

New Physics / Resonances in Vector Boson Scattering at the LHC



Jürgen R. Reuter, DESY



based on work with A. Alboteanu, W. Kilian, T. Ohl, M. Sekulla

PRD93(16),3.036004 [1511.00022], PRD91(15),096007 [1408.6207],
US Snowmass Summer Study 1310.6708, 1309.7890, 1307.8180,
JHEP 0811.010 [0806.4145], EPJC48(06)353 [hep-ph/0604048]



Seen signals, unseen signals, seen un-signals (?)

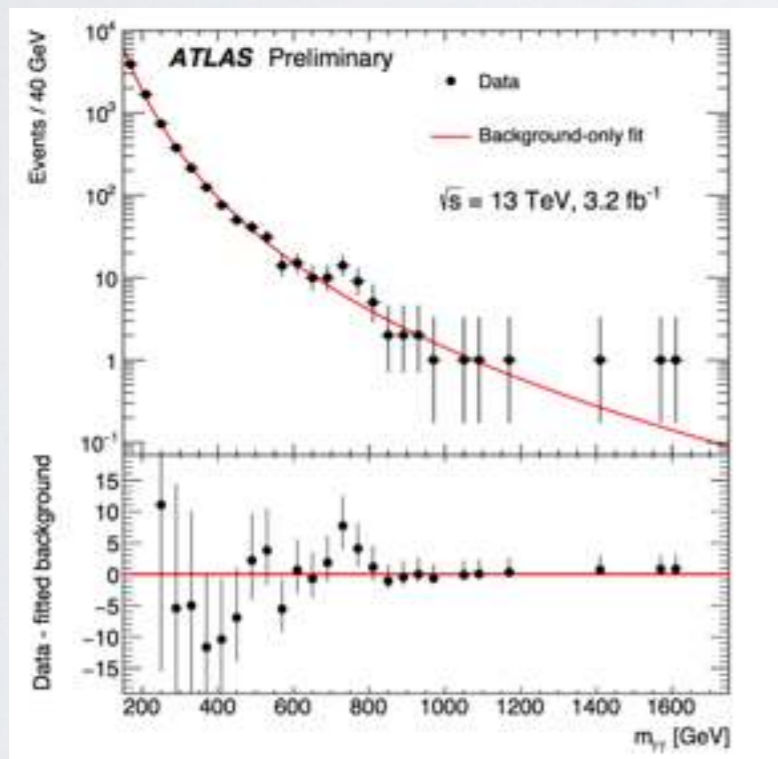
- Discovery of a light Higgs boson leaves still open questions:
 1. Nature of Electroweak Symmetry Breaking
 2. Higgs boson potential, all the way like the Standard Model!?
 3. Does it fulfill the US-fermion/Europe-boson rule?
 4. Is the 125 GeV state the only resonance in the system of EW vector bosons?
 5. How do EW vector bosons scatter? (true heart of weak interactions)
 6. Is there something related to the Little Hierarchy problem (strong or weak)



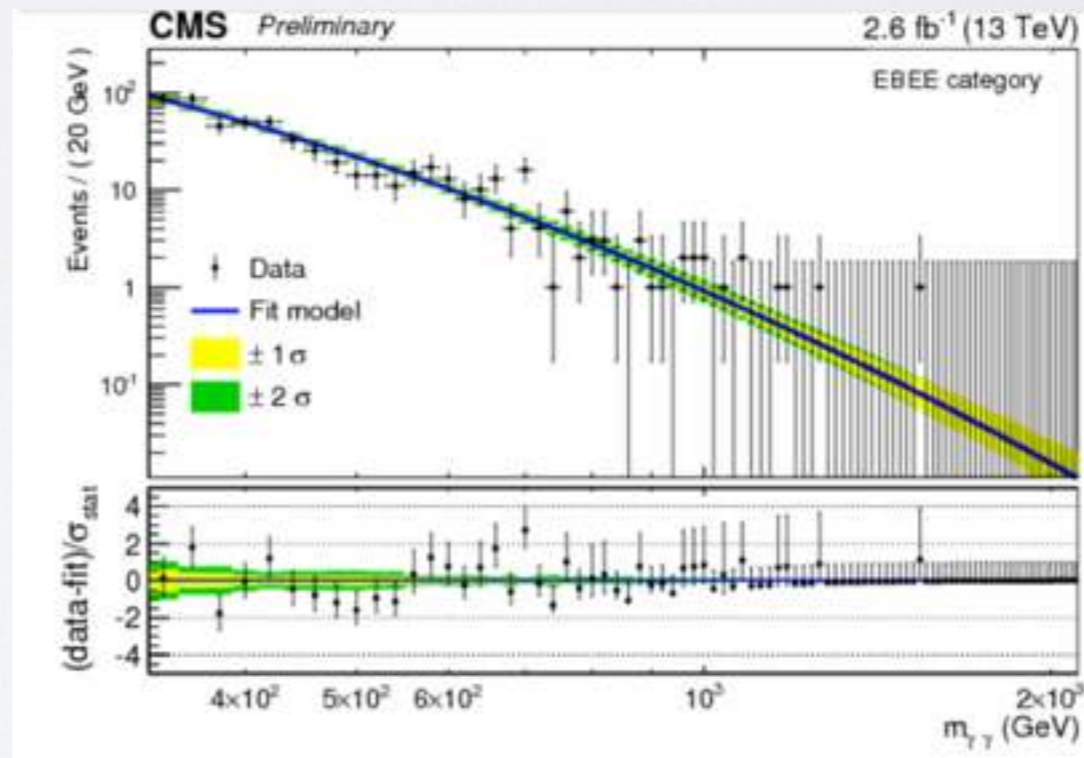
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CMS-PAS-EXO-15-004



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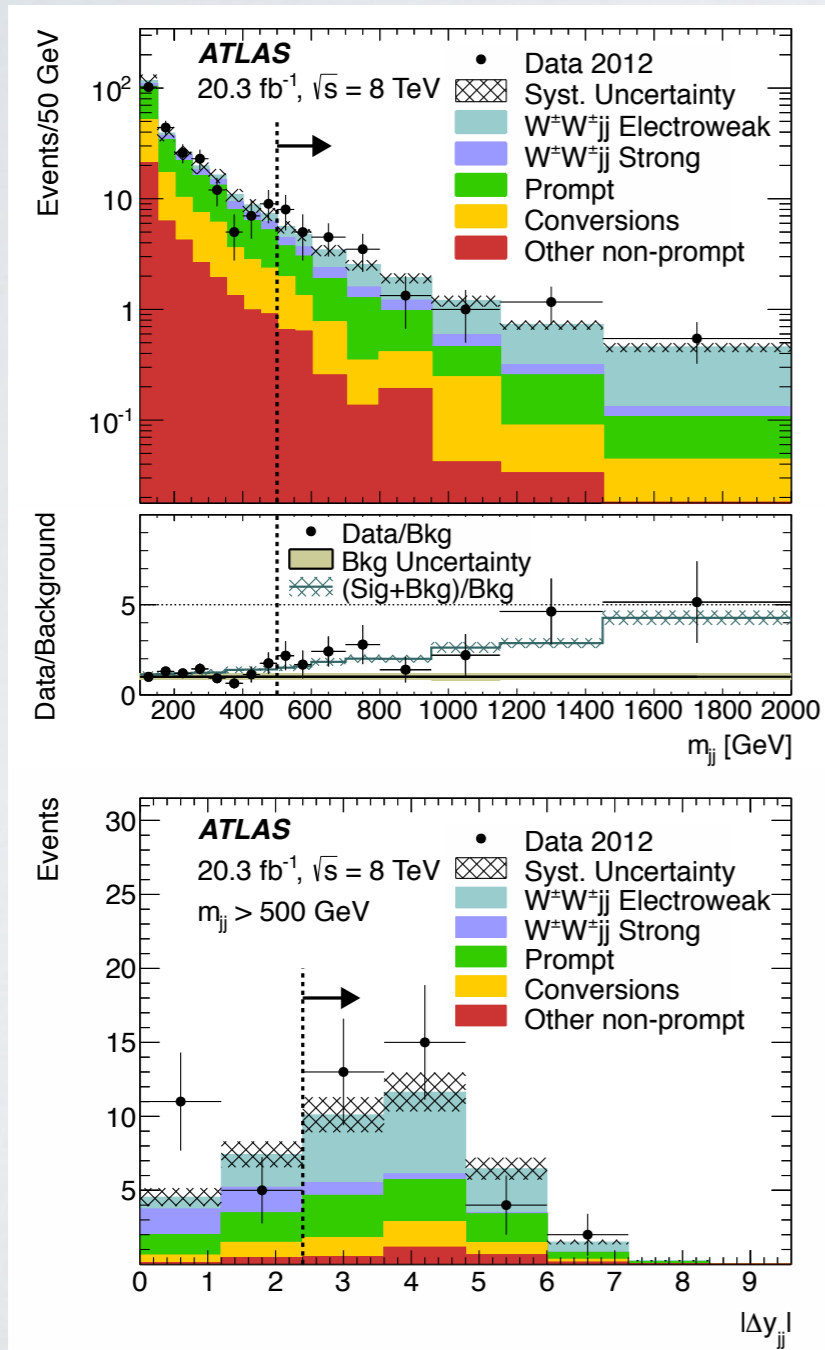
- Evidence for W^+W^+jj (electroweak production) Talk by Brigitte Vachon
ATLAS PRL 113(2014)14, 141803 [1405.6241]; CMS PRL 114(2015), 051801 [1410.6315]
- First limits on New Physics in pure electroweak gauge/Goldstone sector

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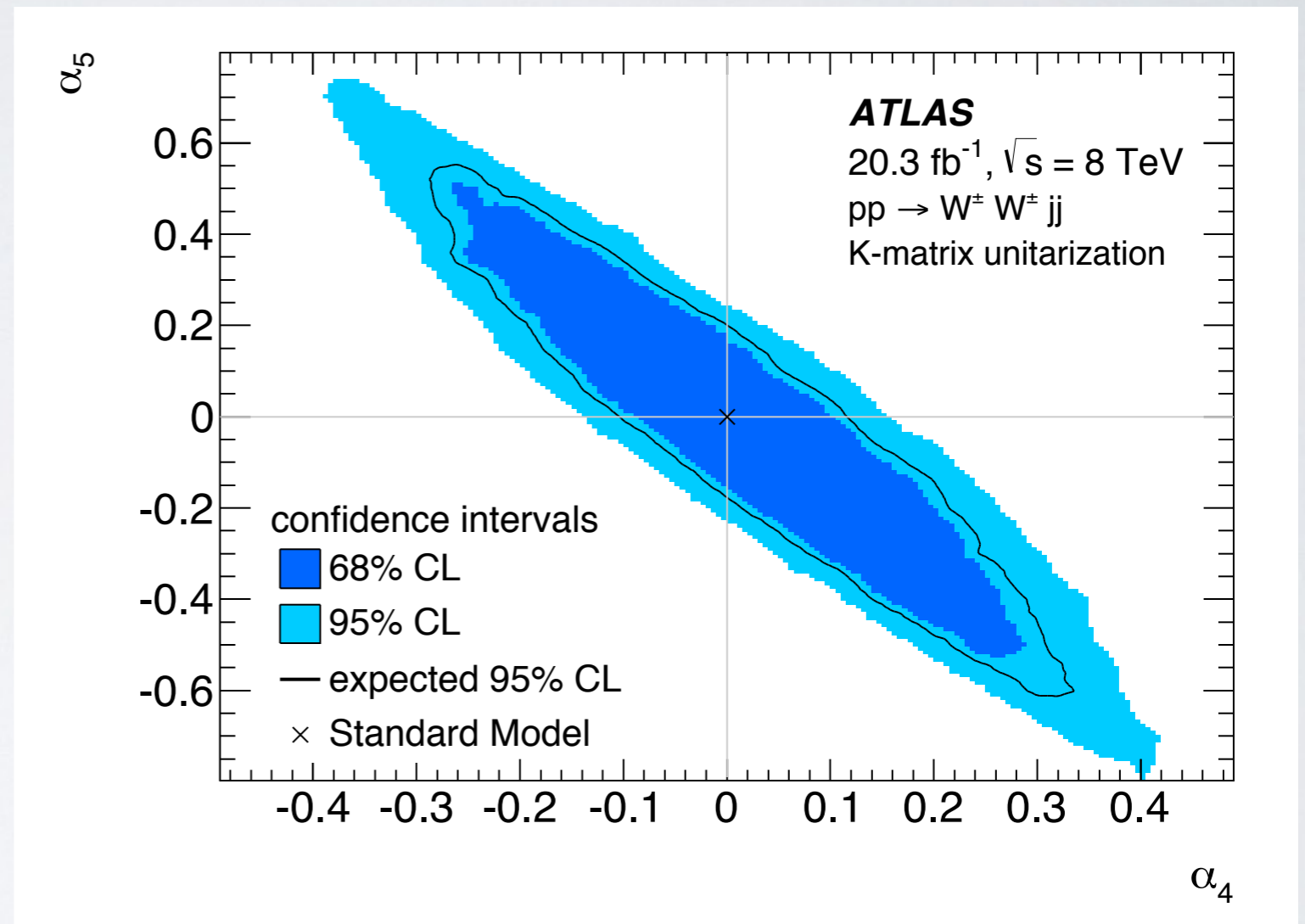
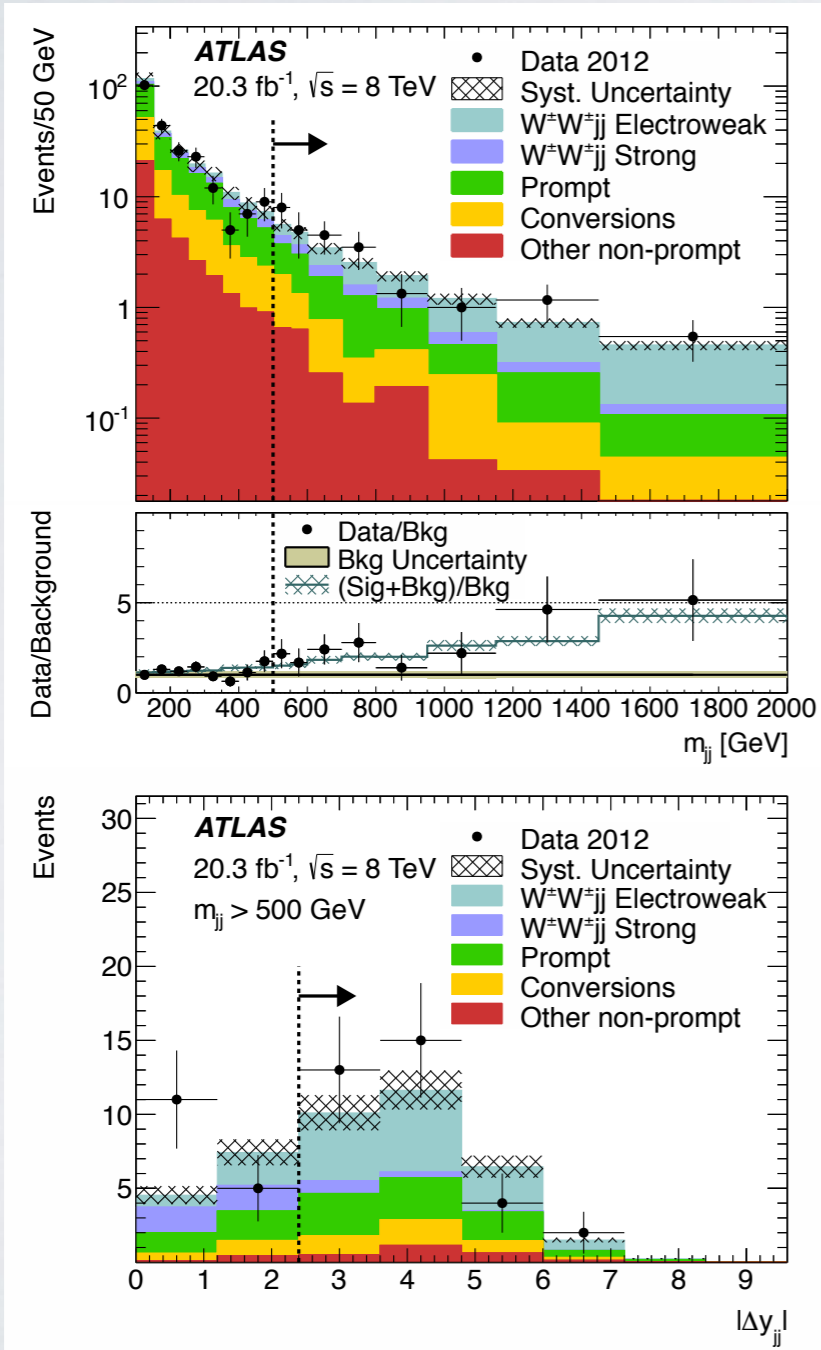


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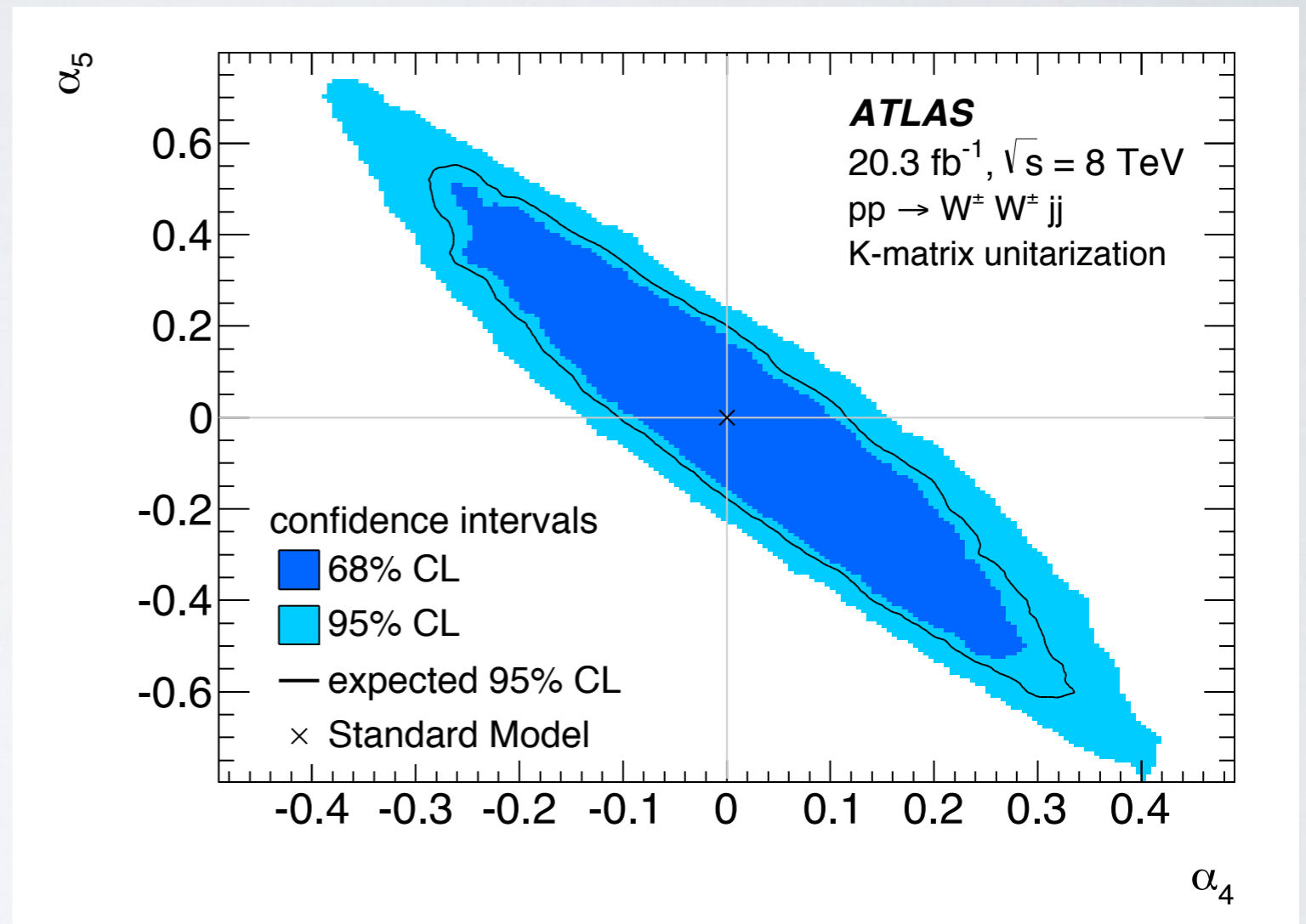
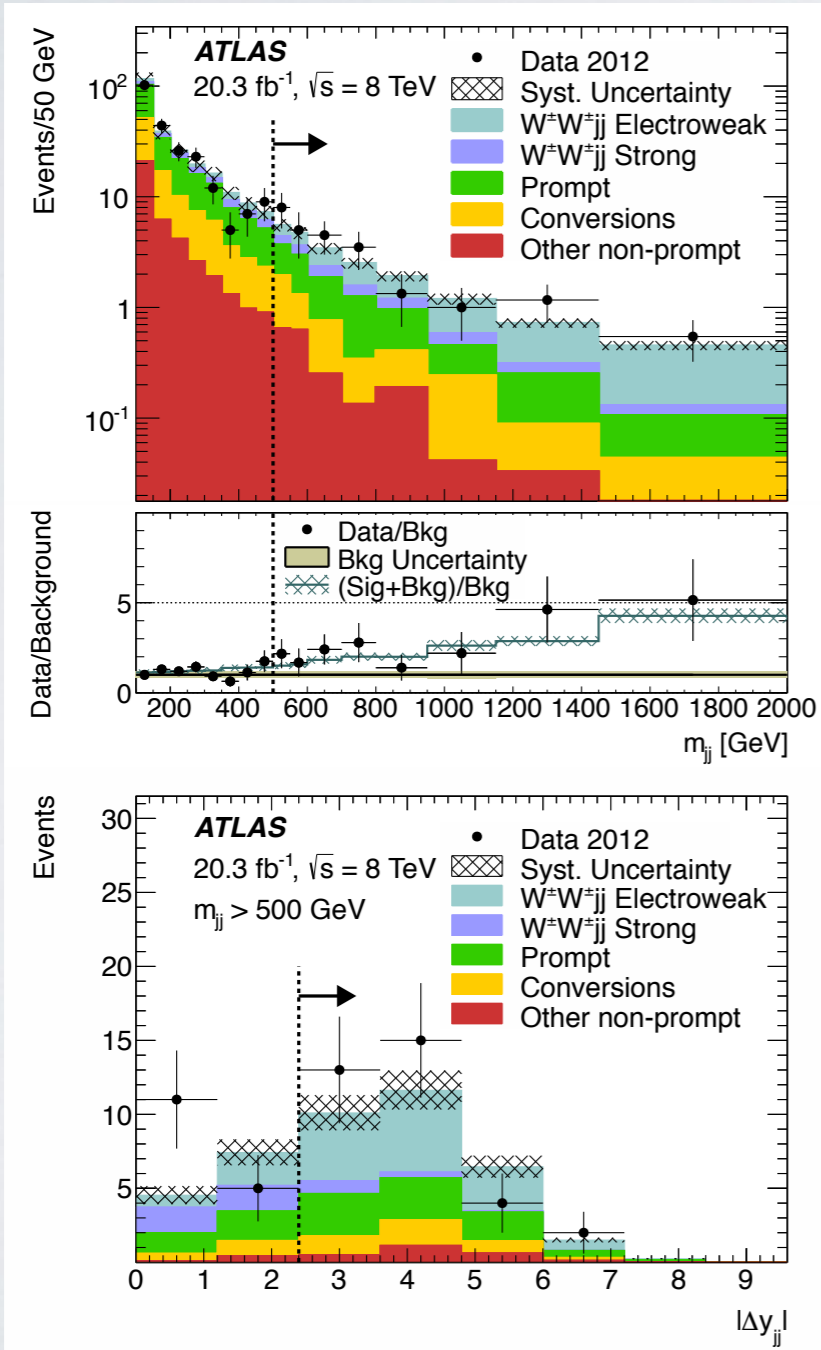


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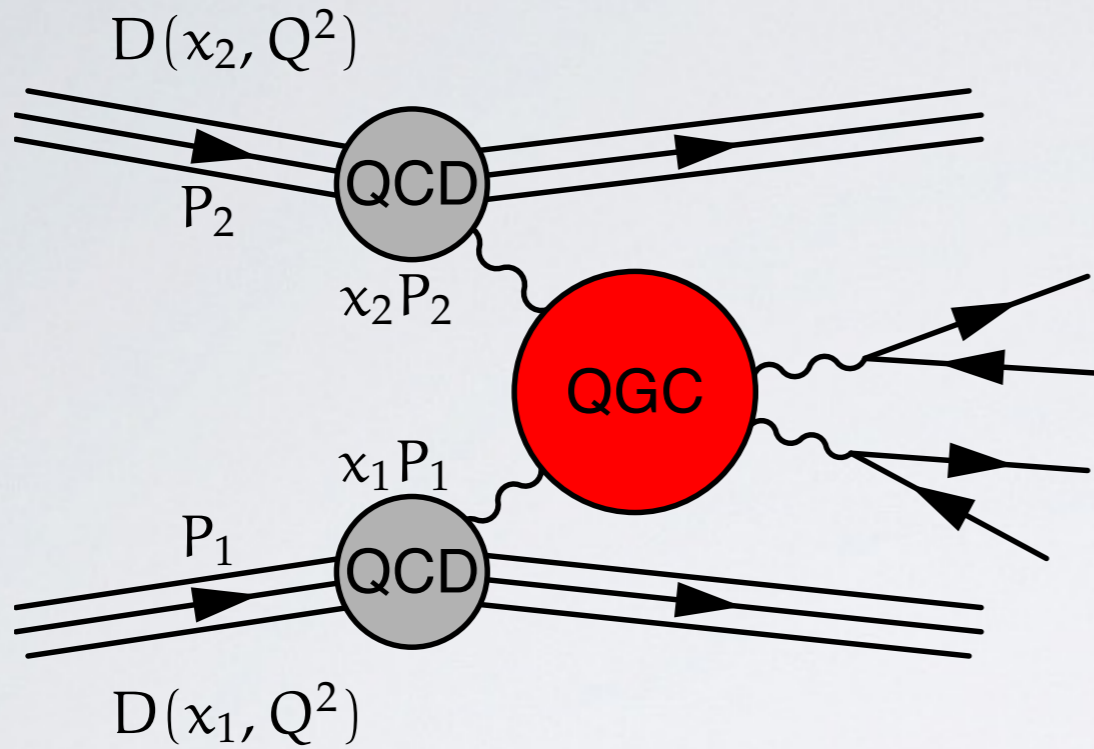
Exploration of E-frontier → look for heavy objects, including high-mass $V_L V_L$ scattering:
□ requires as much integrated luminosity as possible (cross-section goes like $1/s$)

F. Gianotti, 01/2014



Anatomy of Vector Boson Scattering (VBS)

$$pp \rightarrow WWjj \rightarrow \ell\nu\nu jj$$

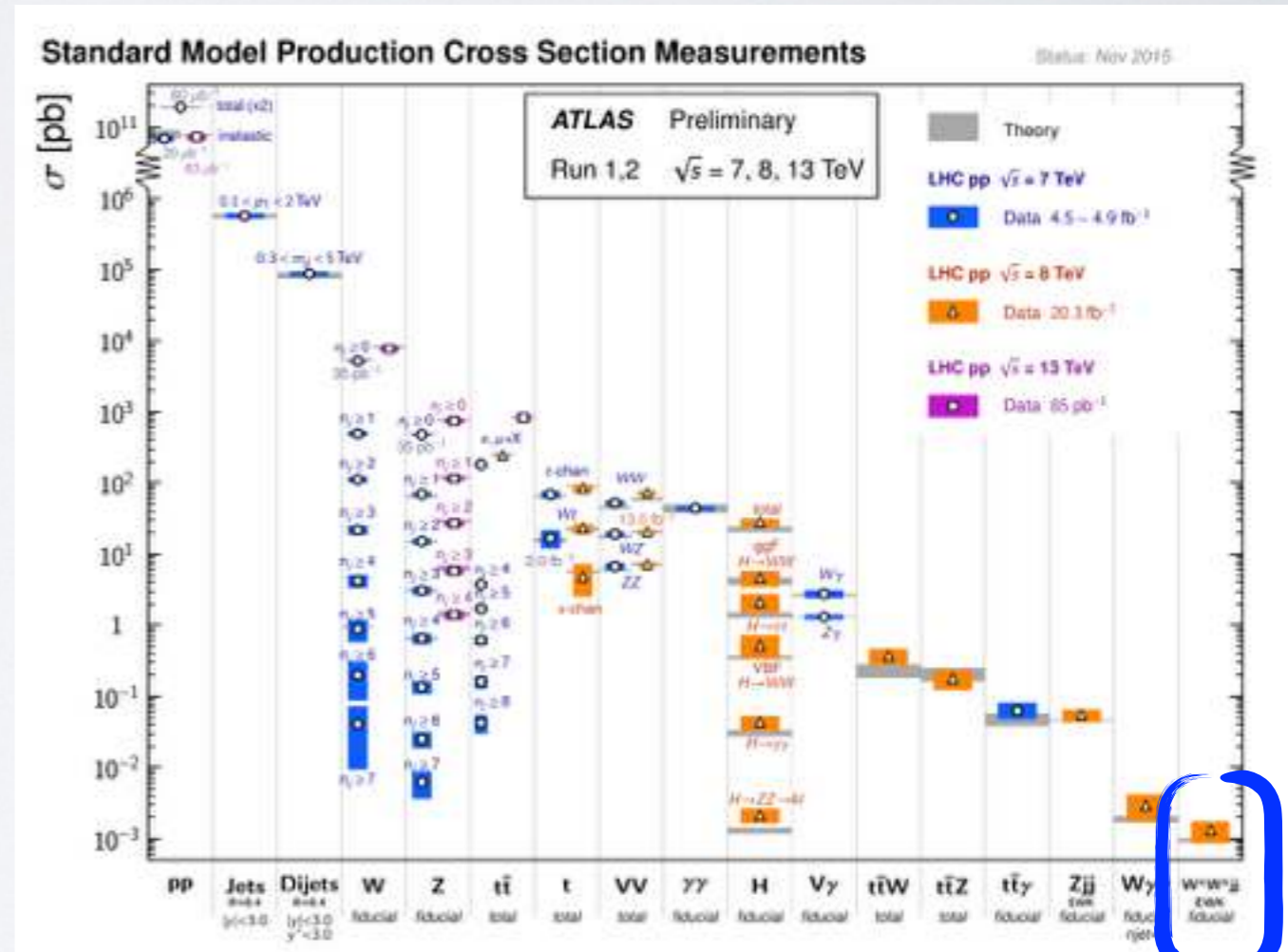


Backgrounds [+ $V_T V_T$ bkgd.]:

- $tt \rightarrow WbWb$
- $W + jets$
- single top, misreconstructed jet
- $WWjj$ QCD production
- $ll + X + Emiss$ (“prompt”)

Fiducial phase space volume:

- $lljj$ tag
- $m_{jj} > 500$ GeV (“jet recoil”)
- $y_{j,1} \cdot y_{j,2} < 0$ (“collinear beams”)
- $|\Delta y_{jj}| > 2.4$ (“rapidity distance”)
- Cuts on E_j , p_T^j
- No mini jet vetoes



EFTs: Higher-dimensional operators

- ◆ Must include all dim 6 operators from SM fields Buchmüller/Wyler, 1986
- ◆ Redundancy of operators \implies minimal set of operators (in principle)
 1. Equations of motion: $D_\mu \mathbf{W}^{\mu\nu} = \Phi^\dagger (D^\nu \Phi) - (D^\nu \Phi)^\dagger \Phi + \dots$
 2. Gauge symmetry: $[D_\mu, D_\nu] \Phi \propto \mathbf{W}_{\mu\nu} \Phi$
 3. Integration by parts: $(\Phi^\dagger \Phi) \square (\Phi^\dagger \Phi) \longrightarrow \partial_\mu (\Phi^\dagger \Phi) \partial^\mu (\Phi^\dagger \Phi)$
- ◆ Further reduction by use of discrete / horizontal symmetries
 1. B and L conservation (excludes 5 operators per generation)
 2. Flavor symmetries (assumption: Minimal Flavor Violation)
 3. CP symmetry
- ◆ Assuming B and L conservation: number of operators (without ν_R)

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- ◆ **Assuming B and L conservation:** number of operators (without ν_R)
 - 1 dim-2 operator + 15 dim-4 operators
 - **59 dim-6 operators for 1 generation**
 - **2499 dim-6 operators for 3 generations** Alonso/Jenkins/Manohar/Trott, 2013

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- ◆ No unique basis exists (more in a second)
- ◆ Well-known in B physics: different experimental measurements constrain different operators

Effective Field Theories: Operator Bases

No unique basis exists

- ▶ “HISZ” basis: no fermionic operators [Hagiwara/Ishihara/Szalapski/Zeppenfeld, 1993](#)
- ▶ “GIMR” basis: first minimal complete basis [Grzadkowski/Iskrzyński/Misiak/Rosiek, 2010](#)
- ▶ “SILH” basis: complete basis [Giudice/Grojean/Pomarol/Ratazzi, 2007; Elias-Miró et al, 2013](#)
- ▶ Dim. 8 operators: [Eboli et al., 2006; Kilian/JRR/Ohl/Sekulla, 2014+2015](#)



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Φ^6 and $\Phi^4 D^2$	$\psi^2 \Phi^3$	X^3
$\mathcal{O}_\Phi = (\Phi^\dagger \Phi)^3$	$\mathcal{O}_{e\Phi} = (\Phi^\dagger \Phi)(\bar{l}\Gamma_e e\Phi)$	$\mathcal{O}_G = f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$
$\mathcal{O}_{\Phi\Box} = (\Phi^\dagger \Phi)\Box(\Phi^\dagger \Phi)$	$\mathcal{O}_{u\Phi} = (\Phi^\dagger \Phi)(\bar{q}\Gamma_u u\tilde{\Phi})$	$\mathcal{O}_{\tilde{G}} = f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$
$\mathcal{O}_{\Phi D} = (\Phi^\dagger D^\mu \Phi)^*(\Phi^\dagger D_\mu \Phi)$	$\mathcal{O}_{d\Phi} = (\Phi^\dagger \Phi)(\bar{q}\Gamma_d d\Phi)$	$\mathcal{O}_W = \varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$
		$\mathcal{O}_{\tilde{W}} = \varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$
$X^2 \Phi^2$	$\psi^2 X \Phi$	$\psi^2 \Phi^2 D$
$\mathcal{O}_{\Phi G} = (\Phi^\dagger \Phi) G_{\mu\nu}^A G^{A\mu\nu}$	$\mathcal{O}_{uG} = (\bar{q}\sigma^{\mu\nu} \frac{\lambda^A}{2} \Gamma_u u\tilde{\Phi}) G_{\mu\nu}^A$	$\mathcal{O}_{\Phi l}^{(1)} = (\Phi^\dagger i\overleftrightarrow{D}_\mu \Phi)(\bar{l}\gamma^\mu l)$
$\mathcal{O}_{\Phi \tilde{G}} = (\Phi^\dagger \Phi) \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$\mathcal{O}_{dG} = (\bar{q}\sigma^{\mu\nu} \frac{\lambda^A}{2} \Gamma_d d\Phi) G_{\mu\nu}^A$	$\mathcal{O}_{\Phi l}^{(3)} = (\Phi^\dagger i\overleftrightarrow{D}_\mu^I \Phi)(\bar{l}\gamma^\mu \tau^I l)$
$\mathcal{O}_{\Phi W} = (\Phi^\dagger \Phi) W_{\mu\nu}^I W^{I\mu\nu}$	$\mathcal{O}_{eW} = (\bar{l}\sigma^{\mu\nu} \Gamma_e e\tau^I \Phi) W_{\mu\nu}^I$	$\mathcal{O}_{\Phi e} = (\Phi^\dagger i\overleftrightarrow{D}_\mu \Phi)(\bar{e}\gamma^\mu e)$
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$\mathcal{O}_{\Phi \tilde{B}} = (\Phi^\dagger \Phi) \tilde{B}_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{eB} = (\bar{l}\sigma^{\mu\nu} \Gamma_e e\Phi) B_{\mu\nu}$	$\mathcal{O}_{\Phi u} = (\Phi^\dagger i\overleftrightarrow{D}_\mu \Phi)(\bar{u}\gamma^\mu u)$
$\mathcal{O}_{\Phi WB} = (\Phi^\dagger \tau^I \Phi) W_{\mu\nu}^I B^{\mu\nu}$	$\mathcal{O}_{uB} = (\bar{q}\sigma^{\mu\nu} \Gamma_u u\tilde{\Phi}) B_{\mu\nu}$	$\mathcal{O}_{\Phi d} = (\Phi^\dagger i\overleftrightarrow{D}_\mu \Phi)(\bar{d}\gamma^\mu d)$
$\mathcal{O}_{\Phi \tilde{W}B} = (\Phi^\dagger \tau^I \Phi) \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$\mathcal{O}_{dB} = (\bar{q}\sigma^{\mu\nu} \Gamma_d d\Phi) B_{\mu\nu}$	$\mathcal{O}_{\Phi ud} = i(\tilde{\Phi}^\dagger D_\mu \Phi)(\bar{u}\gamma^\mu \Gamma_{ud} d)$
+ 25 four-fermion operators Grzadkowski et al.		



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$\mathcal{O}'_\Phi = \partial_\mu (\Phi^\dagger \Phi) \partial^\mu (\Phi^\dagger \Phi)$	$\mathcal{O}'_{u\Phi} = (\Phi^\dagger \Phi)(\bar{q} \Gamma_u u \tilde{\Phi})$	$\mathcal{O}'_{\tilde{G}} = f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$
$\mathcal{O}'_T = (\Phi^\dagger \overleftrightarrow{D}_\mu \Phi)(\Phi^\dagger \overleftrightarrow{D}^\mu \Phi)$	$\mathcal{O}'_{d\Phi} = (\Phi^\dagger \Phi)(\bar{q} \Gamma_d d \Phi)$	$\mathcal{O}'_W = \varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$
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$X^2 \Phi^2$	$\psi^2 X \Phi$	$\psi^2 \Phi^2 D$
$\mathcal{O}'_{DW} = (\Phi^\dagger \tau^I i \overleftrightarrow{D}^\mu \Phi) (D^\nu W_{\mu\nu})^I$	$\mathcal{O}'_{uG} = (\bar{q} \sigma^{\mu\nu} \frac{\lambda^A}{2} \Gamma_u u \tilde{\Phi}) G_{\mu\nu}^A$	$\mathcal{O}'_{\Phi 1}^{(1)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi) (\bar{l} \gamma^\mu l)$
$\mathcal{O}'_{DB} = (\Phi^\dagger i \overleftrightarrow{D}^\mu \Phi) (\partial^\nu B_{\mu\nu})$	$\mathcal{O}'_{dG} = (\bar{q} \sigma^{\mu\nu} \frac{\lambda^A}{2} \Gamma_d d \Phi) G_{\mu\nu}^A$	$\mathcal{O}'_{\Phi 1}^{(3)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu^I \Phi) (\bar{l} \gamma^\mu \tau^I l)$
$\mathcal{O}'_{D\Phi W} = i(D^\mu \Phi)^\dagger \tau^I (D^\nu \Phi) W_{\mu\nu}^I$	$\mathcal{O}'_{eW} = (\bar{l} \sigma^{\mu\nu} \Gamma_e e \tau^I \Phi) W_{\mu\nu}^I$	$\mathcal{O}'_{\Phi e} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi) (\bar{e} \gamma^\mu e)$
$\mathcal{O}'_{D\Phi \tilde{W}} = i(D^\mu \Phi)^\dagger \tau^I (D^\nu \Phi) \tilde{W}_{\mu\nu}^I$	$\mathcal{O}'_{uW} = (\bar{q} \sigma^{\mu\nu} \Gamma_u u \tau^I \tilde{\Phi}) W_{\mu\nu}^I$	$\mathcal{O}'_{\Phi q}^{(1)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu \Phi) (\bar{q} \gamma^\mu q)$
$\mathcal{O}'_{D\Phi B} = i(D^\mu \Phi)^\dagger (D^\nu \Phi) B_{\mu\nu}$	$\mathcal{O}'_{dW} = (\bar{q} \sigma^{\mu\nu} \Gamma_d d \tau^I \tilde{\Phi}) W_{\mu\nu}^I$	$\mathcal{O}'_{\Phi q}^{(3)} = (\Phi^\dagger i \overleftrightarrow{D}_\mu^I \Phi) (\bar{q} \gamma^\mu \tau^I q)$
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Giudice et al. / Contino et al.

+ (25-2) four-fermion operators



Operators and Multi(EW)-boson Physics (I)



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Dimension-6 operators for Multiboson physics (CP-conserving)

$$\mathcal{O}_{WWW} = \text{Tr}[W_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}]$$

$$\mathcal{O}_W = (D_{\mu}\Phi)^{\dagger} W^{\mu\nu} (D_{\nu}\Phi)$$

$$\mathcal{O}_B = (D_{\mu}\Phi)^{\dagger} B^{\mu\nu} (D_{\nu}\Phi)$$

$$\mathcal{O}_{\partial\Phi} = \partial_{\mu} (\Phi^{\dagger}\Phi) \partial^{\mu} (\Phi^{\dagger}\Phi)$$

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Dimension-6 operators for Multiboson physics (CP-violating)

$$\begin{aligned}\mathcal{O}_{\widetilde{W}W} &= \Phi^{\dagger} \widetilde{W}_{\mu\nu} W^{\mu\nu} \Phi & \mathcal{O}_{\widetilde{W}WW} &= \text{Tr}[\widetilde{W}_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}] \\ \mathcal{O}_{\widetilde{B}B} &= \Phi^{\dagger} \widetilde{B}_{\mu\nu} B^{\mu\nu} \Phi & \mathcal{O}_{\widetilde{W}} &= (D_{\mu}\Phi)^{\dagger} \widetilde{W}^{\mu\nu} (D_{\nu}\Phi)\end{aligned}$$

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Dimension-6 operators for Multiboson physics (CP-violating)

$$\begin{aligned}
 \mathcal{O}_{\tilde{W}W} &= \Phi^{\dagger} \tilde{W}_{\mu\nu} W^{\mu\nu} \Phi & \mathcal{O}_{\tilde{W}WW} &= \text{Tr}[\tilde{W}_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}] \\
 \mathcal{O}_{\tilde{B}B} &= \Phi^{\dagger} \tilde{B}_{\mu\nu} B^{\mu\nu} \Phi & \mathcal{O}_{\tilde{W}} &= (D_{\mu}\Phi)^{\dagger} \tilde{W}^{\mu\nu} (D_{\nu}\Phi)
 \end{aligned}$$

Affect the following electroweak couplings:

	ZWW	AWW	HWW	HZZ	HZA	HAA	WWWW	ZZWW	ZAWW	AAWW
\mathcal{O}_{WWW}	✓	✓					✓	✓	✓	✓
\mathcal{O}_W	✓	✓	✓	✓	✓		✓	✓	✓	
\mathcal{O}_B	✓	✓		✓	✓					
$\mathcal{O}_{\Phi d}$			✓	✓						
$\mathcal{O}_{\Phi W}$			✓	✓	✓	✓				
$\mathcal{O}_{\Phi B}$				✓	✓	✓				
$\mathcal{O}_{\tilde{W}WW}$	✓	✓					✓	✓	✓	✓
$\mathcal{O}_{\tilde{W}}$	✓	✓	✓	✓	✓					
$\mathcal{O}_{\tilde{W}W}$			✓	✓	✓	✓				
$\mathcal{O}_{\tilde{B}B}$				✓	✓	✓				

Operators and Multi(EW)-boson Physics (I)

Dimension-6 operators for Multiboson physics (CP-conserving)

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 \mathcal{O}_{WWW} &= \text{Tr}[W_{\mu\nu} W^{\nu\rho} W_{\rho}^{\mu}] & \mathcal{O}_{\partial\Phi} &= \partial_{\mu} (\Phi^{\dagger}\Phi) \partial^{\mu} (\Phi^{\dagger}\Phi) \\
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 \mathcal{O}_{\tilde{B}B} &= \Phi^{\dagger} \tilde{B}_{\mu\nu} B^{\mu\nu} \Phi & \mathcal{O}_{\tilde{W}} &= (D_{\mu}\Phi)^{\dagger} \tilde{W}^{\mu\nu} (D_{\nu}\Phi)
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Affect the following electroweak couplings:

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\mathcal{O}_{WWW}	✓	✓					✓	✓	✓	✓
\mathcal{O}_W	✓	✓	✓	✓	✓		✓	✓	✓	
\mathcal{O}_B	✓	✓		✓	✓					
$\mathcal{O}_{\Phi d}$			✓	✓	✓					
$\mathcal{O}_{\Phi W}$			✓	✓	✓	✓				
$\mathcal{O}_{\Phi B}$				✓	✓	✓				
$\mathcal{O}_{\tilde{W}WW}$	✓	✓					✓	✓	✓	✓
$\mathcal{O}_{\tilde{W}}$	✓	✓	✓	✓	✓					
$\mathcal{O}_{\tilde{W}W}$			✓	✓	✓	✓				
$\mathcal{O}_{\tilde{B}B}$				✓	✓	✓				

connected to Higgs physics



Operators and Multi(EW)-boson Physics (II)

Dimension-8 operators for Multiboson physics

$$\mathcal{O}_{T,0} = \text{Tr} [W_{\mu\nu} W^{\mu\nu}] \cdot \text{Tr} [W_{\alpha\beta} W^{\alpha\beta}]$$

$$\mathcal{O}_{T,1} = \text{Tr} [W_{\alpha\nu} W^{\mu\beta}] \cdot \text{Tr} [W_{\mu\beta} W^{\alpha\nu}]$$

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$$\mathcal{O}_{T,8} = B_{\mu\nu} B^{\mu\nu} B_{\alpha\beta} B^{\alpha\beta}$$

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$$\mathcal{O}_{S,0} = [(D_\mu \Phi)^\dagger D_\nu \Phi] \times [(D^\mu \Phi)^\dagger D^\nu \Phi]$$

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	WWWW	WWZZ	ZZZZ	WWAZ	WWAA	ZZZA	ZZAA	ZAAA	AAAA
$\mathcal{O}_{S,0/1}$	✓	✓	✓						
$\mathcal{O}_{M,0/1/6/7}$	✓	✓	✓	✓	✓	✓	✓		
$\mathcal{O}_{M,2/3/4/5}$		✓	✓	✓	✓	✓	✓		
$\mathcal{O}_{T,0/1/2}$	✓	✓	✓	✓	✓	✓	✓	✓	✓
$\mathcal{O}_{T,5/6/7}$		✓	✓	✓	✓	✓	✓	✓	✓
$\mathcal{O}_{T,8/9}$			✓			✓	✓	✓	✓



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$\mathcal{O}_{T,5/6/7}$		✓	✓	✓	✓	✓	✓	✓	✓
$\mathcal{O}_{T,8/9}$			✓			✓	✓	✓	✓

- Dim. 8 generate aQGCs independently
- generate neutral quartic couplings



Unitarity in vector boson scattering

Optical Theorem (Unitarity of the S(cattering) Matrix):

$$\sigma_{\text{tot}} = \text{Im} [\mathcal{M}_{ii}(t=0)] / s \quad t = -s(1 - \cos \theta)/2$$

Partial wave amplitudes:

$$\mathcal{M}(s, t, u) = 32\pi \sum_{\ell} (2\ell + 1) \mathcal{A}_{\ell}(s) P_{\ell}(\cos \theta) \quad (\text{"Power spectrum"})$$

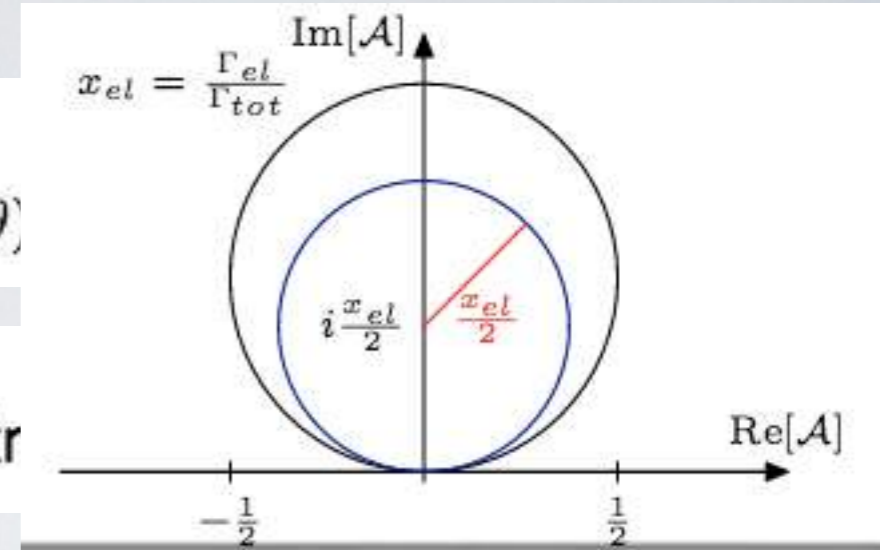
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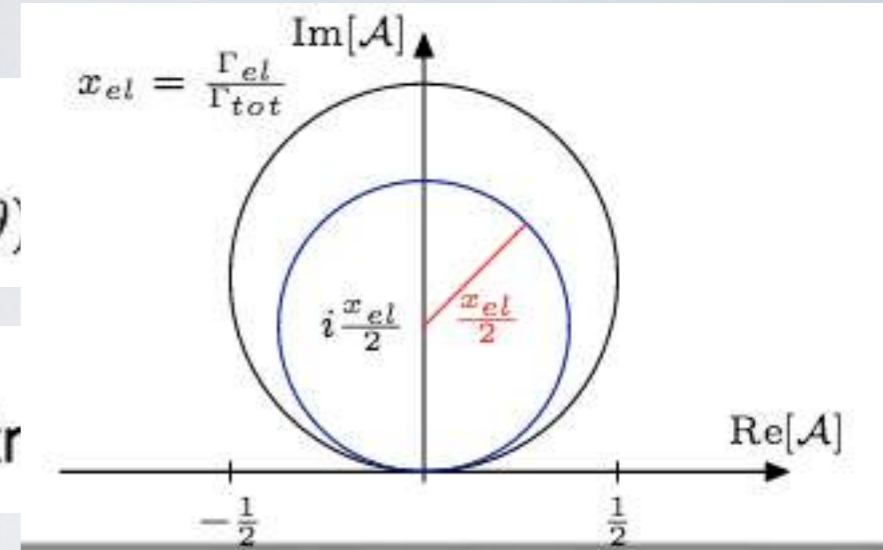
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Assuming only elastic scattering:

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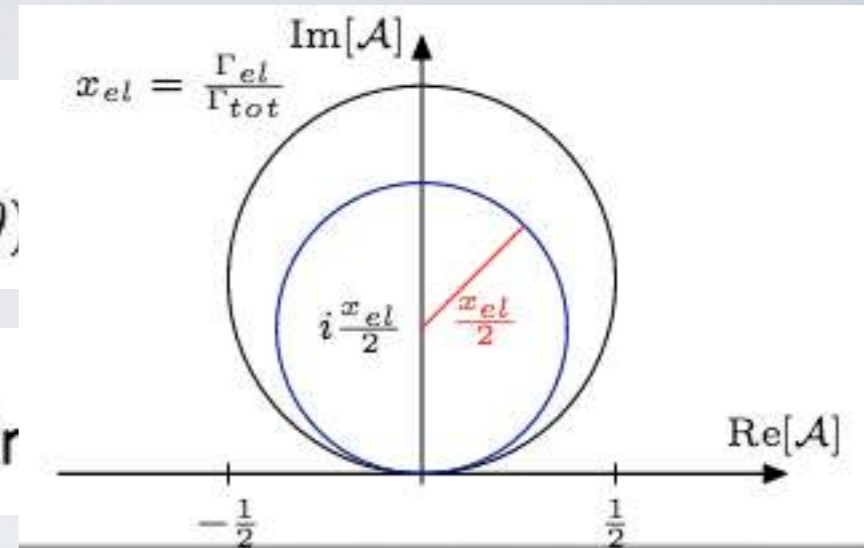
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SM longitudinal isospin eigenamplitudes ($\mathcal{A}_{I, \text{spin}=J}$):

$$\mathcal{A}_{I=0} = 2 \frac{s}{v^2} P_0(s) \quad \mathcal{A}_{I=1} = \frac{t-u}{v^2} = \frac{s}{v^2} P_1(s) \quad \mathcal{A}_{I=2} = -\frac{s}{v^2} P_0(s)$$

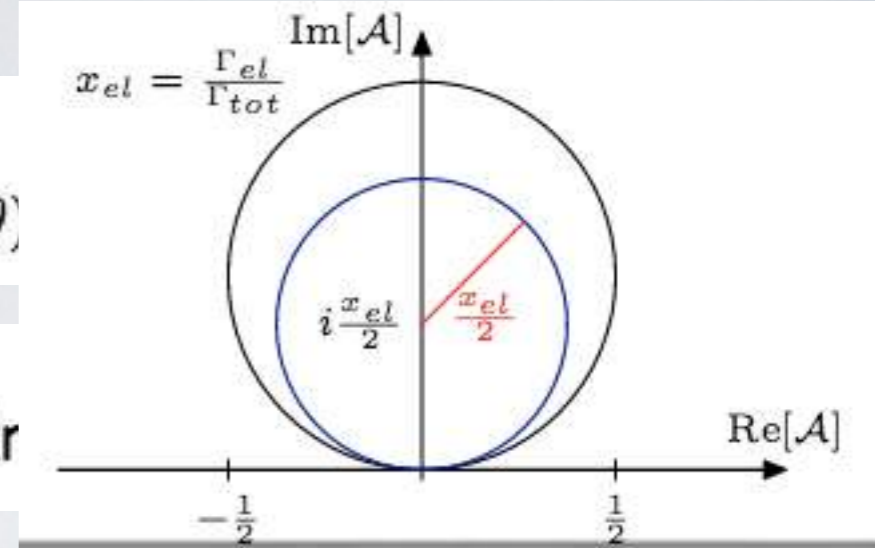
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Lee/Quigg/Thacker, 1973

exceeds unitarity bound $|\mathcal{A}_{IJ}| \lesssim \frac{1}{2}$ at:

$$I = 0 : \quad E \sim \sqrt{8\pi} v = 1.2 \text{ TeV}$$

$$I = 1 : \quad E \sim \sqrt{48\pi} v = 3.5 \text{ TeV}$$

$$I = 2 : \quad E \sim \sqrt{16\pi} v = 1.7 \text{ TeV}$$

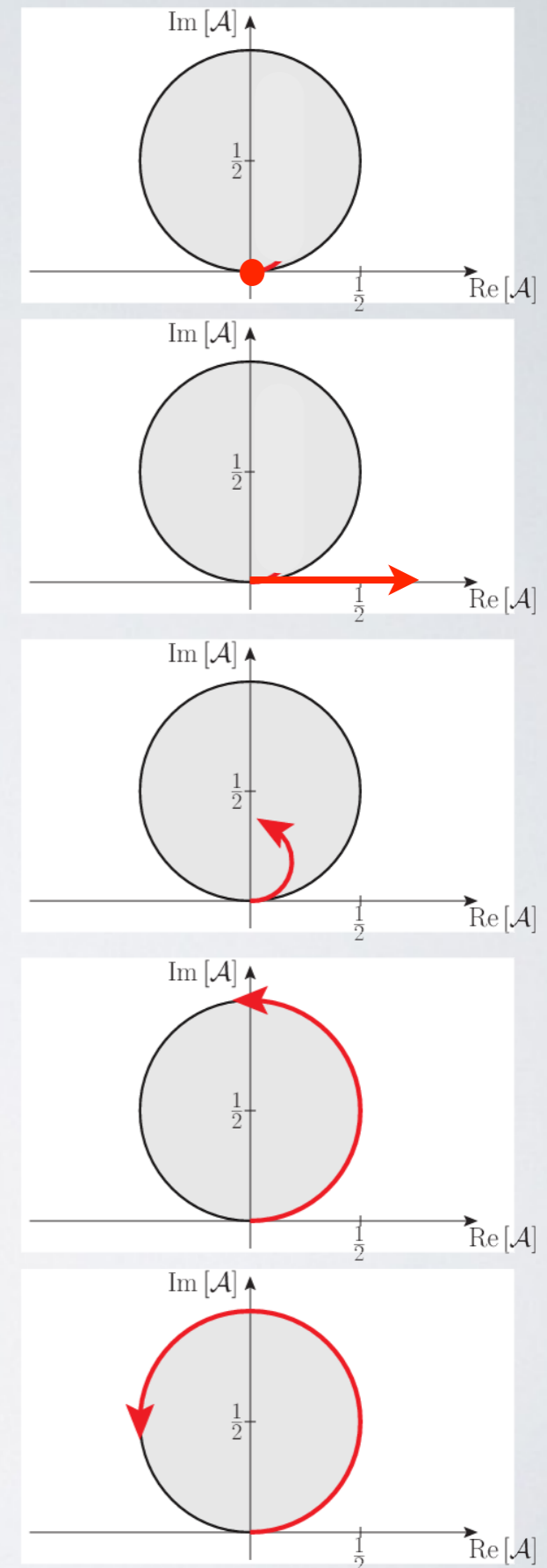
Higgs exchange:

$$\mathcal{A}(s, t, u) = -\frac{M_H^2}{v^2} \frac{s}{s - M_H^2}$$

Unitarity: $M_H \lesssim \sqrt{8\pi} v \sim 1.2 \text{ TeV}$

Scenarios for New Physics in VBS

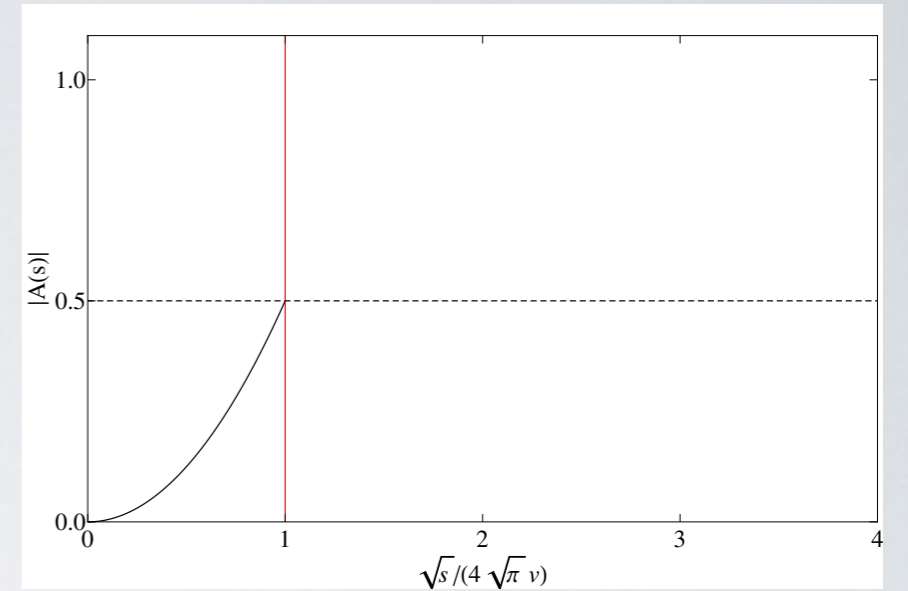
1. **SM or weakly coupled physics (e.g. 2HDM):** amplitude remains close to origin
2. **Rising amplitude (at least one dim-8 operator):** rise beyond unitarity circle [unphys.], strongly interacting regime
3. **Inelastic channel opens (form-factor description):** new channels open out, multi-boson final states
4. **Saturation of amplitude:** maximal amplitude, strongly interacting continuum, K-/T-matrix unitarization
5. **New resonance:** amplitude turns over



Procedures to treat unitarity violations

Cut-off (a.k.a. “Event clipping”) $\theta(\Lambda_C^2 - s)$

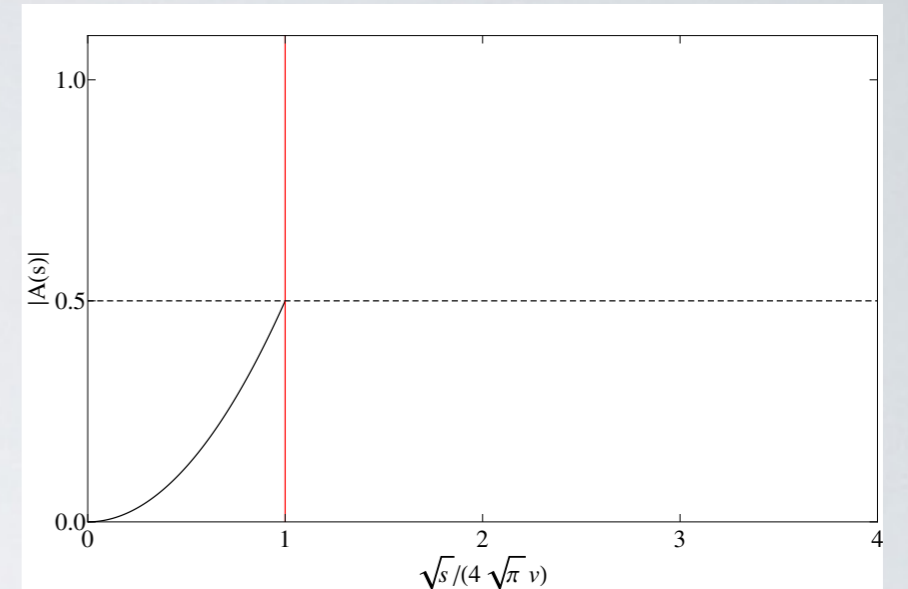
unitarity bound (0th partial wave) at Λ_C
no continuous transition beyond



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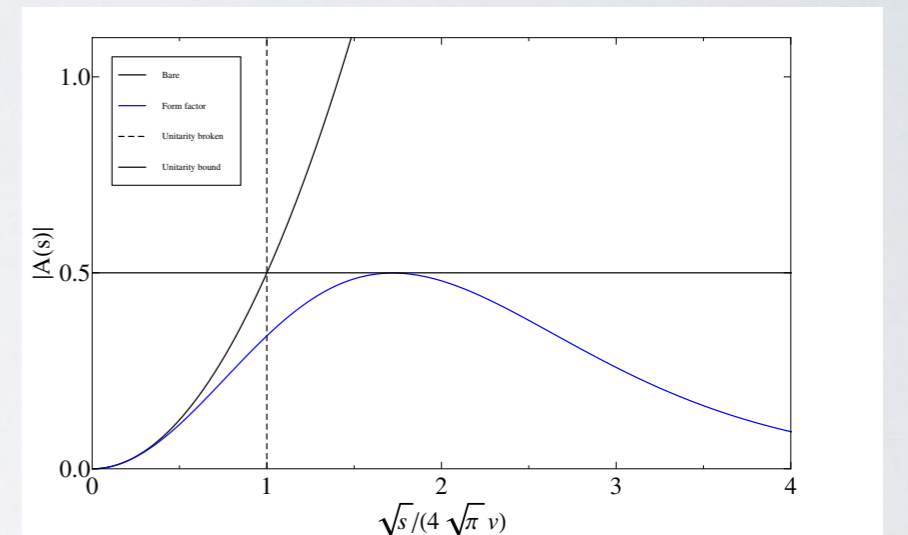
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Form factor

$$\frac{1}{\left(1 + \frac{s}{\Lambda_{FF}^2}\right)^n}$$

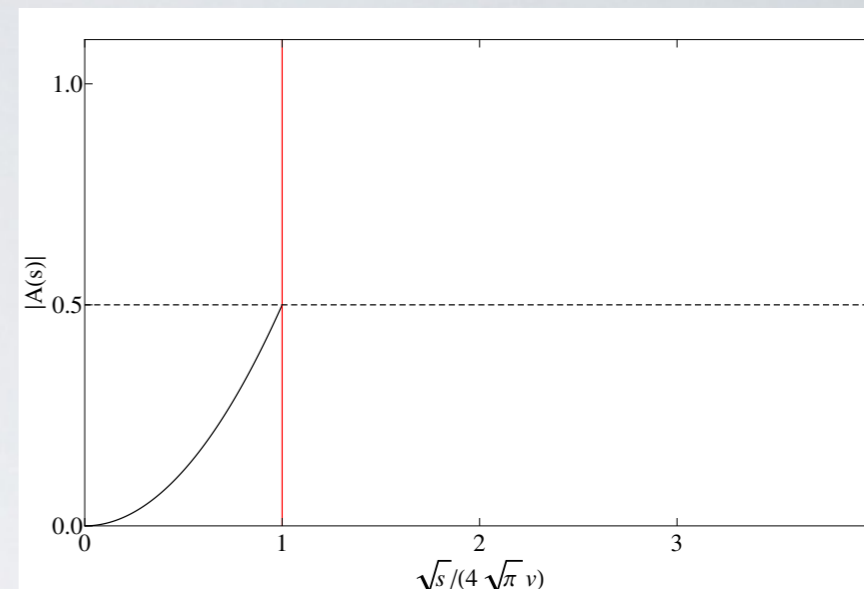
Applicable for arbitrary operators, tuning in 2 parameters: n damps unitarity violation, Λ_{FF} highest value to satisfy 0th partial wave



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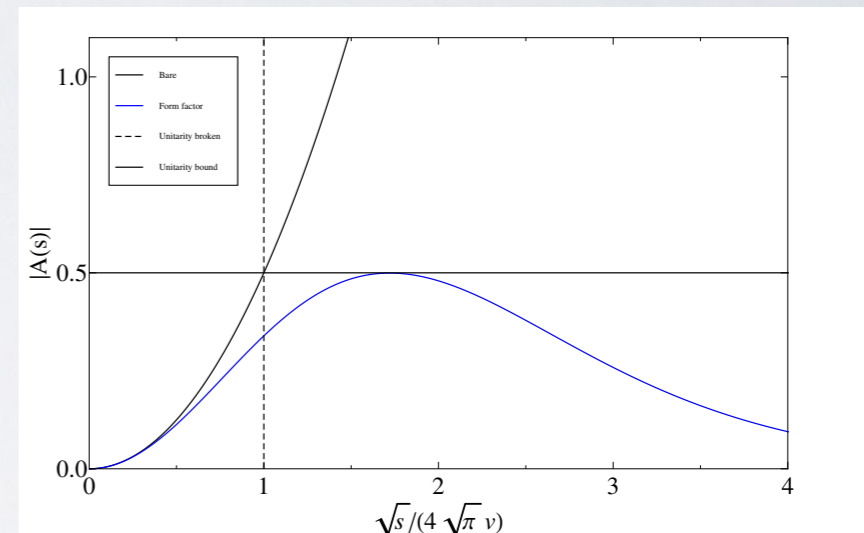
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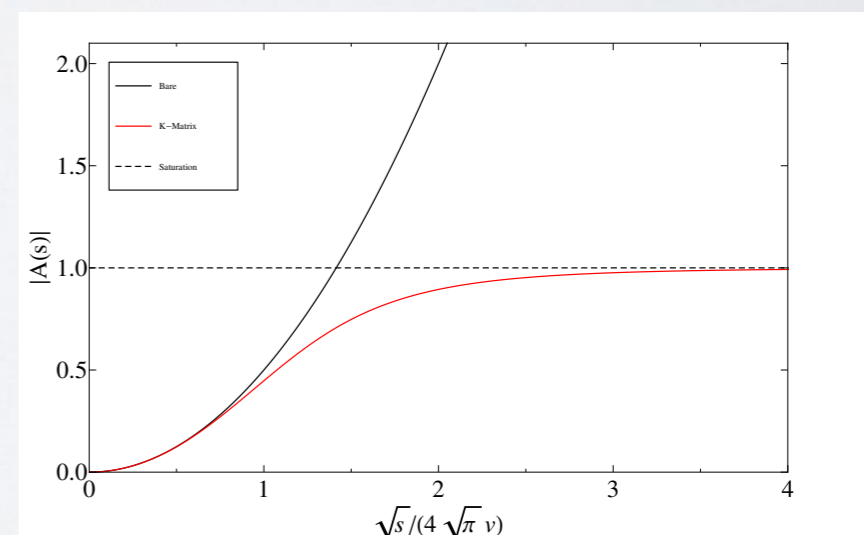
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K-/T-matrix saturation

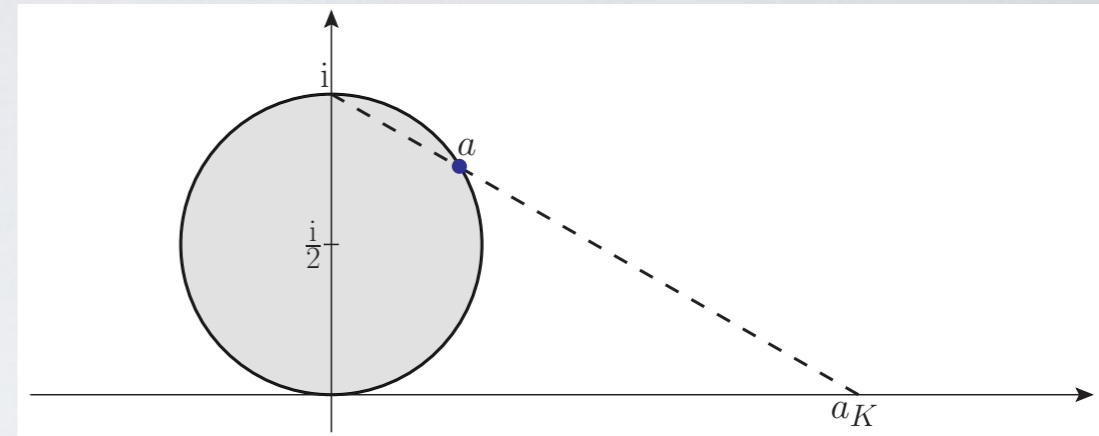
saturates the amplitude, usable for complex amplitudes, **no additional parameters**



Different unitarity projections

- **K-matrix:** Cayley transform of S-matrix Heitler, 1941; Schwinger, 1949; Gupta, 1950
- Stereographic projection to Argand circle

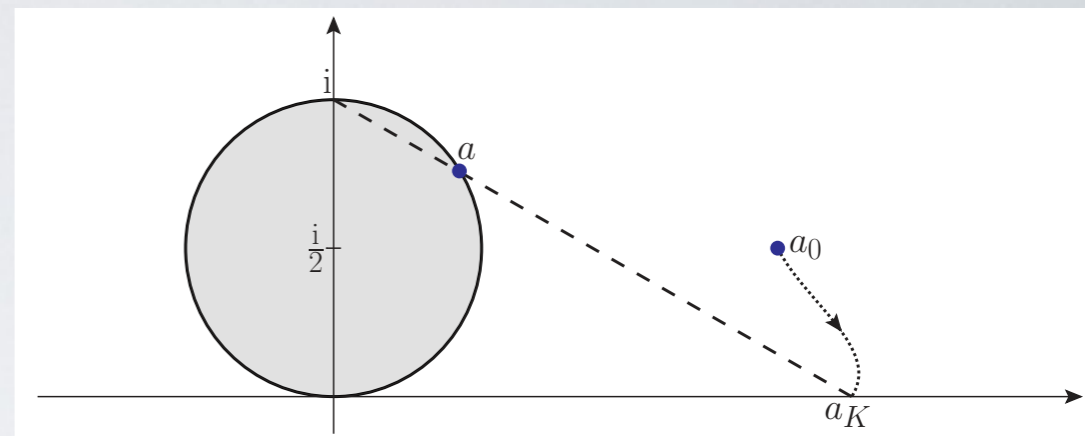
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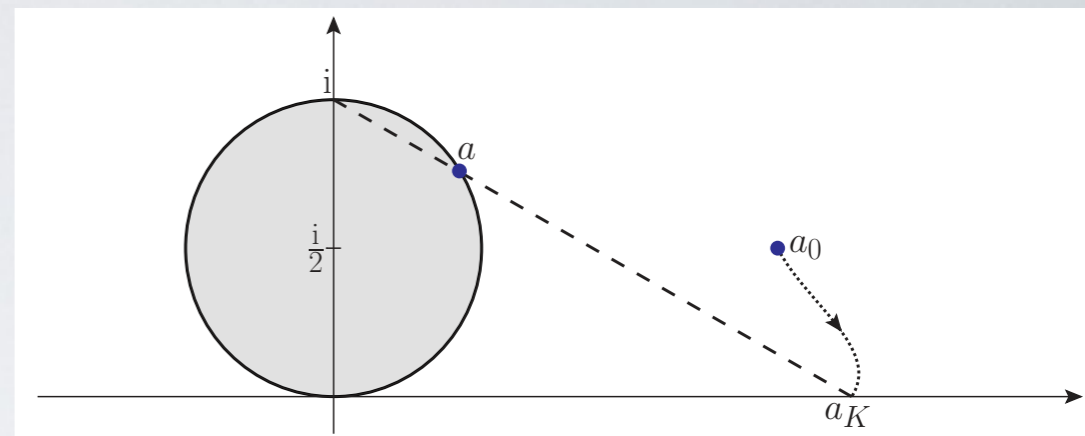
- Stereographic projection to Argand circle
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Problems, if S-matrix non-diagonal, presence of non-perturbative contrib.

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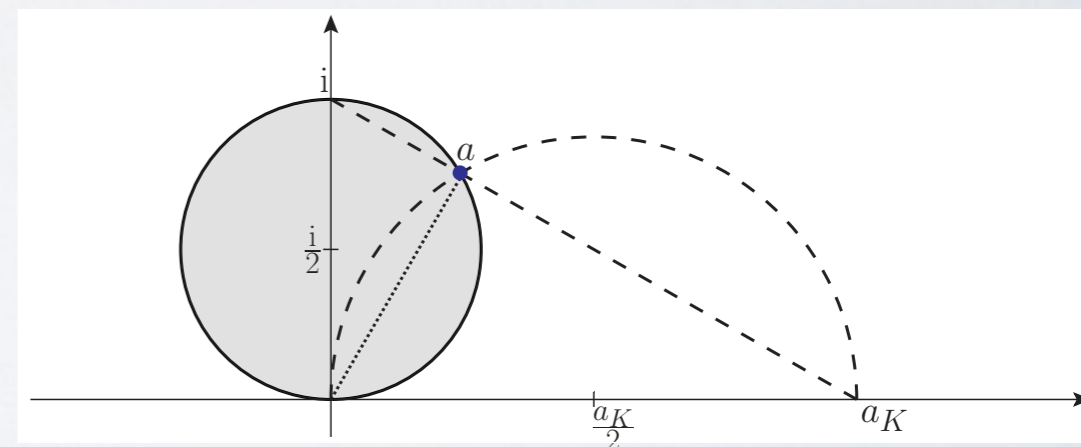
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Kilian/Ohl/JRR/Sekulla, 2014

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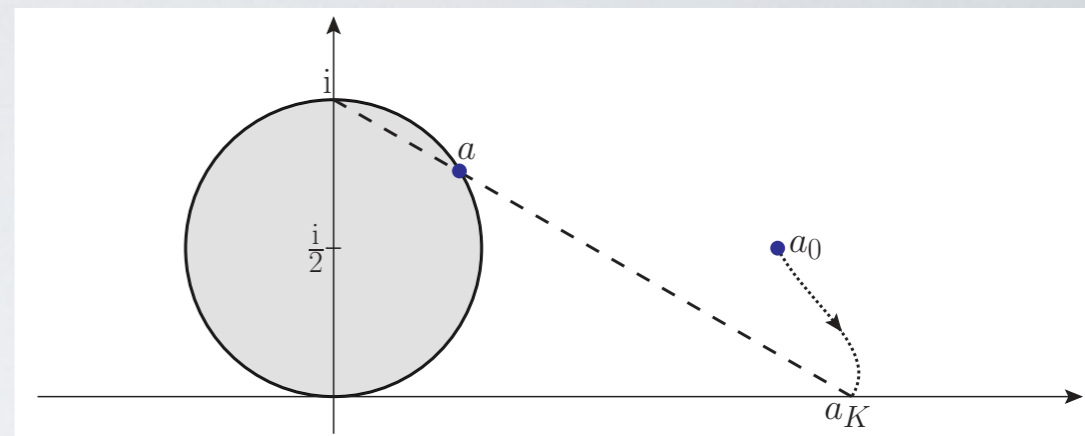


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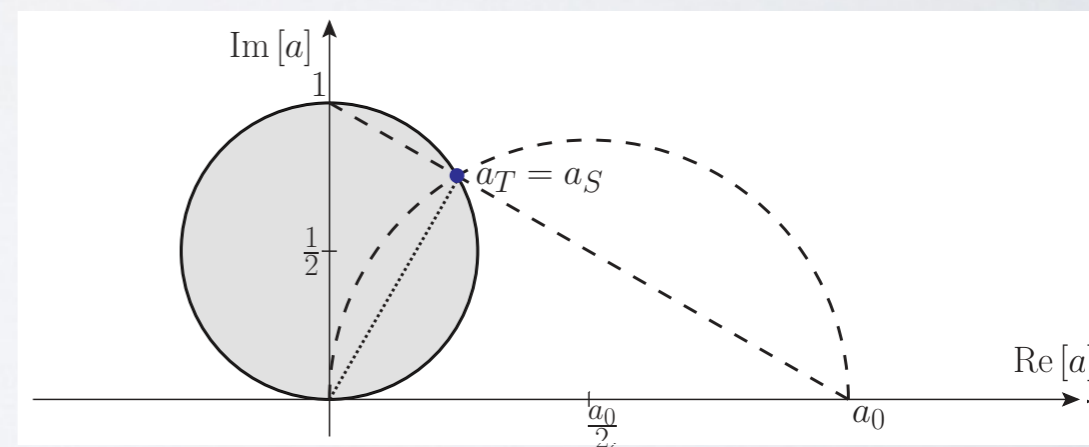
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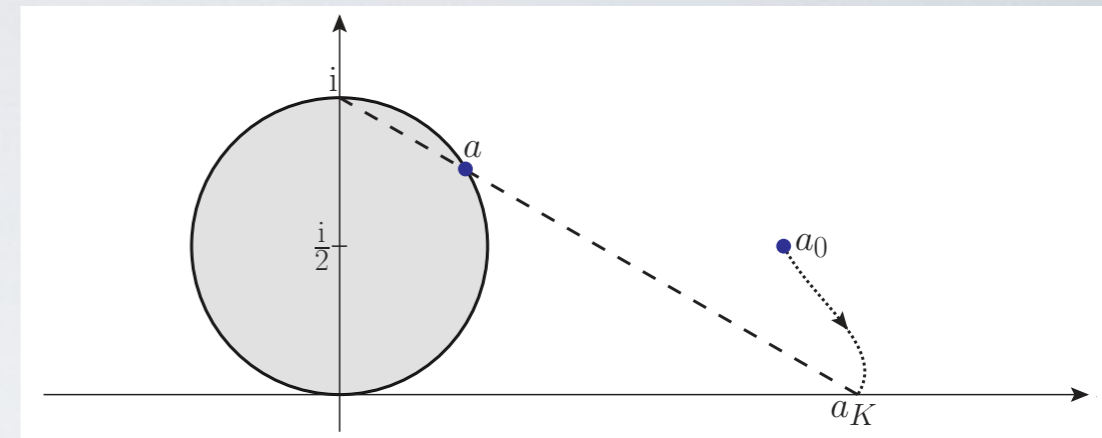
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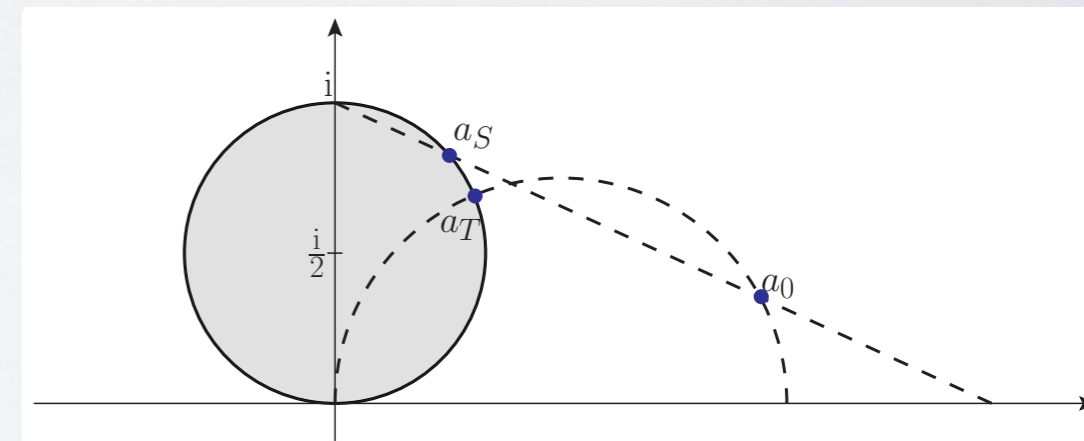
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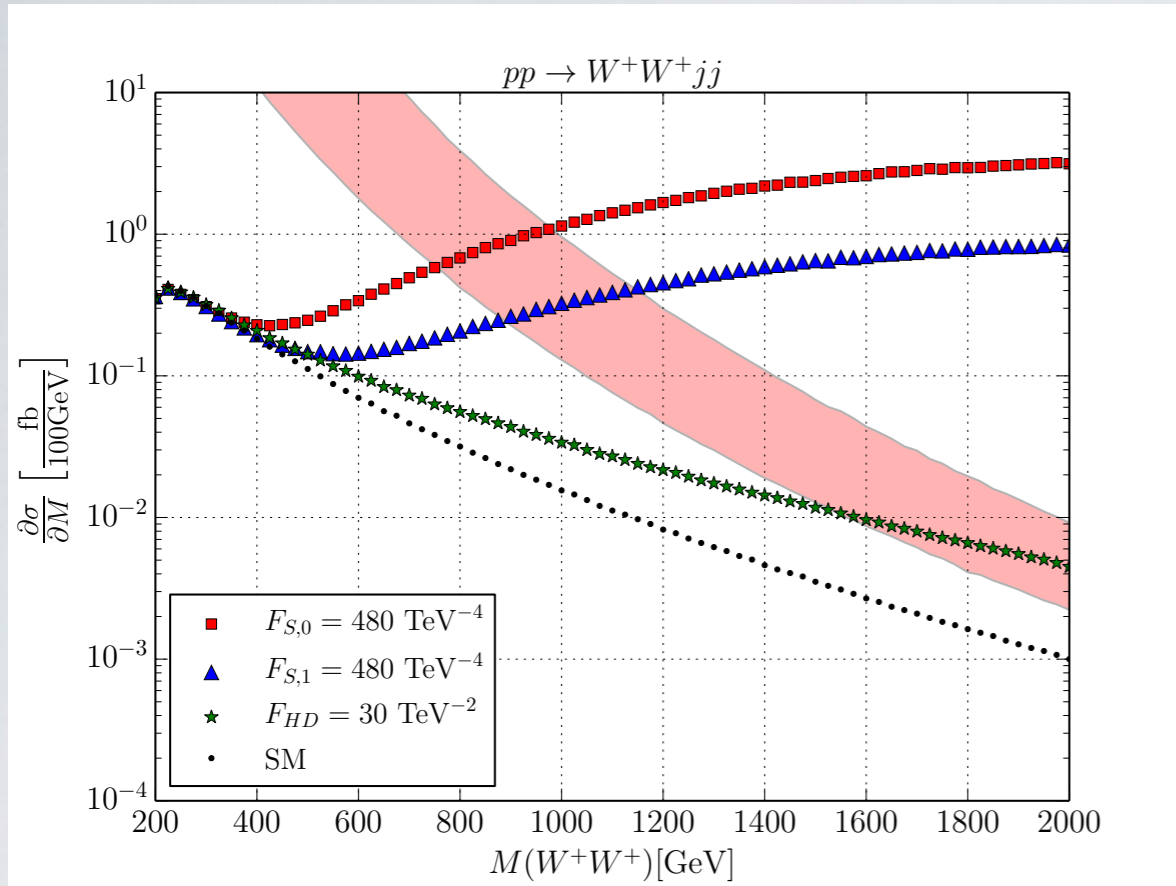
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VBS diboson spectra



$$\begin{aligned} \text{WWWW-Vertex: } \alpha_4 &= \frac{f_{S,0} v^4}{\Lambda^4 8} \\ \alpha_4 + 2 \cdot \alpha_5 &= \frac{f_{S,1} v^4}{\Lambda^4 8} \end{aligned}$$

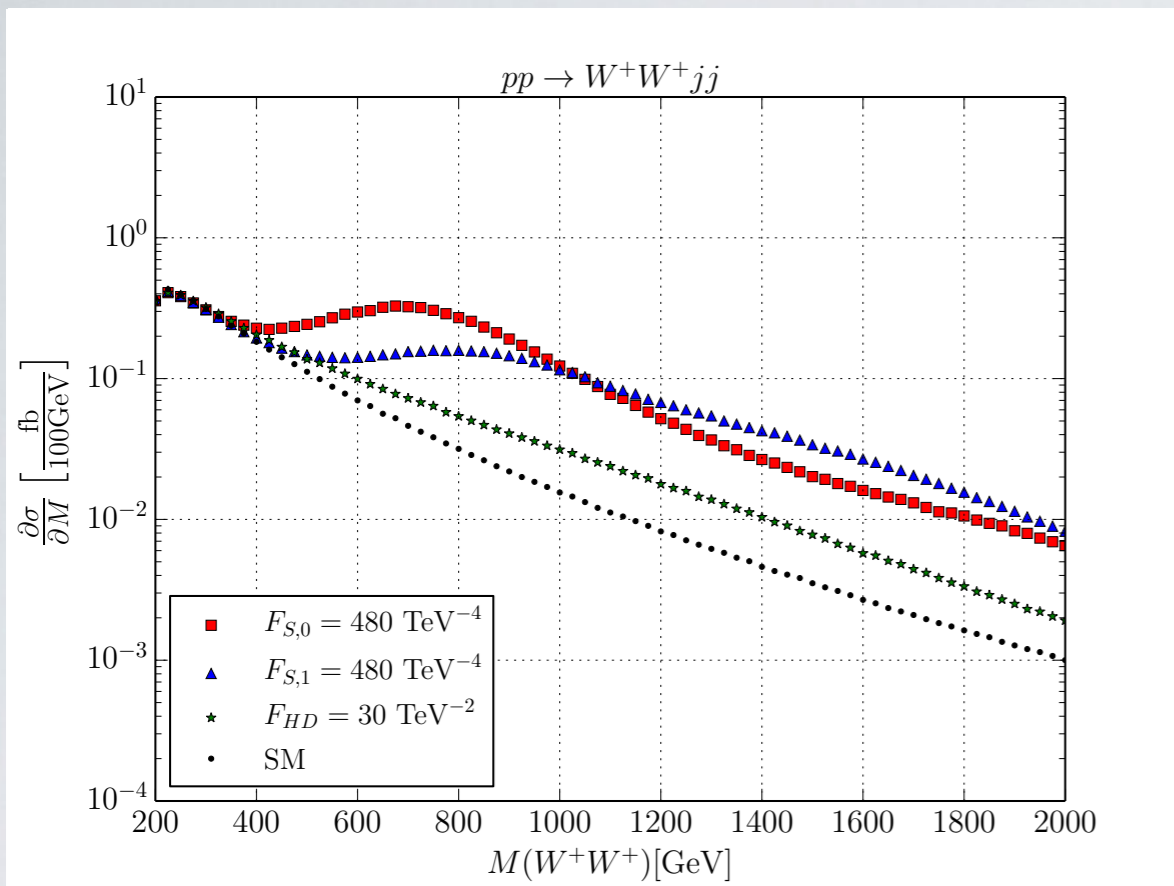
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$$\begin{aligned} \text{ZZZZ-Vertex:} \\ \alpha_4 + \alpha_5 &= \left(\frac{f_{S,0}}{\Lambda^4} + \frac{f_{S,1}}{\Lambda^4} \right) \frac{v^4}{16} \end{aligned}$$

General cuts: $M_{jj} > 500 \text{ GeV}$; $\Delta\eta_{jj} > 2.4$; $p_T^j > 20 \text{ GeV}$; $|\Delta\eta_j| < 4.5$



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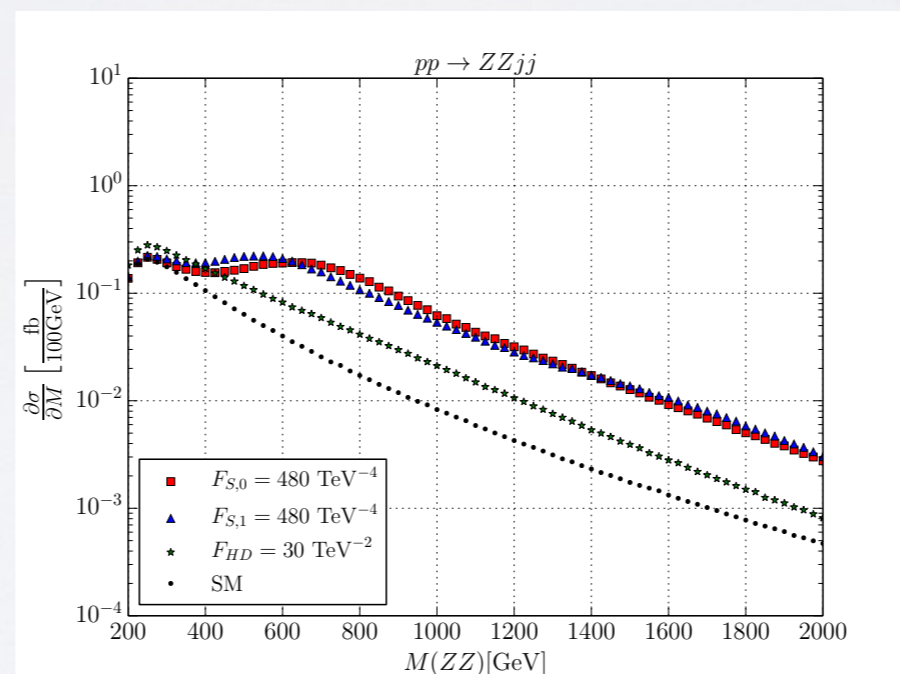
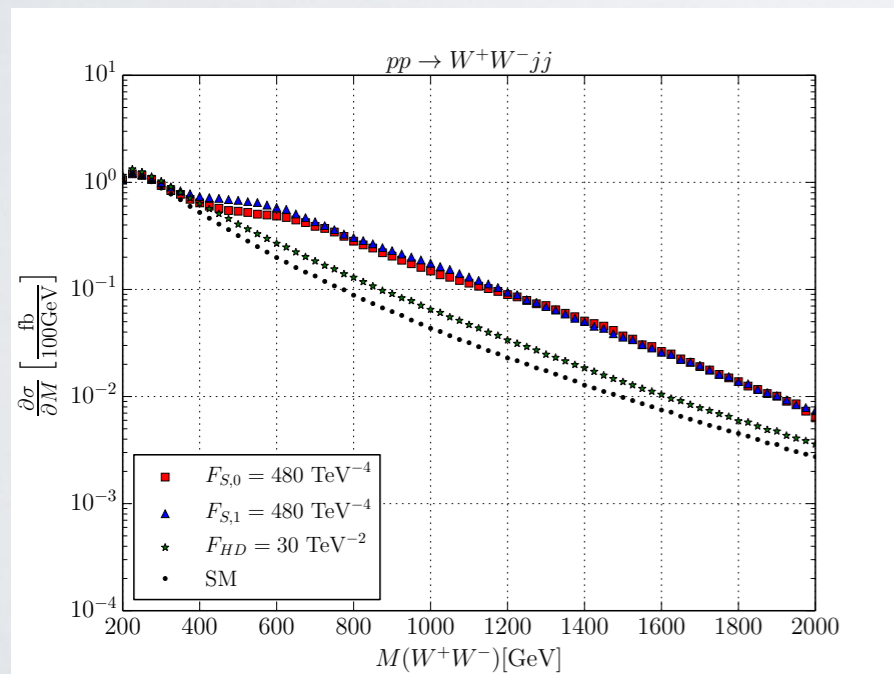
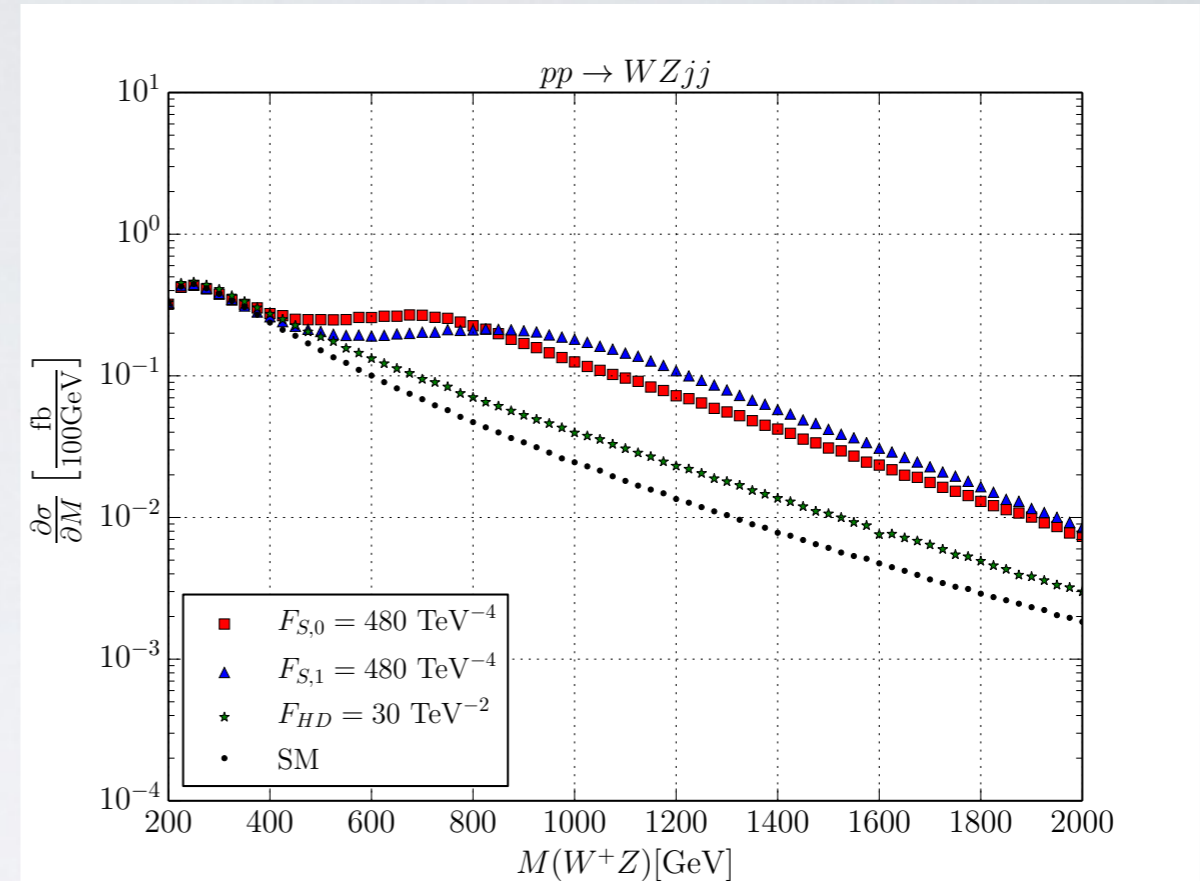
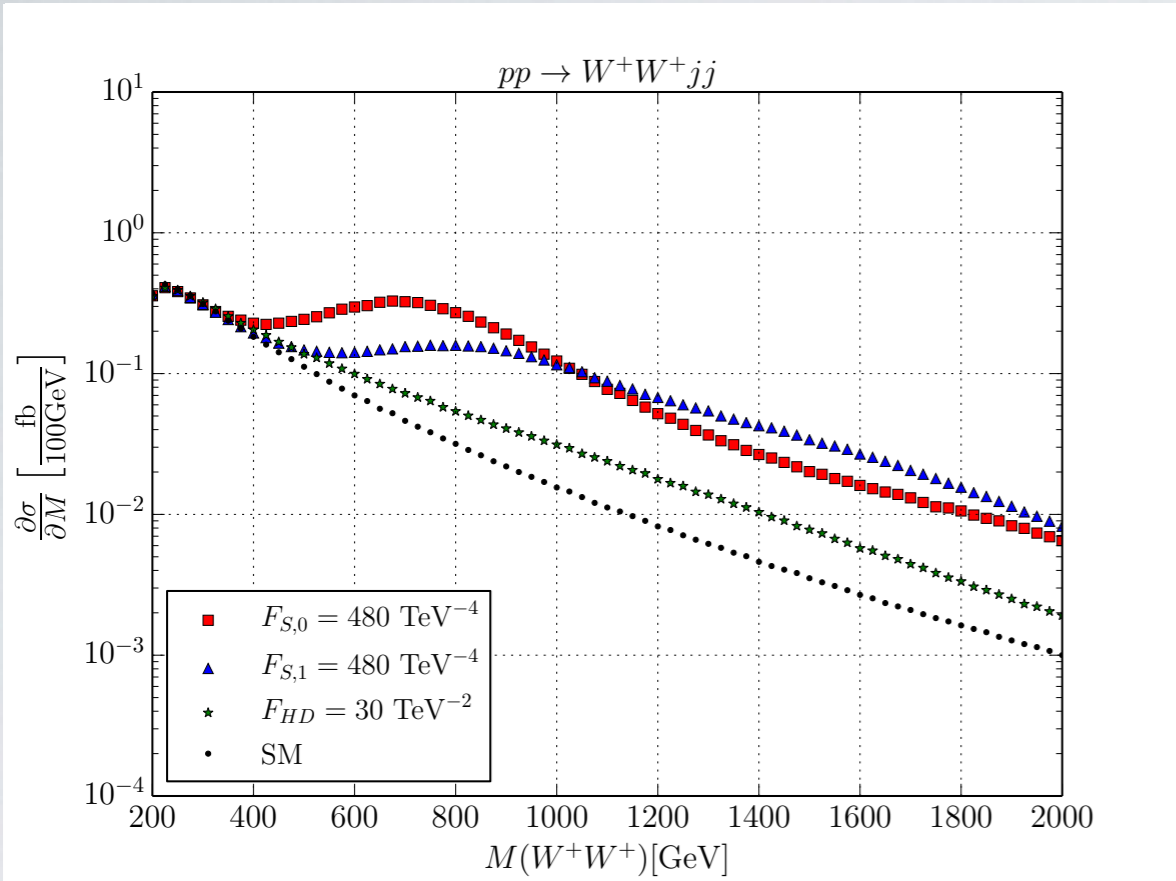
$$\begin{aligned} \text{WWZZ-Vertex: } \alpha_4 &= \frac{f_{S,0} v^4}{\Lambda^4 16} \\ \alpha_5 &= \frac{f_{S,1} v^4}{\Lambda^4 16} \end{aligned}$$

$$\text{ZZZZ-Vertex: } \alpha_4 + \alpha_5 = \left(\frac{f_{S,0}}{\Lambda^4} + \frac{f_{S,1}}{\Lambda^4} \right) \frac{v^4}{16}$$

General cuts: $M_{jj} > 500 \text{ GeV}$; $\Delta\eta_{jj} > 2.4$; $p_T^j > 20 \text{ GeV}$; $|\Delta\eta_j| < 4.5$



VBS diboson spectra



WWWW-Vertex: $\alpha_4 = \frac{f_{S,0} v^4}{\Lambda^4 8}$

$\alpha_4 + 2 \cdot \alpha_5 = \frac{f_{S,1} v^4}{\Lambda^4 8}$

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Differential spectra in VBS

$$pp \rightarrow e^+ \mu^+ \nu_e \nu_\mu jj \quad \sqrt{s} = 14 \text{ TeV} \quad \mathcal{L} = 1 \text{ ab}^{-1}$$

Simulations with WHIZARD [<http://whizard.hepforge.org>, Kilian/Ohl/JRR]



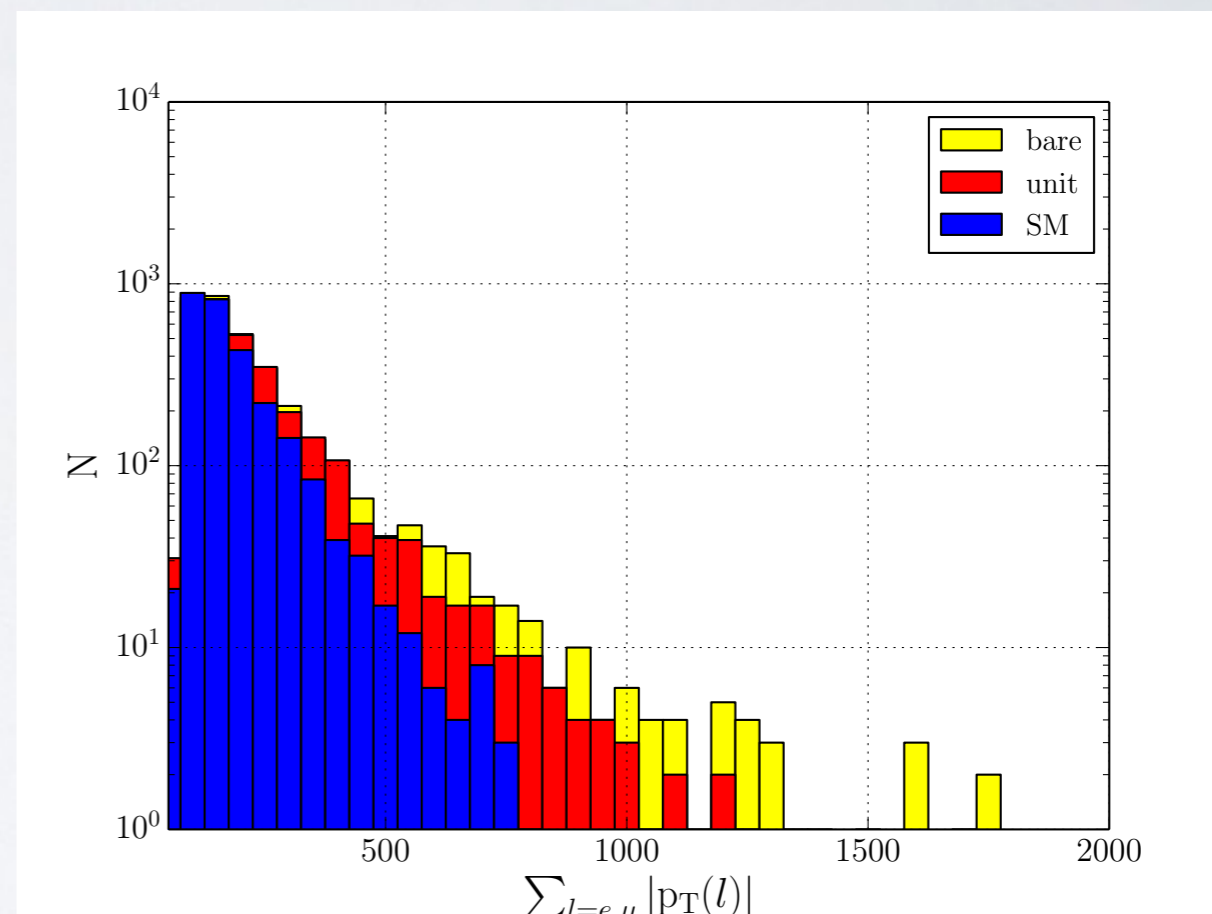
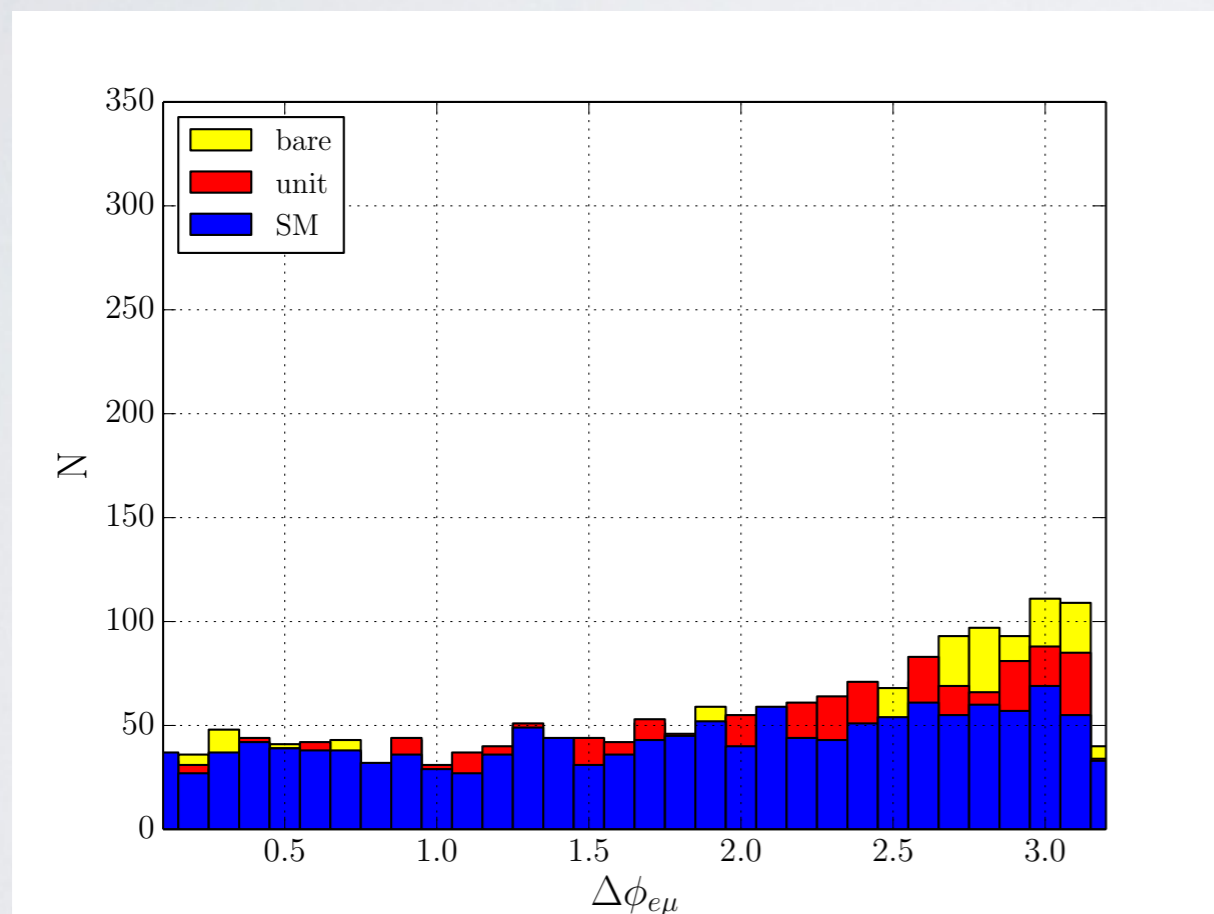
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$$F_{HD} = 30 \text{ TeV}^{-2}$$



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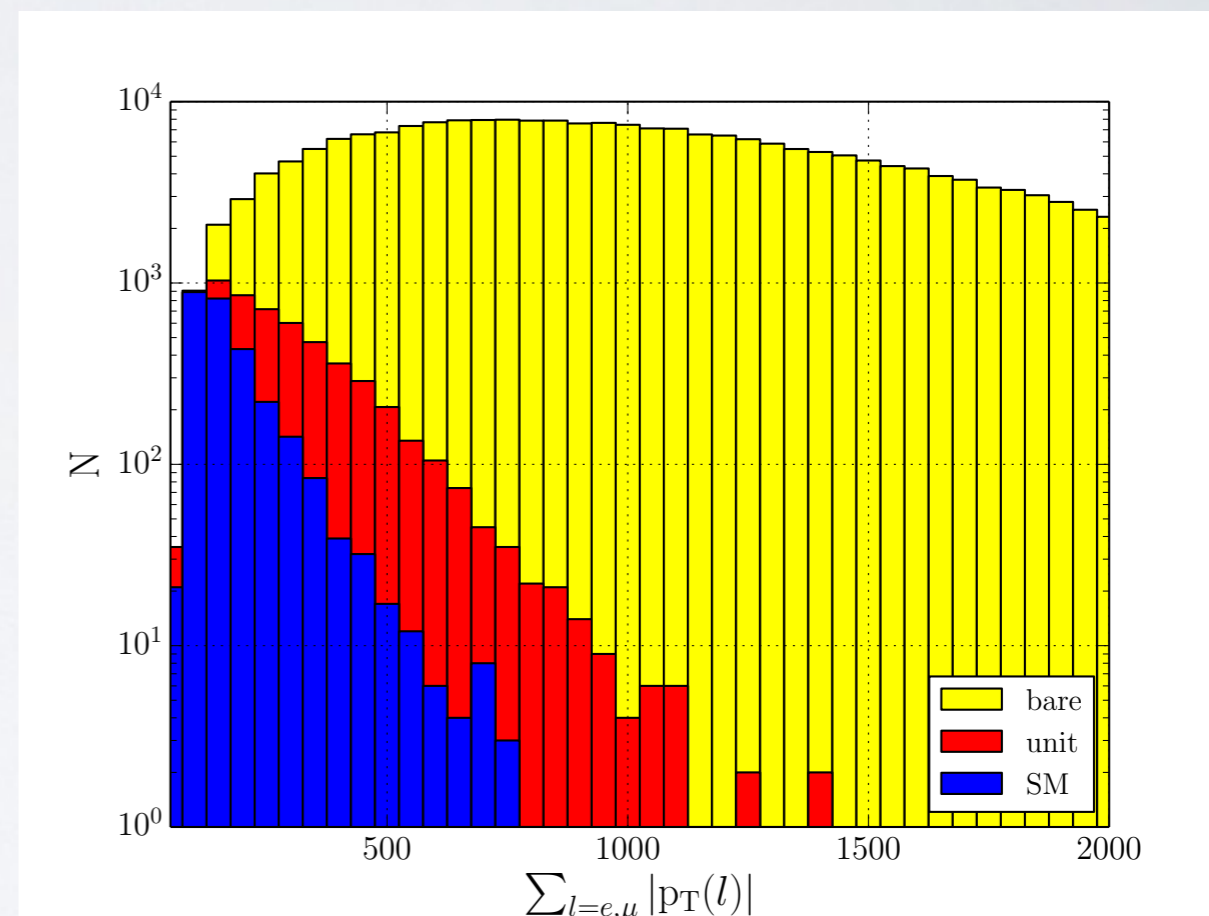
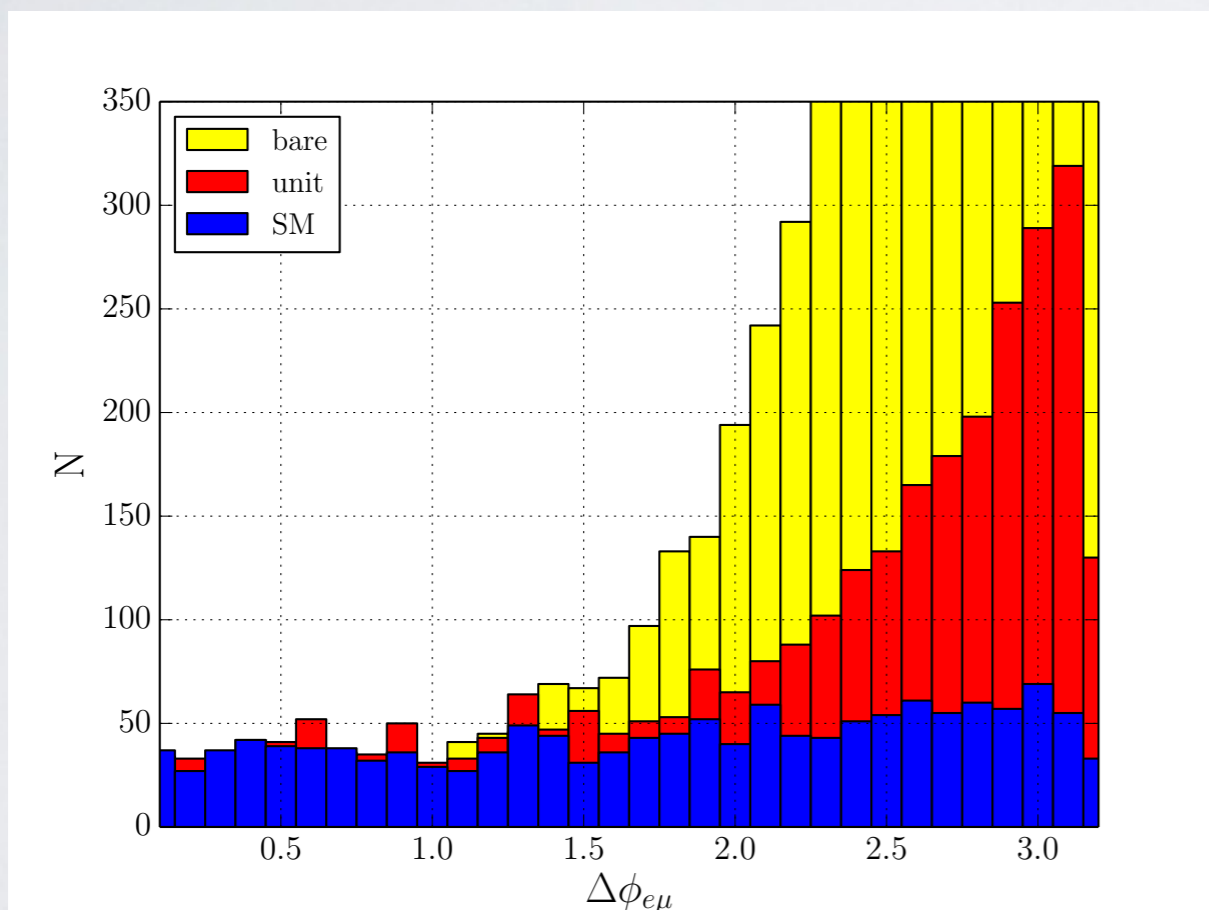


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$$F_{S,0} = 480 \text{ TeV}^{-4}$$



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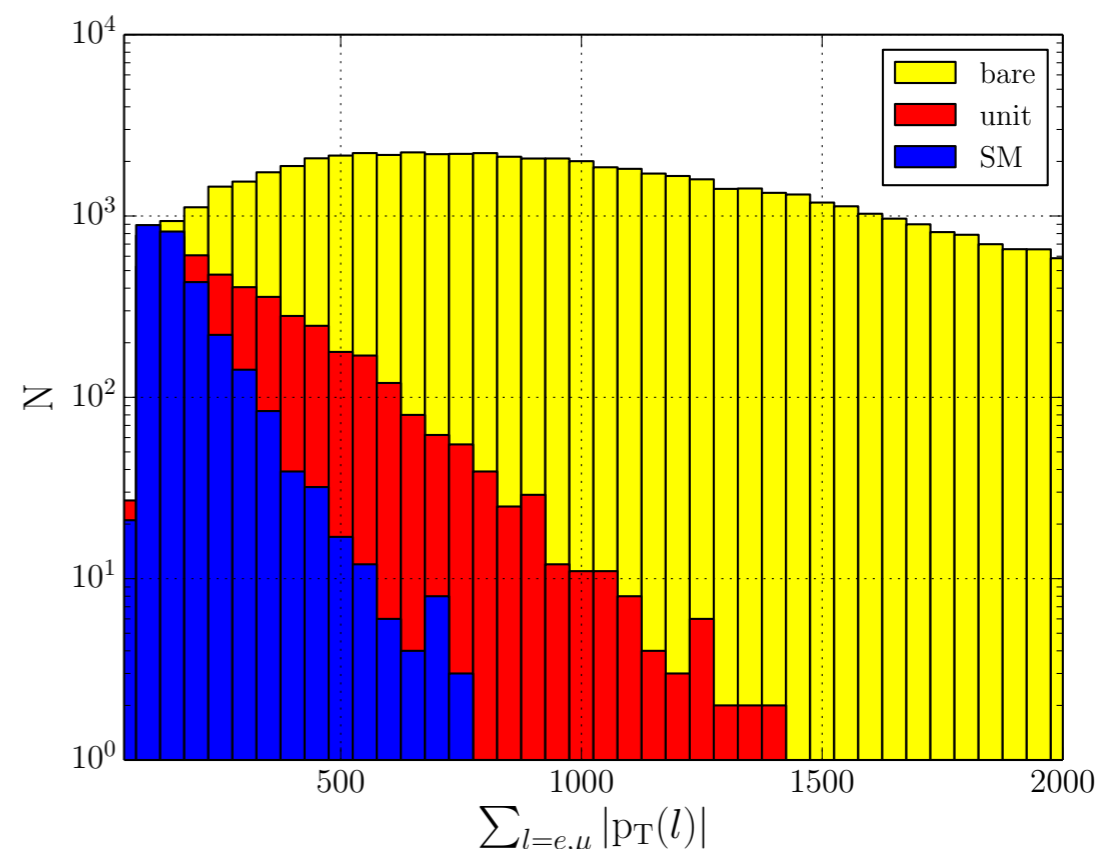
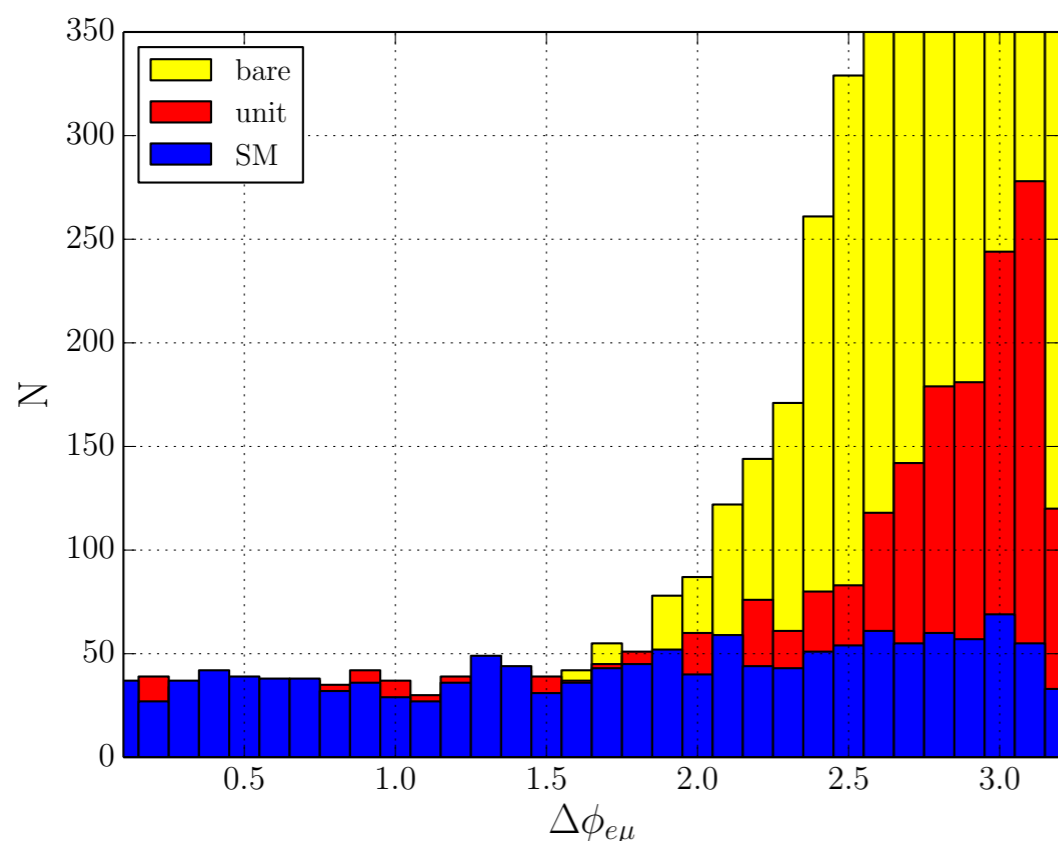


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$$F_{S,1} = 480 \text{ TeV}^{-4}$$



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Resonances: Quantum numbers & simplified models

- Rise of amplitude / anomalous coupling: Taylor expansion below a resonance
- Resonances might be in direct reach of LHC
- EFT framework EW-restored regime: $SU(2)_L \times SU(2)_R, SU(2)_L \times U(1)_Y$ gauged
- Include EFT operators in addition (more resonances, continuum contribution)
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	isoscalar	isotensor
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Tensor resonances

- Symmetric tensor $f_{\mu\nu}$
- On-shell conditions: 10 \rightarrow 5 components
- Tracelessness: $f_{\mu}^{\mu} = 0$
- Transversality: $\partial_{\mu} f^{\mu\nu} = 0$

How to deal with *off-shell* tensor in realistic processes?

Tensor resonances: Fierz-Pauli vs. Stückelberg

- Start with **Fierz-Pauli Lagrangian** for symmetric tensor

$$\begin{aligned}\mathcal{L}_{\text{FP}} = & \frac{1}{2} \partial_\alpha f_{\mu\nu} \partial^\alpha f^{\mu\nu} - \frac{1}{2} m^2 f_{\mu\nu} f^{\mu\nu} - \frac{1}{2} \partial_\alpha f^\mu{}_\mu \partial^\alpha f^\nu{}_\nu + \frac{1}{2} m^2 f^\mu{}_\mu f^\nu{}_\nu \\ & - \partial^\alpha f_{\alpha\mu} \partial_\beta f^{\beta\mu} - f^\alpha{}_\alpha \partial^\mu \partial^\nu f_{\mu\nu} + f_{\mu\nu} J_f^{\mu\nu}\end{aligned}$$

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- $f^{\mu\nu}$: on-shell $f^{\mu\nu}$
- ϕ : $\partial_\mu \partial_\nu f^{\mu\nu}$
- A^μ : $\partial_\nu f^{\mu\nu}$
- σ : $f^\mu{}_\mu$

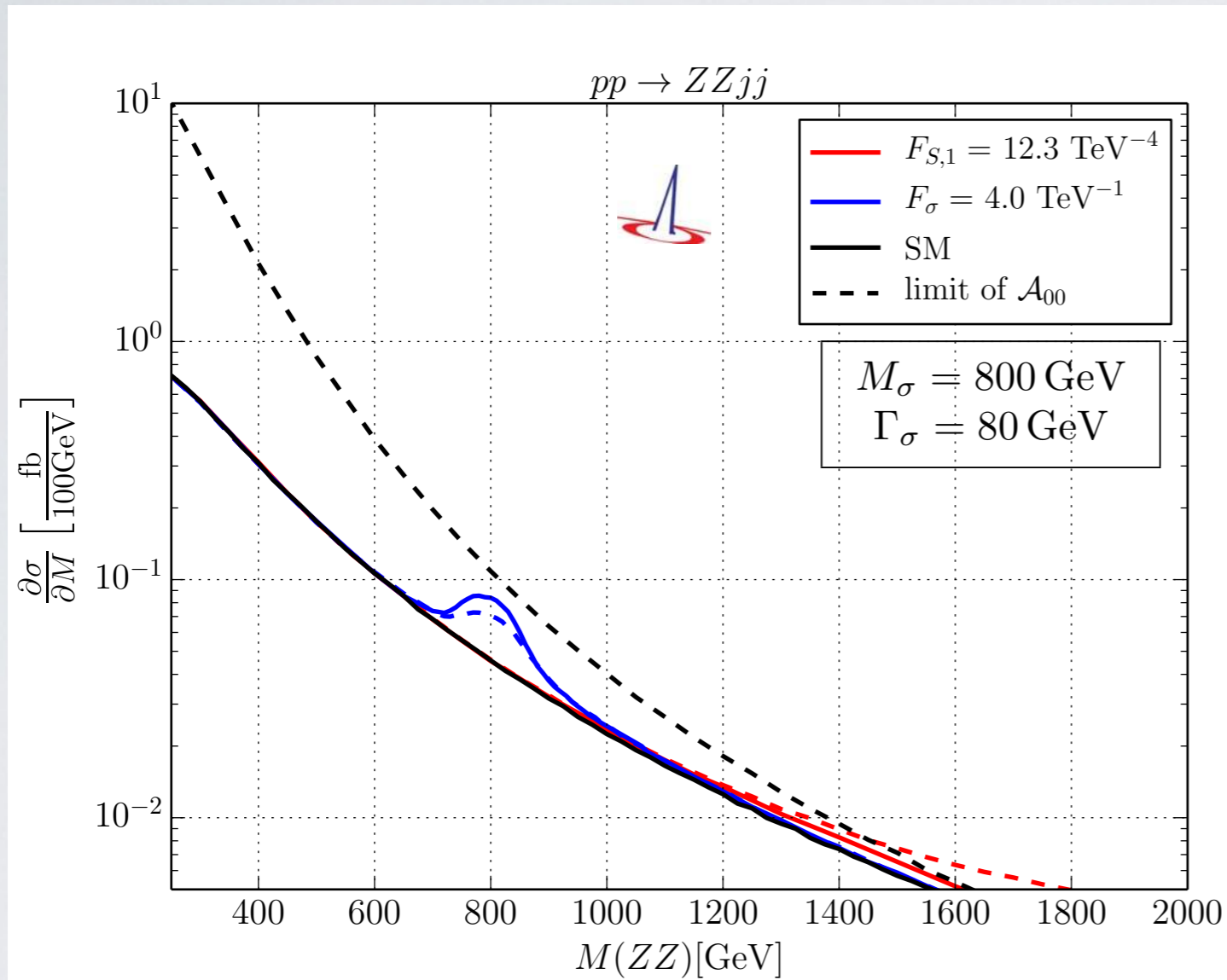
Gauge fixing: $\sigma = -\phi$

$$\begin{aligned} \mathcal{L} = & \frac{1}{2} f_{f\mu\nu} (-\partial^2 - m_f^2) f_f^{\mu\nu} + \frac{1}{2} f_{f\mu}^\mu \left(-\frac{1}{2} (-\partial^2 - m_f^2) \right) f_{f\nu}^\nu \\ & + \frac{1}{2} A_{f\mu} (\partial^2 + m_f^2) A_f^\mu + \frac{1}{2} \sigma_f (-\partial^2 - m_f^2) \sigma_f \\ & + \left(f_{\mu\nu} - \frac{1}{\sqrt{6}} \sigma_f g_{\mu\nu} \right) J_f^{\mu\nu} \\ & - \left(\frac{1}{\sqrt{2} m_f} (A_{f\mu} \partial_\nu + A_{f\nu} \partial_\mu) - \frac{\sqrt{2}}{\sqrt{3} m_f^2} \sigma_f \partial_\mu \partial_\nu \right) J_f^{\mu\nu} \end{aligned}$$

Comparison: Simplified Models & EFT

Kilian/Ohl/JRR/Sekulla: PRD93(16),3. 036004 [1511.00022]

Black dashed line:
saturation of $\mathcal{A}_{22}(W^+W^+)/\mathcal{A}_{00}(ZZ)$



- EFT fails at resonance
- aQGC describe rise of resonance
- Unitarization applied
- Tensor resonances better visible than scalars

$$32\pi\Gamma/M^5$$

	σ	ϕ	f	X
$F_{S,0}$	$\frac{1}{2}$	2	15	5
$F_{S,1}$	—	$-\frac{1}{2}$	-5	-35

$$M_{jj} > 500 \text{ GeV}; \Delta\eta_{jj} > 2.4; p_T^j > 20 \text{ GeV}; |\Delta\eta_j| < 4.5$$

$$|F_{S,0}| < 480 \text{ TeV}^{-4} \quad |F_{S,1}| < 480 \text{ TeV}^{-4}$$

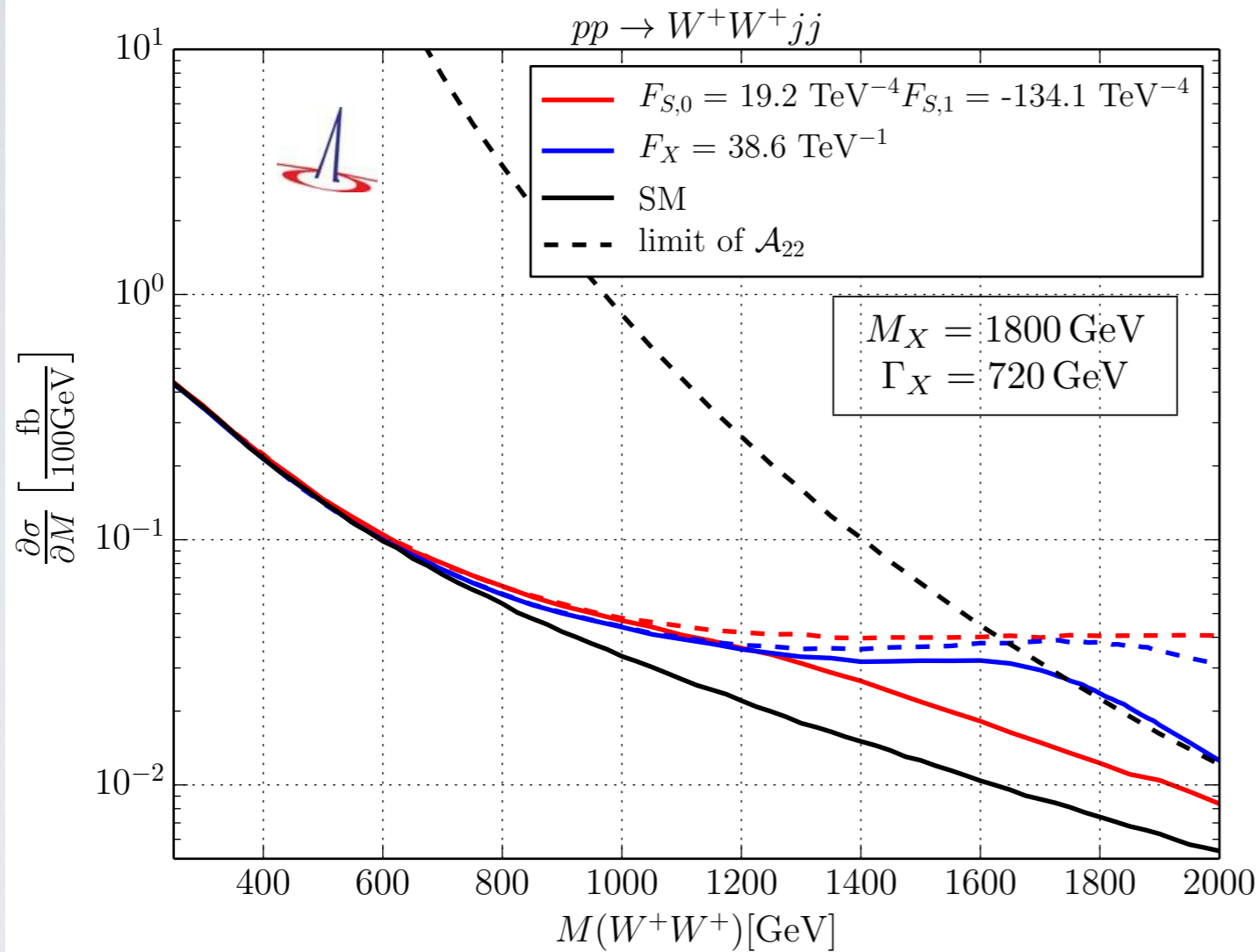
ATLAS PRL 113(2014)14, 141803 [1405.6241]



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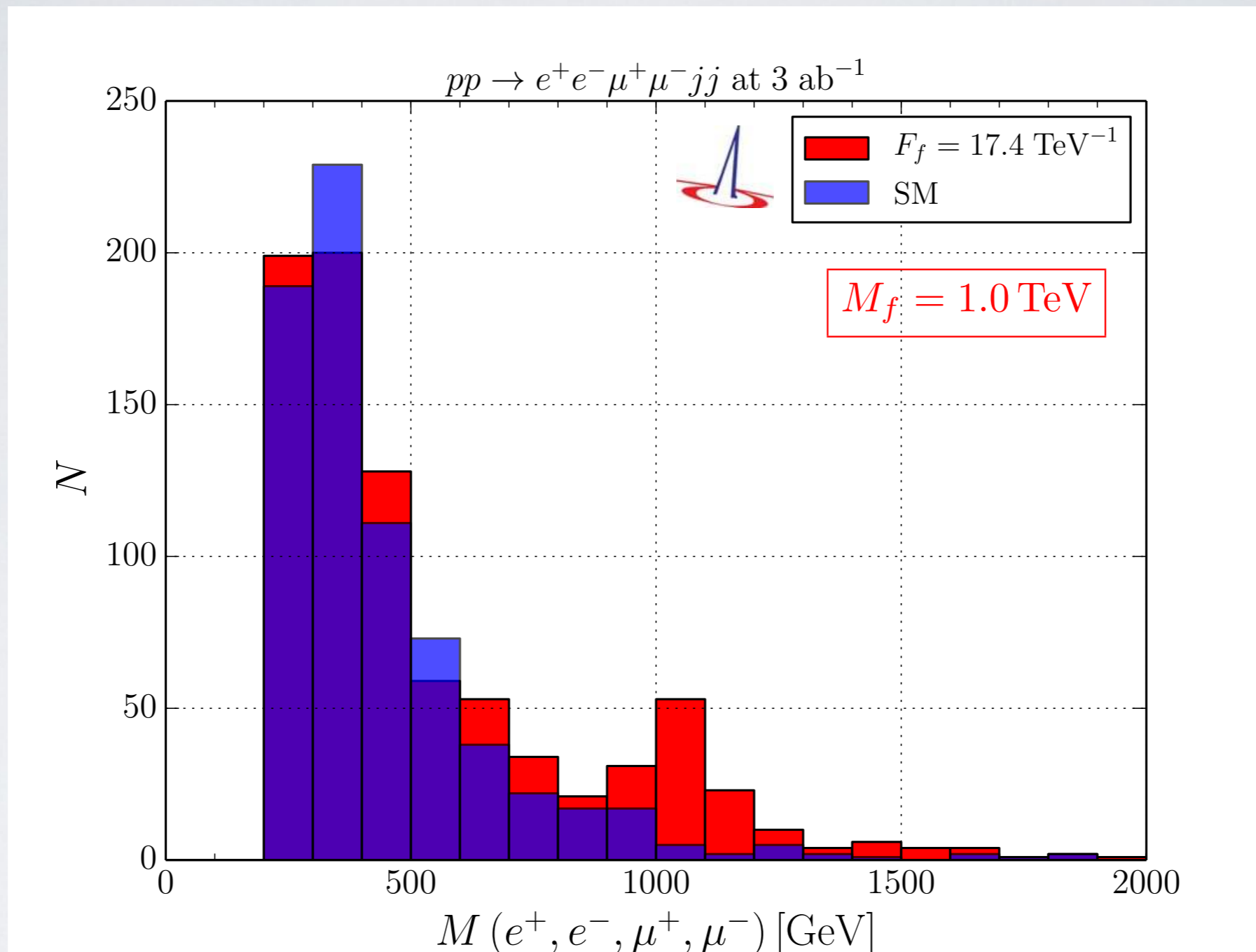
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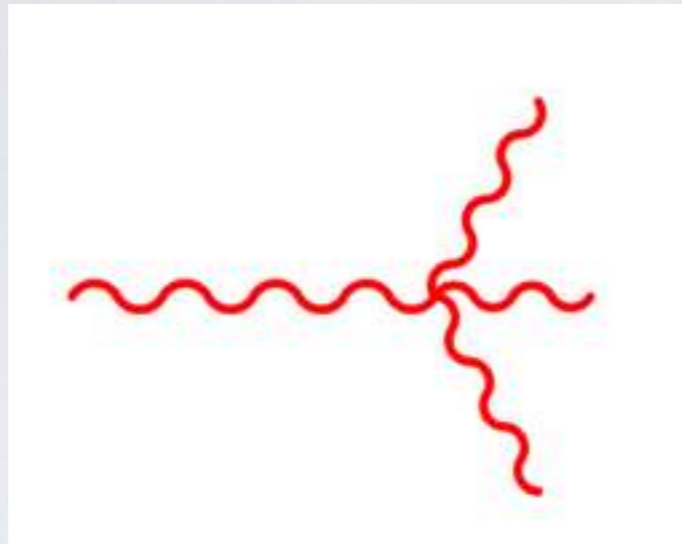


Complete LHC process at 14 TeV

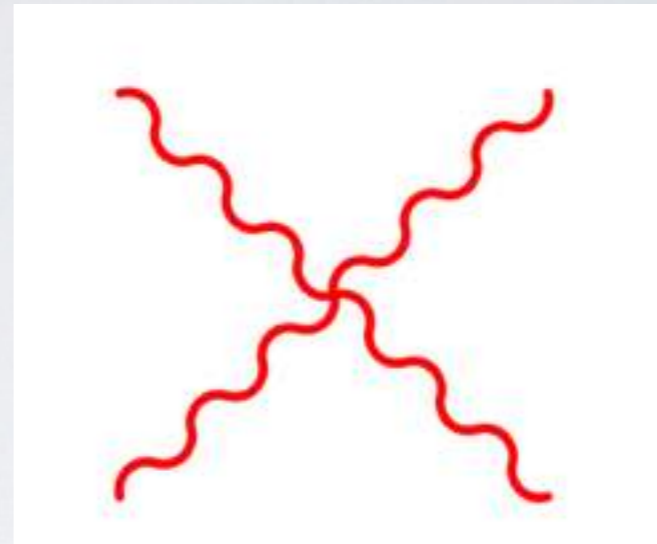


Triple [multiple] Vector Boson Production ?

Relate



to



?

- ▶ Yes, same Feynman rule as in VBS, but ...
- ▶ one external $W/Z/\gamma$ always far off-shell
- ▶ Unitarization formalism not available (would need $2 \rightarrow 3$ unitarizations)
- ▶ Different Wilson coefficients dominate (particularly for resonances)
- ▶ Important physics (partially) independent from VBS

Conclusions / Summary

- ◆ Vector boson scattering one of flagship measurements of Runs II/III
- ◆ EFT provides *a* (!) [not *the*] consistent framework for SM deviations
- ◆ Very well-defined (and limited) range of applicability
- ◆ Accounts for access to New Physics in VBS and Di-/Triboson channels
- ◆ Unitarization for theoretically sane description (allows to calculate 'best limit')
- ◆ *T*-matrix unitarization universal scheme for EFT and resonances
- ◆ Simplified models: generic electroweak resonances
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- ◆ Make sure that actual limits are meaningful and comparable



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ILC 1 TeV, 1/ab expectations:

LHC 13/14 TeV, 0.3-3/ab

Spin	$I = 0$	$I = 1$	$I = 2$
0	1.55	—	1.95
1	—	2.49	—
2	3.29	—	4.30

Spin	$I = 0$	$I = 1$	$I = 2$
0	1.39	1.55	1.95
1	1.74	2.67	—
2	3.00	3.01	5.84



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light Higgs: also needs to be updated

ca. 1-3 TeV
[very preliminary]



whatever approach



whatever approach ... always get the correct ellipses



BACKUP SLIDES



Effective Field Theory (EFT) for Weak Interactions

- * SpS: discovery of W, Z (on-shell)
- * SLC/LEP: proof of non-Abelian weak structure, **failure to find (very) light Higgs**
- * **Measurement of longitudinal W s:** $ee \rightarrow WW$ (LEP), $t \rightarrow Wb$ (Tevatron)
- * Using all known d.o.f., **parameterizing all possible interactions**

Building blocks for EFT:

$$\psi \quad , \quad \mathbf{W}_\mu \quad , \quad \mathbf{B}_\mu \quad , \quad \Sigma = \exp \left[\frac{-i}{v} \mathbf{w} \boldsymbol{\tau} \right]$$

SM fermions weak bosons hypercharge boson longitudinal d.o.f.

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Minimal Lagrangian describing measurements at SLC / LEP [II] / Tevatron

$$\mathcal{L}_{\text{pre-LHC}} = \sum_{\psi} \bar{\psi} (i \not{D}) \psi - \frac{1}{2g^2} \text{tr} [\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu}] - \frac{1}{2g'^2} \text{tr} [\mathbf{B}_{\mu\nu} \mathbf{B}^{\mu\nu}] + \frac{v^2}{4} \text{tr} [(\mathbf{D}_\mu \Sigma)(\mathbf{D}^\mu \Sigma)]$$

with the following useful definitions:

$$\mathbf{D}_\mu = \partial_\mu + \frac{i}{2} g \boldsymbol{\tau}^I \mathbf{W}_\mu^I + \frac{i}{2} g' B_\mu \boldsymbol{\tau}^3$$

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Electroweak Chiral Lagrangian

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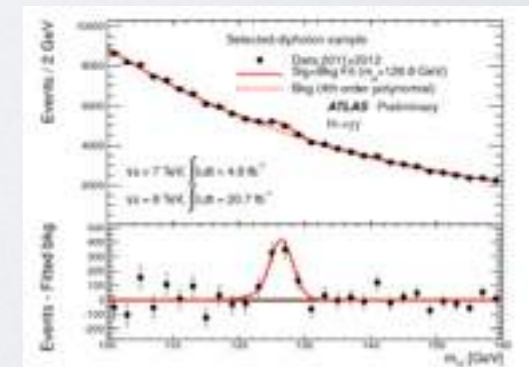
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Electroweak Chiral Lagrangian

Ruled out by LHC data (Higgs discovery)



Parameterizing SM deviations

★ Specific models (SUSY, Compositeness, Little Higgses, 2HDM, Modified Higgses, Xdim,

- Could give strong signals in VBS (presumably Little Higgses, Compositeness, Xdim)
- Could give faint signals in VBS (presumably SUSY, 2HDM [Higgs data!],)
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★ Effective Field Theory

- (Almost) model-independent, consistent calculation of perturbative corrections (power counting !?)
- Depends on (possibly) many free parameters
- Requires decoupling of New Physics
- Range of applicability strongly depends on couplings and scales (unitarity issue)



General Procedure using EFTs

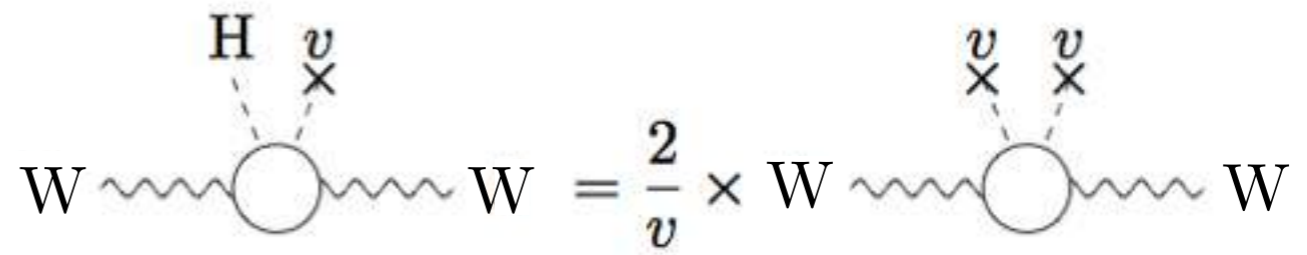
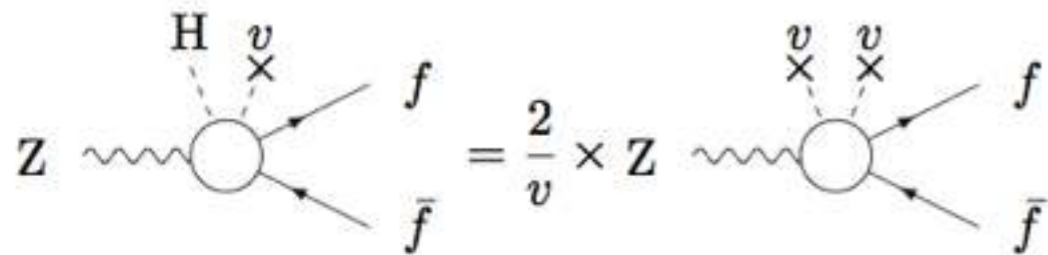
- Use all experimental observables \implies global fit to all Wilson coefficients
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- Too many independent variables \implies needs staged fitting
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- Try to find minimal “physically well motivated” operator basis
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Effects in $H \rightarrow Zff$ related to
 $Z \rightarrow ff \implies$ constrained by SLC/LEP

visible in Higgs
 physics: $H \rightarrow WW$

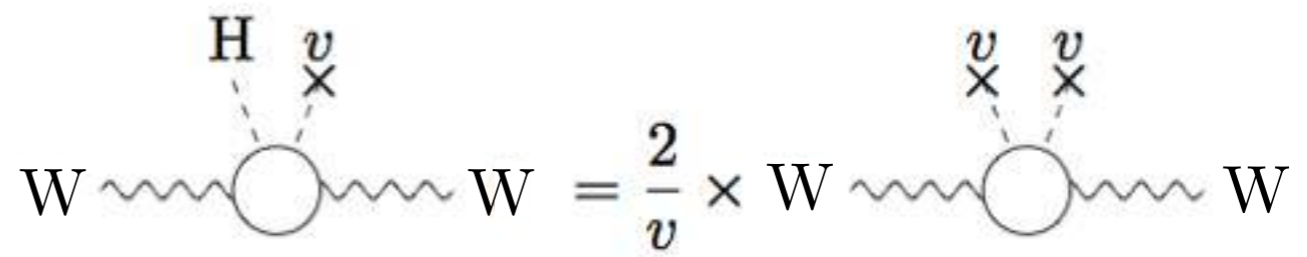
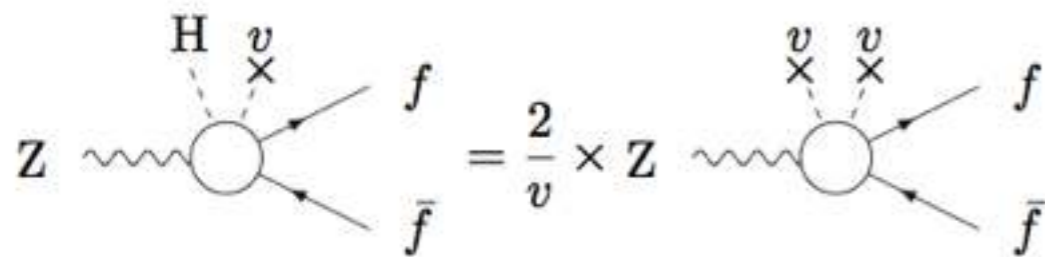
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- Often use vev-subtracted operators: $\mathcal{O}(\Phi^\dagger \Phi) \longrightarrow \mathcal{O}'(\Phi^\dagger \Phi - v^2)$
- EFT allows to systemically calculate higher-order corrections

How to get EFTs from New Physics

- ✦ Consider effects from heavy states by using (known) low-energy d.o.f.s

In addition to being a great convenience, effective field theory allows us to ask all the really scientific questions that we want to ask without committing ourselves to a picture of what happens at arbitrarily high energy.

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- ◆ Toy Example: two interacting scalar fields φ, Φ

Path integral

$$\mathcal{Z}[j, J] = \int \mathcal{D}[\Phi] \mathcal{D}[\varphi] \exp \left[i \int dx \left(\frac{1}{2} (\partial\varphi)^2 - \frac{1}{2} \Phi (\square + M^2) \Phi - \lambda \varphi^2 \Phi - \dots + J \Phi + j \varphi \right) \right]$$

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$$\Phi' = \Phi + \frac{\lambda}{M^2} \left(1 + \frac{\partial^2}{M^2} \right)^{-1} \varphi^2 \quad \Rightarrow \quad \text{Diagrammatic representation}$$

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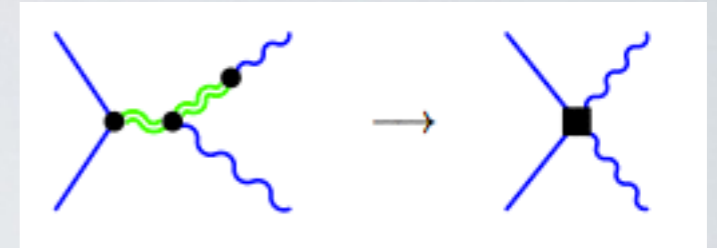
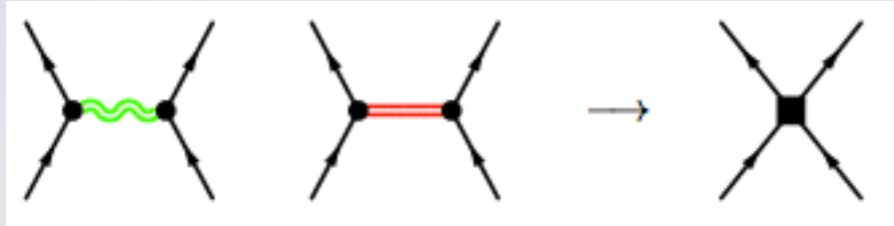
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In the Lagrangian remove the high-scale d.o.f.s:

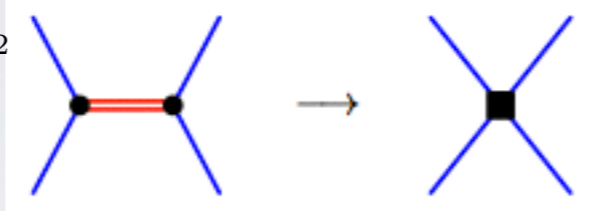
$$\frac{1}{2} (\partial\Phi)^2 - \frac{1}{2} M^2 \Phi^2 - \lambda \varphi^2 \Phi = \underbrace{-\frac{1}{2} \Phi' (M^2 + \partial^2) \Phi'}_{\text{Irrelevant normalization of the path integral}} + \underbrace{\frac{\lambda^2}{2M^2} \varphi^2 \left(1 + \frac{\partial^2}{M^2} \right)^{-1} \varphi^2}_{\text{Tower of higher and higher-dim. operators of light fields}}$$

Generation of Higher-dimensional Operators

$$\mathcal{O}_{JJ}^{(I)} = \frac{1}{\Lambda^2} \text{tr} [J^{(I)} \cdot J^{(I)}]$$



$$\mathcal{O}'_{\Phi,1} = \frac{1}{\Lambda^2} ((D\Phi)^\dagger \Phi) \cdot (\Phi^\dagger (D\Phi)) - \frac{v^2}{2} |D\Phi|^2$$



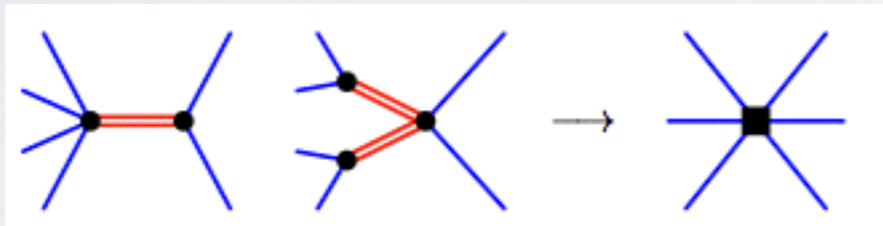
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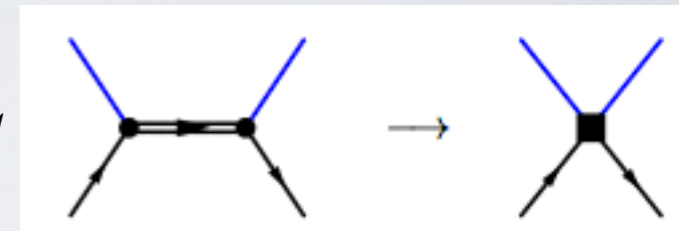
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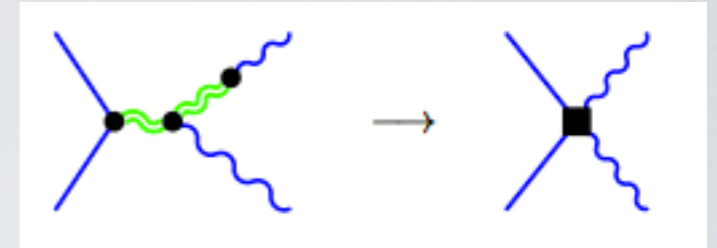
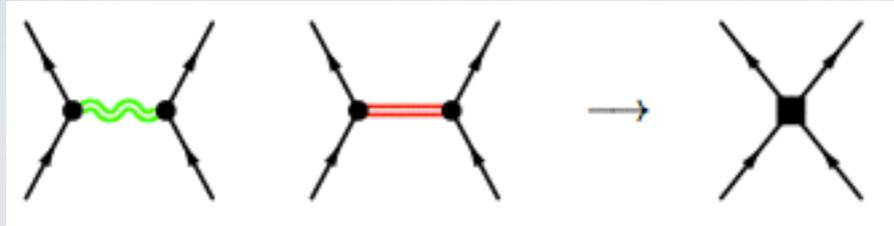


Couplings of new states to the longitudinal / transversal diboson system

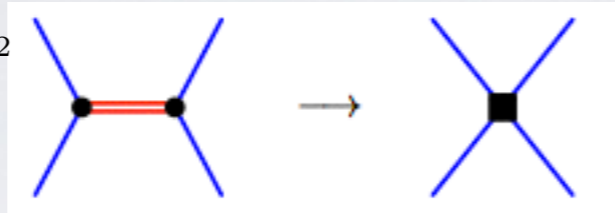
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$I = 0$	σ^0 (Higgs singlet?)	ω^0 (γ'/Z' ?)	f^0 (Graviton ?)
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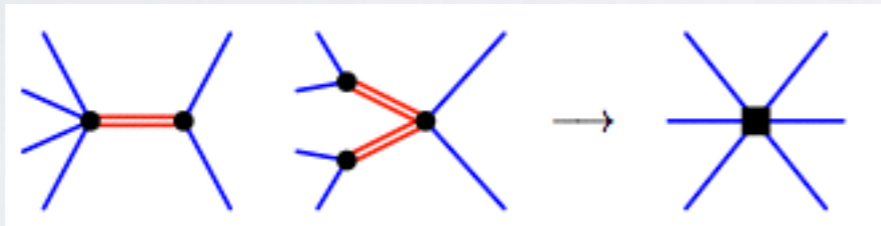
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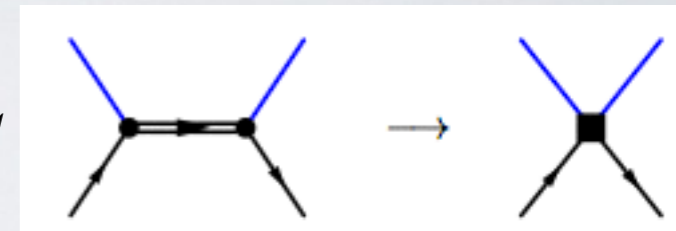
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Different power counting for weakly and strongly interacting theories

$$\frac{c_i}{\Lambda} \sim \frac{g}{4\pi\Lambda} \quad \text{vs.} \quad \frac{c_i}{\Lambda} \sim \frac{g}{\Lambda}$$

