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# Nonlinear Polarization Rotation in Semiconductor Optical Amplifiers: Theory and Application to All-Optical Flip-Flop Memories 

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#### Abstract

We present a model for polarization-dependent gain saturation in strained bulk semiconductor optical amplifiers. We assume that the polarized optical field can be decomposed into transverse electric and transverse magnetic components that have indirect interaction with each other via the gain saturation. The gain anisotropy due to tensile strain in the amplifier is accounted for by a population imbalance factor. The model is applied to a nonlinear polarization switch, for which results are obtained, that are in excellent agreement with experimental data. Finally, we describe an all-optical flip-flop memory that is based on two coupled nonlinear polarization switches.


Index Terms-Nonlinear polarization rotation, optical flip-flop memories, optical signal processing, optical switching, semiconductor optical amplifiers.

## I. Introduction

THE USE of polarization switches based on nonlinear polarization rotation in semiconductor optical amplifiers (SOAs) in optical signal processing applications is receiving considerable interest by many research groups. Applications of polarization switches to wavelength conversion are presented in [1]-[4]. Applications of polarization switches to optical time domain demultiplexing are presented in [5], [6]. Recently, the importance of polarization switches for all-optical logic has also been recognized [7]-[9]. Despite the large amount of experimental results that are published on polarization switches, the underlying concepts are not well understood [8]. In [10], theoretical results are published on polarization-dependent gain in SOAs in the context of optical switching and optical bistability, but their results are based on a microscopic model that is impractical as a design tool for optical switching configurations. We present a simple rate-equation model that can be used to model the switching characteristics of a polarization switch.

Our model is based on the decomposition of the polarized optical field into a transverse electric (TE) and transverse magnetic (TM) component. These modes propagate "independently" through the SOA, although they have indirect

[^1]interaction with each other via the gain saturation. We have accounted for different TE and TM gains by assuming that these polarizations couple to different hole reservoirs. This assumption is justified by the fact that the optical transitions occur between the $j=1 / 2$ type conduction band states and the $j=3 / 2$ type valence band states, where the latter correspond to the light-hole and heavy-hole valence bands. Two out of the three possible transition types are selected by the TE and TM polarizations, which define two corresponding inversions. In the isotropic bulk situation, these two transitions occur in a fully symmetric manner, but we are now interested in the case where tensile strain is built into the bulk medium, causing an asymmetry between the two transition types, such that TM will be favored over TE transitions. This will be modeled by introducing a population imbalance factor $f$.

Our rate equation model is applied to describe the switching characteristics of a polarization switch that is based on these principles. We find excellent agreement between our model and experimental data. Our results also reveal that there is an interesting similarity between the switching properties of a polarization switch and those of a Mach-Zehnder switch, which indicates that the polarization switch acts as a Mach-Zehnder switch, where the roles of the different light path are now played by the independently operating TE and TM modes of the optical field. Finally, we demonstrate an all-optical flip-flop memory that is made from two coupled polarization switches. This all-optical flip-flop has a simple structure, separate set and reset inputs and a large input wavelength range. We demonstrate the feasibility of the concept and we show that the contrast ratio between output states of flip-flop is over 20 dB , while the switching power is less than -3 dBm .

In Section II, we present the rate equation model that is based on the assumptions given above. Experimental results show that this model can explain the polarization-dependent gain saturation of a SOA. In Section III, we point out how our results can explain polarization switching in systems employing SOAs. We find excellent agreement between our model and experimental results. In Section IV, we demonstrate an optical flip-flop memory that is made from two coupled polarization switches. The paper is concluded with a discussion.

## II. Model

We decompose the incoming arbitrarily polarized electric field in a component parallel to the layers in the waveguide

TABLE I
SOA Parameter Definitions and Their Values

| Parameter | Symbol | Value | Units |
| :--- | :--- | :--- | :--- |
| Confinement factor | $\Gamma^{T E}, \Gamma^{T M}$ | $0.2,0.14$ |  |
| Phase modulation coefficients | $\alpha^{T E}, \alpha^{T M}$ | 5,5 |  |
| Modal loss | $\alpha_{\text {int }}^{T E}, \alpha_{\text {int }}^{T M}$ | $0.27,0.27$ | $\mathrm{ps}^{-1}$ |
| Gain coefficient | $\xi^{T E}, \xi^{T M}$ | $7.0,6.5$ | $10^{-9} \mathrm{ps}^{-1}$ |
| Hole population imbalance factor | $f$ | 0.5 |  |
| Electron-hole recombination time | $T_{1}$ | 500 | ps |
|  |  |  |  |
| Hole-hole relaxation time | $T_{2}$ | 0.1 | ps |
| Optical transition state number | $N_{0}$ | $10^{8}$ |  |
| Group velocity | $v_{g}$ | 100 | $\mu \mathrm{~m} / \mathrm{ps}$ |
| Electrical current | $I$ | 160 | mA |
| SOA length | $L$ | 800 | $\mu \mathrm{~m}$ |

(TE mode) and a perpendicular component (TM mode). These two polarization directions are along the principal axes that diagonalize the wave propagation in the SOA. In fact, apart from their indirect interaction through the carrier dynamics in the device, these two polarizations propagate independently from each other. It is our aim to develop a model capable of describing the polarization behavior up to speeds of a few tens of gigahertz. In this case, we can use relatively simple propagation and rate equations, i.e., without necessity of taking into account the ultrafast (subpicosecond timescale) intraband relaxation dynamics.

The propagation equation for the TE-polarized electric field component $A^{\mathrm{TE}}(z, t)$ is given by

$$
\begin{align*}
\left(\frac{\partial}{\partial t}+v_{g}^{\mathrm{TE}} \frac{\partial}{\partial z}\right) A^{\mathrm{TE}}(z, t)=\frac{1}{2} \Gamma^{\mathrm{TE}}\left(1+i \alpha^{\mathrm{TE}}\right) \\
\cdot g^{\mathrm{TE}}(z, t) A^{\mathrm{TE}}(z, t)-\frac{1}{2} \alpha_{\mathrm{int}}^{\mathrm{TE}} A^{\mathrm{TE}}(z, t) . \tag{1}
\end{align*}
$$

Here, $A^{\mathrm{TE}}(z, t)$ is the weakly time and space-dependent complex envelope of the optical field, $v_{g}^{\mathrm{TE}}$ is the corresponding group velocity taken at the central frequency of the wave, $\Gamma^{\mathrm{TE}}$ is the confinement factor, $g^{\mathrm{TE}}(z, t)$ is the (real) gain function, $\alpha^{\mathrm{TE}}$ is the phase-modulation parameter, and $\alpha_{\mathrm{int}}^{\mathrm{TE}}$ is the modal loss. A similar rate equation holds for the complex field envelope $A^{\mathrm{TM}}(z, t)$ corresponding to the TM mode

$$
\begin{align*}
&\left(\frac{\partial}{\partial t}+v_{g}^{\mathrm{TM}}\right.\left.\frac{\partial}{\partial z}\right) A^{\mathrm{TM}}(z, t)= \\
& \frac{1}{2} \Gamma^{\mathrm{TM}}\left(1+i \alpha^{\mathrm{TM}}\right)  \tag{2}\\
& \cdot g^{\mathrm{TM}}(z, t) A^{\mathrm{TM}}(z, t)-\frac{1}{2} \alpha_{\mathrm{int}}^{\mathrm{TM}} A^{\mathrm{TM}}(z, t)
\end{align*}
$$

where $A^{\mathrm{TM}}(z, t)$ is the weakly time- and space-dependent complex envelope of the optical field, $v_{g}^{\mathrm{TM}}$ is the corresponding group velocity, $\Gamma^{\mathrm{TM}}$ is the confinement factor, $g^{\mathrm{TM}}(z, t)$ the (real) gain function, $\alpha^{\mathrm{TM}}$ is the phase-modulation parameter,


Fig. 1. Waveguide structure and definition of coordinate frame.
and $\alpha_{\mathrm{int}}^{\mathrm{TM}}$ is the modal loss. The envelopes for each polarization can be expressed as

$$
\begin{align*}
A^{\mathrm{TE}}(z, t) & =\sqrt{S^{\mathrm{TE}}(z, t)} e^{i \phi^{\mathrm{TE}}(z, t)} \\
A^{\mathrm{TM}}(z, t) & =\sqrt{S^{\mathrm{TM}}(z, t)} e^{i \phi^{\mathrm{TM}}(z, t)} \tag{3}
\end{align*}
$$

where $S^{\mathrm{TE}}(z, t)$ and $S^{\mathrm{TM}}(z, t)$ are the photon numbers and $\phi^{\mathrm{TE}}(z, t)$ and $\phi^{\mathrm{TM}}(z, t)$ are the phases for the TE and TM components.

The two optical modes have indirect interaction via the carriers. We assume that the TE and TM polarizations couple the electrons in the conduction band with two distinct reservoirs of holes. This assumption is justified by the fact that in zincblende structures such as GaAs and InP, optical transitions occur between $j=1 / 2$-type conduction band states and the $j=3 / 2$-type valence band states, where the latter are subdivided into light- and heavy-hole band states. In principle, three types of transitions can occur, but for the waveguide structure shown in Fig. 1, with the optical field propagating in the $z$ direction, the transitions with $z$ polarization are not activated. The remaining two transitions with $x$ and $y$ polarizations correspond to TE and TM polarizations, respectively. Hence, two out of the three possible transition types are selected by the TE and TM polarizations and these transitions define two relevant hole reservoirs, with corresponding numbers $n_{x}$ and $n_{y}$, respectively. In the isotropic bulk situation, the two transitions will occur in a fully symmetric manner, but we are now interested in the case where tensile strain is built into the bulk medium, causing an asymmetry between the two transition types, such that TM will be favored over TE transitions [17]. This compensates for extra TM waveguide losses and confinement factor differences so as to make the SOA polarization independent.

The number of electrons in the conduction band is denoted by $n_{c}(z, t)$, while the number of holes involved in the $x$ and $y$ transitions is denoted by $n_{x}(z, t)$ and $n_{y}(z, t)$. A more in-depth analysis shows that $n_{y}$ is just the number of holes in the light-hole band, while $n_{x}$ is made up of a mixture of light ( $25 \%$ ) and heavy ( $75 \%$ ) holes. In fact, due to tensile strain the light-hole population can be enhanced over the heavy holes, leading to enhanced TM transitions. This latter effect will be


Fig. 2. Experimental setup that is used to measure the polarization-dependent SOA gain. SOA: Semiconductor optical amplifier. ISO: Isolator. ATT: Attenuator. Circ: Circulator. BPF: Bandpass filter. PM: Power meter.
accounted for by an imbalance factor $f$ [see (8)-(10)]. The (linearized) gain $g^{\mathrm{TE}}(z, t)$ for TE polarization is given by

$$
\begin{equation*}
g^{\mathrm{TE}}(z, t)=\xi^{\mathrm{TE}}\left[n_{c}(z, t)+n_{x}(z, t)-N_{0}\right] \tag{4}
\end{equation*}
$$

where $\xi^{\mathrm{TE}}$ is the gain coefficient for the TE mode and $N_{0}$ is the total number of electronic states involved in the optical transition. Similarly, the gain $g^{\mathrm{TM}}(z, t)$ can be expressed as

$$
\begin{equation*}
g^{\mathrm{TM}}(z, t)=\xi^{\mathrm{TM}}\left[n_{c}(z, t)+n_{y}(z, t)-N_{0}\right] \tag{5}
\end{equation*}
$$

where $\xi^{\mathrm{TM}}$ is the gain coefficient for the TM mode. In cases of high-intensity optical beams, one should correct $\xi^{\mathrm{TE} / \mathrm{TM}}$ for saturation due to the carrier heating according to

$$
\xi^{\mathrm{TE} / \mathrm{TM}}=\frac{\xi_{0}^{\mathrm{TE} / \mathrm{TM}}}{1+\varepsilon S^{\mathrm{TE} / \mathrm{TM}}}
$$

where $\varepsilon$ is typically $10^{-7}$ per photon present in the SOA [11]. In the experiments that follow, we use optical fields that have a much lower intensity so that in good approximation $\xi^{\mathrm{TE} / \mathrm{TM}}=$ $\xi_{0}^{\mathrm{TE} / \mathrm{TM}}$. In writing down (4) and (5), we tacitly assumed that the semiconducting medium in the active layer gives rise to anisotropic gain, such as can be realized in a bulk layer with tensile strain [12]. If we assume that the total number of holes is equal to the number of electrons

$$
\begin{equation*}
n_{c}(z, t)=n_{x}(z, t)+n_{y}(z, t) \tag{6}
\end{equation*}
$$

and substitute this into (5) and (6), we can express $g^{\mathrm{TE}}(z, t)$ and $g^{\mathrm{TM}}(z, t)$ as

$$
\begin{align*}
g^{\mathrm{TE}}(z, t) & =\xi^{\mathrm{TE}}\left[2 n_{x}(z, t)+n_{y}(z, t)-N_{0}\right] \\
g^{\mathrm{TM}}(z, t) & =\xi^{\mathrm{TM}}\left[2 n_{y}(z, t)+n_{x}(z, t)-N_{0}\right] \tag{7}
\end{align*}
$$

The rate-equation for $n_{x}(z, t)$ can be written as

$$
\begin{align*}
\frac{\partial n_{x}(z, t)}{\partial t}=-\frac{n_{x}(z, t)-\bar{n}_{x}}{T_{1}}- & \frac{n_{x}(z, t)-f n_{y}(z, t)}{T_{2}} \\
& -g^{\mathrm{TE}}(z, t) S^{\mathrm{TE}}(z, t) \tag{8}
\end{align*}
$$

and similarly for $n_{y}(z, t)$

$$
\begin{align*}
\frac{\partial n_{y}(z, t)}{\partial t}=-\frac{n_{y}(z, t)-\bar{n}_{y}}{T_{1}}- & \frac{f n_{y}(z, t)-n_{x}(z, t)}{T_{2}} \\
& -g^{\mathrm{TM}}(z, t) S^{\mathrm{TM}}(z, t) \tag{9}
\end{align*}
$$

where $\bar{n}_{x}$ and $\bar{n}_{y}$ are the respective equilibrium values determined by the applied pump current as will be discussed below, $T_{1}$ is the electron-hole recombination time, and $T_{2}$ is the
inter-hole relaxation time. The last terms in the right-hand sides of (8) and (9) account for the stimulated recombinations. It should be noted that the inter-hole relaxation time $T_{2}(\sim 100 \mathrm{fs})$ is much shorter than the electron hole recombination time $T_{1}$ ( $\sim 500 \mathrm{ps}$ ). Since we do not consider applications that involve ultrafast dynamics here, the two populations $n_{x}$ and $n_{y}$ will be clamped tightly together, i.e.,

$$
\begin{equation*}
n_{x}(z, t)=f n_{y}(z, t) \tag{10}
\end{equation*}
$$

In case of unstrained bulk material, the gain will be isotropic and $f=1$. In case of tensile strain, TM gain will be larger than TE, i.e., $f<1$. For the equilibrium values, consistent with (10), we can write

$$
\begin{equation*}
\bar{n}_{x}=\frac{\bar{n} f}{1+f}, \quad \bar{n}_{y}=\frac{\bar{n}}{1+f} \tag{11}
\end{equation*}
$$

where

$$
\begin{equation*}
\bar{n}=\frac{I}{e} T_{1} \tag{12}
\end{equation*}
$$

and $I$ is the electric current and $e$ is the electric unit charge. In (8)-(11), $f$ expresses the magnitude of the anisotropy.

Equations (1)-(12) form a closed set of equations. First, we will calculate the small-signal gain. To this end, we substitute the equilibrium values (11) in the gain expressions (7) and obtain the small-signal gain $g_{0}^{\mathrm{TE} / \mathrm{TM}}$

$$
\begin{align*}
& g_{0}^{\mathrm{TE}}=\xi^{\mathrm{TE}}\left[\left(\frac{1+2 f}{1+f}\right) \bar{n}-N_{0}\right] \\
& g_{0}^{\mathrm{TM}}=\xi^{\mathrm{TM}}\left[\left(\frac{2+f}{1+f}\right) \bar{n}-N_{0}\right] . \tag{13}
\end{align*}
$$

These expressions are quite general, but derived under the assumption of linear relationship between gain and carrier numbers. This implies that (13) can only be used in a small interval of the pump current. Within this given interval the parameter values occurring in (13) can be determined, but for different intervals, different parameter values will be obtained.

According to (1) and (2), the net amplifications by the SOA (in decibels), in absence of spatial inhomogeneity, are given by

$$
\begin{equation*}
4.343 \times\left(\Gamma^{\mathrm{TE}} g^{\mathrm{TE}}-\alpha_{\mathrm{int}}^{\mathrm{TE}}\right) \frac{L}{v_{g}^{\mathrm{TE}}}, \quad \text { for } \mathrm{TE} \tag{14}
\end{equation*}
$$

and

$$
\begin{equation*}
4.343 \times\left(\Gamma^{\mathrm{TM}} g^{\mathrm{TM}}-\alpha_{\mathrm{int}}^{\mathrm{TM}}\right) \frac{L}{v_{g}^{\mathrm{TM}}}, \quad \text { for } \mathrm{TM} \tag{15}
\end{equation*}
$$



Fig. 3. (a) Measured polarization-dependent small-signal gain for the TE mode and TM mode as a function of the injected current $I$. (b) Similar to (a), but now with a saturating control signal. The intensity of the control signal is 0.32 dBm .
where $L$ is the length of the SOA. The small-signal amplification can be obtained by replacing $g^{\mathrm{TE}}$ by $g_{0}^{\mathrm{TE}}$ and $g^{\mathrm{TM}}$ by $g_{0}^{\mathrm{TM}}$ in (14) and (15).

The experimental setup that is used to measure the polar-ization-dependent gain of the SOA is shown in Fig. 2. A laser source emits a continuous wave (CW) probe beam at a wavelength of 1552.60 nm . This probe beam is fed into the SOA via an attenuator and an isolator. The SOA was manufactured by JDS-Uniphase and employs a strained-bulk active region with a length of $800 \mu \mathrm{~m}$. An attenuator is used to assure the light that enters the SOA has a low intensity $(-15.24 \mathrm{dBm})$ so that the SOA is operated in the linear regime (with this, we mean that no gain saturation is introduced by the probe beam). The SOA can be saturated by a high-intensity CW-pump beam at a wavelength of 1550.90 nm that enters from the opposite direction. The SOA output is fed into a power meter via a circulator. A tuneable bandpass filter with a bandwidth of 2 nm is used to filter out the spontaneous emission that is produced by the SOA. The polarization controllers are used to adjust the polarization of the input signals (pump and probe) to the orientation of the SOA layers.

As a first experiment, the polarization-dependent gain is measured as a function of the injected current $I$ in the absence of a saturating control beam. This is done by adjusting the polarization of the small-signal probe beam in such a way that the minimum and maximum amplification is measured. The results are


Fig. 4. Computed SOA gain for the TE mode (solid line) and the TM mode (dashed line) as a function of the intensity of a saturating control signal. The SOA was pumped with 160 mA .
presented in Fig. 3(a), where the curve with the maximum amplification is attributed to the TE mode and the curve with minimum amplification is attributed to the TM mode. If we compensate for the coupling losses, estimated to be 5.6 dB (this includes two times $2.5-\mathrm{dB}$ facet losses and two times $0.3-\mathrm{dB}$ connector losses), it follows from Fig. 3(a) that for a current $I=160$ mA , the gain of the TE mode equals to 18.1 dB and that of the TM mode 13.6 dB . Moreover, if we use the following parameter values: $\alpha_{\mathrm{int}}^{\mathrm{TE}}=\alpha_{\mathrm{int}}^{\mathrm{TM}}=0.27 \mathrm{ps}^{-1}, f=0.5, N_{0}=10^{8}$, $T_{1}=500 \mathrm{ps}, e=1.610^{-19} \mathrm{C}, v_{g}^{\mathrm{TE}}=v_{g}^{\mathrm{TM}}=100 \mu \mathrm{~m} / \mathrm{ps}$, $\Gamma^{\mathrm{TE}}=0.2$, and $\Gamma^{\mathrm{TM}}=0.14$ [13], [14], then it follows from (14) and (15) that $\xi^{\mathrm{TE}}=7.010^{-9} \mathrm{ps}^{-1}$ and $\xi^{\mathrm{TM}}=6.510^{-9}$ $\mathrm{ps}^{-1}$.

If a saturating control beam is also injected into the SOA, the gain can be computed by using (7)-(9), (14), and (15). The optical power $P^{\mathrm{TE} / \mathrm{TM}}$ for each mode is related to the intensity $S^{\mathrm{TE} / \mathrm{TM}}$ according to

$$
\begin{equation*}
S^{\mathrm{TE} / \mathrm{TM}}=\frac{P^{\mathrm{TE} / \mathrm{TM}}}{\hbar \omega} \frac{L}{v_{g}^{\mathrm{TE} / \mathrm{TM}}} \tag{16}
\end{equation*}
$$

where $\hbar$ is Planck's constant and $\omega$ is the optical frequency. In Fig. 3(b), the saturated gain is plotted as a function of the injected current if a saturating pump signal with an intensity of 0.32 dBm is applied. The polarization of the pump beam was adjusted in such a way that maximum gain saturation for both the TE and TM modes was obtained. In Fig. 4, the computed gain saturation is presented for the two modes as a function of the injected optical power at a bias current of 160 mA , while it is assumed that $50 \%$ of the injected power is used to saturate the TE mode and the other $50 \%$ of the injected power is used to saturate the TM mode. If we correct for $2.8-\mathrm{dB}$ coupling losses of the pump beam, and if we assume $\hbar \omega=0.8 \mathrm{eV}$, it follows from (16) that under these circumstances, a pump beam with an intensity of 0.32 dBm leads to a saturated gain of 13.4 dB for the TE mode and 10.5 for the TM mode. This is in agreement with the experimental data that are presented in Fig. 3(b).

We have also compared the experimental gain saturation and the computed gain saturation for other intensities of the saturating control beam, and we find that the experimental results are in good agreement with the theoretical results. It should be remarked, however, that from an experimental point of view, it


Fig. 5. Schematic setup of a nonlinear polarization switch. PC: polarization controller. SOA: semiconductor optical amplifier. PBS: polarizing beam splitter.
is difficult to control the intensities of the light that is injected in each mode.

We have shown that our SOA model can accurately describe the polarization-dependent gain saturation. It should be noted, however, that the SOA parameters $N_{0}, T_{1}, \Gamma^{\mathrm{TE} / \mathrm{TM}}, \alpha_{\mathrm{int}}^{\mathrm{TE} / \mathrm{TM}}$, and $v_{g}^{\mathrm{TE} / \mathrm{TM}}$ cannot be estimated accurately. We solve this problem by compensating the combined uncertainties in these parameter values by assigning values to $f$ and $\xi^{\mathrm{TE} / \mathrm{TM}}$ in such a way that the (measured) fiber-to-fiber gain is reproduced. In the most simple approach, one would choose $\xi^{\mathrm{TE}}=\xi^{\mathrm{TM}}$, as this would be exact in the case of isotropic gain, so that $f$ can be estimated from the measured TE and TM gain curves by using (14) and (15). In this case, the polarization-dependent gain would be totally explained by the band-filling effects that are represented by the factor $f$. However, this leads to gain saturation that is not in agreement with experimental data. We have, therefore, chosen to allow for a small difference in the values for $\xi^{\mathrm{TE}}$ and $\xi^{\mathrm{TM}}$ (as this could be due to a small difference in effective transition strength). This approach leads to a gain saturation that is in good agreement with experimental data. The difficulties in estimating $f$ and $\xi^{\mathrm{TE} / \mathrm{TM}}$ may be inherent to our modeling the SOA strain in terms of a population imbalance factor $f$. In a more accurate-but also much more complicated-model, one can calculate the band structure and transition matrix elements in the presence of tensile strain and keep track of the different optical transitions involved as well as the relevant populations. This would, however, extend beyond the scope of the present approach.

## III. Nonlinear Polarization Switching

The principle of polarization-dependent SOA gain discussed in the previous section will now be applied to a nonlinear polarization switch (PSW) schematically indicated in Fig. 5. The PSW is made from two laser sources: a SOA, three polarization controllers, and a polarization beam splitter (PBS) [5]. The first laser (Laser 1) emits a CW probe beam at wavelength $\lambda_{1}$ that is fed into the SOA. The SOA output is sent into the PBS. One polarization controller $\left(\mathrm{PC}_{1}\right)$ is used to adjust the polarization direction of the input signal at approximately $45^{\circ}$ to the orientation of the SOA layers, while the second polarization controller $\left(\mathrm{PC}_{2}\right)$ adjusts the polarization of the (amplified) output light to the orientation of the PBS. The SOA gain can be saturated by injection of a high-intensity pump (control) signal produced by the second laser (Laser 2). The wavelength $\lambda_{2}$ of the pump beam should be distinguishable from the wavelength of


Fig. 6. Output of the setup of Fig. 5. The system is tuned in such a way that the maximum output intensity of the polarization switch is equal to the intensity of the control light that is required to suppress the output of the polarization switch. Horizontal axis: represents the switching intensity. Vertical axis: represents the output intensity of the polarization switch. Solid curve: experimental result. Dashed curve: theoretical result.
the probe beam if the two beams co-propagate. If the control light counter-propagates with the probe signal, the two wavelengths may be identical. The polarization of the light from Laser 2 is controlled by the third polarization controller $\left(\mathrm{PC}_{3}\right)$.

The solid curve in Fig. 6 shows the experimental PBS output as a function of the intensity of the saturating control light. The SOA used in this experiment was pumped with 162 mA of current. Fig. 6 clearly demonstrates that a control beam of sufficient intensity suppresses the output of the PSW. This effect is a consequence of the polarization-dependent gain saturation described in Section II. The gain saturation generally leads to different refractive-index changes for TE and TM, which results in a saturation-induced phase difference between these modes. If this phase difference is an odd multiple of $\pi$, the output from the PBS is suppressed, i.e., switched off.

In the experiment, the polarization direction of the input probe light is approximately at $45^{\circ}$ to the layers of the SOA, but not exactly. This is because our SOA had a polarization sensitivity of almost 4 dB at 1550 nm , implying a difference in the saturation properties of TE and TM modes also. The input angle is carefully adjusted to compensate for this, thus achieving more than $20-\mathrm{dB}$ switching contrast ratio.

The phase difference $\theta$ between the TE and TM modes can be computed from (1) and (2)

$$
\begin{equation*}
\theta=\phi^{\mathrm{TE}}-\phi^{\mathrm{TM}}=\frac{1}{2}\left(\frac{\alpha^{\mathrm{TE}} \Gamma^{\mathrm{TE}} g^{\mathrm{TE}}}{v_{g}^{\mathrm{TE}}}-\frac{\alpha^{\mathrm{TM}} \Gamma^{\mathrm{TM}} g^{\mathrm{TM}}}{v_{g}^{\mathrm{TM}}}\right) L \tag{17}
\end{equation*}
$$



Fig. 7. Configuration of the all-optical flip-flop based on two polarization switches. CW: Continuous wave. PSW: Polarization switch. PC: Polarization controller. SOA: Semiconductor optical amplifier. PBS: Polarization beam splitter. Mux: Optical multiplexer. $\mathrm{P}_{\text {out } 1}$ : the output of $\mathrm{PSW}_{1} . \mathrm{P}_{\text {out } 2}$ : the output of $\mathrm{PSW}_{2}$.
where spatial inhomogeneity is neglected altogether. Such effects can be taken into account, but then the propagation equation should be numerically integrated. In the cases considered here, (17) turns out to be an adequate approximation. The intensity $S_{\text {out }}$ of the light that outputs the PBS is given by

$$
\begin{equation*}
S_{\text {out }}=S^{\mathrm{TE}}+S^{\mathrm{TM}}+2 \sqrt{S^{\mathrm{TE}} S^{\mathrm{TM}}} \cos \theta \tag{18}
\end{equation*}
$$

where

$$
\begin{align*}
S^{\mathrm{TE}} & =S_{\mathrm{in}}^{\mathrm{TE}} e^{\left(\Gamma^{\mathrm{TE}} g^{\mathrm{TE}}-\alpha_{\mathrm{int}}^{\mathrm{TE}}\right)\left(L / v_{g}^{\mathrm{TE}}\right)} \\
S^{\mathrm{TM}} & =S_{\mathrm{in}}^{\mathrm{TM}} e^{\left(\Gamma^{\mathrm{TM}} g^{\mathrm{TM}}-\alpha_{\mathrm{int}}^{\mathrm{TM}}\right)\left(L / v_{g}^{\mathrm{TM}}\right)} \tag{19}
\end{align*}
$$

and $S_{\mathrm{in}}^{\mathrm{TE} / \mathrm{TM}}$ in (19) represent the intensities of the TE and TM components of the probe beam at the SOA input. The gains $g^{\mathrm{TE} / \mathrm{TM}}$ can be computed from (7) and (9). Once the gain for each mode is known, the phase difference can be computed by using (17).

If we use the SOA parameters that are presented in Section II, we can compute $S_{\text {out }}$ as a function of the intensity of a control beam by using (17)-(19). The result is shown by the dashed curve in Fig. 6 if $\alpha_{\mathrm{TE}}=\alpha_{\mathrm{TM}}=5$. It is clearly visible in Fig. 6 that our SOA model leads to results that are in excellent agreement with the experimental data. Note that curves in Fig. 6 are similar to the ones presented in [15], in which the suppressed output of an active Mach-Zehnder interferometer is discussed. This reflects that the nonlinear polarization switch operates in a similar fashion as a Mach-Zehnder interferometer switch, since in the PSW, the role of the different light paths is played by the different polarizations.

## IV. All-Optical Flip-Flop Based on Nonlinear PSWs

Similar to [15], an optical flip-flop can be realized by coupling two identical PSWs as shown in Fig. 7. The first PSW, hereafter to be called $\mathrm{PSW}_{1}$, outputs light that is injected into the second polarization switch (to be called $\mathrm{PSW}_{2}$ ) via the PBS. Hence, the output light from $\mathrm{PSW}_{1}$ acts as a saturating control signal that can suppress $\mathrm{PSW}_{2}$ and vice versa. The solid curve in Fig. 8 represents the intensity $\mathrm{P}_{\text {out } 1}$ of the light that outputs $\mathrm{PSW}_{1}$ as a function of the intensity $\mathrm{P}_{\text {out } 2}$ of the light that outputs $\mathrm{PSW}_{2}$ and saturates the SOA in $\mathrm{PSW}_{1}$. Conversely, the dashed curve in Fig. 8 represents the intensity $\mathrm{P}_{\text {out } 2}$ of the light


Fig. 8. Intensity $\mathrm{P}_{\text {out } 1}$ of the light that outputs $\mathrm{PSW}_{1}$ as a function of the intensity $\mathrm{P}_{\text {out } 2}$ of the light that outputs $\mathrm{PSW}_{2}$ (solid curve). Intensity $\mathrm{P}_{\text {out } 2}$ of the light that outputs $\mathrm{PSW}_{2}$ as a function of the intensity $\mathrm{P}_{\text {out } 1}$ of the light that outputs $\mathrm{PSW}_{1}$ (dashed curve). It is visible that the two curves are complementary. Both curves are experimental results.
that outputs $\mathrm{PSW}_{2}$ as a function of the amount of light $\mathrm{P}_{\text {out } 1}$ that outputs $\mathrm{PSW}_{1}$ and saturates the SOA in $\mathrm{PSW}_{2}$. Both curves in Fig. 8 are experimental results. They are obtained under the conditions that are presented later in this section. Since the polarization switches are identical, the solid curve is complementary to the dashed curve. At point A, $\mathrm{PSW}_{2}$ is suppressed and $\mathrm{PSW}_{1}$ is dominant while at Point B, $\mathrm{PSW}_{1}$ is suppressed and $\mathrm{PSW}_{2}$ is dominant. Point S is an unstable point [16].

The system of two coupled PSWs can function as an optical flip-flop as follows. The state of the flip-flop can be determined by observing the amount of light at the outputs of the PSW. In State 1, PSW 1 dominates and suppresses $\mathrm{PSW}_{2}$, while in State 2, $\mathrm{PSW}_{2}$ dominates and suppresses $\mathrm{PSW}_{1}$. To switch the flip-flop between the states, light can be injected in the PSW that dominates (that is the one injecting the most light into the other PSW) via the set state and reset ports. The injected light reduces the light exiting the dominant PSW, which allows the suppressed PSW to increase its light output and become the dominant switch.

The all-optical flip-flop is implemented as in Fig. 7. Lasers 1 and 2 emit CW light at wavelengths $\lambda_{1}=1549.32 \mathrm{~nm}$ and $\lambda_{2}=$ 1550.92 nm , respectively. However, it is not essential to bias the PSWs with light at different wavelengths. The output power is -3.34 dBm for Laser 1 and -3.05 dBm for Laser 2 . $\mathrm{SOA}_{1}$ is biased with 163.97 mA of current and $\mathrm{SOA}_{2}$ is biased with 161.86 mA of current. The PBS has four ports and an extinction ratio of $30 \mathrm{~dB} . \mathrm{PSW}_{1}$ and $\mathrm{PSW}_{2}$ are coupled to each other via the PBS.

The static operation of the flip-flop that is discussed in the previous section is presented in Fig. 8. The flip-flop operation is demonstrated by toggling the state of the flip-flop by injecting a regular sequence of optical pulses into the switch that was currently the master. These pulses had a wavelength of 1552.52 nm and duration of 150 ns . The pulses were injected in the master once every 1.85 ms through the set and reset port (see Fig. 7). Fig. 9 shows the oscilloscope traces of the optical output power of flip-flop for each state. The optical peak power for the set and reset pulses were -3.91 dBm and -4.35 dBm . In Fig. 9, regular toggling between flip-flop states every 1.85 microseconds can be observed. Furthermore, it is visible that the flip-flop state is stable in the time between the state changes. Also, the contrast


Fig. 9. Regular toggling between the two flip-flop states if, every 1.85 ms , a set or reset pulse is injected.


Fig. 10. Optical spectrum of the flip-flop output states. It can be observed that $20-\mathrm{dB}$ contrast between the states is obtained. On the left, the spectrum $\mathrm{PSW}_{1}$ dominates. On the right, the spectrum $\mathrm{PSW}_{2}$ dominates.
between States 1 and 2 was investigated by using a spectrum analyzer. The result is presented in Fig. 10. It turns out that the contrast ratio between the two states of the flip-flop is over 20 dB .

## V. Conclusions

We have presented a simple rate-equation model that is capable of describing the behavior of polarization switches based on nonlinear polarization rotation in strained bulk SOAs. This model is based on the assumption that TE and TM components of the light correspond to the two principle axes of the SOA while the carriers establish an indirect coupling between the components. The effect of tensile strain is accounted for by a population imbalance factor $f$ and a small difference in gain coefficients for TE and TM.

The polarization-dependent gain saturation of the SOA can be explained with our model. The TE and TM modes experience different refractive indexes, which leads to a phase difference between the two modes. The operation of a nonlinear PSW is based on this principle, in which the phase difference is used to suppress the output of the PSW. The nonlinear polarization switch turns out to behave similarly as a Mach-Zehnder interferometer, in which the roles of the different light paths are taken by the independently propagating TE and TM modes.

Finally, we present an all-optical flip-flop memory based on two coupled PSWs. The contrast ratio between output states of flip-flop is over 20 dB and the optical switching power is less than -3 dBm . The speed of this flip-flop is determined by the speed of the PSW and the propagation distance between two SOAs. In the experimental setup, approximately 12 m of fiber is used between the two SOAs, which implies that about at least 100 ns are required for the states of the flip-flop to change. However, integrated versions of the flip-flop could reduce the distance two SOAs to several millimeters. In this case, the speed
of flip-flop is dominated by the speed of the PSW. It has been demonstrated that the switches can operate at 10 GHz [5]; thus, we expect the presented flip-flop to reach at least similar speeds.

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