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Numerical Approximation of Hyperbolic Systems of Conservation Laws

With 75 Illustrations



Springer

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