Numerical modelling of multicomponent LNAPL dissolution kinetics at residual saturation in a saturated subsurface system

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Characterization of aquifers contaminated by petroleum hydrocarbons is Abstract. limited by the use of dissolution mass transfer correlations developed for single compounds without considering the effects of the mass transfer limitations in presence of other components. A one-dimensional implicit numerical model is developed for the coupled mass transfer and transport processes and the results are analysed using existing mass transfer correlations for better understanding of the single and multicomponent dissolution processes. The mass transfer coefficient in the multicomponent system is found to be more nonlinear and extending with changing slope, unlike the exponential reduction for single compound system. During the initial phase, the dissolution rate of a soluble compound is very high due to the high concentration gradient, and as dissolution progresses, its effective solubility decreases with change in mole fraction. At higher pore volumes, the mole fractions of lower solubility fractions increase which can result in higher effective solubility. The kinetics of interphase mass transfer by dissolution and sorption is favoured by coupled biodegradation. However, mass transfer limitation for more soluble compounds under the conditions of low residual saturation and low mole fraction is observed to be due to low dissolution rate coefficient rather than decreasing concentration gradient.

Keywords. Multicomponent dissolution; numerical modelling; petroleum hydrocarbons; residual saturation.

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1. Introduction

Accidental spills and leakage of organic compounds such as petroleum hydrocarbons (PHC) are becoming the continuing source of subsurface contamination because of their inherent toxicity and partitioning tendency to various environmental compartments, especially to the aquifer material and ground water. Subsurface transport of these multicomponent organic compounds poses a significant threat to the quality of potential drinking water reservoir through continuous but slow release, finally reaching the water table, which can contribute to groundwater contamination for many decades (Kao & Prosser 2001; Ucankus & Unlu 2008). Following migration and subsequent removal of free phase liquid, still the organic compounds are present as entrapped non-aqueous phase liquid (NAPL) blobs occupying soil micro-pores, resulting in residual NAPL saturation, which serves as the source of mass transfer limited dissolution (Yang *et al* 1995; Johnson *et al* 2003; Liu *et al* 2007).

The complexity associated with dissolution mass transfer of organic compounds is closely related to their relative hydrophobic nature, distribution of the non-aqueous phase mass within the aquifer pore volume, prevailing flow and other geochemical properties of the porous medium (Saba & Illangasekare 2000; Soga *et al* 2004). Uniformly distributed non-aqueous phase PHC at residual saturation in homogeneous subsurface conditions are more conducive to contaminant removal compared to adverse heterogeneous conditions. It is well-established that there is considerable limitation on interphase mass transfer when the contributing residual contaminant is occupying small interfacial area or when the flushing fluid velocity is substantially high enough to reduce the residence time (Powers *et al* 1994; Hamed *et al* 2000; Keller & Sirivithiyapakorn 2000). Depending on the scale of the problem and mass transfer limitation considerations, various empirical mass transfer correlations were derived in terms of dimensionless numbers with suitable coefficients (Abriola 1989; Geller & Hunt 1993; Imhoff *et al* 1994; Mayer & Miller 1996; Kim & Chrysikopoulos 1999; Nambi & Powers 2000; Chu *et al* 2007; Liu *et al* 2007; Corapcioglu *et al* 2009).

Correlation developed by Nambi & Powers (2003) is well-suited for heterogeneous lab scale systems for wide range of initial NAPL saturation, especially for high initial NAPL saturations. Similarly, Schaerlaekens et al (2000) developed correlations with three and four parameters incorporating the effect of intermittent stopping of flow on mass transfer phenomena. The correlation by Powers et al (1994) which is widely referred for uniform residual saturation in a homogeneous porous media is, however, limited in application only to similar saturation conditions. The correlation by Imhoff et al (1994) is incorporating the effect of dissolution fingering in terms of relative domain size, suggest the effect of contamination history on mass transfer coefficient, but it is substantially poor in predicting the dissolution breakthrough for laboratory scale domain. These correlations are claimed to be capable of being up-scaled to different sized NAPL source zones, but it is not clear how these mass transfer correlations perform for the purpose of simulating NAPL dissolution coupled with geo-biochemical reactions. Seagren et al (1999) showed that dissolution is enhanced the most when the time scale of the first order reaction is shorter than that of purely physical dissolution. Also, the local diffusion length is reduced for the case of reaction-coupled dissolution when compared with that of no reaction. Moreover, since there is no term representing the effect of reaction on dissolution, studies on reaction-enhanced NAPL pool dissolution indicates that this assumption is questionable.

The dissolution behaviour exhibited by a particular compound when it is the sole occupant is not sufficient for understanding its behaviour when present in a mixture, because of the variation in the effective solubility in accordance with the NAPL composition and other possible interactions resulting in non-ideal behaviour of the mixture (Gonullu 1996; Powers *et al* 1994;

Mayer & Miller 1996; Garg & Rixey 1999; Keller & Sirivithiyapakorn 2000; Mobile et al 2012; Burke 2012). For the multicomponent system, the transient behaviour of the mass transfer coefficient pertaining to the variations in pore velocity and volumetric saturation is significant in addition to the variability in molecular diffusion of each component. Since the petroleum fuels contain multiple components with varying physical and chemical properties, the dissolved plume of individual components can spread at different rates in accordance to the difference in effective solubility as well as differential retardation caused by sorption, even though they occupy same pore volume (Borden & Piwoni 1992; Frind et al 1999; Prommer et al 2000; Hansen 2012; Vasudevan et al 2012). Several numerical investigations have been carried out using linear as well as nonlinear sorption isotherms in homogeneous as well as heterogeneous porous systems (Johnson et al 2003; Zhang & Brusseau 2004; Sekhar & Suresh Kumar 2006; Sekhar et al 2006; Suresh Kumar 2008; Suresh Kumar et al 2008; Suresh Kumar 2009; Natarajan & Suresh Kumar 2010; Renu & Suresh Kumar 2012; Suresh Kumar 2014). However, these properties are significant for the estimation of kinetic nature of dissolution from residually trapped sources since the interactions between various phases in the aquifer system are significant at the pore scale. In order to simulate the subsurface contamination scenario, numerical approach is preferred to handle nonlinearity constraints over simplified analytical solutions even though it is to be constructed to minimize the possible numerical error (Yang et al 1995; Molson 2000; Clement et al 2004; Chamkha 2007; Couto & Malta 2008; Sulaymon & Gzar 2011).

In the present study, we discuss the scenario of residually trapped non-aqueous phase petroleum hydrocarbons present at different residual saturation conditions with implications of modelling the fate and transport of aqueous concentration plume under coupled geo-biochemical reactions. The study also addresses the suitability of mass transfer correlation for modelling the dissolution process of individual components present in a mixture under the effect of coupled reactions. We also attempt to study the comparative effect of rate limitation on the dissolution mass transfer rate coefficient when the contaminant is present as single as well as in a mixture considering the complexity of physico-chemical reactions of the compounds involved.

2. Materials and methods

2.1 Physical system and governing equations

Since the flow through porous media is mainly restricted to the pore space around the immobile NAPL blobs and pore throats, there will be considerable variation in the average pore velocity. As the volume of the residual NAPL source decreases as a result of inter-phase mass transfer, there will be corresponding reduction in the interfacial area between the NAPL blob and surrounding aqueous phase. However, at the present scale of our model, the change in aqueous concentration at the downstream of the NAPL source is assumed to be not affected by the morphological change resulting from dissolution.

In order to model the contaminant plume distribution and evolution in the subsurface, the governing equation should include the effects of transport processes such as advection and dispersion, and reactive processes such as dissolution, adsorption and biodegradation. The ratelimited dissolution and sorption are represented here using first order kinetic expression, whereas the Monod equation for the biodegradation is having a mixed order. Further, in order to address the mass transfer limitations at the aqueous-soil interface, the sorption process is taken as a combination of equilibrium and kinetic processes, contributing to the surface properties of the porous media. Considering the overall effect of these mass transfer processes on the contaminant evolution within the domain, the transient transport of each dissolving component under steady-state uniform flow conditions is given by (Schaerlaekens *et al* 2000; Brauner & Widdowson 2001);

$$Ret \frac{\partial C_{a_i}}{\partial t} = D_{L_i} \frac{\partial^2 C_{a_i}}{\partial x^2} - v \frac{\partial C_{a_i}}{\partial x} + K_{wn_i} (C_{sat_i} - C_{a_i}) - K_m \left[(1 - f) k_{d_i} C_{a_i} - S_i \right] - \left[\frac{V_{\max_i} X_{a_i} C_{a_i}}{K_{s_i} + C_{a_i}} \right],$$
(1)

where *Ret* is the retardation factor due to equilibrium sorption (calculated asRet = $1 + f\rho_b k_d/\varphi$, where *f* is the fraction of equilibrium sorption sites [-], ρ_b is the bulk density of the aquifer material [ML⁻³], k_d is the linear partitioning coefficient [L³M⁻¹] and ϕ is the porosity [-]); C_{a_i} is the aqueous phase concentration of component *i* [ML⁻³]; D_{L_i} is the longitudinal dispersion coefficient [L²T⁻¹] (given by $D_{L_i} = D_{m_i} + \alpha_L v$, where D_{m_i} is the molecular diffusion coefficient of component *i* [L²T⁻¹] and α_L is the longitudinal dispersivity of the porous medium [L]); *v* is the mean fluid velocity [LT⁻¹] (calculated as $v = q/\varphi$, where *q* is the Darcy velocity [LT⁻¹]); K_{wn_i} represents the lumped mass transfer coefficient of transient dissolution for component *i* from non-aqueous phase to aqueous phase [T⁻¹]; C_{sat_i} is the effective solubility of component *i* in the multicomponent system [ML⁻³]; K_m is the sorption mass transfer rate parameter [T⁻¹], S_i is the sorbed phase contaminant concentration, [MM⁻¹]; V_{max_i} is the maximum specific substrate utilization rate [T⁻¹]; X_{a_i} is the aqueous phase biomass concentration [ML⁻³] and K_{s_i} is the half saturation constant [ML⁻³].

2.2 Dissolution kinetics for multicomponent system

The dissolution term in Eq. (1) accounts for the influence of film resistance at the interface, NAPL composition and the effective solubility of each component defined according to Raoult's law. Since it is extremely difficult to capture the details of intrinsic mass transfer coefficient and the effective normalized interfacial area between NAPL and aqueous phase at the pore-scale using experiments or field investigations, the above two parameters are lumped together as a single entity called the 'lumped mass transfer coefficient (K_{wn_i})', which represents the mean value over the Representative Elementary Volume (REV). Hence the term K_{wn_i} accounts for the combined effects of fluid flow, interfacial area at the contact surface, and molecular diffusion of each contaminant as given by Eq. (2). It is generally represented in terms of dimensionless numbers that can be easily linked with the Darcy flux (Powers *et al* 1994; Garg & Rixey 1999; Nambi & Powers 2003; Chu *et al* 2007; Mobile *et al* 2012).

$$K_{wn_i} = \frac{Sh'D_{m_i}}{d_p^2},\tag{2}$$

where Sh' is the modified Sherwood number [-] and d_p is mean particle size of the porous medium [L].

The progression over years has been to modify the mass transfer correlation by including many parameters in order to closely represent actual phenomena of inter-phase mass transfer. It has been reported that most of the mass transfer occurs through molecular diffusion from the NAPL blob to the external flowing fluid through narrow pore throats, which is also influenced by the flow and NAPL properties (Miller *et al* 1990; Imhoff *et al* 1994; Mayer & Miller 1996; Powers *et al* 1994; Nambi & Powers 2003; Corapcioglu *et al* 2009; Burke 2012). By realizing that NAPL is actually providing the transferred mass, not the solid phase of the porous medium, the inclusion of volumetric residual NAPL saturation (S_n) within the empirical correlation as an

exponential term seems to modify the determination of characteristic length. In order to compare the mass transfer kinetics, suitable mass transfer correlation are selected according to the range of volumetric residual NAPL content (θ_n , which is defined as $\theta_n = \varphi S_n$) and Reynolds number (*Re*), as mentioned in table 1.

The concept of residual saturation will serve as the identity for multicomponent scenario because all of them occupy the same pore volume represented by the residual saturation (Hamed *et al* 2000; Carroll & Brusseau 2009, Mobile *et al* 2012). But the change in mole fraction influences the effective solubility as well as the remaining mass distribution in the NAPL phase, which in turn affect the dissolution mass transfer coefficient. It is observed that depending on the initial composition and spilled volume, methodology for estimating the effective solubility varies considerably (Borden & Piwoni 1992; Feenstra 1997; Frind *et al* 1999; McCray & Dugan 2002). In this regard, for the present scenario of known initial spilled volume and known composition, the following approach is used for estimating the change in NAPL saturation with the effect of change in mole fraction of each component.

Step 1: Initial volume of the NAPL mixture,

$$V_n = \varphi V_T S_n,\tag{3}$$

where V_T is the total volume of domain [L³]; S_n is the residual saturation of NAPL [-].

Step 2: Total moles of all components initially present,

$$m_t = \frac{V_n}{\sum\limits_{i=1}^k \frac{X_{n_i} W_i}{\rho_{n_i}}},\tag{4}$$

where k is the total number of components in the NAPL mixture [-]; X_{n_i} is the mole fraction of the component *i*; W_i is the molecular weight of each component *i* [Mmol⁻¹] and ρ_{n_i} is the liquid density of each component *i* [ML⁻³].

Step 3: Initial mass of component 'i' in NAPL phase,

$$M_{n_i} = X_{n_i} m_t W_i. ag{5}$$

Step 4: Volume of pore water,

$$V_w = \varphi V_T - V_n. \tag{6}$$

Step 5: The number of pore volume during each time step,

$$N_{PV} = \frac{q\,\Delta t}{L\varphi S_a},\tag{7}$$

Table 1. Selected mass transfer correlations for the study, with their range of parameters.

Mass transfer correlation	Notation	Range of θ_n	Range of Re	Reference
$Sh' = 37.15 \text{Re}^{0.61} S_n^{1.24}$	MTC # 1	0-0.168	0.018-0.134	Nambi & Powers (2003)
$Sh' = 150 \text{Re}^{0.87} \theta_n^{0.79}$	MTC # 2	0-0.04	0.0012-0.021	Imhoff <i>et al</i> (1994)
$Sh' = 150 \text{Re}^{0.87} \theta_n^{0.79}$ $Sh' = 6.25 \text{Re}^{0.56} \theta_n^{0.64}$	MTC # 3	0-0.09	0.013-0.05	Schaerlaekens et al (2000)
$Sh' = 340 \operatorname{Re}^{0.71} \theta_n^{0.87} \left(\frac{x}{d_{50}}\right)^{-0.31}$	MTC # 4	0-0.04	0.0012-0.021	Imhoff <i>et al</i> (1994)

where L is the length of domain [L], Δt is the time step [T] and S_a is volumetric water saturation [-].

Step 6: Mass of component '*i*' added to the aqueous phase (i.e., removed from non-aqueous phase) during each time step,

$$M_{a_i} = C_{a_i} V_w N_{pv} \tag{8}$$

Step 7: Mass of component 'i' remaining in NAPL phase,

$$M_{n,new_i} = M_{n_i} - M_{a_i}. (9)$$

Step 8: Total number of moles in the NAPL phase for new time step,

$$m_{t,new} = \sum_{i=1}^{k} \left(\frac{M_{n,new_i}}{W_i} \right).$$
(10)

Step 9: NAPL phase mole fraction for new time step,

$$X_{new\,i} = \left(\frac{M_{n,new_i}}{m_{t,new_i}W_i}\right).\tag{11}$$

Step 10: New effective solubility,

$$C_{sat_i} = C_{sat_i}^0 X_{new_i}.$$
 (12)

where $C_{\text{sat}i}^{\text{o}}$ is the pure phase solubility of component *i* in aqueous phase [ML⁻³]. Step 11: Available NAPL volume for next time step,

$$V_{n,new} = \sum_{i=1}^{k} \left(\frac{M_{n,new_i}}{\rho_{n_i}} \right).$$
(13)

Step 12: New NAPL saturation,

$$S_{n,new} = \frac{V_{n,new}}{\varphi V_T}.$$
(14)

Step 13: New volumetric NAPL content,

$$\theta_{n,new} = \varphi S_n. \tag{15}$$

Step 14: Dissolution mass transfer term is updated based on the new values of volumetric NAPL content θ_n as well as effective solubility C_{sat_i} .

Step 15: Value of NAPL volume $V_{n,new}$ from step 11 will be updated in step 1.

Step 16: Value of mole fraction, X_{new_i} from step 9 will be updated in step 2.

Step 17: Value of NAPL mass remaining is checked for accuracy between step 7 and step 3 during every interval.

Generally, mass transfer of sorbing solutes may be affected by physical or chemical nonequilibrium resulting in delay in concentration breakthrough as well as tailing effect (Wang 2004; Couto & Malta 2008). When the partitioning of dissolved contaminants between the solid and liquid phases is assumed to be rate-limited, the simulated concentration results in intermediate stages of retardation (Clement *et al* 1998). The value of the linear partitioning coefficient (k_d) can be calculated from the fraction of organic carbon (f_{oc}) and soil organic carbon partitioning coefficient (k_{oc}) as given by $k_d = f_{oc}k_{oc}$. The sorbed phase concentration is obtained by the following mass balance equation (Clement *et al* 2004);

$$\frac{\rho_n}{\varphi} \frac{\partial S_i}{\partial t} = K_m \left[(1 - f) k_{d_i} C_{a_i} - S_i \right].$$
(16)

In order to investigate the bioremediation potential of organic pollutants, aerobic biodegradation conditions in the saturated aquifer were studied in relation with sorption effects (Kim *et al* 2003; Couto & Malta 2008; Yadav & Hassanizadeh 2011). One of the primary reasons for enhanced dissolution is that it increases the concentration gradient at the interface, which increases the bio-availability of the compounds for the safe clean-up of the contaminated site (Bekins *et al* 1998; Clement *et al* 2004; Chu *et al* 2007; Diplock *et al* 2009). Based on the Monod kinetics for the mixed-order biodegradation reaction, concentration of the immobile biomass concentration was given by Bekins *et al* (1998):

$$\frac{\partial X_{a_i}}{\partial t} = \frac{Y V_{\max_i} X_{a_i} C_{a_i}}{K_{s_i} + C_{a_i}} - K_{decay} X_{a_i},\tag{17}$$

where *Y* is the biomass yield coefficient [-] and K_{decay} is the endogenous decay rate of biomass $[T^{-1}]$.

The domain size for the problem under consideration is taken as 15 cm length and having a diameter of 2.5 cm, typically representing a laboratory scale column uniformly filled with fine sand. The typical toxic compounds in petroleum such as benzene, toluene, ethylbenzene and xylene are selected as the target compounds, which are present initially at a specific mole fraction contributing to the initial residual saturation and distributed uniformly throughout the domain.

2.3 Numerical solution

The system of coupled partial differential equations is discretized in temporal and spatial coordinates using finite difference approximations to make it in algebraic form. The advection term is modelled as fully implicit and dispersion term as semi-implicit (Crank–Nicholson). The resulting set of tri-diagonal matrix is solved using Thomas algorithm in FORTRAN environment. The initial and boundary conditions for the numerical scheme are given in table 2. The top boundary is Cauchy-type, because the NAPL source is distributed within the domain as residual saturation (S_n) , and the net advective and dispersive flux at the boundary is due to constant inflow characterized by Darcy velocity and dispersivity as given in table 3. However, the variation in the overall dispersion is taken into account by incorporating the molecular diffusion of NAPL as well as change in pore velocity (v) as a function of S_n .

The dissolution model for the contaminant coupled with rate-limited sorption as well as biodegradation governed by Monod kinetics is given by Eq. (1), whereas sorbed phase concentration and biomass concentration can be estimated sequentially from Eqs. (16) and (17), respectively. The rate-limited dissolution model is solved by selecting suitable mass transfer correlation provided in table 1 and substituting Eqs. (2) in (1). The details of the parameters used for the numerical study are given in table 3. The values of important physical and chemical properties of the compounds are given in table 4.

Initial conditions	Boundary conditions
$C_{a_i}(x, t = 0) = 0$ $X_i(x, t = 0) = 2$ $S_i(x, t = 0) = 0$	$\frac{vC_{a_i} - D\frac{\left(C_{a_{i+1}} - C_{a_i}\right)}{\Delta x} = 0}{\frac{\partial C_{a_i}}{\partial x}\Big _{(x=L,t)}} = 0$

Table 2. Initial and boundary conditions for the selected numerical scheme.

 Table 3. Dataset of parameters for the numerical model.

Parameter	Notation	Value	Reference
Length of column (m)	L	0.15	Assumed value
Diameter of column (m)	d	0.022	Assumed value
Soil porosity (-)	n	0.40	Couto & Malta (2008)
Longitudinal dispersivity (m)	α	0.001	Couto & Malta (2008)
Soil bulk density (10^6g/m^3)	ρ_b	1.60	Clement et al (1998)
Fraction of organic carbon (-)	f_{oc}	0.01	Essaid et al (2003)
pore velocity (m/day)	V	1.0	Assumed value
Initial NAPL saturation (-)	S _n	0.03-0.3	Assumed value
Medium grain size (m)	d_p	0.00032	Couto & Malta (2008)
Time step (day)	Δt	0.005	Calculated value
Length step (m)	Δx	0.01	Calculated value

Table 4. Physical and chemical properties of benzene (B), toluene (T), ethylbenzene (E) and xylene (X).

Parameter	В	Т	Е	Х	Reference
Molecular weight (g mol)	78	92	106	106	ASTM 1995
Pure phase density (10^6 g/m^3)	0.88	0.87	0.86	0.87	ASTM 1995
Pure phase solubility (mg/L)	1750	535	152	198	ASTM 1995
Molecular diffusion coefficient, $D_m(10^{-5} \text{ m}^2/\text{day})$	1.10	0.95	0.85	0.85	ASTM 1995
Soil organic carbon partitioning coefficient, k _{oc} (log L/kg)	1.58	2.13	1.98	2.38	Lovanh et al 2000
Sorption mass transfer coefficient, K_m (day ⁻¹)	0.015	0.015	0.015	0.015	Lovanh et al 2000
Effective retardation factor, Ret (-)	1.15	1.54	1.38	1.96	Calculated value
Maximum specific substrate utilization rate, V_{max} (day ⁻¹)	1.2	1.9	0.9	0.9	Maliyekkal <i>et al</i> 2004; Alvarez 1991
Half-saturation constant, K_s (mg/L)	80	100	50	50	Maliyekkal <i>et al</i> 2004; Bielefeldt & Stensel, 1999
Endogenous decay constant, K_{decay} (day ⁻¹)	0.02	0.02	0.02	0.02	Couto & Malta 2008
Yield coefficient, Y (-)	0.3	0.3	0.2	0.2	Priya & Philip 2013; Couto & Malta 2008

3. Results and discussions

The results of numerical simulation studies are important to assess the versatility of the numerical techniques, the significance of the prevailing assumptions and the selection of dissolution mass transfer correlation. The present model is checked for its numerical stability and the contaminant mass balance is confirmed within close proximity. The present multicomponent dissolution model is tested against the experimental data given by Borden & Piwoni (1992) for the aqueous concentrations of benzene, toluene and xylene in order to select suitable mass transfer correlation for a similar experimental condition.

Figure 1 provides the comparison of numerically simulated concentrations of benzene, toluene and xylene present as a mixture using various mass transfer correlations in comparison with the experimental data from Borden & Piwoni (1992). Even though these compounds resemble in many physico-chemical characteristics, their relative solubility and structural properties differ significantly to constitute non-ideal nature. Hence, in most cases, the simulation of realistic breakthrough profile of these compounds is relatively tough to appreciate in terms of peak concentration and extended tailing (Johnson *et al* 2003). It is observed from figure 1 that the correlation MTC#1 is in close agreement with the initial phase of dissolution as well as capturing the peak concentration of benzene and toluene corresponding to their effective solubility; however the peak value of xylene is slightly lower than the observed value of effective solubility.

The mass balance estimates revealed that error is minimal with the use of MTC#1, which is also clear from figure 1. It is observed that the peak value pertaining to the equilibrium concentration of xylene has taken a relatively longer duration (nearly 2 days) in comparison with that of toluene (nearly 1 day) and benzene (0.5 day). Conversely, the present model is able to capture the tailing part of dissolution profile more closely for lesser soluble compound (xylene) than for more soluble compound (benzene). It is also observed from figure 1 that other mass transfer correlations are not able to closely simulate this kinetic nature of dissolution, especially when the conditions are conducive for equilibrium mass transfer (for highly soluble compounds), which is attributed to the range of coefficients used in these correlations. During the initial phase, the dissolution mass transfer rate is very high due to the high concentration gradient, and as dissolution progresses, the mole fraction decreases in the mixture, which in turn decreases its effective solubility. While studying the behaviour of these correlations on the extent of simulation time, it is observed that occurrence of high peak concentration is inversely proportional to the extent of tailing because of the decrease in effective solubility facilitated by the change in mole fraction.

3.1 Simulation results for equimolar mixture of BTEX at residual saturation

The model is run for the selected problem domain (table 3) with equimolar mixture of benzene, toluene, ethylbenzene and xylene (BTEX) using the four different mass transfer correlations (table 2) and the results are presented in figure 2. The domain conditions resemble typical lab scale experimental set-up with initial residual saturation of 25 percent and Darcy velocity of 0.5 m/day. It is clearly observed from figure 2 that concentration elution follows chromatographic nature with variable breadth of the peak concentration in accordance with their effective solubility. The apparent tailing in the concentration of low soluble fraction in the mixture is due to the declining solubility rather than mass transfer kinetics as reported in previous studies (Frind *et al* 1999; Johnson *et al* 2003).

One distinct observation is that the peak concentration of toluene occurs at the same time when benzene concentration is almost zero. Similarly, the peaks of ethylbenzene and xylene occur at

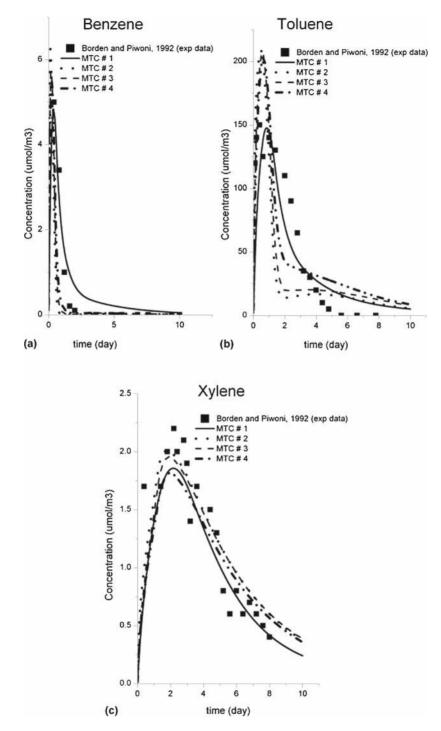


Figure 1. Validation of the multicomponent dissolution model using different mass transfer correlations (MTC) for aqueous concentrations of Benzene, Toluene and Xylene in comparison with Borden & Piwoni (1992) [Refer table 1 for details].

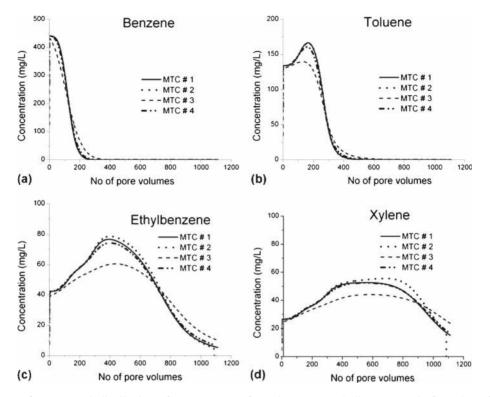


Figure 2. Temporal distribution of (a) Benzene, (b) Toluene, (c) Ethylbenzene and (d) Xylene for different dissolution mass transfer correlations [Refer table 1 for details].

the time when toluene has almost disappeared. It is observed from figure 2 that time required for the arrival of peak concentration for individual components is inversely proportional to their effective solubility and hence the total time required for complete source removal is limited by the solubility of the lowest soluble compounds (ethylbenzene and xylene) and their mole fraction in the mixture.

The mean error obtained during the mass balance calculation for the simulation of single compound as well as multicomponent system for different mass transfer correlations is provided in table 5. It is observed that the difference between initial mass of contaminant and the total eluted mass as estimated by the numerical model is more precise in case of single compound system. However, for the multicomponent model, estimated error is similar for all correlations except for MTC#3 which is influenced by the low coefficient values of the model parameters (Schaerlaekens *et al* 2000). It is reported that the correlation developed by Nambi & Powers (2003) is suitable for handling heterogeneity of the porous media and for higher ranges of

]	Error (%) calculation for various mass transfer correlations				
	MTC#1	MTC#2	MTC#3	MTC#4		
Single component	0.0003	0.0205	0.0651	0.1268		
Multicomponent	1.5021	1.4977	2.5900	1.4922		

Table 5. Comparison of mass balance error between single and multicomponent models.

NAPL saturation and Reynolds number (Grant & Gerhard 2004; Prakash & Nambi 2012). Since majority of mass transfer correlations yielded similar profiles as Nambi & Powers (2003) with minimum relative error, it is chosen for further simulations.

The coupled effect of kinetic sorption and biodegradation with rate limited dissolution on the aqueous concentration of benzene, toluene, ethylbenzene and xylene for the selected domain were also studied. It is observed from figure 3a that there is no apparent distinction with the effect of coupled reactions in the concentration of benzene due to the high effective solubility (440 mg/L), resulting in faster reduction within first 250 pore volumes. From figure 3b, the toluene concentration showed a peak value of 170 mg/L at 200 pore volumes, which occurred when benzene concentration has significantly receded. The effect of coupled reactions is clearly seen during the descending limbs of the profile, especially for lesser soluble compounds. At earlier times, the degradation has resulted in increasing concentration gradient resulting in higher mass transfer rates and higher aqueous concentrations. The same phenomena has been the driving force for drop in concentration at later times under rate limited dissolution conditions resulting in reduction in total pore volumes for fast removal.

It is observed that as the higher soluble fractions have flushed out, the mole fraction of lesser soluble fractions increase; further increase their effective solubility, which is progressive towards higher pore volumes. At this stage, these compounds partition to the aqueous phase irrespective of low mass transfer rate, resulting in significant reduction of aqueous concentration due to the

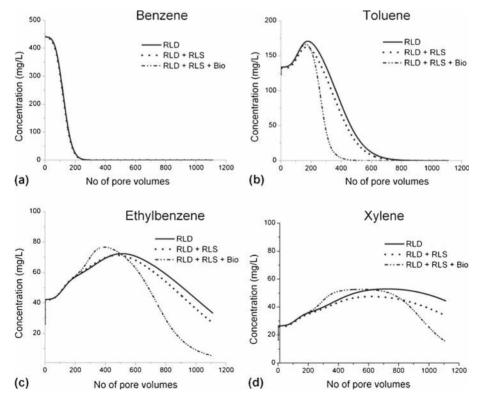


Figure 3. Temporal distribution of (a) Benzene, (b) Toluene, (c) Ethylbenzene and (d) Xylene under various coupled reaction scenarios. [RLD = Rate limited dissolution, RLS = Rate limited sorption, Bio = Biodegradation].

coupled biodegradation. However, it is interesting to note that complete removal of lower solubility compounds is not achieved within the simulation period of 1100 pore volumes, although there is a significant reduction in concentrations due to biodegradation and sorption when compared to concentrations when dissolution alone is present.

3.2 Comparison of mass transfer models for single and multi-component NAPL

The simulation results are compared between single and multi-component system for the same mass of compounds, as established by the residual saturation. When specific composition of the mixture is not known, the concept of residual saturation will serve as the sole representative of contaminants. However, for the multi-component mixture, apart from the initial mole fraction and effective solubility for less soluble compounds, the combined effect of sorption and biodegradation will determine the extent of contamination. Hence it is important to recognize the dissolution pattern for the sparingly soluble compounds when they are present as the sole constituent as well as when they come in a mixture.

As it is clear from figure 4, the kinetic nature of single compound dissolution is increasing with decreasing solubility, even though the peak concentration is always lower than aqueous solubility value. However, when they are present in a mixture, the peak value corresponds to the effective solubility of individual compounds at a particular mole fraction. This is clear from figure 4a that benzene concentration in the mixture reached its effective solubility of 440 mg/L, whereas when

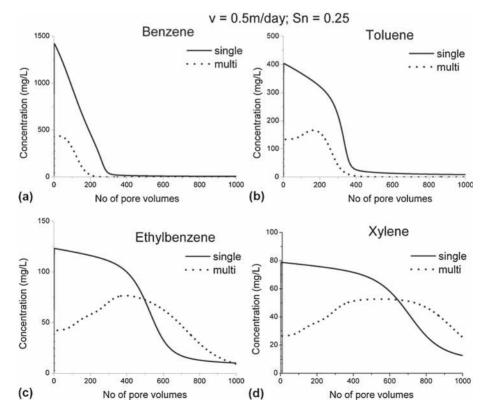


Figure 4. Comparison of concentration profiles of (a) Benzene, (b) Toluene, (c) Ethylbenzene and (d) Xylene when present in single and multicomponent system.

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it is present alone the peak concentration is 1450 mg/L which is near to its solubility value. Similarly, the aqueous concentration profile for toluene as a single compound is always higher than for the multicomponent system. Since toluene reaches peak value after significant flushing of benzene, the apparent increase in the mole fraction of toluene results in higher effective solubility than observed during the initial phase of dissolution. However, for ethylbenzene and xylene, the effective solubility values cross over the single compound solubility values towards higher pore volumes indicating the fact that the apparent increase in the mole fraction after 400 pore volumes result in high effective solubility. The pore volume requirement for the more soluble fractions is less in the mixture compared to their single state, whereas more hydrophobic compounds exhibit comparatively higher mass transfer limitation especially when they are present in the mixture.

3.3 Sensitivity analysis of single and multi-component models

It is generally observed that at high flow rate lesser contact time is available, and at lower saturation dissolution occurs over smaller interfacial area; hence both conditions are conducive for mass transfer limitation. Similarly, higher residual NAPL saturation and lower flow rates result in higher aqueous phase concentration close to equilibrium and more time for complete mass removal. Hence it is important to evaluate the influence of initial source strength and mean fluid velocity on the dissolution mass transfer in order to understand the extent of mass transfer limitation.

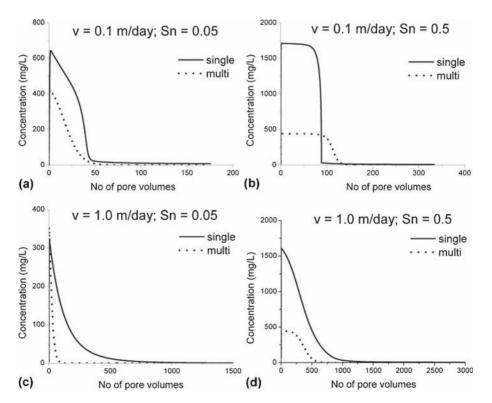


Figure 5. Comparison of benzene concentration in a single and multicomponent system for different combinations of v and S_n .

It is observed from figure 5 that for single compound system, increasing velocity by an order of magnitude results in increase in pore volume requirement by one order due to the mass transfer limitation at higher velocity conditions. Also the increase in NAPL saturation by an order of magnitude results in doubling the pore volume requirement. However, for multicomponent system, the increase in pore volume requirement corresponding to increase in NAPL saturation is about 2.5 times and 5 times for velocity results in increase of pore volume requirement by 2 times and 4 times corresponding to NAPL saturation values of 5 and 50 percent, respectively. Benzene concentration reached its maximum solubility only when the velocity is low and NAPL saturation is high resulting in more contact time, which is in agreement with the equilibrium dissolution criteria (Seagren *et al* 1999; Johnson *et al* 2003). Also under low NAPL saturation and low velocity conditions, the difference in the behaviour of single and multicomponent NAPL dissolution is significantly less.

The shape of the dissolution profile for toluene is also studied under similar conditions as shown in figure 6, showing the influence of residual NAPL saturation and mean fluid velocity. It is observed that when the S_n is high, toluene exhibits tendency towards equilibrium dissolution which is more significant at low velocity (figures 6b and d), resulting in shock like high concentration during the initial phase. When toluene is present in the mixture, it resulted in lower effective solubility and low pore volume requirement. But the peak concentration in figure 6c is higher because of the high flow rate and increased mole fraction of toluene after the elution of

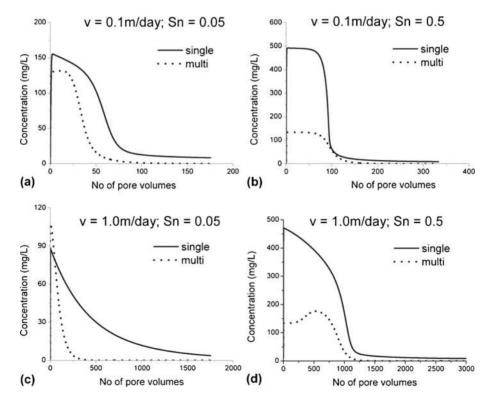


Figure 6. Comparison of toluene concentration in a single and multicomponent system for different combinations of v and S_n .

benzene from the system. For single compound model at low saturation conditions (figures 6a and c), the peak concentrations are lower than the expected solubility values irrespective of velocity, indicating the prevailing kinetic nature of dissolution. As observed from figure 6c, high velocity and low S_n is conducive for exponential decrease in concentration profile, but when S_n is very high (figure 6d), it results in high peak value and subsequently sharp declining limb, unlike the case of benzene.

The concentration profile of ethylbenzene is compared in figure 7 for different values of velocity and residual saturation to understand the extent of mass transfer for the less soluble fraction under rate limiting conditions. The kinetic nature of dissolution is prominent during the initial pore volumes is mainly due to low contact time, but at higher pore volumes the effect of velocity is more significant even though S_n has reduced considerably, resulting in reduced available interfacial area (figure 7c). It is to be noted from figures 7a and c that both single and multicomponent system behave closely near peak values, but multicomponent model predicts more sharp decrease towards larger pore volumes due to the increase in effective solubility resulting from increased mole fraction.

Figures 7b and d show that the peak concentrations predicted by multicomponent model is much lower and delayed as compared to single compound model. This is particularly important to understand the dissolution behaviour at high S_n values when majority of mole fraction is composed of low soluble compounds. It is also observed that high velocity conditions are conducive for higher dispersive effects for the concentration profile after achieving the peak concentration.

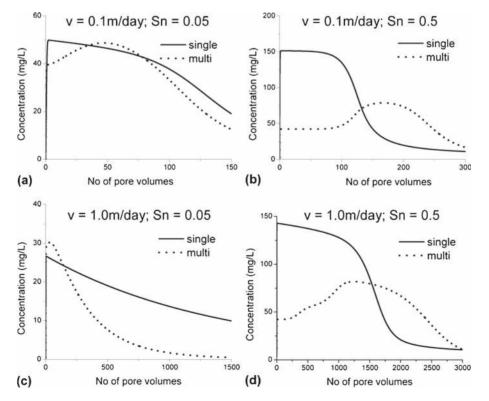


Figure 7. Comparison of ethylbenzene concentration in a single and multicomponent system for different combinations of v and S_n .

The concentration profile of the least soluble compound in the mixture, xylene is compared for different conditions of velocity and S_n as given in figure 8 to understand dissolution behaviour. It is observed from figure 8 that when present alone, there is considerable reduction in xylene concentration only after prolonged flushing and it is not much effective at high flushing velocity. However, when it is present in the mixture, it reaches the peak value with much delay compared to other compounds (figures 8b and d), and thereafter the NAPL saturation is solely dependent on xylene concentration. Because of the low solubility and hence low mass transfer rate, practically it is not possible to remove xylene completely from the system under the given conditions. It can be concluded from figure 8 that when the initial NAPL saturation is high, the time required for complete removal of lesser soluble components will be extremely high as compared to the more soluble components in the mixture. Also, since the residual NAPL saturation is not completely removed within the simulated time period, it is to be considered as a continuing source of contamination, even though significant amount of higher soluble fractions have been removed.

Figure 9 provides the quantitative estimation of dissolution mass transfer rate coefficient of benzene for the above selected conditions in order to highlight the coupled effect of transient and nonlinear reactions. At high residual saturation and low velocity, the condition resembles equilibrium mass transfer for dissolution. Since the mass transfer rate coefficient (K_{wni}) is exponentially dependent on the residual NAPL saturation (S_n), it is expected to have higher influence compared to the increase in velocity (table 1). This is expected to be a favourable condition for efficient mass transfer, and is in accordance with concentration profiles (Figures 5, 6, 7 and 8).

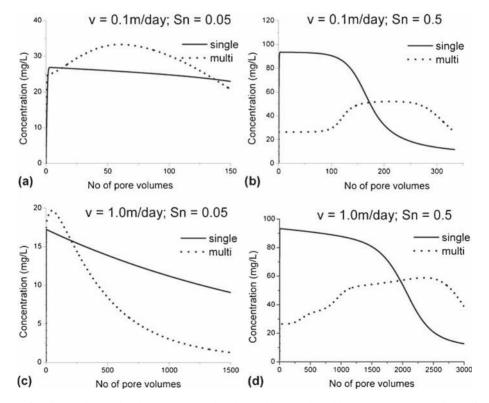


Figure 8. Comparison of xylene concentration in a single and multicomponent system for different combinations of v and S_n .

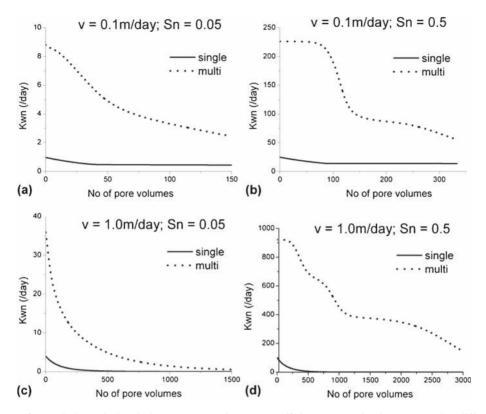


Figure 9. Variation of dissolution mass transfer rate coefficient (K_{wn}) for benzene under different conditions of velocity and S_n .

In the case of multi-component dissolution the mass transfer rate of individual component depends more on the evolution of the components of Sn rather than S_n as a whole. This is controlled by the preferential partitioning of the more soluble components in the mixture and the mole fractions of the same. The evolution of mole fraction is also found to be nonlinear, which is increasing for the lesser soluble compounds, when the soluble compounds dissolve. Hence, in accordance with the removal of more soluble fraction, the mass transfer rate is high initially and decreases until considerable mass has been removed. It is observed from figures 9a and c that the decrease in mass transfer rate is progressive but steeper for high velocity. Also, figures 9b and d indicate that mass transfer rate is very high for large values of S_n , and its reduction is similar to the reduction in concentration up to 150 pore volume and 1000 pore volumes, respectively. Thereafter the dissolution rate is slow but continuous due to the presence of S_n in the system. The dissolution mass transfer coefficient in the multicomponent system is found to be highly nonlinear and extending with changing slope, unlike the exponential reduction in case of single compound system. Hence understanding the variation of dissolution rate coefficient is necessary to explain the mass transfer limiting conditions at higher pore volumes, especially for more soluble compounds. It is observed from the multicomponent model that the reduction of S_n is highly favoured by high velocity conditions resulting in complete removal of compound from the system. The present model is able to predict the long tailing portion for these conditions with minimum mass balance error, indicating that S_n value is more dependent on the mole fraction of the least soluble component. Considering residual NAPL saturation as the true indication for contaminant source strength, it is evident from this study that complete source zone clean up is possible by high velocity flushing, if no other solubility enhancement methods are utilized.

4. Summary and conclusion

Present study discusses the applicability of a comprehensive numerical model for characterizing the possible mass transfer limitation when a multicomponent NAPL is undergoing simultaneous dissolution, sorption and biodegradation. The predictions were validated with existing data in literature. The predictions made using the correlation developed by Nambi & Powers (2003) are in close agreement with the initial phase of dissolution as well as capturing the peak concentration of benzene and toluene corresponding to their effective solubility. The present model is able to predict the multicomponent fate and transport with minimum mass balance error. For single compound model, the kinetic nature of dissolution is increasing with decreasing solubility, even though the peak concentration is always lower than aqueous solubility value. However, when they are present in a mixture, the peak value corresponds to the effective solubility of individual compounds at a particular mole fraction.

The shape of the dissolution profile is significantly influenced by the initial NAPL source strength as well as mean fluid velocity. It is observed that occurrence of high peak concentration for soluble compounds are inversely proportional to the extent of tailing because of the decrease in effective solubility facilitated by the change in mole fraction. For the lesser soluble fractions, the effect of biodegradation is predominant when they reach higher mole fraction in the mixture, which is observed during the descending limb of the profile at higher pore volumes.

The total time required for complete source removal is limited by the solubility of the lowest soluble compounds (ethylbenzene and xylene) and their mole fraction in the mixture. The effect of coupled reactions is minimal for the elution of benzene because of its faster removal caused by high concentration gradient. The sensitivity analysis showed that benzene concentration reached its maximum solubility when the velocity is low (0.1m/day) and NAPL saturation is high (50 percent) resulting in near equilibrium condition with more contact time. The residual NAPL saturation at later times is controlled by the mole fraction of least soluble component.

Mass transfer limitation for the soluble compounds under conditions of low NAPL saturation and low mole fraction is due to low dissolution rate coefficient rather than decreasing concentration gradient. Because of the low solubility and hence low mass transfer rate, practically it is not possible to remove xylene completely from the system under mass transfer limited conditions. The variation of dissolution mass transfer coefficient is found to be highly nonlinear and extending with changing slope for high velocity conditions. The apparent tailing in the concentration of less soluble compounds in the mixture is observed to be due to the declining solubility rather than mass transfer kinetics.

When a multicomponent NAPL system is dissolving, the dynamics of the system, mass transfer rates and the concentration of various compounds in the aqueous phase are quite different in later time periods when compared to early time phenomena. The gradual reversal of mole fractions of the high and low solubility compounds cause these changes which is also carried over to the sorption and biodegradation rates. Models such as this enables us to identify when a specific compound of interest is in significantly high levels and how fast it is removed by taking into consideration the transient mole fractions, mass transfer rates, and associated sorption and biodegradation. These models are advantageous compared to single compound fate and transport models which can over or under-predict aqueous phase concentrations to a large extent.

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However, laboratory scale investigations attempted in the present study would better provide an insight on the effect of variation of porous media properties on the dissolution mass transfer kinetics, which can be highly influential for large scale domain.

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