winds from the two days with a nominal orientation also show a large degree of consistency with each other, even though the maximum amplitudes are significantly higher than the model values. The wind derived from the sideways-flying period is inconsistent in comparison with those from the surrounding days, but it is more consistent in comparison with the model results, especially on the descending (evening) pass.

There are several reasons to believe that the wind data from the sideways-flying period are the most accurate. First, the compact satellite shape is less sensitive to errors in the aerodynamic and geometrical modeling than the elongated shape of the nominal configuration. Second, the larger frontal area when flying sideways results in a larger drag signal. This makes the wind derivation less susceptible to acceleration errors, due to issues with the calibration and solar radiation pressure modeling. The fact that the evening wind data seem less noisy than the equivalent data on the surrounding days supports this reasoning. Third, and perhaps a bit more tentatively, because the accelerometer axes for the along-track and cross-track axes are switched during the maneuver, the wind determination can benefit from the accurate GPS-derived calibration of the X_{SBF} axis during the surrounding days. This axis is in the crucial crosswind direction during the sideways-flying period.

The difference between the low-latitude crosswind data on the sideways-flying days and the surrounding days amounts to 50–150 m/s. If we assume that the sideways-flying crosswind data are accurate and that the day-to-day natural variability of the

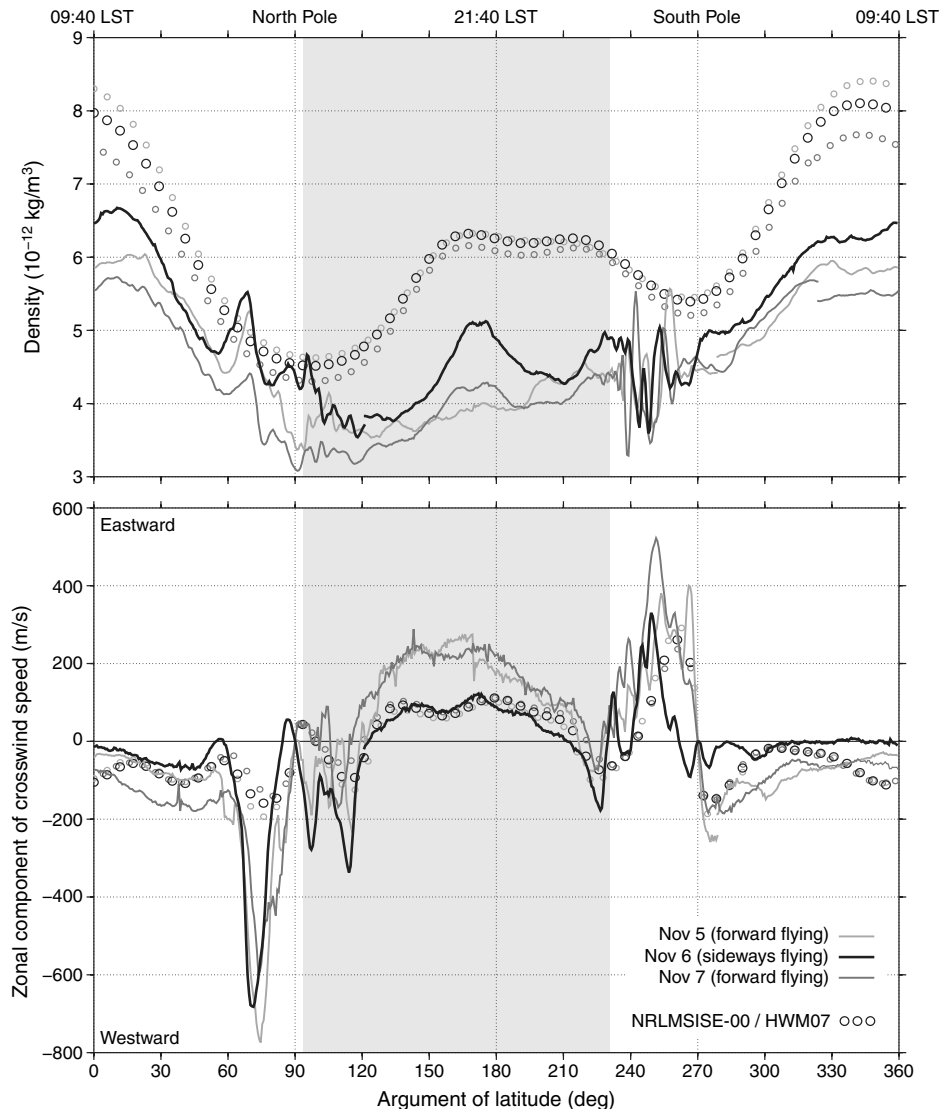


Fig. 7 Comparison of three orbits of CHAMP accelerometer-derived and modeled density and wind data from the 6 November 2002 sideways-flying period and the two surrounding days of nominal attitude.

low-latitude zonal wind is limited, this means that the wind errors in the nominal configuration are at this level as well. This conclusion is in line with the results of Table 2.

Data from the other sideways-flying period in October 2001 lead to similar conclusions. These data are not presented here, because the density and wind results are less clear than those for the 2002 event. This is mainly due to atypically large instrument calibration errors and the larger day-to-day density variability at that time.

Further studies into the instrument calibration and geometrical and aerodynamic modeling are required to reconcile the wind data from both attitude modes.

V. Recommendations for Future Missions

It should be noted once more that the current generation of accelerometer-carrying satellite missions (CHAMP, GRACE, GOCE, and Swarm) were not designed for thermosphere density and wind studies as part of their primary mission objectives. The experience gained in the study of the CHAMP data, in particular, and the development and analysis of the iterative algorithm presented in this paper have led to several recommendations for the development of possible future thermosphere missions with the aim to reduce density and wind errors.

First, a compact and simple design of the satellite external shape (without protruding antennae, camera baffles, booms, etc.) will reduce the uncertainty in geometrical and aerodynamic satellite modeling, which will result in a more reliable estimate of absolute density values. The availability of additional instruments on accelerometer missions, which could make contemporaneous in situ measurements of the atmospheric temperature, the molecular mass, the in-track wind, and other parameters important for gas-surface interaction, would increase the accuracy of the aerodynamic calculations required for the accelerometer processing, as discussed in Sec. II.C. At the same time, such instruments would provide valuable data for atmospheric and aerodynamic modeling in general, which could, in turn, aid in a more accurate reprocessing of historical accelerometer data sets.

A large area-to-mass ratio of the satellite will increase the acceleration signal, which is especially beneficial for wind derivation. Flying at high solar activity and low altitude will help in that respect as well, but that is, of course, limiting to a mission's sampling characteristics. A high eccentricity orbit might aid in the calibration and the separate fine tuning of radiation pressure and aerodynamic satellite models but, again, at the cost of the beneficial atmospheric sampling characteristics of circular orbits.

Finally, the example of CHAMP's sideways-flying data shows that a more versatile or more loosely defined attitude control of an irregularly shaped satellite will provide data that can be used to identify and possibly reduce density and crosswind errors. If the attitude control can be designed such that each of the three accelerometer axes can spend a sufficient amount of time (in turn) in the satellite flight direction, this could be beneficial for the instrument calibration using orbit tracking data and reduce the crosswind error in particular. The data processing of such a mission is possible when using the iterative algorithm presented here.

VI. Conclusions

In contrast to the previously published direct algorithms for deriving density and wind from accelerometer data, the iterative algorithm introduced in this paper can be applied in situations without a close alignment of the accelerometer axes with the along-track and cross-track directions. In fact, it can be used for arbitrary orientations of the accelerometer axes in space. An analysis using simulated CHAMP data shows that errors due to assumptions on the orientation are significantly reduced when the new algorithm is applied. However, this analysis also shows that errors in the instrument calibration and input models that are common in the use of both algorithm types lead to more significant density and wind errors than the errors in the algorithms. Users of the current CHAMP and GRACE data (and possibly GOCE and Swarm data in the future

as well) should be aware of the level and nature of the errors inherent in these data. The investigation of these algorithms and their related error sources has led to recommendations for improvements of possible future dedicated accelerometer-carrying space missions for studies of the thermosphere.

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