Numerical Modelization of the Flow in Centrifugal Pump: Volute Influence in Velocity and Pressure Fields

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A 3D-CFD simulation of the impeller and volute of a centrifugal pump has been performed using CFX codes. The pump has a specific speed of 32 (metric units) and an outside impeller diameter of 400 mm. First, a 3D flow simulation for the impeller with a structured grid is presented. A sensitivity analysis regarding grid quality and turbulence models were also performed. The final impeller model obtained was used for a 3D quasi-unsteady flow simulation of the impeller-volute stage. A procedure for designing the volute, the nonstructured grid generation in the volute, and the interface flow passage between the impeller and volute are discussed. This flow simulation was carried out for several impeller blades and volute tongue relative positions. As a result, velocity and pressure field were calculated for different flow rates, allowing to obtain the radial thrust on the pump shaft.

Keywords and phrases: CFD, centrifugal pump, unsteady flow, radial thrust.

1. INTRODUCTION

The design of radial- and mixed-flow centrifugal pumps remains still very empirical because it relies on the use of a number of experimental and statistical rules. However, except for the principal dimensions, this fact is rather logical since the selection of a large number of second-order parameters must be done in order to define the complete impeller and volute geometry. This choice is often guided by several optimization criteria such as uniform flow, low machine footprint, stable characteristic curves, and performance improvement (efficiency, NPSH, noise, pressure fluctuations, etc.). During the last few years, the design and performance analysis of turbomachinery have experienced great progress due to the joint evolution of computer power and the accuracy of numerical methods.

Recently, several authors (Paßrucker and Van den Braembussche [1]; Cravero [2]; Sloteman et al. [3]; Goto et al. [4]) have proposed integral procedures to design and analyze turbomachines combining different computational

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tools. Mostly, these procedures combine a one-dimensional (1D) performance analysis method with a quasi-threedimensional (Q-3D) method to verify the optimum pump geometry. The optimum geometry has been validated using 3D CFD flow simulations, concluding the effectiveness and the importance of the 1D and Q-3D approaches on pump design.

1.1. CFD in the turbomachinery

The CFD occupies today a very significant place in the disciplines of fluid mechanics and turbomachinery due to the great progress in the development of numerical methods and computing power. However, the initially use of CFD tools to design a new machine represents a nonrealistic procedure (see Arnone et al. [5]). The design of a new machine (or upgrading an existing machine) would require a great investment of time without guarantee of success. Along with the introduction of CFD tools, the incorporation of computeraided design (CAD) codes has speeded up the design process because of a faster geometry and grid generation (see Asuaje et al. [6]). Nevertheless, the problem always reduces down to the selection of reasonable values for a number of geometric parameters. At this point, the "know-how," skills and talent of the designer remain the principal ingredients for designing and optimizing a machine (see Yedidiah [7]).

1D and Q-3D approaches to design and analyze turbomachines can be considered well adapted and powerful enough for most applications. However, for designing a highperformance pump, it is necessary to accurately determine the internal flow in the pump. Results from the literature regarding CFD show a good correspondence with experimental results. Blanco-Marigorta et al. [8] have studied the influence of the volute geometry and relative position between impeller and volute casing. They performed a 2D unsteady flow simulation in centrifugal pump (ns = 30) using the commercial code FLUENT.

González et al. [9] continued the preceding study towards the 3D simulation. A very satisfactory comparison between calculations and experimental results is presented (see Parrondo-Gayo et al. [10])

Several others' works (Gu et al. [11]; Muggli et al. [12]; Cravero and Marini [13]) have shown good agreement between simulation and experimental results.

If 3D techniques keep growing in power and help to understand the 3D flow behavior in the machine, the design cycle of turbomachinery will be closed with the construction and testing of a prototype. The purpose of the present paper is to show a 3D numerical study of a centrifugal pump. Simulations have been done with the commercial CFD software CFX-TASCflow 2.12 and CFX 5.5.

2. IMPELLER 3D FLOW SIMULATION

A 3D CFD flow simulation was carried out on an isolated impeller of a mixed-flow centrifugal pump with specific speed of 32 (impeller NS32). The main pump parameters and geometry are presented in Figure 1 and Table 1.



FIGURE 1: Visualization 3D of NS32 impeller.

TABLE 1: Geometrical parameters of the pump $N_S = 32$.

Pump NS32. MP 250-200-400						
Parameter	Value	Description				
Impeller						
R_0	115 mm	Inlet flange radius				
R_1	75 mm	Mean impeller inlet radius				
b_1	85.9 mm	Inlet impeller width				
β_1	70°	Inlet blade angle				
$ heta_1$	37°	Blade LE inclination angle				
R_2	204.2 mm	Mean impeller outlet radius				
b_2	42 mm	Outlet impeller width				
β_2	63°	Outlet blade angle				
θ_2	90°	Blade TE inclination angle				
Na	5	Blade number				
е	8 mm	Blade thickness				
Volute						
<i>R</i> ₃	218 mm	Base volute radius				
b_3	50 mm	Volute width				
$\phi_{ m outlet}$	200 mm	Outlet flange diameter				

The first task to accomplish on a numerical flow simulation is the definition of the geometry, followed by the grid generation. This step is maybe the most important step in this work. For the study of an isolated impeller, assuming an axisymmetric flow simplifies the domain to a single blade passage. The simulation domain for the impeller pump NS32 is schematized in Figure 2. A structured grid was created using the CFX-Turbogrid software.

2.1. Simulation parameters and boundary conditions

The general parameters and boundary conditions used for the 3D flow simulation of the impeller are summarized in Table 2.

For all simulations, the boundary conditions are as follows.

- (i) Inlet: total pressure applied in the rotation axis direction.
- (ii) Outlet: imposed mass flow.



FIGURE 2: Impeller NS32: flow simulation domain and structured grid.

TABLE 2: Impeller NS32: simulation parameters.

Parameters	CFX-TASCflow				
Flow simulation domain	Single impeller flow channel				
Flow simulation domain	(periodic interface)				
Grid	Structured				
Fluid	Water at standard conditions				
Inlet	Total pressure = 101 325(Pa)				
Outlet	Mass flow = variable (kg/s)				
Turbulence model	$K - \varepsilon/K - \omega/SST$				
Discretization	Second order				
Maximum residual convergence	$10^{-4}(DSM)$				
Criteria	10 (K3IVI)				

- (iii) Periodic: two symmetry surfaces positioned in the middle of the blade passage.
- (iv) Wall: general boundary condition by default.

The simulation domain at the inlet and outlet sections was sufficiently extended to allow inlet recirculation and the elliptic influence of the flow.

2.2. Mesh independence

Theoretically, the errors in the solution related to the grid must disappear for an increasingly fine mesh (see Ferziger and Péric [14]). The pump head at nominal flow conditions was taken as the parameter to evaluate seven grids (Table 3) and determine the influence of the mesh size on the solution. The selected convergence criteria were a maximum residual of 10^{-4} . In Figure 3, it is observed how the calculated impeller head reaches an asymptotic value as the number of nodes increases. According to this figure, the grid *E* (49 824 nodes) is considered to be sufficiently reliable to ensure mesh independence.

Looking further into the mesh size influence, Figures 4 and 5 present the meridional velocity profile at the leading

TABLE 3: Evaluated grid sizes.

Characteristics	Number of nodes				
Grid A	10 879				
Grid B	19 097				
Grid C	28 905				
Grid D	41 174				
Grid E	49 824				
Grid F	79 065				
Grid G	101 637				



FIGURE 3: Influence of grid size on impeller head.

and trailing edges of the blade, as a function of the number of nodes. The evolution of the velocity profile at the trailing edge confirms the previous result. A good convergence can be only achieved with a grid size which is equal to or higher than the grid *E*.

2.3. Turbulence models

Three criteria influence the choice of a turbulence model: (1) the physical nature of the problem, (2) the quality of attended



FIGURE 4: Influence of grid size on the meridional velocity at the leading edge of the blade: CFX-TASCflow code and impeller NS32.



FIGURE 5: Influence of grid size on the meridional velocity at the trailing edge of the blade: CFX-TASCflow code and impeller NS32.

results, and (3) computing power (see Bradshaw [15]). Depending on the flow complexity, this choice is always crucial when using CFD codes. Nevertheless, the traditional RANS models, like $\kappa - \varepsilon$ or $\kappa - \omega$, are widely used and yield satisfactory results.

According to the flow complexity, this choice is always a delicate point for the use of CFD codes. Nevertheless, the traditional RANS models, like $\kappa - \varepsilon$ or $\kappa - \omega$, are amply used and produce satisfactory results.

The models $\kappa - \varepsilon$, $\kappa - \omega$, and *SST* were evaluated in the impeller flow simulation, under similar conditions and for the nominal flow rate of the pump. This part of the study



FIGURE 6: Influence of turbulence model on the calculated pump head.

was carried out on mixed-flow impeller by using the grid *E*, with a maximum residue lower than or equal to 10^{-4} .

Figure 6 shows the influence of the three turbulence models on the calculated pump head. The calculated head H varies very slightly (less than 0.02%).

The same tendency is observed in Figures 7 and 8, where no significant influence of the turbulence model on the meridional velocity field and velocity profile near the wall is observed.

3. IMPELLER-VOLUTE 3D QUASI-UNSTEADY FLOW SIMULATION

The 3D views of the impeller, volute casing, and impellervolute assembly are shown in Figure 9.

The volute-casing skeleton was imported by the preprocessor of CFX-5 (CFX-Build) to build the surfaces and volumes of the volute. After this process was conducted, the grid generation was completed. Figure 10 shows the three steps to generate the grid of the volute casing.

The original configuration of the outlet volute casing was modified in order to avoid the occurrence of a big recirculation in that area. The extension of the volute outlet is essential for numerical and physical reasons, since convergence problems and related flow instabilities are prevented if the swirling zone is captured into the simulation domain.

As it will be shown later, another swirling zone appears in the impeller inlet for flow rates lower than the rates corresponding to the best efficiency point. For this reason, it was also necessary to extend the impeller inlet upstream (see Figure 11).

Due to the change between the reference frame of the rotating impeller and static volute casing, the interaction of impeller volute has been simulated using the Frozen-Rotor



FIGURE 7: Influence of turbulence model on the meridional velocity field.



FIGURE 8: Influence of turbulence model on the velocity profile at the trailing of the blade.



FIGURE 9: 3D elements of the pump NS32.

interface model. In this model, the simulation is performed for a determined relative position of the machine components, then this relative position is changed step by step in a quasi-unsteady calculation.



FIGURE 10: Grid generation steps of pump-volute casing NS32.



FIGURE 11: Definition of flow simulation domain showing extend of inlet and outlet sections.

For the pump studied, nine relative positions have been analyzed starting at the position of $\alpha = 0^{\circ}$ named position



FIGURE 12: Relative positions between blade trailing edge and volute tongue.

flow rate ratio	α								
now rate ratio	0°	8°	16°	24°	32°	40°	48°	56°	64°
0.5									
0.7									
0.8									
0.9									
1.0									
1.2									
1.4									

TABLE 4: Matrix of proposed quasi-unsteady flow simulations.

zero. The remaining relative positions correspond to an impeller rotation $\Delta \alpha = 8^{\circ}$ (see Figure 12). The matrix of the performed simulations is shown in Table 4.

The general simulation parameters for the impellervolute assembly are summarized in Table 5.

The CFD simulation offers a virtual image of the internal flow in the machine allowing the analysis and comprehension of more complex phenomena. The flow is strongly influenced by the asymmetry introduced by the volute casing and the volute tongue position. First, the flow field at the mean plane, normal to the rotating axis (rotational plane), is presented for the BEP flow rate of the pump. The velocity vectors in the impeller (relative vector) and volute casing (absolute vector) are shown in Figure 13 for $\alpha = 0^{\circ}$. Although there is a good guidance of the flow in the volute, a strong recirculation zone appears at the volute diverging outlet. Inside the impeller, the flow velocities are relatively uniform for all blade passages. This behavior was observed for all analyzed relative positions.

Figure 14 shows the static pressure field at the mean rotational plane. Even though the effect of the volute tongue is appreciable, a relatively uniform pressure distribution is obtained around the impeller. This tendency was also obtained for different positions of the impeller (see Figures 15 and 16). TABLE 5: Impeller-volute assembly simulation parameters.

Parameter	CFX-5				
Domain of simulation	Whole impeller (5 blade				
Domain of simulation	passages) + volute				
Extended inlet duct grid	Unstructured 104 973 node				
Impeller grid	Structured 355 225 nodes				
Volute casing grid	Unstructured 217 753 node				
Inlet	Total pressure = 101 325 Pa				
Interface duct / impeller	Frozen rotor				
Interface impeller / volute	Frozen rotor				
Outlet	Mass flow				
Turbulence model	$\kappa - \varepsilon$				
Discretization	Second order				



FIGURE 13: Velocity vectors of pump NS32 at the best efficiency point $(Q/Q_{bep} = 1)$ and $\alpha = 0^{\circ}$.



FIGURE 14: Static pressure field of pump NS32 at the best efficiency point $(Q/Q_{bep} = 1)$ and $\alpha = 0^{\circ}$.

The impeller-volute interaction is evidenced by a nonuniform pressure distribution at the impeller periphery. The static pressure distribution for the pump BEP flow rate and



FIGURE 15: Static pressure field of pump NS32 at the best efficiency point $(Q/Q_{bep} = 1)$ for different relative positions of impeller-volute tongue.

 $\alpha = 0^{\circ}$ is presented in Figure 17. The pressure pulsation amplitudes reach 27% of the mean pressure generated by the impeller.

Figures 18 and 19 show the influence of the pump flow rate on flow kinematics. In Figures 18 and 19, the velocity and pressure fields for different pump capacities (0.5 Q_{bep} , 0.8 Q_{bep} , 1.0 Q_{bep} , and 1.2 Q_{bep}) and $\alpha = 0^{\circ}$ are shown.

For the BEP flow rate, the fluid is well conducted by the volute leading to a uniform operation of the impeller. There are not large differences in the velocity and pressure fields for the various blade passages. On the other hand, a more significant variation in velocity and pressure is observed when the pump operates off the best efficiency point.

For flow rates larger than that at BEP, the blade passage arriving at the volute tongue undergoes a strong pressure drop (see Figure 20). Therefore, this area favors the appearance of cavitation. This phenomenon has been reported in the literature by Bakir et al. [16] and Kouidri et al. [17].

The opposite occurs for partial pump capacities. The blade passage leaving the volute tongue experiences the largest pressure gradient. This effect is hardly noticeable when the pump flow rate is reduced to 0.8 Q_{bep} , but accentuated when the flow rate is reduced to 0.5 Q_{bep} .

3.1. Radial trust

The nonuniform pressure distribution around the impeller periphery is the origin of periodic loads causing the *radial trust*. This fundamental parameter affects the life cycle of the pump shaft and bearings as well as the vibration behavior of the machine. The pressure distribution around the impeller periphery is shown in Figure 21 for $\alpha = 0^{\circ}$ and different flow rates.

As expected, the weakest amplitudes pressure pulsation is found in the range BEP. For flow rates outside this range, $(0.5 Q_{bep} \text{ and } 1.4 Q_{bep})$ pressure pulsations are more significant and can reach up 50% of relative values.

The radial trust can be determined from the pressure distributions by carrying out the integration of the elementary forces around the impeller periphery (see Figure 22).

As a function of the angle θ , the elementary force is written as

$$dF(\theta) = p(\theta) \cdot dS \cdot \hat{n}.$$
 (1)



FIGURE 16: Static pressure field of pump NS32 at the best efficiency point $(Q/Q_{bep} = 1)$ for different relative positions of impeller-volute tongue.



FIGURE 17: Static pressure distribution at the impeller periphery, for $Q/Q_{\rm bep} = 1$ and $a = 0^{\circ}$.

The two Cartesian components of this force are

$$dF_x(\theta) = p(\theta) \cdot dS \cdot \cos \theta,$$

$$dF_y(\theta) = p(\theta) \cdot dS \cdot \sin \theta.$$
(2)

The components of the resulting force F_x and F_y are determined by the integrals

$$F_{x} = \int_{0}^{2\pi} dF_{x}(\theta) d\theta,$$

$$F_{y} = \int_{0}^{2\pi} dF_{y}(\theta) d\theta.$$
(3)

Finally, the resulting radial force is written

$$F = \sqrt{F_x^2 + F_y^2}.\tag{4}$$

The radial trust F has been calculated for different relative

Velocity Velocity 28 30 24 22 20 - 16 15 12 8 7.5 0 (ms^{-1}) (ms^{-1}) $Q/Q_{\rm bep} = 0.8$ $Q/Q_{\rm bep} = 0.5$ (a) (b) Velocity Velocity 24 24 18 18 12 12 6 6 0 (ms^{-1}) (ms^{-1}) $Q/Q_{\rm bep} = 1$ $Q/Q_{\rm bep}=1.2$ (c) (d)

FIGURE 18: Velocity field at different pump capacities.

positions, the results are presented in Figure 23. The direction and module of the radial force change according to the relative position between the impeller and volute tongue.

Figure 24 shows the amplitudes of the radial force as function of the pump flow rate for $\alpha = 0^{\circ}$. As it can be observed, this curve reaches a minimum at the BEP pump flow rate and the radial force values are comparable to those obtained by an empirical correlation suggested by Stepanoff [18].

4. CONCLUSIONS

In this research work, an integral procedure for the optimization of centrifugal pumps has been developed based on 3D quasi-unsteady flow simulation using CFX-TASCflow and CFX 5.5 codes.

The sensitivity study performed on the isolated impeller has shown two relevant aspects.

- (i) The numerical solution is stabilized with grids containing more than 40 000 nodes.
- (ii) All turbulence models used $(k \varepsilon, k \omega, k \omega, SST)$ gave almost identical results, for the same simulating conditions.

The impeller-volute assembly requires the addition of two extended computational domains; one at the impeller inlet and the other at the volute outlet. The Frozen-Rotor interface model (quasi-unsteady) is considered for the study of the impeller-volute assembly since it represents the best accuracy of computing time tradeoff.

Pressure Pressure $\times 10^3$ $\times 10^4$ 520 60 54 455 48 - 390 42 - 325 36 260 30 24 195 18 130 12 65 6 0 0 (Pa) (Pa) $Q/Q_{\rm bep} = 0.5$ $Q/Q_{\rm bep} = 0.8$ (a) (b) Pressure Pressure $\times 10^4$ $\times 10^4$ 45 50 45 40 40 - 35 35 - 30 - 30 25 - 25 20 - 20 15 - 15 10 - 10 5 5 0 0 (Pa) (Pa) $Q/Q_{\rm bep} = 1$ $Q/Q_{\rm bep} = 1.2$ (c) (d)

FIGURE 19: Pressure field at different pump capacities.



FIGURE 20: Experimental cavitation observation in two channels of impeller NS32 at capacity greater than that at the best efficiency point.

The main results of this study are the following.

 (i) The volute tongue causes an unsymmetrical flow distribution in the impeller. As a consequence, a nonaxisymmetric cavitation appears in some of the blade



FIGURE 21: Static pressure distribution at the impeller periphery, for different pump capacities ($\alpha = 0^{\circ}$).



FIGURE 22: Radial force integration around impeller periphery.



FIGURE 23: Module and direction of radial force at different pump capacities $(0.8Q_{bep}, 1.0Q_{bep}, and 1.2Q_{bep})$.

passages of the impeller. These results are corroborated by experiments conducted on a centrifugal pump tested in the LEMFI test loop.

(ii) A nonuniform pressure distribution develops at the impeller periphery as a function of the pump flow rate, causing a fluctuating radial thrust of significant amplitude.

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FIGURE 24: Radial thrust versus flow rate ratio, NS32 pump, $\alpha = 0^{\circ}$.

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