NUCLEOSYNTHESIS IN MASSIVE STARS WITH IMPROVED NUCLEAR AND STELLAR PHYSICS

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ABSTRACT

We present the first calculations to follow the evolution of all stable nuclei and their radioactive progenitors in stellar models computed from the onset of central hydrogen burning through explosion as Type II supernovae. Calculations are performed for Population I stars of 15, 19, 20, 21, and 25 M_{\odot} using the most recently available experimental and theoretical nuclear data, revised opacity tables, neutrino losses, and weak interaction rates and taking into account mass loss due to stellar winds. A novel "adaptive" reaction network is employed with a variable number of nuclei (adjusted each time step) ranging from ~700 on the main sequence to $\gtrsim 2200$ during the explosion. The network includes, at any given time, all relevant isotopes from hydrogen through polonium (Z = 84). Even the limited grid of stellar masses studied suggests that overall good agreement can be achieved with the solar abundances of nuclei between ¹⁶O and ⁹⁰Zr. Interesting discrepancies are seen in the 20 M_{\odot} model and (so far, only in that model) are a consequence of the merging of the oxygen, neon, and carbon shells about a day prior to core collapse. We find that, in some stars, most of the "*p*-process" nuclei can be produced in the convective oxygen-burning shell moments prior to collapse; in others, they are made only in the explosion. Serious deficiencies still exist in all cases for the *p*-process isotopes of Ru and Mo.

Subject headings: nuclear reactions, nucleosynthesis, abundances — stars: evolution — supernovae: general

On-line material: machine-readable tables

1. INTRODUCTION

The nucleosynthetic yields of massive stars are important to many areas of astronomical research. Besides the inherent interest in understanding our nuclear origins, the abundances made in supernovae are used to diagnose models for the explosion and as input to still grander models for the formation and chemical evolution of galaxies and the intergalactic medium. They are the target of X-ray observations of supernova remnants and gamma-ray studies of radioactivities in the interstellar medium. Some can be used as cosmochronometers, others power the light curves, and still others appear as anomalous abundances found in tiny meteoritic grains in our own solar system.

For these reasons, nucleosynthesis calculations have a long history and a sizable community that carries them out. Most recently, nucleosynthesis in massive stars has been studied by Woosley & Weaver (1995, hereafter WW95), Thielemann, Nomoto, & Hashimoto (1996), Limongi, Straniero, & Chieffi (2000), and others. With this paper, we embark on a new survey, similar to WW95, that will ultimately include stars of many masses and initial metallicities. The characteristics of this new study are improvements in the stellar physics (mass-loss rates, opacities, reaction network, etc.; § 2) and revisions to nuclear reaction rates (§ 3) that have occurred during the last eight years.

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This first paper particularly addresses recent improvements in nuclear physics. For elements heavier than about silicon, the nuclear level densities are sufficiently high (provided that the particle separation energies are not too small) that the statistical-or "Hauser-Feshbach"-model can be used. Here, in their maiden voyage, we use rates calculated using the NON-SMOKER code (Rauscher, Thielemann, & Kratz 1997; Rauscher & Thielemann 1998). The reaction library, from which the network is drawn, includes all nuclei from the proton drip line to the neutron drip line and elements up to and including the actinides (Rauscher & Thielemann 2000⁵). For elements lighter than silicon, where they have been measured, results are taken from the laboratory. Several different compilations are explored. The most critical choices are the rates for ${}^{12}C(\alpha, \gamma){}^{16}O, {}^{22}Ne(\alpha, n){}^{25}Mg$, and ²²Ne(α , γ)²⁶Mg. In order to facilitate comparison, we have chosen a constant value equal to 1.2 times that of Buchmann (1996) for the ${}^{12}C(\alpha, \gamma){}^{16}O$ rate in *all* our calculations. For our *standard* models (defined in \S 3.1) we further adopt the lower bound of Käppeler et al. (1994) for 22 Ne(α , n) 25 Mg (Hoffman, Woosley, & Weaver 2001). In future publications we will explore, in greater depth, the consequences of different choices for these rates [for ${}^{12}C(\alpha, \gamma){}^{16}O$, see also Weaver & Woosley 1993; M. M. Boyes, A. Heger, & S. E. Woosley 2002, in preparation].

A novel reaction network is employed, unprecedented in size for stellar evolution calculations. The network used by WW95, large in its day, had about 200 nuclides and extended only to germanium. Studies using reaction networks of over 5000 nuclei have been carried out for single zones or regions of stars in order to obtain the *r*-process (e.g., Cowan, Cameron, & Truran 1985; Freiburghaus et al.

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⁵ Also available at http://nucastro.org/reaclib.html.

1999; Kratz et al. 1993), but "kilonuclide" studies of nucleosynthesis in complete stellar models (typically of 1000 zones each for 20,000 time steps) have not been done before. We describe in § 2.2 a dynamically evolving network that adds and subtracts nuclides as appropriate during the star's life to ensure that all significant nuclear flows are contained. Our present survey uses a network that has the accuracy of a fixed network of 2500 isotopes.

Section 4 discusses aspects of the stellar evolution that are critical to the nucleosynthesis, and \S 5 gives the main results of our survey. We find overall good agreement of our nucleosynthesis calculations with solar abundances for intermediate-mass elements (oxygen through zinc) as well as the "weak component" of the s-process ($A \leq 90$), and most of the *p*-process isotopes. However, there is a systematic deficiency of *p*-process isotopes below $A \approx 125$ that is particularly acute for Mo and Ru and around $A \approx 150$. Possible explanations are discussed in § 5.5. We also find that the nucleosynthesis is at least as sensitive to the stellar model as to the nuclear physics and, in particular, find unusual results for a 20 M_{\odot} model (in the sense that the results differ greatly from both the Sun and those at either 19 or 21 M_{\odot}). This is because of the merging of convective oxygen, neon, and carbon shells that occurred well before collapse in that model and not in the others (\S 5).

2. STELLAR PHYSICS AND COMPUTATIONAL PROCEDURE

All stellar models were calculated using the implicit hydrodynamics package, KEPLER (Weaver, Zimmermann, & Woosley 1978; WW95), with several improvements to the physical modeling of stellar structure and to the nuclear reaction network (see also Heger et al. 2001; Hoffman et al. 2001; Rauscher et al. 2001). In the following, we discuss only those improvements. For further details on the basic approaches we refer the reader to the previous publications (e.g., see Weaver et al. 1978; Weaver & Woosley 1993; WW95).

2.1. New and Improved Physics since WW95

The most important change in stellar physics compared to WW95 is the inclusion of mass loss. The prescription employed (Nieuwenhuijzen & de Jager 1990) gives a massloss rate that is sensitive to surface temperature and luminosity. Operationally, the mass lost in each time step is subtracted from a stellar zone situated 0.01 M_{\odot} below the surface of the star, and the surface layers are automatically rezoned (dezoned) whenever necessary, while conserving mass, momentum, energy, and composition. The advection term for the enthalpy flux and the expansion term due to mass loss can be neglected in these outer layers since the energy input in the mass loss $(u\nabla\phi)$ is small compared to the luminosity. The total mass loss of our stars is dominated by the red supergiant phase and depends on the modeling of semiconvection and overshooting and on the ${}^{12}C(\alpha, \gamma){}^{16}O$ rate (M. M. Boyes et al. 2002, in preparation). We obtain final masses that lie between the "normal" and the "double" mass-loss rates of Schaller et al. (1992).

For temperatures below 10^8 K, the OPAL95 opacities are employed (Iglesias & Rogers 1996). In particular, these result in a better representation of the hydrogen envelope in the red giant stage where the "iron bump" in the opacities of Iglesias & Rogers (1996) is known to be important (e.g., Heger et al. 1997). Above 10^8 K, the opacity was the same as in WW95 (and Weaver et al. 1978).

Plasma neutrino losses were updated to use the rates by Itoh et al. (1996) and coding by F. Timmes (2000, private communication). Hydrogen burning and weak losses during this phase were updated as described in Heger, Langer, & Woosley (2000b). Weak rates and weak neutrino losses in the late evolution stages now use the rates of Langanke & Martínez-Pinedo (2000; see Heger et al. 2000a, 2001).

Convection is basically treated as presented in Weaver et al. (1978) and Weaver & Woosley (1993; see also Woosley, Heger, & Weaver 2002 for a recent summary). However, convective overshooting (on either side) is now suppressed for isolated convective zone interfaces to avoid a numerical instability present in the work of WW95. Changes to the nuclear reaction rates, both strong and weak, are discussed in § 3.

2.2. Dynamic Nuclear Reaction Network

As in WW95, two reaction networks are used. A small network directly coupled to the stellar model calculation provides the approximate nuclear energy generation rate (Weaver et al. 1978), i.e., is solved implicitly with the Newton-Raphson solver for each time step in each zone. A larger one is used to track the nucleosynthesis. This smaller network is essentially the same as in WW95 and Weaver et al. (1978), but with updated nuclear rates as described in the following sections. For a study of small versus large networks and their ability to accurately and efficiently provide input values of the nuclear energy generation rate during advance stages of stellar evolution, see Timmes, Hoffman, & Woosley (2000).

The nucleosynthesis is coupled to convection in an "operator split" mode. At the end of each time step for the evolutionary model, the large reaction network is called, for the existing conditions (temperature and density), and the chemical species are diffusively mixed. To save computer time, the composition is not updated in zones where the temperature is too low for any nuclear activity during the previous time step, although every zone participates in convective mixing, where appropriate, every time step.

One of the major improvements over WW95 and other stellar models is that, for the first time, the synthesis of all nuclides of any appreciable abundance is followed simultaneously in an *adaptive network*. Using a library containing rate information for 4679 isotopes from hydrogen to astatine, the "adaptive" network automatically adjusts its size to accommodate the current nuclear flows. This means that the constitution of the network evolves to accommodate the most extreme thermodynamic conditions present anywhere in the model. If the mass fraction of an isotope exceeds a parameter, here 10^{-18} , anywhere in the star, the neighboring isotopes, and all to which that species might decay, are added. Similarly, if the abundance of an isotope drops below 10^{-24} , it is removed (unless it is along the decay chain of an abundant nucleus). Because different zones may become convectively coupled at unpredictable times, the same network must be used throughout the star. The network includes all strong reactions involving nucleons, α particles, and photons plus a few "special" reactions for light isotopes (like the triple- α process, ${}^{12}C + {}^{12}C$, etc.; for details see WW95), as well as all weak interactions: electron

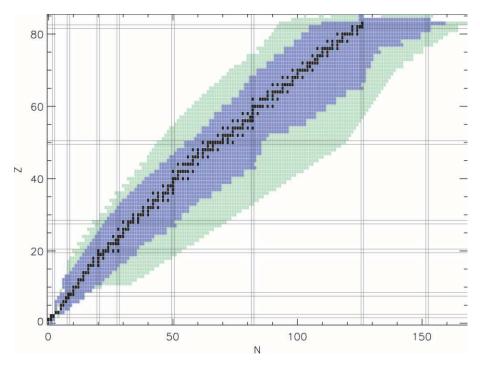


FIG. 1.—Isotopes in our database (green), used by model S15 (blue) and stable/long-lived isotopes (black)

capture, positron decay, and β -decay. The network is solved implicitly using a sparse matrix inverter (Timmes, Woosley, & Weaver 1995).

For our 15 M_{\odot} star, for example, the network initially contained 645 isotopes during hydrogen burning, including 283 stable or long-lived species (like ⁴⁰K or ¹⁸⁰Ta). This number grew to \gtrsim 740 isotopes at the end of central helium burning (to accommodate the *s*-process), \gtrsim 850 during carbon (shell) burning, \gtrsim 1050 during oxygen burning, \gtrsim 1230 during oxygen shell burning, and \gtrsim 1400 at the presupernova stage. When the supernova shock hit the base of the helium shell, causing a weak *r*-process, the network reached its maximum size, \gtrsim 2200. In total, 2435 different isotopes were included at one time or another. A network plot is shown in Figure 1.

The major limitation of this network is that it purposefully does not include elements beyond astatine, i.e., the heavy *r*-process and fission cycling could not be followed. Given the current uncertainties in the explosion mechanism and our simplified treatment, a description of the highentropy zones close to the proto-neutron star is beyond the scope of this paper. Thus, we did not calculate the *r*-process that might occur in the neutrino wind (Woosley et al. 1994). Another limitation in the current implementation of the network is that it only includes one state per isotope, which limits its accuracy for a few isotopes like ²⁶Al and ¹⁸⁰Ta.

3. NUCLEAR PHYSICS

Since 1993, when the nuclear physics used in WW95 was "frozen," there have been numerous revisions to nuclear reaction rates. In this work we are presenting our choice of a thoroughly updated standard rate set, including most recent experimental data and theoretical results. Numerically, the greatest fraction of nuclear information is theoretical, coming from a statistical model calculation (Rauscher & Thielemann 2000), described in § 3.3. These theoretical rates are supplemented by experimental values where they are known. Details are discussed in the following sections and the experimental rates employed are summarized in Table 1. The table is truncated at ⁴²Ca because above that, with the few exceptions indicated, all rates are from either Bao et al. (2000) for (n, γ) reactions (see Table 5 for a listing of these nuclei) or Rauscher & Thielemann (2000). The weak rates used here are discussed in § 3.4.

3.1. Experimental Rates below Silicon

Nuclear reactions involving elements lighter than silicon are particularly important for both nucleosynthesis and determining the stellar structure. Our standard set of lightelement reaction rates begins with Caughlan & Fowler (1988) as updated by Hoffman et al. (2001) and Iliadis et al. (2001). Further minor modifications were made to the rates ¹H(n, γ)D and ³He(n, γ)⁴He (Thielemann et al. 1995⁶). Table 1 gives the sources of all charged-particle reaction rates not taken from Rauscher & Thielemann (2000). The proper references can be found in Table 2.

Some important rates, e.g., those of Iliadis et al. (2001), have been given by these authors in tabular form and not as fitted functions of temperature. In Appendix A we describe a novel procedure that we shall follow for all such tabulations in the future and that we recommend to the community. The bulk of the temperature sensitivity is extracted from the rate using a simple fitting function that does *not* by itself give the necessary accuracy across the temperature grid. The ratios of the actual rate to the fitting function are then carried as a table in the computer and can be interpolated much more accurately than the rate itself.

⁶ Available at http://ie.lbl.gov/astro/friedel.html.

 TABLE 1

 Experimental Reaction Rate Reference Matrix

^{A}Z	$(n,\gamma)^{A+1}Z$	$(p,n)^A Z + 1$	$(p,\gamma)^{A+1}Z+1$	$(\alpha, p)^{A+3}Z + 1$	$(\alpha, n)^{A+3}Z + 2$	$(\alpha,\gamma)^{A+4}Z+2$
¹ H	WIES ^a					
² H	WIES ^a		CF88 ^{a,b}			CF88 ^{a,b}
³ H		CF88 ^a	CF88 ^a		CF88 ^a	CF88 ^{a,b}
³ He	WIES ^a			CF88 ^{a,b}		CF88 ^{a,b}
⁶ Li			CF88 ^{a,b}	CF88 ^{a,b}		CF88 ^a
⁷ Li	RA94 ^a	CF88 ^a	CF88 ^{a,b}		CF88 ^{a,b}	CF88 ^{a,b}
⁸ Li	WIES ^a				RA94 ^a	FKTH
⁷ Be			CF88 ^{a,b}	CF88 ^{a,b}		CF88 ^{a,b}
⁹ Be	WIES ^a	CF88 ^{a,b}	CF88 ^{a,b}		WB94 ^{a,b}	
⁸ B			WIES ^a	CF88 ^a		
¹⁰ B	WIESa		CF88 ^{a,b}		CF88 ^a	
¹¹ B	RA94 ^a	CF88 ^{a,b}	CF88 ^{a,b}	CF88 ^a	CF88 ^a	
¹¹ C	RA94 ^a		CF88 ^a	CF88 ^{a,b}		
¹² C	BAALa		FCZ2 ^{a,b}	HFCZ ^{a,b}	HFCZ ^a	BU96 ^a
¹³ C	RA94 ^a	FCZ2 ^{a,b}	CF88 ^{a,b}		FCZ2 ^{a,b}	RATH
¹⁴ C	RA94 ^a	CF88 ^a	CF88 ^a		RA94 ^a	CF88 ^a
¹³ N	WIES ^a		KL93 ^{a,b}	HFCZ ^a		
¹⁴ N	WIES ^a	FCZ2 ^{a,b}	CF88 ^{a,b}	LA90 ^{a,b}	CF88 ^{a,b}	FCZ2 ^{a,b}
¹⁵ N	WIES ^a	CF88 ^{a,b}	FCZ2 ^{a,b}	CF88 ^{a,b}	CF88 ^a	CF88 ^{a,b}
¹⁴ O				CF88 ^a	RATH	CF88 ^a
¹⁵ O				WK82 ^a		CF88 ^a
¹⁶ O	BAAL ^a		FCZ2 ^{a,b}	HFCZ ^{a,b}	RATH	CF88 ^{a,b}
¹⁷ O	RA94 ^a	FKTH	LA90 ^{a,b}		FCZ2 ^{a,b}	FCZ2 ^a
¹⁸ O	RA94 ^a	FKTH	CF88 ^{a,b}		CF88 ^{a,b}	GB94 ^{a,b}
¹⁷ F	FKTH		WK82 ^a	CF88 ^{a,b}		
¹⁸ F	FKTH		WK82 ^a			
¹⁹ F	BAAL ^a	CF88 ^{a,b}	FCZ2 ^{a,b}	CF88 ^a	CF88 ^a	
¹⁹ Ne	RATH	RATH	CF88 ^a	RATH	RATH	RATH
²⁰ Ne	WM88 ^a	RATH	ID01 ^{a,b}	ID01 ^{a,b}	RATH	RTGW ^b
²¹ Ne	BAAL ^a	RATH	ID01 ^{a,b}	RATH	FCZ2 ^{a,b}	HFCZ ^a
²² Ne	BAAL ^a	CF88 ^a	ID01 ^{a,b}	RATH	KA94 ^{a,b}	KA94 ^{a,b}
²⁰ Na	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²¹ Na	RATH	RATH	ID01 ^{a,b}	CF88 ^{a,b}	RATH	RATH
²² Na	RATH	RATH	ID01 ^{a,b}	RATH	RATH	RATH
²³ Na	BAAL ^a	CF88 ^{a,b}	ID01 ^{a,b}	RATH	RATH ^b	RATH
²² Mg	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²³ Mg	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²⁴ Mg	BAAL ^a	RATH	ID01 ^{a,b}	ID01 ^{a,b}	RATH	RTGW
²⁵ Mg	BAAL ^a	RATH	ID01 ^{a,b}	CF88 ^a	FCZ2 ^{a,b}	HFCZ ^a
²⁶ Mg	BAAL ^a	RATH	ID01 ^{a,b}	RATH	FCZ2 ^{a,b}	HFCZ ^a
²³ A1	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²⁴ A1	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²⁵ A1	RATH	RATH	ID01 ^{a,b}	RATH	RATH	RATH
²⁶ A1	RATH	RATH	ID01 ^{a,b}	RATH	RATH	RATH
²⁷ A1	BAAL ^a	RATH	ID01 ^{a,b}	RATH	CF88 ^{a,b}	RATH
²⁶ Si	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²⁷ Si	RATH	RATH	ID01 ^{a,b}	RATH	RATH	RATH
²⁸ Si	BAAL ^a	RATH	ID01 ^{a,b}	ID01 ^a	RATH	RTGW
²⁹ Si	BAAL ^a	RATH	ID01 ^{a,b}	RATH	RATH	RATH
³⁰ Si	BAAL ^a	RATH	ID01 ^{a,b}	RATH	RATH	RATH
²⁷ P	RATH	RATH	ID01 ^a	RATH	RATH	RATH
²⁸ P	RATH	RATH	ID01	RATH	RATH	RATH
²⁹ P	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³⁰ P	RATH	RATH	ID01	RATH	RATH	RATH
³¹ P	BAAL ^a	RATH	ID01 ^a	RATH	RATH	RATH
³⁰ S	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³¹ S	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³² S	BAAL ^a	RATH	ID01 ^a	RATH	RATH	RTGW
³³ S	BAAL ^a	RATH	ID01	RATH	RATH	RATH
³⁴ S	BAALa	RATH	ID01	TS92 ^a	TS92 ^a	TS92 ^a
³¹ C1	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³² Cl	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³³ Cl	RATH	RATH	ID01 ID01	RATH	RATH	RATH
³⁴ Cl	RATH	RATH	ID01 ID01	RATH	RATH	RATH
³⁵ Cl	BAAL ^a	RATH	ID01 ID01 ^a	RATH	RATH	RATH
CI	DAAL	1111	11001	KA111	1/111	111

^{A}Z	$(n,\gamma)^{A+1}Z$	$(p,n)^A Z + 1$	$(p,\gamma)^{A+1}Z + 1$	$(\alpha, p)^{A+3}Z + 1$	$(\alpha, n)^{A+3}Z + 2$	$(\alpha,\gamma)^{A+4}Z+2$
³⁴ Ar	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³⁵ Ar	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³⁶ Ar	BAAL	RATH	ID01 ^a	ID01	RATH	RTGW
³⁸ Ar	BAAL	RATH	RATH	SM86 ^a	SM86 ^a	RATH
³⁵ K	RATH	RATH	ID01 ^a	RATH	RATH	RATH
³⁶ K	RATH	RATH	ID01	RATH	RATH	RATH
³⁷ K	RATH	RATH	ID01	RATH	RATH	RATH
³⁸ K	RATH	RATH	ID01	RATH	RATH	RATH
³⁹ K	BAAL ^a	RATH	ID01	RATH	RATH	RATH
⁴⁰ K	BAAL	RATH	RATH	RATH	RATH	RATH
⁴¹ K	BAAL ^a	RATH	RATH	SM91 ^a	RATH	RATH
³⁹ Ca	RATH	RATH	ID01 ^a	RATH	RATH	RATH
⁴⁰ Ca	BAAL ^a	RATH	ID01 ^a	RATH	RATH	RTGW
⁴² Ca	BAAL ^a	RATH	RATH	MK85 ^a	RATH	MK85 ^a
⁴⁵ Sc	BAAL ^a	RATH	RATH	HT89 ^a	HT89 ^a	RATH
⁴⁸ Ti	BAAL ^a	RATH	RATH	MT92 ^a	RATH	RATH
⁷⁰ Ge	BAAL ^a	RATH	RATH	THIS	THIS	FU96 ^a
¹⁴⁴ Sm	BAAL ^a	RATH	RATH	THIS	THIS	SO98 ^a

TABLE 1—Continued

NOTE.—Identification labels are explained in Table 2. Only those targets are given for which there are experimental data beyond Bao et al. 2000. The full rate set is constructed by combination of theoretical rates (Rauscher & Thielemann 2000) with the data given in this table and Table 5. Ellipses indicate that no rate is available for the given channel.

^a The reaction rate is based on experiment.

^b The reaction rate was varied in the calculations (see the text).

Besides models that used this standard set of nuclear physics (the "S"-series of models; for 15, 19, 20, 21, and 25 M_{\odot}), we also present calculations using two other rate sets. This was done to facilitate the comparison of different choices of reaction rates in otherwise identical stellar models. One other set was the NACRE compilation of charged-particle rates from Angulo et al. (1999; model series "N"; for 15, 20, and 25 M_{\odot}). For one 25 M_{\odot} star, we used the network and rates of Hoffman et al. (2001). Since that work only included nuclear data up to about mass 110, the recalculation here used a similar static network of 477 nuclides (set "H"; for 25 M_{\odot} only).

3.1.1. ${}^{12}C(\alpha, \gamma){}^{16}O$

Of utmost importance for nucleosynthesis is the rate adopted for ${}^{12}C(\alpha, \gamma){}^{16}O$. The same value was used in all studies reported in this paper (sets S, N, H) since variation of this single rate would alter the stellar model and obscure the sensitivity to the other nuclear physics. The rate previously used in WW95 and Hoffman et al. (2001) was that of Caughlan & Fowler (1988) multiplied by 1.7. Here the more recent evaluation of Buchmann (1996; L. Buchmann 2000, private communication) was used as a basis for the temperature dependence, but the overall rate was multiplied by a factor of 1.2 to bring the recommended value S(300) = 146keV barn into better accord with our standard S(300) = 170 keV barn (Weaver & Woosley 1993). This value and temperature dependence is also consistent with recent measurements by Kunz et al. (2001, 2002).

3.1.2. ²²Ne(α , *n*)²⁵Mg and ²²Ne(α , γ)²⁶Mg

The reaction ${}^{22}\text{Ne}(\alpha, n){}^{25}\text{Mg}$, acting in competition with ${}^{22}\text{Ne}(\alpha, \gamma){}^{26}\text{Mg}$, is critical for determining the strength of the helium-burning *s*-process in massive stars (e.g., Käppeler et al. 1994). Here, while experimenting with several choices, the standard set employed is the lower limit of Käp-

peler et al. (1994; the same rates as used by Hoffman et al. 2001). This choice is in reasonable agreement with more recent work by Jaeger et al. (2001). Following an early recommendation by M. Wiescher (1995, private communication), only the resonance at 828 keV was considered in the rate for ${}^{22}Ne(\alpha, n){}^{25}Mg$ and the resonance at 633 keV was ignored. Furthermore, the 828 keV resonance itself was given a strength equal to its 1 σ lower limit, 164 μ eV. The rate for 22 Ne $(\alpha, \gamma)^{26}$ Mg was that recommended by Käppeler et al., but with the strength for the 633 keV resonance multiplied by 0.5. The modified Käppeler et al. (1994) rates were merged with the rate given by Caughlan & Fowler (1988), which was used for temperatures $T_9 \ge 0.6$. For model series N, we used the same $^{\hat{1}2}C(\alpha, \gamma)$ rate (1.2 times that of L. Buchmann 2000, private communication) but the recommended values for 22 Ne $(\alpha, \gamma)^{26}$ Mg, 22 Ne $(\alpha, n)^{25}$ Mg, and all other rates provided by NACRE.

3.2. Experimental Rates above Silicon

Additional experimental rates for nuclei heavier than silicon are given in Table 1. These are largely drawn from R. D. Hoffman & S. E. Woosley (1992, unpublished).⁷ The entries in Table 1 are referenced in Table 2.

Recent measurements of the reactions ${}^{70}\text{Ge}(\alpha, \gamma){}^{74}\text{Se}$ (Fülöp et al. 1996) and ${}^{144}\text{Sm}(\alpha, \gamma){}^{148}\text{Gd}$ (Somorjai et al. 1998) are of great importance for the γ -process yields. Especially the predictions of the latter reaction were found to be very sensitive to the optical model α potential used (Woosley & Howard 1990; Rauscher, Thielemann, & Oberhummer 1995). For our rate library, the resulting experimental rates of both reactions were fitted to the format described in Rauscher & Thielemann (2000). The experimental information was also used to recalculate other rates

⁷ See also http://ie.lbl.gov/astro/hw92_1.html.

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TABLE 2 Reference List for the Reaction Rate Reference Matrix (Table 1)

Label	Reference	Comment
BAAL	Bao et al. 2000	See Table 5
BU96	Buchmann 1996	
CF88	Caughlan & Fowler 1988	
EC95	El Eid & Champagne 1995	
FCZ2	Fowler, Caughlan, & Zimmermann 1975	
FKTH	Thielemann, Arnould, & Truran 1987; Thielemann et al. 1995	
FU96	Fülöp et al. 1996	
GB94	Giessen et al. 1994	
GW89	Görres, Wiescher, & Rolfs 1989	
HFCZ	Harris et al. 1983	
HT89	Hansper et al. 1989	
ID01	Iliadis et al. 2001	
KA94	Käppeler et al. 1994	Modified (see text)
KL93	Kiener et al. 1993	
LA90	Landré et al. 1990	
MK85	Mitchell et al. 1985	
MT92	Morton et al. 1992	
RA94	Rauscher et al. 1994	
RTGW	Rauscher et al. 2000	For implementation, see Table 4
SO98	Somorjai et al. 1998	
THIS	This paper	See Table 3
TS92	Scott et al. 1992	
SM86	Sevior et al. 1986	
SM91	Scott et al. 1991	
WB94	Wrean, Brune, & Kavanagh 1994	
WFHZ	Woosley et al. 1978	
WIES	M. Wiescher 1992, private communication	See also Thielemann et al. 1995
WK82	Wiescher & Kettner 1982	
WM88	Winters & Macklin 1988	

involving the same α potentials. See § 3.3 for a further discussion.

3.3. Hauser-Feshbach Rates

For those cases in which experimental information was lacking and the level density was sufficiently high (typically A > 24) we employed the Hauser-Feshbach rates obtained using the NON-SMOKER code (Rauscher et al. 1997; Rauscher & Thielemann 1998). A library of theoretical reaction rates calculated with this code and fitted to an analytical function-ready to be incorporated into stellar model codes-was published recently, in the following (and in Table 1) referred to as RATH (Rauscher & Thielemann 2000, 2001). It includes binary reaction rates involving nucleons, α -particles, and photons interacting with all possible targets from neon to bismuth and all isotopes of these elements from the proton to neutron drip lines. It is thus the most extensive published library of theoretical reaction rates to date. For the network described here, we utilized the rates based on the FRDM set as these provide the most reliable description around the valley of stability.

Partition functions were also taken from Rauscher & Thielemann (2000) but were converted to the format defined in Holmes et al. (1976) to be used in KEPLER. This was achieved by fitting them with the appropriate functions. Low-lying nuclear levels had to be used for a few cases, and in such a case the same information as for the NON-SMOKER calculation was utilized (Rauscher & Thielemann 2001).

Recent investigations underline the fact that the α +nucleus optical potential for intermediate and heavy tar-

gets is not well understood at astrophysically relevant energies. Although α capture itself will be negligible for highly charged nuclei, the optical potential still is a necessary ingredient to determine the reverse (γ, α) reaction that is important in the γ -process (Woosley & Howard 1990; Rauscher et al. 1995). Two α capture reactions have been studied experimentally close to the relevant energy range. While the reaction ${}^{70}\text{Ge}(\alpha, \gamma){}^{74}\text{Se}$ (Fülöp et al. 1996) was essentially well predicted by theory and needed only a small adjustment of the optical potential, ${}^{144}\text{Sm}(\alpha, \gamma){}^{148}\text{Gd}$ exhibited strong deviations from previous estimates (Somorjai et al. 1998). As stated above, the experimental rates were implemented in RATH format in our rate library. Moreover, for reasons of consistency, all reactions involving the channels $\alpha + {}^{70}\text{Ge}$ and $\alpha + {}^{144}$ Sm were recalculated with the statistical model code NON-SMOKER, utilizing the optical potentials derived from the capture data (Somorjai et al. 1998). The resulting fit parameters in RATH format are given in Table 3.

Of special interest are α -capture reactions on self-conjugate (N = Z) target nuclei. The probabilities for these reactions are suppressed by isospin effects and require special treatment in any theoretical model. Capture data are scarce, even for lighter nuclei. Recently, Rauscher et al. (2000) published a semiempirical evaluation of resonance data [i.e., α resonances taken not only from (α , γ) reactions but also from other approaches] and compared it to predictions made with the code NON-SMOKER, which includes an improved treatment of the isospin suppression effect (Rauscher & Thielemann 1998). Reasonable agreement was found around $T_9 = 1-2$. At lower temperatures the statisti-

TABLE 3 Fit Parameters for Reactions Including the α +⁷⁰Ge and α +¹⁴⁴Sm Channels

Reaction	a_0	a_1	<i>a</i> ₂	<i>a</i> ₃	a_4	<i>a</i> ₅	a_6
70 Ge $(\alpha, \gamma)^{74}$ Se	-9.051749E02	2.096414E01	-2.210416E03	3.222456E03	-1.757347E02	9.295969E00	-1.599497E03
144 Sm (α, γ) 144 Gd	-9.547989E02	5.832285E00	-4.444873E03	5.555737E03	-2.560688E02	1.178841E01	-3.015931E03
73 As(p, α) 70 Ge	1.513141E02	-9.065257E00	3.503307E02	-5.256190E02	2.489691E01	-1.153807E00	2.762916E02
147 Eu(<i>p</i> , α) 144 Sm	-3.239141E02	-7.576453E00	-3.349700E02	6.806995E02	-4.521575E01	2.685919E00	-2.840773E02
73 Se $(n, \alpha)^{70}$ Ge	2.750996E01	-1.475808E-01	1.093870E01	-2.401239E01	1.486014E00	-3.967125E-02	1.028549E01
147 Gd $(n, \alpha)^{144}$ Sm	-1.203181E01	1.696984E-01	-1.675541E01	4.310292E01	-3.403980E00	3.122087E-01	-1.666362E01

NOTE.—See Rauscher & Thielemann 2000 for the definition of the coefficients. The reverse rates can be derived as explained in Rauscher & Thielemann 2000, 2001.

cal model either was not applicable or had problems with the prediction of the optical α potential (similar as discussed above), depending on the considered reaction. Since we need a reliable rate across the whole temperature range, a mixed approach was chosen: below a certain temperature T_{match} the contributions of single resonances—taken from Rauscher et al. (2000)—are added, and above T_{match} the statistical model rate renormalized to the experimental value at T_{match} is used. Table 4 lists the parameters and temperatures.

Also important are the rates for neutron capture. These directly affect both the neutron budget (acting as neutron "poisons") and the abundance of all s-process isotopes, including many species below the iron group (see Table 3 of Woosley et al. 2002). Where available, the theoretical rates of RATH were supplemented by experiment using the Bao et al. (2000) compilation of recommended neutron capture cross sections. Because only 30 keV Maxwellian averaged cross sections (MACSs) are given in that reference, we renormalized the fits given in RATH in order to obtain the same MACS values at 30 keV, thus maintaining the (weak) temperature dependence of the theoretical rates. The normalization factors are given in Table 5. Both forward and reverse rates of RATH are multiplied by the same factor. For targets below Ne, for which statistical model calculations cannot be applied with any accuracy, a 1/v dependence of the cross section-leading to a constant rate-was assumed, unless other experimental information was available.

3.4. Weak Interactions

The experimental β^{-} , β^{+} , and α -decay rates of Tuli et al. (1995; calculated from the laboratory ground-state half-

TABLE 4 Rates for α Capture Reactions on Self-conjugated Targets

Reaction	T _{match}	a_0^{renorm}
20 Ne(α, γ) ²⁴ Mg	3.0	$1.333837363 \times 10^{2}$
24 Mg(α, γ) ²⁸ Si	2.0	$1.428649975 imes 10^2$
28 Si $(\alpha, \gamma)^{32}$ S	3.0	$9.623587 imes 10^{1}$
${}^{32}S(\alpha, \gamma){}^{36}Ar$	0.0	$-1.915768 imes 10^{2}$
36 Ar(α, γ) 40 Ca	0.0	$-1.289706 imes 10^{2}$
40 Ca(α, γ) ⁴⁴ Ti	0.0	$-7.490256 imes 10^{2}$

NOTE.—For $T_9 < T_{\text{match}}$ a sum of resonances (taken from Rauscher et al. 2000) was used; for $T_9 \ge T_{\text{match}}$ a renormalized RATH rate was used with the new parameter $a_0 = a_0^{\text{renorm}}$ (the reverse rate has to be renormalized by the same factor). life) and their respective branching ratios were implemented. Where feasible, a temperature-dependent weak rate was coded that couples the ground state to a shorter lived excited state (both assumed to be in thermal equilibrium; Clayton 1968). Further experimental β^- -decay rates were taken from K.-L. Kratz et al. (1996, private communication; see also Möller, Nix, & Kratz 1997). For all other targets, we used the theoretical β^- - and β^+ -decay rates of Möller et al. (1997). As a special case, we implemented a temperature-dependent ^{180m}Ta decay rate (Belic et al. 2000).

Usually, the ground-state rates are a lower bound to the actual weak decay rates. Where fitted functions are available, we also utilize temperature- and density-dependent weak rates (Fuller, Fowler, & Newman 1980, 1982a, 1982b, 1985) accounting for a continuum of excited states. An important change of the weak interaction rates for $45 \le A \le 65$ is brought about by the recent work of Langanke & Martínez-Pinedo (2000). Where information is available, we use Langanke & Martinez-Pinedo (2000) rates in preference to Fuller et al. Their inclusion leads to interesting changes in the presupernova structure (see § 4.1), but not so much in the abundances outside the iron core.

Neutrino losses are a critical aspect of stellar evolution in massive stars beginning with carbon burning. The dominant losses before silicon burning are due to thermal processes (chiefly pair annihilation), which provide a loss term that is very roughly proportional to T^9 in the range of interest for advanced burning stages (Clayton 1968). This temperature sensitivity, combined with the need to burn heavier fuels at higher temperatures to surmount the increasing charge barriers, is what leads to the rapid decrease in lifetime to burn a given fuel, with obvious consequences for nucleosynthesis. We include the latest treatment (Itoh et al. 1996).

The neutrino flux of a core-collapse supernova is high enough to contribute to the nucleosynthesis of certain rare elements and isotopes. In this so-called ν -process, inelastic neutral-current scattering of a neutrino leads to the formation of an excited daughter nuclide, which then decays by particle emission. Rare isotopes with highly abundant "neighbors" (or neighbors of their radioactive progenitors) can be significantly produced by this process. As previously used by WW95, we adopt the rates of Woosley et al. (1990).

4. STELLAR EVOLUTION

4.1. Presupernova Evolution

Table 6 summarizes the presupernova properties of the new models. The helium, carbon-oxygen, and neon-oxygen cores are defined as the enclosed mass where hydrogen,

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TABLE 5

Renormalization Factors $f = r_{\text{exp}}/r_{\text{theory}}$ of the Theoretical (n, γ) Rates of Rauscher & Thielemann (2000) in Order to Yield a 30 keV Maxwell-averaged Cross Section Consistent with Bao et al. (2000)

		MAXWELL-AVERAGED CROSS SECTION CONSISTENT WITH DAO ET AL. (2000)								
Target	f	Target	f	Target f	Target	f	Target f	Target f	Target	f
²⁰ Ne	0.072	⁵⁴ Fe	0.594	⁸⁶ Rb 0.428	¹¹² Cd	1.053	¹³⁵ Ba 0.918	¹⁵⁶ Gd 1.183	¹⁸² W	0.680
²¹ Ne	0.332	⁵⁵ Fe	0.895	⁸⁷ Rb 0.302	¹¹³ Cd	1.232	¹³⁶ Ba 0.596	¹⁵⁷ Gd 1.122	¹⁸³ W	0.746
²² Ne	0.132	⁵⁶ Fe	0.447	⁸⁴ Sr 0.924	¹¹⁴ Cd	0.894	¹³⁷ Ba 0.647	¹⁵⁸ Gd 1.145	¹⁸⁴ W	0.894
²³ Na	0.697	⁵⁷ Fe	1.186	⁸⁶ Sr 0.305	¹¹⁵ Cd	0.667	¹³⁸ Ba 0.696	¹⁶⁰ Gd 0.758	¹⁸⁵ W	1.369
^{24}Mg	0.965	⁵⁸ Fe	0.944	⁸⁷ Sr 0.278		0.656	¹³⁹ La 0.514	¹⁵⁹ Tb 1.091	¹⁸⁶ W	1.221
²⁵ Mg	0.777	⁵⁹ Co	0.740	⁸⁸ Sr 0.402	¹¹³ In	0.659	¹³² Ce 0.913	¹⁶⁰ Tb 1.204	¹⁸⁵ Re	1.432
²⁶ Mg	0.075	⁵⁸ Ni	0.811	⁸⁹ Sr 0.406	¹¹⁴ In	0.800	¹³³ Ce 0.616	¹⁵⁶ Dy 1.342	¹⁸⁶ Re	1.080
²⁷ A1	0.630	⁵⁹ Ni	0.940	⁸⁹ Y 0.214		0.709	¹³⁴ Ce 0.787	¹⁵⁸ Dy 0.899	¹⁸⁷ Re	1.443
²⁸ Si	0.529	⁶⁰ Ni	0.902	⁹⁰ Zr 0.420		0.543	¹³⁵ Ce 0.621	¹⁶⁰ Dy 1.386	¹⁸⁴ Os	0.868
²⁹ Si	0.895	⁶¹ Ni	1.136	⁹¹ Zr 0.386		0.490	¹³⁶ Ce 0.547	¹⁶¹ Dy 1.200	¹⁸⁶ Os	0.676
³⁰ Si	3.218	⁶² Ni	0.650	⁹² Zr 0.477		0.648	¹³⁷ Ce 0.685	¹⁶² Dy 0.991	¹⁸⁷ Os	0.874
³¹ P	0.156	⁶³ Ni	0.873	⁹³ Zr 0.501		0.531	¹³⁸ Ce 0.614	¹⁶³ Dy 1.042	¹⁸⁸ Os	1.131
³² S	0.367	⁶⁴ Ni	0.858	⁹⁴ Zr 0.391		0.750	¹³⁹ Ce 0.611	¹⁶⁴ Dy 1.035	¹⁸⁹ Os	1.023
³³ S	0.489	⁶³ Cu	0.925	⁹⁵ Zr 0.624		0.597	¹⁴⁰ Ce 0.487	¹⁶³ Ho 1.025	¹⁹⁰ Os	1.374
³⁴ S	0.064	⁶⁵ Cu	0.731	⁹⁶ Zr 0.742		0.594	¹⁴¹ Ce 0.597	¹⁶⁵ Ho 1.038	¹⁹¹ Os	1.684
³⁶ S	0.599	⁶⁴ Zn	0.773	⁹³ Nb 0.620		0.572	¹⁴² Ce 0.744	¹⁶² Er 1.456	¹⁹² Os	2.537
³⁵ C1	0.627	⁶⁵ Zn	0.799	⁹⁴ Nb 0.596		0.714	¹⁴¹ Pr 0.425	¹⁶⁴ Er 1.083	¹⁹¹ Ir	1.366
³⁶ C1	0.659	⁶⁶ Zn	0.735	⁹² Mo 0.546		0.556	¹⁴² Pr 0.531	¹⁶⁶ Er 1.156	¹⁹² Ir	1.291
³⁷ Cl	0.992	⁶⁷ Zn	1.041	⁹⁴ Mo 0.674		0.559	¹⁴³ Pr 0.811	¹⁶⁷ Er 1.063	¹⁹³ Ir	1.416
³⁶ Ar	0.615	⁶⁸ Zn	0.671	⁹⁵ Mo 0.605		0.752	¹⁴² Nd 0.423	¹⁶⁸ Er 1.200	¹⁹⁰ Pt	0.762
³⁸ Ar	0.789	⁷⁰ Zn	1.285	⁹⁶ Mo 0.712		0.410	¹⁴³ Nd 0.526	¹⁶⁹ Er 1.488	¹⁹² Pt	0.954
³⁹ Ar	0.900	⁶⁹ Ga	0.768	⁹⁷ Mo 0.830		0.553	¹⁴⁴ Nd 0.715	¹⁷⁰ Er 0.983	¹⁹³ Pt	0.948
⁴⁰ Ar	0.709	⁷¹ Ga	1.318	⁹⁸ Mo 1.050		0.753	¹⁴⁵ Nd 0.809	¹⁶⁹ Tm 1.183	¹⁹⁴ Pt	1.120
³⁹ K	0.855	⁷⁰ Ge	0.820	¹⁰⁰ Mo 1.762		0.870	¹⁴⁶ Nd 0.895	¹⁷⁰ Tm 1.333	¹⁹⁵ Pt	1.504
⁴⁰ K	1.047	⁷² Ge	1.272	⁹⁹ Tc 1.141	¹²³ Te	1.113	¹⁴⁷ Nd 1.471	¹⁷¹ Tm 0.862	¹⁹⁶ Pt	1.179
⁴¹ K	0.968	⁷³ Ge	1.246	⁹⁶ Ru 0.842		0.772	¹⁴⁸ Nd 1.630	¹⁶⁸ Yb 1.207	¹⁹⁸ Pt	1.211
⁴⁰ Ca	0.544	⁷⁴ Ge	1.269	⁹⁸ Ru 0.659	¹²⁵ Te	0.945	¹⁵⁰ Nd 1.512	¹⁷⁰ Yb 1.020	¹⁹⁷ Au	1.136
⁴¹ Ca	0.973	⁷⁶ Ge	1.442	⁹⁹ Ru 0.836		0.717	¹⁴⁷ Pm 1.038	¹⁷¹ Yb 1.177	¹⁹⁸ Au	1.089
⁴² Ca	0.932	⁷⁵ As	1.893	¹⁰⁰ Ru 0.965		0.829	¹⁴⁸ Pm 1.466	¹⁷² Yb 0.851	¹⁹⁶ Hg	1.556
⁴³ Ca	1.533	⁷⁴ Se	1.290	¹⁰¹ Ru 1.504		0.609	¹⁴⁹ Pm 2.179	¹⁷³ Yb 0.873	¹⁹⁸ Hg	0.729
⁴⁴ Ca	1.186	⁷⁶ Se	1.380	102 Ru 1.262		0.866	¹⁴⁴ Sm 0.426	¹⁷⁴ Yb 0.834	¹⁹⁹ Hg	1.208
⁴⁵ Ca	1.045	⁷⁷ Se	1.356	103Ru 0.935	¹²⁹ I	1.114	¹⁴⁷ Sm 0.655	¹⁷⁵ Yb 1.112	²⁰⁰ Hg	1.040
⁴⁶ Ca	1.694	⁷⁸ Se	1.477	¹⁰⁴ Ru 1.595		0.803	¹⁴⁸ Sm 0.929	¹⁷⁶ Yb 0.977	²⁰¹ Hg	2.333
⁴⁸ Ca	1.315	⁷⁹ Se	1.193	¹⁰³ Rh 1.001	¹²⁶ Xe	0.666	¹⁴⁹ Sm 1.596	¹⁷⁵ Lu 1.077	²⁰² Hg	1.533
⁴⁵ Sc	1.189	⁸⁰ Se	1.097	¹⁰² Pd 0.998		0.799	¹⁵⁰ Sm 1.754	¹⁷⁶ Lu 1.036	²⁰³ Hg	1.450
⁴⁶ Ti	0.770	⁸² Se	0.482	¹⁰⁴ Pd 0.955		0.734	¹⁵¹ Sm 1.987	¹⁷⁴ Hf 1.182	²⁰⁴ Hg	2.796
⁴⁷ Ti	0.803	⁷⁹ Br	1.422	¹⁰⁵ Pd 1.236		0.880	¹⁵² Sm 1.644	¹⁷⁶ Hf 0.802	²⁰³ T1	0.975
⁴⁸ Ti	2.083	⁸¹ Br	1.170	¹⁰⁶ Pd 1.137		0.744	¹⁵³ Sm 1.176	¹⁷⁷ Hf 1.286	²⁰⁴ T1	1.274
⁴⁹ Ti	0.966	⁷⁸ Kr	0.916	¹⁰⁷ Pd 1.604		0.884	¹⁵⁴ Sm 0.955	¹⁷⁸ Hf 0.900	²⁰⁵ T1	1.033
⁵⁰ Ti	1.092	⁷⁹ Kr	1.179	¹⁰⁸ Pd 1.292		0.807	¹⁵¹ Eu 1.604	¹⁷⁹ Hf 0.991	²⁰⁴ Pb	1.345
⁵⁰ V	0.974	⁸⁰ Kr	1.313	¹¹⁰ Pd 1.395		0.576	¹⁵² Eu 1.312	¹⁸⁰ Hf 0.955	²⁰⁵ Pb	1.505
⁵¹ V	1.959	⁸¹ Kr	1.142	¹⁰⁷ Ag 0.849		0.612	¹⁵³ Eu 1.073	¹⁸¹ Hf 0.840	²⁰⁶ Pb	0.588
⁵⁰ Cr	1.091	⁸² Kr	0.764	¹⁰⁹ Ag 0.891	¹³³ Cs	0.752	¹⁵⁴ Eu 1.145	¹⁸² Hf 1.101	²⁰⁷ Pb	0.637
⁵¹ Cr	1.015	⁸³ Kr	0.786	¹¹⁰ Ag 0.768		0.697	¹⁵⁵ Eu 1.004	¹⁷⁹ Ta 0.899	²⁰⁸ Pb	0.918
⁵² Cr	0.523	⁸⁴ Kr	0.609	¹⁰⁶ Cd 0.665		0.690	¹⁵² Gd 1.802	¹⁸⁰ Ta ^a	²⁰⁹ Bi	0.334
⁵³ Cr	2.237	⁸⁵ Kr	0.448	¹⁰⁸ Cd 0.536		1.038	¹⁵³ Gd 1.519	¹⁸¹ Ta 0.854	²¹⁰ Bi	0.465
⁵⁴ Cr	0.715	⁸⁶ Kr	0.419	¹¹⁰ Cd 0.814		0.803	¹⁵⁴ Gd 1.631	182 Ta 0.854		5.105
⁵⁵ Mn	1.135	⁸⁵ Rb	0.529	¹¹¹ Cd 1.318		0.767	¹⁵⁵ Gd 1.198	¹⁸⁰ W 0.793		
14111	1.155	100	5.527	Cu 1.510	Du	5.707	Gu 1.170	0.175		

NOTE.—Forward as well as reverse rates have to be multiplied by the given factor.

^a The RATH rate is for ^{180g}Ta, whereas in Bao et al. 2000 the MACS for ^{180m}Ta is given. The proper renormalized rate coefficients for ^{180m}Ta(n, γ) are $a_0 = -9.899046$, $a_1 = 0.2659302$, $a_2 = -27.6891$, $a_3 = 59.43646$, $a_4 = -3.639849$, $a_5 = 0.03887359$, and $a_6 = -25.80838$.

helium, and carbon mass fractions first drop below 1%. The silicon core is defined by where silicon becomes more abundant than oxygen and the iron core by where the sum of the mass fractions of iron group nuclei first exceeds 50% (all criteria applied moving inward). The deleptonized core is the region where the number of electrons per baryon, Y_e , drops below 0.49.

Revisions in opacity and the introduction of mass loss generally lead to smaller helium cores that also tend to decrease the mass of the carbon-oxygen and the silicon cores. Note, however, that the absolute values of these core masses depend on many uncertainties, in particular, in the efficiencies of mixing processes in the stellar interior: semiconvection, overshooting, and rotationally induced mixing (not included here; see also Imbriani et al. 2001). For example, the helium core of the new model S25 is about 1 M_{\odot} smaller than in the equivalent 25 M_{\odot} model of WW95. A model that was computed with the new opacity tables, but without mass loss, had about half a solar mass smaller helium core. Thus, we attribute the other half solar mass of

PROPERTIES OF STELLAR I	MODELS AT TH	E ONSET OF	CORE COLLAR	2SE AND EXI	PLOSION PARAMETER	(5
Model(s)	S15, N15	S19	S20, N20	S21	S25, N25, H25	S25P
Initial mass (M_{\odot})	15.081	19.103	20.109	21.114	25.136	25.136
Wind mass loss (M_{\odot})	2.469	4.268	5.369	6.403	12.057	12.057
Final mass (M_{\odot})	12.612	14.835	14.740	14.711	13.079	13.079
Helium core (M_{\odot})	4.163	5.646	6.131	6.540	8.317	8.317
$C/O \operatorname{core}(M_{\odot})$	2.819	4.103	4.508	4.849	6.498	6.498
$Ne/Mg/O \operatorname{core}(M_{\odot})$	1.858	2.172	1.695	2.021	2.443	2.443
Si core (M_{\odot})	1.808	1.699	1.601	1.739	2.121	2.121
"Iron" core (M_{\odot})	1.452	1.458	1.461	1.548	1.619	1.619
$M_{\text{piston}}/$ " Y_e " core (M_{\odot})	1.315	1.458	1.461	1.357	1.619	1.619
$g_{\rm piston} (GM_{\rm piston}/r)$	0.460	0.710	2.320	0.770	0.670	0.930
E_{expl} (×10 ⁵¹ ergs)	1.205	1.204	2.203	1.765	1.735	2.293
Fallback (M_{\odot})	0.368	0.221	0.087	0.403	0.422	0.342
Remnant (baryonic, M_{\odot})	1.683	1.679	1.548	1.760	2.041	1.961

 TABLE 6

 Properties of Stellar Models at the Onset of Core Collapse and Explosion Parameters

decrease in helium core mass to the action of mass loss. Of course, the two effects are not entirely independent.

As a result of the reduced helium core size, our new models generally have lower carbon-oxygen and oxygen-neon cores. Because of the interaction of the different phases of shells burning, the sizes of the "inner cores" do not always monotonically change with the size of the helium core, although a general trend is followed (Woosley et al. 2002).

The change in the weak rates (Langanke & Martínez-Pinedo 2000), important after central oxygen burning, leads to a 2%–3% increase in the central value of Y_e at the time of core collapse (over what would have resulted using Fuller et al. 1980), and the "deleptonized core" tends to contain less mass. More importantly, we find 30%–50% higher densities in the region $m = 1.5-2 M_{\odot}$, which may affect the core-collapse supernova mechanism as a result of correspondingly higher ram pressure of the infalling matter (see Janka 2001). Further details concerning the effect of the new weak rates are discussed in Heger et al. (2001).

4.2. Supernova Explosions

The most recent multidimensional calculations of core collapse and supernova explosion still offer little guidance as to the exact placement of the mass cut, the entropy and Y_e of the innermost ejecta, or even if a given model will explode (Herant et al. 1994; Burrows, Hayes, & Fryxell 1995; Janka & Müller 1996; Mezzacappa et al. 1998; Fryer & Heger 2000). Nucleosynthesis studies must still parameterize the explosion as best they can. In the present paper supernova explosions were simulated, as in WW95, by a piston that first moved inward for 0.45 s to a radius of 500 km and then rebounded to a radius of 10,000 km. For the inward motion, the initial velocity is the local velocity of the corresponding mass shell at the time of the presupernova model, and the acceleration of the piston is a constant fraction of the actual local gravitational acceleration, $GM_{\rm piston}/r$. The arbitrary fraction is chosen such that the piston arrives at a radius of 500 km in 0.45 s. The subsequent outward movement also is a ballistic trajectory in a gravitational field given by a different constant fraction of the actual local gravitational acceleration. Now the factor is chosen such that an explosion of 1.2×10^{51} ergs of kinetic energy in the ejecta (measured at infinity) results in the 15 and 19 M_{\odot} models. This much kinetic energy is commonly assumed for SN 1987A (e.g., Woosley 1988), but it could have been very different in other supernovae. For the heavier stars, this relatively modest energy gives large amounts of "fallback," so that much of the interesting nucleosynthesis falls into the neutron star (see also WW95). Therefore, an alternate prescription that resulted in larger energies was used for the 20, 21, and 25 M_{\odot} stars. The energy there was adjusted (increased) until the ejecta contained about 0.1 M_{\odot} of ⁵⁶Ni. This is comparable to the mass of ⁵⁶Ni, ~0.07 M_{\odot} , commonly adopted for SN 1987A (e.g., Arnett et al. 1989). For model S25P, which had the same presupernova evolution as model S25, a still more powerful explosion was calculated that ejected about 0.2 M_{\odot} of ⁵⁶Ni (see Tables 6 and 9).

The final mass cut outside the piston was determined by the mass that had settled on the piston at 2.5×10^4 s after core collapse. Note that the amount of fallback resulting from this prescription depends on both the initial location of the piston used and its energy. In particular, the yields of ⁴⁴Ti and ⁵⁶Ni are very sensitive to the "final mass cut" often determined by the fallback.

The neutrino process (ν -process) during the supernova explosion was implemented using the same prescription as in WW95 and using the same cross sections. We used a neutrino pulse characterized by a total energy of 3×10^{53} ergs decaying exponentially on a timescale of 3 s. The neutrinos were assumed to have a mean energy of 4 MeV for the electron neutrinos and 6 MeV for the μ and τ neutrinos (different from WW95, who used 8 MeV for the μ and τ neutrinos). The lower value is recommended by Myra & Burrows (1990).

5. NUCLEOSYNTHESIS RESULTS

Yields were determined for 15, 19, 20, 21, and 25 M_{\odot} stars (series S; models S15, S19, . . .) with initial solar composition (Anders & Grevesse 1989; see also Table 7) and the standard rate set (Table 1). Identical stellar models having 15, 20, and 25 M_{\odot} were also calculated using the NACRE rate set (set N; see also Table 1). That is, all reactions given by NACRE were substituted for their counterparts, except for ¹²C(α , γ)¹⁶O; all rates not given by NACRE were left the same. A single 25 M_{\odot} star was calculated that employed the rate set of Hoffman et al. (2001; set H; see § 3.1), which is much smaller than our current network.

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TABLE 7Initial Mass Fractions

				INTIAL IVIA	ASS FRACTIONS				
Ion	X	Ion	X	Ion	X	Ion	Х	Ion	Х
¹ H	7.057(-1)	⁵³ Cr	1.716(-6)	⁹⁵ Mo	9.760(-10)	¹³¹ Xe	3.380(-9)	¹⁶⁹ Tm	1.620(-10)
² H	4.801(-5)	⁵⁴ Cr	4.357(-7)	⁹⁶ Mo	1.030(-9)	¹³² Xe	4.140(-9)	¹⁶⁸ Yb	1.370(-12)
³ He	2.929(-5)	⁵⁵ Mn	1.329(-5)	⁹⁷ Mo	5.990(-10)	¹³⁴ Xe	1.560(-9)	¹⁷⁰ Yb	3.250(-11)
⁴ He	2.752(-1)	⁵⁴ Fe	7.130(-5)	⁹⁸ Mo	1.520(-9)	¹³⁶ Xe	1.280(-9)	¹⁷¹ Yb	1.530(-10)
⁶ Li	6.496(-10)	⁵⁶ Fe	1.169(-3)	¹⁰⁰ Mo	6.220(-10)	¹³³ Cs	1.250(-9)	¹⁷² Yb	2.630(-10)
⁷ Li	9.349(-9)	⁵⁷ Fe	2.855(-5)	⁹⁶ Ru	2.500(-10)	¹³⁰ Ba	1.570(-11)	¹⁷³ Yb	1.750(-10)
⁹ Be	1.662(-10)	⁵⁸ Fe	3.697(-6)	⁹⁸ Ru	8.680(-11)	¹³² Ba	1.510(-11)	¹⁷⁴ Yb	3.470(-10)
¹⁰ B	1.067(-9)	⁵⁹ Co	3.358(-6)	⁹⁹ Ru	5.910(-10)	¹³⁴ Ba	3.690(-10)	¹⁷⁶ Yb	1.400(-10)
¹¹ B	4.730(-9)	⁵⁸ Ni	4.944(-5)	¹⁰⁰ Ru	5.920(-10)	¹³⁵ Ba	1.010(-9)	¹⁷⁵ Lu	1.580(-10)
¹² C	3.032(-3)	⁶⁰ Ni	1.958(-5)	¹⁰¹ Ru	8.070(-10)	¹³⁶ Ba	1.210(-9)	¹⁷⁶ Lu	4.630(-12)
¹³ C	3.650(-5)	⁶¹ Ni	8.594(-7)	¹⁰² Ru	1.520(-9)	¹³⁷ Ba	1.750(-9)	¹⁷⁴ Hf	1.100(-12)
¹⁴ N	1.105(-3)	⁶² Ni	2.776(-6)	¹⁰⁴ Ru	9.150(-10)	¹³⁸ Ba	1.120(-8)	¹⁷⁶ Hf	3.530(-11)
¹⁵ N	4.363(-6)	⁶⁴ Ni	7.269(-7)	¹⁰³ Rh	8.960(-10)	¹³⁸ La	1.430(-12)	¹⁷⁷ Hf	1.280(-10)
¹⁶ O	9.592(-3)	⁶³ Cu	5.753(-7)	¹⁰² Pd	3.660(-11)	¹³⁹ La	1.570(-9)	¹⁷⁸ Hf	1.890(-10)
¹⁷ O	3.887(-6)	⁶⁵ Cu	2.647(-7)	¹⁰⁴ Pd	4.080(-10)	¹³⁶ Ce	7.430(-12)	¹⁷⁹ Hf	9.510(-11)
¹⁸ O	2.167(-5)	⁶⁴ Zn	9.924(-7)	¹⁰⁵ Pd	8.230(-10)	¹³⁸ Ce	9.880(-12)	¹⁸⁰ Hf	2.460(-10)
¹⁹ F ²⁰ Ne	4.051(-7)	⁶⁶ Zn ⁶⁷ Zn	5.877(-7)	¹⁰⁶ Pd ¹⁰⁸ Pd	1.020(-9)	¹⁴⁰ Ce ¹⁴² Ce	3.580(-9)	¹⁸⁰ Ta	1.130(-14)
²⁰ Ne	1.619(-3)	⁶⁸ Zn	8.762(-8)	¹⁰⁰ Pd	1.010(-9)	¹⁴¹ Pr	4.530(-10)	¹⁸¹ Ta ¹⁸⁰ W	9.480(-11)
²² Ne	4.127(-6)	⁷⁰ Zn	4.059(-7) 1.339(-8)	¹⁰⁷ Ag	4.540(-10) 6.820(-10)	¹⁴² Nd	5.960(-10)	¹⁸² W	7.880(-13) 1.610(-10)
²³ Na	1.302(-4) 3.339(-5)	⁶⁹ Ga	3.962(-8)	¹⁰⁹ Ag	6.450(-10)	¹⁴³ Nd	8.080(-10) 3.620(-10)	¹⁸³ W	8.800(-11)
²⁴ Mg	5.148(-4)	⁷¹ Ga	2.630(-8)	¹⁰⁶ Cd	5.390(-11)	¹⁴⁴ Nd	7.180(-10)	¹⁸⁴ W	1.900(-11)
²⁵ Mg	6.766(-5)	⁷⁰ Ge	4.320(-8)	¹⁰⁸ Cd	3.910(-11)	¹⁴⁵ Nd	2.520(-10)	¹⁸⁶ W	1.900(-10) 1.790(-10)
²⁶ Mg	7.760(-5)	⁷² Ge	5.940(-8)	¹¹⁰ Cd	5.590(-10)	¹⁴⁶ Nd	5.240(-10)	¹⁸⁵ Re	9.030(-11)
²⁷ Al	5.805(-5)	⁷³ Ge	1.710(-8)	¹¹¹ Cd	5.780(-10)	¹⁴⁸ Nd	1.790(-10)	¹⁸⁷ Re	1.660(-10)
²⁸ Si	6.530(-4)	⁷⁴ Ge	8.120(-8)	¹¹² Cd	1.100(-9)	¹⁵⁰ Nd	1.770(-10)	¹⁸⁴ Os	5.680(-13)
²⁹ Si	3.426(-5)	⁷⁶ Ge	1.780(-8)	¹¹³ Cd	5.630(-10)	¹⁴⁴ Sm	2.910(-11)	¹⁸⁶ Os	5.030(-11)
³⁰ Si	2.352(-5)	⁷⁵ As	1.240(-8)	¹¹⁴ Cd	1.340(-9)	¹⁴⁷ Sm	1.480(-10)	¹⁸⁷ Os	3.820(-11)
³¹ P	8.155(-6)	⁷⁴ Se	1.030(-9)	¹¹⁶ Cd	3.550(-10)	¹⁴⁸ Sm	1.090(-10)	¹⁸⁸ Os	4.270(-10)
³² S	3.958(-4)	⁷⁶ Se	1.080(-8)	¹¹³ In	2.260(-11)	¹⁴⁹ Sm	1.340(-10)	¹⁸⁹ Os	5.210(-10)
³³ S	3.222(-6)	⁷⁷ Se	9.150(-9)	¹¹⁵ In	5.120(-10)	¹⁵⁰ Sm	7.250(-11)	¹⁹⁰ Os	8.550(-10)
³⁴ S	1.866(-5)	⁷⁸ Se	2.900(-8)	¹¹² Sn	1.050(-10)	¹⁵² Sm	2.650(-10)	¹⁹² Os	1.350(-9)
³⁶ S	9.379(-8)	⁸⁰ Se	6.250(-8)	¹¹⁴ Sn	7.180(-11)	¹⁵⁴ Sm	2.280(-10)	¹⁹¹ Ir	1.190(-9)
³⁵ C1	2.532(-6)	⁸² Se	1.180(-8)	¹¹⁵ Sn	3.750(-11)	¹⁵¹ Eu	1.780(-10)	¹⁹³ Ir	2.020(-9)
³⁷ C1	8.545(-7)	⁷⁹ Br	1.190(-8)	¹¹⁶ Sn	1.630(-9)	¹⁵³ Eu	1.970(-10)	¹⁹⁰ Pt	8.170(-13)
³⁶ Ar	7.740(-5)	⁸¹ Br	1.190(-8)	¹¹⁷ Sn	8.670(-10)	¹⁵² Gd	2.540(-12)	¹⁹² Pt	5.100(-11)
³⁸ Ar	1.538(-5)	⁷⁸ Kr	3.020(-10)	¹¹⁸ Sn	2.760(-9)	¹⁵⁴ Gd	2.800(-11)	¹⁹⁴ Pt	2.160(-9)
⁴⁰ Ar	2.529(-8)	⁸⁰ Kr	2.020(-9)	¹¹⁹ Sn	9.870(-10)	¹⁵⁵ Gd	1.910(-10)	¹⁹⁵ Pt	2.230(-9)
³⁹ K	3.472(-6)	⁸² Kr	1.070(-8)	¹²⁰ Sn	3.790(-9)	¹⁵⁶ Gd	2.670(-10)	¹⁹⁶ Pt	1.680(-9)
⁴⁰ K	5.545(-9)	⁸³ Kr	1.080(-8)	¹²² Sn	5.460(-10)	¹⁵⁷ Gd	2.050(-10)	¹⁹⁸ Pt	4.820(-10)
⁴¹ K	2.634(-7)	⁸⁴ Kr	5.460(-8)	¹²⁴ Sn	6.930(-10)	¹⁵⁸ Gd	3.280(-10)	¹⁹⁷ Au	9.320(-10)
⁴⁰ Ca	5.990(-5)	⁸⁶ Kr	1.710(-8)	¹²¹ Sb	5.420(-10)	¹⁶⁰ Gd	2.920(-10)	¹⁹⁶ Hg	2.380(-12)
⁴² Ca	4.196(-7)	⁸⁵ Rb	1.100(-8)	¹²³ Sb	4.110(-10)	¹⁵⁹ Tb	2.430(-10)	¹⁹⁸ Hg	1.710(-10)
⁴³ Ca	8.973(-8)	⁸⁷ Rb	4.640(-9)	¹²⁰ Te	1.310(-11)	¹⁵⁶ Dy	8.720(-13)	¹⁹⁹ Hg	2.880(-10)
⁴⁴ Ca	1.425(-6)	⁸⁴ Sr	2.800(-10)	¹²² Te	3.830(-10)	¹⁵⁸ Dy	1.510(-12)	²⁰⁰ Hg	3.980(-10)
⁴⁶ Ca	2.793(-9)	⁸⁶ Sr	5.050(-9)	¹²³ Te	1.330(-10)	¹⁶⁰ Dy	3.730(-11)	²⁰¹ Hg	2.280(-10)
⁴⁸ Ca	1.384(-7)	⁸⁷ Sr	3.320(-9)	¹²⁴ Te	7.180(-10)	¹⁶¹ Dy	3.030(-10)	²⁰² Hg	5.160(-10)
⁴⁵ Sc ⁴⁶ Ti	3.893(-8) 2.234(-7)	⁸⁸ Sr ⁸⁹ Y	4.320(-8)	¹²⁵ Te ¹²⁶ Te	1.080(-9)	¹⁶² Dy ¹⁶³ Dy	4.140(-10) 4.050(-10)	²⁰⁴ Hg ²⁰³ Tl	1.200(-10) 2 790(-10)
⁴⁷ Ti	2.234(-7) 2.081(-7)	⁹⁰ Zr	1.040(-8) 1.340(-8)	¹²⁸ Te	2.900(-9) 4.950(-9)	¹⁶⁴ Dy	4.050(-10) 4.600(-10)	²⁰⁵ T1	2.790(-10) 6.740(-10)
⁴⁸ Ti	2.081(-7) 2.149(-6)	⁹¹ Zr	1.340(-8) 2.950(-9)	¹³⁰ Te	4.930(-9) 5.360(-9)	¹⁶⁵ Ho	4.600(-10) 3.710(-10)	²⁰⁴ Pb	3.150(-10)
⁴⁹ Ti	2.149(-0) 1.636(-7)	⁹² Zr	4.560(-9)	¹²⁷ I	2.890(-9)	¹⁶² Er	1.440(-12)	²⁰⁶ Pb	3.130(-10) 3.090(-9)
⁵⁰ Ti	1.630(-7) 1.644(-7)	⁹⁴ Zr	4.300(-9) 4.710(-9)	¹²⁴ Xe	1.790(-11)	¹⁶⁴ Er	1.440(-12) 1.680(-11)	²⁰⁷ Pb	3.090(-9) 3.370(-9)
⁵⁰ V	9.258(-10)	⁹⁶ Zr	7.770(-10)	¹²⁶ Xe	1.620(-11)	¹⁶⁶ Er	3.540(-10)	²⁰⁸ Pb	9.630(-9)
⁵¹ V	3.767(-7)	⁹³ Nb	1.640(-9)	¹²⁸ Xe	3.330(-10)	¹⁶⁷ Er	2.430(-10)	²⁰⁹ Bi	7.610(-10)
⁵⁰ Cr	7.424(-7)	⁹² Mo	8.800(-10)	¹²⁹ Xe	4.180(-9)	¹⁶⁸ Er	2.860(-10)		,.010(10)
⁵² Cr	1.486(-5)	⁹⁴ Mo	5.610(-10)	¹³⁰ Xe	6.740(-10)	¹⁷⁰ Er	1.610(-10)		
			5.010(10)		5	21		l	

Figures 2–6 show the production factors after the explosion and the decay of all unstable species (except 40 K and 180 Ta) in our "standard" S-series. The abundances edited are those outside the mass cut given as "remnant mass" in Table 6. The resulting abundances, including all those lost to winds, have been divided by their solar (i.e., initial) values. Isotopes of each element are drawn in the same color and connected by lines. The production factor of ${}^{16}O$ —the

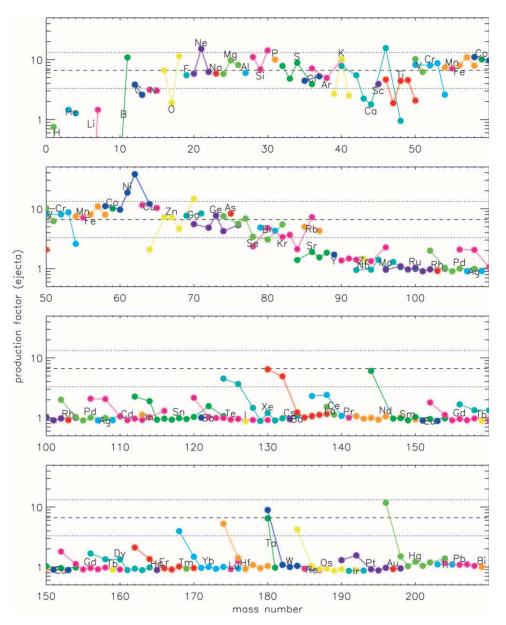


FIG. 2.—Postexplosive production factors following the decay of all radioactivities in model S15. Comparison is relative to solar abundances (Anders & Grevesse 1989). Note the consistent production at the factor of 10 level of most of the isotopes from A = 16 to 88 as well as a large fraction of the *p*-process isotopes. The relative overproduction of $^{61, 62}$ Ni may indicate some lingering uncertainty in the destruction cross sections for these species by (n, γ) . Many of the *p*-isotopes, especially those in the mass range A = 90–130, are underproduced. This may also improve with the inclusion of other models, but it seems to be chronic and may indicate an incomplete understanding of the *s*-process is massive stars (the *s*-process is the seed from which the *p*-process is made). Other deficiencies are discussed in WW95 and Woosley et al. (2002).

dominant "metal" yield of massive stars—is used as a fiducial point to provide a band of acceptable agreement of ± 0.3 dex relative to its value (*dashed and dotted lines*).

These yields are also given in Table 8 and are available electronically from the authors. Table 9 gives the yields of all radioactivities still having appreciable abundance at 2.5×10^4 s, the time of the mass cut determination (Table 6). For a few isotopes, the edits include progenitors that have not decayed at that time. For example, ⁵⁷Co is almost all produced initially as ⁵⁷Ni and results from its decay. Consequently, the ⁵⁷Co yield as given in Table 9 is only slightly higher than that of ⁵⁷Ni.

Figure 7, for model S25, allows the reader to gauge the importance of explosive versus preexplosive nucleosynthesis

for various isotopes in a 25 M_{\odot} star. The presupernova production factors of model S21 are shown in Figure 8.

Figures 9, 10, and 11 show the resulting postexplosive production factors of the NACRE runs relative to our standard set (e.g., yields of model N15 divided by yields of model S15), and Figure 12 gives the same comparison for the rate set H for the 25 M_{\odot} star. The reaction network of Hoffman et al. (2001) only reached up to Ru.

In addition, starting from the presupernova stage of model S25 and using the standard rate set, we followed a more powerful explosion that gave twice the amount of ⁵⁶Ni (model S25P). The results are shown along with the others in Tables 8 and 9. Figure 13 gives a direct comparison of nucleosynthesis in the model with high explosion energy

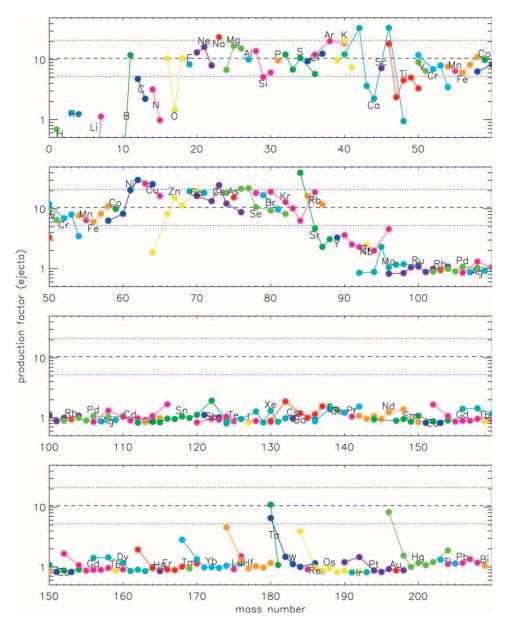


FIG. 3.—Similar to Fig. 2, but for model S19, a 19 M_{\odot} star. Note that the *p*-process around A = 180 is weaker than in model S15 and around A = 130 is essentially missing. The reason is that before the explosion the star had a convective shell close to the end of oxygen burning in which all isotopes with $A \gtrsim 100$ had already been largely destroyed, so the explosion cannot make heavy γ -process here. The neon-rich layer above was located too far out to become hot enough and make the *p*-process nuclei near A = 130. It became hot enough, however, to have some partial explosive neon burning at its bottom and make a little of the *p*-process isotopes of the A = 180 group, although less than we typically observed in the other models.

(S25P) relative to the one with lower (standard model S25) energy.

5.1. Production from Light Elements to the Fe Peak

The light isotopes ²H and ³He as well as the elements Li, Be, and B were destroyed during pre–main-sequence and main-sequence evolution. Although some ³He is initially made, it is destroyed again in the inner parts of the star. Different for WW95, fragile isotopes can additionally be preserved in the stellar wind, especially in the more massive stars, resulting in a slightly increased yield of, e.g., ³He in the S25 star compared to model S25A of WW95. However, substantial amounts of ⁷Li and ¹¹B were created, along with ¹⁹F, by the ν -process during the explosion (Fig. 7). The significant underproduction of ¹⁷O is a result of the revised reaction rates for ¹⁷O(p, α)¹⁴N and ¹⁷O(p, γ)¹⁸F (Hoffman et al. 2001).

Nucleosynthesis from Ca to Fe shows considerable scatter that only partly relates to the nuclear rates. Yields in this region are particularly sensitive to the details of the explosion and fallback as can be seen in the comparison between S25 and S25P. The higher explosion energy mostly alters the iron group (Fig. 13). In particular, the yields of ⁴⁴Ca, ⁴⁸Ti, ⁵⁶Fe, ⁵⁷Fe, ⁵⁹Co, and ^{58, 60–62}Ni are significantly enhanced. Lighter nuclei produced farther out in the star and heavier nuclides made by the *s*-process are not greatly affected by the explosion (hence Fig. 13 does not extend to high atomic mass).

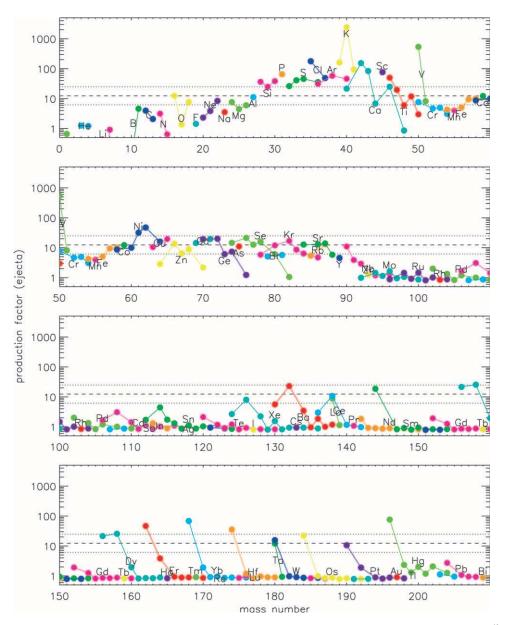


FIG. 4.—Similar to Fig. 2, but for model S20, a 20 M_{\odot} star. Note the very large overproduction of the *s*-process here, especially of 40 K and 50 V. These overproductions are unique within the five masses studied (15, 19, 20, 21, and 25 M_{\odot}) and show the importance of integrating over a large number of masses. The *s*-process is overly strong here because of a link-up and mixing of the convective carbon, neon, and oxygen shells about a day before the supernova. Note that despite this vigorous *s*-process isotopes are still underproduced from A = 92 to 124.

5.2. The 19, 20, and 21 M_{\odot} Models

It is necessary to discuss the 19, 20, and 21 M_{\odot} models separately because of the peculiar evolution of the 20 M_{\odot} model. Model S20 is at the transition mass [for our choice of ${}^{12}C(\alpha, \gamma){}^{16}O$ and convection theory] where stars change from excergic convective carbon core burning at their centers (less than 20 M_{\odot}) to stars where central carbon burning never generates an excess of energy above neutrino losses (although carbon shell burning always does). We show the history of the convective structure and energy generation for models S15, S20, and S25 in the Kippenhahn plots given in Figures 14–16. Model S20 exhibits a strong overproduction of several elements between Si and V, especially isotopes of Cl, K, and V (Fig. 4). Interestingly, Cr, Mn, and the light Fe isotopes are underproduced. This is atypical and is due to a stellar structure effect that appears, for the five stellar masses considered, only in this model. Specifically, model S20 experienced the merging of the convective oxygen, neon, and carbon shells (see also Bazan & Arnett 1994) well before (about 1 day) the end of the star's life, during the core contraction phase from central silicon burning until silicon shell ignition (Fig. 15). The merged shells carry neutron sources such as ²²Ne and especially ²⁶Mg to depths where they burn rapidly and provide a strong source of free neutrons. Capture of these neutrons is responsible for the largest overproductions.

To illustrate that this feature is confined to models close to 20 M_{\odot} , we also computed 19 and 21 M_{\odot} models (Figs. 3 and 5). In the 19 M_{\odot} model, ²³Na, ^{38, 40}Ar, ^{42, 46}Ca, and ⁸⁴Sr are enhanced whereas the other elements follow the expected trend when compared to models S15 and S25. Interestingly, S19 does not show any traces of a γ -process up to mass 152. In the 21 M_{\odot} model, ²³Na is overproduced

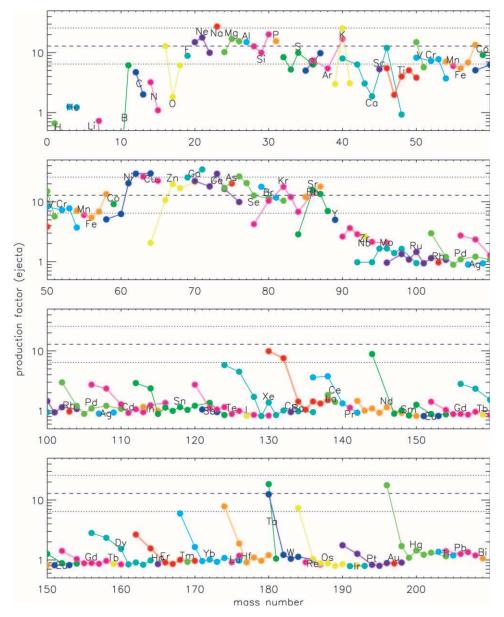


FIG. 5.—Similar to Fig. 2, but for model S21, a fully evolved and exploded 21 M_{\odot} star. These results look much more like those for a 25 M_{\odot} star than for a 20 M_{\odot} star.

as in S19, but S, Cl, and the odd K isotopes are produced less. Otherwise a "standard" pattern is emerging. In addition, similar *p*-process features (as in S15 and S25) are emerging, with the same Mo-Ru deficiency.

Clearly the solar abundances have not originated in stars of any single mass, and calculations of galactic chemical evolution must use many more stars (and with a range of initial metallicities) than the five presented here.

5.3. The s-Process

Nuclei above the iron group up to about A = 90 are produced in massive stars mainly by the *s*-process. When these yields are combined with those of metal-poor stars that contribute correspondingly less *s*-process, it is helpful if they are somewhat large, say, at the factor of 2 level, compared to those for primary species like oxygen. For current choices of rates, our *s*-process yields are, overall, consistent with this requirement. There is significant overproduction of the

s-process products in the range $70 \le A \le 90$ in the 25 M_{\odot} model, but this is partly offset, for many isotopes, by a more consistent production (relative to ¹⁶O) in the 15 M_{\odot} model. This is because of the well-known tendency of higher mass stars to be more effective in burning ²²Ne (Prantzos, Hashimoto, & Nomoto 1990).

In terms of specific isotopes, ⁶⁴Zn is underproduced in all cases studied. This nucleus may be a product of the neutrino wind from the proto-neutron star (Hoffman et al. 1996) not simulated here. The overabundance of the neutron-rich nickel isotopes, ^{61, 62, 64}Ni, and other *s*-process products in the A = 60-90 mass range has been observed before (Timmes et al. 1995; Hoffman et al. 2001) and is still not well understood. This overproduction is especially pronounced in the 25 M_{\odot} model. Chiefly as a result of a reduced ²²Ne(α , γ) rate in our "standard" rate set, we obtain a smaller *s*-process overproduction in S25 compared to H25.

While the overproduction may be related to residual uncertainties in the stellar model, this is a place where the

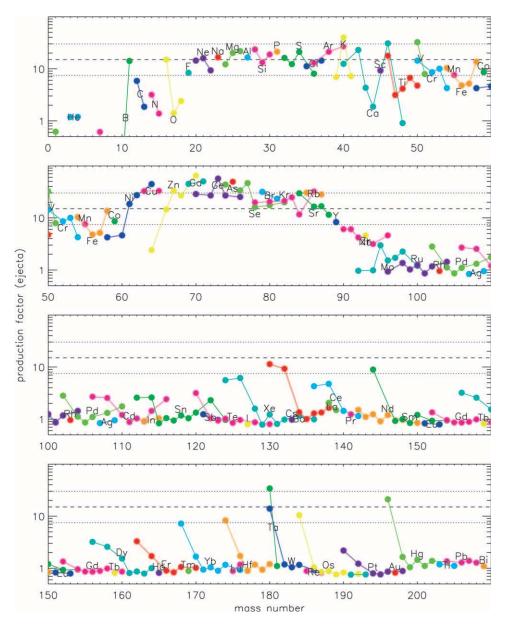


FIG. 6.—Similar to Fig. 2, but for model S25, our standard 25 M_{\odot} star. The *s*-process is overproduced but not badly, especially if one is to average these yields with lower mass stars like S15 and lower metallicity stars. As previously noted by Hoffman et al. (2001), the common coproduction of many *r*-, *s*-, and *p*-isotopes from A = 60 to 88 is striking. Production of iron group elements would be higher in an explosion with greater energy (Fig. 13).

TABLE 8Yields (in Solar Masses)

Ion	S15	S19	S20	S21	S25	S25P	N15	N20	N25	H25
¹ H	7.136	8.446	8.700	8.994	1.012(1)	1.012(1)	7.146	8.717	1.014(1)	1.012(1)
² H	2.735(-7)	2.021(-7)	2.094(-7)	2.156(-7)	2.429(-7)	2.427(-7)	2.927(-7)	2.321(-7)	2.604(-7)	2.425(-7)
³ He	5.695(-4)	6.612(-4)	6.836(-4)	7.065(-4)	7.994(-4)	7.994(-4)	5.716(-4)	6.866(-4)	8.029(-4)	7.994(-4)
⁴ He	4.684	5.939	6.229	6.514	7.597	7.607	4.673	6.209	7.574	7.596
⁶ Li	5.476(-11)	6.837(-11)	7.161(-11)	7.457(-11)	8.782(-11)	8.781(-11)	5.535(-11)	7.238(-11)	8.877(-11)	8.782(-11)
⁷ Li	1.820(-7)	1.824(-7)	1.588(-7)	1.315(-7)	1.327(-7)	1.142(-7)	1.814(-7)	1.598(-7)	1.335(-7)	1.321(-7)
⁹ Be	5.457(-11)	6.768(-11)	6.873(-11)	6.857(-11)	8.024(-11)	8.022(-11)	5.461(-11)	6.891(-11)	8.071(-11)	8.024(-11)
${}^{10}\mathbf{B}$	2.003(-9)	2.080(-9)	1.974(-9)	2.284(-9)	2.337(-9)	2.319(-9)	1.385(-9)	1.072(-9)	1.223(-9)	2.307(-9)
	6.905(-7)	9.790(-7)	4.046(-7)	5.633(-7)	1.542(-6)	1.477(-6)	7.387(-7)	4.477(-7)	1.654(-6)	1.010(-6)
¹² C	1.555(-1)	2.520(-1)	2.233(-1)	2.764(-1)	4.093(-1)	4.080(-1)	1.554(-1)	2.231(-1)	4.089(-1)	4.098(-1)

NOTE.—Table 8 is published in its entirety in the electronic edition of the Astrophysical Journal. A portion is shown here for guidance regarding its form and content.

 TABLE 9
 9

 Radioactive Yields (in Solar Masses)
 9

Ion	S15	S19	S20	S21	S25	S25P	N15	N20	N25	H25
³ H	2.385(-10)	3.358(-10)	2.141(-10)	2.297(-10)	2.086(-11)	2.051(-11)	2.234(-10)	7.774(-10)	2.037(-11)	2.078(-11)
¹⁴ C	4.744(-5)	9.458(-6)	6.054(-6)	1.822(-5)	9.611(-6)	1.070(-5)	3.917(-5)	5.155(-6)	7.408(-6)	2.458(-6)
²² Na	8.019(-7)	4.929(-6)	4.422(-7)	4.038(-6)	3.998(-6)	3.703(-6)	9.461(-7)	5.433(-7)	4.349(-6)	3.907(-6)
²⁶ A1	2.589(-5)	3.182(-5)	2.969(-5)	4.574(-5)	6.991(-5)	6.953(-5)	2.704(-5)	2.858(-5)	6.495(-5)	4.806(-13)
³² Si	1.862(-6)	5.142(-7)	2.265(-7)	4.915(-7)	2.407(-6)	3.145(-6)	1.733(-6)	1.977(-7)	2.299(-6)	2.366(-6)
³⁶ C1	1.499(-6)	2.605(-6)	1.165(-4)	2.757(-6)	6.884(-6)	6.521(-6)	1.596(-6)	1.111(-4)	7.305(-6)	6.308(-6)
³⁹ Ar	5.607(-6)	1.498(-5)	4.252(-5)	1.404(-5)	2.235(-5)	2.215(-5)	5.178(-6)	3.795(-5)	1.944(-5)	1.832(-5)
⁴² Ar	2.704(-8)	2.781(-9)	1.395(-9)	2.148(-9)	2.805(-8)	4.655(-8)	2.060(-8)	1.098(-9)	2.021(-8)	3.226(-8)
⁴¹ Ca	4.316(-6)	2.658(-5)	4.285(-4)	6.942(-6)	3.218(-5)	2.650(-5)	4.132(-6)	5.577(-4)	3.954(-5)	2.890(-5)
⁴⁵ Ca	9.659(-7)	2.676(-6)	4.389(-6)	9.296(-7)	3.403(-6)	3.433(-6)	9.003(-7)	3.921(-6)	3.023(-6)	1.880(-6)

NOTE.—Table 9 is published in its entirety in the electronic edition of the Astrophysical Journal. A portion is shown here for guidance regarding its form and content.

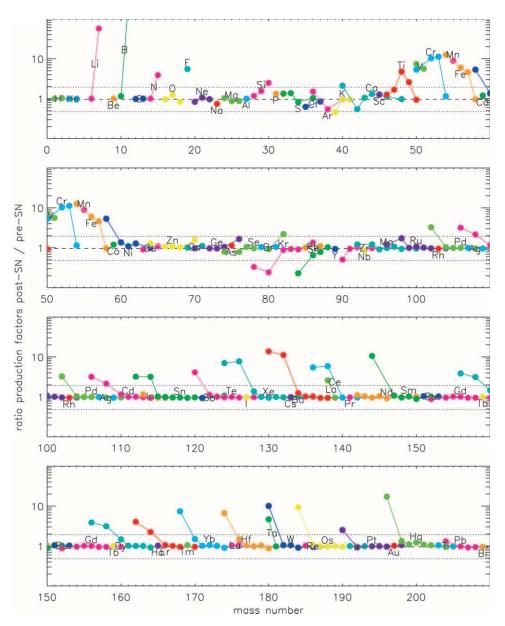


FIG. 7.—Ratio of the decayed production factors of model S25 after explosion to those before the explosion. In both cases we only consider the mass layers ejected in the supernova explosion and include the abundances ejected in the wind. Most pronounced is the production of the ν -process nuclei (⁷Li, ¹¹B, ¹⁵N, and ¹⁹F), most of the iron group, and the *p*-nuclei (with $A \ge 110$) made during the operation of the γ -process. The abundances of the light *p*-nuclei ⁷⁸Kr and ⁸⁴Sr are reduced from their peak levels made prior to the explosion.

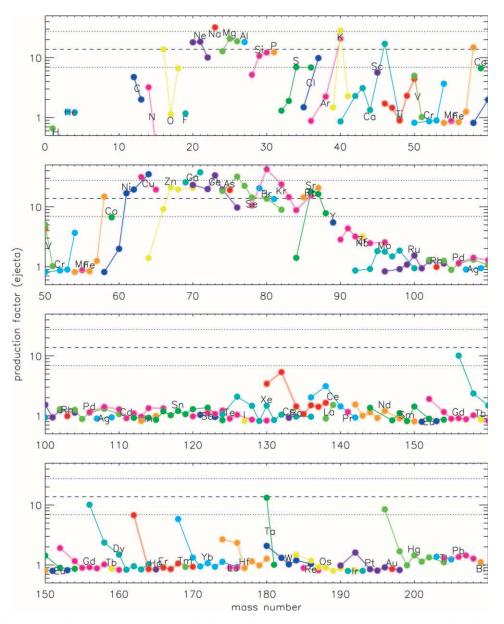


FIG. 8.—Similar to Fig. 2, but showing the *presupernova* production factors of model S21, a 21 M_{\odot} star. Only the mass outside of the baryonic remnant mass (Table 6), including winds, is considered. One can already see significant γ -process at $A \approx 130$ and A = 155-200.

nuclear physics might also be suspect. For ⁶²Ni in particular, the neutron capture rate given in Bao et al. (2000) is about a factor of 3 lower than that given previously in Bao & Käppeler (1987). Using the earlier rate, more ⁶²Ni would be destroyed by neutron capture, bringing the production factor down into the acceptable range. Both recommended rates are based on different extrapolations of the same experimental thermal neutron capture cross section. Both extrapolations assume s-waves, but the more recent one includes the estimated effect of a subthreshold resonance (H. Beer 2001, private communication). Such extrapolations have large uncertainties, especially for a heavy nucleus where resonance contributions can be expected already at around 30 keV. Therefore, it is important to measure the cross sections of the Ni isotopes directly in the relevant energy range.

The sensitivity of the *s*-process to changes in the chargedparticle reaction rates can be seen by comparing to the results obtained with rate set N (NACRE). The ratio of the production factors from sets S and N is shown in Figures 9– 11. The overproduction of the problematic Ni isotopes is less pronounced with set N, but the production of all nuclides between Ni and Pd is reduced. This is mainly due to the different ²²Ne (α , n)²⁵Mg and ²²Ne(α , γ)²⁶Mg rates, particularly the latter. Consequently, the *p*-isotopes at A > 100are also produced less because of the decreased production of seed nuclei in the *s*-process. To underline the fact that the (α , γ) and (α , n) reactions on ²²Ne are the main source of the differences, in Figure 17 we show the result of a test calculation using the NACRE set but replacing the two rates in question by our standard rates as given in § 3.1.2.

The large uncertainty in a few NACRE rates allows the existence of a much stronger *s*-process. Recent work (Costa et al. 2000) claims that, with an $^{22}Ne(\alpha, n)^{25}Mg$ rate enhanced by a factor of 100–1000 over the recommended NACRE value, the well-known problem of the underproduction of the *p*-isotopes of Mo and Ru might be cured. However, leaving aside the important question of whether

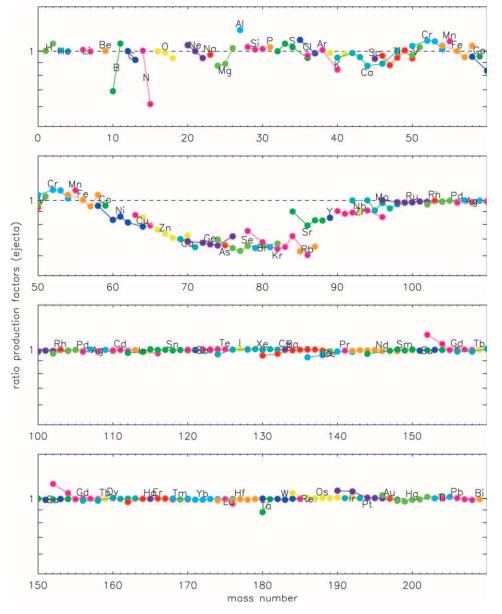


FIG. 9.—Production factors of the 15 M_{\odot} model N15 (NACRE) divided by S15 (standard). Note a weaker *s*-process in the run using the NACRE rates. This is chiefly because of their choice of a larger rate for the reaction ²²Ne(α , γ)²⁶Mg.

such a large variation can be tolerated given more recent laboratory data (Jaeger et al. 2001), a dramatic alteration in rates of this sort would have consequences, not only for the *p*-process, but for the production of numerous nuclei between Fe and Ru (Figs. 9–11). An intolerably strong *s*-process may result. A strongly enhanced ²²Ne (α , *n*)²⁵Mg rate might also pose problems for the *s*-process in asymptotic giant branch (AGB) stars. We defer a detailed numerical study of this and related questions to another paper, but certainly a more accurate determination of the cross sections for ²²Ne interacting with α -particles should have a very high priority in the nuclear astrophysics laboratory.

On the other hand, a comparison of models H25 and S25 (Fig. 12) shows considerable variations in the *s*-process, especially for individual isotopes, despite the fact that both studies used the same rates for ²²Ne(α , n)²⁵Mg and ²²Ne(α , γ)²⁶Mg. This is because H25 is the only case in which the neutron capture cross sections along with all Hauser-

Feshbach rates were different. All other studies changed only the mass of the star, explosion energy, or chargedparticle rate set. The size of the variations in Figure 12—up to a factor of 5 in some cases in which the network of H25 was still adequate—suggests that there is still a lot of work to be done in the nuclear laboratory. For example, the capture rates were about a factor of 2 *lower* at *s*-process temperatures for the Sr isotopes in model H25 and up to 3 times *greater* for the *s*-process isotopes of Mo. Inclusion of ¹⁶O as a neutron poison in model S25, and not in H25, as well as a larger cross section for the neutron poison ²⁶Mg in model S25, also contributed to making the *s*-process in S25 a little weaker.

Above A = 100 the s-process does very little, although there are redistributions of some of the heavy nuclei. This has a minor impact on the γ -process, as mentioned above. Most of the s-process above mass 90 is believed to come from AGB stars.

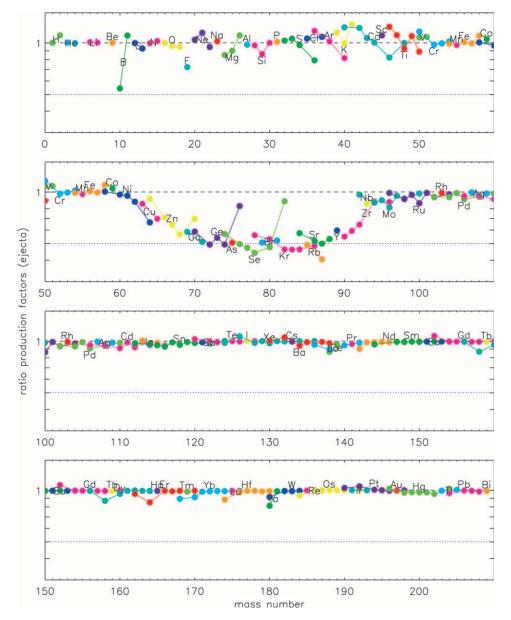


FIG. 10.—Similar to Fig. 9, but showing the production factors of the 20 M_{\odot} model N20 (NACRE) divided by S20 (standard)

5.4. The n-Process

The base of the helium shell has long been promoted as a possible site for fast neutron capture processes as the supernova shock front passes (Hillebrandt et al. 1981; Truran, Cowan, & Cameron 1978). In our present models a slight redistribution of heavy mass nuclei was found at the base of the helium shell, including significant production of the gamma-ray line candidate ⁶⁰Fe. Integrated over the star, however, the production of either the *r*-process in general or an appreciable subset of *r*-process nuclei above mass 100 was negligible compared with other species. Quite a few *r*-process isotopes above the iron group but lighter than mass A = 88 were made chiefly in the carbon and neon shells.

5.5. The γ -Process

The production of the "*p*-process" nuclei results from photodisintegration of heavy nuclei during hydrostatic and explosive oxygen and neon burning. This is more properly called the γ -process (Arnould 1976; Woosley & Howard 1978; Rayet, Arnould, & Prantzos 1990; Rayet et al. 1995). The present calculations are the first to follow the γ -processes through the presupernova stages and the supernova explosion in a self-consistent fashion. Here the γ -process operates in stellar regions that previously experienced the *s*-process, with the "seeds" being provided by the initial "solar" distribution of these Population I stars plus any additional production ($64 \le A \le 88$) that occurred in situ prior to explosion (Fig. 8).

For the 15, 21, and 25 M_{\odot} models, in the mass ranges $124 \le A \le 150$ and $168 \le A \le 200$, the proton-rich heavy isotopes are produced in solar abundance ratios within about a factor of 2 relative to ¹⁶O (Figs. 2, 5, and 6). Below A = 124 and between $150 \le A \le 165$ the production of the proton-rich isotopes is down by about a factor of 3–4. Similar trends can be found in all our models, although with different magnitudes. The total production of the proton-rich isotopes increases for higher entropy in the oxygen shell,

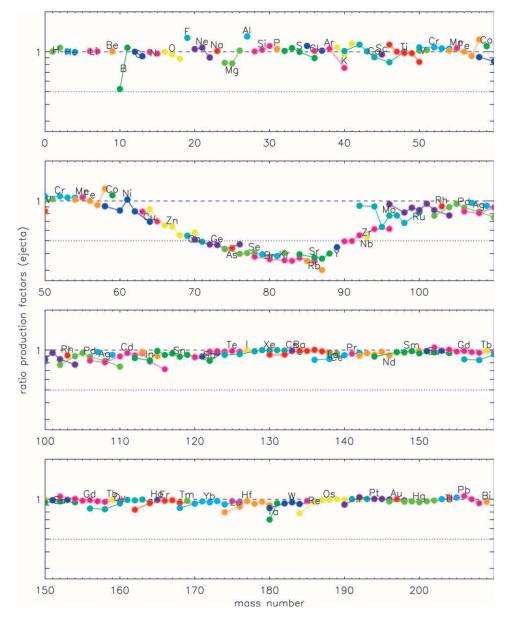


FIG. 11.—Similar to Fig. 9, but showing the production factors of the 25 M_{\odot} model N25 (NACRE) divided by S25 (standard)

i.e., with increasing mass of the helium core, as one can see in the 25 M_{\odot} star, but also depends on details of stellar structure and the composition of the star at the time of core collapse.

It is interesting to note that in some stars, production of the *p*-process nuclei occurs to varying extents in the oxygenburning shell *before* the explosion. For example, in the 25 M_{\odot} star, *p*-nuclei with A < 90 are made before the explosion (as also noted by Hoffman et al. 2001), but essentially none for A > 90 (Fig. 7). In the 21 M_{\odot} star a large production of *p*-nuclei at A > 90 occurs before the explosion (Fig. 8). This preexplosive production is even more pronounced in the 20 M_{\odot} model where the carbon and oxygen shells merged. Indeed, some of the production factors of *p*-nuclei in the 20 M_{\odot} model are so large that they will remain important even if this is a comparatively rare event. The 15 M_{\odot} star shows a significant γ -process in the A = 160-200 region before the explosion, but not around A = 130. In the 19 M_{\odot} star, essentially no γ -process occurs before the collapse. The details of the preexplosive *p*-production depend, of course, on the adopted convection model (Bazan & Arnett 1994).

Once again, the diversity of nucleosynthetic outcomes for stars of comparable mass is highlighted. A fine grid of masses must be calculated to correctly weight all these contributions. Because it depends on the extent of prior *s*-processes, the depth and possible merging of convective shells in the last hours of the star's life, and the strength of the explosion, the γ -process yields of stars can vary wildly. Ultimately this may make the γ -process an important diagnostic of stellar evolution.

In terms of nuclear physics, it should be noted that the $(\gamma, \alpha)/(\gamma, n)$ branching at ¹⁴⁸Gd, which determines the production ratio ¹⁴⁴Sm/¹⁴⁶Sm (Woosley & Howard 1990; Rauscher et al. 1995), is now known to much better accuracy than in previous investigations (see § 3.3). Although the experiment of Somorjai et al. (1998) did not quite reach the relevant energy window, it highly improved on the necessary extrapolation and yielded an *S*-factor that was several orders of

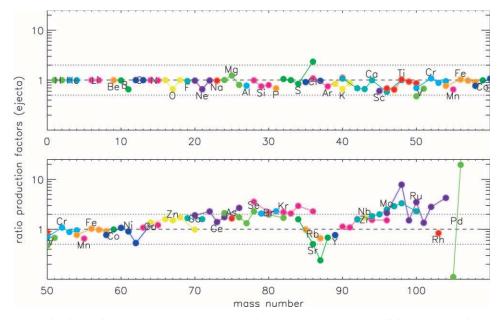


FIG. 12.—Ratio of the production factors for a model that used the rate set of Hoffman et al. (2001), H25, divided by those of the standard model S25. Both models have an identical stellar structure and evolution; only the network and reaction rates used to calculate nucleosynthesis were changed. Most of the differences, which can be quite significant, are due to differences in the cross sections for (n, γ) in the two studies. In particular, H25 had *larger* destruction cross sections for the *s*-process isotopes of Sr [in the case of ⁸⁷Sr, the (n, γ) rate was 2.6 times greater] and *smaller* cross sections for the isotopes of Mo. The increased production of ⁹⁸Ru, a *p*-process isotope, reflects the larger abundance of seeds heavier than A = 98. The abundance of this isotope and heavier ones are not accurately calculated in H25 because of the truncated network that ended at Ru.

magnitude lower than previous estimates. The remaining uncertainty is almost entirely due to the ${}^{148}\text{Gd}(\gamma, n){}^{147}\text{Gd}$ branch. Obviously, the total production of ${}^{144}\text{Sm}$ and ${}^{146}\text{Sm}$ is still sensitive to a number of photodisintegration rates only known theoretically.

5.5.1. The Case of 180 Ta

The production factors of the isotope ¹⁸⁰Ta, the rarest stable nuclear species in the solar abundance pattern, need special consideration. In the 25 M_{\odot} model ¹⁸⁰Ta shows a slight

overproduction, despite our taking into account its destruction by de-excitation into the short-lived ground state through thermal excitation into an intermediate state (Belic et al. 2000). However, in the calculation we do not explicitly follow the population of ground and isomeric state and therefore what is found is rather the sum of the produced ¹⁸⁰gTa + ^{180m}Ta. The nucleus ¹⁸⁰Ta is peculiar in the way that its ground state has a half-life of only 8.152 hr, much shorter than the half-life of the isomeric state with $T_{1/2} > 1.2 \times 10^{15}$ yr. In order to determine the fraction of the long-lived isomer in the total yield, one would have to

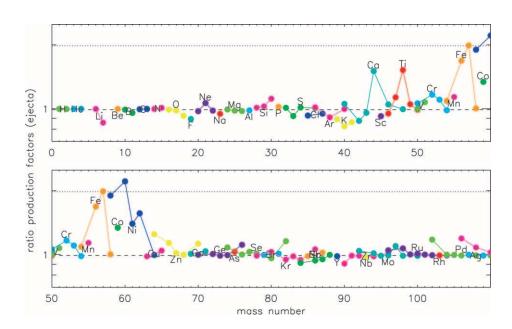


FIG. 13.—Decayed postexplosive production factors of model S25P (high explosion energy) relative to model S25. Shown are only isotopes up to mass number 110; beyond this the changes are only minor.

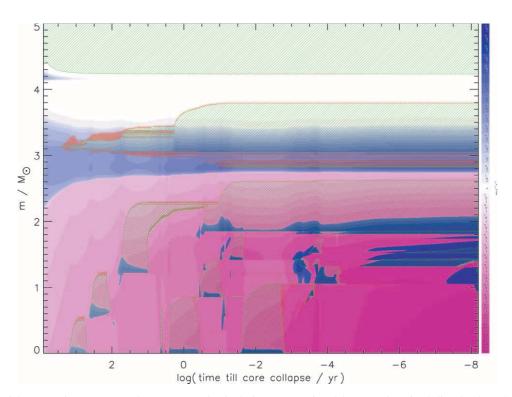


FIG. 14.—History of the convective structure and energy generation in the inner 5 M_{\odot} of model S15 starting after helium has been depleted in the center of the star. Time is given on a logarithmic scale measured backward, in years, from the instant of iron core collapse (*x*-axis). The vertical axis shows the interior mass in solar masses. Nuclear and neutrino losses are also given on a logarithmic color-coded scale with pink corresponding to energy loss and blue energy gain (in units of 10^{-1} ergs g^{-1} s⁻¹; each level of more intense [darker] coloring indicates an increase by 1 order of magnitude). Convective regions are indicated by green hatching and semiconvective layers by red cross-hatching. Note the convective red supergiant envelope outside about 4 M_{\odot} . Going along the *x*-axis at, e.g., an interior mass of 1 M_{\odot} , one encounters sequential episodes of convective carbon, neon, oxygen, and silicon burning (neon burning is comparatively brief). Unlike stars above about 20 M_{\odot} , carbon burning occurs convectively in the center of this star. Note the existence of a convective helium shell at death reaching from 3.0 to 3.8 M_{\odot} and a merged carbon, neon, and oxygen convective shell from 1.8 to 2.6 M_{\odot} .

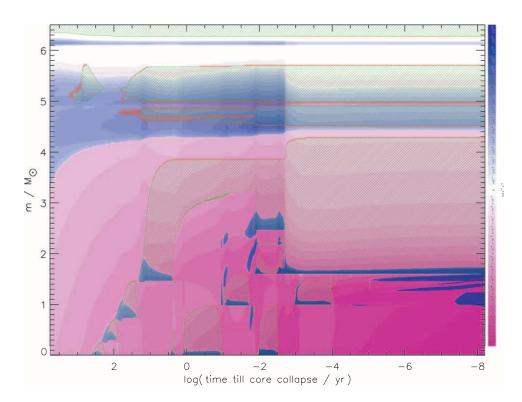


FIG. 15.—Similar to Fig. 14, but for model S20, a 20 M_{\odot} star. Carbon burning ignites in the middle of the star, but barely so. Note the merging of the oxygen-burning shell with the first carbon-burning region about a day before the death of the star. This leaves enough time for hydrodynamic adjustment of the CO core and extended merging of the carbon-, neon-, and oxygen-burning regions before death. The result is the very peculiar nucleosynthesis pattern we observe only in this model.

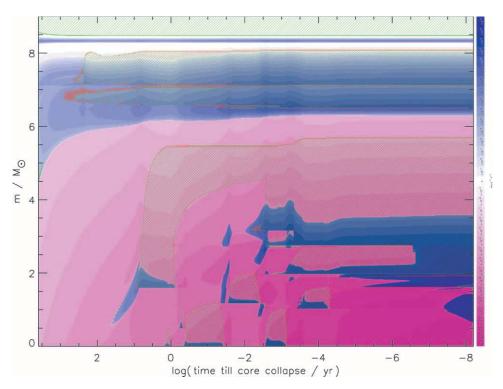


FIG. 16.—Similar to Fig. 14, but for model S25, our standard 25 M_{\odot} star. Note that carbon burning starts out radiatively (not convectively) in the center of the star and is not excergic when neutrino losses are included. Shell carbon burning becomes excergic only later, off center. A narrow semiconvective region, poorly resolved in the figure, separates the oxygen-burning and carbon-neon-burning shell until about 5 s before core collapse (as compared to a day in the 20 M_{\odot} model). Mixing does start, but the remaining lifetime of the star is too short to significantly alter its structure or nucleosynthesis.

know the population of ground and isomeric states. In Appendix B we show how to arrive at an estimate of the state population based on the experiment of Belic et al. (2000). It is concluded that about 30%–50% of the produced ¹⁸⁰Ta are actually in the isomeric state ¹⁸⁰mTa. Therefore, our production factors and yields have to be renormalized by that factor. This brings the production factor of this isotope down into the acceptable range for all stellar models.

6. SUMMARY AND CONCLUSIONS

Using a nuclear reaction network of unprecedented size, nucleosynthesis has been investigated in several stellar models in the mass range 15–25 M_{\odot} . The models include the best currently available nuclear and stellar physics. For the first time, it was also possible to self-consistently follow the γ -process up to Bi.

Overall good agreement can be achieved with the solar abundances of nuclei between ¹⁶O and ⁹⁰Zr. This good agreement is, to first order, independent of the reaction rate set employed: our current standard, Angulo et al. (1999), or Hoffman et al. (2001), although several key nuclear uncertainties are identified. In addition to the well-known need for greater accuracy in the rate for α -capture on ¹²C, the rates for ²²Ne(α , n)²⁵Mg and ²²Ne(α , γ)²⁶Mg are critical. We also urge a reexamination of some of the neutron capture cross sections for the isotopes of nickel. For the *p*-isotopes, two regions of atomic mass are found where those isotopes are underproduced, $92 \le A \le 124$ and $150 \le A \le 165$. It remains unclear whether this deficiency is due to nuclear cross sections, stellar physics, or if alternative (additional) *p*-process scenarios have to be invoked. However, we find that part of the *p*-nuclides may be produced in convective oxygen shell burning during the last hour of the star's life. The remainder is made explosively.

Interesting and unusual nucleosynthetic results are found for one particular 20 M_{\odot} model as a result of its special stellar structure. This effect, a merging of heavy-element shells late in the star's evolution, seems to be confined to a narrow range of masses. In particular, it is not seen in 19 and 21 M_{\odot} models. However, we have explored a very limited set of masses and those only in one spatial dimension (for caveats see Bazan & Arnett 1994).

We are grateful to Tom Weaver for his central role in developing the Kepler computer code and to Frank Timmes for providing the sparse matrix inverter we used for the large network. This research was supported, in part, by the DOE (W-7405-ENG-48 and the SciDAC program, grant DE-FC02-01ER41176), the National Science Foundation (AST 97-31569, INT 97-26315), the Alexander von Humboldt Foundation (FLF-1065004), and the Swiss National Science Foundation (2000-061822.00). T. R. acknowledges support by a PROFIL professorship from the Swiss National Science Foundation (grant 2124-055832.98).

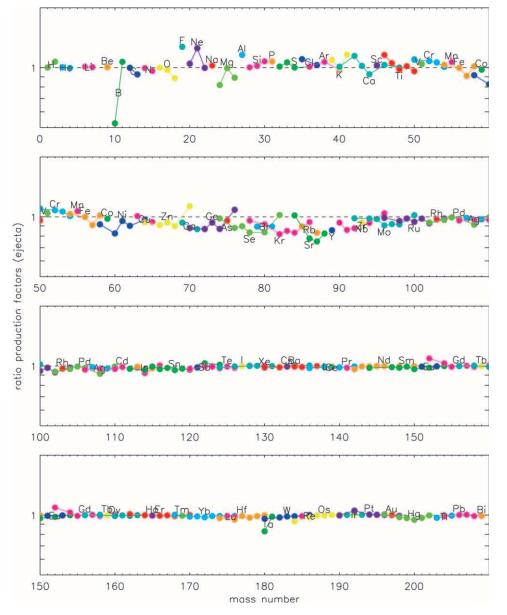


FIG. 17.—Ratio of the production factors of the 25 M_{\odot} model M25 divided by S25 (standard). Model M25 was a test calculation using the NACRE rate set except for the ²²Ne(α , n) and ²²Ne(α , γ) rates for which we implemented our "standard" rates (Hoffman et al. 2001).

APPENDIX A

A NEW APPROACH TO FITTING REACTION RATES

Frequently, experimentalists find it easiest to provide reaction rate data in tabular form, but there are several issues that make using such tables difficult for the stellar modeler. First is the issue of accuracy. Most charged-particle reaction rates change by many orders of magnitude over narrow temperature ranges, making direct interpolation difficult. To improve accuracy, a fine temperature grid is required. Coupled with the vast number of reaction rates required in a large reaction network, the memory storage issues alone have historically forced the designers of astrophysical databases to adopt fits to reaction rates and accept a (marginal) loss of accuracy. This is especially true for theoretical (Hauser-Feshbach) reaction rates, which are often smooth enough to be accurately fitted. Reaction rates that use a standard form, for example, some combination of powers of temperature in a single exponential, are also particularly efficient to calculate on the machine. This is an important consideration when computing many thousands of rates in every zone of a star at every time step.

The most important rates (usually those on targets lighter than silicon, and especially those that play a dominant role in energy generation) have, until now, been fitted to analytical functions (Caughlan & Fowler 1988; Angulo et al. 1999, who provide both tables and fits). Over the years these formulae have become increasingly diverse and complicated. These important reactions are small in number and in principle can be used in tabular form.

We propose an approach that takes advantage of the best features of both approaches—analytic fits and tables—while functioning efficiently on the machine at a modest cost in memory allocation. All of the charged-particle reaction rates from the recent compilation of Iliadis et al. (2001) were fitted this way and used in our calculations.

The reaction rate as a function of temperature $\lambda(T_9)$, provided in tabular form by the experimenter, is first fitted to an analytic function chosen for its accuracy, speed in evaluation, and approximately correct physical behavior at low temperatures. For the charged-particle reactions treated in Iliadis et al. (2001), we used equation (8) of Woosley et al. (1978) (always fitted in the exoergic direction):

$$\lambda_{jk} = T_9^{-2/3} \exp\left[A - \left(\frac{\tau}{T_9^{1/3}}\right) \left(1 + BT_9 + CT_9^2 + DT_9^3\right)\right],\tag{A1}$$

where $\tau = 4.2487(Z_I Z_j \hat{A}_j)^{1/3}$ reflects the Coulomb barrier for a charged particle in the entrance channel of reaction I(j,k)L, Z_I and Z_j are the charges of the target and incident particle, and \hat{A}_j is the reduced mass of the compound system. This fit is intended to contain the bulk of the temperature dependence of the rate but often does not, by itself, constitute an acceptable fit over the tabulated temperature range, especially if individual resonances are important. But also available from the fitting process are the residuals at each tabulated temperature. The logarithms of the ratios of the actual rate to the rate predicted by the fitting function are carried as a table in the computer and can be interpolated much more accurately than the rate itself. Such a procedure is directly analogous (for rates) to the traditional representation of cross sections as a value times an "S-factor" that contains the zeroth-order Coulomb penetration function. Indeed, the low-temperature behavior of the analytic fit function is precisely that of a reaction rate calculated with a constant S-factor. Typical accuracy achieved at nontabulated grid points is better than 10% at temperatures where the rate is important.

APPENDIX B

POPULATION OF GROUND AND ISOMERIC STATE IN ¹⁸⁰Ta

The ground state of ¹⁸⁰Ta has $J^{\pi} = 1^+$, whereas the isomeric state is a $J^{\pi} = 9^-$ state. Because of the spin and parity assignments, the isomeric state cannot directly decay into the ground state, but when the nucleus is thermally excited, it can be depopulated via an intermediate state that lies above the isomeric state. The temperature-dependent half-life derived in Belic et al. (2000) is based on the condition that the nucleus is in thermal equilibrium with the photon bath at a given temperature. In an explosive scenario ¹⁸⁰Ta is produced at a temperature sufficiently high to provide thermal equilibrium. During freezeout the populations of the states will remain in equilibrium as long as the temperature is high enough to sufficiently feed the ground state. Below a critical temperature T^{crit}, the de-excitation of the isomeric state will not be fast enough to compensate for the decay of the ground state and the isotope drops out of equilibrium. From that moment isomer and ground states have to be considered as two distinct species. Therefore, we have to take the population ratio at the lowest temperature (i.e., T^{crit}) before equilibration ceases in order to determine how much ^{180m}Ta actually remains.

A time-dependent calculation of the transition probabilities and the speed of the process is very involved. However, an estimate of T^{crit} can be found by using the result of Belic et al. (2000). The effective half-life curve (Fig. 4 in that paper) shows three different regimes: (1) at $T_9 > 0.35$ the states are fully equilibrated and the effective half-life is essentially the half-life of the ground state; (2) at $T_9 < 0.15$ the two states are fully decoupled and the contribution of the ground state to the effective halflife is negligible; and (3) the intermediate region with $0.15 \le T_9 \le 0.35$ is a transitional region in which the communication between the two states quickly ceases and equilibrium is not well established.

In thermal equilibrium the population P_{iso} of the isomer relative to the ground state is given by

$$P_{\rm iso} = \frac{(2J_{\rm iso} + 1)\exp(-E_{\rm iso}/kT)}{(2J_{\rm gs} + 1)} = \frac{19}{3}e^{-0.8738/T_9} .$$
(B1)

The effective decay rate is given by

$$\lambda_{\rm eff} = \lambda_{\rm gs} + P_{\rm iso}\lambda_{\rm iso} \;. \tag{B2}$$

Thus, for $T_9 = T_9^{\text{crit}} = 0.35$ there would be about 0.52 times more ^{180m}Ta than ^{180g}Ta; i.e., we have to divide the final total abundance of ¹⁸⁰Ta by 3 to get the surviving abundance of the isomer.

In order to get proper amounts of ^{180g}Ta and ^{180m}Ta, one would have to know how much time is spent in the intermediate region. If that region is covered quickly, it should be safe to take $T_9^{\text{crit}} = 0.35$. A choice of $T_9^{\text{crit}} = 0.4$ appears reasonable to compensate for neglecting the intermediate phase and any additional production in that phase. This would lead to a relative

abundance of $P_{\rm iso} = 0.71 P_{\rm gs}$. The temperature $T_9^{\rm crit}$ at which equilibrium is left does not strongly depend on the ground-state half-life. The largest uncertainty comes from the excitation energy of the intermediate state, which is not well determined experimentally. However, based on the Belic et al. (2000) results, we can assume an upper limit of ^{180m}Ta to be half of the ¹⁸⁰Ta produced in our models, and an educated guess would be between 0.3 and 0.5 of the produced 180 Ta.

REFERENCES

Arnould, M. 1976, A&A, 46, 117 Bao, Z. Y., Beer, H., Käppeler, F., Voss, F., Wisshak, K., & Rauscher, T. 2000, At. Data Nucl. Data Tables, 76, 70

Anders, E., & Grevesse, N. 1989, Geochim. Cosmochim. Acta, 53, 197

Angulo, C., et al. 1999, Nucl. Phys. A, 656, 3 Arnett, W. D., Bahcall, J. N., Kirshner, R. P., & Woosley, S. E. 1989, ARÁ&A, 27, 629

Bao, Z. Y., & Käppeler, F. 1987, At. Data Nucl. Data Tables, 36, 411

- Bazan, G., & Arnett, D. 1994, ApJ, 433, L41
- Belic, D., et al. 2000, Phys. Rev. Lett., 83, 5242
- Buchman, L. 1996, ApJ, 468, L127 Burrows, A., Hayes, J., & Fryxell, B. A. 1995, ApJ, 450, 830
- Caughlan, G. A., & Fowler, W. A. 1988, At. Data Nucl. Data Tables, 40,
- Clayton, D. D. 1968, Principles of Stellar Evolution and Nucleosynthesis (New York: McGraw-Hill) Costa, V., Rayet, M., Zappalà, R. A., & Arnould, M. 2000, A&A, 358, L67 Cowan, J. J., Cameron, A. G. W., & Truran, J. W. 1985, ApJ, 294, 656 El Eid, M., & Champagne, A. 1995, ApJ, 451, 298 Fowler, W. A., Caughlan, G. R., & Zimmermann, B. A. 1975, ARA&A,

- 13,69
- 13, 69 Freiburghaus, C., Rembges, F., Rauscher, T., Kolbe, E., Thielemann, F.-K., Kratz, K.-L., Pfeiffer, B., & Cowan, J. J. 1999, ApJ, 516, 381 Fryer, C. L., & Heger, A. 2000, ApJ, 541, 1033 Fuller, G. M., Fowler, W. A., & Newman, M. J. 1980, ApJS, 42, 447 ________. 1982a, ApJ, 252, 715 _________. 1982b, ApJS, 48, 279 ________. 1985, ApJ, 293, 1 Fülöp, Zs., et al. 1996, Z. Phys. A, 355, 203 Giessen, U., et al. 1994, Nucl. Phys. A, 567, 146 Görres, J., Wiescher, M., & Rolfs, K. 1989, ApJ 343 365

- Görres, J., Wiescher, M., & Rolfs, K. 1989, ApJ, 343, 365 Hansper, V. Y., Tingwell, C. I. W., Tims, S. G., Scott, A. F., & Sargood, D. G. 1989, Univ. Melborne School of Physics preprint UM-P-89/30
- Harris, M. J., Fowler, W. A., Caughlan, G. R., & Zimmermann, B. A. 1983, ARA&A, 21, 165
- Heger, A., Jeannin, L., Langer, N., & Baraffe, I. 1997, A&A, 327, 224
 Heger, A., Langanke, K.-H., Martinez-Pinedo, G., & Woosley, S. E. 2000a, Phys. Rev. Lett., 86, 1678
 Heger, A., Langer, N., & Woosley, S. E. 2000b, ApJ, 528, 368
 Heger, A., Woosley, S. E., Martinez-Pinedo, G., & Langanke, K.-H. 2001, ApJ, 560, 307

- Herant, M., Benz, W., Hix, R. J., Fryer, C., & Colgate, S. A. 1994, ApJ, 435, 339
- Hillebrandt, W., Thielemann, F. K., Klapor, H. V., & Oda, T. 1981, A&A, 99.195
- Hoffman, R. D., Woosley, S. E., Fuller, G., & Meyer, B. S. 1996, ApJ, 460, 478
- Hoffman, R. D., Woosley, S. E., & Weaver, T. A. 2001, ApJ, 549, 1085 Holmes, J., Woosley, S. E., Fowler, W. A., & Zimmerman, B. 1976, At.
- Itomics, J., Woostey, S. E., Powiel, W. A., & Zimmerman, B. 19/6, At. Data Nucl. Data Tables, 18, 305
 Iglesias, C. A., & Rogers, F. J. 1996, ApJ, 464, 943
 Iliadis, C., D'Auria, J., Sumner, S., Thompson, W., & Wiescher, M. 2001, ApJS, 134, 151

- Imbriani, G., Limongi, M., Gialanella, L., Terrasi, F., Straniero, O., & Chieffi, A. 2001, ApJ, 558, 903
 Itoh, N., Hayashi, H., Nishikawa, A., & Kohyama, Y. 1996, ApJS, 102,
- 411
- Jaeger, M., Kunz, R., Mayer, A., Hammer, J. W., Staudt, G., Kratz, K.-L., & Pfeiffer, B. 2001, Phys. Rev. Lett., 87, 201803
- Janka, H.-T. 2001, A&A, 368, 527

- Janka, H.-1. 2001, A&A, 368, 527
 Janka, H.-T., & Müller, E. 1996, A&A, 306, 167
 Käppeler, F., et al. 1994, ApJ, 437, 396
 Kiener, J., et al. 1993, Nucl. Phys. A, 552, 66
 Kratz, K.-L., et al. 1993, ApJ, 403, 216
 Kunz, R., Fey, M., Jaeger, M., Mayer, A., Hammer, J. W., Staudt, G., Harissopulos, S., & Paradellis, T. 2002, ApJ, 567, 643
 Kunz, R., Jaeger, M., Mayer, A., Hammer, J. W., Staudt, G., Harissopulos, S., & Paradellis, T. 2001, Phys. Rev. Lett., 86, 3244
 Landré V. Prantzos, N. Auger, P. Boragett G. Lefebyre, A. & Thibaud
- Langanke, K.-H., & Martínez-Pinedo, G. 2000, Nucl. Phys. A, 673, 481
- Limongi, M., Straniero, O., & Chieffi, A. 2000, ApJS, 129, 625

- Mezzacappa, A., Calder, A. C., Bruenn, S. W., Blondin, J. M., Guidry, M. W., Strayer, M. R., & Umar, A. S. 1998, ApJ, 495, 911
 Mitchell, L. W., Kavanagh, R. W., Sevior, M. E., Tingwell, C. I. W., & Sar-
- good, D. G. 1985, Univ. Melborne School of Physics preprint UM-P-85/
- Möller, P., Nix, J. R., & Kratz, K.-L. 1997, At. Data Nucl. Data Tables, 66, 131
- Morton, A. J., Tims, S. G., Scott, A. F., Hansper, V. Y., Tingwell, C. I. W., & Sargood, D. G. 1992, Nucl. Phys. A, 537, 167 Myra, E. S., & Burrows, A. 1990, ApJ, 364, 222
- Nieuwenhuijzen, H., & de Jager, C. 1990, A&A, 231, 134
- Prantzos, N., Hashimoto, M., & Nomoto, K. 1990, A&A, 234, 211 Rauscher, T., Applegate, J. H., Cowan, J. J., Thielemann, F.-K., & Wiescher, M. 1994, ApJ, 429, 499
- Rauscher, T., Hoffman, R. D., Heger, A., & Woosley, S. E. 2001, Nucl. Phys. A, 688, 193
 Rauscher, T., & Thielemann, F.-K. 1998, in Stellar Evolution, Stellar Explosions, and Galactic Chemical Evolution, ed. A. Mezzacappa (Bristol: IOP), 483
 - . 2000, At. Data Nucl. Data Tables, 75, 1 . 2001, At. Data Nucl. Data Tables, 79, 47
- Rauscher, T., Thielemann, F.-K., Görres, J., & Wiescher, M. C. 2000, Nucl. Phys. A, 675, 695
- Rauscher, T., Thielemann, F.-K., & Kratz, K.-L. 1997, Phys. Rev. C, 56, 1613
- Rauscher, T., Thielemann, F.-K., & Oberhummer, H. 1995, ApJ, 451, L37
- Rayet, M., Arnould, M., Hashimoto, M., Prantzos, N., & Nomoto, K. 1995, A&A, 298, 517
- Rayet, M., Arnould, M., & Prantzos, N. 1990, A&A, 227, 271

- Kayet, M., Ahloud, M., & Pfallzos, N. 1990, A&A, 227, 271
 Schaller, G., Schaerer, D., Meynet, G., & Maeder, A. 1992, A&AS, 96, 269
 Scott, A. F., Morton, A. J., Tims, S. G., Hansper, V. Y., & Sargood, D. G. 1992, Univ. Melborne School of Physics preprint UM-P-92/16
 Scott, A. F., Morton, A. J., Tingwell, C. I. W., Tims, S. G., Hansper, V. Y., & Sargood, D. G. 1991, Nucl. Phys. A, 523, 373
 Sevior, M. E., Mitchell, L. W., Tingwell, C. I. W., & Sargood, D. G. 1986, Nucl. Phys. A 454, 128
- Nucl. Phys. A, 454, 128 Somorjai, E., et al. 1998, A&A, 333, 1112
- Thielemann, F.-K., Arnould, M., & Truran, J. 1987, in Advances in Nuclear Astrophysics, ed. E. Vangioni-Flam (Gif sur Yvette: Editions Frontière), 525
- Thielemann, F.-K., et al. 1995, Reaction Rate Library REACLIB
- Thielemann, F.-K., Vian, 1995, Reaction Rate Elotaly REACED The Thielemann, F.-K., Nomoto, K., & Hashimoto, M. 1996, ApJ, 460, 408 Timmes, F. X., Hoffman, R. D., & Woosley, S. E. 2000, ApJS, 129, 377 Timmes, F. X., Woosley, S. E., & Weaver, T. A. 1995, ApJS, 98, 617 Truran, J. W., Cowan, J. J., & Cameron, A. G. W. 1978, ApJ, 222, 63

- Tuli, J. K., et al. 1995, Nuclear Wallet Charts (5th ed.; Brookhaven National Laboratory)

- National Laboratory) Weaver, T. A., & Woosley, S. E. 1993, Phys. Rep., 227, 65 Weaver, T. A., Zimmermann, G. B., & Woosley, S. E. 1978, ApJ, 225, 1021 Wiescher, M., & Kettner, K.-U. 1982, ApJ, 263, 891 Winters, R. R., & Macklin, R. L. 1988, ApJ, 329, 943 Woosley, S. E. 1988, ApJ, 330, 218 Woosley, S. E., Fowler, W. A., Holmes, J. A., & Zimmerman, B. A. 1978, At. Data Nucl. Data Tables, 22, 371 Woosley, S. E., Heger, A., & Weaver, T. A. 2002, Rev. Mod. Phys., in press Woosley, S. E., Hoffman, R. D., Hartmann, D., & Haxton, W. 1990, ApJ, 356, 272

- Wrean, P. R., Brune, C. R., & Kavanagh, R. W. 1994, Phys. Rev. C, 49, 2, 1205

Landré, V., Prantzos, N., Aguer, P., Bogaert, G., Lefebvre, A., & Thibaud, J. P. 1990, A&A, 240, 85