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# NEUTRON DIFFRACTION STUDIES OF HAFNIUM-HYDROGEN AND TITANIUM-HYDROGEN SYSTEMS 

by

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# 2 <br> NEUTRON DIFFRACTION STUDIES OF HAFNIUM-HYDROGEN AND TITANIUM-HYDROGEN SYSTEMS 

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#### Abstract

Results of neutron and X-ray diffraction studies on Hf and Ti hydrogen systems are reported. The first single phase hydride formed is a nonstoichiometric compound with a CaF $\mathrm{Ca}_{2}$-type structure. It deforms to a face-centered tetragonal structure as the composition approaches $\mathrm{MX}_{2}$. From the crystal structure data of these hydrides the positions of hydrogen atoms, the nearest neighbor atoms and their interatomic distances are determined. It is indicated that the size of the "hole" for the hydrogen atom in the hydride is such that it must enter as an ion. The effect of metal-hydrogen bonds on the physical properties of hydrides, such as characteristic temperature and vibration frequency, is given. Evidence and explanation for the embrittlement of metals by hydrogen are offered.


## INT RODUCTION

Studies of metal-hydrogen systems by thermal, metallographic and $X$-ray diffraction methods usually reveal the formation of metal-hydride phases, the dimensions of the unit cell and the positions of the metal atoms. The positions of hydrogen atoms in general, however, are determined either by high precision and relatively laborious methods or are just inferred. This difficulty or inability to locate the positions of hydrogen atoms with respect to one another and to the metal atoms prevents precise determination of crystal structures of the phases and, thereby, the type of bonding formed between metal and gas atoms. This has led to qualitative explanations and hypotheses 1 regarding the state of hydrogen in metals that are in some instances ambiguous and difficult to justify.

Neutron diffraction effects make it possible to locate metal and hydrogen atoms, at least in simple systems, with equal accuracy. This is due to the fact that the neutrons are scattered by the nuclei, except, of course, for the atoms possessing magnetic moments; and the nuclear coherent scattering amplitudes for both the light and the heavy atoms are of the same magnitude. Typical metal-hydrogen systems were studied. The objects were: (1) to determine the positions of hydrogen atoms, the nearest neighbor atoms

[^0]and the interatomic distances in each lattice, and (2) to obtain quantitative structure data which would form a basis for the explanation of the state of hydrogen, not only in these systems but other similar systems as well.

## EXPERIMENTAL PROCEDURE

In order to make use of the higher coherent scattering amplitude and lower spin diffuse scattering of deuterium as compared with those of hydrogen, the samples of hydrogen-containing polycrystalline materials were deuterated for the present studies. Rolled metal strip about 5 mils thick was cut into approximately $1 / 2^{\prime \prime} \times 1 / 2^{\prime \prime}$ pieces. Each piece was dipped in an acid solution of $40 \% \mathrm{HNO}_{3}, 5 \% \mathrm{Hf}$ and $55 \% \mathrm{H}_{2} \mathrm{O}$, and removed when it became bright, then rubbed with a brush while under running water, rinsed in acetone and air dried. The samples were weighed, and then heated and outgassed in a quartz tube evacuated to a pressure of $10^{-6} \mathrm{~mm} \mathrm{Hg}$ at about $1100^{\circ} \mathrm{C}$ for 16 to 48 hours. At $1000^{\circ} \mathrm{C}$ a measured volume of deuterium gas was introduced into the tube at a known pressure. Most of the absorption of gas took place at $700-800^{\circ} \mathrm{C}$. To assure a thoroughly reacted sample it was cycled several times between approximately 500 and $1000^{\circ} \mathrm{C}$, corresponding to deuterium pressures of 140 and 573 mm , respectively. Usually the sample was held for several hours at the lower temperature and finally cooled slowly to room temperature. The composition of the sample was calculated from the weight of the metal and the volume of $a b-$ sorbed deuterium. The metals used were of crystal bar purity.

In contrast to the ductile metals, the deuterides were brittle, the ductility decreasing with increasing concentration of deuterium. The deuterides with compositions $\mathrm{MD}_{1.7-1.97,} \mathrm{M}$ being the metal atom, were so brittle that they could be easily pulverized by crushing in mortar and pestle. All the samples studied in these investigations, however, were stable at room temperature and were handled without any special precautions.

The specimens were annealed at $350^{\circ} \mathrm{C}$ for 24 hours or longer. X-ray diffraction data were obtained for each phase for identification and for aid in structure determination. Neutron diffraction patterns were made from cylindrical samples consisting of about $10-15$ grams of powderedspecimen contained in a $7 / 16^{\prime \prime}$ diameter vanadium tube, $2^{\prime \prime}$ long and $5-\mathrm{mil}$ wall thickness, with cadmium end plugs. These patterns were very nearly comparable to those obtained with $X$-ray diffraction techniques both in intensity and resolution. This was made possible by the high intensity neutron beams available from the heavy water Argonne reactor, that were made monoenergetic by diffracting from a $2-1 / 2^{n} \times 5^{\prime \prime}$ and $1 / 2^{\prime \prime}$ thick copper single crystal cut parallel to the (111) plane, and by a neutron diffraction spectrometer which has a $2 \theta$ Bragg angle range from $-44^{\circ}$ to $+136^{\circ}$.

Automatic recording of neutron diffraction patterns were obtained. The spectrometer arm moved with constant angular speeds of $1-1 / 2,3,6$, 12 , or 24 degrees per hour, and the neutron diffraction pattern was recorded on a chart which traveled at compatible speeds for convenience of angular measurement. A fission chamber placed between the copper crystal and the sample was employed as a monitor of the incident beam, and a $\mathrm{BF}_{3}$ counter mounted on the spectrometer arm served as a detector of the diffracted neutrons. The monitor served as a timer, in that the pulses received from the detector during a preset number of monitor counts were stored in an eleatronic computer system. At the end of the preset monitor count, the monitor and the detector circuits were gated out for a two-second interval while the stored detector counts were first recorded and then cleared from the computer circuit. Therefore, each point recorded on the chart corresponded to the ratio of the diffracted intensity to the incident intensity over the indrement of angle which the spectrometer arm had moved during the counting period. In practice this angular increment of $2 \theta$ was about one tenth of a degree, insuring a sufficient number of counts for good statistics and still maintaining adequate resolution.

A provision was made for a systematic sampling of the background at the same time that a diffraction pattern was being obtained. A cadmium shutter was electronically inserted in the path of the incident beam every second, third, fourth, - - - , or tenth counting period. The cadmium shutter prevented the incident beam from striking the sample and the recorded value, therefore, was the background intensity.

## RESULTS

Hafnium-Hydrogen System: This system at room temperature consists of at least three phases, ${ }^{2}$ a deformed cubic or a tetragonal phase, a cubic phase, and another tetragonal phase. The deformed cubic phase coexists with $\alpha$-hafnium and extends up to $\mathrm{HfH}_{1.53}$. It converts into the facecentered cubic phase above $\mathrm{HfH}_{1} .53$. The single cubic phase exists within a narrow range of compositions and transforms into the tetragonal phase between $\mathrm{HfH}_{1.80}$ and $\mathrm{HfH}_{1.87}$. The tetragonal phase then extends up to $\mathrm{HfH}_{2.0}$. The range of compositions just before the system becomes a single
${ }^{2}$ Sidhu, S. S. and McGuire, J. C., J. Appl. Phys. 23, 1257 (1952)
cubic phase is quite sensitive to conditions under which the samples are prepared. Under certain conditions a transition phase ${ }^{3}$ is formed between the deformed cubic and the single cubic phases.

Crystal Structure of Cubic Phase - $\mathrm{HfD}_{1.628: ~} \mathrm{X}$-ray and neutron diffraction patterns of HfD ${ }_{1.628}$ are shown in Figure 1 and the diffraction data in Table 1. The value of the lattice parameter, $a_{0}$, is $4.681 \pm 0.005 \AA$ as determined from $X$-ray data. This value is slightly smaller than the value $4.708 \pm 0.002 \AA$ previously reported for the cubic hafnium hydride. The decrease is ascribed at least in part to the lattice contraction ${ }^{4}$ when hydrogen atoms are replaced by deuterium atoms in this system.

Since a face-centered cubic structure was suggested by X-ray diffraction data, the intensities were calculated by assuming both MX and $\mathrm{MX}_{2}$ type cubic structures. The structure factors, $|F|$, that gave the best agreement with the observed intensities were computed for the CaF $\mathrm{Ca}_{2}$-type struc ${ }^{-}$ ture with:

$$
4 \mathrm{Hf} \text { at: }(000 ; 1 / 21 / 20 ; 1 / 201 / 2 ; 01 / 21 / 2)
$$

and

$$
8 \mathrm{D} \text { at: } \pm(1 / 41 / 41 / 4 ; 3 / 43 / 41 / 4 ; 3 / 41 / 43 / 4 ; 1 / 43 / 43 / 4)
$$

where the normal deuterium atom sites are only partially filled by $1.628 / 2$ fraction of atoms. The calculated relative intensities were computed from the following equations:

$$
\begin{align*}
& \text { for } X \text {-rays, } \quad I \propto|F|^{2} m \cdot \frac{1+\cos ^{2} 2 \theta}{\sin ^{2} \theta \cos \theta}  \tag{1}\\
& \text { for neutrons, } \quad I \propto|F|^{2} m \cdot \frac{1}{\sin ^{2} \theta \cos \theta}\left(e^{-2 B \sin ^{2} \theta / \lambda^{2}}\right) \tag{2}
\end{align*}
$$

where,

$$
\begin{aligned}
& \qquad \begin{aligned}
|F|_{h k 1}= & \left\{1+e^{\pi i(h+k)}+e^{\pi i(h+1)}+e^{\pi i(k+1)}\right\} \\
& \left\{f_{H f}+1.628 f_{D} \cos \frac{\pi}{2}(h+k+1)\right\}
\end{aligned} \\
& \text { and } \exp \left(-2 B \frac{\sin ^{2} \theta}{\lambda^{2}}\right) \text { is the }{ }^{\text {s Debye-Waller }} \text { factor. }
\end{aligned}
$$

3 Ellinger, F. H., of Los Alamos Scientific Laboratory, communicated to us that in their studies of the hafnium-hydrogen system they observed a single cubic phase at about $\mathrm{HfH}_{1} .75$ which gradually deformed to an orthorhombic phase with a decrease in hydrogen content, reaching maximum deformation at about $\mathrm{HfH}_{1.5}$. At this composition a tetragonal phase appeared which coexists with the orthorhombic phase to about $\mathrm{HfH}_{1.25}$, and then with continued decrease in hydrogen content the orthorhombic and tetragonal phases coexist with $\alpha$-hafnium.
${ }^{4}$ Sidhu, S. S., J. Chem. Phys. 22, 1062 (1954).

Figure 1
ction Patterns of HfD 1.628 : (a) X-ray Filtered Cu K $\alpha$ Radiation;
Camera Diameter 114.6 mm . (b) Neutron, $\lambda=1.330 \AA$.

TABLE 1
Interplanar Spacings (d), Calculated and Observed X-ray and Neutron Diffraction Relative Intensities (I/I $I_{0}$ for $\mathrm{HfD}_{1.628}$

| hkl | d ( $\AA$ ) | X-rays |  | Neutrons |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | I/ $/ I_{0}$ (calc. $)$ | I/I $\mathrm{I}_{0}$ (obs.) | 1/ $\mathrm{I}_{0}$ (calc.) | I/I $\mathrm{I}_{0}$ (obs.) |
| 111 | 2.702 | 100.0 | vs | 38.3 | 33.2 |
| 200 | 2.334 | 48.9 | s | 0.7 | 2.5 |
| 220 | 1.652 | 34.5 | s- | 100.0 | 100.0 |
| 311 | 1.409 | 39.9 | s | 29.3 | 26.6 |
| 222 | 1.351 | 10.9 | w | 0.4 | 2.1 |
| 400 | 1.170 | 5.5 | vw | 23.9 | 20.3 |
| 331 | 1.073 | 17.9 | m | 16.3 | 15.7 |
| 420 | 1.047 | 17.1 | m | 0.6 | 1.6 |
| 422 | 0.956 | 16.0 | m- | 62.3 | 61.9 |
| 333,511 | 0.901 | 17.0 | m | 15.3 | 17.3 |
| 440 | 0.829 | 11.9 | w | 24.1 | 25.3 |
| 531 | 0.793 | 71.9 | $s$ | 18.6 | 17.9 |
| 442,600 | 0.781 | 13.4 | w+ | 0.5 | 1.5 |
| 620 | 0.744 |  |  | 43.7 | 40.4 |
| $\mathrm{v}=\mathrm{ver}$ | $s=$ strong |  | $\mathrm{m}=$ medium |  | = weak |
|  | $* \mathrm{f}_{\mathrm{Hf}}=0.88 \times 10^{-12} \mathrm{~cm} ; \mathrm{fD}=0.65 \times 10^{-12} \mathrm{~cm}$ |  |  |  |  |
|  |  | $\mathrm{R}=\frac{\Sigma \mid \mathrm{I}_{\mathrm{Ob}}}{\Sigma}$ | $\frac{-I_{\text {calc }}}{\text { bs }}=$ |  |  |

* The value used here for the hafnium scattering amplitude was calculated from diffraction patterns for both $\mathrm{HfD}_{1.628}$ and $\mathrm{HfD}_{1.983}$ containing many more peaks than used before, and is, therefore, more precise than the approximate value reported previously. 5

[^1]The value of $2 B$ was determined from the slope of the plot of logarithm of (I obs./ I calc.) vs. $\frac{\sin \theta}{\lambda}$. The value of $\bar{\mu}$, the root mean square displacement of the atom perpendicular to the reflecting planes, and of $\theta$, the characteristic temperature, were calculated by substituting $B$ in the expression

$$
\begin{align*}
B \frac{\sin ^{2} \theta}{\lambda^{2}} & =8 \pi \overline{\mu^{2}} \frac{\sin ^{2} \theta}{\lambda^{2}}  \tag{3}\\
& =\frac{6 h^{2} T}{M_{a} k \theta^{2}}\left\{\phi(x)+\frac{x}{4}\right\} \frac{\sin \theta}{\lambda^{2}}
\end{align*}
$$

in which $h$ is Planck-constant, $k$ Boltzmann's constant, $T$ is absolute temperature, $\underline{x}=\Theta / T$, and $M_{a}$ is the mass of the "crystal atom" or the weighted average mass (a) of two types of atoms expressed in atomic mass units.

The specific heat was calculated from the expression:

$$
\begin{equation*}
C_{V}=3 R(x)^{2} \frac{e^{x}}{\left(e^{x}-1\right)^{2}} \tag{4}
\end{equation*}
$$

and the vibration frequency from:

$$
\begin{equation*}
\psi_{\mathrm{m}}=\frac{\mathrm{k}}{\mathrm{~h}} \Theta \tag{5}
\end{equation*}
$$

R in equation (4) is the gas constant.
Crystal Structure of Tetragonal Phase $-\operatorname{HfD}_{1.983}$ : Positions of hafnium and hydrogen atoms in a body-centered tetragonal unit cell of this phase were determined from X-ray diffraction and low-angle portions of neutron diffraction patterns of the phase and were employed in explaining the effect on metal-metal bonds of increased concentration of hydrogen in
(a)

It is realized that to use an "average mass" in expression 3, the masses of different atoms, in general, should be nearly the same. However, the ( hk l ) reflections, for which $h, k$, and 1 are all odd, have contributions from only the Hf atoms, whereas, the reflections for which $h, k$ and 1 are all even have contributions from both the Hf and $D$ atoms. The values of $2 B$ determined from both sets of reflections agreed within experimental error, giving some justification to the use of an "average mass" for computation purposes and for at least qualitative interpretations.
its structure. 5 In the present study a complete crystal structure has been determined. To visualize its relation to face-centered cubic structure of $\mathrm{HfD}_{1.628}$ more readily, it is described by face-centered tetragonal unit cell and Miller Indices.

X -ray and neutron diffraction patterns are given in Figure 2 and the diffraction data in Table 2. The relative intensities were calculated by equations (1) and (2) and the structure factors by the expression:

$$
\begin{aligned}
|F|_{h k l}= & \left\{1+e^{\pi i(h+k)}+e^{\pi i(h+1)}+e^{\pi i(k+1)}\right\} \\
& \left\{f_{\mathrm{Hf}}+1.983 f_{\mathrm{D}} \cos \frac{\pi}{2}(\mathrm{~h}+\mathrm{k}+1)\right\}
\end{aligned}
$$

The structure constants for $\mathrm{HfD}_{1.628}$ and $\mathrm{HfD}_{1.983}$, including lattice parameters, interatomic distances, volume of unit cell and calculated density are tabulated in Table 3. The constants of hafnium are included for comparison.

Titanium-Hydrogen System: X-ray diffraction studies of titaniumhydrogen system have shown that at room temperature the system consists of at least three regions of concentration of hydrogen, $\alpha$-titanium, followed by a transformation region, in which $\alpha$-titanium transforms to a facecentered cubic hydride as additional hydrogen is added to the system, and a single face-centered cubic phase. The composition range of the single homogeneous cubic phase is approximately $60-66$ atomic per cent hydrogen or deuterium ( $\mathrm{TiD}_{1.50=1.94}$ ). With increasing concentration of gas in this phase, however, there is a definite broadening of diffraction lines originoting from (200), (220), (311), (400), etc. planes, while (111) and (222) reflections remain sharp. Hence, as the composition approaches $\mathrm{TiD}_{2}$, the cubic unit cell deforms to a face-centered tetragonal cell.

Crystal Structure of TiP $\mathrm{T}_{1.971}: X-\mathrm{ray}$ and neutron diffraction patterns of titanium dideuteride are given in Figure 3 and the diffraction data in Table 4. The structure of this phase is face-centered cubic, again of the CaFe $2_{2}$-type, which confirms the structure reported by Fag ${ }^{6}$ for $\beta$-phase of Ti-H system. Relative intensities and structure factors were calculated similarly as for $H f D_{1.628}$. The structure constants for $T i$ and $T i D_{1.971}$ are given in Table 5.

## DISCUSSION

The structure of the cubic phase of hafnium-deuterium system (Figure 4) as derived from neutron and X-ray diffraction data is of the $\mathrm{CaF}{ }_{2}$ type. The shortest metal-metal atom distance is $a_{0} / \sqrt{2}$ or

[^2]
Diffraction Patterns of $\mathrm{HfD}_{1.983}$ : (a) X-ray Filtered $\mathrm{Cu} \mathrm{K} \alpha$ Radiation: Camera Diameter 114.6 mm . (b) Neutron, $\lambda=1.330 \AA$.

TABLE 2
Interplanar Spacings (d), Calculated and Observed X-ray and Neutron Diffraction Relative Intensities
(I/I $I_{0}$ for $H_{f(1.983}$

| $\begin{gathered} \mathrm{hkl} \\ \left(\mathrm{~F}, \mathrm{C} . \mathrm{T}_{\mathrm{o}}\right) \end{gathered}$ | d (A) | X-rays |  | Neutrons |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $1 / I_{0}$ (calc.) | I/ $\mathrm{I}_{0}$ (obs.) | $\mathrm{I} / \mathrm{I}_{0}$ (calc.) | I/ $\mathrm{I}_{0}$ (obs.) |
| 111 | 2.70 | 100.0 | vs | 39.3 | 39.3 |
| 200 | 2.45 | 37.4 | $s$ | 3.6 | 3.7 |
| 002 | 2.173 | 13.1 | m | 1.5 | -- |
| 220 | 1.728 | 12.8 | m | 61.7 | 63.0 |
| 202 | 1.624 | 20.7 | $\mathrm{m}+$ | 100.0 | 100.0 |
| 311 | 1.457 | 29.3 | s | 23.4 | 24.4 |
| 222 | 1.354 | 11.8 | m | $2.1\}$ | 14.8 |
| 113 | 1.336 | 11.5 | m | $9.9\}$ | 14.8 |
| 400 | 1.221 | 4.7 | w | 25.0 | 24.4 |
| 331 | 1.114 | 8.7 | m- | 6.77 |  |
| 420 | 1.093 | 8.7 | m- | $1.5\}$ | 14.8 |
| 004 | 1.086 | 2.2 | vw | 10.0 |  |
| 402 | 1.065 | 8.9 | w ${ }^{+}$ | 1.43 | 14.1 |
| 313 | 1.058 | 18.3 | m+ | $12.5\}$ | 14.1 |
| 204 | 0.993 | 10.7 | m | 1.3) | 68.9 |
| 422 | 0.978 | 22.8 | $m+$ | $66.2\}$ | 68.9 |
| 511 | 0.937 | 15.6 | m | 10.27 |  |
| 224 | 0.921 | 20.0 | m + | $30.1\}$ | 58.2 |
| 333 | 0.903 | 35.6 | $s$ | 4.8 |  |
| 440 | 0.863 |  |  | $14.0\}$ | 15.1 |
| 115 | 0.853 |  |  | $4.5\}$ | 15.1 |
| 531 | 0.822 |  |  | $8.6\}$ | 370 |
| 404 | 0.817 |  |  | 25.9 $\}$ | 37.0 |
| 424 | 0.766 |  |  | 50.5 | 58.7 |
| $\mathrm{v}=\mathrm{very}$ |  | $\mathrm{s}=$ strong $\quad \mathrm{m}=\mathrm{m}$ |  | dium | $\mathrm{w}=\mathrm{weak}$ |
|  |  | $=\frac{\Sigma \mu_{\text {obs }}}{\Sigma}$ | calc. $=$ |  |  |

TABLE 3
Structure Constants of $\mathrm{Hf}, \mathrm{HfD}_{1.628}$, and $\mathrm{HfD}_{1,983}$

| Composition | Structure | Lattice Parameters | Interatomic Distances ( $\AA$ ) | Volume of Unit Cell $\left(10^{-24} \mathrm{~cm}^{3}\right)$ | Calculated Density $\left(\mathrm{g} \mathrm{cm}^{-3}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Hf | Hexagonal | $\begin{aligned} a_{0} & =3.198 \pm 0.003 \AA \\ c_{0} & =5.055 \pm 0.003 \AA \\ c_{0} / a_{0} & =1.581 \end{aligned}$ | About Hf: <br> 6 Hf at $3.131 \pm 0.003$ <br> 6 Hf at $3.198 \pm 0.003$ <br> 6 Hf at $4.475 \pm 0.003$ | 44.77 | 13.25 |
| $\mathrm{HfD}_{1,528}$ | Face-centered Cubic | $a_{0}=4.680 \pm 0.003 \AA$ | About Hf: <br> 8 D at $2.026 \pm 0.003$ <br> 12 Hf at $3.309 \pm 0.003$ <br> 24 D at $3.880 \pm 0.003$ <br> About D: <br> 4 Hf at $2.026 \pm 0.003$ <br> 6 D at $2.340 \pm 0.003$ <br> 12 D at $3.309 \pm 0.003$ <br> 12 Hf at $3.880 \pm 0.003$ <br> 8 D at $4.053 \pm 0.003$ | 102.50 | 11.78 |
| $\mathrm{HfD}_{1.983}$ | Face-centered Tetragonal | $\begin{aligned} a_{0} & =4.887 \pm 0.003 \AA \\ c_{0} & =4.345 \pm 0.003 \AA \\ c_{0} / a_{0} & =0.889 \end{aligned}$ | About Hf: <br> 8 D at $2.041 \pm 0.003$ <br> 8 Hf at $3.270 \pm 0.003$ <br> 4 Hf at $3.456 \pm 0.003$ <br> 8 D at $3.688 \pm 0.003$ <br> 16 D at $4.013 \pm 0.003$ <br> About D: <br> 4 Hf at $2.041 \pm 0.003$ <br> 2 D at $2.173 \pm 0.003$ <br> 4 D at $2.444 \pm 0.003$ <br> 8 D at $3.270 \pm 0.003$ <br> 4 D at $3.456 \pm 0.003$ <br> 4 Hf at $3.688 \pm 0.003$ <br> 8 Hf at $4.013 \pm 0.003$ | 103.77 | 11.69 |



Figure 3
Diffraction Patterns of $\mathrm{TiD}_{1.971}:(\mathrm{a}) \mathrm{X}-\mathrm{ray}$ Filtered Co $\mathrm{K} \alpha$ Radiation:
Camera Diameter 114.6 mm . (b) Neutron, $\lambda=1.337 \AA$.

TABLE 4

Interplanar Spacings (d), Calculated and Observed X-ray and Neutron Diffraction Relative Intensities (I/I $I_{0}$ for TiD ${ }_{1.971}$

| hkl | d (A) | X -rays |  | Neutrons |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | I/Io (calc.) | $\mathrm{I} / \mathrm{I}_{0}$ (obs.) | I/I $I_{0}$ (calc.) | I/ $\mathrm{I}_{0}$ (obs.) |
| 111 | 2.563 | 100.0 | vs | 9.5 | 9.2 |
| 200 | 2.221 | 43.0 | s | 100.0 | 100.0 |
| 220 | 1.569 | 29.1 | m+ | 27.9 | 24.0 |
| 311 | 1.339 | 29.3 | m+ | 6.9 | 6.3 |
| 222 | 1.281 | 7.9 | w | 39.6 | 40.0 |
| 400 | 1.112 | 4.0 | vw | 6.3 | 4.0 |
| 331 | 1.019 | 13.0 | m | 3.6 | 80 |
| 420 | 0.993 | 12.3 | m | 65.3 ) |  |
| 422 | 0.906 | 13.5 | m | 15.6 | 12.8 |
| 333,511 | 0.854 | 21.1 | m+ | 3.2 | 1.4 |
| 442,600 |  |  |  | 49.0 | 40.0 |
| $\mathrm{v}=\mathrm{very}$ |  | $s=$ strong $\quad m=m$ |  | um | $\mathrm{w}=\mathrm{weak}$ |
| ${ }^{\mathrm{f}_{\mathrm{Ti}}=-0.38 \times 10^{-12} \mathrm{~cm}} \mathrm{f}_{\mathrm{D}}=0.65 \times 10^{-12} \mathrm{~cm}$ |  |  |  |  |  |
| $R=\frac{\sum\left\|I_{\text {obs. }}-I_{\text {calc. }}\right\|}{\sum I_{\text {obs }}}=0,098$ |  |  |  |  |  |

TABLE 5
Structure Constants of Ti and $\mathrm{TiD}_{1.971}$

| Composition | Structure | Lattice Parameters | Interatomic Distances ( $\AA$ ) | Volume of Unit Cell $\left(10^{-24} \mathrm{~cm}^{3}\right)$ | Calculated Density $\left(\mathrm{g} \mathrm{cm}^{-3}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Ti | Hexagonal | $\begin{aligned} a_{0} & =2.952 \pm 0.002 \AA \\ c_{0} & =4.689 \pm 0.002 \AA \\ c_{0} / a_{0} & =1.588 \end{aligned}$ | ```About Ti: 6 Ti at 2.899\pm0.002 6 Ti at 2.952\pm0.002 6 Ti at 4.137\pm0.002``` | 35.39 | 4.50 |
| TiD $\mathrm{D}_{1.971}$ | Face-centered Cubic | $a_{0}=4.440 \pm 0.003 \AA$ | ```About Ti: 8D at 1.923 \pm0.003 12 Ti at 3.140 \pm0.003 24D at 3.681\pm0.003 About D: 4 \mathrm { Ti } \text { at 1.923 士0.003} 6 \mathrm { D } \text { at 2.220 土0.003} 12D at 3.140 \pm0.003 12 Ti at 3.681 \pm0.003 8D at 3.845\pm0.003``` | 87.53 | 3.94 |



Figure 4
Face-centered Cubic Unit Cell of $\mathrm{HfD}_{1.628}$ Structure.
$3.309 \pm 0.003 \AA$, and, as shown in Table 3, this distance is larger by 3.5 to 5.7 per cent than the interatomic distances in the pure metal. The nearest neighbors of each metal, however, are the deuterium atoms that are at a distance of $a_{0} \cdot \frac{\sqrt{3}}{4}$ or $2.026 \pm 0.003 \AA$. If all normal sites for deuterium atoms were occupied each metal atom would be surrounded by eight deuterium atoms. Since the transformation of the cubic phase to the tetragonal phase of this system takes place in the region of $64-65$ atomic per cent deuterium, ( $\mathrm{HfD}_{1.78-1.86}$ ) it is apparent that the normal deuterium sites in the cubic phase are never filled. The structure, therefore, is typically a defect structure.

In the composition range of the cubic phase, 62-64.5 atomic per cent deuterium ( $\mathrm{HfD}_{1.63-1,81}$ ), the lattice parameter $a_{0}$ appears to remain constant. At the transformation point, however, there is a first-order change. The fluorite structure of the cubic phase transforms to a facecentered tetragonal structure with compression along one axis and expansion along the other two. This provides for shorter metal-metal atom bonds. As shown in Table 3, the distance of nearest approach of metalmetal atoms decreases from $3.309 \pm 0.003 \AA$ in the cubic phase to $3.270 \pm 0.003 \AA$ in the tetragonal phase. The strengthening of atomic bonds in the tetragonal structure on the whole is evidenced from the changes produce in some of the physical properties of the two structures as given in Table 6. For example, both the Debye characteristic temperature and the vibrational frequency of atoms in the tetragonal structure are higher than those in the cubic structure.

TABLE 6
Some Physical Constants of Hafnium and Titanium Deuterides

| Composition | $\frac{2 \mathrm{~B}}{(\AA)^{2}}$ | $\frac{\bar{\mu}}{(\AA)}$ | $\frac{\mathrm{M}_{\mathrm{a}}}{(\mathrm{amu})}$ | $\frac{\Theta}{\left({ }^{\circ} \mathrm{K}\right)}$ | $\left(\mathrm{cal} / \mathrm{C} \mathrm{C}_{\mathrm{V}}\right.$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left.{ }^{\circ} \mathrm{C}\right)$ | $\left(\right.$ vibrations $\left./ \mathrm{sec}_{0}\right)$ |  |  |  |  |  |
| $\mathrm{HfD}_{1.628}$ | 1.68 | 0.103 | 69.21 | 244 | 5.64 | $5.08 \times 10^{12}$ |
| $\mathrm{HfD}_{1.983}$ | 1.06 | 0.082 | 61.21 | 329 | 5.40 | $6.86 \times 10^{12}$ |

As additional deuterium is absorbed by the sample in the tetragonal phase and the composition approaches $\mathrm{HfD}_{2}$, there is a further distortion of the tetragonal unit cell, causing a decrease in $c_{0}$ and an increase in $a_{0}$. This has been ascribed to formation of additional hafnium-deuterium bonds 5 that
strengthen the short bonds, $\frac{\sqrt{a_{0}^{2}+c_{0}^{2}}}{2}$, along the [101] direction and weaken the metal-metal bonds in the (001) plane. The volume of the unit cell of the distorted fluorite structure is larger than that of the cubic cell. The number of atom sites per each cell, however, is the same.

X-ray diffraction studies of the zirconium hydrogen system have shown that the phases formed in this system are analogous to those in the hafnium-hydrogen system. The crystal structure of $Z r D_{2}$ determined by $X-r a y$ and neutron diffraction techniques 7 is similar to that of $H_{f} \mathrm{D}_{1.983}$. The crystal structures of other corresponding hydrides in the two systems are also similar. 8 It may be inferred, therefore, that the conclusions drawn from the study of the hafnium-hydrogen system apply equally to the zirconium hydrogen system.

The titanium hydrides and deuterides, 9 prepared under identical conditions as for those of hafnium and zirconium, show that the face-centered cubic phase in this system extends over a wider range of compositions, and does not seem to transform to the tetragonal phase as readily as in the other two systems. 10 Some of the physical properties of $\mathrm{TiD}_{1.971}$, analogous to those of $H f D_{1.628}$, are as follows: the root mean square displacement, $\bar{\mu}=0.120 \AA_{\text {; }}$ the mass of the "crystal atom" $\mathrm{Ma}_{\mathrm{a}}=17.46$ amu; the characteristic temperature, $\Theta=428^{\circ} \mathrm{K}$, and the vibrational frequency, $\nu_{m}=8.92 \times 10^{12}$ vibrations per second. If high characteristic temperature and vibration frequency are taken as an indication of a strongly bound substance, it would appear that the $\mathrm{TiD}_{1.971}$ cubic structure is more strongly bound than that of $H_{f} \mathrm{D}_{1.628}$, as the values of these physical properties are greater than can be accounted for by mass differences alone. This may account for the lack of ready transformation to the tetragonal structure.
${ }^{7}$ Rundle, R.E., Shull, C. G. and Wollan, E.O. " ${ }^{\text {THe Crystal Structure }}$ of Thorium and Zirconium Dihydrides by X-ray and Neutron Diffraction," Acta. Cryst., 5, 22 (1952).
${ }^{8}$ Sidhu, S. S., Trans. Am. Soc. Metals, 46, 652 (April 1954).
${ }^{9}$ The titanium hydrides and deuterides were prepared with due knowledge of the difficulties that previous investigators had experienced: cf. Gibb, Jr., T. R. P. and Kruschwitz, Jr., H. W., "The Titanium-Hydrogen System and Titanium Hydride," J. Am. Chem. Soc., 72, 5365 (1950). For the study made here, well reacted homogeneous samples were prepared from pure metal and purified gas.

10It is reported that this deformation is much more pronounced below room temperature. (Private communication, C. G. Shull, Brookhaven National Laboratory.)

## SUMMARY AND CONCLUSIONS

Studies of typical metal-hydrogen systems have been made by combined methods of neutron and $X$-ray diffraction. An increasedintensity of neutron flux from the heavy water reactor, a wide range $2 \theta$ Bragg angle covered by the present Argonne Neutron Diffraction Spectrometer and an automatic recording of neutron diffraction patterns made it possible to obtain quantitative data that lent to comprehensive interpretations. By reducing the size of the incident beam and consequently the amount of the specimen used, the resolution of the neutron diffraction peaks was improved. The exposuretime to obtain a complete neutron pattern was comparable to that for the $X$-ray diffraction pattern. Although the neutron diffraction patterns presented here were obtained with wave length, $\lambda=1.315 \AA$, it could be reduced to $1 \AA$ and thus many additional diffraction peaks observed. The main features of the techniques employed, the results obtained, and the interpretations made may be summarized as follows:

1. It was found necessary to use only pure metals and purified gas. The metal had to be rolled into thin sheets to obtain well reacted homogeneous samples. In the thick metal samples a gradient of gas concentration was observed, the greatest concentration being at the surface. The same sample contained hydrides and unreacted metal. Long annealing and degassing of thin metal strips at approximately $1100^{\circ} \mathrm{C}$ in no way affected the absorption of hydrogen by the metal. The concept that in order to establish an entirely normal solubility equilibrium with hydrogen, a metal must be strained rather than thoroughly annealed seems to be untenable in this case.
2. Vanadium has a coherent scattering amplitude, 11
$f=-0.053 \times 10^{-12} \mathrm{~cm}$, and essentially gives no diffraction peaks. The polycrystalline samples studied here with neutron diffraction, therefore, were contained in thin vanadium tube holders machined from solid metal rods. As an improvement over vanadium specimen holders, however, an alloy containing 62 atomic per cent titanium and 38 atomic per cent zirconium was developed; the scattering lengths of the two metals being such that the resultant coherent scattering amplitude is practically zero.
3. In the solid state conversion of the metal to the hydride, the bonds formed between hydrogen and metal atoms readily displace the metal atoms from their normal positions in the lattice without impairment of the metal structure, the metal-hydrogen bonds being stronger than metal-metal atom bonds. In the transformation

[^3]of a metal into a hydride or of one metal hydride into another, both kinds of phase transitions are observed. The first kind or the first order, in which energy, volume, and crystal structure change discontinuously, is evidenced by the abrupt change that takes place when face-centered cubic structure in hafnium and zirconium hydrogen systems transforms to face-centered tem tragonal structure; the second kind or the continuous transitions, in which energy and volume change continuously, is the change observed when deformed cubic structure in hafniumhydrogen system deforms to a single face-centered cubic phase, 2 and face-centered cubic phase of titanium-hydrogen system deforms to face-centered tetragonal structure.
4. In the formation of these hydrides the hexagonal structure of metals is completely changed, first to a cubic and then to a tetragonal structure with unit cells of different dimensions, volumes, densities, and containing larger number of atoms in them. In every respect these structures are of new compounds. However, as in the case of the cubic phase, all atom sites in the unit cell are seldom filled, and as a result the compounds formed are nonstoichiometric. Even the tetragonal phases in the hafnium and the zirconium hydrogen systems are formed below the stoichiometric ratios of $\mathrm{HfH}_{2}$ and $\mathrm{ZrH}_{2}$, and they approach these compositions only when additional hydrogen is added to the systems. The range of variable compositions is considerable.
5. As given in Tables 3 and 5 hydrogen or deuterium atoms occupy definite positions in the lattice with respect to one another and to the metal atoms. The nearest neighbors of each atom, metal or gas, are the unlike atoms. The distances between metal-metal atoms in the hydrides are longer than those in the pure metals, and those between hydrogen-hydrogen or deuterium-deuterium atoms are longer than nuclear distances 12 of diatomic molecules of H.H or $D \cdot D(d=0.75 \AA)$. For the size of site available to a gas atom to occupy in these hydrides, an indication of a smaller size hydrogen (loss of electron) is evident. It must enter, apparently, as an ion rather than an atom. 13

[^4]${ }^{13}$ Isenberg, Irvin, "The Ionization of Hydrogen in Metals;" Phys. Rev., 79, 736 (1950).

## 21

6. Another striking characteristic of these hydrides is that the first pure hydride phase formed in the three systems favors $\mathrm{CaF}_{2}$-type structure with a fraction of the atom sites unfilled. The metal-hydrogen bonds in this structure are anisotropic, and their directional nature becomes pronounced when the face-centered cubic structure transforms to the face-centered tetragonal structure with contraction along one axis and expansion along the other two. The brittleness observed in these hydrides may be ascribed to these directional bonds rather than to the mechanical defects such as the presence of pores, microcracks, fissures, intergranular holes, etc., so often mentioned in the literature. 9,14 it seems that the causes of embrittlement of metals by gases in general lie in the type of bonds formed ${ }^{15}$ in a given metal-gas system rather than in its macroscopic appearance.

## ACKNOWLEDGMENT

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[^5]
## APPENDIX

## Calculation of Root Mean Square Displacement $\bar{\mu}_{;}$Characteristic

Temperature $\theta$; Specific Heat $C_{V}$; and Frequency of
Vibration $\nu_{m}$ of $\mathrm{HfD}_{1.628,} \mathrm{HfD}_{1.983}$ and TiD $\mathrm{T}_{1.971}$

1. The relative intensities of neutron diffraction peaks in the diffraction patterns of $H \mathrm{HD}_{1.628}, \mathrm{HfD}_{1.983}$ and $\mathrm{TiD}_{1.971}$ were calculated from the expression:

$$
\begin{equation*}
I \propto|F|_{h k l} m \frac{1}{\sin ^{2} \theta \cos \theta}\left(e^{-2 B \sin ^{2} \theta / \lambda^{2}}\right) \tag{1}
\end{equation*}
$$

in which

$$
\begin{aligned}
|F|_{h k 1}= & \left\{I+e^{\pi i(h+k)}+e^{\pi i(h+1)}+e^{\pi i(k+1)}\right\} \\
& \left\{f_{H f}+\operatorname{CfD}_{\mathrm{D}} \cos \frac{\pi}{2}(h+k+1)\right\}
\end{aligned}
$$

and

$$
\begin{align*}
\frac{B \sin ^{2} \theta}{\lambda^{2}} & =8 \pi^{2} \bar{\mu}^{2} \frac{\sin ^{2} \theta}{\lambda^{2}}  \tag{2}\\
& =\frac{6 h^{2} T}{M_{a} k \theta^{2}}\left\{\phi(x)+\frac{x}{4}\right\} \sin ^{2} \theta / \lambda^{2}
\end{align*}
$$

where $|F|_{\text {hk }}$ is the structure factor, $m$ the multiplicity factor and $\lambda$ the neutron wavelength: $e^{-2 B} \frac{\sin ^{2} \theta}{\lambda^{2}}$ is the Debye-Waller factor; $C$ is mole fraction of deuterium in a given deuteride: $\bar{\mu}$ is the root mean square displacement of the atoms perpendicular to the reflecting planes; $h$ is Planck's constant, $k$ is Boltzmann's constant: $T$ is absolute temperature; $\Theta$ is the Debye "characteristic temperature," $x=\frac{\theta}{T}$, and $M_{a}$ is the mass of the "crystal atoms," or the average mass of two types of atoms expressed in atomic mass units.

The value of $B$ for each deuteride was determined from the slope of the plot of $\log \left(I_{\text {obs }} / I_{\text {calc. }}\right)$ against $\sin \theta / \lambda$. The values of $\bar{\mu}_{\mathrm{c}}$ as given in Table 7, were calculated by substituting the experimentally determined values of $B$ in the expression $\bar{\mu}^{2}=B / 8 \pi^{2}$.

## TABLE 7

Values of $B, \bar{\mu}^{2}$ and $\bar{\mu}$ for Various Phases

| Phase | $2 B$ <br> $(\AA)^{2}$ | $\bar{\mu}^{2}$ <br> $(\AA)^{2}$ | $\bar{\mu}$ <br> $(\AA)$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{HfD}_{1.628}$ | 1.68 | 0.01064 | 0.103 |
| $\mathrm{HfD}_{1.983}$ | 1.06 | 0.00671 | 0.082 |
| $\mathrm{TiD}_{1.971}$ | 2.26 | 0.01431 | 0.120 |

2. To calculate $\Theta$ expression (2) was simplified by substituting the following constants:

$$
\begin{aligned}
& 6 h^{2}= 6\left(6.6252 \times 10^{-27} \mathrm{erg-sec}\right)^{2}=263.359650 \times 10^{-54}(\mathrm{erg}-\mathrm{sec})^{2} \\
& k= 1.38042 \times 10^{-16} \mathrm{erg}-\mathrm{deg}^{-1} \cdot \\
& \text { Mass of "crystal atom" }=\frac{\mathrm{M}_{\mathrm{a}}}{6.0254 \times 10^{23}} \text { atomic mass units. } \\
&\left(\lambda_{\AA}\right)^{2}=\left(\lambda \times 10^{-16} \mathrm{~cm}\right)^{2}
\end{aligned}
$$

and

$$
\begin{aligned}
& \frac{6 \mathrm{~h}^{2} \mathrm{~T}}{\mathrm{M}_{\mathrm{a}} \mathrm{e} \Theta^{2}}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\} \frac{\sin ^{2} \theta}{\lambda^{2}} \\
& =\frac{263.359650 \times 10^{-54}(\mathrm{erg}-\mathrm{sec})^{2} \times 6.0254 \times 10^{23} \mathrm{~T}}{1.38042 \times 10^{-16} \mathrm{erg}-\operatorname{deg}^{-1} \times \mathrm{M}_{\mathrm{a}} \theta^{2}}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\} \frac{\sin ^{2} \theta}{\lambda^{2} \times 10^{-16} \mathrm{~cm}^{2}} \\
& =\frac{1.14955 \times 10^{4} \mathrm{~T}}{\mathrm{M}_{\mathrm{a}} \theta^{2}}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\} \frac{\sin ^{2} \theta}{\lambda^{2}}
\end{aligned}
$$

Therefore, from equation (2),

$$
8 \pi^{2} \bar{\mu}^{2}=\frac{1.14955 \times 10^{4} \mathrm{~T}}{\mathrm{Ma}_{\mathrm{a}} \Theta^{2}}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}
$$

or

$$
\begin{equation*}
\Theta^{2}=\frac{1.14955 \times 10^{4} \mathrm{~T}}{8 \pi^{2} \bar{\mu}^{2} \mathrm{M}_{\mathrm{a}}}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\} \tag{3}
\end{equation*}
$$

The average mass of the "crystal atom" was calculated as follows: for example,

$$
\begin{aligned}
\mathrm{M}_{\mathrm{a}} \text { for } \mathrm{HfD}_{1.628} & =\frac{\mathrm{m}_{\mathrm{Hf}}+1.628 \mathrm{~m}_{\mathrm{D}}}{2.628} \\
& =\frac{178.6+1.628 \times 2.015}{2.628} \\
& =69.21
\end{aligned}
$$

where $m_{H f}$ and $m_{D}$ are atomic weights of hafnium and deuterium atoms respectively. The value of $\mathrm{M}_{\mathrm{a}}$ for each phase is tabulated below:

| Phase | $\mathrm{Ma}_{\text {a }}$ |
| :---: | :---: |
| HfD ${ }_{1.628}$ | 69.21 |
| $\mathrm{HfD}_{1.983}$ | 61.21 |
| TiD ${ }_{1.971}$ | 17.46 |

Substituting the values of $\bar{\mu}^{2}$ from Table $7, \mathrm{M}_{\mathrm{a}}$ from above and of $T$ as $295^{\circ} \mathrm{K}$ in equation (3), expressions for $\Theta^{2}$ and $\Theta$ for each phase were obtained as follows:

| Phase | $\Theta^{2}$ | ${ }^{(1)}$ |
| :---: | :---: | :---: |
| $\mathrm{HfD}_{1.628}$ | $5.8323 \times 10^{4}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}$ | $241.50\left\{\phi(x)+\frac{x}{4}\right\}^{\frac{1}{2}}$ |
| $\mathrm{HfD}_{1.983}$ | $10.4575 \times 10^{4}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}$ | $323.38\left\{\phi(x)+\frac{x}{4}\right\}^{\frac{1}{2}}$ |
| TiD ${ }_{1.971}$ | $17.3461 \times 10^{4}\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}$ | $416.49\left\{\phi(x)+\frac{x}{4}\right\}^{\frac{1}{2}}$ |

The value of factor $\left\{\phi(x)+\frac{x}{4}\right\}^{\frac{1}{2}}$ is approximately 1. Therefore, an approximate value of $x$ may be taken as $\Theta / T$, or
for

$$
\begin{aligned}
\mathrm{HfD}_{1.628}, \mathrm{x} & =241.5 / 295 \\
& =0.8186 \\
\mathrm{HfD}_{1.983}, x & =1.0963 \\
\operatorname{TiD}_{1.971}, x & =1.4119
\end{aligned}
$$

Using values of $x$ thus obtained, the factor $\left\{\phi(x)+\frac{x}{4}\right\}$ was evaluated from the curve $\left\{\phi(x)+\frac{x}{4}\right\}$ vs. $x$ as given in Figure 5. Substituting these values above, $\Theta$ for each phase was calculated as given in Table 8.

## TABLE 8

Values of $\mathrm{x},\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}^{\frac{1}{2}}$ and $\Theta$

| Phase | x | $\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}$ | $\left\{\phi(\mathrm{x})+\frac{\mathrm{x}}{4}\right\}^{\frac{1}{2}}$ | $\Theta$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{HfD}_{1.628}$ | 0.8186 | 1.0190 | 1.0095 | $244^{\circ} \mathrm{K}$ |
| $\mathrm{HfD}_{1.983}$ | 1.0963 | 1.0335 | 1.0166 | $329^{\circ} \mathrm{K}$ |
| $\mathrm{TiD}_{1.971}$ | 1.4119 | 1.0545 | 1.0269 | $428^{\circ} \mathrm{K}$ |

3. The specific heat $C_{V}$ was calculated from the expression

$$
\begin{equation*}
C_{v}=3 R(x)^{2} \frac{e^{x}}{\left(e^{x}-1\right)^{2}} \tag{4}
\end{equation*}
$$

where

$$
\begin{aligned}
\mathrm{R} & =8.31662 \times 10^{7} \mathrm{erg} / \mathrm{mole}{ }^{\circ} \mathrm{C} \\
& =1.98677 \mathrm{cal} / \mathrm{mole}{ }^{\circ} \mathrm{C}
\end{aligned}
$$

By substituting the value of $X=\frac{\Theta}{T}$ in equation (4) and multiplying by $3 R$, one obtains:

| Phase |  |  |  |  | $C_{v}=3 R(x)^{2} \frac{e^{x}}{\left(e^{x}-1\right)^{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | X | $(\mathrm{X})^{2}$ | $e^{x}$ | $e^{x /\left(e^{x}-1\right)^{2}}$ | cal/mole ${ }^{\circ} \mathrm{C}$ |
| $\mathrm{HfD}_{1.628}$ | 0.8186 | 0.6701 | 2.2673 | 1.4117 | 5.638 |
| $\mathrm{HfD}_{1.983}$ | 1.0963 | 1.2019 | 2.9931 | 0.7535 | 5.398 |
| TiD 1.971 | 1.4119 | 1.9935 | 4.1037 | 0.4260 | 5.062 |


4. The frequency of vibration was calculated from the expression:

$$
\nu_{\mathrm{m}}=\frac{\mathbf{k}}{\mathrm{h}} \Theta
$$

where

$$
\begin{aligned}
\frac{\mathrm{k}}{\mathrm{~h}} & =\frac{1.38042 \times 10^{-16} \mathrm{erg} /{ }^{\circ} \mathrm{K}}{6.6252 \times 10^{-27} \mathrm{erg-sec}} \\
& =\frac{2.08359 \times 10^{10}}{{ }^{\circ} \mathrm{K}-\mathrm{sec}}
\end{aligned}
$$

Multiplying the above expression by values of $\Theta$ as given in the last column of Table 8, one gets:

| Phase | $\nu_{\mathrm{m}}$ |
| :--- | :---: |
| $\mathrm{HfD}_{1.628}$ vibrations per sec. |  |
| $\frac{5.084 \times 10^{12}}{}$ | $6.855 \times 10^{12}$ |
| $\mathrm{TiD}_{1.983}$ | $8.918 \times 10^{12}$ |

SUMMARY

## TABLE 9

Root Mean Square Displacement; Characteristic Temperature; Specific Heat; and Frequency of Vibration of Hafnium and Titanium Deuterides

| Composition | $\frac{2 B}{(\AA)^{2}}$ | $\frac{\bar{\mu}}{(\AA)}$ | $\frac{\mathrm{M}_{\mathrm{a}}}{(\mathrm{amu})}$ | $\frac{\Theta}{\left({ }^{(\mathrm{K}}\right)}$ | $\frac{\mathrm{C}_{\mathrm{v}}}{\left(\mathrm{cal} / \mathrm{mole}{ }^{\circ} \mathrm{C}\right)}$ | $($ (vibration$/ \mathrm{sec})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{HfD}_{1.628}$ | 1.68 | 0.103 | 69.21 | 244 | 5.638 | $5.084 \times 10^{12}$ |
| $\mathrm{HfD}_{1.983}$ | 1.06 | 0.082 | 61.21 | 329 | 5.398 | $6.855 \times 10^{12}$ |
| $\mathrm{TiD}_{1.971}$ | 2.26 | 0.120 | 17.46 | 428 | 5.062 | $8.918 \times 10^{12}$ |


[^0]:    ${ }^{1}$ For Example, Smith, D. P., Science, 113, 348 (1951)

[^1]:    ${ }^{5}$ Sidhu, S. S., Acta. Cryst. 7, 447 (1954).

[^2]:    ${ }^{6}$ Mag, G., Zs. phys. Chem. B11, 433 (1930).

[^3]:    ${ }^{11}$ Bacon, George, Neutron Diffraction (Oxford University Press, London 1955) p. 28.

[^4]:    12 Mark, H., Physical Chemistry of High Polymeric Systems, (Interscience Publishers, Inc., New York 1940) p. 51.

[^5]:    ${ }^{14}$ Metals Handbook (1948 Edition). Am. Soc. of Metals.
    ${ }^{15}$ Rundle, R. E., Acta Cryst. 1, 180 (1948).

