

# White dwarf and subdwarf stars in the Sloan Digital Sky Survey Data Release 14

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## ABSTRACT

White dwarfs carry information on the structure and evolution of the Galaxy, especially through their luminosity function and initial-to-final mass relation. Very cool white dwarfs provide insight into the early ages of each population. Examining the spectra of all stars with  $3\sigma$  proper motion in the Sloan Digital Sky Survey Data Release 14, we report the classification for 20 088 spectroscopically confirmed white dwarfs, plus 415 hot subdwarfs, and 311 cataclysmic variables. We obtain  $T_{\text{eff}}$ ,  $\log g$  and mass for hydrogen atmosphere white dwarf stars (DAs), warm helium atmosphere white dwarfs (DBs), hot subdwarfs (sdBs and sdOs), and estimate photometric  $T_{\text{eff}}$  for white dwarf stars with continuum spectra (DCs). We find 15 793 sdAs and 447 dCs between the white dwarf cooling sequence and the main sequence, especially below  $T_{\text{eff}} \approx 10\,000$  K; most are likely low-mass metal-poor main sequence stars, but some could be the result of interacting binary evolution.

**Key words:** white dwarfs – subdwarfs – catalogues

## 1 INTRODUCTION

White dwarf stars are the end state for all stars formed with initial masses below around  $7\text{--}11.8 M_{\odot}$ , depending on metallicity (e.g. Ibeling & Heger 2013; Doherty et al. 2015; Woosley & Heger 2015; Lauffer et al. 2018), which translates to more than 97% of all stars. Therefore the properties of the white dwarf population reflect the result of the initial mass function, the star formation rate and the initial-to-final mass relation, for different metallicities. White dwarf stars are also possible outcomes of the evolution of multiple systems, with 25–30 per cent of white dwarfs estimated to be the result of mergers (Toonen et al. 2017). White dwarfs with masses lower than  $0.3\text{--}0.45 M_{\odot}$  are generally explained as outcomes of close binary evolution (Kilic, Stanek & Pinsonneault 2007), given that the single progenitors of such low-mass white dwarfs have main sequence lifetimes exceeding the age of the Universe. The formation mechanism of the so-called extremely-low mass white dwarfs (ELMs) – those with masses below  $\approx 0.2\text{--}0.3 M_{\odot}$  (e.g. Sun & Arras 2018; Cal-

caferro, Althaus, & Córscico 2018, and references therein) – is similar to that proposed to explain composite hot subdwarf stars (e.g. Heber 2016): the outer envelope is lost after a common envelope or a stable Roche-lobe overflow phase, leaving the stellar core exposed (e.g. Li et al. 2019). Hot subdwarfs result when the envelope is lost after He-burning is triggered in the core – hence they lie above the zero-age horizontal branch, whereas an ELM will result if the mass is lost when the core He is in a degenerate state, but He fusion has not been triggered. ELMs show similar  $\log g$  to subdwarfs, but generally lower temperature ( $T_{\text{eff}} \lesssim 20\,000$  K).

White dwarfs do not present ongoing core nuclear burning, but residual shell burning may occur depending on the thickness of the hydrogen layer. ELMs are believed to show residual burning before reaching the final white dwarf cooling track (Córscico et al. 2012; Istrate et al. 2016). This happens in the pre-ELM phase (Maxted et al. 2014a,b), which can cause them to show luminosities comparable to main sequence and even horizontal branch stars (e.g. Pietrzyński et al. 2012).

Because the timescales for gravitational settling are of the order of a few million years or smaller, the atmospheric

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composition of white dwarf stars is generally simple, with around 80% showing solely H lines (spectral class DA). The remaining are dominated by He lines, when the atmospheric temperature is sufficient to excite the He atoms. The spectral class is DB if only HeI lines are present, and DO if HeII lines are visible (typically  $T_{\text{eff}} \gtrsim 40\,000$  K). Very cool white dwarfs ( $T_{\text{eff}} \lesssim 5\,000$  K for H atmosphere,  $T_{\text{eff}} \lesssim 11\,000$  K for He atmosphere) show featureless spectra and are classified as DCs. A substantial fraction (20–50 per cent, [Zuckerman et al. 2003](#); [Koester, Gänsicke, & Farihi 2014](#)) of white dwarfs show contamination by metals, which can only be explained by ongoing accretion, except for very hot objects ( $T_{\text{eff}} \gtrsim 50\,000$  K), where radiative levitation can still play a significant role (e.g. [Barstow et al. 2014](#)); a Z is added to the spectral classification to flag metal pollution. In rare cases, for stars classified as DQs, carbon may be dragged to the surface by convection (e.g. [Koester, Weidemann, & Zeidler 1982](#)). Cool DQs show spectra similar to dwarf carbon (dC) stars, which are themselves believed to be one outcome binary evolution ([Whitehouse et al. 2018](#)).

In this paper we extend the work of [Kleinman et al. \(2013\)](#) and [Kepler et al. \(2015, 2016\)](#), continuing the search for new spectroscopically confirmed white dwarf and subdwarf stars in the data release 14 of the Sloan Digital Sky Survey (SDSS DR14, [Abolfathi et al. 2018](#)). Spectroscopy allows precise determinations of  $T_{\text{eff}}$ ,  $\log g$ , and abundances, serving as a valuable resource for studying stellar formation and evolution in the Milky Way (e.g. [Winget et al. 1987](#); [Bergeron, Saffer, & Liebert 1992](#); [Liebert, Bergeron, & Holberg 2005](#); [Tremblay et al. 2014](#)). As a by-product, we also identify cataclysmic variables (CVs) — white dwarfs with ongoing mass exchange from a companion, and presenting emission lines, generally of hydrogen and/or helium — and dC stars, due to their similarity with carbon-rich white dwarfs. These dC stars ([Roulston et al. 2018](#)), as well as hot subdwarfs and ELMs, hold potential to shed light on the poorly understood process of close binary evolution.

## 2 DATA ANALYSIS

### 2.1 Identification of the candidates

We started with the 4 851 200 optical spectra in the SDSS DR14. We selected the 259 537 spectra of stars with  $3\sigma$  proper motion larger than 20 mas/yr, as well as all 68 836 newly observed spectra of stars with colours within the [Kleinman et al. \(2013\)](#) selected white dwarf colour range, and all 225 471 spectra classified by the SDSS spectral pipeline as WHITE\_DWARF, A, B, OB or O stars, or CV (cataclysmic variables). In addition, we performed an automated search for similar spectra as described in [Kepler et al. \(2015, 2016\)](#) on all the 4 851 200 optical spectra, selecting further  $\approx 4\,000$  spectra. We examined these selected spectra by eye ( $\approx 500\,000$  spectra, given the overlap between the different selections) to identify broad line spectra characteristic of white dwarfs, hot subdwarfs, and dCs, resulting in our identification of 34 321 high signal-to-noise ( $S/N_g$ ) spectra containing white dwarf, subdwarf, CVs and dCs stars.  $S/N_g$  is the signal-to-noise parameter in the g-band in the SDSS spectra reduction pipeline. Our visual inspection showed that most objects in the SDSS catalogue with proper motion

smaller than 30 mas/yr and magnitude  $g > 20$  are in fact galaxies, from their composite spectrum, high red-shifted lines, or broad emission lines. We also inspected 1449 additional spectra for *Gaia* DR2 stars in the colour–magnitude white dwarf region [ $M_{\text{GG}} > 3.333 \times (G_{\text{BP}} - G_{\text{RP}}) + 8.333$ ], not included in our previous selection. This white dwarf region was selected using the photometric conditions in [Kilic et al. \(2018\)](#), but with parallax/error  $> 4$ , flux/error  $> 3$ , as we are looking for stars with spectra and SDSS photometry, matching to 3 arcsec in the SDSS coordinates.

In previous SDSS white dwarf catalogues, we had not employed a proper motion criterion for selection, obtaining a signal-to-noise limited sample, determined by a colour–magnitude selection. The main reason we expanded our selection to include low signal-to-noise spectra from high proper motion objects is that our previous colour selection excluded the low temperature white dwarfs ( $T_{\text{eff}} < 8\,000$  K), because their SDSS colours are similar to the more numerous cool dwarf stars. However, considering that all stars born more than 2 Gyr ago with masses larger than  $\sim 1.5 M_{\odot}$  are now white dwarfs cooler than 10 000 K, our colour selection was excluding a significant population of these objects. We still limited our classification to spectra with  $S/N_g \geq 3$ –7, depending on the spectral type — down to lower  $S/N_g$  for DA stars because hydrogen lines are stronger and easier to detect, but to higher  $S/N_g$  in other classes.

### 2.2 Spectral Classification

DR14 uses improved flux-calibration, with atmospheric differential refraction corrected on a per-exposure basis following the recipe described in [Margala et al. \(2016\)](#), and improved co-addition of individual exposures. The Stellar Parameters Pipeline, which we used for our initial spectral class selection, are from [Lee et al. \(2008a,b\)](#) and [Allende Prieto et al. \(2008\)](#).

The wavelength coverage is from 3800 to 9200 Å for the SDSS spectrograph (up to Plate 3586), and 3650 to 10 400 Å, for the BOSS spectrograph, with a resolution of 1500 at 3800 Å and 2500 at 9000 Å, and a wavelength calibration better than 5 km/s. All the spectra used in our analysis were processed with the spectroscopic reduction pipeline version v5\_10\_0 for BOSS/SEQUELS/eBOSS, the spectroscopic reduction pipeline version 26 for the SDSS Legacy and SEGUE-1 programs, the special SDSS pipeline version 103 to handle stellar cluster plates, and the pipeline version 104 run on SEGUE-2 plates. These RUN2D numbers denote the version of extraction and redshift-finding code used. In all SDSS spectral line descriptions, vacuum wavelengths are used. The wavelengths are shifted such that measured velocities are relative to the solar system barycentre at the mid-point of each 15-minute exposure.

Because we are interested in obtaining accurate mass distributions for our DA and DB stars, we were conservative in labelling a spectrum as a clean DA or DB, adding additional subtypes and uncertainty notations (:) if we saw signs of other elements, unresolved companions, or magnetic fields (H) in the spectra. While some of our mixed white dwarf subtypes would probably be identified as clean DAs or DBs with better signal-to-noise spectra, few of our identified clean DAs or DBs would likely be found to have additional spectral features within our detection limit.

**Table 1.** Classification of 37 053 spectra in Table 2.

Number	Type
15716	DA
1358	DB
1847	DC
524	DQ
598	DZ
45	DO/PG1159/O(He)/O(H)
210	sdB
205	sdO
311	CV
4	DS
1	DH
14	BHB
15793	sdA
447	dC
8	BL LAC

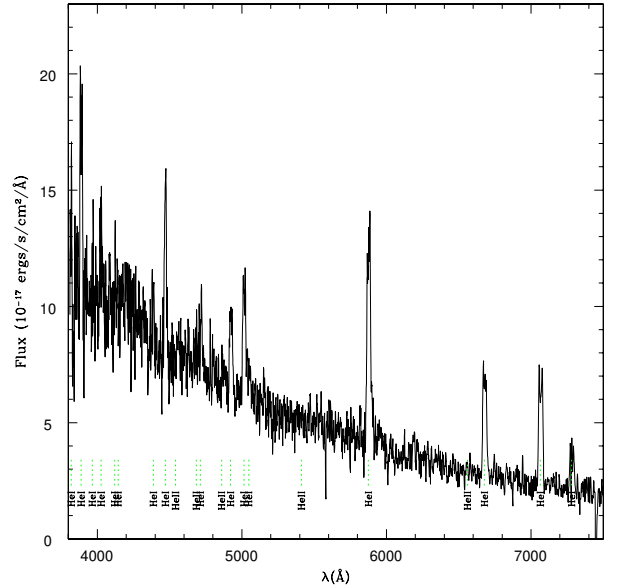
We looked for the following features to aid in the classification for each specified white dwarf subtype:

- Balmer lines — normally broad and with a steep Balmer decrement [DA but also DAB, DBA, DZA, and subdwarfs]
- HeI 4471Å [DB, subdwarfs]
- HeII 4686Å [DO, PG1159, sdO]
- C2 Swan band or atomic CI lines [DQ]
- CaII H & K [DZ, DAZ, DBZ]
- CII 4367Å [HotDQ]
- Zeeman splitting [magnetic white dwarfs]
- featureless spectrum with significant proper motion [DC]
- flux increasing in the red [binary, most probably M companion]
- OI 6158, 7774, 8448Å [DS, oxygen dominated]
- H and He emission lines [CVs and M dwarf companions]

Table 1 is a tally of the 37 053 objects we classified in Table 2. As 15 716 objects were classified by us as DAs and 1363 as DBs, of the 20 109 white dwarfs in the table, 78% are DAs.

Among the 15 716 DAs, we found 474 magnetic DAHs, 598 unresolved binaries with main-sequence M dwarf companions (DA+M), 136 DAZs with Ca and/or Mg lines, and 52 DABs contaminated by He I lines. We also found 41 stars having an extremely steep Balmer decrement (i.e. only a broad H $\alpha$  and sometimes H $\beta$  is observed while the other lines are absent) that could not be fit with a pure hydrogen grid (see section 2.3 below), or indicated extremely high gravities. We find that these objects are best explained as helium-rich DAs, and therefore with an extremely thin H layer mixed with the underlying He, and denote them DA(He).

We classified 447 spectra as dC - dwarf carbon stars, in line with Green (2013) and Farihi et al. (2018). We cannot identify a clear visual discontinuity from the coolest DQs to the hottest dCs either in term of the C line strength or the colour–magnitude diagram (see Fig. 13). We do not have spectral models for dCs, so we do not determine their properties. Of the 340 CVs, 9 are AM CVn type, with pure He spectra, and 87 CVs show both H and He lines. As an example of the spectra of cataclysmic variables found in our search, Fig. 1 shows the spectrum of the ultra-compact white

**Figure 1.** Spectrum of the outbursting AM CVn SDSS J141118.31+481257.66, with He emission double lines.

dwarf binary AM CVn SDSS J141118.31+481257.66, with  $g=19.38$ , spectrum P-M-F 1671-53446-0010, with He emission double lines (Fig. 1). Rivera Sandoval & Maccarone (2019) reported an outburst, the first recorded for this star. Ramsay et al. (2018) review of AM CVns show many have outbursts reported; AM CVn are ultra-compact hydrogen-deficient binaries, each consisting of a white dwarf accreting helium-dominated material from a degenerate or semi-degenerate donor star.

We classified 15 855 stars as sdAs, stars with spectra dominated by narrow hydrogen lines, following Kepler et al. (2016). Solar metallicity main sequence A stars have absolute magnitudes  $M_g \approx 0 - 2$ . As stars brighter than  $g=14.5$  saturate in SDSS, only A stars with distance moduli larger than 12.5 are observed in SDSS, i.e., farther than 3.5 kpc. Because SDSS observed mainly perpendicular to the disk (galactic latitude in general larger than 30deg), these would be located in the halo, where A stars should already have evolved off the main sequence. Thus, these sdA stars are mostly likely very low metallicity main sequence stars ( $[\text{Fe}/\text{H}] \lesssim -1.0$ ), whose spectra are dominated by hydrogen because they lack significant metals, and most have masses smaller than the Sun, or their spectra would show higher effective temperatures than observed. As their absolute magnitude, according to Gaia parallaxes, cover  $-8 \geq M_G \geq 10$  (see Fig. 11), they cannot be classified as normal main sequence A stars, presenting much lower masses and temperature than AV stars. They are hotter than sdF stars (Scholz et al. 2015). Some of these sdAs may be stars that lost mass due to binary interaction, resulting most probably in He core stars, precursors of ELMs, and ELMs (Pelisoli, Kepler, & Koester 2018a; Pelisoli et al. 2018b, 2019) (see Section 3.3).

Plate-MJD-Fiber	RA-DEC (2000)	S/N <sub>g</sub>	u (mag)	$\sigma_u$ (mag)	g (mag)	$\sigma_g$ (mag)	r (mag)	$\sigma_r$ (mag)	i (mag)	$\sigma_i$ (mag)	z (mag)	$\sigma_z$ (mag)	E(B-V) (mag)	ppm (mas/yr)	$\ell$ (deg)	b (deg)	Type
2824-54452-0413	000003.29+282148.18	011	20.887	0.085	19.792	0.025	19.544	0.022	19.349	0.023	19.298	0.062	0.053	013.7	109.4	-33.2	sdA/F
7850-56956-0719	000006.75-004653.98	022	19.236	0.034	18.855	0.024	18.914	0.016	19.123	0.021	19.447	0.049	0.038	002.1	095.7	-60.9	DA
0650-52143-0497	000007.16-094339.84	007	19.429	0.043	19.577	0.028	19.997	0.025	20.275	0.040	21.212	0.415	0.029	040.5	085.7	-68.8	DA
7134-56566-0587	000007.84+304606.35	011	20.214	0.039	19.666	0.017	19.531	0.021	19.499	0.023	19.567	0.059	0.039	044.7	110.1	-30.8	DA
7666-57339-0848	000009.65+260022.32	004	21.119	0.034	21.104	0.045	21.104	0.045	21.231	0.076	20.994	0.233	0.036	000.0	108.8	-35.5	DC:
8740-57367-0705	000010.29+064832.16	040	18.902	0.027	18.020	0.018	17.732	0.019	17.646	0.016	17.607	0.024	0.044	018.6	101.0	-53.9	sdA/F
7167-56604-0752	000011.66-085008.31	019	19.453	0.039	19.111	0.021	19.065	0.023	19.139	0.021	19.338	0.083	0.032	104.7	087.0	-68.1	DQ
4354-55810-0324	000012.04-030831.36	009	20.460	0.058	20.015	0.032	19.939	0.026	19.952	0.033	19.933	0.089	0.033	052.5	093.7	-63.1	DA
7596-56945-0860	000012.57+190213.77	003	22.032	0.262	21.434	0.054	21.656	0.090	22.314	0.254	21.984	0.644	0.030	000.0	106.5	-42.2	sdA
7167-56604-0246	000015.33-105859.15	067	16.616	0.020	15.685	0.026	15.353	0.021	15.242	0.017	15.184	0.017	0.030	032.9	083.8	-69.9	sdA
0650-52143-0217	000022.54-105142.18	011	19.310	0.034	18.912	0.027	18.823	0.022	18.894	0.021	18.962	0.059	0.030	051.1	084.0	-69.8	DA
8740-57367-0716	000022.68+064312.90	019	19.910	0.038	19.514	0.021	19.627	0.023	19.811	0.024	21.759	0.475	0.046	024.3	101.0	-54.0	DAH
7848-56959-0062	000022.88-000635.69	049	18.270	0.019	18.247	0.027	18.571	0.016	18.858	0.027	19.222	0.055	0.029	016.2	096.4	-60.3	DA
2822-54389-0400	000025.40+251726.40	010	20.243	0.045	20.194	0.027	20.502	0.026	20.825	0.046	20.986	0.190	0.042	012.4	108.6	-36.2	DA
6127-56274-0026	000029.28+190638.88	007	23.157	0.045	19.780	0.028	19.780	0.028	19.524	0.038	19.509	0.114	0.031	000.0	106.6	-42.1	DC
0650-52143-0165	000030.08-102420.70	029	18.374	0.021	17.481	0.022	17.215	0.013	17.101	0.019	17.111	0.019	0.034	022.2	084.9	-69.4	sdA/F
2822-54389-0305	000030.24+242307.88	017	20.347	0.045	19.294	0.017	18.928	0.016	18.763	0.022	18.741	0.037	0.074	012.2	108.4	-37.0	sdA/F
7850-56956-0688	000034.07-010819.97	037	18.189	0.015	17.844	0.021	18.013	0.023	18.240	0.020	18.502	0.035	0.032	030.3	095.7	-61.3	DA
7034-56564-0336	000034.10-052922.46	046	16.930	0.023	16.778	0.020	17.060	0.016	17.296	0.015	17.576	0.021	0.029	086.6	091.4	-65.2	DA
7850-56956-0704	000035.59-001115.88	007	23.039	0.347	20.271	0.031	18.813	0.017	18.334	0.026	18.118	0.039	0.030	065.8	096.5	-60.4	dC
2824-54452-0272	000051.85+272405.26	025	18.702	0.029	18.648	0.022	19.063	0.023	19.304	0.029	19.618	0.096	0.045	013.4	109.4	-34.1	DA
4354-55810-0735	000052.12-021437.58	008	20.810	0.081	20.191	0.023	19.944	0.023	19.993	0.032	19.772	0.081	0.031	080.4	094.8	-62.3	DC
2803-54368-0210	000053.33+270330.00	067	16.723	0.015	15.647	0.015	15.618	0.015	15.611	0.017	15.714	0.026	0.037	026.2	109.3	-34.5	sdA
0650-52143-0534	000054.38-090807.58	011	19.317	0.042	18.997	0.033	18.952	0.019	19.030	0.029	19.094	0.061	0.037	053.6	087.0	-68.4	DC
7167-56604-0806	000054.40-090806.92	021	19.317	0.042	18.998	0.033	18.954	0.019	19.037	0.029	19.099	0.061	0.032	053.6	087.0	-68.4	DQ
2630-54327-0342	000055.12-042449.04	010	19.771	0.043	20.016	0.032	20.113	0.026	20.373	0.043	20.642	0.163	0.041	029.3	092.8	-64.3	DBA:
2630-54327-0359	000100.42-042742.87	028	18.814	0.029	18.513	0.043	18.707	0.020	18.882	0.026	19.165	0.047	0.038	016.9	092.8	-64.3	DA
7848-56959-0026	000104.05+000355.82	035	19.220	0.028	18.867	0.028	19.051	0.018	19.212	0.027	19.482	0.053	0.025	010.5	096.9	-60.2	DA
2822-54389-0397	000106.22+250330.05	017	19.516	0.035	19.526	0.023	19.711	0.022	19.970	0.033	20.246	0.135	0.063	015.8	108.7	-36.4	DBAZ
2624-54380-0330	000106.77-034823.43	065	16.347	0.017	15.396	0.014	15.155	0.023	15.070	0.019	15.036	0.013	0.035	015.8	093.5	-63.8	sdA
4534-55863-0466	000106.93+082825.58	019	19.401	0.028	18.946	0.017	18.848	0.015	18.840	0.018	18.922	0.046	0.049	067.1	102.3	-52.4	DA
4216-55477-0238	000107.55-000042.83	021	19.924	0.033	19.033	0.028	18.695	0.022	18.599	0.021	18.591	0.039	0.027	013.9	096.8	-60.3	sdA/F
1489-52991-0542	000108.80+001744.48	044	17.337	0.038	16.479	0.014	16.213	0.019	16.059	0.022	16.052	0.015	0.028	045.7	097.1	-60.0	sdA/F
2824-54452-0207	000110.10+073520.40	011	20.335	0.038	20.071	0.025	20.071	0.025	20.139	0.040	20.461	0.161	0.043	009.8	109.5	-34.0	DA
7850-56956-0267	000111.74-015620.55	031	19.049	0.023	18.208	0.022	17.870	0.014	17.765	0.015	17.736	0.022	0.031	017.2	095.3	-62.1	sdA/F
2824-54452-0432	000115.77+285647.28	013	20.110	0.044	19.749	0.023	19.956	0.023	20.148	0.032	20.350	0.143	0.043	018.1	109.9	-32.7	DA
6877-56544-0616	000115.78+261912.10	006	21.346	0.089	20.692	0.026	20.455	0.025	20.399	0.034	20.160	0.092	0.034	018.4	109.1	-35.2	DC:

**Table 2.** Spectral classification. The complete table is available electronically.

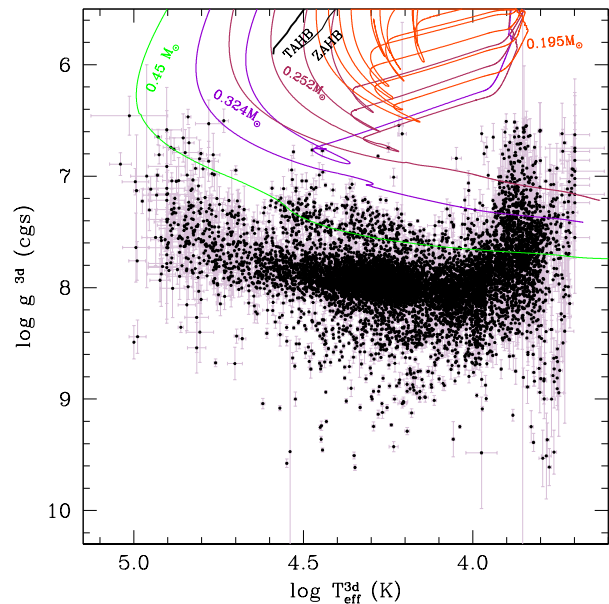
### 2.3 Models

After classifying white dwarf and subdwarf stars, we fitted the observed spectra to improved models of pure DAs and DBs (Koester et al. 2011; Koester & Kepler 2015), DOs (Reindl et al. 2014,a; Reindl & Rauch 2015), sdBs and sdOs (Geier et al. 2015, 2017a,b). For DAs, we used ML2/ $\alpha = 0.7$  models, with an LTE grid extending from  $5000 \text{ K} \leq T_{\text{eff}} \leq 80000 \text{ K}$  and  $3.5 \leq \log g \leq 9.5$  dex (cgs). For  $T_{\text{eff}} \leq 14000 \text{ K}$  we corrected the temperature and gravity to the 3D calculations of Tremblay et al. (2013), resulting in a flat  $\log g$  distribution down to  $T_{\text{eff}} \approx 10000 \text{ K}$ , as shown in Fig. 2. The figure also show models for He core pre-white dwarfs (Althaus et al. 2015; Istrate et al. 2016) and for the Zero Age Horizontal Branch (ZAHB) to show the region where we do not consider the objects as white dwarfs. For DAs whose LTE analysis indicates  $T_{\text{eff}} \geq 45000 \text{ K}$  (that is where NLTE effects become important), we employed NLTE models. We computed a pure H grid with the Tübingen non-LTE Model-Atmosphere Package (TMAP, Werner et al. 2003, 2012; Rauch & Deetjen 2003) spanning from  $T_{\text{eff}} = 40000 - 200000 \text{ K}$  (step size  $5000 \text{ K}$  for  $T_{\text{eff}} < 100000 \text{ K}$  and  $10000 \text{ K}$  for  $T_{\text{eff}} > 100000 \text{ K}$ ) and  $\log g = 6.0 - 9.0$  (step size  $0.5$  dex). To calculate synthetic line profiles, we used Stark line-broadening tables provided by Tremblay & Bergeron (2009). To derive the effective temperatures and surface gravities the Balmer lines of the hot DAs were fitted in an automated procedure by means of  $\chi^2$  minimisation using the FITSB2 routine (Napiwotzki 1999) and calculated the statistical one sigma errors. Each fit was then inspected visually to ensure the quality of the analysis. We excluded hot DAs whose spectra show a red excess and/or central emission features in the Balmer lines that cannot be the result of NLTE effects but are likely due to the irradiation of a cool companion by the hot white dwarf.

Fig. 3 shows the histogram of the number of DA stars versus effective temperature. The hottest DAs we analysed have  $T_{\text{eff}} \approx 120000 \text{ K}$ . The decrease of the number in the coolest bin is mainly due to incompleteness, because cooler stars are fainter — partially compensated by the low mass stars that are brighter, but also affected by the finite age of the disk stars (Winget et al. 1987).

For DBs we use ML2/ $\alpha = 1.25$  LTE models as in Koester & Kepler (2015), with  $12000 \text{ K} \leq T_{\text{eff}} \leq 45000 \text{ K}$ , and  $7 \leq \log g \leq 9.5$  dex (cgs), resulting in the  $T_{\text{eff}} - \log g$  distribution shown in black in Fig. 4. An increase in the estimated  $\log g$  can be seen for  $T_{\text{eff}} \lesssim 16000 \text{ K}$ . This is not solved when pure He 3D corrections are applied (Cukanovaite et al. 2018), shown in red in Fig. 4, and is probably caused by poor estimates of neutral broadening.

Because the spectral fits are normally degenerate between a hot solution(s) and a cool one, we also fitted the *ugriz* colors of DAs and DBs to synthetic colours derived from the same atmospheric models, and used the photometric values to guide our spectral parameter determinations. For DCs, DQs and DZs, we only estimated their  $T_{\text{eff}}$  from the colours derived from the atmospheric models of Koester (2010).



**Figure 2.** Surface gravity ( $\log g$ ) and effective temperature ( $T_{\text{eff}}$ ) estimated for the 10189 DA white dwarf stars for which the SDSS spectra has  $S/N_g > 10$ , after applying three-dimensional convection atmospheric model corrections from Tremblay et al. (2013), in black. The Zero Age Horizontal Branch (ZAHB) plotted was calculated with solar composition models. These delimit the region of solar metallicity Blue Horizontal Branch stars. It indicates the highest possible surface gravity for a hot subdwarf. Stars with  $T_{\text{eff}} \leq 45000 \text{ K}$  and smaller surface gravities than the ZAHB are sdBs. We have also plotted  $0.45$ ,  $0.3$ ,  $0.2$  and  $0.15 M_{\odot}$  models of He core pre-white dwarfs (Althaus et al. 2015; Istrate et al. 2016) to guide the eye to the limiting region of what we call white dwarfs.

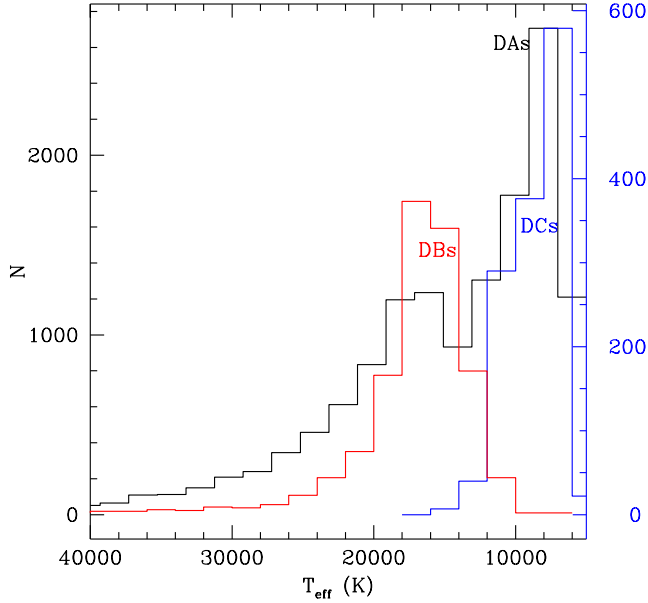
## 3 RESULTS

### 3.1 Masses

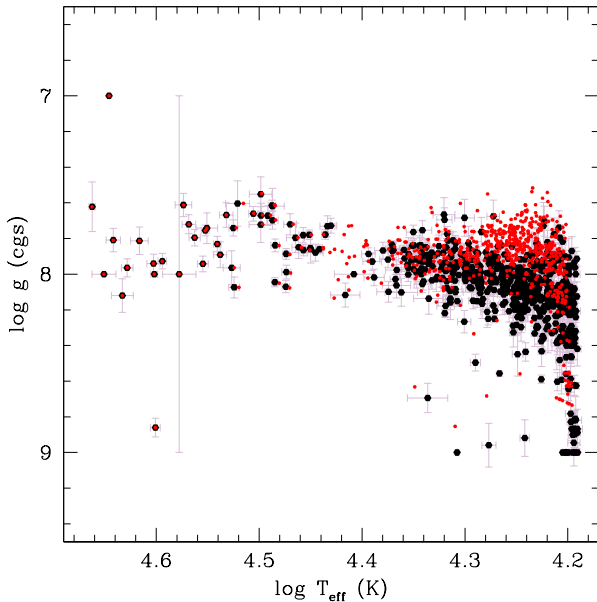
For white dwarfs, the main indicator of  $\log g$  is the width of the atmospheric absorption lines. However, for  $T_{\text{eff}} < 10000 \text{ K}$ , the width of the hydrogen lines becomes very weakly dependent on gravity. As a result, it is very difficult to distinguish low mass white dwarfs and metal-poor main sequence A/F stars in the  $T_{\text{eff}} < 10000 \text{ K}$  and  $\log g < 6.5$  range solely with visual inspection, even though low metallicity main sequence stars have an upper limit to  $\log g \lesssim 4.64$ , for a turn-off mass of  $\sim 0.85 M_{\odot}$ . The two steps we took to overcome this limitation was the extension of the model grid to  $\log g \geq 3.5$ , fitting all the spectra we classified as DAs and sdAs, using the result to separate  $\log g \geq 6.5$  as white dwarfs, and finally, after Gaia DR2, using the parallaxes, as discussed in Section 4.

Kleinman et al. (2013) limited the white dwarf classification to surface gravity  $\log g \geq 6.5$ . At the cool end of our sample,  $\log g = 6.5$  corresponds to a mass around  $0.2 M_{\odot}$ , well below the single mass evolution in the lifetime of the Universe — but reachable via interacting binary evolution. The He-core white dwarf stars in the mass range  $0.2 - 0.45 M_{\odot}$ , referred to as low-mass white dwarfs, are usually found in close binaries, often double degenerate systems (Marsh, Dhillion & Duck 1995), being most likely a prod-





**Figure 3.** Histogram of the number of DA stars versus effective temperature (in black), compared to the distribution for DCs (in blue), and DBs (in red). The number scale for DCs and DBs is shown on the right.



**Figure 4.** Surface gravity ( $\log g$ ) and effective temperature ( $T_{\text{eff}}$ ) estimated for 805 DB white dwarf stars with spectral  $S/N_g \geq 10$ . The increase in apparent gravity below  $T_{\text{eff}} \approx 16000$  K is probably caused by incorrect neutral broadening estimative (Schaeuble et al. 2017). In red are the values after applying the pure He 3D corrections of Cukanovaite et al. (2018).

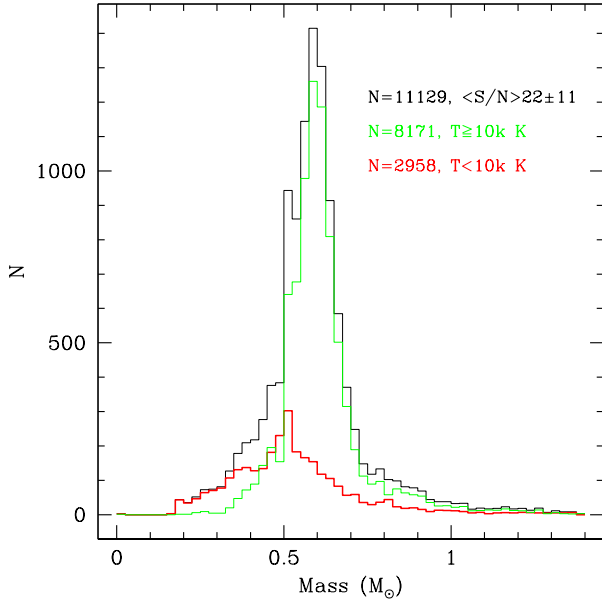
uct of interacting binary stars evolution. More than 70% of those studied by Kilic et al. (2011) with masses below  $0.45 M_{\odot}$  and all but a few with masses below  $0.3 M_{\odot}$  show radial velocity variations (Brown et al. 2013; Gianninas et al. 2014; Brown, Kilic, & Gianninas 2017). Kilic, Stanek & Pinsonneault (2007) suggest single low-mass white dwarfs result from the evolution of old metal-rich stars that truncate evolution before the helium flash due to severe mass loss. They also conclude all white dwarfs with masses below  $\approx 0.3 M_{\odot}$  must be a product of binary star evolution involving interaction between the components.

The spectroscopic sdA sample defined in Kepler et al. (2016) and used in our pre-selection here, being only a visual determination of narrow H lines and absence of strong metal lines, includes many types of objects: real white dwarfs, ELMs, pre-ELMs, low metallicity main sequence stars and even giants with low atmospheric metallicity. We need to define separate classes depending on the absolute luminosity (radius) to distinguish among them (see Section 3.3). Even though the nomenclature would suggest that subdwarfs have smaller radii than main sequence stars, it is not always the case — they mainly have smaller masses.

Table 3 shows the atmospheric parameters obtained from the fitting of the spectra for DAs. Fig. 5 shows the mass distribution for DAs with  $S/N_g \geq 10$ , with 11 129 stars, and result in a mean mass  $\langle M_{\text{DA}} \rangle = 0.5903 \pm 0.0014 M_{\odot}$ , and individual dispersion of  $0.152 M_{\odot}$ . For the 8171 DAs with  $T_{\text{eff}} \geq 10000$  K, the mean mass is  $\langle M_{\text{DA}} \rangle = 0.6131 \pm 0.0014 M_{\odot}$ , with a dispersion  $0.126 M_{\odot}$ , while for those 2958 with  $T_{\text{eff}} < 10000$  K,  $\langle M_{\text{DA}} \rangle = 0.5276 \pm 0.0035 M_{\odot}$  with a dispersion  $0.174 M_{\odot}$ . Fig. 6 shows the density of DAs versus temperature and surface gravity, showing the surface gravity decreases significantly below  $T_{\text{eff}} \approx 10000$  K.

Plate-MJD-Fiber	RA-DEC (2000)	Type	$T_{\text{eff}}$ (K)	$\sigma(T)$	$\log g$	$\sigma(\log g)$	$V_r$	$\sigma(V_r)$	d[pc]	z[pc]	Mass <sup>Q</sup> = 0.7	$\sigma(\text{mass})$	$T_{\text{eff}}^{3D}$	$\log g^{3D}$	Mass <sup>3D</sup>	$\sigma(\text{mass}^{3D})$
0266-51602-0314	094107.47-001949.70	DA	011493	00122	8.396	0.079	64	22	00199	00118	0.841	0.049	011437	8.235	0.73677	0.03484
0266-51630-0026	094901.28-001909.61	DA	010809	00027	8.094	0.025	-18	5	00077	00048	0.654	0.014	010702	7.875	0.53674	0.00847
0266-51630-0031	094804.30-000738.16	DA	010135	00050	8.525	0.068	25	14	00111	00069	0.920	0.042	010033	8.255	0.74933	0.03043
0266-51630-0037	094917.06-000023.67	DA	011614	00152	8.437	0.095	-28	23	00183	00114	0.867	0.059	011568	8.281	0.77233	0.04207
0266-51630-0570	094640.35+011319.86	DA	019971	00126	7.922	0.022	43	7	00201	00125	0.583	0.010	019971	7.922	0.58328	0.00723
0266-51630-0629	094844.84+003516.63	DA	012900	00106	8.146	0.034	93	23	00151	00094	0.688	0.019	013007	8.105	0.66503	0.01347
0266-51608-0099	095329.20-005100.49	DA	011068	00113	8.653	0.092	87	23	00145	00091	0.993	0.047	010952	8.438	0.86676	0.04082
0268-51633-0129	095759.16-010707.29	DA	007578	00028	7.708	0.076	29	5	00091	00058	0.463	0.033	007574	7.567	0.40172	0.02207
0268-51633-0503	095940.23+003634.17	DA	010566	00069	8.049	0.078	28	15	00199	00130	0.629	0.043	010452	7.800	0.51644	0.02100
0270-51909-0008	101435.26-004714.40	DA	009869	00073	8.497	0.120	7	22	00145	00099	0.902	0.075	009783	8.232	0.73154	0.05228
0270-51909-0468	100955.38+000943.86	DA	010622	00035	8.170	0.037	11	7	00119	00081	0.699	0.020	010512	7.922	0.56011	0.01355
0271-51883-0181	101741.70-002934.12	DA	014581	00094	7.993	0.018	0	0	00000	00000	0.000	0.000	014581	7.993	0.60708	0.00657
0271-51883-0557	102003.39+000902.54	DA	006148	00094	9.742	0.147	-188	99	00000	00000	1.372	0.034	006147	9.693	1.36091	0.02447
0272-51941-0289	102041.74-011101.13	DA	009211	00076	7.697	0.229	55	20	00214	00148	0.464	0.093	009153	7.426	0.35929	0.05511
0272-51941-0307	101911.51+000017.25	DA	012777	00153	8.408	0.051	129	14	00156	00109	0.850	0.032	012856	8.326	0.79890	0.02096
0272-51941-0518	102546.72+002857.43	DA	007890	00029	7.787	0.065	21	5	00092	00066	0.500	0.027	007883	7.616	0.42446	0.01977
0273-51957-0337	102653.12+005110.54	DA	014768	00478	7.939	0.096	84	29	00322	00233	0.580	0.048	014768	7.939	0.57950	0.03363
0273-51957-0615	103448.94+005201.33	DA	010070	00095	8.409	0.133	170	27	00166	00123	0.847	0.082	009973	8.140	0.67917	0.05632
0274-51913-0222	103833.50-001959.70	DA	020825	00225	7.479	0.036	0	0	00000	00000	0.000	0.000	020825	7.479	0.43104	0.00825
0274-51913-0303	103635.66-000036.42	DA	012283	00197	7.605	0.067	27	14	00335	00248	0.440	0.026	012339	7.583	0.43140	0.01832
0274-51913-0536	104100.56+010909.44	DA	009563	00049	8.211	0.085	9	14	00168	00128	0.718	0.054	009495	7.946	0.57061	0.03150
0276-51909-0073	105612.32-000621.66	DA	011167	00038	7.891	0.030	32	6	00149	00116	0.546	0.015	011078	7.746	0.49279	0.00956
0276-51909-0097	105405.75-011132.96	DA	011621	00162	7.453	0.137	0	0	00000	00000	0.000	0.000	011547	7.413	0.36752	0.02974
0276-51909-0593	105727.81+002118.70	DA	010731	00052	8.535	0.052	52	13	00145	00114	0.927	0.032	010615	8.287	0.77429	0.02439
0277-51908-0025	110636.72-001122.37	DA	014717	00307	7.671	0.067	17	17	00305	00243	0.475	0.025	014717	7.671	0.47527	0.01757
0277-51908-0066	110420.04-003628.21	DA	012528	00160	8.179	0.060	41	16	00203	00160	0.707	0.035	012613	8.106	0.66488	0.02404
0277-51908-0414	110015.66+010740.55	DA	014348	00302	7.611	0.073	0	23	00407	00324	0.452	0.027	014404	7.612	0.45284	0.01892
0277-51908-0513	110326.71+003725.80	DA	010636	00040	8.229	0.046	-8	9	00115	00091	0.731	0.030	010527	7.981	0.59129	0.01728
0277-51908-0596	110515.32+001626.13	DA	013080	00049	8.275	0.011	15	3	00045	00036	0.771	0.007	013180	8.235	0.74002	0.00577
0278-51900-0367	110623.40+011520.95	DA	010952	00066	7.943	0.063	4	13	00197	00159	0.573	0.033	010848	7.759	0.49790	0.01833
0278-51900-0593	111230.14+003002.55	DA	009629	00038	8.159	0.062	51	10	00133	00108	0.690	0.035	009556	7.894	0.54301	0.01928
0279-51984-0308	111028.70-003343.46	DA	009478	00048	8.299	0.091	6	14	00137	00109	0.779	0.059	009416	8.033	0.61710	0.03553
0279-51984-0321	111047.52+005421.35	DA	008651	00026	8.127	0.052	33	6	00079	00064	0.669	0.031	008628	7.877	0.53219	0.01434
0281-51614-0476	112712.17+001644.29	DA	012152	00269	8.116	0.119	54	33	00370	00308	0.670	0.067	012200	8.026	0.61951	0.04541
0282-51658-0304	113036.48-002155.76	DAZ	005295	00201	6.765	0.537	0	0	00000	00000	0.000	0.000	005294	6.761	0.18157	0.05746
0282-51658-0537	113614.89+005106.92	DA	009470	00062	8.564	0.095	47	19	00144	00123	0.944	0.055	009409	8.299	0.77928	0.04347
0283-51584-0349	113901.22+000321.79	DA+M:	013256	00493	8.541	0.209	0	0	00000	00000	0.000	0.000	013329	8.490	0.90135	0.08629
0283-51959-0117	114720.41-002405.66	DA	017517	00236	7.928	0.047	70	16	00318	00271	0.581	0.023	017517	7.928	0.58051	0.01610

Table 3. Parameters from spectral fitting to atmospheric models for DAs. The complete table is available electronically.



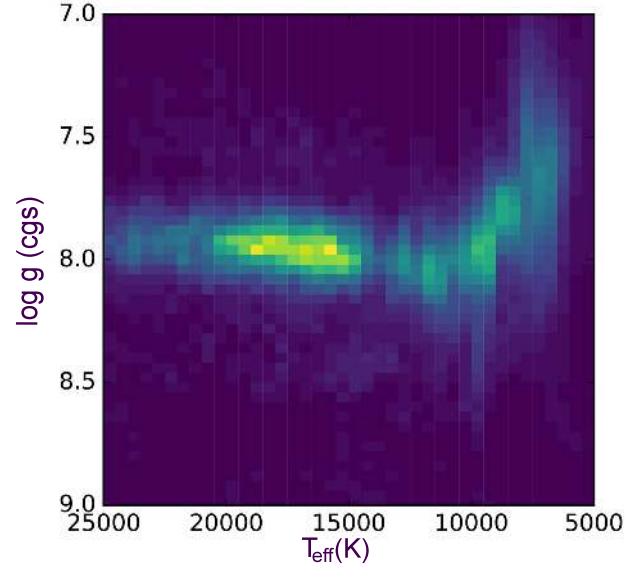
**Figure 5.** Mass distribution for the 11 129 DAs with  $S/N_g \geq 10$ . This sample overall shows a mean mass of  $\langle M \rangle = 0.5904 \pm 0.0014 M_\odot$ . For stars with  $T_{\text{eff}} > 10000$  K, however, the mean mass is  $\langle M \rangle = 0.6131 \pm 0.0014 M_\odot$ , whereas for stars with  $T_{\text{eff}} < 10000$  K, the mean mass is  $\langle M_{\text{DB}} \rangle = 0.5276 \pm 0.0035 M_\odot$ . Most of the low mass DAs concentrate below  $T_{\text{eff}} = 10000$  K.

Table 4 shows the effective temperature distribution for DAs in our sample that were found to have effective temperatures in the range specified. The hottest we found is the DAO SDSS J160828.69+422101.77, with a  $S/N_g = 43$  spectrum and  $T_{\text{eff}} = 120000 \pm 10000$  K, while the hottest pure DA is SDSS J101756.24+411524.72, with a  $S/N_g = 26$  spectrum and  $T_{\text{eff}} = 110000 \pm 8000$  K. The most massive pure DAs are SDSS J121234.85+165320.26, with a  $S/N_g = 17$  spectrum and  $T_{\text{eff}} = 5944 \pm 91$  K,  $\log g = 9.611 \pm 0.166$ ,  $M = 1.370 \pm 0.006 M_\odot$ , and SDSS J152958.12+130454.80, with a  $S/N_g = 48$  spectrum and  $T_{\text{eff}} = 5758 \pm 99$  K,  $\log g = 9.476 \pm 0.197$ ,  $M = 1.364 \pm 0.005 M_\odot$ . We caution that the quoted uncertainties are only the internal uncertainties from the least-square fits. For stars with multiple spectra, our mean external uncertainty is 5% in the effective temperature and 0.05 dex in  $\log g$ , but for  $T_{\text{eff}} \leq 10000$  K, the real uncertainty is unknown.

The histogram of the number of DB stars versus effective

**Table 4.** Distribution of DAs with  $T_{\text{eff}}$ .

Number	Temperature Range
273	< 6000 K
2938	6000 to 8000 K
2312	8000 to 10000 K
3325	10000 to 15000 K
3179	15000 to 20000 K
2968	20000 to 40000 K
596	> 40000 K
15591	total



**Figure 6.** Hess diagram — density distribution — across effective temperature and surface gravity for DAs with spectra with  $S/N \geq 10$ , showing the low mass DA white dwarfs concentrate below  $T_{\text{eff}} = 10000$  K.

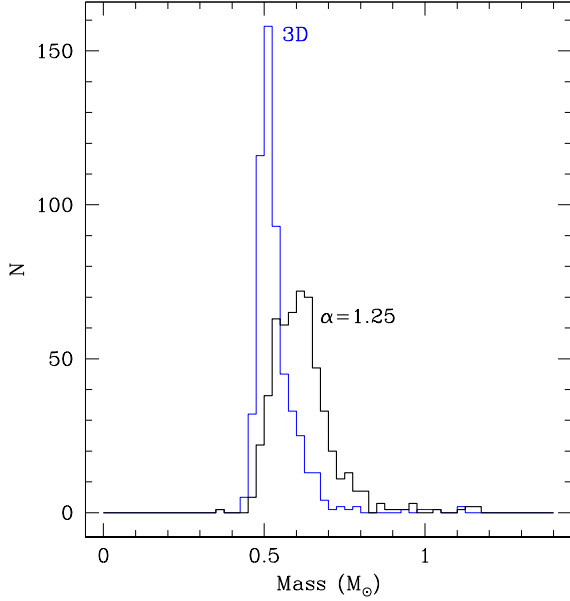
temperature can be seen in Fig. 3 (in red), compared to for DAs (in black). We see no obvious DB gap, just the normal decrease in DBs hotter than 30000 K due to the ionization of HeI.

Fig. 7 shows the mass distribution for the 550 pure DBs with  $S/N_g \geq 10$  spectra and  $T_{\text{eff}} \geq 16000$  K, with and without the pure He 3D convection correction following Cukanovaite et al. (2018). Without the correction, the mean mass is  $\langle M_{\text{DB}}^{\alpha=1.25} \rangle = 0.618 \pm 0.004 M_\odot$ , and a dispersion of  $0.098 M_\odot$ . With the 3D correction, the mean mass decreases to  $\langle M_{\text{DB}}^{3D} \rangle = 0.536 \pm 0.003 M_\odot$ , and a dispersion of  $0.074 M_\odot$ . The theoretical neutral broadening used in the models overestimates the  $\log g$ , and therefore masses, for lower temperatures (e.g. Koester & Kepler 2015; Schaeuble et al. 2017). For the 333 pure DB with  $S/N_g \geq 20$ , we obtain  $\langle M_{\text{DB}}^{3D} \rangle = 0.533 \pm 0.003 M_\odot$ , with a dispersion of  $0.058 M_\odot$ , i.e., the signal-to-noise is not changing the mean value. The low mean mass is a direct consequence of the pure He 3D corrections. Our fitted mean surface gravity, with the ML2/ $\alpha = 1.25$  models is  $\log g = 8.032 \pm 0.008$ , while the 3D corrected  $\log g = 7.864 \pm 0.007$ . A similar mean mass for DBs was obtained by Genest-Beaulieu & Bergeron (2019).

The two highest mass DBs, above 16000 K, are SDSS J163757.58+190526.01, with  $S/N_g = 24$ ,  $T_{\text{eff}} = 39895 \pm 441$  K,  $\log g = 8.86 \pm 0.05$ ,  $M = 1.111 \pm 0.017 M_\odot$ , and SDSS J081223.85+254842.82, with  $S/N_g = 14$ ,  $T_{\text{eff}} = 20394 \pm 1000$  K,  $\log g = 8.85 \pm 0.05$ ,  $M = 1.100 \pm 0.005 M_\odot$ , but our models, prior to the 3D correction, only go up to  $\log g = 9.0$ .

For the 1314 DCs in Table 2 with Gaia DR2 parallaxes, we obtain their masses from the *ugriz* colours and Gaia DR2 parallax, following Ourique et al. (2019). Their radius is estimated from the observed flux and distance, assuming a He atmosphere mass-radius relation. Their distribution shows a mean surface gravity  $\langle \log g^{DC} \rangle = 8.166 \pm 0.007$  dex (cgs),





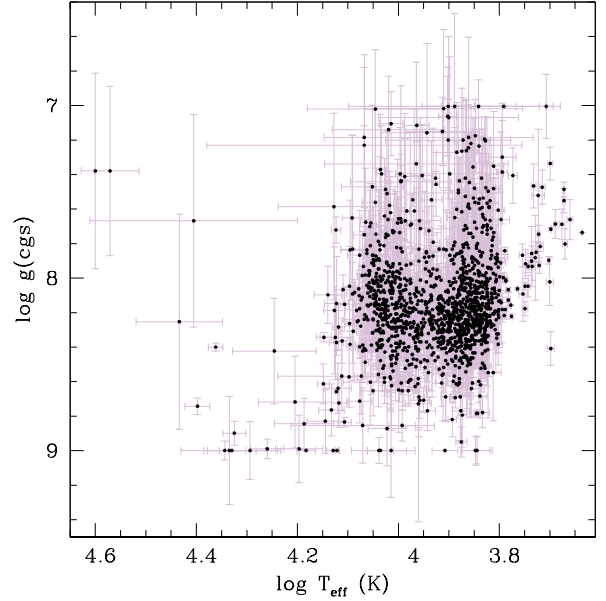
**Figure 7.** Mass distribution for the 550 pure DBs with  $S/N_g \geq 10$  with  $T_{\text{eff}} > 16000$  K, the distribution shows a mean mass of  $\langle M_{\text{DB}}^{\alpha=1.25} \rangle = 0.618 \pm 0.004 M_{\odot}$ , and a dispersion of  $0.098 M_{\odot}$ . With the pure He 3D correction, in blue, the mean mass decreases to  $\langle M_{\text{DB}}^{3\text{D}} \rangle = 0.536 \pm 0.003 M_{\odot}$ , with a dispersion of  $0.074 M_{\odot}$ . For lower temperatures the  $\log g$ , and therefore mass, is not trustworthy due to large uncertainties in the neutral broadening estimative. The DB mass distribution does not extend to masses below  $0.45 M_{\odot}$  or masses above  $1.1 M_{\odot}$ ; however, the statistics is much poorer than for DAs. The average signal-to-noise of the spectra is  $\langle S/N_g \rangle = 25$ .

with a dispersion of 0.245 dex, and a mean mass of  $\langle M^{\text{DC}} \rangle = 0.694 \pm 0.004 M_{\odot}$ , with a dispersion of  $0.127 M_{\odot}$ .

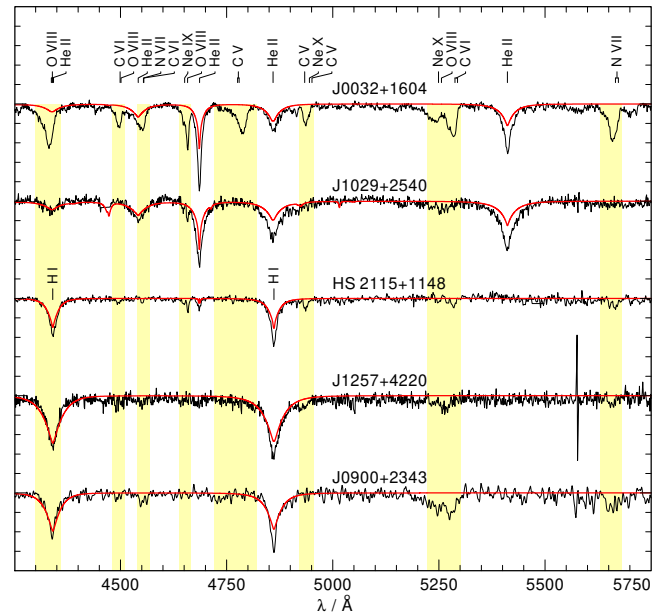
Figure 8 shows the effective temperature and surface gravity for 1314 DCs with Gaia DR2 parallaxes and *ugriz* SDSS colours. The mean mass obtained is  $\langle M \rangle_{\text{DC}} = 0.694 \pm 0.004 M_{\odot}$  with a dispersion of  $0.127 M_{\odot}$ . [Ourique et al. \(2019\)](#) presented the first DC mass distribution, using the Gaia colours and distances, showing it concentrates at higher masses than DBs. It is unlikely caused by an increase in the pressure by undetected hydrogen dredged up affecting the colours, as the non-DA to DA ratio increases below 16000 K.

### 3.2 Hot White Dwarfs

We identified spectroscopically in our sample a total of 12 PG 1159 and O(He) stars and 36 DOs with spectra dominated by He II lines. Furthermore, we found one O(H) star ([Reindl et al. 2016](#)) and 48 DAO stars, with spectra showing both H and He II lines as well as 310 hot DAs, showing only H lines. All these stars are hotter than  $T_{\text{eff}} = 45000$  K, where NLTE effects are important in the spectral analysis. We note that the majority of these objects were already known and that our catalogue is far from being complete with respect to the hottest white dwarfs found in previous SDSS data releases. This is a consequence of the  $3\sigma$  proper motion criterion, because hot white dwarfs are intrinsically



**Figure 8.** Surface gravity ( $\log g$ ) for the DCs, obtained from the SDSS *ugriz* photometry, Gaia DR2 parallax and a He-atmosphere mass–radius relation.



**Figure 9.** Normalized SDSS spectra of the newly discovered DO (upper two) and DA (bottom two) hot wind white dwarfs. The spectrum of SDSS J090023.89+234353.2 is convolved with a Gaussian ( $\text{FWHM}=3\text{\AA}$ ) to smooth out the noise. The TWIN spectrum of HS 2115+1148, for more than twenty years the only known H-rich hot wind white dwarf, is shown for comparison.

more luminous and are detected over larger distances, and the more distant ones will have small proper motions.

One of the PG 1159 stars and ten of the DO white dwarfs belong to the group of the so-called hot-wind white dwarfs (Werner et al. 1995), i.e. they show abnormally broad and deep He II lines with seven of them showing additionally ultra-high excitation (uhe) absorption lines (e.g., O VIII). For the latter objects we introduce the sub-classification uhe, i.e. PG 1159uhe and DOuhe. Our sample includes two newly identified hot wind DO white dwarfs, SDSS J003213.13+160434.7, which shows the strongest uhe features detected in any hot wind white dwarf so far, and SDSS J102907.31+254008.3, which shows only abnormally broad and deep He II lines and possible an uhe feature located at 5250Å. We also report the discovery of uhe features in two of the hot DA white dwarfs SDSS J090023.89+234353.2 and SDSS J125724.04+422054.2 (PG 1255+426). After more than twenty years, these are the first two H-rich hot wind white dwarfs discovered since HS 2115+1148 (Dreizler et al. 1995). Figure 9 shows the normalized SDSS spectra of the newly discovered objects. The uhe lines were recently shown to originate from an extremely hot, wind-fed circumstellar magnetosphere (Reindl et al. 2019). The two newly discovered DA hot wind white dwarfs show the Balmer line problem (failure to achieve a consistent fit to the Balmer lines, Werner 1996), which is also present in HS 2115+1148. Thus, the Balmer line problem can serve as a first indicator for the hot wind phenomenon. It is assumed that the cooler parts of the magnetosphere constitute an additional line forming region of the too-broad and too-deep H I/-He II lines (Reindl et al. 2019).

### 3.3 Subdwarfs

We classified 77 stars as hot subdwarf sdOs, 128 sdOBs and 209 sdBs. To refine the visual classification and derive the atmospheric parameters, a quantitative spectral analysis was performed for all sdO/B candidates in our sample with data of sufficient quality ( $S/N_g > 20$ ) and no atmospheric parameter determination in the literature.

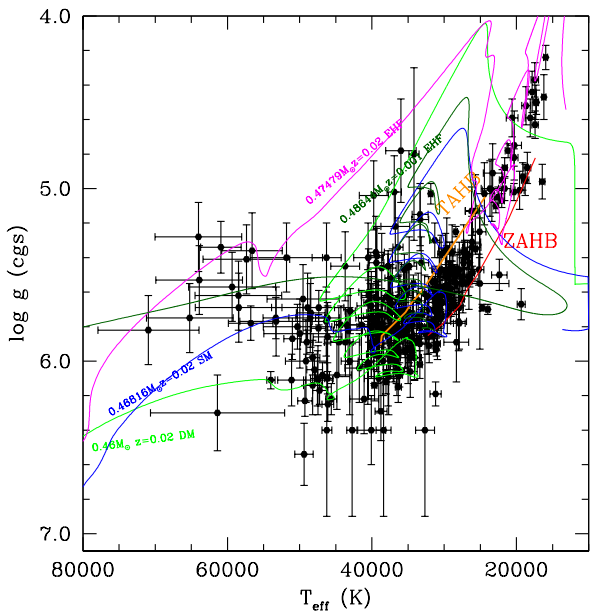
The method is described in Geier et al. (2011). We used appropriate model grids for the different sub-classes of sdBs and sdOBs. The hydrogen-rich and helium-poor [ $\log y = \log n(\text{He})/n(\text{H}) < -1.0$ ] stars with effective temperatures below 30 000 K were fitted using a grid of metal line blanketed LTE atmospheres with solar metallicity (Heber et al. 2000). Helium-poor stars with temperatures ranging from 30 000 K to 40 000 K were analysed using LTE models with enhanced metal line blanketing (O’Toole & Heber 2006). Metal-free NLTE models (Ströer et al. 2007) were used for hydrogen-rich stars with temperatures below 40 000 K showing moderate He-enrichment ( $\log y = -1.0 - 0.0$ ). The uncertainties provided are from statistical bootstrapping errors only. For more realistic uncertainties, additional random errors of about  $\pm 1000$  K in  $T_{\text{eff}}$  and  $\pm 0.1$  dex in  $\log g$  should be adopted for sdBs and sdOBs. For the hotter sdOs  $\pm 2000$  K and  $\pm 0.2$  dex are more appropriate.

Table 5 shows the hot subdwarfs analysed in this work, their classifications following the scheme proposed in Geier et al. (2017a) and their derived atmospheric parameters from the literature or this work. Fig. 10 shows effective tempera-

ture and surface gravity for the sample of hot subdwarf O- and B-type stars.

**Table 5.** Table of Hot Subdwarfs

P-M-F	SDSS J	Type	Teff	$e_{\text{Teff}}^{\text{fit}}$	$e_{\text{Teff}}^{\text{total}}$	log g	$e_{\text{logg}}^{\text{fit}}$	$e_{\text{logg}}^{\text{total}}$	log n(He)/n(H)	$e_{\text{logn(He)/n(H)}}^{\text{fit}}$	$e_{\text{logn(He)/n(H)}}^{\text{total}}$	New/Known
4017-55329-0110	151250.01-015436.33	BHB	17321	372	623	4.50	0.10	0.14	-2.46	0.28	0.34	New
5325-55980-0738	095638.14+145258.60	BHB	17411	449	672	4.63	0.08	0.13	-1.74	0.18	0.27	New
5420-56009-0298	130625.91+133349.14	BHB	17247	213	543	4.50	0.07	0.12	-2.23	0.33	0.39	New
4775-55708-0626	151519.21+054333.33	BHB	15960	274	570	4.24	0.07	0.12	-2.01	0.34	0.39	New
0793-52370-0623	151847.69+551154.24	BHB	18669	604	784	4.52	0.11	0.15	-1.99	0.21	0.29	New
4504-55571-0996	082216.14+133822.54	He-sdB	32648	1296	1523	6.40			1.25	0.09	0.22	New
5064-55864-0668	220711.11+125755.59	He-sdO	53992	565	2078	6.11	0.05	0.16	2.00			New
4493-55585-0560	080833.77+180221.83	He-sdO	46857	966	2221	6.08	0.07	0.17	2.00			New
5200-56091-0132	161023.39+371315.74	He-sdO	47257	958	2218	6.17	0.08	0.17	2.00			New
5172-56071-0644	144321.34+402834.06	He-sdO	49283	987	2230	6.23	0.09	0.17	2.00			New



**Figure 10.** Hot subdwarfs, sdOs and sdBs. The Zero Age Horizontal Branch (ZAHB) and the Terminal Age Horizontal Branch (TAHB) plotted were calculated with solar composition models. In green we also plot a  $0.46816 M_{\odot}$ ,  $z=0.02$ , SM (shallow mixing hot flasher), DM (deep mixing hot flasher), and EHF (early hot flasher) models from [Battich et al. \(2018\)](#).

We also classified 15 793 as sdAs, which is only a spectroscopic class to flag objects with narrow H lines ([Kepler et al. 2016](#)). The classification carries no information on their origin or radius. The *Gaia* DR2 parallax determinations (next section) are somewhat uncertain for these objects (see Fig. 11), being in many cases of the same order of the error. This leads to a large scatter, placing objects above and below the main sequence, the latter a region compatible with low metallicity main sequence stars, or interacting binary remnants (e.g. [Maxted et al. 2014a](#); [Pelisoli, Kepler, & Koester 2018a](#); [Pelisoli et al. 2018b, 2019](#); [van Roestel et al. 2018](#); [Wang et al. 2018](#)). Some sdAs could be very low mass white dwarfs or pre-ELMs, but with the current parallax uncertainties this cannot be confirmed. We verified that by simply adding twice the parallax uncertainty to its value, over 95 per cent of the objects in the region between the main sequence and the white dwarf cooling track become compatible with the main sequence, suggesting that an inaccuracy of only  $2\text{-}\sigma$  in the parallax values is sufficient to explain this spread. Moreover, most of these objects have tangential velocities larger than 200 km/s, the criterion used for halo stars in the *Gaia* papers, providing further indication that they are compatible with low-mass main sequence stars in the halo. However, we caution that a high tangential velocity could also be observed for an object in a close binary, which is the case for the ELMs. In the next *Gaia* data releases, when the astrometry of binary objects and nearby contamination is more accurate, we will have a better understanding of the origin of these sdAs.

Fig. 11 shows the  $M_G$  vs.  $G_{BP} - G_{RP}$  diagram of the identified sdAs (colour coded by `parallax_over_error`), with a

tentative colour separation for canonical white dwarfs, (pre-)ELM candidates, and stars in the main sequence region and giant, which might be low-metallicity main sequence stars or binaries (e.g. [Istrate et al. 2016](#)).

## 4 GAIA

*Gaia* DR2 listed proper motion for 34 499 of our objects, but did not obtain parallax for 4 539 of these. The proper motions were mainly compatible with those from the USNO, APOG and GPS1, and the distances from the parallax are compatible with the spectroscopic distances we obtained. Fig. 12 shows a comparison of the distances estimated from *Gaia* parallax by [Bailer-Jones et al. \(2018\)](#) versus the distance estimated from our spectroscopic fits for DA stars, showing they are compatible but with a large scatter. The scatter is sometimes caused by the degeneracy of hot and cold solutions in the spectroscopic determination, and low  $S/N_g$ , but mainly above magnitude  $g=20$  or distances larger than 1.5 kpc.

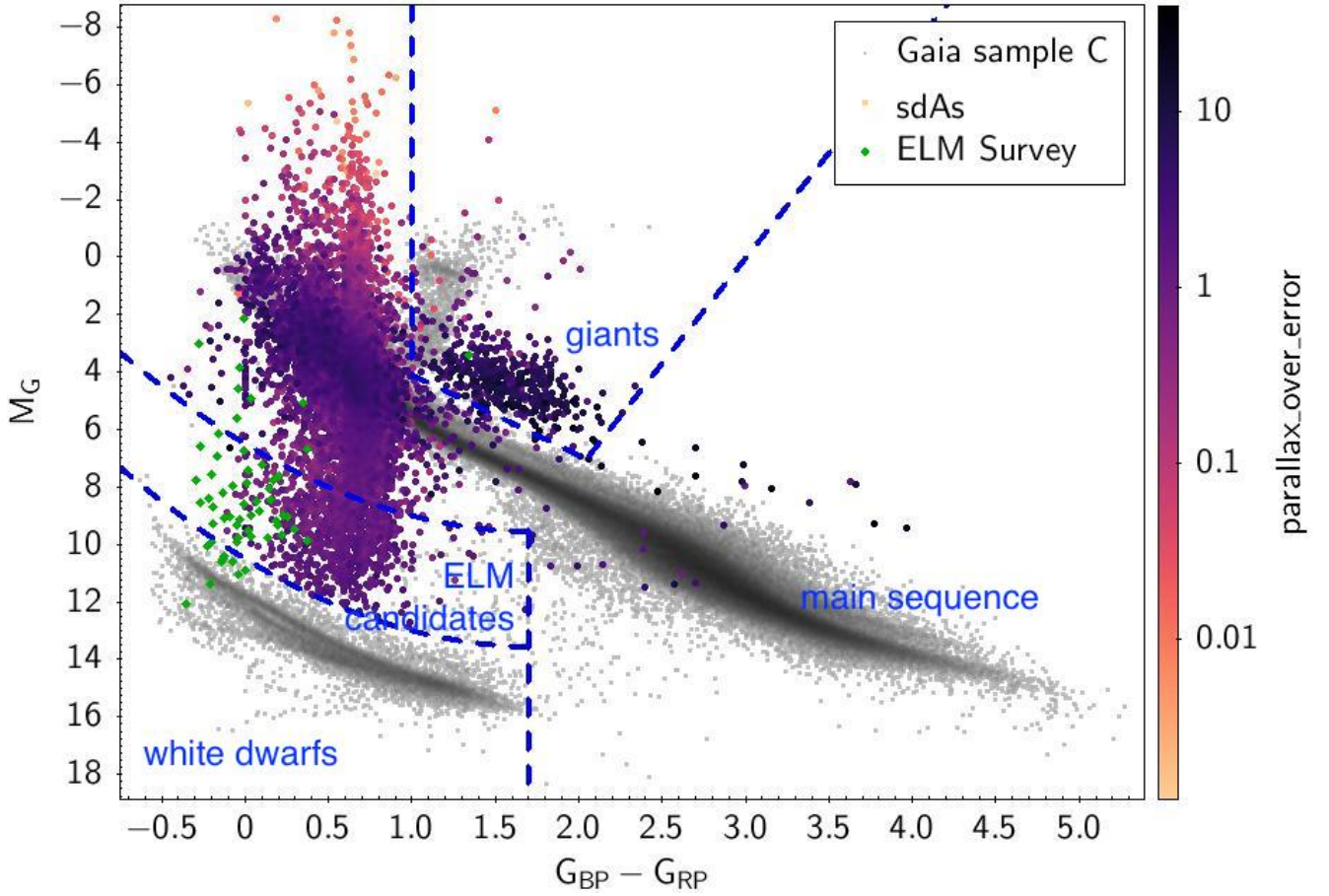
Fig. 13 shows the Hertzsprung-Russell colour-magnitude diagram of our DR14 sample, using only the *Gaia* measurements, totally independent of our spectroscopic measurements. They show DAs and DBs spread through the diagram, compatible with the [Kilic et al. \(2018\)](#) conclusion that the gap seen in [Gaia Collaboration et al. \(2018\)](#) white dwarf HR diagram is not mainly due to atmospheric composition. [El-Badry, Rix, & Weisz \(2018\)](#); [El-Badry et al. \(2018a\)](#); [El-Badry & Rix \(2018b\)](#) used the main sequence — white dwarf wide binaries with  $\text{parallax/error} > 20$  for  $\text{parallax} > 10$  mas ( $d < 100$  pc) and  $M_G < 14$ , corresponding to  $T_{\text{eff}} > 6000$  K, in *Gaia* DR2, to study the IFMR of white dwarfs, specially for initial masses  $< 4M_{\odot}$ , and conclude the bi-modality seen in the *Gaia* data constrains the data to multiple populations.

## 5 DISCUSSION

The systematic uncertainties in our atmospheric parameters derived from spectral analysis are minimized by the use of only SDSS spectra, i.e., same telescope and only two spectrographs (SDSS and BOSS), and fitting all the spectra with the same models and fitting technique.

[Gentile Fusillo et al. \(2018\)](#) selected photometrically white dwarf candidates from the *Gaia* DR2 and classified those they matched to SDSS spectra in DR14, similar but a subset of our work. We matched their catalogue and we did not miss any star they classified, but we do include other objects they did not classify, because of their selection criteria.

[Rolland, Bergeron, & Fontaine \(2018\)](#) analysed 115 helium-line DBs and 28 cool He-rich hydrogen-line DAs through  $S/N \geq 50$  spectra and concluded 63% of the DBs show hydrogen lines. [Koester & Kepler \(2015\)](#), using  $S/N_g \approx 20$  SDSS spectra, measured 75% DBs show hydrogen and speculated all DBs show hydrogen, if observed at high resolution and  $S/N$ . The surface gravity obtained with fits of pure He, for DBs containing H, and of pure H for DAs containing He, are overestimated, because of the extra particle pressure. [Rolland, Bergeron, & Fontaine \(2018\)](#) conclude only if  $M_H \geq 10^{-6} M_{*}$  H will not mix with the underlying He



**Figure 11.** sdAs (colour-coded according to `parallax_over_error`) separated using their *Gaia* absolute magnitude and colour. They extend from the white dwarf cooling region, binary region, through the low metallicity main sequence, to the giant phase. As a comparison, we also show the sample C of [Lindgren et al. \(2018\)](#), consisting of solar neighbourhood stars (within 100 pc) with clean parallax, and the ELMs of [Brown et al. \(2016\)](#)

layer by convective mixing at low effective temperatures. In our mean mass determination, we only included DBs hotter than  $T_{\text{eff}} \geq 16000$  K and that we did not see any contamination, but it is limited by our signal-to-noise and resolution. We fitted 3171  $S/N \geq 20$  DR14 spectra for DAs and 405 DBs for the white dwarfs selected by [Gentile Fusillo et al. \(2018\)](#), applying 3D corrections for both DAs and DBs, as we did, and compared to those they obtain from the *Gaia* photometry and parallax, concluding the agreement is good, for DAs. They concluded the DA and DB and DBAs mean masses obtained from the *Gaia* data match within 2%, but their Figs. 4, 5 and 12 show the disagreement for DBs, between spectroscopy and *Gaia* parallaxes is *larger* when the pure He 3D corrections are applied. As discussed in section 3.1, the introduction of the pure 3D correction for DBs is the cause of the reduction in the mean mass of DBs, and it is probably not real. [Ourique et al. \(2019\)](#) show there is strong evidence for spectral evolution with effective temperature.

[Latour et al. \(2018\)](#) analysed the hot subdwarfs of the globular cluster  $\omega$  Cen, and found a ratio of 26% sdBs ( $T_{\text{eff}} \leq 30,000$  K), 10% sdOs ( $T_{\text{eff}} \geq 42,000$  K), and the majority as sdBs (intermediate  $T_{\text{eff}}$ ). They also found the majority of

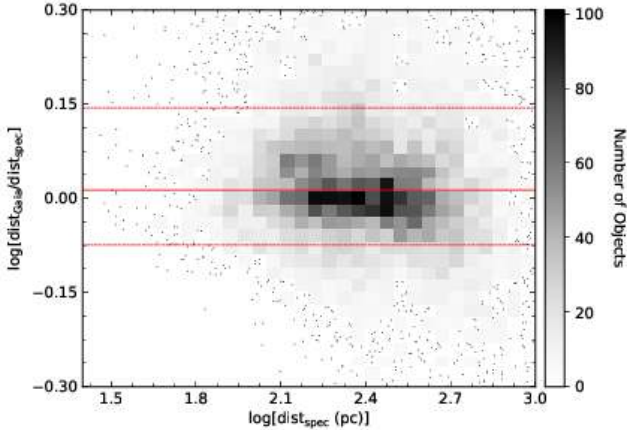
their sdOBs were helium-enriched, without a counterpart in Galactic field, while we found 33/128=26% of sdOBs are He-sdOBs.

## 6 CONCLUSIONS

We extended our search of white dwarf and subdwarf stars to SDSS DR14. In addition to searching all spectra with significant proper motion for new white dwarfs, we also fitted known DAs and DBs that fell in our selection criteria. The SDSS flux calibration is based on hundreds of comparison stars and in general more accurate than those derived from single night observations. We fitted the spectra of highest signal-to-noise for each star, taking into account that SDSS re-observes fields and improves the quality of the spectra. Our classifications are independent from previous classifications, and should be considered improvements.

Of the total 37053 objects in our Table 2, only 6 per cent come from plates obtained after DR12, but only 13927 are in the SDSS DR 7 to DR 12 catalogues. The DR7 to DR12 catalogues contain 35590 stars, including 29262 DAs, so our catalogues are not a subset or complete sets, but com-





**Figure 12.** Distances for DA white dwarfs in our sample, estimated from the Gaia parallax uncertainty distribution, compared with the distance calculated from the spectroscopic distance modulus. The solid red line represent the median. The lower and upper dashed red lines represent, respectively, the 16 and 84 percentiles. The points represents bins with less than 5 objects. We did not use a Gaia DR2 parallax precision limit in this plot, or used the parallax to select the best spectroscopic solution. The distances from the parallax are compatible with the spectroscopic distances we obtained given the large error bars.

plementary. The total number of unique stars in [Kleinman et al. \(2013\)](#); [Kepler et al. \(2015, 2016\)](#) and this DR14 catalogue is 52 299, with 28 681 DAs, 2287 DCs, 2148 DBs, 1126 DZs, 572 DQs, 137 DOs, 4 DS, 396 sdB, 410 sdOs, and 324 CVs.

For the first time we include 3D convection corrections to the derived effective temperatures of DBs, in addition to DAs. The obtained mean masses for DAs and DBs are lower than any previous determinations. For DAs, the main difference was the inclusion of more DAs cooler than  $T_{\text{eff}} = 10\,000$  K, which show substantially smaller masses, while for DBs the inclusion of the convection correction was the main difference. ? show the disagreement between the spectroscopic determinations and the Gaia parallaxes and colours increases when the 3D correction is applied.

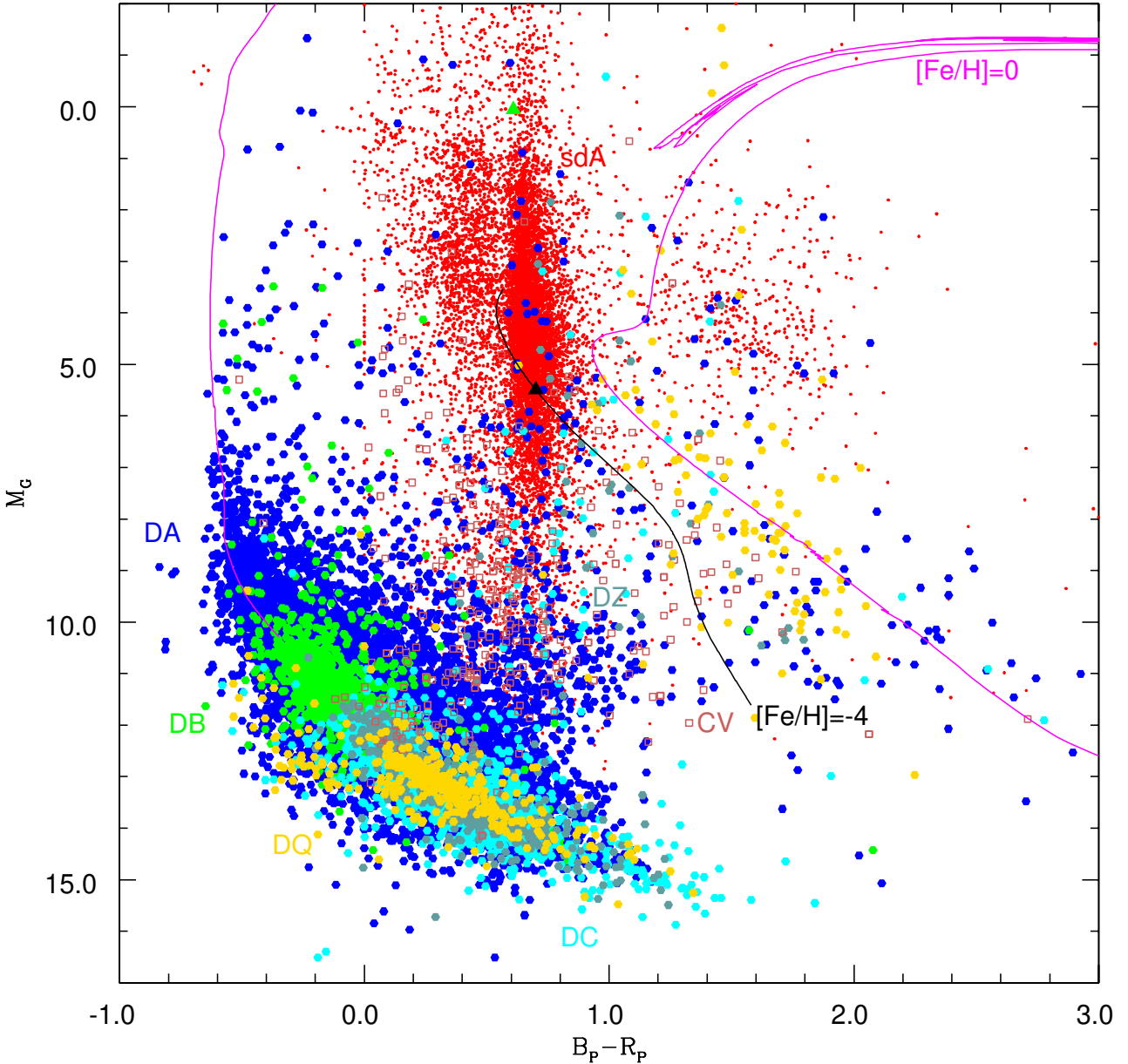
The Gaia distances and colours show there is large spread in the region between cool white dwarfs and cool main sequence stars. Due to the considerable uncertainty in the parallax (of the same order of the parallax itself for most stars in this region), a reliable separation between different types of sdAs is not possible. This spread causes many stars to be in the region between the main sequence and the white dwarf cooling range, which is compatible with interacting binary evolution. This region is occupied by known sdBs, sdOs, CVs, and WD+MS binaries. The parallax uncertainties suggest most (> 95 per cent) of the sdAs in this intermediary region are consistent with low-mass metal-poor halo stars, but a few could be products of binary evolution such as ELMs.

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**Figure 13.** Colour  $\times$  magnitude diagram of our sample, from Gaia distances and colours. The lines are 10 Gyr MIST isochrones with solar metallicity and  $[\text{Fe}/\text{H}]=-4$  (Choi et al. 2018). We also included two triangles, the upper one (green) with  $T_{\text{eff}} = 6000$  K, 10 Gyr,  $[\text{Fe}/\text{H}]=-2.5$ , off the main sequence, and the lower one (black), for  $[\text{Fe}/\text{H}]=-4$ , still on the main sequence, for reference, from the MIST models.

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