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Henry Chermette, <sup>[2]</sup> Jer	zy Ciosic	wski," Julia C	ontreras-Garc	ia, <sup>191</sup> David L. Co	oper, "
Gernot Frenking 🔍, 🖱 Ca	rlo Gatti	, <sup>o</sup> Farnaz Heid	lar-Zadeh, <sup>101</sup> l	aurent Joubert, <sup>r</sup>	Ŋ
Ángel Martín Pendás, <sup>[1]</sup>	Eduard I	Matito, <sup>[m,n]</sup> Ist	/án Mayer, <sup>[o]</sup> /	Alston Misquitta,	<sup>[p]</sup> Yirong Mo, <sup>[q]</sup>
Julien Pilmé 🔍 <sup>[g]</sup> Paul L	. A. Pope	elier <sup>(r,s]</sup> Mart	in Rahm, <sup>[t]</sup> Ele	ov Ramos-Cordol	oa, <sup>[m,n]</sup>
Pedro Salvador <sup>[u]</sup> W. H.	Eugen	Schwarz <sup>[v,w]</sup> S	hant Shahbaz	ian. <sup>[x]</sup> Bernard Si	vi 🔍 *[g]
Julien Pilmé <sup>©</sup> , <sup>[g]</sup> Paul L Pedro Salvador, <sup>[u]</sup> W. H. Miquel Solà <sup>©</sup> , <sup>[y]</sup> Krzyszt	of Szale	wicz. <sup>[z]</sup> Vincen	t Tognetti <sup>[k]</sup>	Frank Weinhold	<sup>[aa]</sup> and
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[a] J. Andrés			[0] stván Mayer	nic Chemistry, Research Centre	for Natural Sciences
Departament de Ciències Experimental	ls Universitat Ja	aume I, 12080,		my of Sciences, Budapest 111.	
Castelló, Spain			[p] A. Misquitta		
[b] P. W. Ayers, F. Heidar-Zadeh Department of Chemistry and Chemica	al Riology McN	Master University 1280		and Astronomy, Queen Mary n E1 4NS, United Kingdom	University of London, Mile
Main Street West, L8S 4M1, Hamilton,	5,7		[q] Y. Mo	n ET 4NS, Onitea Kingaoni	
[c] R. A. Boto			Chemistry Depart	ment, Western Michigan Univ	ersity, Kalamazoo, Michigan,
CICECO, Aveiro, Portugal [d] R. Carbó-Dorca			49008		
Institute of Computational Chemistry,	University of G	irona, Campus de	[r] P. L. A. Popelier Manchester Institu	ite of Biotechnology (MIB), 13	1 Princess Street, Manchester
Montilivi, 17071, Girona, Spain	-		M1 7DN, United K		
[e] H. Chermette Université Lyon 1 et UMR CNRS 5280 li	nstitut Sciences	Analytiques	[s] P. L. A. Popelier	try, University of Manchester, (	Dyford Poad Manchester
Université de Lyon, 69622, Paris, Franc		Analytiques,	M13 9PL, United I		Diora Roda, marchester
[f] J. Cioslowski			[t] M. Rahm		
Institute of Physics, University of Szczec Poland	in, Wielkopolsk	a, 1570-451, Szczecin,	-	emistry and Chemical Enginee 96, Gothenburg, Sweden	ering, Chalmers University of
[g] J. Contreras-Garcia, J. Pilmé, B. Silvi		Y	[u] P. Salvador	o, domenourg, sweden	
Sorbonne Universitś, UPMC, Univ Paris				ca Computacional i Catàlisi, U	
Chimie Théorique, case courrier 137, 4 E-mail: sbernard@lct.jussieu.fr	place Jussieu,	75005, Paris, France		nany 69, 17003, Girona, Spain	
[h] D. L. Cooper			[v] W. H. E. Schwarz Theoretical Chem	istry Groups at Tsinghua Univ	ersity, Beijing 100084, China
Department of Chemistry, University o	f Liverpool, Live	erpoolL69 7ZD, United	[w] W. H. E. Schwarz	, , , ,	
Kingdom [i] G. Frenking			•	oretical Chemistry Laboratory, rersity of Siegen, Siegen 57068	•
Fachbereich Chemie, Philipps-Universitä	it Marburg, Ha	ns-Meerweinstr. 4,	[x] S. Shahbazian	icially of alegen, alegen 2/000	, cernuny
35032, Marburg, Germany	-		Department of Ph	nysics, Shahid Beheshti Univers	ity, P.O. Box 19395-4716,
<ul> <li>[j] C. Gatti hCNR-ISTM Istituto di Scienze e Tecnolo</li> </ul>	aie Malecalari	via Golai 19-20133	G. C., Evin, 19839, [v] M. Solà	. Tehran, Iran	
Milan, Italy	קוב אוטובנטועוו,	10 GOIGI 12, 20133,	[y] M. Solà Institut de Químic	a Computacional i Catàlisi (IC	CC) and Departament de
[k] L. Joubert, V. Tognetti			Química, Universi	tat de Girona, Campus de Mo	
COBRA UMR 6014 & FR 3038, INSA Rou Normandie, Mont-St-Aignan, France	uen, CNRS, Uni	versité de Rouen	Catalonia, Spain		
[1] Ángel Martín Pendás			[z] K. Szalewicz Department of Ph	nysics and Astronomy, Universi	ty of Delaware, Newark,
Departamento de Química Física y Ana	ılítica, Universio	lad de Oviedo, 33006,	Delaware	,	, -, -,
Oviedo, Spain			[aa] F. Weinhold	nistry Institute and D	t of Chamister II.
[m] E. Matito, E. Ramos-Cordoba Kimika Fakultatea, Euskal Herriko Uni	bertsitatea (LID	V/FHU), and Dopostia		nistry Institute and Departmer on, Madison, Wisconsin, 5370	
International Physics Center (DIPC), P.			[bb] Émilie-Laure Zin		
Spain			Sorbonne Unive	rsité, UPMC Univ. Paris 06, MO	NARIS, UMR 8233, Université
[n] E. Matito, E. Ramos-Cordoba			<b>D</b> <sup>1</sup> · · · · ·	Curie, 4 Place Jussieu, Case Cou	

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- 4. Are partition schemes subject to scientific Darwinism? If so, what is the influence of a community's sociological pressure in the "natural selection" process?
- 5. To what extent does/can/should investigated systems influence the choice of a particular partition scheme?
- 6. Do we need more focused chemical validation of EDA methodology and descriptors/terms in general?
- 7. Is there any interest in developing common benchmarks and test sets for cross-validation of methods?
- 8. Is it possible to contemplate a unified partition scheme (let us call it the "standard model" of partitioning), that is proper for all applications in chemistry, in the foreseeable future or even in principle?
- 9. In the end, science is about experiments and the real world. Can one, therefore, use any experiment or experimental data be used to favor one partition scheme over another? © 2019 Wiley Periodicals, Inc.

### DOI: 10.1002/jcc.26003

construction, perturbation-based methods only apply to weak interactions, where they are typically quite successful.<sup>[19,20]</sup>

73 Variational-based EDAs require quantum chemical descrip-74 tions of the entire system as well as the considered fragments. 75 This approach is able to treat weak intermolecular interactions 76 as well as multiple kinds of bonds.<sup>[21,22]</sup> A decomposition of the 77 interaction energy of the water dimer was published in 1957 by 78 C. A. Coulson.<sup>[23]</sup> However, the first acknowledged variational 79 EDA method is due to Morokuma and co-workers.<sup>[24-27]</sup> This 80 first EDA method is limited to the Hartree–Fock level of theory 81 and it suffers from the presence of nonphysical contribution to 82 the interaction energy. The latter problem is significantly 83 reduced in the reduced variational space (RVS) EDA.<sup>[28]</sup> A few 84 years after Morokuma's seminal article, Ziegler and Rauk pro-85 posed an energy decomposition of the energy calculated in the 86 framework of the Hartree-Fock-Slater method known as Transi-87 tion State (ETS)-EDA.<sup>[29,30]</sup> This method enables the analysis of 88 both weaker and stronger bonds. There are several approaches 89 in which localized orbitals are used to define EDAs. For exam-90 ple, Natural Energy Decomposition Analysis (NEDA),<sup>[31,32]</sup> Block 91 Localized Wave functions (BLW-EDA),<sup>[33,34]</sup> and Fragment 92 Molecular Orbitals (FMO) in the Pair Interaction Energy Decom-93 position Analysis (PIEDA),<sup>[35]</sup> Absolutely Localized Molecular 94 Orbitals in ALMO-EDA,<sup>[36-39]</sup> and Natural Orbitals for Chemical 95 Valence<sup>[40]</sup> (NOCV-EDA).<sup>[41]</sup> The use of the variational-based 96 EDA is mostly limited to HF and DFT calculations although 97 post-Hartree-Fock correlation methods do exist. For example, 98 for partitioning energies within the Local Pair Natural Orbital 99 Coupled Cluster Framework,<sup>[42]</sup> for MP2 wave functions,<sup>[43]</sup> and 100 for evaluating dispersion corrections.<sup>[44]</sup> 101

A third family of EDA only requires electronic data (wave 102 function or electron densities) of the entire system. The "Chemi-103 cal Hamiltonian" approach,<sup>[45]</sup> makes use of atomic projection 104 operators to express the total Hamiltonian as a sum of one-105 center and two-center terms. The resulting energy decomposi-106 tion yields true intra-atomic and true interatomic energy 107 components and basis extension terms. As the projection oper-108 ators are defined in the LCAO-MO formalism, the method is 109 restricted to this kind of calculations. In position space par-110 titioning, the interaction energy is defined in terms of contribu-111 tions of the one-electron and of the two-electron density 112 distribution functions. The considered domains may have either 113 sharp or fuzzy boundaries. The quantum theory of atoms in 114

### Introduction

### Bernard Silvi

During the preparation of the second European Symposium on Chemical Bonding held last summer in Oviedo, I have 19 been asked by the organizers to propose a reflection topic 20 for the Bond Slam session. I chose the Energy Decomposition 21 Analyses (EDAs) because these methods are among the most 22 useful as well as controversial tools helping to get insights 23 on the electronic structure of molecules. I further thought 24 that it should be helpful to collect opinions on the epistemo-25 logical issues of these methods. I had the experience of a col-26 lective paper in which a panel of scientists was invited to 27 give their opinions on the topological approaches in Theoret-28 ical Chemistry<sup>[1]</sup> and I proposed to renew this exciting 29 approach. Nine questions have been selected and proposed 30 to the contributors. 31

# Bernard Silvi, Eduard Matito, and Martin Rahm

35 We begin with a brief overview of EDA methodology and devel-36 opment. This introduction is not meant to be a comprehensive review and the interested reader is encouraged to consult the 37 literature for more details. One comprehensive description of 38 several different EDA schemes can be found in the article of 39 Phipps et al.<sup>[2]</sup> In their 2015 review, Phipps et al. describe two 40 groups of EDAs, classified depending on the nature of their 41 underlying theories. Perturbation-based methods express the 42 interaction energy in terms of corrections to a noninteracting 43 44 description. Variational-based methods explicitly require the 45 use of intermediate fragment wave functions corresponding to 46 idealized nonphysical situations.

47 Perturbation-based methods stem from the theory of intermolecular forces pioneered by Eisenschitz and London in 48 1930.<sup>[3,4]</sup> The method has been consistently improved over 49 decades<sup>[5–14]</sup> yielding the Symmetry-Adapted Perturbation The-50 ory (SAPT) which appears to be the latest link in of the evolu-51 tion process.<sup>[15–18]</sup> For each order of perturbation, the energy 52 53 contributions are derived directly from the expressions of per-54 turbation operators. In this way, perturbation-based energy terms can be related to physical effects. Put differently, these 55 methods explain interactions in terms of physical arguments 57 based on properties of monomers. For this reason, and by



molecules (QTAIM) considers domains bounded by zero-flux 1 surfaces of the density as defined by Bader, which are open sys-2 tems that, among other properties, have associated energies.<sup>[46]</sup> 3 4 In this sense, the QTAIM provides an atomic partition. An exten-5 sion of this partition, considering atomic and diatomic terms, as well as individual energy components, is known as the Inter-6 acting Quantum Atoms scheme<sup>[47-50]</sup> considers domains 7 bounded by zero-flux surfaces of the density as defined by 8 Bader.<sup>[46]</sup> However, other nonoverlapping partition schemes, 9 such as ELF basins,<sup>[51]</sup> can be considered at the expense of the 10 determination of the fragment kinetic energies. Methods for 11 fuzzy atom partitioning have been developed by Salvador and 12 Maver.<sup>[52,53]</sup> 13

14 Finally, Experimental Quantum Chemistry (EQC) is an energy-15 based partitioning unique in that it can interchangeably rely on 16 the quantum chemical calculation, at any level of theory, as well as on experimental thermochemical data, vibrational and 17 18 photoelectron, and X-ray diffraction and absorption measurements.<sup>[54,55]</sup> Developed by Rahm and Hoffmann, EQC makes 19 20 use of observable "reference frames." For example, when studying chemical bonding, the EQC partitioning refers to the bond 21 22 dissociation process. EQC is, in principle, applicable to any 23 chemical or physical transformations yet consists of relatively 24 few energetic terms. One of these terms is defined as the electronegativity of the system.[56] 25

26 EDA methods are multipurpose methods used to quantify, 27 characterize, and explain interactions between fragments of 28 quantum systems. Whereas we have not mentioned all varie-29 ties here, most EDAs can provide important pieces of information on chemical interactions. This class of methods can also 30 have other practical uses, maybe most notably for the design 31 of molecular mechanics force fields.<sup>[14,57,58]</sup> The explanations 32 33 offered by EDAs are seldom "chemical explanations" in the 34 sense that interactions are not directly described in terms of 35 "atom in molecules" chemical properties, such as electronega-36 tivity, valence, ionic, and covalent radii. The latter properties being determined by the location of the constituent atoms in 37 38 the periodic table. Most EDA methods instead rely on either 39 physical or quantum chemical concepts. In EDAs, interaction energies are described as the sum of contributions arising 40 from a sequence of equations that typically are specific to 41 42 each method. The physical (or quantum chemical) interpreta-43 tions of these equations, and the balance of the resulting 44 energy contributions, yields a deterministic explanation 45 focused on the dominant terms. Challenges for EDA methodology and future development of the field are what we will 46 47 discuss in this article.

# Alston Misquitta and Krzysztof Szalewicz

We will address the nine questions from the perspective of SAPT, sometimes also called exchange perturbation theory. SAPT has been presented in detail in many original papers,<sup>[15,59–68]</sup> reviews,<sup>[16,18]</sup> and textbooks.<sup>[20,69,70]</sup> Thus, there is no need for its extensive description here. However, we will briefly lay out the main features of SAPT, particularly those that do not seem to have been understood in the non-SAPT literature. We will also dispel some myths about SAPT as these58can cloud our understanding of this method in the context of59the questions posed in this article.60

SAPT is a perturbation theory that calculates interaction 61 energy directly, starting from isolated monomers. Thus, in con-62 trast to the supermolecular approach, no subtractions are 63 involved and, in consequence, SAPT is free of basis-set superposi-64 tion error. The interaction operator V is the sum of all Coulomb 65 interactions between particles of different monomers. The sim-66 plest approach is to use Rayleigh-Schrödinger (RS) perturbation 67 theory, but such approach is unphysical at short separations 68 since it does not predict the existence of the repulsive wall. To 69 include repulsion, one has to properly antisymmetrize the cluster 70 wave function, that is, enforce Pauli's exclusion principle, 71 resulting in SAPT. There are several ways to perform such adap-72 tation, the simplest one is to symmetrize the wave functions of 73 the RS method, leading to symmetrized RS (SRS).<sup>[59]</sup> 74

SAPT is the theory of intermolecular forces and most text-75 books discussing intermolecular interactions use SAPT concepts 76 even if the SAPT acronym is not mentioned. SAPT is also known 77 under several other names, for example, the effective fragment 78 potential (EFP) method.<sup>[71]</sup> SAPT provides what can be called 79 the standard model of energy decomposition analysis (EDA) for 80 intermolecular interactions (also called noncovalent interac-81 tions). This is because SAPT by design defines the interaction 82 energies in terms of electrostatic, induction (polarization and 83 charge-transfer, or charge-delocalization), dispersion, and 84 exchange terms. These terms are defined in a unique way and 85 can be calculated with potentially arbitrary accuracy and at 86 87 complete basis set (CBS) limits.

Since exact wave functions are unknown for larger mono-88 mers, SAPT approximates these functions at several available 89 levels of electronic structure theory. In fact, SAPT is a double 90 perturbation theory with the other perturbation due to the 91 intramonomer correlation operator  $W = W_A + W_B$ , where  $W_X$  is 92 the Møller-Plesset (MP) fluctuation potential of monomer X. If 93 W is neglected, monomers are described at the Hartree-Fock 94 (HF) level. Higher levels include consecutive powers of W, possi-95 bly with selective summations to infinite order applying the 96 coupled-cluster (CC) method. A version of SAPT, denoted as 97 SAPT (DFT), uses monomers described at the Kohn-Sham 98 (KS) density-functional (DFT) level (however, interaction ener-99 gies are computed using wave-function theory). 100

While SAPT has become a mainstream electronic structure 101 method, various myths about SAPT are in circulation and these 102 are far from the truth. In particular, it is sometimes stated that 103 SAPT is "just" one more EDA method, useful only for inter-104 preting interaction energies. This is not strictly correct. An EDA 105 takes a total interaction energy and, by various manipulations 106 of the density matrices or basis sets, seeks to decompose this 107 energy into terms that reflect something physical. What is done 108 in SAPT is conceptually quite different: one starts from physical 109 components, term-by-term, and sums them up to get the total 110 interaction energy. This process does not involve any arbitrary 111 choices. Thus, instead of decomposing a quantity, SAPT assem-112 bles it from well-defined components. What is important, if this 113 assembly is performed up to sufficiently high order (second 114

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order in *V* and fourth order in *W* are adequate for most pur poses), SAPT gives interaction energies similarly accurate to
 those given by the supermolecular approach in the fourth order
 (MP4) or the CC method with single, double, and non pertubative triple excitations [CCSD(T)].

SAPT, in fact, is an exact method in the sense that it repro-6 7 duces the exact interaction energy as the order in V goes to 8 infinity provided that appropriate symmetry-enforcing tech-9 niques and exact monomer wave functions are used (or the number of excitations in the CC method used to describe monomers approaches the number of electrons in each 11 12 monomer). These statements are based on high-order calcu-13 lations for small systems, see Ref. [65] for a review of 14 this work.

15 Since SAPT is a perturbation expansion in powers of V, one 16 may expect that SAPT will start to diverge as R becomes small and consequently V is no longer a small perturbation. Appar-17 18 ently, with proper symmetry enforcing, this divergence is not observed even for interactions as strong as those characteristics 19 of chemical bonds.<sup>[65]</sup> Also, low-order SAPT calculations for 20 larger systems show only a minimal worsening of convergence 21 when one goes to small R's, see Ref. [72] for an analysis of the 22 23  $Ar_2$  SAPT results at R = 1.5 Å, where the interaction energy is 24 more than three orders of magnitude larger than the absolute value of this quantity at the van der Waals minimum, 25 26 *R* = 3.76 Å.

27 Another myth is that the programmed general version of SAPT<sup>[73-75]</sup> is at the best equivalent to MP2. In fact, the version 28 29 of SAPT that is applicable to interactions of arbitrary closedshell molecules and some open-shell ones includes terms up to 30 third-order in V and a high-order treatment of electron correla-31 32 tion in monomers. By analyzing individual terms, one can show 33 that this version of SAPT is approximately equivalent to the 34 CCSD(T). This is confirmed by the agreement between these 35 two methods to within a few percent found in most calcula-36 tions. In particular, for the helium dimer, the calculations of 37 Refs. [76,77] performed at CBS limits and including also a 38 benchmark all-order calculation estimated to be accurate to about 0.01% show that the potential from SAPT at the level 39 available in the SAPT codes<sup>[73]</sup> and the CCSD(T) potential are 40 similarly accurate, although SAPT is slightly more accurate at 41 the van der Waals minimum. 42

A broader comparison of SAPT with CCSD(T) was performed 43 44 in Ref. [78] In this work, CCSD(T)/CBS benchmarks were com-45 puted for 10 dimers, containing up to 28 atoms, varying R from asymptotic to repulsive configurations. The median unsigned 46 47 percentage error of SAPT(DFT) is only about 1% larger than that 48 of CCSD(T), both methods computed in the same basis set [the 49 CCSD(T) error here is, of course, entirely due to basis set incom-50 pleteness]. SAPT (DFT) performs significantly better than all other DFT-based methods investigated in Ref. [78] 51

The next myth is that SAPT (DFT) is an approximation to the KS DFT supermolecular approach. While it should be already clear from the discussion above that this is not the case, a dramatic illustration is presented in Refs. [72,79] Figure 1 in Ref. [72] shows that CCSD(T) and SAPT [SAPT(DFT) is almost indistinguishable from SAPT] potential energy curves for Ar<sub>2</sub> are very close to each other. In stark contrast, supermolecular DFT calculations produce curves spread all over the place.

### Question 1: Is the Lack of Precision in the Definition of Many Chemical Concepts One of the Reasons for the Coexistence of Many Partition Schemes?

### Ramon Carbó-Dorca

Lack of precision is a mild description term. Chemistry has a heavy historical influence of intuitive concepts, which possess no well-defined physical basis. If such a physical basis must rely on guantum mechanics, then there might be one can chemically consider well defined just isolated atoms, molecules, and molecular swarms (a molecule surrounded by other molecules, for instance) only. These systems cannot be separated into parts or fragments from the quantum mechanical point of view. Atomic and bond contributions to the electronic energy of molecular systems are to be considered approximate and mainly related to the LCAO MO theoretical structure under Born-Oppenheimer approach. A simple situation might illustrate the difficulties of energy (or other molecular characteristics) partition. Whenever in LCAO MO theory one allows using AO or basis set functions in a general manner, allowing them being not centered in an atom, but a point within the threedimensional space of the molecular neighborhood. For example, one can choose the molecular center of charge, or even better: the center of charge of every atomic pair, as a locus where to center one electron basis functions. In this case, there might be defined as a one center contribution, which cannot be associated with any physical atomic electron source. At the same time, there could be bicentric partition contributions, made by a hybrid basis set center and the physical atom cen-91 ters. This might illustrate the arbitrariness of any partition 92 scheme. 93

### Shant Shahbazian

It is usually perceived that evolution of a "qualitative" chemical 96 concept to a "quantitative" one is the hallmark of precision; this 97 is the business of the indices in computational chemistry, for 98 example, indices probing the presence and/or strength of 99 bonding/aromaticity. However, lack of precision may have 100 another face: "over-quantification", which is many mathemati-101 cally rigorous but "nonequivalent" definitions of a chemical 102 concept; the mentioned bonding and aromaticity indices 103 belong to this category (although sometimes it is tried to sell 104 this nonequivalence as revelation of the "complementary" 105 nature of definitions, it seems hard to conceive how "contradic-106 tory" results must be avoided in case studies). There is no 107 bound on the number of proposed indices so the over-108 quantification grows with time and ruins the whole initial pro-109 gram of reaching precision by the qualitative to quantitative 110 transition. This is the same situation for a large number of pro-111 posed energy partitioning schemes in the last decades. There-112 fore, the reverse question is more legitimate to me: "Is the 113 coexistence of many partitioning schemes the reason for lack 114 of precision in the definition of many chemical concepts?". As I stressed elsewhere,<sup>[80]</sup> as far as one does not have a comprehensive theory for the concept of interest and just tries to make the qualitative to quantitative transition intuitively, the problem of over-quantification will be prevailed.

MPUTATIONAL

### István Mayer

Physicists consider the molecule as a set of electrons and nuclei, chemist treats it as a set of chemically bonded atoms. These conceptually different approaches can be connected by performing partition of different physically (chemically) relevant quantities in terms of atoms or pairs of atoms. However, while the electrons and nuclei used in the calculations are guite welldefined entities (at least at the energies relevant to chemistry), the individual atoms within a molecule are in some sense only constructions of the human mind. They represent very good generalizations of the enormous chemical experience but, if looking closely, are somewhat fuzzy concepts: one cannot tell apart exactly where one atom is ended and the other is started—if that guestion has a meaning at all. The absence of a unique definition of the atom within the molecule makes inevitable "the coexistence of many partition schemes". (Note that the bond order index also emerges from a partitioning: it is the integral of the diatomic component of the exchange density.<sup>[81]</sup>)

### Martin Rahm

I think so, yes. However, I do not see an inherent problem with trying to quantify the same "fuzzy" concepts in several different ways. Future cross-comparison efforts, discussed in questions six and seven, will hopefully indicate which precise EDA definitions are more predictive and chemically useful.

### Frank Weinhold

On the contrary, we contend that the dubious physical assumptions underlying EDA partitions (i.e., existence of mutually exclusive and simply additive "components" whose labels correspond to chemical concepts as broadly understood) are the issue. This is particularly so when the partition is formulated in terms of nonorthogonal "reference fragment" orbitals and their attendant conceptual ambiguities. Dubious premises lead inevitably to a multiplicity of (equally dubious) EDA partitions.

### Ángel Martín Pendás

In a sense, the lack of precision in defining concepts will inevi-48 tably lead to different partition schemes. However, there are 49 several levels at which differences will arise, and much as in 50 other fields of Chemistry, a set of minimal rules for an EDA to be acceptable for the community should be given. Are there 52 references? If so, are they well defined, or may they be chosen 53 at will by the user? Similarly, are there intermediate states from which particular energy components are defined? If so, are they well behaved, that is, are they compliant with the quantum 56 mechanical framework? It is my opinion that, in many cases, it 57 is not the fuzziness of chemical concepts that multiplies the number of available EDAs, but on the contrary, the somewhat 58 forced construction of partitioning schemes fitting available 59 computational or methodological levels. 60

### Julien Pilmé

Yes, it can be argued that the lack of precision or the lack of physical basis of some simple chemical concepts such as the "lone pair" concept, promotes the coexistence of numerous partition schemes. However, even if these concepts were better defined, one might think that the abundance of partition schemes will be sustained due to the difficulty to build a rigorous bridge between a unique definition of an atom and the quantum mechanics. Therefore, the lack of clear relationship between the chemical concepts and the quantum mechanics leads to an arbitrary character in the definition of partitions dictated by a compelling need to rationalize the diversity of interactions observed in the matter at the microscopic level.

### Carlo Gatti 💧

77 In my view, rather than the lack of precision in the definition of 78 many chemical concepts, it is the quite different perspective of 79 the various partitioning schemes that lead to and motivate, to 80 some extent, their coexistence. Indeed, broadly speaking, 81 energy decomposition analyses (EDAs) may be grouped in two 82 main categories, according to whether the decomposition is 83 performed in Fock (orbital) space or in the position space R3, 84 using some convenient partitioning of R3 in subdomains 85 (e.g., QTAIM). Advantages and shortcomings of the two 86 approaches have been masterfully analyzed and discussed by 87 Martín Pendás et al.<sup>[82]</sup> In the former, attention is directed to 88 the composing energies of the (often fictitious) intermediate 89 steps through which the analyzed system is formed from some 90 initial moieties, whereas in the second kind of approaches, 91 attention is focused on dissecting intra and intersubdomains 92 energy contributions for the very final step of such system (and 93 with a similar analysis performed on a given initial step of the 94 system, if the approach is applied to the interaction energy 95 also). The proposers of the real space EDAs are like a film direc-96 tor or a mystery writer which focus and analyze the last scene 97 of the movie or of the murder based only on what they see, 98 using unbiased scissors and zooming lenses. Instead, those of 99 the orbital space EDAs are eager to reconstruct a sequence of 100 Gedanken facts which have led the actors to the final outcome. 101 Actors keep changing (and often losing) their identity through 102 this process and in most cases, represent purely imaginary char-103 acters. Clearly, in the case of "orbital space" EDAs, the film 104 directors or mystery writers enjoy more freedom in their work 105 and their products may more largely differ among each other 106 and raise more vibrant, yet often nonsense, debates. 107

### **Paul Popelier**

Yes, is the short answer. I can think of one important example 110 of a chemical concept that causes a proliferation of EDAs. The 111 concept is that of the molecule itself and, in particular, the 112 identity of a molecule when in close contact with other mole-113 cules. More precisely, nontopological EDAs suffer from an 114

FULL PAPER

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unclear definition of a molecule at short range. At close inter-1 2 molecular distances, the separation of charge transfer and 3 polarization then becomes increasingly ill-defined. Of course, at 4 long range, the identity of a molecule is not problematic. RS 5 perturbation theory is based on this clear idea of a molecule at long range but this theory's vulnerability is that it breaks down 6 7 at short range. In that regime, molecules stop "owning" their 8 electrons and strong delocalization (i.e., exchange) start spoiling 9 the classical picture of what a given molecule is within a molecular assembly. In other words, if one is uncomfortable with finite (bounded) subsystems (i.e., the "real space" approach) 11 12 then the challenge is to determine where a given molecule 13 stops and starts. On the other hand, if one is inclined toward 14 infinite and overlapping subsystems (i.e., the "fuzzy" or "orbital" 15 or "Hilbert space" approach) then the challenge is to determine 16 which orbital or basis function still belong to the molecule in question. In any event, without a clear decision on the matter 17 18 of how to carve out a molecule from a molecular assembly, one 19 will face ambiguities down the line, such as the one mentioned 20 above. It is important to make the right decision upfront in 21 order to avoid issue that needs fixing later. I still like to think 22 that the topological partitioning offers a clear definition of a 23 molecule at short range and is thus a good starting point for an 24 EDA. Indeed, IQA defines charge transfer and polarization in a 25 well-defined way.

26 Finally, I had to comment on Carlo's nice metaphor. Of 27 course, at first sight, it is true that IQA does not invoke any 28 intermediate steps unlike nontopological EDAs. However, 29 strictly speaking, this is not really true, depending on one's starting point. Granted, IQA does not introduce a state that vio-30 lates the Pauli principle but it could do this, and still apply its 31 32 topological partitioning to it. To me, how one partition and 33 which reference states one brings in are two independent 34 things. In fact, one can argue that IQA also refers to an artificial 35 reference state, by the fine structure of the second-order 36 reduced density matrix. This object contains an electrostatic 37 part, an exchange part, and an electron correlation part. The lat-38 ter is a by-product of the fictitious Hartree-Fock state, while the 39 exchange part can be seen as a by-product of the fictitious Hartree state. So maybe the last scene of the IQA movie had some 40 predecessor scenes after all... 41

### 42 43

### 44 Pedro Salvador

To some extent, yes. But, I think it is worth to start by pointing out that we are referring here to two main families of energy decomposition schemes, as the reason for not having a unique, unambiguously defined, scheme is different in each case. I do not consider either of these two approaches superior from a conceptual point of view, they merely provide different insight.

51 On one hand, there are approaches that decompose the total 52 energy into a number of global contributions that bear some 53 physical/chemical significance. In this case, the main issue 54 appears to be that some of these global energy contributions 55 are defined with respect to a reference. Another family of 56 methods decomposes the total energy into domain contribu-57 tions, the latter often identified with the atoms within the molecule. In this case, we essentially have different realizations 58 of the same scheme, using one or another atom-in-molecule 59 (AIM) definition. Indeed, by introducing real-space atomic 60 weight functions one can accommodate both disjoint and over-61 lapping AIM approaches. Furthermore, there is no need to fur-62 ther distinguish between "Hilbert-space" and real-space 63 methods in this context. Some years ago<sup>[83,84]</sup> it was shown that 64 on the (numerical) one-electron basis set formed by the so-65 called effective atomic orbitals (obtained for a given real-space 66 AIM definition), the classical "Hilbert-space" and the real-space 67 formulae vield exactly the same results (even beyond the 68 LCAO-MO framework, for example, for plane-wave calcula-69 tions<sup>[85]</sup>). Hence, the arbitrariness in this scheme comes solely 70 from the definition of AIM, as is the case of many other descrip-71 tors such as partial atomic charges or, to some extent, bond 72 orders. 73

However, it is also worth to point out that, contrary to, for example, electron population analyses, energy decomposition schemes may differ from one particular electronic structure method to another, just because the way the total energy is determined can also be different. This adds an additional source of ambiguity even if we merely consider the case of formally exact theories such as density functional theory of full-CI methods. 80

### Jerzy Cioslowski

The coexistence of many schemes is a direct consequence of 84 the concept of energy partitioning being replete with ambigui-85 ties. To begin with, it encompasses two very different 86 approaches, namely, (1) partitioning into contributions due to 87 physical phenomena and (2) partitioning into contributions due 88 to subsystems and clusters comprising them. This observation, 89 already made by Pedro Salvador in his answer above, deserves 90 further elaboration. 91

In the first case, the interaction between two subsystems is 92 analyzed by application of a sequence of contrived processes 93 such as geometry relaxation, charge transfer, polarization, 94 etc..., each giving rise to a particular energy component. It is 95 important to understand the distinction between the terms 96 "sequence" and "superposition" in this context as the contribu-97 tions of these processes to the total energy are not commutative. To further complicate matters, not all permutations among 99 the members of the sequence in question are allowed. Thus, for 100 example, one can relax the nuclear and electronic degrees of 101 freedom in arbitrary order (by unfreezing the geometries of 102 subsystems while keeping their electron densities frozen, or 103 vice versa), each time obtaining different values of the respec-104 tive energy components. On the other hand, if one defines 105 polarization as complete relaxation of the electron density and 106 charge transfer as relaxation of the total charges of the subsys-107 tems, then obviously that the latter has to precede the former. 108 To summarize, the plethora of the possible energy partitioning 109 schemes of the first kind arises not only from certain degree of 110 arbitrariness in the definitions of the individual physical pro-111 cesses (polarization, charge transfer, etc...) but also from the 112 (limited) arbitrariness of the order in which they are applied. 113 Another layer of ambiguity is added by the necessity of 114

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specifying the definition of the partitioning of the electronic 1 properties into subsystem contributions that underlie the entire 2 3 energy partitioning scheme.

4 In the second case, one attempts to write the total energy as 5 a sum of contributions due to individual subsystems, pairs of subsystems, clusters of three subsystems, and so on. Usually, 6 7 these subsystems are atoms or functional groups. Again, all of 8 such schemes derive from particular definitions of properties of 9 atoms in molecules. However, there is another conceptual difficulty that has to be considered. The electronic Hamiltonian is 10 composed of one- and two-particle terms that give rise to the 11 12 respective one- and two-electron energy densities. Integration 13 of these densities over the entire Cartesian space produces the 14 corresponding energy components (i.e., kinetic, electron-15 nuclear attraction, and electron-electron repulsion) whose 16 atomic and diatomic contributions are obtained by analogy upon multiplication of the integrands by atomic projection 17 18 functions (whose sum over all atoms equals one; the functions 19 themselves can be smooth or not). Consequently, the atomic 20 contributions can be defined for all the three energy compo-21 nents, whereas the diatomic contributions arise strictly from the 22 electron-electron repulsion energy (though one may further 23 partition the electron-nuclear attraction energy by separating it 24 into terms due to individual nuclei). Thus, the "many-body" 25 energy contributions due to clusters of more than two atoms cannot be defined in a meaningful way, which runs contrary to 26 27 expectations from chemists (who would often prefer to deal 28 with atomic and diatomic energies transferable from one sys-29 tem to another, the residual energy is accounted for by interac-30 tions involving more than two atoms) and physicists (who are inspired by the cluster expansions of energies of systems com-31 32 posed of noble gas atoms, etc...). Even worse, this observation 33 appears to contradict at the first glance the results of 34 perturbative treatments of the dispersion interactions that pro-35 duce closed-form expressions for, for example, three-body 36 interactions (the AxilrodTeller potential).

### 37

#### 38 **Gernot Frenking** 39

The coexistence of many partition schemes is due to the fact 40 41 that different concepts and bonding models exist, which come 42 from different viewpoints and which address different questions. 43 Chemical bonding is a very complex phenomenon, which can be 44 interpreted in various ways. There will always be several chemical 45 concepts in chemical research, which consider diverse aspects of chemical phenomena. Chemical concepts and bonding models 46 47 are not right or wrong, but they are more or less useful and the 48 usefulness depends on the question that is asked. Partition 49 schemes are tools in the arsenal of bonding models, which serve 50 as a bridge between the numerical results of quantum chemical 51 calculations and the human desire to understand them in terms 52 of classical concepts. Chemistry has rather a problem with the 53 coexistence of (1) historically developed and poorly defined heu-54 ristic concepts and (2) more recently suggested quantum chemi-55 cal partitioning schemes. The conclusions of the two models 56 may contradict each other. In such cases, it is important to exam-57 ine the origin of both approaches.

### Julia Contreras

Indeed, there is an inherent lack of precision in chemistry, but I would not call them "physical," but rather "mathematical." It is mathematically impossible to univocally define an atom in a molecule or the point-wise energy in a molecule. However, I completely disagree there is no physics behind. There are physics behind from the moment people have been able to find patterns and make predictions in chemistry in terms of atoms and functional groups way before Quantum Chemistry entered the scene. This makes some partitions more physically sound than others, and the use of some bases more physically sound than others. Atomic basis sets are used in molecules because atoms are still a good physical entity/model. Although mathematically we could choose any function, atomic basis sets (located at the atomic nuclei) are a good option to describe the molecule in the sense that it accelerates convergence and reduces the number of functions to use. This basically means there is a physical truth behind the choice, even though other functions would also be mathematically good options to expand a function. Of course, this is not elegantly mathematically defined, but one should not forget the physics behind it, and deny the predictive power of chemistry because it is neither mathematically nor elegantly univocally defined. So just like in any other theory, we should look for partitions that contain the physics we need to reveal following a very simple principle: "as simple as it can be, but not simpler". Just like many models coexist for describing other problems in physics, I also agree that what we probably need is not less models, but a good hierarchy of them, so that we know when a given model is valid or we should go for a higher rung and more complex-description of chemical reality. I agree with C. Gatti that equivalencies among partitions as the one carried out in Ref. [82], and the limits of each method, are absolutely needed in this respect.

### **Henry Chermette**

The ambiguity of the bond concept relies on the fact that only nuclei and electrons are well-defined objects whereas the atoms in molecules are not, since the electrons in molecules are not stuck to nuclei. Therefore, although some definitions look more reasonable than others, the coexistence of several definitions is unavoidable. The lack of precision in the definitions is therefore a by-product.

### Émilie-Laure Zins

In contrast with most of the previous answers, I think that the 103 lack of precision of many key chemical concepts is not the main 104 reason for the existence of many partition schemes. The phe-105 nomena that theoretical chemists seek to describe nowadays 106 are highly complex, which fully justifies the development of 107 suitable and tunable tools adapted to each type of problem. It 108 seems to me that this phase of coexistence of many partition 109 schemes could be temporary: a convergence toward a single or 110 a small number of partition schemes could take place in the 111 coming years via fundamental theorems such as Hellman-112 Feynmann's, Bethe-Salpeter's equation, or guantum field the-113 ory. This "unification" could be an objective in itself for the 114

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community, leading to a simplification of concepts and descriptions. Shant Shahbazian proposed another question: "Is the coexistence of many partitioning schemes the reason for lack of precision in the definition of many chemical concepts?" I think that the development of a "universal" partition scheme could lead to a simplification of chemical concepts and an easier dialogue between theoretical and experimental chemists.

### Laurent Joubert and Vincent Tognetti

We think that the reciprocal question is also interesting: do we need an energy decomposition to define chemical concepts? For instance, conceptual DFT has often provided firm physical ground to empirical concepts using very simple equations: Pearson's molecular hardness and Parr's electrophilicity index can be derived in two lines, in contrast with many EDAs that require much more maths...

### Paul W. Ayers

Yes and no. Insofar as people cannot agree on the precise defi-20 nition of induction, or dispersion, or electron transfer, or polari-21 zation, there can never be a unique EDA. (As a pernicious 22 example, electron transfer energy can always be viewed as an 23 extreme form of polarization, where the electron density of a 24 fragment becomes extremely delocalized. Similarly, the mere 25 idea of a local or regional kinetic energy is mathematically ill-26 defined.) So yes. However, the existence of many partitioning 27 methods leads to ambiguity in chemical concepts, since differ-28 ent EDA methods give qualitatively different explanations of 29 chemical phenomena in many cases. So no-it is not fair to 30 "blame", the coexistence of many partition systems on the 31 ambiguity in chemical concepts any more than it is fair to 32 blame the ambiguity of chemical concepts on the existence of 33 myriad partitioning schemes. 34

### Farnaz Heidar-Zadeh

37 Given that chemical concepts are nonempirical, any attempt 38 toward quantifying them is doomed to be nonunique. Par-39 titioning schemes are no exception! Considering the fact that partitioning schemes cannot be defined accurately, putting too 40 much effort into the precision of various definitions is futile. Each 41 scheme starts from a different set of assumptions (some of 42 43 which may be unknown or not carefully laid out at the begin-44 ning) and consequently gives a different set of results. The best 45 one can hope for is having a rigorous mathematical definition of partitioning schemes (and other concepts) which confirms chem-46 47 ical trends and aids us in rationalizing the behavior of molecules 48 and materials. So, even though it is interesting to quantitatively 49 compare various schemes (i.e., the so-called precision of various 50 schemes), only their qualitative comparison can truly testify to 51 their value (i.e., assessing how various schemes comply with or 52 improve chemical reasoning is the closest thing to an accuracy 53 check we can dream of). As G. Frenking clearly explained, these 54 schemes are tools for making sense of numerical results of quan-55 tum chemistry calculations in terms of familiar classical chemical 56 concepts and depending on the problem at hand, some of these tools will be more/less useful than the others. 57

		System		
		Same	Different	
qe	Same	Reproducible	Replicable	
ů	Different	Robust	Generalizable	

### Juan Andrés

Many chemical concepts (aromaticity, chemical bonds, oxidation states, and atomic charges) employed in chemistry today can be traced to the early stages of the field, notwithstanding the significant developments, refinements, and extensions made during the last years. Chemical nature aside, the terminology is introduced by these chemical concepts is now ubiquitous and has had a pronounced effect on the way that chemistry is practiced and taught. These concepts remain invaluable in providing frameworks that allow us to rationalize trends in chemical structure and reactivity, as well to realm current knowledge, consideration of new observations, and finally as pedagogic instruments.

76 These concepts described above were established without 77 fully understanding the physical principles underlying the inter-78 actions between electrons and atomic nuclei. As Robert Heinlein 79 wrote, "The difference between science and the fuzzy subjects is 80 that science requires reasoning while those other subjects 81 merely require scholarship". The work of Jansen and Wedig<sup>[86]</sup> 82 serves as an example of how chemical concepts (in this case, 83 atomic charge and oxidation state) can achieve progressively 84 improved operational definition. Unfortunately, their concepts 85 are not observables, that is, there is no quantum mechanical 86 operator that would work on the wave function to give the 87 corresponding value as an observable. They can be criticized for 88 being unphysical and nonobservable; although are highly useful 89 but often not backed by solid theory, in particular, not by quan-90 tum mechanics. This a very common situation approach in 91 chemistry and it is an inherent part of various quantum tools uti-92 lizing chemical concepts in molecules and crystals. One way of 93 overcoming this conundrum was proposed recently by Ayers 94 et al.<sup>[87]</sup> in which an axiomatic approach to chemical concepts is 95 introduced. Therefore, it is lack of precision in the definition of 96 many chemical concepts one of the reasons for the coexistence 97 and proliferation of many partition schemes. Moreover, our 98 future findings have immediate implications for the development 99 of the next generation of physically motivated procedures to be 100 able to capture the physics of the chemical concepts properly, a 101 new strategy is needed to take the benefits of fully into account. 102

### Yirong Mo

The literal definitions and conceptual understanding of various 105 concepts are often consistent and shared by all chemists. But in 106 the process of realizing these concepts, one need to use 107 approximations and set up rules within one's field (e.g., either 108 molecular orbital theory or valence bond theory or different 109 MO methods). This can be understood as getting more precise 110 definitions. As a consequence, different approximations lead to 111 different partition schemes with different (sometimes con-112 flicting) outcomes. For instance, we often regard charge transfer 113 as a process occurring from one monomer to another 114

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monomer, or from one fragment to another fragment of one molecule, or approximately from one fragmental HOMO to another fragmental LUMO. But, in computations, we need to define the fragmental orbitals. Here the disparity comes up because we usually get only canonical MOs which are extended over the whole system. Approximations are introduced to get fragmental orbitals and different approaches lead to different solutions and eventually different energy terms.

### 10 Eduard Matito

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Yes, but in my opinion, it is actually one particular chemical concept that is most responsible for the proliferation of energy partitions. Since an atom in a molecule (AIM) is a fuzzy chemical concept, it is only natural that many partition schemes coexist. This most evident in the case of real-space energy partitions: we can have as many such energy partitions as definitions of AIMs. In this sense, one way to reduce the number of energy partitions would be to focus on the reliability of the AIM definition. For instance, we have found that some AIMs do not provide correct predictions when they are used to analyze certain properties (see my answer to question 4).

### 23 Eloy Ramos-Cordoba

24 Since traditional chemical concepts are not observables, they 25 are not well defined in the context of quantum mechanics. As a 26 consequence, a given chemical concept can, in principle, be 27 described by many different mathematically rigorous partition 28 schemes. The number of reasonable schemes can be reduced 29 by imposing a series of physical constraints on the partition for-30 malism. For instance, in variational EDA, one can impose that all 31 the intermediate wavefunctions must be antisymmetrized. 32

# <sup>33</sup><sub>34</sub> W. H. Eugen Schwarz

35 Many chemical concepts should not only comply with the general 36 laws of basic physics, but at best also match the set of specific 37 chemical materials of interest, the properties, and reactions of main 38 interest, and the ways different chemists are trained to understand 39 and intuitively guess and predict them. The chemical concepts should be designed in a clear, unique, rational, consistent, and pur-40 41 posive manner. Accordingly, there will and shall emerge related, slightly different concepts, without lack of conceptual quality. A 42 simple example is the partitioning of interatomic distances, 43 44 modeled by sums of various types of "atomic radii" (van der Waals 45 radii opposite and orthogonal to a bond, ionic radii for different formal charges and coordination numbers, covalent radii for differ-46 47 ent formal bond orders, hydrogen bond radii, etc.). The richness of 48 chemistry requires a richness of concepts and schemes.

49 Namely, Physics is the science of matter in simple, prototypi-50 cal, ideal sectors of reality, to be described in the most general 51 and most accurate way. Chemistry is the science of matter in 52 complex, special, realistic, and "human" cases, to be described 53 in a useful, simple and appropriately and reasonably reliable 54 way. ("Human" conditions here typically mean matter around 55 temperatures of 300 K  $\times$  10<sup> $\pm 2$ </sup> and pressures of 1 atm  $\times$  10<sup> $\pm 4$ </sup> during timespans of 1 h  $\times$  10<sup> $\pm 6$ </sup>.) Physics and chemistry are two 56 57 hard sciences of different kind.

In principle, physics is more distinct and chemistry is fuzzier. 58 59 That is, "lack of precision" may exists in cases where one is still in the phase of development of the chemical concepts, but it 60 is misleading and biased discrediting the principle of fuzziness 61 as a lack of some improper requirement in mature scientific 62 cases. Also note that the clear physical concept of, for exam-63 ple, an electronic particle (in a molecule) in the low-energy 64 approximation fades away in the high energy regime (near 65 heavy nuclei), where it must be replaced by the electron-66 positron matter field of noncoinciding charge, mass and spin 67 distributions. Or the clear physical concept of a sharp spatial 68 boundary (sometimes postulated between "atoms" in a mole-69 cule) in the low-velocity approximation fades away in the real-70 istic relativistic regime. 71

Therefore, many chemical concepts cannot be that general 72 and unique as most of the basic physical concepts. They have 73 to be appropriately adjusted to the ranges of materials, to the 74 typical conditions and to the useful purposes, which the 75 researchers want them to apply to. Experienced researchers 76 with some special interest in some field of chosen materials will 77 78 search for useful parameters as a quantification of their experience-quided fuzzy ideas. Related concepts of different scholars 79 may be analyzed with the help of statistical techniques, see 80 below. 81

Finally, we must distinguish between descriptive, analytic, and 82 explanative concepts. Description is the qualitative or quantita-83 tive specification of the interactions of some specimen with its 84 surrounding, as given by nature and its laws. (The specimen 85 may be a molecule or nanoparticle or droplet or crystallite or 86 surface layer etc. of some material or compound. The interac-87 tion properties may be described by mass, charge, polarizabil-88 ity, color, chirality, various specific reactivity parameters, etc.) 89 Respective probability distributions and source functions of 90 these interaction properties can be analyzed in spatial detail, as 91 for instance in the QTAIM. As long as no restraints of the 92 description are imposed, such as monopole approximations, or 93 same average values for whole sets of specimens or homolo-94 gous series, the descriptive parameters should be comparatively 95 unique. 96

There are then two further steps toward a deeper under-97 standing of WHY is WHAT is. First, there is the question of the 98 internal structure of the data, and relations between them. That 99 is so to say an "autonomous" intrachemical approach. One 100 approach is by additive increment systems, approximating the 101 property parameters of compounds by sums over atomic, 102 diatomic, and possibly multi-atomic (three-center or ring) con-103 tributions. Examples are effective atomic radii, effective atomic 104 charges, ionic conductivities, diamagnetic (Pascal) increments, 105 diatomic bond energy increments, spectroscopic ligand field 106 parameters, stereospecific ligand parameters, and so 107 on. Depending on the chosen set of compounds, the chosen 108 types of properties, and the perspectives of the researchers, 109 related alternative partition schemes may emerge, where the 110 increments may have different meanings. As long as observable 111 properties  $P_i$  of specimens *j* can reasonably well be approxi-112 mated by different sets of increments  $b_k$  and  $d_l$  as in eq. (1), it 113 is fine 114

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$$P_{j} \approx \sum_{k \text{for}i} b_{k} \approx \sum_{l \text{for}i} d_{l} \tag{1}$$

We remember the interchange theorem of double-perturbation theory, where a response property for two perturbations can be represented by two different types of expressions, giving different perspectives of insight. The success in the development of research and teaching of chemistry should decide which schemes survive. Suggestions as by the Bader school that chemists should give up those useful analysis tools that do not fit into their special frame of the QTAIM approach do not appear fruitful.

11 Second, one shall search for connections between specific sec-12 tors of chemical experiences and the general framework of physi-13 cal theories. That is the *reductive* interphysicochemical approach. 14 In order to construct intuitively convincing and theoretically sound 15 arguments, one usually needs a two-step analysis. To understand, 16 why a chemical compound system forms and behaves in this 17 manner, one also needs to understand why the chosen fragments 18 or reference states relax or response in the manner they do. To 19 this end, measuring or calculating the stationary molecule of inter-20 est or the overall changes upon a chemical reaction is not 21 enough. One must choose both appropriate references and appro-22 priate intermediates, which both are not uniquely determined by 23 nature, for instance when analyzing covalent or dative or ionic or 24 various secondary interactions. The real world is a quantum world 25 (with the emergence of classical features due to quantum 26 decoherence), yet it is admissible to apply classical physical con-27 cepts in real chemistry, as more or less excellent approximations. 28 Similarly, one may, at least for "separated" fragments and even for 29 overlapping intermediates, discuss what would happen in a classi-30 cal world with states that are "nonexistent" in reality, since they 31 violate the Pauli principle, and talk about Pauli forces.

32 In summary, the main reason for the coexistence of related 33 chemical concepts is that chemists may take different viewpoints 34 and ask nonidentical questions, looking into real space and/or 35 onto the quantum field in space. The development of computa-36 tional methods may open the birth and survival of more options, 37 while unreliable approaches of extreme computational simplicity 38 (the arbitrary AO basis in the Mulliken population analyses) may 39 disappear. Modern scientific chemistry was given birth in the 40 1780s (by Lavoisier, his wife Marie-Anne Pierrette Paulze, and 41 their Parisian colleagues) with the invention of the chemical ele-42 ments as the conserved entities in chemical reactions, and the 43 representation of macroscopic materials by atoms in molecules 44 (by Dalton in the 1800s). The very basis of scientific chemistry is 45 the fuzzy concept of microscopic elemental atoms in macroscopic 46 stuffs; therefore the typically chemical concepts are fuzzy. Intro-47 ducing physical theory to explain chemistry in an intuitive manner 48 thereby supporting intuitive predictions, which are the basis of 49 fruitful chemical science and technology for the benefit of soci-50 ety, requires the smart choice of physical reference states and 51 more or less physical intermediate states for discussion of the 52 specific physical situation in the case at hand. 53

### Alston Misquitta and Krzysztof Szalewicz

56 On the basis of the description of SAPT presented above, we 57 will now address question number 1. As we have shown above, the physical components of SAPT are uniquely defined and can 58 be computed to potentially arbitrary accuracy. These terms 59 have a precise physical interpretation. The electrostatic energy 60 is the Coulomb interaction of unperturbed charge distributions. 61 The induction energy of second order in V results from 62 response of monomer A (B) to the field of unperturbed charge 63 distribution of monomer B (A). The dispersion energy results 64 from correlations of electron positions between monomer A 65 and B. All these components are precisely defined at all R's, not 66 only in the asymptotic region. Finally, the exchange-repulsion 67 component results from exchange tunneling of electrons 68 between interacting systems. Thus, in the case of SAPT, there is 69 no lack of precision in defining these chemical concepts. Conse-70 quently, SAPT can be used as the standard model for EDAs in 71 the intermolecular interaction sector and EDAs inconsistent 72 73 with SAPT should be discarded.

For induction interactions, one should always consider the 74 sum of induction and exchange-induction corrections, some-75 times denoted as  $E_{indx}$ . The reason is that at R near the van der 76 Waals minimum and smaller, the overlap contributions in 77 78 induction energies become large, leading to large discrepancies between the asymptotic expansion of induction energy and 79 SAPT values,<sup>[88]</sup> larger in magnitude than typical damping 80 effects and of opposite sign. This is due to the fact that for sys-81 tems with one of the monomers having more than two elec-82 trons, the interacting system is submerged in the continuum of 83 Pauli-forbidden states unless such states are projected out by 84 enforcing antisymmetry,<sup>[64]</sup> which is not done in RS. If the 85 exchange-induction term is added, the contributions coming 86 from the violation of symmetry are canceled out to a large 87 extent. When higher-order induction effects are important, as 88 they are in strongly bound systems with a large polarization 89 and charge-delocalization, one should include E<sub>indx</sub> computed 90 to third order in V, as well as the  $\delta_{int}^{HF}$  term. This term is defined 91 92 as the difference between the supermolecular interaction 93 energy  $E_{int}^{HF}$  and the sum of the first-order, induction, and 94 exchange-induction components. 95

### Question 2: Does the Adoption of a Given Partition Scheme Imply a Set of more Precise Definitions of the Underlying Chemical Concepts?

### Ramon Carbó-Dorca

Looks like it does not. The impression is that the great number of partition schemes worsens the definitions of underlying chemical concepts, adding a bit of more fuzziness to their already fuzzy character.

### Shant Shahbazian

In my opinion, there is no such thing as "more" or "less" precise 109 quantitative definition of a chemical concept and all mathematically rigorous definitions of a concept are equally precise and 111 definitions lacking mathematical rigor do not deserve to be categorized as quantitative. Assuming that the intended partitioning schemes are rigorously constructed, the concept of 114

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1 interest is also precisely defined within the "context" of each 2 given partitioning scheme. The problematic situation appears 3 when one tries to compare the nonequivalent definitions not 4 within, but between various partitioning schemes. As I stressed 5 also in answer to question 1, this is the result of "over-quantification". At a personal level, one may simply dismiss all available 6 7 partitioning schemes but a single one and adopt the preferred scheme trying to avoid the dilemma though, at the level of 8 9 community the problem retains (the relevant literature however hardly supports that even at a personal level this is the pre-10 ferred strategy). Since part of what we mean by precise defini-11 12 tion is the "consensus" of a scientific "community", not a single 13 person, to use the "preferred" partitioning scheme, without a 14 consensus the above-mentioned formal mathematical view-15 point on the precise definition is at best handicap. These are 16 the motivations to address questions 8 and 9.

#### István Mayer 18

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Any partition scheme is based on a selected well-defined definition of the atoms within the molecule.

#### 22 Martin Rahm 23

In one way of looking at it, yes. Chemical concepts are what we 24 make of them. Different chemists can and will have different 25 opinions on the best definition of what is covalence, electro-26 negativity, etc. Differences in such definitions are also a conse-27 quence of the development of the concepts over time. 28 Different partition schemes will naturally be a reflection of this. 29 As such, different EDA schemes can provide precise definitions 30 within their respective frameworks. If a particular incarnation is 31 chemically useful is another question. 32

#### 33 Frank Weinhold 34

35 Not in any rational process of advancing science. Any EDA com-36 ponent "label" is a language construct, not a "concept" per 37 se. The correlations (if any) between EDA component labels 38 and more broadly understood chemical concepts should be 39 demonstrated, not assumed.

### Ángel Martín Pendás

If an EDA is seen as a way to compress (or to compact) the complex energy information content of a wavefunction (or set of wavefunctions if references are needed), different EDAs should provide different readings of the same physical (or mathematical) objects. In this sense, all EDAs should be compatible among themselves (and that is why I advocate partitions which can be applied to any or at least to a large class of wavefunctions). By understanding how different methods read the same function providing different answers, the limits and windows of applicability of the underlying chemical concepts might probably be sharpened.

### David L. Cooper

56 There are indeed senses in which the adoption of a particular partitioning scheme leads to more precise definitions of particular EDA "labels" within that scheme, but such "labels" are 58 likely to have somewhat different meanings in equally valid 59 alternative approaches. I agree with Frank Weinhold that sup-60 posed correlations with underlying chemical concepts need to 61 be demonstrated, without any such links simply being 62 assumed. I am also struck by a point that is reiterated in a 63 recent perspective article<sup>[89]</sup>: the use of models (including EDA 64 schemes) can risk blurring the distinction between what is 65 really mathematical modeling and what is, at least in some 66 sense, an underlying chemical/physical "reality" or a "meaning-67 ful set of concepts". [That particular article classifies exchange. Pauli repulsion, and orbital interactions as being part of the mathematical model, and it also addresses the extent to which there is really any proper distinction between charge transfer and polarization. Then again, picking (say) exchange, it can be important to remember that not everyone agrees as to what such entities really signify even in a qualitative sense.<sup>[90]</sup>]

### Carlo Gatti

Not necessarily and surely not in the present state of affairs. Chemical concepts are in general very much intertwined in the energetic terms of the various EDAs based on orbital space decompositions and they may be so to a different extent, depending on the given scheme adopted. A clear and enlightening analysis of this rather convoluted problem is presented in 82. I'm personally in favor of retaining only those energy partitioning schemes where each energy component has a clearly defined physical basis and then of possibly observing whether and which of these components may be roughly related to chemical concepts, if any. This is the typical situation one is facing with position space EDAs, like IQA. To make an example, charge transfer, which is a typical chemical concept, may be clearly defined and easily evaluated with all these approaches. However, it is not possible to isolate its energetic impact in standard real space EDA schemes. One should make recourse to the theory of resonance structures in real space to estimate such energy component.[91]

### Paul Popelier

According to the way I answered guestion 1, the current guestion sounds almost like the opposite of question 1, and thus I am inclined to answer yes. As a fan of IQA (a sentiment to be updated when something better comes along) I am happy (hopefully not naively) with the way this EDA defines the following chemical concepts: covalency (via exchange), ionicity and polarity (via electrostatics), dispersion (via electron correlation), and steric effects<sup>[92]</sup> (via the intra-atomic or self-energy). 105 Because IQA is able to also provide intra-atomic "dispersion" it 106 has the potential to perhaps define a new chemical concept, 107 which focuses on stability of weakly bound van der Waals com-108 plexes but then from an (intra)atomic point of view. 109

### Pedro Salvador

If we assume an atom-in-molecule definition being a partition 112 scheme, I think the answer is yes. Not only the numerical results 113 differ from one AIM to another (sometimes quite dramatically), 114

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but some particular chemical concepts may only be achieved by making use of a given AIM. This is, for instance, the case of the so-called "overlap population", which can only be accounted for with "fuzzy" atomic domains. This, however, compromises this particular concept, which probably should be considered deprecated. In a way, one should stick to chemical concepts that can be achieved, at least quantitatively, with any reasonable (see question 7) partition scheme.

### Jerzy Cioslowski

As put succinctly by István Mayer in his answer above, "any partition scheme is based on a selected well-defined definition of the atoms within the molecule." However, in the case of energy partitioning schemes formulated in terms of (imaginary) physical processes, specification of the order of their application is equally important (see my response to question 1). Thus, the implication is always one way, namely definitions of chemical/physical concepts) energy partitioning.

### Gernot Frenking

I agree with Martin Rahm that "Chemical concepts are what we make of them." A useful partitioning scheme should indeed lead to a more precise definition of the underlying chemical concept. Five conditions are to be fulfilled by a reasonable partitioning scheme: (1) it should be based on accurate quantum chemical calculations; (2) it should be mathematically unambiguously defined; (3) the results should be largely independent of the level of theory used; (4) the different terms should lead to a plausible interpretation; (5) it should be useful for chemical problems. The adoption of a particular partition scheme comes from its usefulness. The agreement with chemical concepts is a fuzzy condition because chemical concepts are fuzzy. I think that this comes out of the necessity to bring the pandemonium of chemical facts into an ordering scheme in terms of rules and models, which are accessible to the human mind. I was puzzled by the statement in Ref. [82], that the use of bonding models "sometimes leads to a blurring of the distinction between mathematical modeling and physical reality." In the guantum world, physical reality of an electron is not entirely assigned to its electronic charge distribution, which represents only a pro-41 jection onto a space of lower information content; its complete-42 ness is only provided by its wave function  $\Psi$ . The wave 43 function  $\Psi$  contains more information about the behavior of 44 the electron than  $\rho$ . In chemistry, this comes to the fore for 45 example in the outcome of pericyclic reactions, or in any spec-46 troscopic investigation, which can only be explained when the 47 symmetry and sign pattern of  $\Psi$  are considered. 48

# <sup>49</sup><sup>50</sup> Émilie-Laure Zins

Most of the current chemical concepts are based on the observations, interpretations, and intuitions of experimental chemists. One of the roles of theoretical chemistry is to explain and develop chemical concepts based on the fundamental equations of quantum physics and to link these concepts to those of the experimental chemists. Thus, the use of any partition scheme to explain any empirical chemical concept should lead to more precise definitions of the underlying chemical concepts58from the perspective of our community, provided that the59energy partition is based on variables that have physical significance. However, experimental chemists will not necessarily be60immediately convinced by the increase in precision that we can62bring to empirical concepts they work with on a daily.63

### **Miquel Solà**

It is an advantage, not a problem, to have different partitions schemes as far as they prove to be useful, to be rooted in quantum mechanics, to be mathematically unambiguous, to provide physically meaningful energy terms, to give insight, and to possess predictive power. Let me quote Dewar who said: "the only criterion of a model is usefulness, not its *truth*".<sup>[93]</sup>

### Paul W. Ayers

In a narrow sense, once one chooses a partitioning method (either for the atom-in-molecule or the energy-into-fragments) then those choices can be profitably used as a "model chemistry" to elucidate chemical phenomena, to observe trends, and to draw inferences. In this sense, all computed quantities within the selected partitioning are "precise" (in the sense of being exactly defined) within the context. However, a different partitioning method might reveal different trends and different insights that are not less precise, but merely more or less useful (as a matter of preference and opinion).

### Farnaz Heidar-Zadeh

A well-defined scheme is based on a rigorous set of physical assumptions, consequently, it consistently prescribes the definition of underlying chemical concepts. So, I would use the term "consistent" instead of "precise." This gives an elegant and unambiguous framework for further developing concepts. Even if a concept was proposed on heuristic grounds, but proved to be useful, establishing a framework within which it is mathematically justified is essential.

### Juan Andrés

As Solà remarked recently<sup>[94]</sup>: "My usual answer is that the most 99 fruitful concepts in chemistry share the same lack of strict defi-100 nition.<sup>[95]</sup>" In addition, there is not a unique way to compute 101 quantities related with such intuitive chemical concepts and 102 therefore, partition schemes. As Martín Pendás et al. write<sup>[96]</sup> "A 103 chemical bond has an energetic strength (its bond energy) that 104 is somehow connected to a particular electron count (its bond 105 order). Interestingly, neither bond energies nor bond orders are 106 (Dirac) observables. The former vanish into thin air once we 107 pass from diatomics to polyatomics, whereas the latter too 108 often rely on the orbital approximation. Notwithstanding, 109 chemists feel comfortable with such an edifice otherwise built 110 on shifting sands". Therefore, the different partition schemes 111 need to be rooted in guantum mechanics, to be mathematically 112 unambiguous, in order to provide physical basis of the underly-113 114 ing chemical concepts.

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Due to the lack of direct experimental data to endorse any partition scheme as individual energy terms are not observables, it is hard to reach any consensus in adopting any particular partition scheme. Users adopt certain partition schemes often based on the accessibility and their own familiarity. Nevertheless, there are indirect experimental data to justify partition schemes, though it is everyone's taste whether to believe or not.

### Eduard Matito

As it has been repeatedly said, a model should be judged by its 13 usefulness. In the context of this question, the usefulness refers 14 to the faithfulness with which it represents the underlying 15 chemical concept. Since I understand the guestion as "can the 16 energy partition go beyond the definition of some concepts", I 17 am inclined to say that it pretty much depends on the fuzziness 18 of the concept. Fuzzy concepts can be surpassed (and rep-19 laced!) by the model, the temperature is a nice example of this 20 kind, as Shant indicated earlier. Aromaticity could be a more 21 current example of a fuzzy concept that has been influenced 22 by computational models and tools. However, it is difficult to 23 imagine that energy partitions can go beyond long-standing 24 and more consistent concepts. In particular, concepts that 25 transgress computational chemistry (and even chemistry) are 26 difficult to change. 27

### Eloy Ramos-Cordoba

By selecting a particular partition scheme, the ambiguities on the underlying chemical concepts disappear within the framework of that particular decomposition. As Prof. Mayer stated above, energy partitioning schemes are mathematically welldefined, and so are the energetic components that one can extract from them.

### W. H. Eugen Schwarz

No: In principle, experimental and theoretical inquiries are auton-39 omous, with theoretically defined and empirically originated con-40 cepts to be connected as well as possible. Empirically motivated 41 concepts need improvement if theoretically shown to be inter-42 nally inconsistent, while theoretical constructs are senseless if 43 unrelated to empirical concepts. The correspondence of a partic-44 ular theoretical partitioning scheme to some particular chemical 45 observation-coupled concepts attaches guantum chemical mean-46 ing to the latter ones. This may in some cases help more pre-47 cisely specifying the empirical concepts. Since most chemical 48 concepts are fuzzy to become broadly applicable, this correspon-49 dence will remain somewhat fuzzy. 50

### Alston Misquitta and Krzysztof Szalewicz

As stated in the answer to Q1, SAPT partition scheme does provide a precise definition of the chemical concepts such as electrostatic, induction, dispersion, and exchange energies. While
EDAs that are in a significant disagreement with SAPT should
not be used, the question arises what is the threshold for such

cutoff. While it is difficult to set any strict limits, perhaps a few 58 percent agreements should be the goal. The agreement is best 59 for Morokuma-type methods which are based on iterations of 60 Hartree-Fock equations starting from monomer orbitals. See 61 Ref. [97] for recent comparisons. On the other hand, methods 62 decomposing supermolecular interaction energies using local-63 ized molecular orbitals (LMO) can only agree with SAPT in an 64 65 approximate way.

Another criterion is the asymptotic behavior. The exchange 66 components should decay purely exponentially, that is, should 67 not involve any  $1/R^n$  terms. The electrostatic, induction, and dis-68 persion components should decay as appropriate powers of 1/ 69 R. In methods based on LMOs, these criteria are difficult to sat-70 isfy at very large intermolecular separations since, by the very 71 nature of LMOs, the dispersion terms always have a small com-72 ponent originating from the intramonomer correlation contri-73 bution to electrostatic energies, so that for polar systems at a 74 large R, the  $1/R^3$  decay of the latter energies will dominate. 75

The electronic structure theories that are most advanced, 76 most complex, and therefore, most difficult to interpret physi-77 cally. Therefore, one sometimes chooses to use manifestly inac-78 curate theories like Hückel theory because of the 79 understanding it yields. Here is where SAPT shines as it con-80 structs the interaction energy from the sum of physical compo-81 nents. Importantly, there is nothing ambiguous about these 82 definitions, although there are some issues we need to be 83 aware of, as described in the next paragraph. 84

There is no ambiguity in the asymptotic region where orbital 85 overlap effects can be neglected, and, what is very important 86 for physical interpretation, in this region the multipole expan-87 sion can be used to cast the interaction energy components 88 (electrostatic, induction, and dispersion) in terms of the molecu-89 lar properties like the electrostatic multipoles, and static and 90 frequency-dependent polarizabilities. SAPT interaction energies 91 agree with those from the multipole expansion to arbitrary 92 accuracy provided that R is large enough. Thus, SAPT is seam-93 lessly connected to the multipole expansion. Since the multi-94 pole expansion of interaction energy is expressed in terms of 95 multipole moments and static and frequency-dependent polar-96 izabilities of monomers, this adds another level of physical 97 insight into SAPT interaction energies. Furthermore, there is a 98 smooth transition between the overlap region and the asymp-99 totic region. The monomer densities used to calculate the elec-100 trostatic energies can be replaced by a set multipole moments 101 at large R. Similarly the density-density response functions can 102 be replaced by polarizabilities. The multipole moments as well 103 as static and frequency-dependent polarizabilities are measur-104 able, thus providing a strong link of SAPT components to 105 experiment. This is, at least in the region of small density-over-106 lap, an unambiguous link. This feature alone separates SAPT 107 from all EDA methods since, to the best of our knowledge, no 108 relation to experiment is possible in these methods. 109

While all acceptable variants of SAPT must have the same110asymptotic behavior as SRS, and therefore, the components are111asymptotically unique, one may question the uniqueness in the112overlap region. Fortunately, all acceptable SAPT variants give113identical first-order energies and second-order induction and114

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dispersion energies. The nonuniqueness appears only in the second-order exchange corrections. Of those, the exchange-2 3 dispersion energies are relatively small so the potential differ-4 ences can usually be safely ignored. The differences in 5 exchange-induction corrections are eliminated by the  $\delta_{int}^{HF}$  term. 6 Also, some variants that perform best in all orders are equiva-7 lent or very close to SRS in low order. In conclusion, whereas 8 there is a small nonuniqueness in definitions of physical contri-9 butions resulting from the flavors of SAPT, differences between 10 best theories can be ignored.

### **Ouestion 3: How Can One Use the Results of a** Partition Scheme to Improve the Clarity of **Definitions of Concepts?**

### Ramon Carbó-Dorca

In case one can observe such a publication phenomenon, time which provides with various research fashions and hypes the research panorama will act as the way partition schemes appear from previous techniques and evolve into new schemes, according to the increasing number of researchers in guantum chemistry and their publication needs. Perhaps leaving apart the real research task of understanding molecular behavior within a general framework valid in any circumstance.

#### 26 Shant Shahbazian

In my opinion, there is no direct relationship between the 28 results of a partitioning scheme and the clarity of chemical con-29 cepts. As I stressed in answer to question 1, to have a well-30 defined concept, a comprehensive theory for the concept of 31 interest must be developed. Let me give an example. While 32 humans had always an intuitive qualitative understanding of 33 temperature, since the time of Galileo people tried to quantify 34 this intuition through constructing various thermometers. In 35 one sense, in this period, temperature was an index of 36 hotness/coldness but temperature only conceived as a physical 37 "observable" when thermodynamics was formulated and the 38 absolute temperature was introduced independently from ther-39 mometers, based on its relationship with internal energy and 40 entropy. In other words, thermodynamics is an organized web 41 of connections between various thermal concepts and the posi-42 tion of each concept, for example, temperature, in the web 43 makes it a well-defined and clarified concept.<sup>[98]</sup> What currently 44 lacks in theoretical chemistry is a similar comprehensive theory 45 (or theories) that not only introduce each chemical concept 46 quantitatively but also makes a web of relationships between 47 various concepts. Index-based view in computational chemistry 48 that focuses only on quantitative definition of a single concept 49 lacks such capability and, in my opinion, current partitioning 50 schemes are also no exceptions. 51

#### 52 Martin Rahm 53

54 It would depend on the concept in question. For example, I 55 have, together with Roald Hoffmann, redefined the chemical concept of electronegativity within the framework of the 56 "Experimental Quantum Chemistry"-partitioning.<sup>[54]</sup> Together 57

with Tao Zeng, this precise definition allowed us to revise the 58 scale of atomic electronegativity in a way that compares well 59 with previous scales, such as Pauling, Mulliken, and Allen.<sup>[56]</sup> 60 Other chemical concepts such as "covalence" and "ionicity" are 61 less straightforward. One way toward clarifying such concepts 62 is to use EDA-descriptors and creates maps of chemical interactions. In well-known materials under ambient conditions we mostly know what to expect: NaCl should come out as ionic, a C-C bond better have some covalency, and the helium dimer should be different from the previous two.<sup>[55]</sup> A partitioning scheme that agrees with conventional wisdom, while providing new insight, has a better chance of improving the clarity of definitions of chemical concepts.

### Frank Weinhold

Reference [99] serves as an example of how a concept (in this case, "hydrogen bond") can achieve progressively improved operational definition. Can any component of any current EDA partitioning scheme meet the operational criteria of mutually consistent correlations with experimental properties, as illustrated in this work?

### Roberto A. Boto

On the one hand, a partition scheme is built from some theoretical framework, which at the same time, is built from a set of, in principle, well-defined concepts. Therefore, the quality of the results should be determined by the theory behind. It is hard to imagine a feedback process.

On the other hand, energy partitions could be constrained to follow some conditions, such as produce energy contributions within the chemical scale, or equalize energy terms obtained by different partition schemes. These would not improve or worsen the definition of concepts but would add some uniformity into the different definitions of the same chemical concepts.

### Ángel Martín Pendás

Uhm, well, some of the most cherished chemical concepts do implicitly rely on some kind of partitioning. Covalency, for instance, is one of them. Whatever source is used to find an operational definition (including IUPAC's gold book) of what we mean by a covalent bond will include the word "sharing." And sharing implies at least two objects which share, so a partition. Typically those objects are understood as atoms, so in some sense, partitioning schemes may help develop a concept in a bootstrapping process, as in the temperature example commented by Dr. Shahbazian.

### Julien Pilmé

In my opinion, results obtained from only one partition scheme 109 are probably not sufficient to really clarify the definition or the 110 meaning of simple concepts commonly used in chemistry 111 because most of these concepts go beyond any partition 112 scheme. Maybe, if the targeted concept has a typical "signa-113 ture" which can be identified through several partition 114

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schemes, the confrontation of results arising from numerous partition schemes would be useful to improve the definition of the concept. I think for example that the case of the covalent bond, already reported by Ángel, falls into this category.

### Carlo Gatti

I see a risk in this process as chemical concepts evolve and generally become wider and more general with time. One good example is aromaticity. Though hardly definable, the concept of aromaticity has now largely expanded and it is no longer limited to pi-orbital organic chemistry but proved useful in describing bonding and energy stabilization in many inorganic molecular compounds and also in the solid state. Not to talk about recently discussed organic molecules where pi- and sigma-aromatic chains seem to coexist. Therefore, in my view, a physically grounded partition scheme should not be aimed at improving the clarity of definition of a concept, which may possibly evolve, but be able to include and to some extent predict the future evolution of that concept. It is only through this process that the partition scheme will help to improve the clarity of a concept. Non-nuclear attractors and their properties were defined while studying Li clusters as a straightforward extension of Bader's space and virial partitioning. But have then recovered in many other chemical situations, both at ambient or at high pressure and featuring the broad concept of interstitial or "isolated" electrons.

### Paul Popelier

An example of how to use the results of a partition scheme is that of the EDA called IQA being combined with the newly proposed Relative Energy Gradient (REG) method.[100] The REG method is able to handle, automatically and exhaustively, the typically hundreds of individual energy contributions that IQA generates. REG ranks atoms to the degree that they act like the total system they are part of, in terms of energy changes. This minimal method can handle competing for energy contributions, which may appear contradictory and thereby fuelled ongoing debates. For example, in our very recent biphenyl case study,<sup>[101]</sup> we use REG-IQA to explain its planar rotation barrier. The central torsion angle in biphenyl prefers to be 45° and when at 0°, biphenyl's total energy profile reaches a local maximum. REG shows that IQA's intra-atomic energies of the orthohydrogens dominate the barrier, which is compatible with the textbook explanation of a steric clash. However, at the same time, the exchange energy between these two orthohydrogens becomes most stabilizing at 0°, indicative of the formation of a covalent bond. REG is not confused by these two opposing effects and concludes that, while they largely cancel out, it is the energy behavior of the orthocarbons that causes the rotation barrier. This is an example of the Dutch expression "als twee honden vechten om een been loopt de derde er mee heen." (Note: just in case you GoogleTranslate this then know that "been" actually means "bot").

### Pedro Salvador

As Martin stated, that would depend on the particular concept.
For instance, the concept of Oxidation State has lacked a clear
definition for years, but the problem was not related to any

partitioning, but to the rather vague terminology used. After 58 IUPAC has recently revised the concept (albeit not in a fully sat-59 isfactory way in my view), new first-principles schemes<sup>[102]</sup> 60 (which at the end of the day also make use of a partitioning 61 scheme) can be devised to match with the so-called chemical 62 intuition. Another illustrative example is that of the "local spin". 63 In this case, it is the nature of the mathematical object that 64 needs to be partitioned (which particular formulation of the 65 expectation value of the spin-squared operator), rather than the 66 actual partition used that brings about meaningful numbers for 67 this concept.[103] 68

As I stated in the previous question, concepts that can be achieved only by using specific partition schemes are undesirable. At the same time, a given partition scheme is put into jeopardy when it cannot reproduce even qualitatively the expected results/trends of a well-established concept. So, instead, concepts could be (wisely) used to improve the definition of partition schemes.

### Gernot Frenking

Chemical concepts are fuzzy objects, which may be defined in different ways. Carlo Gatti mentioned already aromaticity, which can be defined by energetic, geometric, magnetic, or other criteria such as chemical reactivity. I refer to the five conditions given in my answer to question 2, which should be fulfilled by a partitioning scheme. Other than this, I see no further clarification of the definition of a concept.

### Julia Contreras

For a partition scheme to improve clarity, it should be able to do just what any other theory is expected to do: describe what we know and predict what we do not. Both Hilbert and real space energetic decompositions have been focused on describing what we know, plaguing the literature with different views of things for what we have an intuition. However, in my viewpoint, more efforts should be paid in describing things for which we do not have an intuition (e.g., high pressure) and predict what will happen in those cases. After all, that is what most chemical concepts were born for. I have the impression we have been focused on giving mathematical definitions to concepts that were born without the need for a mathematical framework, and we have barely gone beyond that.

### Émilie-Laure Zins

I am not convinced that there can be a single way to use the 103 results of a partition scheme to improve the clarity of all chemi-104 cal concepts as suggested by the question. In the case of defini-105 tions of weak intermolecular and intramolecular interactions, it 106 seems to me that a quantitative approach based on energy 107 decomposition analysis followed by a principal component 108 analysis may be a promising way to clarify the definitions and 109 to properly classify the interactions. 110

### Laurent Joubert and Vincent Tognetti

It is not obvious from our point of view that the exactness of 113 an energy partition (or even its usefulness) is correlated to its 114



1 use for deciphering chemistry. To expand this point, it is important to recall that (as already stated by Jerzy Cioslowski in dis-2 3 cussion for question 1) EDAs can be divided into two main 4 categories: those obtained during the generation of 5 wavefunction or molecular energy, and those coming from a subsequent post-treatment. Let us, for instance, consider a MPn 6 7 calculation: it will naturally provide a decomposition into vari-8 ous additive contributions, from the zeroth to the *n*-th pertur-9 bation orders. Alternatively, KS energy is by definition split into the KS kinetic energy, the interaction energy between electrons and nuclei and the Hartree and exchange-correlation contribu-11 12 tions. One can then wonder whether such decompositions may 13 convey chemical information. For instance, the second-order 14 correction in MP treatments is often linked to dispersion 15 (London) effects. Conversely, the chemical meaning of KS 16 kinetic energy (related to the fictitious noninteracting system, 17 and not to the real one) is far from being obvious, as well as 18 exchange-correlation since it involves corrections to kinetic 19 energy and electron repulsion. KS thus provides direct energy decomposition without meaningful chemical information. Note 20 21 that a second exact additive KS decomposition could be 22 straightforwardly obtained from first principles with the orbital 23 energies and exchange-correlation potential. However, it is not 24 deprived of drawbacks: (1) what is the meaning of KS orbital 25 energies? (2) how to interpret the other terms? For the first point, the only exact result is that the HOMO energy is opposite 26 27 to the vertical ionization potential if the exact exchange-28 correlation functional is used. The second problem can be cured using Mel Levy's recent potential shift<sup>[104]</sup> that allows for 29 expressing the total energy as the only sum of orbital energies. 30 Such a scheme would certainly simplify energy decompositions, 31 32 but it is still in the youth age.

### 34 Paul W. Ayers

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If the "clarity of definition" of a concept was dependent on the "results of a [one specific] partitioning scheme" then I am reluctant to embrace that definition. On the other hand, if the "clarity of definition" of a concept is supported by the "results of a [many nonspecific] partitioning schemes", then that concept is well-founded and defined qualitatively (even if the partitionings might give different quantitative results).

# 43 Farnaz Heidar-Zadeh 44

The results of the partitioning schemes (and other concepts) can clarify their usefulness in capturing chemical and physical phenomena. That is, numerical results can demonstrate the domain of applicability of a scheme and lead us to improve our definitions. So, I believe the results can act as a feedback loop: guiding us to a better formulation of the problem and strengthen our intuition.

### 52 53 Juan Andrés

An underlying theme of the above questions has been the gap that exists, in general, between quantitative quantum theory and chemical concepts. In this context, we agree with the comment by Grunenberg<sup>[95]</sup> "I am not writing against the use of qualitative chemical concepts per se, but against their quantifi-<br/>cation. In many cases, qualitative concepts even in combination58with nonperfect experiments led to real progress in chemistry.60However, one striking attribute of the aforementioned disputes61in the literature is the fact, that many of these quantifications62are triggered by a conceptual farrago and by this, most of these63scientific quarrels are inherently insoluble Some even resemble64mock discussions. (Interestingly, in the course of such discussions, usually one side is referring to a medieval scholastic66"questio." Therefore, we need partition schemes precisely67defined mathematically from the underlying physics to reach68clarity on the definitions of concepts.69

### Yirong Mo

The conflicting results from different partition schemes certainly will certainly attract attentions and stimulate discussion and further research work. In this way, the definitions of concepts can be progressively clarified and eventually quantified.

### Eduard Matito

I refer to my answer to question 2: I believe this can only be achieved in the case of concepts that lack consistency. In these cases, there must be a consensus among different partitions (and within the community) before walking the dangerous path of changing (clarifying, if you prefer) the definition of concepts. Again, I believe the concept of aromaticity serves as a nice example. In the 1990s, the definition of aromaticity given by the IUPAC applied only to ground-state pi-aromatic compounds and, although the current definition of aromaticity is not less blurry than it used to be, now recognizes different aspects of aromaticity such as electron delocalization, particular reactivity, thermodynamic stability, and certain structural features. Many of the latter features have been repeatedly confirmed by the corresponding computational measures/models of aromaticity. In fact, the work still continues. The "Aromaticity" conference organized in Riviera Maya in 2018 by Gabriel Merino, Miguel Solà, and Henrik Ottosson included a round-table session to find a consensus among the members of this community (experimental and theoretical) about an updated definition of the concept.

### W. H. Eugen Schwarz

Yes, for instance: statistical correlations and factor and cluster analyses can work out whether one or more conceptual maincomponents are behind a group of related empirical or theoretical concepts, and how narrow the relations between them are. Theoretical schemes may need revision in the case of poor relation to well-proven empirical concepts.

### Alston Misquitta and Krzysztof Szalewicz

The SAPT partition scheme gives indeed a clear definition of 108 concepts. Consider two polar systems. One of the main concepts appearing in many undergraduate courses is that at large 110 separations this interaction is determined by the simple interaction 111 tion of the permanent dipole moments with its  $1/R^3$  decay. As 112 *R* decreases, contributions from higher multipole moments 113 become important. The sum of all these contributions agrees to 114



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a high accuracy with the SAPT electrostatic energy. Once R is so 1 2 small that the  $1/R^6$  terms matter, contributions from induction and dispersion energies are becoming important. At these R, 3 4 such contributions can be expressed in terms of dipole 5 moments and of the static and dynamics polarizabilities. Again, both components are very accurately reproduced by SAPT. As 6 7 R decreases further, overlap and exchange effects come into 8 play. This does not mean any loss of physical insight despite 9 things getting a bit more complicated. For example, the electrostatic energy is still just the Coulomb interaction of two charge 10 distributions. For the induction and dispersion energies, we 11 12 have to use the concept of density-density response function 13 which also has a clear physics meaning. As the distance 14 between monomers is now of the order of a few angstroms, 15 electrons can tunnel through the potential barrier. Tunneling is 16 one of the main concepts of quantum mechanics, with a clear interpretation. Such clarity of definitions of concepts as outlined 17 18 above cannot be achieved if a decomposition starts from the 19 dimer wave function.

#### 21 **Question 4: Are Partition Schemes Subject to** 22 Scientific Darwinism? If So, What Is the 23 Influence of a community's Sociological 24 Pressure in the "Natural Selection" Process? 25

#### 26 Ramon Carbó-Dorca 27

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A chemically and physically bound piece of research cannot be 28 influenced by anything but the theoretical scheme itself. A par-29 tition scheme, if it really conforms according to quantum 30 mechanics, shall be appropriate to any electronic system. If a 31 system influences the construction of a partition scheme, then 32 there cannot be any hope to obtain a general procedure. 33

#### 35 Shant Shahbazian

36 If at the level of a community there is a consensus on the "intrin-37 sic" preference of a method or tool then such question would be 38 irrelevant. So, asking such question means that currently there is 39 no consensus on the intrinsic preference of the available par-40 titioning schemes. As I stressed elsewhere,<sup>[80]</sup> at the extreme level, this means the lack of the scientific "objectivity" and "real-42 ism" that scientists are proud of and is usually used to distinguish 43 science from other human endeavors like philosophy, politics, 44 and religion where the intrinsic preference is always disputable. 45 Accordingly, sometimes it seems to me that the implementation 46 of an index or a partitioning scheme in a well-known or a user-47 friendly software had been the prime factor in its dominance in 48 competition with similar indices or schemes. In short term, such 49 factors are tolerable and probably even inevitable since in the 50 end science is also a human activity, but when such factors are dominant after decades, to me, it is a sign of a crisis... 52

### István Mayer

55 Yes, I think so. One needs results that help interpret the calcu-56 lated and/or experimental quantities. The observation that Mulliken's gross populations often fail to provide chemically reasonable results, motivated the quest for alternative schemes of population analysis. (This was the case although Mulliken's gross population is that definition which is consistent with the internal mathematical structure of the LCAO formalism.<sup>[105]</sup>) When EDA methods are concerned, I have experienced a pressure from chemists to produce a scheme in which the diatomic bonding energies are on the "chemical scale", that is, not equal but comparable with the accepted bonding energies. (Also see my answer to question 6.)

### Martin Rahm

I hope we all can agree that EDAs should be subject to scientific Darwinism. Cross-comparison and "benchmarking" of EDA methods, even if it difficult to do, is one way forward that should allow for more "evolutionary pressure". I stress this point further in my answers to questions six and seven. However, rather than risking extinction, I suspect that EDA methods subjected to comparative studies will thrive. Comparisons will bring out complementarities in different approaches and ultimately allow us to get a better overall grasp of electronic structure and chemical bonding. A nice example highlighting the benefits of comparative studies of EDA methodology is that of Fugel et al.<sup>[106]</sup>

### Frank Weinhold

Yes, of course. By the evidence of their usage, adoption, and cited-applications (or not) in the broader chemical community, EDA approaches should be subject to "selection" according to their impact on how chemistry is actually practiced and taught.

### Roberto A. Boto

90 In my opinion, a partition scheme should not be influenced by 91 anything but its theoretical framework. However, in theoretical 92 chemistry, there has always been a balance between quality 93 and computational resources. It is often found that the more 94 elaborate is the theory, more demanding is the computation of 95 terms derived from it, and approximative routes should be 96 taken. Energy partitions are not an exception, and the pressure 97 of the community toward more complex, often larger, chemical 98 systems could bias the selection of EDAs.

### Ángel Martín Pendás

Like anything in Science, partition schemes are subjected to Darwinism. Whether Darwinism in Science chooses the best solution or only the fanciest one is another problem, since, as a human activity, Science does not escape fashion. Since, unfortunately, many EDAs are intimately associated with particular electronic structure paradigms (e.g., molecular orbital or valence bond descriptions), the waves in the former are clearly conditioned by those in the latter.

### David L. Cooper

Experience suggests that the partitioning schemes that are 112 likely to be the most widely used in the scientific literature will 113 not necessarily be the "best" ones, as determined by cross-114



comparison and "benchmarking", nor indeed those that are 1 best suited to impact the practice and teaching of Chemistry by 2 3 nontheoreticians. Although "fashion" can indeed be an impor-4 tant factor, ultimately it is the availability of particular methods 5 in certain "standard packages" that could end up being the deciding factor. This could, of course, be ameliorated to some 6 7 extent by the availability of free and easy-to-use facilities that implement other schemes. 8 9

#### Carlo Gatti 10

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Yes, they probably do, but are we sure that the more fitted to survive are those schemes with largest scientific rigor? The sociological pressure of the community may largely bias the 14 selection process. Factors like ease of use, simplicity of analysis 15 (few composing energetic terms rather than a potential pleth-16 ora of progressively finer dissections like in the real space EDAs), adoption by large and numerically dominant communities, may clearly bias the game, offsetting the purely scientific selection process. Other counterweighting and disturbing factors might be the implementation of given schemes rather than others in popular quantum-mechanical codes.

#### 23 Julien Pilmé

24 Yes, I agree with that. In my opinion, the "natural" selection pro-25 cess, which should be conducted according to scientific 26 requirements, is hardly efficient owing to the lack of the straight forward link with the experimental data. Maybe, this 28 process becomes more "fashion-driven" and more sensitive to a 29 sociological pressure. Yes, it seems also that the selection pro-30 cess is flawed by the ready availability (or not) of EDA methods in the quantum chemistry software.

#### 33 **Paul Popelier** 34

The metaphor of natural selection is useful to think about 35 where the zoo of EDAs is at, and where it should head for. The 36 answer to question 4 is yes because natural selection is already 37 happening. For example, the recent review by Skylaris et al.<sup>[2]</sup> 38 compares and discusses six test sets. The authors conclude that 39 "Overall the ALMO EDA scheme is shown to provide the most 40 chemically sensible EDA results for our systems relevant to drug 41 optimization." Unfortunately, this comparative study was con-42 fined to nontopological EDAs. Building on the Darwinistic meta-43 phor, this means that topological EDAs happily live on some 44 island or disconnected continent that has had no contact yet 45 with nontopological EDAs (although Ángel and co-workers have 46 published such a comparative study.[107] 47

48 We should keep in mind how natural selection actually works. 49 Ultimately, it is the interaction between the creature (i.e., a given EDA) and its environment (the other EDAs and the community 50 of users) that determines if the creature survives or not. I think 51 52 that as a community we should be a more demanding environ-53 ment, even if that means that an EDA becomes extinct. Experi-54 mentalists can only take the work of theoreticians seriously if it 55 provides future-proof insight or correct predictions. There is no 56 harm in two different EDAs coming to the same conclusion; what is a problem is if they contradict each other. Although I do not 57

have precise references in mind my feeling is that the commu-58 nity allows contradiction to exist, and even worse, allow them to 59 thrive under the false banner of diversity and richness. This is 60 dangerous for Science. I am still dreaming of a consistent world 61 of interpretations and predictions, one where  $\mathbf{F} = ma$  is the only 62 equation that puts a person on the moon rather than F = m/a or 63  $F = ma^2$ . However, equivalent theories (e.g., Matrix Mechanics 64 and Wave Mechanics, or Valence Bond and Molecular Orbital, or 65 String Theory and Quantum Gravity) can coexist as long as they 66 make the same predictions. 67

### Jerzy Cioslowski

Like almost everything in science, the energy partitioning schemes are subject to surges and ebbs in popularity, and even extinction. However, I am reluctant to use the term "Darwinism" in this context as the concept of the "survival of the fittest" (if one defines the fittest as the most rigorous and scientifically justified) obviously does not apply here. I am afraid that the popularity of various definitions of chemical concepts is mostly driven by the prejudices (politely called "chemical intuition") of those regarded as contemporary authorities in (not necessarily theoretical) chemistry. This situation would correspond to the evolution of species being due to supernatural powers (gods, aliens, or whomever) eliminating living organisms according to their preferences, which is not exactly what Darwin had on his mind.

A simple prescription to avoid this undesirable status quo would be axiomatization of chemical concepts. Spelling out a set of axioms that all the concepts have to satisfy would greatly reduce the room for personal preferences and thus diminish the importance of the "human factor in interpretation of electronic wavefunctions."

### Gernot Frenking

92 Darwinism means the survival of the fittest. In that sense, I do 93 think that those concepts will eventually be adopted by the 94 community, which are considered as the most useful ones. 95 However, I see an ongoing preference for simple models that 96 are intuitively easy to accept even when the underlying 97 assumptions are incorrect, instead of a more complicated 98 model, which agrees with a thorough quantum chemical analy-99 sis. There seems to be a human tendency even in science to 100 prefer a known disease to unknown health because one is 101 afraid of the work that comes along with the cure. The great 102 acceptance of the NBO method is at least partly due to the 103 smoothing tranquilizer effect for addicts of the Lewis model 104 who do not want to be bothered by the complexity of the elec-105 tronic structure. The sociological pressure could lead to a situa-106 tion where the well-known illness is preferred over the 107 unknown health. With other words, the frequent use of NBO 108 results may lead to the acceptance of the method even when 109 the shortcomings are well known. 110

### Julia Contreras

Absolutely. I see that there are two main trends: mathematical 113 and physical Darwinism and I totally advocate for physical 114

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Darwinism. Theories can be very elegant, but what I really expect from an energetic partition (or as well any other theory), is to describe the physics of the system. To provide a descriptive and predictive framework. What should not be interpreted as social pressure (and we have seen much of these lobbies in this community): MY method is BETTER than the others (and I reject papers otherwise).

### 9 Henry Chermette

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Darwinism..., yes or no: selection of the survival scheme(s) can be biased by factors like ease of use, availability in (the widely used) software, and simplicity of analysis. And a scheme can be "rediscovered" 20 or 30 later after its (first) description in a (specialized, not popular) journal.

### Émilie-Laure Zins

17 This question suggests a comparison between the theory of 18 evolution and the description of the chemical bond. This com-19 parison seems to me to be particularly relevant and deserves a 20 short comment. Experimental chemists, during their observa-21 tions or interpretations, have proposed and developed many 22 concepts, which can be compared (metaphorically) to different 23 living species: they can appear, persist, evolve, or disappear. It 24 can be hypothesized that some chemical concepts could be 25 merged, in particular, through the use and development of 26 adapted partition schemes. It seems to me that a "massive 27 extinction" in the zoo of chemical concepts, caused by a "uni-28 versal" partition scheme, or by a limited number of partition 29 schemes based on the fundamental theorems of quantum 30 physics, would be beneficial to chemistry. 31

### Laurent Joubert and Vincent Tognetti

34 We think that different communities may have preferences 35 guided by some historical reasons or, let us say, some traditions 36 in interpreting the same results. Assume that we are interested 37 in the energy difference between two conformations (that can 38 be measured experimentally in some cases). The virial theorem 39 actually brings us two explanations: (1) it is due to the electron kinetic energy, (2) it is due to the potential energy. No one is 40 preferable, being both correct, since, quoting Godard, "The 41 42 essential difference between classical mechanics and quantum 43 mechanics is that in classical mechanics the kinetic energy and 44 the potential energy are independent (one is determined by 45 momentum, the other by position), whereas in quantum mechanics T and V are simultaneously determined by the 46 47 wavefunction." However, an experimental chemist is much 48 more accustomed to think of potential energy (linked to inter-49 actions between atoms) than of kinetic energy, and we are thus 50 facing different habits in various chemical communities. T fea-51 tures the advantage of being derived from a one-body opera-52 tor, while V involves a two-body operator. When decomposed 53 into N atoms, it thus generates about N2 values, a number that 54 may make the analysis inextricable. Noteworthy, Popelier 55 recently proposed a powerful relative energy gradient approach to select the most relevant contributions.<sup>[100]</sup> Certainly, such 56 57 analyses will clearly benefit from the big data and artificial intelligence fields. Maybe, they will thus lead to favor some par-58 59 titions to the detriment of others. However, from our point of view, there is nowadays rather coexistence of various theories, 60 within different frameworks (real-space analysis, wavefunction 61 analysis). The fact that there is such a debate indicates that 62 there is currently no natural selection process at work... One 63 can also say that natural selection actually requires a very long 64 evolution time, much more than the age of quantum 65 chemistry... 66

### Paul W. Ayers

Yes, but in a strange way. Science is both "red in tooth and claw" in the sense that the most vociferous, forceful, ruthless, and prominent researchers (and referees) have an advantage. It is also true that people who write/convey their ideas most clearly (and forcefully) have an advantage. Yet (fortunately) vehemence and salesmanship is not everything (though I do feel we often underestimate its importance). Most scientists possess an idealism and thus the drive toward utility and simplicity is strong. I think many of us seek decompositions/partitionings that "can fit on a T-shirt" (Occam's razor). And all of us seek definitions that are helpful to experimentalists. That is, while I often call my work on concepts "chemical philosophy," just like traditional epistemology, the goal is to find precepts/concepts that have broad and practical utility for everyone.

### Farnaz Heidar-Zadeh

There is no doubt that partitioning schemes (and other concepts) evolve over time and the fittest survive, that is, the ones which are well-defined and make better predictions. However, this natural selection is commonly disturbed by our biases and prejudices as humans, which makes the scientific discourse not very scientific. (This was a very disappointing realization for me as a young scientist!)

### Juan Andrés

As Ayala wrote<sup>[108]</sup> "There is a contradiction between Darwin's 95 methodology and how he described it for public consumption." 96 Darwin claimed that he proceeded "on true Baconian [induc-97 tive] principles and without any theory collected facts on a 98 wholesale scale." He also wrote, "How odd it is that anyone 99 should not see that all observation must be for or against some 100 view if it is to be of any service!" The scientific method includes 101 two episodes. The first consists of formulating hypotheses; the 102 second consists of experimentally testing them. What differenti-103 ates science from other knowledge is the second episode: sub-104 jecting hypotheses to empirical testing by observing whether 105 or not predictions derived from a hypothesis are the case in rel-106 evant observations and experiments. A hypothesis is scientific 107 only if it is consistent with some but not other possible states 108 of affairs not yet observed, so that it is subject to the possibility 109 of falsification by reference to experience" But, the more impor-110 tant yet is that Darwin discovered natural selection, the process 111 that accounts for the adaptations of organisms and their com-112 plexity and diversification, in a wide range of research fields, 113 including biology, geology, and also chemistry and physics. In 114



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1 our case, it is necessary to remember that theories such Lewis, Valence Shell Electron Pair Repulsion (VSEPR), molecular orbital 2 3 (MO), its extension to natural bond orbital (NBO), frontier 4 molecular orbital (FMO) of Fukui, valence bond (VB), or even 5 conceptual density functional (CDF). These theories have their advantages and shortcomings, work in some cases but not in 6 7 another, and are still used in the current bibliography. Therefore, it is expected that in the partition schemes occurs the 8 9 same and that many of these are still used. The important and desirable thing is to know if they are used correctly and as far as you can get with the results obtained. A large dose of self-11 12 criticism is necessary to overcome the sociological pressure.

### 14 Yirong Mo

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This may be true. Most computational chemistry practitioners are users of the software and tend to follow the majority and use whatever put into the software designed by others, as in this way, works can be relatively easy to be accepted by the community. In this process, prominent figures may lead the majority to particular partition schemes.

### Eduard Matito

23 Yes, energy partitions and, in general, chemical bonding tools 24 are subject to extinction and, inevitably (and regrettably), they 25 depend on its "popularity." As it has been pointed out, the popu-26 larity depends on its availability, its usefulness, if they are easy to 27 compute, the cost of its calculation, scientific "marketing" and, to 28 some extent, scientific rigor. As developers and experts of chemi-29 cal bonding tools, we should be well aware of this and act 30 accordingly. In the field of aromaticity, NICS became the most 31 popular measure because it is available on a large package 32 (Gaussian) and it could be easily computed with a single key-33 word. NBO is known to computational and experimental chem-34 ists alike because there has been a large effort to advertise it 35 (books and online tutorials, reviews, workshops, and hands-on 36 sessions). I believe is our responsibility to work to facilitate the 37 use of the most useful and rigorous partitions, making them 38 available and as user-friendly as possible. Otherwise, they 39 became complicated and obscure objects that only a handful of 40 people (the so-called experts) can use and understand. Last but 41 not least, we should encourage benchmarks and comparisons 42 that put forward the boundaries and limitations of the energy 43 partitions. For instance, we identified that some atomic partitions 44 could not be employed to compute aromaticity indices<sup>[109]</sup> and 45 Ponec, Cooper, and others found that only with some atomic 46 partitions the bond index attained a maximum value close to the 47 avoided crossing of the two lowest-lying states of LiH.[110-112] 48

### 49 50 W. H. Eugen Schwarz

Yes. First, some sociological pressure may be induced by charismatic colleagues and their followers influencing the fashions of a time. We all know it, concerning "overlapping VB concepts" vs "orthogonal MO concepts," concerning aromaticity as a singledimensional concept best represented by the NICS parameter, concerning QTAIM based molecular partition schemes, or that molecules only consist of atomic one-center parts and diatomic two-center bonding parts, and so on. Second, the viewpoints in 58 common teaching are partly determined by historical traditions 59 and ideologies and by well-written and well-priced textbooks, 60 influencing the convictions of the majority in the scientific com-61 munity. Third, the availability of technical options: an analysis 62 scheme will best survive if it can be applied with little invest-63 ment of money or knowledge and with user-friendly tools; or if 64 it can be easily applied to available data sets. For instance, one 65 can better derive density distributions than wave-functions 66 from X-ray diffraction patterns, so X-ray diffraction research sup-67 ports analyses of densities in three-dimensional space. 68

### Alston Misquitta and Krzysztof Szalewicz

71 A necessary condition for a partition scheme to be of value is 72 that the sum of components should give an accurate interac-73 tion energy at all physically important dimer configurations, so 74 that a potential energy surface (PES) based on this scheme can 75 be used to predict observables in agreement with experiment. 76 Thus, partitions based on CCSD(T) satisfy this condition, but 77 based on DFT will not unless particular care is taken to partly 78 control the self-interaction error (by using a hybrid or range-79 separated hybrid functional) and an adequate dispersion cor-80 rection is included. As discussed above, SAPT satisfies this con-81 dition very well. The second condition is that components are 82 not excessively large in magnitude so that there are no large 83 cancellations in adding them to form the total interaction 84 energy. The third condition is that if components are meant to 85 represent electrostatic, induction, dispersion, and exchange 86 energies, they should agree to within a few percent with SAPT. 87 All methods satisfying these conditions are basically equivalent 88 from the point of view of getting insights into physical mecha-89 nisms of intermolecular interactions. 90

This set of conditions can be used to evaluate various EDAs 91 for the component called charge-transfer energy. While SAPT 92 includes all charge-transfer effects, it does not compute a sepa-93 rate charge-transfer energy, but rather this component is 94 included in the induction energy. As the other part of this 95 energy is the polarization energy, which is negative at the two-96 body level, the charge-transfer energy cannot be smaller, that 97 is, more negative, than the induction energy. For example, for 98 the water dimer at the minimum configuration, the sum of the 99 second-order induction, exchange-induction and  $\delta_{int}^{HF}$  terms is 100 -2.24 kcal/mol.<sup>[113,114]</sup> This can be compared to the total SAPT 101 interaction energy of -4.65 kcal/mol and to the CCSD(T) interac-102 tion energy of -4.95 kcal/mol. Thus, SAPT gives a lower bound 103 for the charge-transfer term of -2.24 kcal/mol. Taking into 104 account the differences between SAPT and CCSD(T), one may 105 assign an uncertainty of  $\pm$ 0.3 kcal/mol to this value. However, 106 the noncharge-transfer part of induction energy, that is, the 107 polarization energy, is not negligible and it is by definition neg-108 ative. This energy can be estimated from the classical polariza-109 tion model and if the procedure developed in Ref. [115] is 110 applied to the water dimer, one gets -0.8 kcal/mol in the first 111 iteration, corresponding to the second-order in V, and an addi-112 tional -0.2 kcal/mol from the further iterations. Thus, the total 113 polarization energy amounts to -1.0 kcal/mol, giving an 114



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estimate for the infinite-order charge-transfer energy of  $-1.2\pm0.3$  kcal/mol. Values much larger in magnitude, often 2 3 found in literature (see a discussion in Refs. [116,117]), cannot 4 be considered to represent true charge-transfer energies. Some 5 EDA schemes are consistent with our estimate, for example, the ALMO method based on CCSD<sup>[118]</sup> gives -0.8 kcal/mol. 6 The method of estimating charge-transfer terms based on the 7 regularized-SAPT(DFT) approach, developed by one of us,<sup>[119]</sup> 8 9 gives a smaller in magnitude value of -0.4 kcal/mol (however, this estimate includes only the second-order terms and would 10 increase in magnitude if higher-order corrections were accounted for).

### **Ouestion 5: To What Extent Does/Can/Should** Investigated Systems Influence the Choice of a Particular Partition Scheme?

### Ramon Carbó-Dorca

It seems difficult to foresee how partition schemes clarify anything, being somehow (or quite) arbitrary. Perhaps they could add more obscurity to the certainly not very clear usual chemical concepts.

### Shant Shahbazian

In principle, a mathematically rigorous partitioning scheme must be applied to any molecular system regardless of the size, type of atoms, or complexity of its electronic structure. However, in practice, the "interpretational" problems emerging from applying a scheme to certain systems may have a strong influence on favoring or dismissing the scheme. As an example, the popular "misinterpretation" of the (3, -1) critical points (CPs) emerging from the topological analysis of the molecular electron densities as indicator of bonds has been a source of confusion.[120,121] There are certain systems that if one insists that (3, -1) CPs are "bond" CPs, that is, BCPs, then inevitably there would be a clash between the quantum theory of atoms in molecules (OTAIM) analysis and most of the other partitioning schemes on the presence/absence of bonds between certain atoms. In such problematic cases, people usually try to avoid the use of the QTAIM analysis, though a proper reinterpretation may fix the problem.<sup>[96]</sup> However, such problems are not confined to just misinterpretations and there are cases where a partitioning scheme does not support (or is at odds with) an established viewpoint regarding a system and people try to avoid the scheme. Such "expectational bias" regarding what "must" emerge for a system may unconsciously (or even consciously) affect the preference/dismissal of a partitioning scheme. For me, this is an unpleasant element of "subjectively"....

### Martin Rahm

I suspect it often does not. This is in large part because most EDA methods require quite some expertise to execute and interpret. There are also a lot of methods out there, and it is not always easy to evaluate pros and cons in an objective manner. Publishing work addressing chemical validation and crossvalidation of EDA methods, discussed in guestions six and seven, should help in this respect.

### Frank Weinhold

In principle, the EDA method of choice should be independent of the problem. To the extent that such influence exists (i.e., for possible subjective choice of EDA method or "reference fragments"), it seems to represent a particularly dangerous aspect of the partitioning approach.

### Roberto A. Boto

A well-defined partition scheme should be valid for any chemical system. Energy partitions are based on chemical concepts such as covalency, ionicity, and polarizability. These concepts should be well-defined regardless of the nature of the system.

Otherwise, we may create a chaotic scenario with a panoply of partitions, one for each chemical system.

Ángel Martín Pendás

Ideally, it should not. However, it is usually the case that, as it happens with density functionals, basis sets, or many other of our computational knobs, ideas propagate that advice the use of this or that method to deal with these or those problems. In many cases, the partition scheme is chosen a posteriori, a practice that should not be allowed.

### Carlo Gatti

Generally speaking, if someone believes that his or her favorite 89 partitioning scheme is suited for some classes of compounds 90 and (much) less for others, he/she should probably make a step 91 92 back and ask himself or herself what prevent his or her favorite method to be general enough to be applied equally well to any 93 chemical system. This is an important exercise that may lead to 94 an improvement of the scheme or to abandon it in favor of a 95 more general one. I also believe that more than the investi-96 gated system, it is the chemical guestion to be addressed that 97 98 may influence the choice of a particular partition scheme.

### **Paul Popelier**

I agree with the general consensus building up here, which is 102 that the nature of a system should not influence the choice of 103 the partition scheme used, in the end. Unfortunately, this is not 104 the case at the moment. For example, anionic systems or sys-105 tems with large rings need diffuse Gaussian primitives in order 106 for their wave functions to be properly described. Partitioning 107 schemes that depend on the location of the center of these 108 primitives suffer from the use of diffuse functions (because the 109 mapping between center and ownership starts breaking down). 110 Hence such partitioning schemes cannot be used in that case 111 or they have to be modified. Anthony Stone did the latter by 112 injecting some real-space partitioning character into his original 113 DMA scheme.<sup>[122]</sup> 114



### Pedro Salvador

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Of course, I also agree that in principle any reasonable partitioning scheme should be applicable to any chemical system at hand. However, I also have the impression that EDAs and topological EDAs (borrowing Paul's terminology) are somehow designed to answer different type of questions, so the nature of the system under scrutiny could drive one to use one or another scheme. Unfortunately, there are not too many works where both topological and nontopological EDAs are applied to the same problem aiming at answering the same questions (I do remember a nice poster at the ESB2 Oviedo this year showing striking similarities of both approaches).

### Jerzy Cioslowski

16 As illustrated by the recent proliferation of density functionals, 17 there is great temptation (especially among those not well-18 versed in quantum chemistry) to select the theoretical 19 approach on the basis of the expected answer. It is quite disconcerting to observe the ongoing harkening back to the times 20 21 of semiempirical approaches when there was at least one 22 method for each set of electronic properties (CNDO/S for excita-23 tion energies, ZINDO for molecules with transition elements, 24 MNDO and its endless modifications for geometries and heats 25 of formation, etc...). Back then, this plethora of approaches was justified by the very limited power of computational hardware 26 27 that dictated the use of various approximations. Since this is 28 not an excuse nowadays, whenever carrying out computations 29 of electronic wavefunctions or their interpretations, one should 30 strive to limit the variety of the methods employed. Otherwise, there will always be pressure to legitimize one's interpretative 31 32 prejudices and/or experimental results with a suitably chosen 33 "theoretical justification".

#### 35 **Gernot Frenking**

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36 The investigated systems and associated questions rightfully 37 influence the choice of a partitioning scheme. Different systems 38 and questions may request different methods. For example, the 39 chemical bond in LiF may be analyzed in terms of interactions 40 between the ions Li<sup>+</sup> and F<sup>-</sup> or the neutral atoms Li and F. The 41 former choice of the fragments is better suited to investigate 42 the final bond, while the choice of Li and F as fragments 43 encompasses all changes in the electronic structure along the 44 bond formation/dissociation. It is strength and not a weakness 45 of partitioning schemes to be able to choose different frag-46 ments as interacting moieties. However, it is often only the 47 combination of several methods (charge and energy decompo-48 sition schemes) that provide a faithful account of the electronic 49 structure in terms of a model. 50

### Laurent Joubert and Vincent Tognetti

53 An important related question is: can we compare EDA results 54 for systems that strongly differ? In question 3, we stated that 55 there are two categories of EDA and we discussed there the 56 first one. The second EDA category gathers those carried out 57 after the initial quantum chemistry calculation. They aim at dividing energies into physicochemical components (charge 58 59 transfer, polarization, and induction) whose definitions are in general not unique, and/or into subsystems (atoms, substitu-60 ents...) for which various partitions also exist. All these energy 61 decompositions can be based either on the wavefunction 62 and/or the electron density, but they are performed indepen-63 dently of how these functions were obtained. For such reasons, 64 they can reproduce or not the molecular energy obtained at 65 the previous step. In such a case, two corrections are often 66 implemented: (1) defining an ad hoc new contribution to fill 67 the gap, (2) scaling the energy sum to the targeted energy. This 68 strategy is very often used with the virial theorem. Indeed, for 69 the exact wavefunction, the molecular energy is equal to minus 70 the electron kinetic energy, or, equivalently, to half the poten-71 tial energy. Unfortunately, the scaling parameter that is used in 72 practice can be significantly different from one system to 73 another. It can lead to questionable conclusions when compar-74 ing molecules of too much different type.<sup>[4]</sup> Coming back to 75 question 5, it thus appears that some EDAs should not be used 76 to investigate a molecular dataset composed of several differ-77 78 ent classes. From this point of view, the investigate systems will influence the EDA choice by precluding the use of some of 79 them.[123] 80

### **Miquel Solà**

83 I agree that ideally, the choice of the EDA method employed 84 should not be dependent on the system studied. What is criti-85 cal, however, is the definition of the fragments to analyze a 86 given bonding situation. For instance, the answer to the ques-87 tion of how much covalent is the LiF bond may change from 88 14% to 91% depending on whether the fragments considered 89 in the EDA are Li<sup>+</sup> and F<sup>-</sup> ions or Li. and F. radicals, respec-90 tively.<sup>[124]</sup> Moreover, in a series of similar bimolecular chemical 91 reactions, the use of the activation strain model<sup>[125,126]</sup> provides 92 deep insight into the origin of the energy barriers associated to 93 these chemical reactions by taking the reactants as the frag-94 ments of choice. However, if one wants to analyze the whole 95 reaction profile from reactants to products, then after the tran-96 sition state, in the product region, the use of reactants as frag-97 ments is generally not a good choice. The whole reaction 98 profile is probably better analyzed considering the different 99 atoms as fragments. Moreover, if reactions are unimolecular, in 100 most cases, it could be hard to define two fragments to per-101 form an EDA and probably considering atoms as fragments 102 may be the smartest choice. Finally, the analysis of isomeriza-103 tion energies can be performed using different fragments. In 104 many cases, one can use the same fragments to build the two 105 isomers just placing them with different orientation (we called this procedure the turn-upside-down approach).<sup>[127,128]</sup> With 107 this procedure, one usually gets a deep understanding of the 108 physical origin of the isomerization energy. 109

### Paul W. Ayers

I wish there were a universally applicable and useful par-112 titioning scheme, but I'm not convinced any such scheme exists 113 at present. For example, some methods are strongly dependent 114

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on a specific electronic structure ansatz, and would not be applicable, for example, to a diffusion guantum Monte Carlo calculation, or to a calculation that use nonatom-centered basis sets (e.g., plane waves). Others could not be applied to a lattice (e.g., a Hubbard or Pariser-Parr-Pople model for an aromatic system), or to a periodic solid. Even among the few methods that are universal in scope (and there are very few such methods), their utility is unlikely to be universal.

#### 10 Farnaz Heidar-Zadeh

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In theory, a partitioning scheme should be applicable to any system, because the same physical laws apply to them all. Any deviation from universal applicability is a warning sign that should give one-second thoughts about using the scheme. If a scheme is suitable for only a specific class of systems, it is very unlikely to be physically sound.

### Juan Andrés

It is not appropriate or desirable to investigate a system in order to choose a particular partition scheme. We must remember that history tells us that opening this path can cause great confusion with the proliferation of different methods. One has to remember the extensive number of semiempirical methods. basis sets, functional hybrids, and so on, as also have pointed by Profs. Martin-Pendás, Cioslowski, and Ayers.

### Yirong Mo

May be not much. See question 3.

#### **Eduard Matito** 32

33 I believe it depends on the motivation. Making a choice of the partition based on the premise that it provides the answer you are looking for is obviously scientific misconduct. As Jerzy 36 points out, a scenario in which a large collection of energy partitions is available, each being adequate for a particular problem is highly undesirable. Ideally, any method should be universally valid and provide a correct and complete description of the system. However, in practice, they are not. If validation tests (see questions 6 and 7) offer us some hints of flaws and boundaries of current energy partitions, I find adequate to 43 use these results to select (or discard) an energy partition 44 scheme. For instance, a method having a slow convergence with the basis set size should probably be discarded in situations where we cannot afford a sufficiently large basis set.

#### 48 **Eloy Ramos-Cordoba** 49

50 Ideally, the molecular system under study or the electronic structure method employed should not influence the choice of 51 52 a particular EDA scheme. In practice, the system dependency 53 seems to be unavoidable since there are EDAs which are only 54 defined for some electronic structure methods, and some of 55 them are restricted to be used in conjunction with atomic-56 centered basis sets. In this sense, topological energy decompo-57 sitions seem to be more general since they can always be

employed provided the 1- and 2-particle density matrices are available.

### W. H. Eugen Schwarz

They must. The field of chemical substances with static and reactive properties is unboundedly rich. Useful and fruitful partition schemes should be intuitively understandable, that is, simpler than reality. A scheme that is applicable to everything will be too complicated. It is better to have different schemes say, for primarily and for weakly bonded systems, or for weakly and for heavily electron-correlated systems.

### Alston Misquitta and Krzysztof Szalewicz

SAPT partition works for all closed-shell dimers and so should all other schemes.

### Question 6: Do We Need more Focused Chemical Validation of EDA Methodology and **Descriptors/Terms in General?**

### Ramon Carbó-Dorca

Might be what it is needed is a reflection on the chemical practical use of EDA. Perhaps the problem lies on the fact that there appears to be a large variety of procedures (see the recent review by M. J. S. Phipps, T. Fox, C. S. Tautermann, and C.-K. Skylaris<sup>[2]</sup>). Along the past 3 years since this publication, possibly, even more techniques have been defined.

### Martin Rahm

Yes, we do! And this one I feel guite strongly for. EDA methods are most often used as descriptive tools, that is, they analyze a given electronic structure and provide a picture of the bonding situation. There are many elegant EDA definitions that can provide detailed information about electronic structure in this manner. Whereas this can be useful, the ultimate goal of any electronics structure analysis should be predictive utility. "Chemical validation" can, of course, come in many forms, but it offers the safest route to demonstrating predictive utility. One approach toward "chemical validation" is to attempt thorough answers to the following three questions:

- 1. What chemically relevant experimental observable does the EDA-term [X] correlate with?
- 2. When does the correlation break down?
- 3. Why does the correlation exist [here] and not [there]?

### Shant Shahbazian

I find the question to some extent vague. For the validation 107 process, we must have a reference set of data that the EDA 108 method under study may reproduce them properly. In the case 109 of validation of ab initio methods, these are thermodynamics or 110 spectroscopic experimental data that no one disputes their 111 authenticity as an objective reference set. What is the reference 112 set of data in the case of an EDA? Can we come to a "consen-113 sus" what is the "standard" reference set for such chemical 114

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validation? I am currently pessimistic about the whole idea (please also check my answer to question 9).

### lstván Mayer

Ideally, the energy decomposition produces diatomic energy components representing the interatomic bonding (or repulsion) at the actual configuration of the molecule, and one center ones describing the promotion of the atoms when the molecule is formed. However, in several EDA schemes (including semiempirical, e.g., MNDO ones) one encounters the difficulty, that delocalizations responsible for bond formation also give rise to ionic wave function components (in VB terminology) that increase the intra-atomic electron repulsion energies, thus also the apparent atomic promotion energies. As compensation, one obtains very negative diatomic energy components, that are not on the "chemical scale." No doubt, such a straightforward energy decomposition may be quite useful for comparing different bonds, etc., or even making some predictions. However, chemists are inclined "not to buy" these large (in absolute values) numbers. This reservation of colleagues chemists served for me as a strong stimulus to introduce a corrected scheme.<sup>[129]</sup> The ionic terms are due to the bond formation, so their interelectronic energy was distributed between the different bonds in accordance with partial bond orders formed by different "effective atomic orbitals."

### Frank Weinhold

Yes (see question 3).

### Ángel Martín Pendás

I tend to agree with the need of validation to properly screen the different methods available, but I also acknowledge the difficulty in finding a suitable set of quantities that might be taken as a reference validation set. To focus just a bit, let us simply take the Pauling repulsion term of many EDAs. What chemical relevant observable (In Martin's words) does it correlate with? In the absence of a consensus on what types of energetic terms should be allowed/not-allowed in a partitioning scheme, validation is desirable but difficult.

### Paul Popelier

44 Yes, I believe so. I come back to this question in question 7 because the latter question overlaps with question 6, in which 45 the word "focused" pops out. I had like to interpret this word in 46 47 a sociological sense. The community of interpretative theoreti-48 cal chemistry, especially that of Quantum Chemical Topology 49 (which is younger and somewhat lags behind), should scour 50 more for "hot case studies" and work on them. These regularly appear in the popular scientific magazines (e.g., Chemistry 51 52 World of the Royal Society of Chemistry). We can then to test 53 (and showcase) partitioning methods. In the medium and lon-54 ger term we can find out what we can do for experimentalists 55 (e.g., material scientists and synthetic chemists). After all, there 56 is a reason why the largest scientific funding body in Britain, called EPSRC, launched as one of its main research themes the 57

Grand Challenge of "Directed Assembly" (short title). The associ-58 ated vision for the next 50 years is, in EPSRC's own words, to be 59 able to control the assembly of matter with sufficient certainty 60 and precision to allow preparation of materials and molecular 61 assemblies with far more sophisticated and tuneable properties 62 and functions. To me, our goal should be to produce a minimal, 63 trustworthy and well-thought through partitioning scheme that 64 delivers trustworthy and consistent insight. Partitioning 65 schemes should not be "afterthoughts" to what experimental-66 ists already know, nor should they confuse experimentalists 67 with contradictions. Instead, they should guide and boldly but 68 robustly confirm or correct the intuition of the experimentalist. 69

Jerzy Cioslowski

In my opinion, "chemical validation" should be limited to checking whether energy components (and other descriptors) computed for similar systems are themselves similar. This may also include the "chemical scale" argument of István Mayer, that is, that diatomic (bond) contributions should have values similar in order to those encountered experimentally (bond dissociation energies, etc...). Anything more than that amounts to falling back into the trap of "chemical intuition", which is what one presumably hoped to avoid from the start.

### **Gernot Frenking**

"Chemical validation" is an ill-defined fuzzy expression. I agree with Jerzy Cioslowski that chemical validation leads to the danger of using "chemical intuition" as measure for the validity of the EDA results, which is one step toward alchemy. A useful partitioning scheme should provide a self-consistent ordering scheme for the pandemonium of chemical facts. The physical interpretation of the energy terms will always be debatable.

### Julia Contreras

92 YES! In this direction, chemical interpretation has always been 93 too much influenced by pre-QM concepts, trying to reproduce 94 what was already there. However, these concepts were intro-95 duced to predict composition, reactivity. I think we should go 96 back to these roots. Just like in many other fields where 97 theoretical/computational answers are difficult and the field is 98 still at a strong development stage (e.g., solvation energies, 99 molecular solid structure), we could propose "games" to predict 100 the outcome of a given molecular change (not easy to calcu-101 late). Extremely naive, but double-blind tests are a wonderful 102 way of testing methods! Of course, this means being able to 103 predict the behavior or energy terms upon perturbations, a 104 point that has not been paid much attention..., and which 105 chemists overcame long ago. However, it would provide a 106 clear-cut (and fun) way of taking the next step in energy 107 decomposition. 108

### Paul W. Ayers

Hell yes. We should be careful about what we mean by "valida-111tion." There are a few molecules that might be proposed as112such canonical examples of a concept that any EDA/partitioning113that disagrees with them should at least be heavily scrutinized,114

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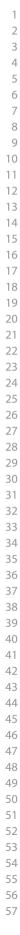
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and probably discarded outright. (For example, a method that did not predict that benzene has an "aromatic stabilization energy," however one might define that, has questionable utility.) There are more sequences of molecules for which a clear chemical trend may be asserted, and EDA can be validated against that.

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### Farnaz Heidar-Zadeh

Definitely, and this is long overdue! The systematic study of partitioning schemes in order to put them on equal footing is necessary and gives us a better understanding of their strengths and shortcomings. However, we first need to agree on this "validation protocol". As elaborated by many contributors, as a community, we need to make a comprehensive list of desirable axioms/features (distancing ourselves from intuitive measures) to assess and scrutinize various schemes and concepts. The five conditions suggested by G. Frenking are a great starting point.

### Juan Andrés

Yes, chemical validation of EDA methodology is mandatory. But this opens the door to start a path with many slopes to be able to solve and know to what extent a method and/or model can be used and gives good results in particular situations, which in some cases coincide with the experimental results. With this, the fundamental problem that must be managed is transformed and masked, that is to achieve a methodology based on quantum mechanics, which manages observables, and which is based on an adequate mathematical apparatus.

One can remember, for example, how the semi-empirical method MINDO/3 failed in the study of systems involving hydrogen bonds, or how, depending on the type of function used, one can calculate band gaps values in solids that agree with experimental values. This is a computational task.

On the other hand, we also need descriptors/terms in general, but many of these descriptors/terms derived from chemical concepts that can be considered fuzzy concepts, compared to unicorns or even noumenons. This is because there exists no physical observable associated with them. Therefore, is a very challenging task to reach this aim, we need to, first, clarify EDA methodology and descriptors/terms in order to obtain a chemical validation of both subjects.

### Yirong Mo

Absolutely.

### **Eduard Matito**

Indeed! This is probably a quite arduous task but is certainly needed in the field. Given the proliferation of energy partitions, "outsiders" from the chemical bonding community need guidance and, therefore, benchmarks (see question 7) and "chemical validation tests" are essential. However, as many people pointed out before, it is not straightforward to design a chemical validation test. In this sense, it is important putting the focus on the reliability of the tests (for which we need consensus within the community) rather than on having extensive tests that cover the many facets of energy partitions. Indeed, some 58 aspects of energy partitions cannot be easily tested (for 59 60 instance, the Pauli repulsion term mentioned by Ángel) and, 61 hence, the validation test is deemed to be incomplete. How-62 ever, this should not preclude the search for such validation 63 tests because they do not only help in classifying and assessing energy partitions, they also provide important hints to modify 64 65 and improve current energy partition schemes. Maybe a chal-66 lenge for our community in the next editions of ECCB confer-67 ences (and bond slams) could be suggesting chemical 68 validation tests that would be subsequently debated openly in 69 a forum like this until a consensus test set is obtained.

### W. H. Eugen Schwarz

Yes. Statistical data analyses (cluster analyses, factor analyses) can clarify what is behind a group of related concepts, and quantify the correspondence of different partition schemes.

### Alston Misquitta and Krzysztof Szalewicz

No, this is soft science with a weak connection to experiments. EDAs as such have no predictive power (the methods that are decomposed may have such power, but it is independent of an EDA applied). Such research should be reduced to a minimum.

### Question 7: Is there any Interest in **Developing Common Benchmarks and Test** Sets for Cross-Validation of Methods?

### Ramon Carbó-Dorca

The fact is that every EDA technique must be described, and probably it has been with a benchmark set of his own. However, the question is: to prove what? If the answer is: that it works! Then one needs to continue asking what is the sense of working: it means a given EDA technique explains better a molecular situation (perhaps some kind of interaction) than others? If so, why there are different abilities (as it seems there are) to describe some particular EDA nuances?

### **Martin Rahm**

I very much hope so. Reasons for validation against experiment 99 are outlined in the answer to the previous question. Bench-100 marks can help in this by including experimental data but could 101 additionally serve another important service to the community: 102 facilitating for more straightforward comparison of EDA 103 methods. This is beneficial for several reasons. Benchmarks will 104 allow newcomers to the field to more easily get acquainted 105 with advantages and drawbacks with the different methods, 106 which is of relevance to question four. Benchmarks will also 107 help the community to come to better terms with issues raised 108 in all previous questions, 1-6, and question nine. For example, 109 by revealing which EDA-terms and descriptors that do or might 110 relate to the same chemical concepts. In other words, 111 which terms that show the same trends in relation to relevant 112 chemistry. Ultimately, the ability to cross-correlate different 113 approaches should help highlight complementarities between 114

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EDA methods and aid future development of them. One successful example of EDA-term comparison is work of Racioppi et al.<sup>[130]</sup>

### Shant Shahbazian

As I stressed in my answer to question 6, I find it extremely unlikely that a standard set of data (I mean a set of numbers) may be proposed that all scientists find them equally objective and reliable. Think about the concept of bond energy (or something similar to this concept) that probably most people would agree that a good EDA method must deliver as its output. How we may find the proper set of bond energies to start the cross-validation? If there is no such standard set then any cross-validation study will simply reveal the similarities and differences between the applied EDA methods, not the "objectivity" of any EDA method (please also check my answer to auestion 9).

### István Mayer

Yes, it could be of interest to have a selection of different molecules with fixed geometries and a few different basis sets, for 22 which the results of each method are tabulated. Results 23 obtained with different wave functions (HF, DFT, CAS-SCF, CCA, 24 etc.) could be included as well. For the Hilbert space analysis, basis sets of sufficiently atomic character (as e.g., STO-NG, 26 6-31G\*\*, or cc-pVTZ) should be considered and no diffuse functions (augmented basis sets) should be admitted. 28

#### 29 Frank Weinhold 30

31 Self-correlation among closely related EDA variants is of little 32 value. Tests with experimental data (such as those suggested in 33 the reply to question 3) could give a more effective reality 34 check to cull the ranks of proposed partitions. The development 35 of the field would benefit from some common benchmarks that 36 are well chosen to represent a diversity of phenomena and spe-37 cies (cf. guestion 9). Only then can meaningful differences in 38 methods be illuminated and discussed.

#### 40 Ángel Martín Pendás

41 An interesting initiative might be choosing a selection of mole-42 cules, basis sets and methods to construct an EDA 43 benchmarking data set. Although, in agreement with Shant, it 44 would be difficult to find a proper set of values for the chemical 45 concepts that would then be cross-validated, a simple cross-46 correlation among the different EDA energetic terms would 47 provide relevant data about their similarities and differences. 48

#### 49 Carlo Gatti 50

51 Since aims might be guite diverse from method to method (see 52 my answer to question 1), I envisage complementary insights, 53 more than cross-validation from the suggested procedure. 54 However, common benchmarks and test sets could be useful to 55 observe which concepts and conclusions survive the various 56 methods. If concepts and conclusions were found to vary significantly within a class of related EDAs schemes, then this would 57

be a serious indication that these schemes might be deceptive and seemingly unphysical.

### Paul Popelier

Yes, having common benchmarks and test sets would be nice. Developers of force fields, density functionals, and machine learning methods already work with guite a few test sets that offer their development communities clarity on progress made. Designing and using those sets is easy because there is always a crisp and clear measure of success, that is, "golden reference" such as CCSD(T)/CBS wave functions or experimental properties. The problem with test sets for energy partitioning schemes is the usual difficulty that ab initio calculations and experiment typically deliver whole-system information. Nevertheless, it appears that some kind of test set has already naturally emerged in the case of the bond critical point problem. In an attempt to settle the controversial relation of this critical point to chemical bonding papers often report on the same molecular systems. Closer to the subject of EDA comparison, the recent review by Skylaris et al.<sup>[2]</sup> compares and discusses six test sets containing ions, water, and biomolecules (with hydrogen bonding and  $\pi\pi$  stacking interactions).

### Pedro Salvador

82 Coming back to my answer to Q1, topological EDAs only differ 83 on the underlying atom-in-molecule definition used. Thus, 84 rather than merely energy-based tests sets, which in agreement 85 with Ángel and Shant are rather difficult to build, one could 86 make up a multidimensional test set aiming at finding the best 87 AIM definition, analogous to the aromaticity test set put for-88 ward by Feixas et al.<sup>[131]</sup> in order to grade the different aroma-89 ticity indicators. Some work along this line has already been 90 attempted. For instance, the harpoon effect expected in the dis-91 sociation of LiH cannot be recovered with Becke's or Hirshfeld's 92 AIM partitioning.<sup>[111]</sup> Iterative Hirshfeld was also unable to 93 reproduce the higher carbon-carbon electron delocalization in 94 para vs meta position in benzene.<sup>[109]</sup> Semiqualitative energy-95 based tests could be added to the mix. For instance, when 96 using Hirshfeld-type approaches in X-H bonds, the value of the 97 atomic weight function of H at the nucleus significantly differs 98 from 1, and consequently, that of the X atom is nonzero. Is the 99 diatomic electron-nuclear attraction contribution of X-H bonds 100 reasonable? 101

### Jerzy Cioslowski

The only reason for embarking upon cross-validation of differ-104 ent definitions of a given chemical concept (including energy 105 components/contributions) should be the detection of the 106 cases where the concept in question is (using physicist's lan-107 guage) not a scalar. For example, as it is well known, all the 108 known definitions of ionicity are highly correlated, which means 109 that essentially ionicity is specified by just one set of values. A 110 counterexample is provided by aromaticity that is (at least) a 111 two-component vector, that is, it encompasses two sets of 112 values that are linearly independent. Thus, if one insists upon 113 cross-validation of energy partitioning schemes, it should be 114

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carried out with a set comprising a large number of "unusual" molecules, the results being subject to the principal component analysis.

### Gernot Frenking

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It is a good idea to have a test set of species, which are then used to explore the performance of a method for different types of electronic structures. For molecules, this should include, for example, compounds with polar and nonpolar as well as localized and delocalized bonds and it should encompass transition metal complexes as well as main group compounds with "normal" valency and "hypervalent" compounds.

### **Miquel Solà**

16 Benchmarks to prove the reliability of the different energy 17 decomposition analysis (EDA) approaches are highly desirable. 18 While the dissociation energy is an observable, the components 19 of the dissociation energy obtained from an EDA are not 20 observables. To validate concepts or quantities that cannot be precisely defined mathematically from the underlying physics, 21 such as the components of the EDA, Ayers et al<sup>[87]</sup> proposed to 22 23 take an axiomatic approach, which consists on listing the chem-24 ical, mathematical, and computational properties that one 25 desires for a concept to possess. In our group, we followed this approach to prove the reliability of a series of descriptors used 26 27 to quantify aromaticity, a quantity that is not observable, either. 28 To this end, we designed benchmarks containing a series of tests.<sup>[131-133]</sup> The chosen tests fulfilled two requirements: first 29 and most important, they were based on the accumulated 30 chemical experience in such a way that one expects most 31 32 chemists agree about the expected aromaticity trend and, sec-33 ond, the size of the systems involved were relatively small to 34 facilitate a fast application. As an example, we considered dif-35 ferent deformations of benzene, such as the bond length alter-36 nation (BLA). Any good indicator of aromaticity should detect a reduction of aromaticity of the benzene ring when BLA 37 increases. Or, for instance, when going from benzene to pyri-38 39 dine (one heteroatom in the ring), pyrazine (two heteroatoms in the ring) and triazine (three heteroatoms in the ring), aroma-40 ticity should decrease. In the case of EDA, one may proceed 41 42 similarly. It is probably not a good idea to consider results for a particular molecule instead of analyzing particular trends in a 43 series of molecules. Let us consider for instance LiF. According 44 to IQA calculations,<sup>[96]</sup> covalency, defined as the percentage 45 between orbital interaction and the sum of electrostatic plus 46 47 orbital interactions, is 14 the other hand, for the same molecule, 48 a Morokuma-like EDA considering Li<sup>+</sup> and F<sup>-</sup> as fragments indi-49 cates that covalency represents an 8% of the total stabilizing 50 interactions.<sup>[124]</sup> It is not possible to know which of these two results is the correct one. To make things more complicated, if 51 52 fragments considered in the Morokuma-like EDA are F. and 53 Li. radicals, covalency of LiF increases to 91%. The reader could 54 ask whether the ionic or the radical fragments is the best option to discuss bonding in LiF. One may argue that radical 55 56 fragments should be preferred because, for the gas-phase LiF 57 molecule, the homolytic dissociation costs less energy than the

heterolytic one, the latter being favored only if one includes at 58 least five water molecules, that is, for the LiF(H<sub>2</sub>O)<sub>5</sub> species.<sup>[134]</sup> 59 However, in the equilibrium geometry, the electronic distribu-60 tion is closer to Li<sup>+</sup> and F<sup>-</sup> ions than to F. and Li. radicals, so 61 maybe results employing ionic fragments are more realistic. 62 Anyway, using one or the other fragmentation scheme is a mat-63 ter of choice and, in principle, both are acceptable and none of 64 them is unphysical, although the results differ enormously. In 65 this case, the IQA analysis in terms of atoms has the advantage 66 of not requiring a fragmentation scheme for its application. 67 Because of the difficulty to discuss EDA results for a single mol-68 ecule, except in some particular cases (like LiH, vide infra), I con-69 sider that an EDA benchmark should discuss trends and not 70 particular molecules. For instance, for alkali metal chloride salts, 71 the covalency should increase in the order LiCl > NaCl > 72 KCl > RbCl > CsCl, in the same order of increasing the ionization 73 potential. Or for lithium halogen salts, considering the trend of 74 electron affinities of the halogen atoms, one could reach the 75 conclusion that the covalency should increase in the order LiCl 76 > LiBr > Lil > LiAt. Another interesting example corresponds to 77 the dissociation of LiH for which a maximum of covalency 78 should be found around the avoided crossing at about 79 3.5-4 Å.<sup>[112]</sup> Pauli repulsion energy, on the other hand, should 80 increase in the order  $H_2$  < LiH < BeH < BH < CH < NH < OH 81 < HF, at least if all of these diatomic species are considered at 82 the same bond length. Or whereas orbital interaction should 83 dominate the formation of H<sub>2</sub> from two H atoms, Pauli repul-84 sion should be the main component of the interaction between 85 two RH molecules to form the RH····HR complex. These are pos-86 sible tests to prove the reliability of EDA methods but I am sure 87 the reader can think of many others. 88

### Paul W. Ayers

Yes. And the benchmarks should be very broad. It is not necessary to have consensus on all the systems (even things as simple as the interaction energy in the water dimer or the energetic barrier to rotation in ethane are interpreted differently by different partitioning methods). But a panoply of results helps establish the similarities/differences between models and, perhaps, also the cases where their nuances are most helpful. I do not want benchmark sets to become the battleground upon which religious wars about chemical concepts are fought, but rather a proving ground upon which they are understood. It is also important, even critical, that the benchmarks be provided together with data and software tools that allow them to be easily used, so that few (if any) new EDA methods are proposed without first being scrutinized against said benchmark(s).

### Farnaz Heidar-Zadeh

Benchmarking various schemes extensively is the way to go for-109 ward! These give us a better understanding of current par-110 titioning schemes and sets that stage evaluating the future 111 schemes. As elaborated by many contributors, it is crucial to 112 have benchmarks that are diverse and comprehensive, both in 113 terms of systems studies and levels of theories considered. It is 114

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also very important, even though less discussed, results generated for a specific schemes' implementation (code) and molecule (system) need to be reproducible, robust, replicable, and generalizable as depicted in the image below.

### Reliability of a given Scheme's results

### Juan Andrés

It is desirable to develop common benchmarks and test sets for cross-validation of methods. Ayers et al.<sup>[87]</sup> propose an axiomatic approach, as it was previously noted by us (see question 1) and by Prof. Solá (see question 7).

### Yirong Mo

Not sure about this. Experimental evidences are always the gold standards.

### 19 Eduard Matito

20 The short answer is yes, there is a large interest in designing 21 validation tests. There is some overlap between questions 22 6 and 7. I decided to comment on "chemical validation tests" 23 on guestion 6 and here, I will comment on another kind of vali-24 dation tests. Benchmarking should also consider other essential 25 features of energy partitions such as basis set dependency (and 26 convergence toward CBS), size extensivity, and method depen-27 dency. Some of these features might be easy to anticipate from 28 the construction of some energy partition schemes (e.g., size 29 extensivity) but other require the design of tests that are appro-30 priate to this purpose. 31

### 32 W. H. Eugen Schwarz

Yes, it would be very deserving. However, at first, a set of useful
 decomposition methods and a set of empirical, valid, reliable
 data must be agreed upon.

# Alston Misquitta and Krzysztof Szalewicz

The only test that can be conducted are those outlined in the answer to question 4, so each method can be tested individually since this is a pass/fail test.

# Question 8: Is it Possible to Contemplate a Unified Partition Scheme (Let Us Call it the "Standard Model" of Partitioning), that Is Proper for all Applications in Chemistry, in the Foreseeable Future or Even in Principle?

### 49 50 Ramon Carbó-Dorca

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The previous question leads to the present one. One can answer it like: if EDA techniques are somehow arbitrary, then it seems difficult to obtain a unified universal partitioning scheme. However, perhaps research on this topic is missing something, which could transform the EDA problem into a precise description. I must confess that I cannot imagine what might be the nature of this missing link.

### Shant Shahbazian

This question is tightly connected to questions 1–3. If the answer to this question is "no" in principle, then I find it really hard to believe that currently used chemical concepts may have any universally precise definition. This means that there will be always an inherent fuzziness in chemical concepts that personally, I find it quite an unpleasant situation. I am interested to see if anyone have a clue or a proposal for a "yes" answer, at least in principle.

### lstván Mayer

I do not think it possible to get a single "standard partitioning model" right because it does not seem possible to get an ultimate unique definition of an individual atom within the molecule. However, the introduction of two or three standardized procedures—one for Hilbert space analysis and one or two for the 3D one—seems to be quite possible. (In the latter case, separate standard schemes for exclusive and fuzzy atoms can be contemplated.)

### Martin Rahm

Unification seems unlikely at present, but that is not necessarily a bad thing. There is strength in diversity. I suspect most in the community strive toward development of as generally applicable methods as possible. In the long term, methods with higher degrees of chemically relevant predictive utility are likely to see more common use.

### Frank Weinhold

Probably not. The idea of universally partitioning chemical phe-89 nomena into mutually exclusive and additive components is 90 inherently superficial, except as a tautological accounting 91 device. The fact that such "components" commonly exhibit 92 greater variations than the energy difference they purport to 93 analyze is itself a telling indicator that their usefulness to the 94 broader chemical community will be marginal. The NAO-based 95 NEDA variant, which alone avoids the conceptual ambiguities 96 of fragment overlap, seems to be the only plausible candidate 97 for such generality. 98

### Roberto A. Boto

In my opinion, a unified partition scheme would require a unified theory of chemical bonding, something that as far as I know, is far from being achieved. From a more pragmatical point of view, the only way of accomplishing this uniformity in partition schemes is not by means of theory, but by consensus.

### Ángel Martín Pendás

Unification is probably not possible for the time being, but109thinking about the characteristics that would allow the different110available methods to "converge" might be a worthwhile enter-111prise. In my probably biased opinion, if a standard model can112be envisaged it should rely on orbital invariant quantities so113that one is not limited by any underlying computational114

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methodology. In the end, this ultimately leads, in agreement with lstván Mayer, to the atom-in-the-molecule conundrum.

### David L. Cooper

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I remains very deeply skeptical that a utopian model of partitioning could ever emerge that not only is applicable to but also (almost) universally agreed to be the "best" choice for, all applications in Chemistry. There is even a sense in which it would be more than a little disappointing if no new Chemistry could ever be discovered for which such a "standard" model might not be the most appropriate.

### 13 Carlo Gatti

Perhaps yes, but I doubt it would be the most appealing one for most of the chemists. In principle, I would be highly in favor of a unified approach and I fully agree with Ángel Martín Pendás that it should rely on orbital invariant quantities. However, as I discussed in my answer to question 1, the aims behind the present partitioning methods are different. Therefore, adoption of a standard model, while favoring scientific rigor, could also result in a significant loss of richness of interpretation.

### 24 25 Paul Popelier

26 I want to be optimistic about a "standard model of partitioning" 27 and indeed strive for it although it could be a long process. As 28 explained in question 4, schemes that make the same predic-29 tions can co-exist, but if they produce contradictory outcomes then they cannot. Allow me to comment on the related and 30 perhaps less sensitive topic of population analyses. In the pleth-31 32 ora of population analyses, the (original) Hirshfeld method and 33 the QTAIM typically produced answers at the two opposite 34 extremes: Hirshfeld was judged to give too small an answer 35 and QTAIM too large. The community often regarded both as 36 suspicious. However, over time Hirshfeld was modified 37 (in response to a theoretical deficiency related to the reference 38 state it invokes) and then gave less extreme values. This is an 39 example of convergence, which is a weaker form of unification. A further step toward convergence would be to finally ditch 40 the Mulliken population analysis, which has been heavily criti-41 42 cized for decades but still regularly pops up. In my PhD thesis, Mulliken charges served the purpose of creating a sufficiently 43 44 reliable crystal field in which solid state molecular geometries could be obtained. However, when I saw a few years later that 45 the Mulliken population analysis assigned a non-negligible neg-46 ative net charge (i.e., -0.26) to a boron atom<sup>[135]</sup> then I am 47 48 happy to ditch Mulliken because its answer violates any of the 49 dozen electronegativity scales. In terms of Darwinian selection, 50 a harsher environment consisting of the now more demanding 51 user results in Mulliken not surviving ultimately. To make the 52 main point again: diversity is good provided it leads to a stron-53 ger end product. However, diversity for its own sake, in terms 54 of wallowing in contradictory interpretations and lauding this 55 situation as the richness of Chemistry is wrong. Yes, chemistry 56 is a complex science, which is we should do an utmost effort to keep it clean and logical. When I look at typical undergraduate 57

textbooks then I think there is still much work to do. However, I 58 think we will get there. The traditional Sciences of Chemistry 59 and Biology continue to undergo a physicalization process: they 60 become better and better connected with an underlying physi-61 cal and indeed quantum mechanical reality. Whereas a typical 62 biochemistry textbook of today is still nave in its typically intro-63 ductory chapters on physical chemistry, the enzymology it 64 reports later is full of protein crystal structures that take away 65 the yesteryear mysteries of the atomistic working of an enzyme. 66 Optimistically I believe in an irreversible gradient of knowledge. 67 Yes, there are temporary regressions but I would be horrified if 68 Science mere oscillated between stagnating alternative 69 theories. 70

Pedro Salvador

I agree with general view here that a unified partition scheme is unlikely to be set in the near future. Yet, by gathering a sufficient number of "stress tests" for the existing partition schemes as I suggest in question 7, one can probably narrow the search to a handful of them, which hopefully will produce similar outputs for most purposes. On the other hand, in the present context of energy decomposition schemes, unification in the formulation applied to different levels of theory is also desirable. In particular, a rigorous topological EDA for KS DFT that is able to provide energy contributions comparable to those obtained for correlated wavefunction methods is still lacking, in my opinion.

### Jerzy Cioslowski

I very much doubt that it is possible to design "the one and only" energy partitioning scheme within each of the two classes I discussed in my answer to question 1. However, would be very desirable to agree on a set of rules (or axioms) that have to be satisfied by any admissible scheme. At present, some of such axioms (like that the partitioned properties should approach those of isolated systems as the intersystem separation goes to infinity) are both obvious and widely accepted, whereas others (like that the partitioned properties should be retrievable with equal ease from wavefunctions given on a grid or in terms of atom-centered basis functions, single-centered basis functions, or plane waves), while being equally obvious, are ignored by a surprisingly large segment of practitioners of quantum chemistry.

### Gernot Frenking

No! The complexity and diversity of electronic structures in mol-107 ecules and solids requests partitioning schemes that are appro-108 priate for the given situation. The species may be grouped into 109 classes that have similar properties, for which a particular 110 model may be used, while it is less suitable for others. It holds 111 in general to use more than one partitioning scheme and to 112 compare the results before a statement about the best descrip-113 tion of the bonding situation is made. 114 Paul W. Avers



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It is useful to contemplate, but it is a bit like contemplating nirvana. Useful, but it is best to live in the real (imperfect) world most of the time. I tend to feel that while unified partitioning schemes may exist (in the sense that there may be atom-inmolecule partitioning schemes and energy decomposition analysis methods with broad utility and applicability and, indeed, some of our current tools approach this lofty standard) there will always be room for improvement. At some point, though, the "improvements" one might make will be achieved only by adding complexity ("engineering" the model in a way that risks overfitting), and some convergence may occur. However, as every person has a different tolerance for model complexity (in a different context, some prefer PBE, some BLYP, and some M06L), the idea that our community could ever agree upon a "standard model" seems...unfathomable. Indeed, it seems we cannot even agree whether such a standard model should be pursued!

### Farnaz Heidar-Zadeh

Having a unified partitioning scheme is the holy grail. As such, it is not possible to find a universal definition or even get close to one. However, this should not lead one to underestimate the usefulness and value of partitioning schemes (and other concepts) and the need for improving/validating the existing approaches.

### Juan Andrés

It is possible to contemplate a unified partition scheme, but it must be recognized that this is still a pretension. In the current state, I do not see a possible way to reach it.

### Yirong Mo

I am not optimistic about this. Researchers always intend to be unique and propose something different from others. So there will be a constant endeavor to propose "novel" and "for the first time" kind of partition schemes.

### Eduard Matito

I highly doubt that an energy partition "to unite them all" will ever be found. In the best case scenario, I would expect that we find a partition (or a set of them) that gives reasonable predictions for "chemical validation tests".

### Eloy Ramos-Cordoba

I also agree that it is unlikely that a unique "standard model" can be defined. However, as Prof. Cioslowski stated above, I also think it would be convenient to establish a set of axiom or requirements (e.g., well-defined basis set limit), based on mathematical or quantum mechanical arguments that every EDA has to fulfill.

### W. H. Eugen Schwarz

No: The various partition schemes yielding a few small numbersto explain a given class of molecules w.r.t. a given type of

questions (e.g., concerning stability or reactivities) are quite58diverse. The universal cover approach consists of general quan-<br/>tum mechanics combined with a comprehensive set of ques-<br/>tions, which is too demanding to be useful.60

### Alston Misquitta and Krzysztof Szalewicz

Not only contemplate, SAPT already provides the standard model and we believe this has been generally recognized in recent years.

### Question 9: In the End, Science Is about Experiments and the Real World. Can One Therefore Use any Experiment or Experimental Data Be Used to Favor One Partition Scheme over another?

### Ramon Carbó-Dorca

If experimental data could relate to EDA, then possibly the precise description of the theoretical scheme might be solved. The adequate (ultimate) EDA will be the one adapting better to this kind of experiment. Can one imagine any experiment of this kind to be performed soon? However, if there is an experiment which can be (completely) adapted to some EDA, this will mean that the EDA terms will become observables. Therefore, a quantum mechanical operator (or operators) might be constructed to describe the experiment. Can one foresee this observable nature of the EDA partition terms?

### Martin Rahm

88 Aside from valiant efforts toward X-ray constrained 89 wavefunctions,<sup>[136]</sup> which might move all EDA's closer to experi-90 ment, most of what we do in the field requires a quantum 91 mechanical calculation to approximate a wave function or den-92 sity. My personal preference is toward concepts and quantities 93 that are, at least in principle, experimentally measurable. For 94 this reason, I am exploring the possibilities of an EDA that can 95 interchangeably rely on both measurements and quantum 96 chemical calculations.<sup>[54]</sup> Of course, plenty of nonobservable 97 quantities are conceptually valuable. Time will tell when and 98 where an "Experimental Quantum Chemistry" EDA approach is 99 more advantageous in some respects. Experimental comparison 100 and cross-validation, discussed in questions six and seven, 101 should help to highlight complementarities between EDA 102 methods and be a good basis for making more informed 103 choices for particular sets of systems and questions. 104

### Shant Shahbazian

This guestion is tightly connected to guestions 6 and 7. Without 107 any reference to experimental data, which are free from subjec-108 tive judgments and chemical prejudice, it is hard to see how a 109 positive operational answer may be given to questions 6 and 110 7. I am interested to see if someone have any clue or proposal 111 on how a partitioning scheme may, in a nontrivial way, to be 112 connected to quantitative experimental data. However, if there 113 114 is no link, I see no way of real progress.



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### lstván Mayer

Probably not directly. However, the different partition schemes should be globally consistent with the chemical experience in order to be practically useful.

### Frank Weinhold

For H-bonding phenomena, the mentioned reference in question 3 suggests the correlative test that can be applied to the "electrostatics" component common to most EDA partitions. A recent critique of the SAPT partition<sup>[137]</sup> also shows how "steric" or "induction" components can be tested for consistency with measurable properties of prototype chemical species.\*

### Ángel Martín Pendás

Besides X-constrained wavefunction approaches, some EDAs like IQA rely only on an atomic partition of space, that can be retrieved from experimental charge densities, and first and second order densities, which despite being observables, are very difficult to access experimentally. Even though a whole experimental energetic decomposition might still not be possible, some of its components, like the electrostatic energies, indeed are. Electrostatic potentials, which can be envisaged as a byproduct of EDAs, are routinely obtained from experiment and partitioned into atomic contributions. So, although the global answer to the question may be not, I expect some advances in the near future.

### David L. Cooper

Much as it could be very interesting to live in a Universe in which most of the components returned by a well-constructed energy partitioning scheme could be directly related to expectation values of operators or even to experimental data, I strongly suspect that we do not. Even if we did, it would also be important that we could associate the relevant experimental data with a realistic level of chemical interpretation. Otherwise, we could just have decomposed one number into a sum of others that might not really have brought with them any additional useful chemical/physical insights. In this sense, I agree wholeheartedly with István Mayer that useful partitioning schemes need to be consistent with chemical experience.

### Paul Popelier

I wrote about the need<sup>[138]</sup> for falsification in the research of interpretational theoretical chemistry, which is in the spirit of this question. There I proposed the potentially falsifiable example of  $B_2H_6$  where IQA states that the interatomic exchange energy between the bridging hydrogen atoms is about three times larger than that between the two borons. When presented with this information, Roald Hoffmann responded that the HH interaction is something new to him and that there is some BB bonding is easier to understand, based on a molecular orbital argument. Since writing about falsification I have

\*Bernard Silvi: the reply of A. Stone and K. Szalewicz has been published in the same issue of J. Phys. Chem. A<sup>[117]</sup>

received very little response, probably because it is very difficult 58 to set up experiments that can falsify a partitioning scheme. If 59 one looks at the review of Phipps et al.<sup>[2]</sup> then it appears that 60 the comparison between EDAs is not against some experiment 61 but by comparison of disadvantages and problems of the vari-62 ous EDAs. Examples of observations or judgments (see table 2) 63 sound like: "Observed overestimation of polarization and under-64 estimation of charge transfer." or "Presence of the DEMIX 65 energy unascribable to any particular component. Problems of 66 numerically unstable charge transfer and polarization energies 67 with large basis sets and at short intermolecular distance". It 68 appears that we are still a long way off of making contact with 69 experiment. 70

Pedro Salvador

My answer to questions 7 and 8 can also fit in here. In agreement with István and David, agreement with chemical intuition is essential. We should be able to "quantify" such agreement with the chemical experience, at least in a semiquantitative way (e.g., this value should be larger than that other value, or this value must be non-negative, etc...) to build up a survival-ofthe-fittest strategy.

### Julien Pilmé

Yes, this is a fundamental question, in principle any theory needs to be supported (or refuted) by a "face-to-face" meeting with experiment data. Currently, results obtained from EDA methods globally skip this process, these results nevertheless need to be in agreement with the chemical experience based on numerous "fuzzy" concepts, so we go back to question 1. Of course, this latter confrontation is very useful for our daily work but it can be also a little "dangerous" when results contradict the chemical experience, it can become a deadlock situation.

### Jerzy Cioslowski

The only quantities that are presently amenable to experimen-94 tal measurement are those given by matrix elements (including 95 expectation values) of global operators. In practice, this means 96 energies (and their differences), and the electric/magnetic 97 response properties such as multipole moments, polarizabilities, etc...The one-electron densities have never been measured 99 experimentally as: (1) the number of experimental points is 100 always finite whereas the density is a function of a continuous 101 argument and (2) since the amplitudes (but not phases) are 102 measured in scattering experiments, the "measured" densities 103 are really model densities that fit best the amplitudes with the 104 phases approximately inferred from (admittedly clever) inaccu-105 rate methods. These model densities are very useful as a tool 106 for the location of nuclei and may even yield reasonable multi-107 pole moments but nevertheless, they have nothing to do with 108 the expectation values of the sum of one-electron Dirac deltas. 109 Keeping this in mind, one has to be very skeptical about the 110 possibility of (to use Martin Rahm's words) "moving EDA's closer 111 to experiment" as many of the partitioning schemes rely explic-112 itly on both local and global properties of one-electron 113 densities. 114

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### **Gernot Frenking**

The preference of a particular partitioning scheme is not decided by an experiment, but by the interpretation of the experimental results. This is done by the human mind of the observer. "Real world" implies a definition of physical reality in a region where quantum theory is valid but not classical physics. The outcome of a Diels-Alder reaction can only be explained when the symmetry (sign) of the wave functions of the interactions species is considered. This gives the wave function the status of physical reality. Three statements at the end: (1) Physical reality becomes a fuzzy concept when quantum effects are considered. (2) When chemical facts are reduced to physical laws alone, they become mere stamp collection. Fuzzy concepts are an integral part of chemistry. (3) Historically developed concepts must be examined with quantum chemical calculations, because they may be based on assumptions that are not correct.

### Julia Contreras

My answer to this is pretty similar to question 6.

### Émilie-Laure Zins

26 I agree with the general opinion of the previous contributors: a 27 comparison and a dialogue between theoretical and experi-28 mental chemists are essential. But what experimental tools 29 could be used in comparison with theoretical studies on energy partition schemes? Do the existing partition schemes allow a 30 comparison with observable or deductible quantities from 31 32 experiments? Would it be possible to develop new partition 33 schemes allowing an easier comparison with experimental 34 data? I think the answer to the latter question is "yes", and that 35 it would be interesting to move in this direction, probably by 36 using a combination of complementary experimental 37 approaches, or even by developing new experimental 38 approaches. Of course, experimental techniques do not allow 39 an energetic decomposition, but in-depth investigations involving complementary experimental techniques allow to deduce 40 41 information on polarization and polarizability, the contribution 42 of the spin...Among the most versatile tools, we can mention the technique of isolation of the investigated species in a 43 44 matrix (rare gas, para-hydrogen,...at cryogenic temperatures 45 (typically below 20 K). This technique allows to characterize weak interactions, such as hydrogen bonds or agostic interac-46 47 tions. This technique is also useful to probe the spin state of a 48 metal atom in an organometallic complex, or even to induce 49 changes in spin states by photo-excitation. Isomerizations 50 between different inter or intramolecular complexes can also 51 be detected by annealing. This isolation technique is often 52 coupled with vibrational spectroscopy. One could imagine the 53 development of such an experimental set-up allowing to apply 54 a magnetic field. The use of such advanced experimental 55 approaches to deduce some of the physical components of an 56 energy partition scheme would need to be discussed with the 57 experimental chemists and/or physicists.

### Laurent Joubert and Vincent Tognetti

Another important point to emphasize, from our point of view, is that experimental energies are often Gibbs energies. Most energy decompositions discussed here only deal with electronic ones, and thus do not include entropy. However, it is known that entropy is a quantity of fundamental importance to account for experimental results (see Ref. [139] for a recent example in organic chemistry where the experimental selectivity in dipolar cycloadditions is governed by such factors). As well known, entropy can be decomposed into electronic, translational, rotational, and vibrational ones. The last term is the sum of contributions from each normal mode. Unfortunately, the most important ones correspond to the lowest frequency values, characteristic of vibrations of small amplitudes delocalized over the whole molecule. They are thus difficult to analyze from a chemical (regional) point of view. This is an important limit to rationalizing experimental chemical results, in particular for complex systems. In such cases, even if very accurate and meaningful EDAs are obtained for the electronic part, the thermodynamic contributions remained an issue, notably for condensed phases. From this point of view, EDAs cannot guide us for selecting the most relevant physicochemical properties.[139]

### Paul W. Ayers

I often use the following quote from Willard van Orman Quine,<sup>[140]</sup> [1953], "Our acceptance of an ontology is, I think, similar in principle to our acceptance of a scientific theory, say a system of physics; we adopt, at least insofar as we are reasonable, the simplest conceptual scheme into which the disordered fragments of raw experience can be fitted and arranged."

The real world provides the "disordered fragments of raw experience" which we try to "fit and arrange" into our theories. All of our arguments (at least the ones I judge to have some value) are about which theoretical scheme is the simplest (an aesthetic judgment) and how well experimental data fit and arrange into various schemes (which standardized benchmark datasets help us to quantify).

### Farnaz Heidar-Zadeh

It can, but indirectly! The partitioning schemes can be used in interpreting the outcome of experiments (i.e., justification) or designing a specific experimental outcome (i.e., prediction). These indirect experimental tests can ultimately leave us with a smaller set of favorable schemes which perform better in justifying/predicting the experimental results. Ultimately, these schemes will help us design molecules and materials with desired properties.

### Juan Andrés

In this context, it should be noted that in principle a partition111scheme is more desirable if it is based on electron density,112since it is an observable and also can be derived from charge113density that is obtained experimentally.114



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It is the only way. Even there is little direct experimental data for partition schemes, there are many indirect evidences to examine individual energy terms. Structural and spectral parameters are good indicators for partition schemes. In the study of intermolecular interaction, distance-dependent energy profiles are often instructive for the verification of partition schemes. For instance, in the void of orbital (electron transfer) interactions, the optimal intermolecular distances should be comparable to reqular van der Waals distances (unless strong electrostatic interactions exist). Unfortunately, so far, very few partition schemes can perform geometry optimization. But at least numerical test calculations with small systems can be done for all partition schemes.

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### **Eduard Matito**

17 Maybe, but I doubt we will generate numbers that can be directly 18 compared to the experimental ones and, at the same time, pro-19 vide undeniable chemical insight. For instance, in the future, per-20 haps we can obtain reliable electron density data that leads to accurate prediction of, let us say, QTAIM atomic energies. How-22 ever, the fact that we can measure these energies does not make 23 them any more useful to provide chemical insight. On the other 24 hand, I believe experimental evidence can provide qualitative information that is useful in assessing energy partitions.

### **Eloy Ramos-Cordoba**

In principle since energy components are not observables, it seems not possible to quantify them by direct observation. However, some energetic information can be extracted from experiments. For instance, molecular-beam scattering experiments have been used to indirectly quantify the charge-transfer stabilization energy.

#### 35 W. H. Eugen Schwarz 36

37 Yes. Ultimately, the purposes of theory and partition schemes 38 are creating models that help to intuitively understand and 39 extrapolate (predict) the experimental facts. The answer to this last question 9 therefore depends on three points: First, the par-40 41 tition scheme should appropriately explain the experimental 42 trends as seen by the chemists If a theoretical model cannot 43 reproduce differences chemists are commonly talking about 44 (such as nonbonded repulsion vs chemical bonding attraction, 45 or strong vs very strong ionic or covalent interactions) then probably the theoretical scheme should be modified. Second, 46 47 the observation of a positive value may be theoretically repre-48 sented by the sum of one or two positive terms and several 49 small corrections, or as a sum of several large numbers of differ-50 ent signs. The latter model is not satisfactory. It may then help 51 to combine some numbers to get only medium-sized contribu-52 tions of same sign, for instance summing large positive Pauli 53 repulsion and large negative quasi-classical electric attraction to 54 construct the "steric interaction" (or some other combination, 55 depending on the case). Namely, not only the values of a specific 56 partitioning characterize the real system, but also which type of 57 partitioning is simple in the given case. Third, whether a partitioning is useful and efficient also depends on the cogni-58 59 tive competences and preferences of the users. Some experimentalists and theoreticians focus on the observable numbers only; 60 some other ones also consider the process of relaxation that 61 results in the observed outcome. Different partition schemes 62 may be required for different addresses. 63

### Alston Misguitta and Krzysztof Szalewicz

Indirectly, due to SAPT-based PESs providing close interplay 67 with experiments and due to the fact that SAPT interaction 68 energy is built up from components (rather than decomposed), 69 comparisons with experiments provide a real-world connection 70 for these components. SAPT has been used to develop pPESs 71 for a large number of dimers. SAPT PESs are among the most 72 accurate ones published and if used in nuclear dynamics calcu-73 lations predict observables in excellent agreement with experi-74 ment, for example, for the water dimer spectra.<sup>[141,142]</sup> Also, 75 SAPT PESs allow precise predictions of crystal structures.<sup>[143]</sup> 76 Thus, there is a strong connection between SAPT and experi-77 ment. Although these comparisons involve the total PESs, there 78 is a weaker connection to SAPT components as well. For exam-79 ple, to predict correctly crystal densities, one has to have the 80 repulsive walls at the right places, which tests the exchange-81 repulsion energy. Crystals of monomers dominated by disper-82 sion interactions, like for example the argon crystal,<sup>[144]</sup> indi-83 rectly test this component of SAPT. There is a further broad 84 connection to the real world: construction of force fields based 85 on SAPT components and using forms of the fitting functions 86 that reflect the behavior of SAPT components.<sup>[88,145]</sup> One can fit 87 intermolecular interaction energies by several types of analytic 88 functions or even use methods such as neural networks, but 89 fitting with physically relevant forms enables such PES to be 90 transferable. Use of SAPT to develop biomolecular force fields 91 has become increasingly popular.<sup>[146]</sup> A particular example is 92 water clusters. There is experimental data available for such 93 clusters, for example, the authors of Ref. [147] performed mea-94 surements on hexamer, heptamer, and nonamer. A very accu-95 rate force field developed in Ref. [148] was fitted to CCSD(T) 96 calculations for the water dimer and trimer. Predictions of prop-97 erties of clusters from this force field agree very well with accu-98 rate ab initio data available for some clusters. Thus, component-99 based force fields enable calculations for water clusters of 100 essentially arbitrary size, whereas reasonably accurate ab initio 101 calculations are limited to about 20 water molecules. In Ref. 102 <sup>[148]</sup>, not only the form of the fitting function was designed 103 based on the behavior of SAPT components, but also the long-104 105 range asymptotics was computed ab initio using SAPT codes. In contrast, while damping and exchange-repulsion parameters 106 are also consistent with SAPT, the parameters in these terms 107 are just free parameters of the fit. This can be improved by per-108 forming SAPT calculations for close-range separations and 109 fitting component-by-component (as done for water in Ref. 110 [141]). While such direct fits can currently be done for dimers 111 and for small trimers, there remains an issue with higher than 112 three-body contributions. Reference [148] approximated such 113 contributions by a damped classical polarization model iterated 114



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1 to convergence over the whole cluster. While the polarization 2 model alone is a poor approximation to three-body interaction 3 energies, it was shown in Ref. [148] that this model recovers 4 the four- to six-body interaction energies surprisingly well. Since 5 the many-many body polarization models is so critical for clusters and condensed phases, work on improved forms of this 6 7 model is essential. Here the work of Refs. [115,119] is important 8 since it both extends the model beyond the isotropic dipole-9 dipole polarizability case and designs better damping functions which are essential at shorter separations. Furthermore, the 10 11 decomposition of induction energy into polarization (including 12 a part of the exchange components) and charge-transfer terms 13 may lead to improved models of damping.

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### 16 Concluding Remarks

### Bernard Silvi

19 For this article, I tried to collect a large panel of opinions on the 20 use of EDA methods in Quantum Chemistry. I had no 21 preconceived ideas about the outcome and therefore, I have 22 been surprised by the diversity of points of view often appar-23 ently contradictory. Whereas some contributors reject EDA 24 methods, many others consider them as a fundamental contri-25 bution of Quantum Chemistry. The origin of this dispersion of opinions is not a crisis of our discipline announcing the advent. 26 27 of a new paradigm but rather a consequence of its good health. 28 As we wrote in the introduction, EDAs are tools (not theories) 29 providing pieces of information enabling to set up explana-30 tions. They belong to normal science processes and as tools, they have not to strictly satisfy demarcation criteria. They are 31 32 mostly used to understand geometries and stabilities of mole-33 cules and molecular complexes on the basis of quantum chemi-34 cal and physical arguments. Here quantum chemical is related 35 to systems of explanations based on quantum chemical con-36 cepts such as those of orbital, valence-bond structure, etc... 37 whereas physical concerns arguments rooted in the theory of intermolecular forces. These systems of explanation may be 38 39 interdependent and complementary, never contradictory: they address different meanings of a given guestion and are 40 intended for different scientific (sub)communities. Each system 41 42 corresponds to its own representation of the microscopic matter, adopts its own point of view and uses its own vocabulary. 43

44 Moreover, there is an inherent source of difficulty in our 45 attempt to explain the microscopic matter because we try to understand the behavior of quantum objects which is not 46 47 deterministic in a deterministic fashion. Most explanations in science belong to the deductive-nomological account<sup>[149]</sup> 48 49 which provides a scheme for any deterministic explanation of a 50 particular event and consists in a deductive derivation of the 51 occurrence of the event from a set of true propositions involv-52 ing at least a scientific law or principle. The choice of rules and 53 principles leaves additional degrees of freedom.

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55 Keywords: energy decomposition analysis interaction
 56 energy · partitioning · chemical bonding · status of the
 57 methods

How to cite this article: J. Andrés, P. W. Ayers, R. A. Boto, R. Carbó-Dorca, H. Chermette, J. Cioslowski, J. Contreras-Garcia, D. L. Cooper, G. Frenking, C. Gatti, F. Heidar-Zadeh, L. Joubert, Ángel Martín Pendás, E. Matito, I. Mayer, A. Misquitta, Y. Mo, J. Pilmé, P. L. A. Popelier, M. Rahm, E. Ramos-Cordoba, P. Salvador, W. H. E. Schwarz, S. Shahbazian, B. Silvi, M. Solà, K. Szalewicz, V. Tognetti, F. Weinhold, Émilie-Laure Zins. *J. Comput. Chem.* **2019**, 9999, 1–37. DOI: 10.1002/jcc.26003

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Received: 13 May 2019 Accepted: 16 May 2019

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