# NGA-West 2 Equations for Predicting PGA, PGV, and 5%-Damped PSA for Shallow Crustal Earthquakes

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We provide ground-motion prediction equations for computing medians and standard deviations of average horizontal component intensity measures (IMs) for shallow crustal earthquakes in active tectonic regions. The equations were derived from a global database with  $\mathbf{M}$  3.0-7.9 events. We derived equations for the primary  $\mathbf{M}$ - and distance-dependence of the IMs after fixing the  $V_{s30}$ -based nonlinear site term from a parallel NGA-West 2 study. We then evaluated additional effects using mixed effects residuals analysis, which revealed no trends with source depth over the  $\mathbf{M}$  range of interest, indistinct Class 1 and 2 event IMs, and basin depth effects that increase and decrease long-period IMs for depths larger and smaller, respectively, than means from regional  $V_{s30}$ -depth relations. Our aleatory variability model captures decreasing between-event variability with  $\mathbf{M}$ , as well as within-event variability that increases or decreases with  $\mathbf{M}$  depending on period, increases with distance, and decreases for soft sites.

# **INTRODUCTION**

Ground-motion prediction equations (GMPEs) are used in seismic hazard applications to specify the expected levels of shaking as a function of predictor variables such as earthquake magnitude, site-to-source distance, and site parameters. GMPEs for active crustal regions are typically developed from an empirical regression of observed amplitudes against an available set of predictor variables (Douglas, 2003, 2011).

In this paper, we present GMPEs developed as part of the NGA-West 2 project [Bozorgnia et al., 2014]. As with the other NGA-West 2 GMPEs, we use the database described by Ancheta et al. [2014] in which ground motions are taken as the average

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horizontal component (as defined by Boore, 2010) and the intensity measures (IMs) consist of peak ground acceleration and velocity (*PGA*, *PGV*) as well as 5% damped pseudo-spectral acceleration (*PSA*) for periods ranging from 0.01 to 10 s.

We used a three-phase model building approach that strikes a balance between prediction accuracy and simplicity of form and application. Our philosophy was as follows: The primary variables that control ground motion at a site are earthquake moment magnitude M (the primary source variable), distance to the fault (the primary path variable), and time-weighted average shear-wave velocity over the upper 30 m of the profile  $V_{\rm S30}$  (the primary site variable). After constraining site response and some additional effects based on an initial analysis of the data, in what we call Phase 1 of our study, we performed classical two-stage regressions to develop base-case GMPEs based on a simple functional form using just M, distance, and fault type (Phase 2). We then performed mixed effects analysis of residuals (defined by the difference, in natural log units, between the observed and predicted amplitude of motion) and examined trends of between- or within-event residuals against secondary predictor variables. These secondary parameters include the region in which the event occurs, whether the source is Class 1 or 2 (hereafter CL1 and CL2) per Wooddell and Abrahamson [2014] (roughly mainshocks or aftershocks, respectively), various source depths, and basin depth. We assessed the extent to which these additional variables improve the accuracy of the GMPEs in a way that is both statistically significant and practically meaningful. We implemented the inclusion of secondary variables, where warranted, as optional adjustment factors that may be applied to the base-case GMPEs. In this way, we aimed to ensure that our GMPEs are centered for the general case of future events in regions for which site-specific path and site parameters may be unknown.

Our GMPEs are generally applicable for earthquakes of **M** 3.0 to 8.5 (except for lack of constraint for **M**>7 normal slip events), at distances from 0 to 400 km, at sites having  $V_{S30}$  in the range from 150 m/s to 1500 m/s, and for spectral periods (T) of 0.01–10 s. We considered regional variability in source, path and site effects, but did not address directivity effects.

We first review prior work that helps establish the motivation for this research. We then discuss the data and predictor variables used in the analysis, which is followed by a section giving the recommended equations. Subsequent sections describe the derivation of the coefficients in the GMPEs, compare our results to prior studies, and give guidelines for application. Because of space limitations, some details of our results are deferred to Boore et

al. [2013; hereafter BSSA13]. Tables of coefficients can be found in Electronic Supplement materials. To facilitate application of the GMPEs, Fortran programs and routines for other software platforms such as Matlab and Excel can be found at <a href="http://www.daveboore.com/software\_online.html">http://www.daveboore.com/software\_online.html</a> and are forthcoming at the PEER web site (<a href="http://peer.berkeley.edu">http://peer.berkeley.edu</a>).

### PRIOR RELATED WORK

The research described in this paper and BSSA13 builds on the GMPEs of Boore and Atkinson [2008] (BA08), which were part of the NGA-West 1 project [Power et al. 2008 and references therein]. The NGA-West 2 project was formed to take advantage of new data available since NGA-West 1, address some weaknesses in the NGA-West 1 database, and allow the developers to reconsider their functional forms.

One improvement needed to the NGA-West 1 equations involved adding data at small-to-moderate magnitudes. The need to enrich the database at the low-magnitude end to ensure robust magnitude scaling was highlighted by several studies [Atkinson and Morrison 2009; Chiou et al. 2010; Atkinson and Boore 2011], and two of the NGA-West 1 developers provided amendments to improve their equation performance at low magnitudes [Chiou et al. 2010; Atkinson and Boore 2011]; the revised Boore and Atkinson GMPEs that account for this adjustment are referred to as BA08'. Studies by Scasserra et al. [2009], Atkinson and Morrison [2009], and Chiou et al. [2010] also pointed to the need to consider regional variability of path effects, as the attenuation of motions with distance is faster in some active regions than in others.

Finally, the richer database available for NGA-West 2 allows us to improve on prior work by considering additional variables that could not previously be adequately resolved. However, we maintain the same basic functions for the equations as used in BA08.

## **DATABASE**

### **DATA SOURCES**

We use a NGA-West 2 flatfile that contains site and source information, along with distance parameters and computed ground-motion intensity measures (IMs) (Ancheta et al., 2014). Various versions of the flatfile were used during GMPE development as the file evolved (details in BSSA13).

We used variable subsets of the data for different analysis phases. Consistent criteria (i.e., applied in all analysis phases) were applied with respect to the following considerations:

- Availability of metadata: We required the presence of magnitude, distance, and site metadata in order to include a record in the analysis.
- Co-located stations: We do not use more than one record when multiple records from the same earthquake were recorded at the same site (e.g. in a differential array or different sensors at the same site).
- Single-component motions: We only use records having two horizontal-component recordings.
- Inappropriate crustal conditions: We exclude recordings from earthquakes originating in oceanic crust or in stable continental regions.
- Soil-structure interaction (SSI): We exclude records thought to not reasonably reflect free-field conditions as a result of SSI that potentially significantly affects the ground motions at the instrument. Our primary guide to stations not to be used was the Geomatrix 1<sup>st</sup> letter code, available in the flatfile, as indicated in Table 2.1 of BSSA13.
- Proprietary data: Data not publicly available are not used.
- Problems with record: Based on visual inspection, we exclude records with Striggers, second trigger (i.e., two time series from the same event due to consecutive triggers), noisy records, or records with time step problems.
- Usable frequency range: We only use PSAs for periods less than the inverse of the lowest usable frequency, as specified in the flatfile; we did not exclude any records based on the high frequency-filter used in the record processing (Douglas and Boore, 2011).
- Data were screened using **M**, distance, and recording-type criteria, as shown in Figure 1. These criteria are intended to minimize potential sampling bias, which can occur at large fault distances where ground motions have low amplitudes and instruments may only be triggered by unusually strong shaking. Including such records would bias the predicted distance decay of the ground motion towards slower distance attenuation than is present in the real motions.
- An earthquake is only considered if it has at least four recordings within 80 km after applying the other selection criteria.

## **GROUND-MOTION INTENSITY MEASURES**

The ground-motion IMs comprising the dependent variables of the GMPEs include horizontal component *PGA*, *PGV*, and 5%-damped *PSA*. These IMs were computed using the RotD50 parameter [Boore 2010], which is the median single-component horizontal ground motion across all non-redundant azimuths. This is a departure from the GMRotI50 parameter

used in BA08. Shahi and Baker [2014] describe how the maximum component can be computed from RotD50; Boore [2010] describe how RotD50 compares with GMRotI50.

We do not include equations for peak ground displacement (*PGD*), which we believe to be too sensitive to the low-cut filters used in the data processing to be a stable measure of ground shaking [details in Appendix C of Boore and Atkinson, 2007].

### PREDICTOR VARIABLES

The main predictor variables used in our regression analyses are moment magnitude  $\mathbf{M}$ ,  $R_{JB}$  distance (closest distance to the surface projection of the fault plane), site parameter  $V_{S30}$ , and fault type. Fault type represents the classification of events as strike slip (SS), normal slip (NS), or reverse slip (RS), based on the plunge of the P- and T-axes (see Table 2.2 in BSSA13). Almost the same fault type assignments would be obtained using rake angle, with SS events being defined as events with rake angles within 30 degrees of horizontal, and RS and NS being defined for positive and negative rake angles not within 30 degrees of horizontal, respectively. Secondary parameters considered in residuals analysis include:

- Depth to top of rupture  $Z_{tor}$  and hypocentral depth  $Z_{hypo}$
- Basin depth  $z_1$  (depth from the ground surface to the 1.0 km/s shear-wave horizon).
- Event type, being either Class 1 (CL1: mainshocks) or Class 2 (CL2: aftershocks), using the minimum centroid  $R_{JB}$  separation of 10 km from Wooddell and Abrahamson [2014] based on subjective interpretation of results from exploratory analysis.

We did not consider hanging wall effects, as our use of the  $R_{JB}$  distance measure implicitly accounts for larger motions over the hanging wall (Donahue and Abrahamson, 2014). Each of the predictor variables was taken from the NGA-West 2 database flatfile.

# DISTRIBUTION OF DATA BY M, $R_{\text{JB}}\text{, FAULT TYPE, AND }V_{\text{S30}}$

The M and  $R_{JB}$  distribution of data used to develop our GMPEs is shown in Figure 2, differentiated by fault type. There are many more small magnitude data than used in BA08, as well as data from a few new large events such as the 2008 M7.9 Wenchuan, China, earthquake. The magnitude range is widest for SS earthquakes and narrowest for NS earthquakes, suggesting that magnitude scaling will be better determined for SS than for NS—a problem we circumvented by using common magnitude scaling for all fault types.

Figure 3 shows the numbers of recordings and earthquakes used in equation development, differentiated by fault type. There is a rapid decrease in available data for periods longer than several seconds, but there are many more data available at the longest periods than in BA08. Figure 4 shows the data distribution by  $V_{S30}$ ; most of the data are for soil and soft rock sites (NEHRP categories C and D) but there are markedly more data for rock sites (mostly B) than in BA08. The  $V_{S30}$  data include measured and inferred velocities (Seyhan et al., 2014).

The data distributions over the predictor variable space necessarily influence the GMPEs. Note in particular the lack of data at close distances for small earthquakes. This means that the near-source ground motions for small events will not be constrained by observations. In addition, there are many fewer small **M** data for long periods than for short periods, meaning that the small-earthquake **M** scaling will be less well determined for long periods.

# THE GROUND-MOTION PREDICTION EQUATIONS

As with Boore et al. (1997) and BA08, we sought simple functions for our GMPEs, with the smallest number of predictor variables required to provide a reasonable fit to the data. We call these the "base-case GMPEs". We subsequently derived adjustment factors for these base-case GMPEs to account for additional predictor variables. The selection of functions was heavily guided by subjective inspection and study of nonparametric plots of data such as in Figure 5, which shows the magnitude and distance dependence of PSA at four periods for strike slip events. The data have been adjusted to  $V_{S30} = 760$  m/s, using the site amplification function of Seyhan and Stewart (2014; hereafter SS14). Inspection of these and similar plots revealed several features that the functions used for the GMPEs must accommodate: M-dependent geometric spreading; anelastic attenuation effects evident from curvature in the decay of log ground motions versus log distance for distances beyond about 80 km; and strongly nonlinear (and period dependent) magnitude dependence of amplitude scaling at a fixed distance.

Our predictions of ground motion are given by the following equation:

 $\ln Y = F_E \left( \mathbf{M}, mech \right) + F_P \left( R_{JB}, \mathbf{M}, region \right) + F_S \left( V_{S30}, R_{JB}, \mathbf{M}, z_1 \right) + \varepsilon_n \sigma \left( \mathbf{M}, R_{JB}, V_{S30} \right) (1)$  where  $\ln Y$  represents the natural logarithm of a ground-motion IM (PGA, PGV, or PSA);  $F_E$ ,  $F_P$ , and  $F_S$  represent functions for source ("E" for "event"), path ("P"), and site ("S") effects, respectively;  $\varepsilon_n$  is the fractional number of standard deviations of a single predicted

value of  $\ln Y$  away from the mean (e.g.,  $\varepsilon_n = -1.5$  is 1.5 standard deviations smaller than the mean); and  $\sigma$  is the total standard deviation of the model. The predictor variables are  $\mathbf{M}$ , mech,  $R_{JB}$  (in km),  $V_{S30}$  (in m/s), and  $z_1$  (in km). Parameter mech = 0, 1, 2, and 3 for unspecified, SS, NS, and RS, respectively. The units of PGA and PSA are g; the units of PGV are cm/s.

Eqn. (1) is a combination of a base-case function and adjustments derived from analysis of residuals. These equations are given separately in BSSA13, but are combined here into a single equation.

## ELEMENTS OF MEDIAN MODEL (SOURCE, PATH, AND SITE FUNCTIONS)

The source (event) function is given by:

$$F_{E}(\mathbf{M}, mech) = \begin{cases} e_{0}U + e_{1}SS + e_{2}NS + e_{3}RS + e_{4}(\mathbf{M} - \mathbf{M}_{h}) + e_{5}(\mathbf{M} - \mathbf{M}_{h})^{2} & \mathbf{M} \leq \mathbf{M}_{h} \\ e_{0}U + e_{1}SS + e_{2}NS + e_{3}RS + e_{6}(\mathbf{M} - \mathbf{M}_{h}) & \mathbf{M} > \mathbf{M}_{h} \end{cases}$$
(2)

where U, SS, NS, and RS are dummy variables, with a value of 1 to specify unspecified, strike-slip, normal-slip, and reverse-slip fault types, respectively, and 0 if the fault type is unspecified; the hinge magnitude  $\mathbf{M}_h$  is period-dependent, and  $e_0$  to  $e_6$  are model coefficients.

The path function is given by:

$$F_{P}\left(R_{JB}, \mathbf{M}, region\right) = \left[c_{1} + c_{2}\left(\mathbf{M} - \mathbf{M}_{ref}\right)\right] \ln\left(R / R_{ref}\right) + \left(c_{3} + \Delta c_{3}\right)\left(R - R_{ref}\right)$$
(3)

where

$$R = \sqrt{R_{JB}^{2} + h^{2}} \tag{4}$$

and  $c_1$ ,  $c_2$ ,  $c_3$ ,  $\Delta c_3$ ,  $\mathbf{M}_{ref}$ ,  $R_{ref}$  and h are model coefficients. Parameter  $\Delta c_3$  depends on the geographic region, as discussed later.

The site function is given by:

$$F_{S}(V_{S30}, \mathbf{M}, R_{JB}, z_{1}) = \ln(F_{lin}) + \ln(F_{nl}) + F_{\delta z_{1}}(\delta z_{1})$$
(5)

where  $F_{lin}$  represents the linear component of site amplification,  $F_{nl}$  represents the nonlinear component of site amplification, and  $F_{\delta z_l}$  represents the effects of basin depth. Justification for the functional form of terms  $F_{lin}$  and  $F_{nl}$  is given in SS14.

The linear component of the site amplification model  $(F_{lin})$  describes the scaling of ground motion with  $V_{s30}$  for linear soil response conditions (i.e., small strains) as follows:

$$\ln\left(F_{lin}\right) = \begin{cases}
c \ln\left(\frac{V_{S30}}{V_{ref}}\right) & V_{S30} \leq V_{c} \\
c \ln\left(\frac{V_{c}}{V_{ref}}\right) & V_{S30} > V_{c}
\end{cases}$$
(6)

where c describes the  $V_{S30}$ -scaling,  $V_c$  is the limiting velocity beyond which ground motions no longer scale with  $V_{S30}$ , and  $V_{ref}$  is the site condition for which the amplification is unity (taken as 760 m/s). Parameters c and  $V_c$  are period-dependent but not region-dependent (details in SS14). The function for the  $F_{nl}$  term is as follows:

$$\ln(F_{nl}) = f_1 + f_2 \ln\left(\frac{PGA_r + f_3}{f_3}\right) \tag{7}$$

where  $f_1$ ,  $f_2$ , and  $f_3$  are model coefficients and  $PGA_r$  is the median peak horizontal acceleration for reference rock [for a given  $R_{JB}$ , M, and region,  $PGA_r$  is obtained by evaluating Eqn. (1) with  $V_{S30} = 760 \text{ m/s}$ ]. Parameter  $f_2$  represents the degree of nonlinearity as a function of  $V_{S30}$  and is formulated as:

$$f_2 = f_4 \left[ \exp\left\{ f_5 \left( \min\left( V_{s30}, 760 \right) - 360 \right) \right\} - \exp\left\{ f_5 \left( 760 - 360 \right) \right\} \right]$$
 (8)

where  $f_4$  and  $f_5$  are model coefficients.

The term  $F_{\delta z_1}$  is an adjustment to the base model to consider the effects of basin depth on ground-motion amplitude. This adjustment is as follows:

$$F_{\delta Z_1}(\delta z_1) = \begin{cases} 0 & T < 0.65 \\ f_6 \delta z_1 & T \ge 0.65 & \delta z_1 \le f_7/f_6 \\ f_7 & T \ge 0.65 & \delta z_1 > f_7/f_6 \end{cases}$$
(9)

where  $f_6$  and  $f_7$  are model coefficients,  $f_7/f_6$  has units of km, and  $\delta z_1$  is computed as:

$$\delta z_1 = z_1 - \mu_{z_1}(V_{S30}) \tag{10}$$

where  $\mu_{z_1}(V_{S30})$  is the prediction of an empirical model relating  $z_1$  to  $V_{S30}$ . For convenience, we give below relations for  $\mu_{z_1}(V_{S30})$  derived from data in California and Japan (B. Chiou, personal communication, 2013):

California: 
$$\ln(\mu_{z1}) = \frac{-7.15}{4} \ln\left(\frac{V_{S30}^4 + 570.94^4}{1360^4 + 570.94^4}\right)$$
 (11)

Japan: 
$$\ln(\mu_{z1}) = \frac{-5.23}{2} \ln\left(\frac{V_{s30}^2 + 412.39^2}{1360^2 + 412.39^2}\right)$$
 (12)

where  $\mu_{Z1}$  and  $V_{S30}$  have units of km and m/s, respectively. These relationships can be used to estimate  $z_1$  when only  $V_{S30}$  is available. They also provide a convenient estimate of a representative depth for any given  $V_{S30}$ . We realize that in many applications  $z_1$  may be unknown; in such cases we recommend using the default value of  $\delta z_1 = 0.0$ , which turns off this adjustment factor (i.e.,  $F_{\delta z_1} = 0$ ). This is a reasonable default condition because the remaining elements of the model are 'centered' on a condition of no  $F_{\delta z_1}$  adjustment as described further below.

### ALEATORY-UNCERTAINTY FUNCTION

The total standard deviation  $\sigma$  is partitioned into components that represent betweenevent variability ( $\tau$ ) and within-event variability ( $\phi$ ) as follows:

$$\sigma(\mathbf{M}, R_{JB}, V_{S30}) = \sqrt{\phi^2(\mathbf{M}, R_{JB}, V_{S30}) + \tau^2(\mathbf{M})}$$

$$\tag{13}$$

The M-dependent between-event standard deviation  $\tau$  is given by

$$\tau(M) = \begin{cases} \tau_1 & \mathbf{M} \le 4.5 \\ \tau_1 + (\tau_2 - \tau_1)(\mathbf{M} - 4.5) & 4.5 < \mathbf{M} < 5.5 \\ \tau_2 & \mathbf{M} \ge 5.5 \end{cases}$$
(14)

and the M-,  $R_{JB}$ -, and  $V_{S30}$ -dependent within-event standard deviation  $\phi$  is given by

$$\phi(\mathbf{M}, R_{JB}, V_{S30}) = \begin{cases} \phi(\mathbf{M}, R_{JB}) & V_{S30} \ge V_{2} \\ \phi(\mathbf{M}, R_{JB}) - \Delta \phi_{V} \left( \frac{\ln(V_{2}/V_{S30})}{\ln(V_{2}/V_{1})} \right) & V_{1} \le V_{S30} \le V_{2} \\ \phi(\mathbf{M}, R_{JB}) - \Delta \phi_{V} & V_{S30} \le V_{1} \end{cases}$$
(15)

where

$$\phi(\mathbf{M}, R_{JB}) = \begin{cases} \phi(\mathbf{M}) & R_{JB} \leq R_{1} \\ \phi(\mathbf{M}) + \Delta \phi_{R} \left( \frac{\ln(R_{JB}/R_{1})}{\ln(R_{2}/R_{1})} \right) & R_{1} < R_{JB} \leq R_{2} \\ \phi(\mathbf{M}) + \Delta \phi_{R} & R_{JB} > R_{2} \end{cases}$$
(16)

and where the **M**-dependent  $\phi$  is given by:

$$\phi(\mathbf{M}) = \begin{cases} \phi_1 & \mathbf{M} \le 4.5 \\ \phi_1 + (\phi_2 - \phi_1)(\mathbf{M} - 4.5) & 4.5 < \mathbf{M} < 5.5 \\ \phi_2 & \mathbf{M} \ge 5.5 \end{cases}$$
(17)

We recognize that this is a relatively complex form for aleatory uncertainty, being dependent on  $\mathbf{M}$ ,  $R_{JB}$ , and  $V_{S30}$ . We comment further on this subsequently in the paper.

# DEVELOPMENT AND INTERPRETATION OF REGRESSION RESULTS

We developed our GMPEs in three phases. In Phase 1, we analyzed subsets of data and simulation results to evaluate elements of the model that would not be well-constrained if left as free parameters in the regression. Model elements evaluated in this way are  $c_3$  (for apparent anelastic attenuation) and  $F_S$  (for site response), which are then fixed in subsequent analysis phases. Phase 2 comprised the main regression for the base-case model. As in BA08, this was a two-stage regression, the first solving for path function coefficients, and the second stage solving for source function coefficients. Phase 3 consisted of mixed-effects regression analysis to check model performance and to develop adjustment factors for various secondary parameters beyond the base-case predictor variables of  $R_{JB}$ , M, mech, and  $V_{S30}$ . The standard deviation model was also developed from Phase 3 analysis.

As described by SS14, the  $V_{\rm S30}$ -dependent site amplification model (terms  $F_{\rm lin}$  and  $F_{\rm nl}$ ) was developed in an iterative manner with our GMPEs; i.e., Phase 2 results were used as the basis for the analysis establishing the site coefficients (Phase 1), which were then used to redo the Phase 2 analysis, etc.

### PHASE 1: SETTING OF FIXED PARAMETERS

There were three parameters and/or functions determined in Phase 1 analyses that were held fixed in Phases 2 and 3: the apparent anelastic attenuation coefficient  $c_3$  and the site amplification function. Development of the site amplification (not including the basin adjustment) is discussed by SS14 and is not repeated here. Hence in this section we focus on determination of apparent anelastic attenuation coefficient  $c_3$ .

Due to trade-offs between apparent geometric and apparent anelastic attenuation, regression cannot simultaneously determine both robustly; this arises because we cannot distinguish between the slope and the curvature of the distance decay from data with significant scatter. Accordingly, we undertook regressions to constrain the apparent anelastic attenuation term,  $c_3$ , using the large inventory of data from small events ( $\mathbf{M} \leq 5.0$ ) in California, which are now included in the flatfile. Low-magnitude earthquakes were chosen to minimize complexities in the data associated with possible finite fault effects and nonlinear site effects. We applied the site factors from SS14 to adjust each observation to a reference  $V_{S30}$  of 760 m/s (denoted  $\ln Y_{ij}$ ). The data were then grouped into bins 0.5 magnitude units in width and regressed using the following expression, which does not include an  $\mathbf{M}$ -dependent geometric spreading term:

$$\ln Y_{ij} = \eta_i' + c_1' \ln(R/R_{ref}) + c_3(R - R_{ref})$$
(18)

where  $\eta'_i$  is the event term for event i, j indicates a particular observation (and is implicitly contained in the distance R),  $R_{ref} = 1.0 \,\mathrm{km}$ , and  $c'_1$  and  $c_3$  are parameters set by the regression. The  $c'_1$  term represents the apparent geometric spreading for the  $\mathbf{M}$  bin; it would be expected to change with  $\mathbf{M}$ . The prime (') is used on the event term and apparent geometric spreading term to indicate these are associated with the present analyses of binned data and are distinct from the Phase 2 and 3 regressions.

As suggested by the low  $\mathbf{M}$  bins of Figure 5 (greater details are provided in Figure 4.1 of BSSA13), high-frequency IMs exhibit substantial curvature (indicating negative  $c_3$ ) whereas the low-frequency data exhibit negligible curvature (nearly zero  $c_3$ ). The regressions using Eqn. (18) found  $c_3$  terms to be relatively independent of  $\mathbf{M}$ , which is expected if they represent anelastic attenuation effects properly ( $\mathbf{M}$ -dependence is contained in the  $c_1'$  term). These values of  $c_3$  were used in subsequent phases of work.

## PHASE 2: BASE-CASE REGRESSIONS

The objective of the two-stage Phase 2 analyses is to derive the coefficients for the  $F_P$  and  $F_E$  terms in Eqn. (1), with the exception of  $c_3$  (from Phase 1) and  $\Delta c_3$  (from Phase 3). The analyses were performed using the two-stage regression discussed by Joyner and Boore [1993, 1994]. In addition to the data selection criteria described previously, Stage 2 analyses also exclude CL 2 events (aftershocks) and data with  $R_{JB} > 80 \,\mathrm{km}$  (as described further below). Prior to Phase 2 regressions, we adjust all selected observations to the reference velocity of 760 m/s, using the SS14 site amplification model (excluding the basin term).

## **Stage 1 Analysis for Path Term**

In Stage 1, path coefficients are evaluated by regressing observations  $\ln Y_{ij}$  against the following base-case path relationship  $F_{P,B}$  (the base-case excludes  $\Delta c_3$ ):

$$F_{P,B}\left(R_{JB},\mathbf{M}\right) = \left(\overline{\ln Y}\right)_{:} + \left\lceil c_1 + c_2\left(\mathbf{M} - \mathbf{M}_{ref}\right)\right\rceil \ln\left(R/R_{ref}\right) + c_3\left(R - R_{ref}\right) \tag{19}$$

where  $\left(\overline{\ln Y}\right)_i$  represents average observations for event i adjusted to  $R=R_{ref}$ . As explained further in BSSA13, we set  $R_{ref}=1\,\mathrm{km}$  and  $\mathbf{M}_{ref}=4.5$ . With  $c_3$  constrained, these regressions establish  $c_I$ ,  $c_2$ , and h, as well as  $\left(\overline{\ln Y}\right)_i$  for each earthquake. Parameters  $c_1$  and  $c_2$  describe geometric spreading, with  $c_2$  capturing its  $\mathbf{M}$ -dependence. This process is complicated by the appearance of  $\mathbf{M}$  in both the path and source function; the resulting coupling led to unrealistic results in initial Stage 2 analyses whereby the  $\mathbf{M}$ -scaling was small, particularly for small  $\mathbf{M}$ . Following the suggestion of  $\mathbf{K}$ . Campbell (pers. communication, 2012), we recalculated Stage 1 regressions using data for  $R_{JB} \leq 80\,\mathrm{km}$  (still including fixed values of  $c_3$ ), which stabilized the results.

# Stage 2 Analysis for Source Term

In Stage 2, the  $(\overline{\ln Y})_i$  terms from Stage 1 (subsequently referred to as  $\overline{\ln Y}$ ) were used in weighted regressions to evaluate source terms  $e_0$  to  $e_6$ , which control M-scaling and source type effects. The function for the source term (Eqn. 2), which was arrived at after many trials, consists of two polynomials hinged at  $\mathbf{M}_h$ ; a quadratic for  $\mathbf{M} < \mathbf{M}_h$  and a linear function for  $\mathbf{M} > \mathbf{M}_h$ . The hinge magnitude  $\mathbf{M}_h$  was selected from visual inspection of many plots similar to those in Figure 6. Unlike BA08, which used a fixed  $\mathbf{M}_h = 6.75$ , we transition  $\mathbf{M}_h$  from 5.5 for  $T < \sim 0.1$  s to 6.2 for  $T > \sim 0.4$  s. The major considerations in the selections of these values were ensuring robust scaling on both sides of the hinge, while allowing scaling behavior to be data-driven. Unlike BA08, we did not constrain the slope of the linear function  $(e_6)$  to be positive, resulting in negative slopes for high-frequency IMs, as shown in Figure 6. The negative slopes are suggestive of oversaturation, which has been implied by the data since NGA-West 1 and supported by some simulations (Schmedes and Archuletta, 2008). The negative slopes, however, do not result in IM decreases with increasing  $\mathbf{M}$  at close distances (i.e., there is no true oversaturation), which can be understood as follows:

- Oversaturation in the source function occurs at  $R = R_{ref} = 1 \text{ km}$ .
- Distance R (Eqn. 4) can never be less than the pseudo-depth h, but h is always greater than 4.0 km,
- Therefore, regardless of site location relative to the fault, the magnitude-dependent apparent geometrical spreading (Eqn. 3) affects predicted median motions. Those effects more than compensate for the apparent oversaturation from the source term (Eqn. 2).

The fault type coefficients in the Stage 2 regression were computed simultaneously with the **M**-dependence. The coefficients for unspecified fault type  $(e_0)$  were then computed as a weighted average of the SS, NS, and RS coefficients  $(e_1, e_2, \text{ and } e_3)$  (the weights are given in BSSA13).

## **Smoothing of Coefficients**

Coefficients were obtained separately for each period using the above two-stage regression analysis. Results are generally smooth, with the exception of jaggedness for large and small magnitudes at periods exceeding about 2 s. This jaggedness is probably due to the decrease in number of recordings available at longer periods (Figure 3). Accordingly, we

undertook a smoothing process in which we first smoothed the h parameter, re-regressed the model using those values, then computed 11-pt running means of the resulting coefficients.

# Regression Results and Comparison to BA08'

Some well-known features of ground-motion variations with the considered predictor variables are shown in plots of the base-case GMPEs in Figures 7 and 8. From the PGA plot in Figure 7, we see pronounced M-scaling of the motions for M < 6, as shown by the spread of the medians, but very little sensitivity at larger M. Conversely, for long-period PSA, we see substantial M-scaling over the full range of magnitudes. The distance attenuation trends in Figure 7 indicate amplitude-saturation, with amplitudes being nearly constant (flat) for distances  $R_{JB} < \sim 3$ —5 km. For  $R_{JB} > \sim 10$  km, the distance attenuation transitions to a nearly linear slope for  $T > \sim 1$  s while for shorter periods apparent anelastic attenuation produces downward curvature. For short periods and  $R_{JB} > \sim 10$  km, the curves steepen as **M** decreases due to M-dependent geometrical spreading that may be associated with finite-fault effects (i.e., as M increases, geometrical spreading from the small portion of a fault closest to the site is partially offset by contributions from other parts of the finite fault; Andrews, 2001) and duration effects. For the same amount of energy radiated from a source, the longer the duration, the smaller the peak amplitudes of the ground motion. Duration is made up of source and path contributions, which combine through summation. Path duration generally increases with distance, and is relatively more important than the source duration for smaller events. Therefore, the ground motions for smaller events will attenuate more rapidly with distance than for large events (Boore, 2003).

Also shown for comparative purposes in Figure 7 are median predictions of BA08'. The present medians are substantially smaller than those from BA08' for small **M** at  $R_{JB} < 10$  to 20 km and  $T < \sim 3.0$  s. For T = 10 s the medians are now substantially larger. The two situations noted (small magnitudes and long periods) correspond to the conditions having the greatest data increase relative to BA08'.

In Figure 8, many of these features are illustrated by the relative positions of the spectra. This figure is useful in that it shows the  $\mathbf{M}$  dependence of the predominant period  $(T_p)$ , defined as the period of the peak in the spectrum. For rock-like sites,  $T_p$  ranges from approximately 0.1 s for  $\mathbf{M}$  3 to 0.2 s for  $\mathbf{M} > 6$ . Note that for softer site conditions, corresponding to deeper sites,  $T_p$  increases to  $\sim 0.4$ –0.5 s due to site response effects. The

effect of the aforementioned smoothing is also shown in Figure 8 by comparing median *PSA* from smoothed and unsmoothed coefficients.

The 2008 M 7.9 Wenchuan earthquake has been debated regarding its suitability for use in GMPE development. As shown in Figure 9, if the Phase 2 regressions are repeated without that event, short period IMs are unchanged, but long period IMs increase at large M. As we see no justification for excluding data from the Wenchuan earthquake, our GMPEs are those developed with the data including Wenchuan. We show the comparison in Figure 9 only to answer the inevitable question of what influence the Wenchuan data have on our GMPEs.

## **PHASE 3: RESIDUALS ANALYSIS**

Phase 3 is comprised of mixed effects residuals analyses having two purposes: (1) to check that the base-case GMPEs developed through the Phase 1 and 2 analyses are not biased with respect to  $\mathbf{M}$ ,  $R_{JB}$ , or site parameters; and (2) to examine trends of residuals against parameters not considered in the Phase 1 and 2 analyses, including regional effects. We used the data selection criteria given in the *Data Sources* section above, which differ from Phase 2 by including CL2 events and data with  $R_{JB} > 80$  km (but still subject to the distance cut-offs given in Figure 1). This process resulted in some changes to the base-case equations, specifically introduction of the  $\Delta c_3$  coefficient in the  $F_p$  term (for regional anelastic attenuation effects) and the  $F_{\delta z_1}$  term for basin effects. The effects of CL2 source type and source depth were investigated but did not require model adjustments.

# **Methodology and Model Performance**

The methodology for the analysis of residuals employed here is similar to that described in Scasserra et al. [2009]. We begin by evaluating residuals between the data and the base-case GMPEs. Residuals are calculated as:

$$R_{ii} = \ln Y_{ii} - \mu_{ii} \left( \mathbf{M}, R_{JB}, V_{S30} \right) \tag{20}$$

Index *i* refers to the earthquake event and index *j* refers to the recording within event *i*. Term  $\mu_{ij}(\mathbf{M}, R_{JB}, V_{S30})$  represents the base-case GMPE median in natural log units. Hence,  $R_{ij}$  is the residual of data from recording *j* in event *i* as calculated using the base-case GMPEs.

The analysis of residuals with respect to M, distance, and site parameters requires between-event variations to be separated from within-event variations. This is accomplished

by performing a mixed effects regression [Abrahamson and Youngs 1992] of residuals according to the following function:

$$R_{ij} = c_k + \eta_i + \varepsilon_{ij} \tag{21}$$

where  $c_k$  represents a mean offset (or bias) of the data relative to GMPE k (we consider only the present set of GMPEs, so k is singular),  $\eta_i$  represents the event term for event i, and  $\varepsilon_{ij}$  represents the within-event residual for recording j in event i. Event terms are used to evaluate GMPE performance relative to source predictor variables, such as  $\mathbf{M}$ . Event terms have zero mean and standard deviation= $\tau$  (natural log units). Within-event error  $\varepsilon$  is has zero mean and standard deviation= $\phi$ . Mixed-effects analyses with Eqn. (21) were performed using the NLME routine in program R [Pinheiro et al. 2013].

Checks of the base-case GMPEs using these residuals were undertaken by plotting  $\eta_i$  against **M** (to check the **M**-scaling in function  $F_E$ ),  $\eta_i$  against rake angle (to check the focal mechanism terms in  $F_E$ ),  $\varepsilon_{ij}$  against  $R_{JB}$  (to check the path function  $F_P$ ), and  $\varepsilon_{ij}$  against  $V_{S30}$  (to check the site amplification terms). Plots for these effects are given in BSSA13 and support the following principal findings:

- There are some complexities in the plots of  $\eta_i$  with **M** when both CL1 and CL2 events are considered, which are largely related to CL2 aftershocks from China (Figure 4.28 of BSSA13). When these data are excluded, no trends are evident (Figure 4.29 of BSSA13), indicating adequate performance of the **M**-scaling function over the **M** range of 3 to 8.
- Plots of  $\eta_i$  against rake angle show zero bias with the following exceptions positive residuals for NS events with  $\mathbf{M} < 5$  (the bias would have been zero without the focal mechanism adjustment in the model) and positive bias for T > 1.0 s PSA for RS events with  $\mathbf{M} > 5$ . We do not consider these trends to be sufficiently compelling to warrant adjustments to the model terms.
- There is no trend of  $\varepsilon_{ij}$  with distance up to 400 km when the full data set is used; this finding demonstrates that the California-based  $c_3$  provides a good match to the global NGA-West 2 data set (Figure 4.19 of BSSA13).
- There is no trend of  $\varepsilon_{ij}$  with  $V_{S30}$ , indicating satisfactory performance of the SS14 site amplification function. The lack of trend is present for the global data set (Figure 4.24 of BSSA13) and regional subsets.

Since a major region of application for this work will be California, we investigated the relative influence of non-California earthquakes on the GMPEs by examining CL1 (mainshock) event terms ( $\eta_i$ ) by region and fault type, as given in Figure 10. There is no overlap in the magnitudes of the California and non-California NS events, so we cannot

comment on regional differences in that case. For SS, the California and non-California event terms appear similar. For RS events at T=1.0s the California residuals are higher than the non-California events, at least for the larger magnitudes for which there is  $\mathbf{M}$  overlap. This indicates that on average, the motions for California RS events may be under-predicted by our GMPEs for  $T \sim 1.0$ s (not shown here, a similar difference is suggested for longer periods). As our GMPEs are intended for global use, however, we have chosen not to provide a set only applicable to California.

# Regional adjustments to the apparent anelastic attenuation coefficient $c_3$

The lack of distance trends in the within-event residuals ( $\varepsilon_{ij}$ ) (bullet three above) demonstrates that the base-case path-scaling terms for apparent geometric spreading and apparent anelastic attenuation reasonably represent the global data. Recalling that the anelastic term  $c_3$  was constrained from small M data in California, we plotted  $\varepsilon_{ij}$  against distance for various combinations of regions to investigate possible regional variations in crustal damping. As shown in Figure 11, we found California, New Zealand, and Taiwan to have flat trends relative to the global model (indicated as 'Average Q'), Japan and Italy to have downward trends indicating faster distance attenuation (indicated as 'Low Q'), and China and Turkey to have an upward trend (indicated as 'High Q'). (We caution that country names are used as a convenient short-hand to describe the regions, realizing that results for the region may well be applicable beyond the political boundaries of the country and that regional differences of attenuation may occur within the countries; at this time we do not have sufficient data to establish the geographic limits of our results nor to parse the data more finely.) Similarly flat distance attenuation trends for New Zealand were observed by Bradley [2013]. Similarly fast distance attenuation trends have been observed in Japan and Italy (e.g., Stewart et al. [2013]; Scasserra et al. [2009]). The slower attenuation for China is not surprising given the location of the Wenchuan event near the western boundary of a stable continental region [Johnston et al., 1994], with the recordings being located in both stable continental and active crustal regions [Kottke, 2011]. This result for Turkey was not expected, but has been observed by others using larger Turkish data sets [Z. Gulerce, pers. communication, 2013].

For the low and high Q cases, we fit a linear expression through the data according to:

$$\varepsilon = \Delta c_3 \left( R - R_{ref} \right) + \overline{\varepsilon}_{lR} \tag{22}$$

where  $\Delta c_3$  is the additive regional adjustment to the  $c_3$  term from Eqn. (3) and  $\overline{\epsilon}_{lR}$  is the mean value of the residuals at close distance in a given region. In order to prevent the relatively sparse data at the closest distances from affecting the slope  $\Delta c_3$ , we limited the data range used in the regression to  $R_{JB} > 25$  km, which captures the 'flat' region in the residuals before anelastic effects become significant (beyond about 80 km) and encompasses the distance range with abundant data. Adjustments according to Eqn. (22) are plotted in Figure 11. Values of  $\Delta c_3$  are given in the figure and are compiled as regression coefficients. These regional adjustments are used in the computation of residuals for subsequent Phase 3 analyses.

## Adjustment of the base-case GMPEs for sediment depth

The site parameter  $V_{S30}$  strictly describes only the characteristics of sediments in the upper 30 m, even though it has been shown to be correlated to deeper structure [e.g., Boore et al., 2011]. Several previous studies have found site amplification effects related to the depth of the deposit that are not captured by the use of  $V_{S30}$  alone as a site descriptor, including three GMPEs from the NGA-West 1 project [Abrahamson and Silva, 2008; Campbell and Bozorgnia, 2008; and Chiou and Youngs, 2008]. Since residual trends in prior work are typically strongest at long spectral periods ( $T > \sim 1.0 \text{ s}$ ), the depth parameter is descriptive of low-frequency components of the ground motion, which may be related to resonances of sedimentary basin structures. The BA08 model did not include a basin-depth term; here we investigate whether the data support the use of such a term in the present equations.

As indicated in the *Predictor Variables* section, we consider basin-depth parameter  $z_I$ , which is the shallowest of the depth metrics considered in prior work. This choice is motivated by its greater practicality and lack of evidence (from Day et al. [2008] and this study) that deeper metrics are more descriptive of site amplification. We found stronger trends of residuals  $(\varepsilon_{ij})$  against depth differential  $\delta z_1$  (Eqn. 10) than basin depth itself  $(z_I)$ , so  $\delta z_1$  was adopted. In Figure 12, we plot residuals  $\varepsilon_{ij}$  against  $\delta z_1$  along with the model fit from Eqn. (9). At short periods there are no clear trends. For  $T \ge 1$  s we find negative residuals for negative  $\delta z_1$ , a positive gradient for  $\delta z_1 < 0.5$  km, and relatively flat trends thereafter. Model coefficients in Eqn. (9) represent the slope  $f_0$  of the  $\varepsilon_{ij} - \delta z_1$  relation and the limiting value  $f_7$  of  $\varepsilon_{ij}$  for  $\delta z_1 > 0.5$  km in the equation. The coefficients are regressed using all available data

(from southern California, San Francisco Bay Area, and Japan); variations between regions were investigated and found to be modest and are not included in the recommended model.

## **Evaluation of Source Effects Using Between-Event Residuals**

Event terms  $\eta_i$  derived from Eqn. (21) are used to investigate differences between mainshock and aftershock motions (using the CL1 and CL2 designation) and effects of source depth (using depth to top rupture,  $Z_{tor}$ ).

We found a modest correlation between  $\eta_i$  values from 'parent' CL1 events and their 'children' CL2 events (details in BSSA13). Accordingly, we examine differences between mainshock and aftershock ground motions in the form of differences between CL1 event terms  $\eta_{CL1}$  and the mean of their 'children' CL2 event terms  $\bar{\eta}_{CL2}$ :

$$\Delta \eta = \overline{\eta}_{CL2} - \eta_{CL1} \tag{23}$$

There are 13 such pairs in our data set, and the resulting  $\Delta \eta$  values are plotted in Figure 13 against the magnitude of the CL1 event. The results show no systematic departure of  $\Delta \eta$  from zero, indicating that on average CL2 events do not have any more bias relative to the GMPEs than do their parent CL1 events. Accordingly, we consider our GMPEs equally applicable to both event types.

Because our distance metric  $R_{JB}$  is the closest horizontal distance of the site to the surface projection of the fault, rupture depth is not considered. This could conceivably lead to overprediction of motions from deep events (because the ground motions for such events have a longer travel path to reach recording sites), although such effects could possibly be offset by an increase in the value of the stress parameter with earthquake source depth (e.g., Fletcher et al.1984). Figure 14 shows trends of  $\eta_i$  with  $Z_{tor}$  for CL1 and CL2 events with  $\mathbf{M} \geq 5$ , which are essentially flat. Similar trends were observed for hypocentral depth. BSSA13 examined these trends by region, finding no effects, and for small magnitudes, for which trends were observed. Since the hazard for most engineering applications is governed by  $\mathbf{M} \geq 5$  events, we have not included a source depth parameter in our GMPEs.

## Aleatory uncertainty model

Our model for aleatory uncertainty (Eqns. 13-17) is derived on the basis of Phase 3 analysis, due to the relatively large database (as compared to Phase 2), which allows the standard deviation models to cover a broader range of M,  $R_{JB}$ , and  $V_{S30}$  than was used in

Phase 2. Our approach was to bin event terms  $\eta_i$  by **M** to evaluate between-event standard deviation  $\tau$  and bin residuals  $\varepsilon_{ij}$  by distance and  $V_{S30}$  to enable evaluations of within-event standard deviation  $\phi$ . The residuals analyses were performed using the median model given in Eqns. 1–9, including the anelastic attenuation and basin adjustments. Figure 15 shows example plots of binned values of  $\tau$  and  $\phi$  against the respective predictive variables for 0.2 and 1.0 s PSA (results for many additional periods were used to guide model development). Described further in BSSA13, the principal findings of this process are as follows:

- As shown in Figure 15a,  $\tau$  decreases with **M**, but is nearly constant for **M** > 5.5, which is the range of principal engineering interest. We account for this effect through Eqn. (14). Conversely,  $\phi$  decreases with **M** at short periods but increases with **M** for T > 0.6 s (Eqn. 17 and Figure 4.40 of BSSA13). Terms  $\tau_I$  and  $\tau_2$  and  $\phi_I$  and  $\phi_2$  are computed using all residuals ( $\eta$  or  $\varepsilon$ ) within the respective **M** ranges (e.g., **M** < 4.5 for  $\tau_I$  and **M** > 5.5 for  $\tau_2$ ), not as the average of the binned values shown in Figure 15a.
- Figure 15b shows the  $R_{JB}$ -dependence of  $\phi$  for M > 5.5 residuals (indicated as  $\phi_2$ ). We see that  $\phi$  increases with  $R_{JB}$ , but only beyond about 80 to 130 km. Although not shown in the figure, at closer distances  $\phi$  is approximately constant with respect to distance. We account for this effect through Eqn. (16). The increases in  $\phi$  for  $R_{JB} > 80$ -130 km may reflect regional variability in anelastic attenuation. Thus, we expect that this increase is influenced by epistemic uncertainty in regional attenuation rates.
- Figure 15c shows the  $V_{S30}$ -dependence of  $\phi$  for M > 5.5 and  $R_{JB} < 80$  km. We see that  $\phi$  decreases with  $V_{S30}$  at short periods ( $T < \sim 1.0$  s), but only below about 300 m/s, which is captured by Eqn. (15). Results for many IMs in the format of Figure 15c show no trend of  $\phi$  for  $V_{S30} > 300$  m/s. Parameter  $\Delta \phi_V$  is the difference in  $\phi$  values computed from bins of  $\varepsilon$  for  $V_{S30} > V_2$  and  $V_{S30} < V_1$ . We attribute the lower  $\phi$  values for soft sites to nonlinear site response, which amplifies weak motions and de-amplifies strong motions, thus reducing  $\phi$  relative to underlying reference site conditions (Choi and Stewart, 2005).

Seismic hazard analysis for active crustal regions will most often be controlled by  $\mathbf{M} > 5.5$  events at  $R_{JB} < 80$  km and  $V_{S30} > 300$  m/s. These conditions correspond to  $\tau = \tau_2$  and  $\phi = \phi_2$ , which are plotted in Figure 16 along with the standard deviation terms provided in BA08. While the  $\phi$  terms are similar, the  $\tau$  terms have increased notably relative to BA08 for T < 0.2 s and decreased for T > 1.0 s. Reductions from the tabulated  $\phi$  values can be made if site response (and potentially path effects) are evaluated on a site-specific basis (Atkinson, 2006; Al Atik et al., 2010). Moreover, the actual variability may be smaller than that obtained from these regression statistics if applications are for a more controlled set of region and site conditions. For example, Atkinson (2013) finds that aleatory variability for ground motions

recorded on rock sites ( $V_{S30}>1000$  m/s) in a region of eastern North America is significantly lower than the values obtained here – presumably because of the restriction in both region and site condition of the included data.

We recognize that the proposed standard deviation model is more complex than in BA08, which was necessitated by the significant expansion of the data set in NGA-West 2, including a wider range of regions, magnitudes, and distances. Had we kept  $\mathbf{M}$ -,  $R_{JB}$ -, and site-independent  $\phi$  and  $\tau$ , our standard deviations would be high relative to BA08 and the other NGA-West 2 GMPEs. This increase is largely due to the substantial amount of small  $\mathbf{M}$  data introduced to the data set. The additional complexity in the sigma model is worthwhile given the strong effect of sigma on PSHA results (Bommer and Abrahamson, 2006).

As shown in Figure 16, there is a bump (i.e., increase) in the standard deviations near 0.08 s, which is controlled by the  $\tau$  component. This bump is stable when the data is parsed in various ways, including CL1-only events, events in various **M** ranges (< 4.5,  $\geq$  5.5), and various regions, with one exception. The exception is California CL1 events with **M** > 5.5, for which the bump is absent and the  $\tau_2$  terms are lower (i.e., nearly 0.24 for T < 0.5 s) than those given by our model. Due to the relatively modest number of large-**M** California events, and persistence of the bump for all other conditions, we have retained the bump in our model.

We believe that there are physical justifications for the bump: PGA and very short-period PSA are controlled by ground-motion periods in the approximate range of 0.2–0.5 s, so dispersions for the very short periods might be expected to be similar to those in the 0.2-0.5 s range, as observed. Any processes that produce large variability in short-period energy ( $T < \sim 0.5$  s) would therefore be expected to produce effects on PSA variability that are concentrated between about 0.03 and 0.2 s because outside of that range the spectral ordinates are dominated by relatively low-frequency ground motions. Based on point source simulations conducted by the first author and R. Youngs (personal communication, 2013), we suggest two such processes could contribute to the bump in  $\tau$  at  $T \sim 0.08$  s; (1) variations in the source stress parameter for small  $\mathbf{M}$  earthquakes (effect not present for larger earthquakes) and (2) variations in  $\kappa_0$  for larger  $\mathbf{M}$  earthquakes (smaller  $\mathbf{M}$  events were not investigated). Event-to-event variability in  $\kappa_0$  could be postulated to result from regional crustal or geological variations that are not presently well understood. Further study of the short-period peak in  $\tau$  is needed to verify and extend these postulations.

## **SUMMARY AND DISCUSSION**

We have presented a set of ground-motion prediction equations that we believe are the simplest formulation demanded by the NGA-West 2 database used for the regressions. The new relations are a significant improvement over BA08', and provide a demonstrably reliable description of recorded ground-motion amplitudes for shallow crustal earthquakes in active tectonic regions over a wide range of magnitudes, distances, and site conditions.

Our GMPEs are intended for application in tectonically active crustal regions. The equations should not be used for other tectonic regimes such as subduction zones or stable continental regions unless their applicability can be verified. The data controlling the equations are derived principally from California, Taiwan, Japan, China, the Mediterranean region (Italy, Greece, Turkey), and Alaska. We have demonstrated some regional variations in ground motions, so application of the GMPEs to other areas considered to be active crustal regions carries an additional degree of epistemic uncertainty. This includes regions in the western U.S. outside of the portions of California included in our data set.

We recommend the following limits for the predictor variables used in our GMPEs:

- Strike-slip and reverse-slip earthquakes, M = 3 to 8.5
- Normal-slip earthquakes, M = 3 to 7
- Distance,  $R_{JB} = 0$  to 400 km
- Time-averaged shear wave velocities of  $V_{S30} = 150$  to 1500 m/s
- Basin depth,  $z_1 = 0$  to 3.0 km
- CL1 and CL2 event types (mainshocks and aftershocks)

These limits are subjective estimates based on the distributions of the recordings used to develop the equations. We note that our recommended limit of M8.5 for strike-slip and reverse-slip earthquakes is actually beyond the data limits. Events as large as M8.5 are important for hazard applications. Therefore we checked that extrapolation of our GMPEs to M8.5 appears to be reasonable, based on agreement of the magnitude scaling in the GMPEs with predictions from simple SMSIM simulations (Boore, 2005).

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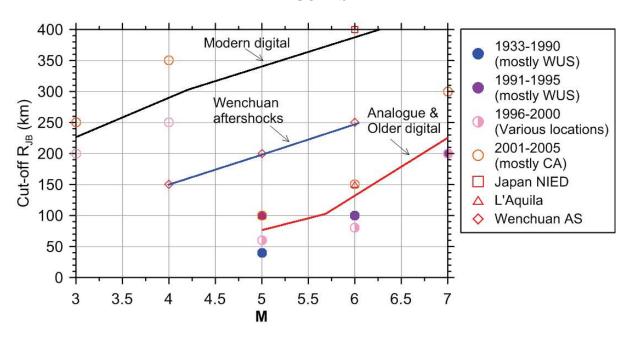
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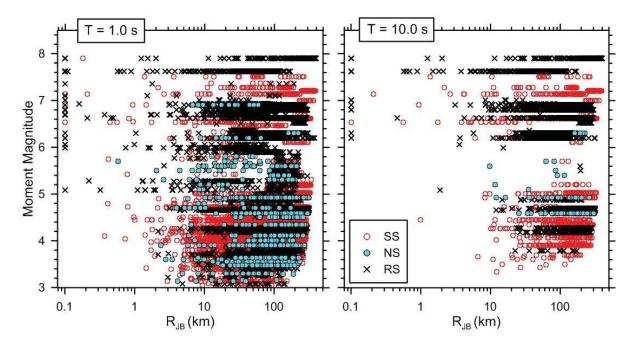
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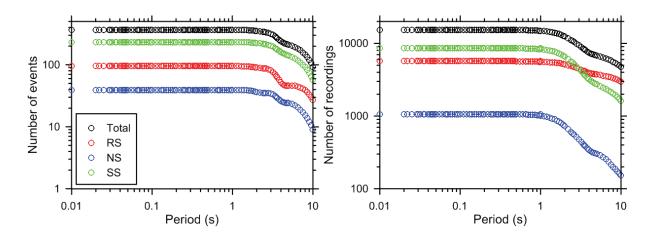
# **FIGURES**



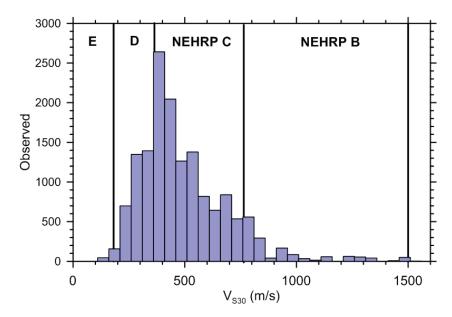
**Figure 1.** Magnitude- and distance-dependent cutoff criteria for using records. Data for a given earthquake with magnitude  $\mathbf{M}$  were only considered for use if  $R_{JB}$  was less than the cutoff distance shown in the figure for that magnitude and type of recording. The symbols in the figure represent judgment-based cutoffs of data reliability. Symbols in figure developed from NGA-West 2 GMPE developer interactions; lines represent our implementation.



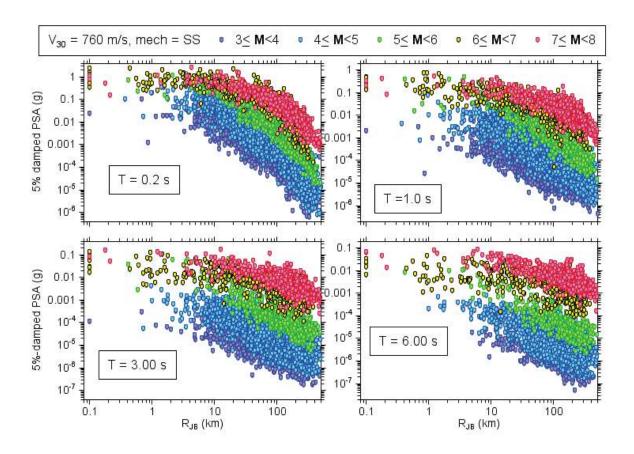
**Figure 2.** Distribution of data, according to fault type, used to develop the GMPEs. SS=strike-slip; NS=normal-slip; RS=reverse-slip.



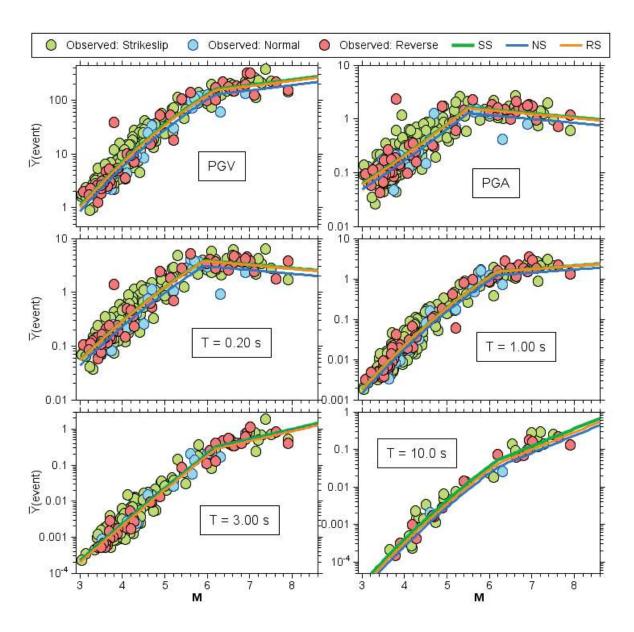
**Figure 3.** Number of events (left) and recordings (right) used to develop the GMPEs. The numbers are differentiated by fault type. SS=strike-slip; NS=normal-slip; RS=reverse-slip.



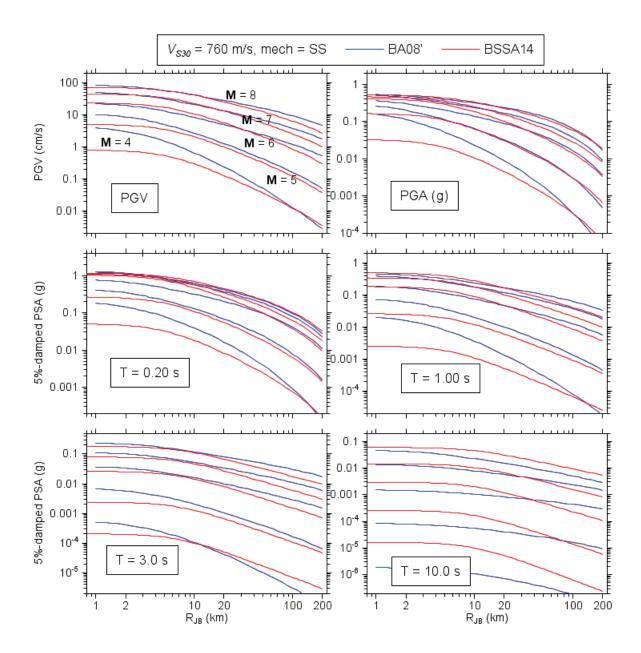
**Figure 4.** Histogram of  $V_{S30}$  for records used in deriving the GMPEs, with NEHRP site classes indicated by the vertical lines. Only two records had  $V_{S30}$  values beyond the range of the plot corresponding to NEHRP class A (1526 m/s and 2016 m/s).



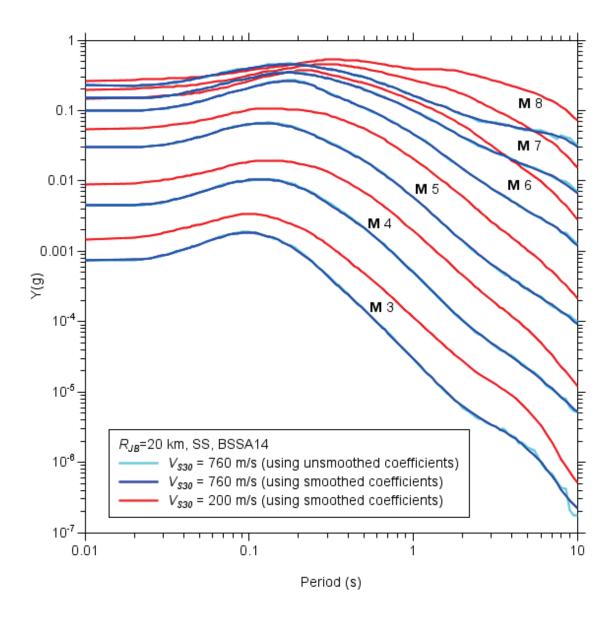
**Figure 5.** PSA at four periods for strike-slip earthquakes. All amplitudes adjusted to  $V_{s30} = 760 \text{ m/s}$  using the soil amplification factors of this study.



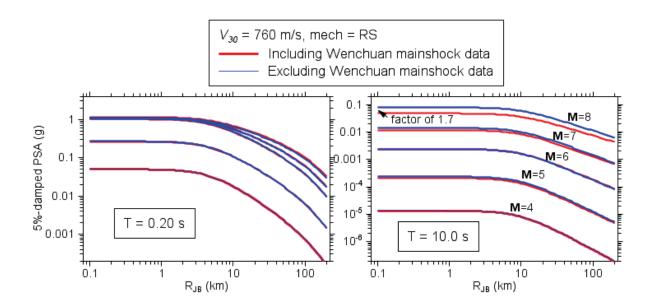
**Figure 6**.  $\overline{Y}$  data points for each event and fit of M-scaling function.



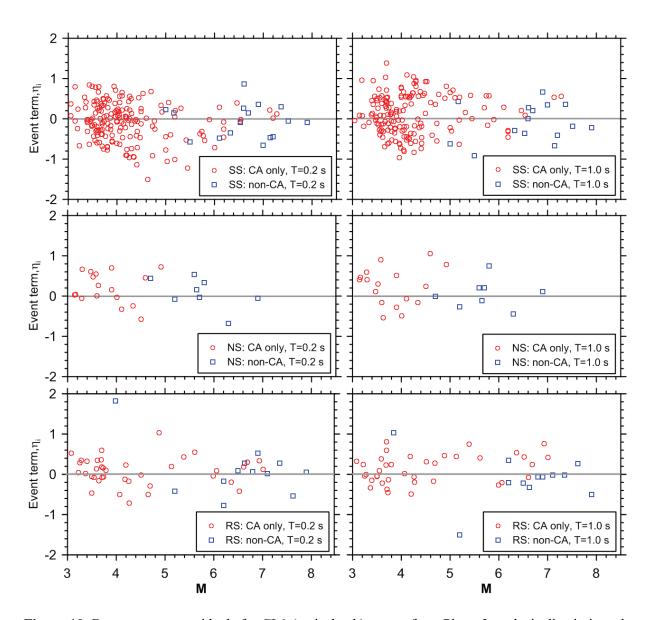
**Figure 7**. Median trends of proposed GMPEs as compared to BA08', as a function of distance for strike-slip earthquakes and  $V_{s30} = 760 \text{ m/s}$ . The BA08' values have been adjusted to RotD50 using the ratios RotD50/GMRotI50 in Boore [2010] (maximum adjustment of 1.06 for T = 10 s).



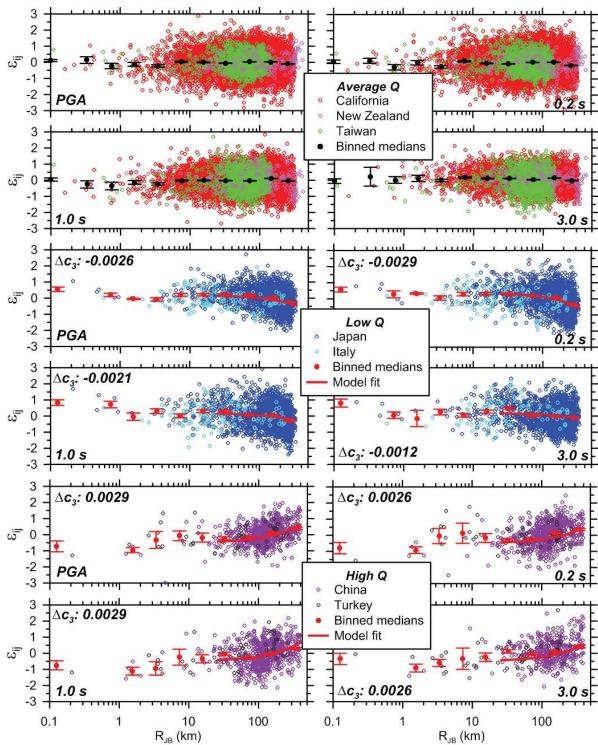
**Figure 8.** Variation of median predicted *PSA* versus period (*T*) for **M** 3, 4, 5, 6, 7, and 8 strike-slip earthquakes for  $R_{JB} = 20$  km and  $V_{S30} = 200$  m/s and 760 m/s.



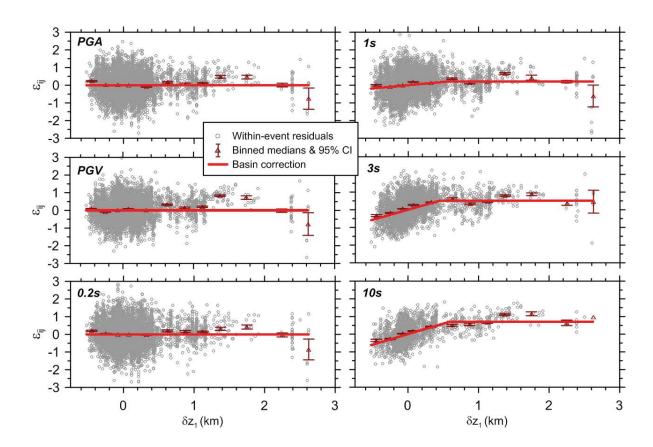
**Figure 9**. *PSA* vs  $R_{JB}$  for two periods,  $V_{S30} = 760 \, \text{m/s}$ , and reverse-slip (RS) events, from equations derived with and without the 2008 **M** 7.9 Wenchuan earthquake.



**Figure 10.** Between-event residuals for CL1 (mainshock) events from Phase 3 analysis discriminated by fault type and CA vs non-CA regions. Note that there is almost no overlap in  $\mathbf{M}$  for the CA and non-CA NS events, so it is difficult to judge possible bias for that condition.



**Figure 11.** Within-event residuals for regions identified as 'Average Q' (California, New Zealand, and Taiwan), 'Low Q' (Japan and Italy), and 'High Q' (China and Turkey). Also shown is the fit line per Eqn. (22) for  $R_{JB} > 25$  km.



**Figure 12.** Within event residuals against sediment depth differential  $\delta z_1$  along with proposed basin model. Results plotted are for southern California, San Francisco Bay Area, and Japan.

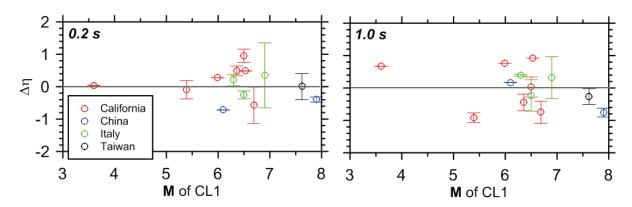
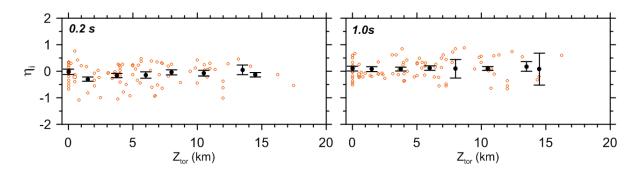
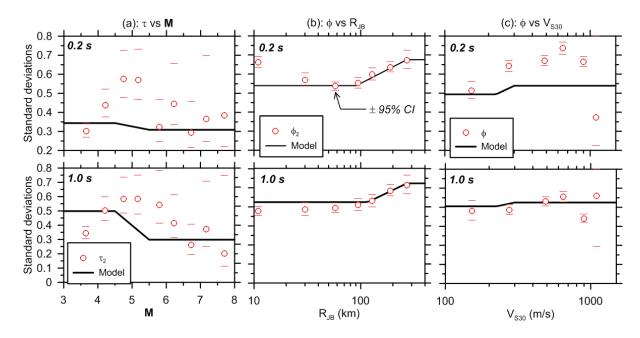


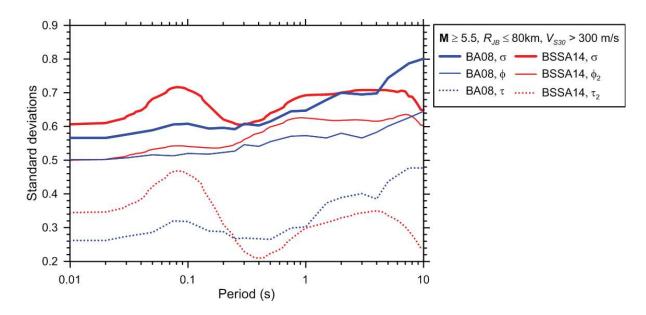
Figure 13. CL2 event term differential  $\Delta \eta$  as function of CL1 magnitude (including binned means and their 95% confidence intervals). Results show no systematic offsets from zero, implying no increasing level of misfit of CL2 'children' events as compared to their 'parent' CL1 event.



**Figure 14.** Event term variation with depth to top of rupture  $(Z_{tor})$  for  $M \ge 5$  CL1 and CL2 events (including binned means and their 95% confidence intervals). Results show no significant offset from zero or trend, indicating lack of dependence of ground motion residuals on rupture depth.



**Figure 15**. Binned standard deviation terms and their 95% confidence intervals from Phase 3 analysis showing: (a) Between-event standard deviation  $\tau$  against  $\mathbf{M}$ ; (b) within-event standard deviation  $\phi$  against  $R_{JB}$  for  $\mathbf{M} > 5.5$ , and (c)  $\phi$  against  $V_{S30}$  for  $\mathbf{M} > 5.5$  and  $R_{JB} < 80$  km. Lines in the figures represent model fits per Eqns. (1) to (9).



**Figure 16.** Comparison of the standard deviation terms in the BSSA14 GMPEs for  $\mathbf{M} \ge 5.5$ ,  $R_{JB} < 80$  km and  $V_{S30} > 300$  m/s with the  $\mathbf{M}$ - and  $R_{JB}$ -independent standard deviations from BA08.