OBJECT-ORIENTED SPECIFICATION OF DATABASES:

AN ALGEBRAIC APPROACH

Amílcar Sernadas Cristina Sernadas Department of Mathematics, IST, Av. Rovisco Pais, 1096 Lisboa Codex, Portugal

Hans-Dieter Ehrich Institut fur Informatik, TUB, PF 3329, D-3300 Braunschweig, FRG

ABSTRACT

The importance of abstract object types (AOTs) in the field of conceptual modeling and database design is discussed. A formal approach to the specification of societies of interacting objects is proposed. The structure and behavior of each object is defined using a primitive language that also provides the means for specifying the interactions between through event sharing. The algebraic objects semantics of this language is outlined. As a byproduct, the Kripke interpretation structure for the envisaged logic of object behavior is established. The specifications are organized in two layers: (a) the universe of objects, their attributes and data; (b) the space of the global trajectories and traces of the society of objects. Constraints of several kinds can be imposed at both layers. The main issue in the construction of the universe is the naming of all possible objects. With respect to (b), the emphasis is on the definition of the joint behavior of the objects in terms of the allowed sequences of events that may happen in their lives.

1 - INTRODUCTION

In the area of database specification there has been a constant interest in the abstract data type concepts and tools. Those concepts and tools provide the necessary means for abstraction and modularization. Moreover, they have been used for defining formally the conceptual modeling and knowledge representation approaches [SeSe85b,SeSe86].

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However, as such they are not useful when dealing with **objects** opposed to data. Herein, we as time evolving entity assume that *an object is a* Actually, databases (compare this to inert data). object-bases, since should be called they are composed of time evolving units. Data types are useful for describing the attribute domains, but object types are more important since they are needed to describe the entities themselves, including their behavior. The interest in objects is growing [DD86], in part due to recent concerns with: the behavioral descriptions of the universe of discourse the (UoD). in area of conceptual modeling [SeSe85a,FiSe86,Che86]; dynamic aspects of the databases [MBW80,CCF82,LEG85,Lip86]; and the manipulation of complex entities in rather engineering databases [SRG83,BaBu84,DaSm86]. Indeed, a complete description of the UoD should include the definition of both the static structure and the dynamic properties of the relevant entities. On the other hand, the full definition of the database units (records and transactions) should also cover these two aspects.

The main goal of this paper is the development of the basic concepts and tools for the specification of abstract object types (AOTs). as а more adequate alternative to the traditional abstract data type (ADT) techniques for conceptual modeling and full database specification. The AOT approach offers several advantages over the ADT solution. Besides allowing the view of the UoD as a society of interacting agents (objects), it also provides the means for the unified treatment of records and transactions.

A very primitive language for AOT specification is proposed. Its usefulness in the conceptual modeling of illustrated. interaction is entities and their given of Moreover. outline is its algebraic an database semantics. The AOT approach to

specification starts with a complete UoD description (i.e. a full description of the society of interacting objects). This description is made in two successive steps for each object class: first its structure is defined; then, its behavior is established. Although no effort has been made so far towards providing facilities for modular descriptions. the primitive language as it stands now allows local definitions of each object class that are rather independent of each other. The extensive work in Artificial Inteligence and Software Engineering (for а survey 500 [StBo84]) on the object definition problem was duly taken into account. However, our approach brings in several novelties that have been missing in the previous proposals. For instance, the problem of object namina was solved following [EDG86,Ehr86], really abstract and descriptions were achieved by adapting the algebraic tools introduced ADTs. already for Moreover, the interaction mechanism between objects was chosen to be as simple as possible (event sharing), along the lines recently advocated in the area of concurrent programming methodology.

We should stress that the presentation of the approach, the primitive working language and its algebraic semantics leaves no room for discussing other very interesting developments. Namely, the methodologial details are left out. Moreover, no attempt is made discuss: the modular to (parameterized) specification of objects and their societies; the problem of incomplete information about the objects and their situations: the aggregation of objects into complex objects: and their classification within inheritance networks. Finally, the resulting logic of societies, objects and events is only sketchily examined.

The paper is organized as follows. Section 2 contains a rather informal introduction to the proposed tools for AOT specification within the context of a very simple UoD example. Section 3 presents the algebraic semantics of the structural descriptions of the objects (naming mechanisms, state attributes and constraints). Section 4 is dedicated to the rest of the algebraic semantics (dealing with events. trajectories, traces and interactions). The complete example discussed in Section 2 is included in the Appendix.

2 - MOTIVATION

According to the object-oriented approach, in order to capture knowledge about the real world entities and their behavior, one should start by perceiving

the relevant types of objects in the universe of discourse (UoD). For each object type it is then necessary to understand both its static and dynamic aspects. That is to say, one should describe the object's attributes and also the events that may occur during its life. As an illustration, consider a very simplified trader's world . In this UoD it seems worthwhile to consider at least the following types of objects: CLIENT, STOCK and ORDER. Note that two rather different kinds of object types were considered: persistent. like CLIENT. and transient, like ORDER. When it comes to the implementation, it is usual to implement a persistent object over a record in the database (plus associated procedures). On the other hand, transient objects tend to be implemented as transactions. At this perception stage, the classification is irrelevant since both persistent and transient object types are be described using the to same abstractions. However, it is important to notice that both kinds should be included in the UoD and that the description of transient entities as events does not seem to be acceptable.

When describing a society of interacting objects, it is essential to find the basic object identification mechanisms, that is to say, for each type of objects, the means for naming the different occurrences of the type. For instance, let us assume that in the trader's world the occurrences of CLIENT are identified using a key mechanism that maps names (strings) into clients. One might also safely assume that, similarly, there is a key mechanism that maps stock identifiers into stocks. Naturally, a more realistic description should include the object type STOCK as a relationship between the object types PRODUCT and DEPOT. Herein, for the sake of simplicity, it is assumed that only stocks are of interest. Note that in the simplified trader's world both CLIENT and STOCK have their occurrences named independently of the other objects in the society. On the contrary, orders are identified for each client by number. That is to say, when identifying an order one has first to identify the client that issued it. Hence, the identification of orders does depend on the identification of other objects in the society.

Following [SeSe85a], the object types *CLIENT* and *STOCK* are said to be **Independent** and the object type *ORDER* is said to be a **characteristic** (of *CLIENT*). Characteristic object types are said to be **dependent**. Other dependent object types are also useful (such as relationships, particularizations, generalizations and aggregations), but they are not

simplified trader's world. A detailed used in the description of the object types in the trader's world is presented in the Appendix. Α preliminary (OBject LOGic) language is version of the OBLOG UoD description is divided used. In OBLOG, the the structure into the following parts: data STRUCT (including the types specification plus the key mechanisms and the state attributes of all object types) and the behavior specification BEHAV (including the events and traces of all object types).

Returning to the example, the key mechanism of the object type CLIENT includes the following key map cli: string \rightarrow CLIENT, as well as the key attribute name: CLIENT \rightarrow string. The key population constraints name(cli(S))=S for every S in string such that cli(S) is in CLIENT and cli(name(C))=C for every C in CLIENT just state the obvious relations between the key attribute name and the key map cli. Such relations are typical of every independent object type. On the other hand, the other key constraint (a kev individual constraint) upper(first(name))=true is specific of this object type: it states that the first character of every client's name must be an upper case letter. Note that, for the sake of simplicity, the argument of the attribute is omitted in individual formulae.

Key maps and attributes do not vary in time. That is to say, they are independent of the object's situation. State-dependent attributes are introduced in the state part of the object type definition. The object type CLIENT has only one state attribute count: CLIENT \rightarrow integer. This attribute maps each client situation into an integer (intended to represent the number of orders already issued by that client at that point of its life). A situation is a snapshot of the objects and their attribute values. When specifying an object type like CLIENT, it is sometimes necessary to impose restrictions on the values of its attributes. For instance, the constraint (zero≤count)=true states that the (integer-valued) attribute count is never below zero. This is an local state constraint. In contrast, example of a global state constraints (to be illustrated later on) are similar but they depend on the situation of other objects. The local state constraint (G(N≤count)=true) If (count=N) states that the value of count never decreases. Note the use of the temporal operator always in the future G in the latter formula, for expressing that if at some situation count is N, then it will remain greater than or equal to N in every subsequent situation.

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worthwhile to mention here the lt is difference between situations and states. as proposed in Situations are snapshots of the existing [Ehr86]. objects and their attribute values. In constrast. states are theories representing some knowledae situations. If that knowledge is partial or about disjunctive there will be many situations satisfying states (having only one that state. Monomorphic situation as model) appear in special cases, like definitive databases with the closed world the assumption. In the monomorphic cases. admissibility of states and state transitions can be derived from the temporal specifications; techniques are also known for enforcing state constraints (see [ELG84,LEG85]).

The third step in the description of an object is the definition of its behavior, in terms of the events that may happen in its life. In the object type CLIENT, one might consider at least two kinds of events: births and (order) issues. Such events are generated using birth: \rightarrow E(C) with C in CLIENT and issue: integer STOCK integer \rightarrow E(C) with C in CLIENT. are formally introduced as CLIENT-indexed These families of functions. For each client C, birth denotes the birth event of C and the function issue maps each stock, requested-quantity> triole <order-number, into the corresponding issue event. E(C) denotes the set of possible events of client C.

The life trajectories of each client are non-empty sequences of these events satisfying some general trajectory restrictions: every begins with а creation event; after a **destruction** event no more events are allowed; and modification events are allowed after the creation event until the eventual destruction event. Note that, in principle, it allow incomplete trajectories, that is useful to say, to trajectories not finishing with a is destruction event. Otherwise, а rather strona liveness requirement is imposed, as discussed in the end of this section.

For each particular trajectory, the set of possible (determining intermediate situations) is traces composed of all non-empty initial parts of the trajectory. In many cases, the observed behavior of the object indicates that some of the theoretically possible trajectories are not allowed. For instance, in the definition of the behavior of clients, the set of trajectories is restricted by the following domain assertion [T>>issue(N,K,R)] only lf (count at T = pre(N) stating that the issue event for (N,K,R) is allowed only if the order-number N is the value of count, just before that event, plus one. lt is important to notice that we are usina trace explicit In such formulae, trace formulae. an argument is given for every state attribute using the connective at.

The dependence of the state attributes on the local trace of the object is defined with valuation and equivalence equations. As an illustration of the former consider (count at <birth>)=zero and (count at [T>>issue(N,K,R)])=suc(count at T) stating that count is zero after the birth event and its value increases by one every time an issue is made. respectively. Valuation equations define the values of attributes as functions of the traces. state (illustrated below) define Equivalence equations equivalences between traces for the sole purpose of attribute evaluation.

When expressing either domain restrictions or valuation and equivalence equations, it is necessary to refer to traces. A very simple notation was adopted for dealing with traces: <a1,...,an> denotes the trace composed of the events a1,...,an; and [x>>a] denotes the trace obtained by suffixing event a to trace x.

The final part of an object type description is composed of the so called Interaction equations that equate events of different objects (of the same or of different types). In order to illustrate the use of those equations, as well as of some other features not present in the CLIENT specification, it is worthwhile to examine in detail the definition of the other object types in the trader's world: ORDER and STOCK. Skipping the key mechanism, it should be clear that the state-dependent attributes stk and reg of ORDER indicate respectively the target stock requested quantity. Their local state and the constraints are easily interpreted. It remains to discuss the global state constraints, such 25 there-is cli. As global constraints, they are not imposed on the local situations of each order but instead on the global situations of the trader's society. Those global situations may be obtained by "gluing together" individual local situations. Only global situations satisfying every global constraint are considered. For instance, the former qlobal constraint states that every existing order points (through cli) to an existing client.

ORDER interaction equation the The in C.issue(N,K,R)= ord(C,N).creation(K,R) specification event by some client states that every issue is order creation (and vice versa). Recall an into each (client,number) that ord maps pair

the corresponding occurrence of ORDER. This means that those events are shared by the two objects. This **sharing of events** (with the same vocabulary or not) is the only interaction mechanism allowed in the proposed framework. Informally, the interaction equations guide the construction of the **global trajectories**, by "gluing together" the local chains at the shared events. Each global trajectory is an interleaving of the local trajectories, respecting every interaction equation. Each global state is determined by the global trace of those events that have already occurred in every object life.

The local behavior of each order is very simple: after its creation, it may be either satisfied or rejected. Note that according to this local description of the order behavior it is not possible to state if the order is to be satisfied or rejected. That can only be established when describing the behavior of the object type STOCK. Indeed, every rejection and every satisfaction is shared by two objects: an order and a stock, as indicated in the interaction axioms of the object type STOCK. The domain [T>>failure(O,R)] only lf (laoh at assertion T < R)=true states that the rejection of the order (the failure of the target stock) takes place only if the requested quantity is greater than the quantity on hand just before the event. The satisfaction (delivery) takes place in the other case. One of the events may happen, but not both. This is an interesting safety property of orders within the context of the proposed trader's world.

it is necessary to express (as Sometimes, а or as a provable theorem) requirement axiom of assertion: a liveness another kind property. desired properties express that some Liveness events must occur. As an illustration consider the following requirement: every order will sooner or later be processed. That is to say, no order that has been created will remain for ever waiting to be rejected or satisfied. This particular requirement is not a property of the described trader's world. Indeed, it is reasonably easy to verify that there are global lattices of events that satisfy the entire specification and where orders exist with incomplete trajectories. A suitable revision of the specification ensuring that liveness property could be made as follows, at the level of the ORDER domain:

<creation(K,R)> only if

(Fafter(satisfaction(K,R))) at <creation(K,R)> or (Fafter(rejection(K,R))) at <creation(K,R)>

Herein, **F** is the **sometime in the future** temporal operator and **after** is a (local) trace predicate allowing the identification of the last event.

Finally, it remains to comment the equivalence equations for traces, such as those included in the description of STOCK. For instance, the equivalence equation [T>>failure(O,R)]=T states that, for the sole purpose of state attribute evaluation, the lefthand trace is equivalent to the righthand one. Indeed, a failure does not change the value of *qoh*.

3-STRUCTURE SPECIFICATION

The purpose of the structure specification is to define the their objects with attributes and relationships, as well as to characterize which collections of objects may exist and how they are allowed to change. This specification is organized into three successive steps: STRUCT=DT+KY+ST, where DT is the specification of the underlying data types that will be used as attribute values; KY specifies the keys, i.e. KY defines an identification mechanism for the occurrences of each object sort; and ST provides the state information on each object sort, i.e. attributes and constraints.

Data type specifications have been studied extensively in the last decade. Without going into details, we assume a monomorphic data type DATA to be given as the semantics of the specification DT (e.g. the initial DT-algebra). As expected, DATA is a generated and typical interpretation of the specification DT. It consists of a carrier set of data (values) for each data sort elements and an appropriate data operation for each operation symbol. Note that DATA satisfies the specification DT. Hence, we write DATA |= DT.

Key specifications extensions of data as type specifications been introduced have in algebra [Ehr86,EDG86] using а final semantics. Herein, we employ a variant of that approach using key maps (a notion introduced in [SeSe85a]) for which an initial algebra semantics can be given. Accordingly, a key extension of DT, $KY=(\Sigma_{KY},C_{KY})$ consists of a key signature $\Sigma_{KY}=(S_{KY},\Omega_{KY})$ and a set of key constraints CKY=PCKYUICKY, where the former is the set of population key constraints is the set of Individual and the latter key constraints. The key signature contains the set SKY of all object sorts, also denoted SOB, plus an SOB-indexed family of key mechanisms. Each key <s1...sn,kmap, mechanism $\Omega_{KY}(s)$ is triple а kattr>, where $s_1...s_n \in (S_DT \cup S_{OB})^*$ is the list of the n key argument sorts, kmap: $s_1...s_n \rightarrow s$ is the key map. and kattr = <ka1,...,kan> is the list of the

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n key attributes, such that $ka_i: s \rightarrow s_i$ for $1 \le j \le n$.

The semantics U of $DT+(\Sigma_{KY},PC_{KY})$ is the free extension of DATA with respect to (Σ_{KY},PC_{KY}) forgetting the key maps. By this free construction, U satisfies the population key constraints. Intuitively, U contains for each object sort all "possible" objects of that sort (in an abstract sense) that can be identified using the specified key mechanisms.

For formulating the individual key constraints we use the key language KL: the first-order predicate language over the signature of DT+KY. For notational and methodological convenience, OBLOG in specifications, we employ a "local dialect" KL(s) when specifying the object type s. Formulae of the form $(\forall y:s) \phi(y)$ are abbreviated to ϕ , omitting all occurrences of the object variable y of sort s. For instance, in the specification of ORDER, the formula *(zero≤numb)=true* is the local abbreviation of a formula of KL: (Vy:ORDER) ((zero≤numb(v))=true). The semantics of DT+KY in the presence of such individual key constraints is somewhat involved. The starting point is the algebra U built as above ignoring those individual key constraints. Then, the envisaged semantics UNIVERSE of DT+KY (taking into account the individual key constraints) should be the largest subalgebra of U satisfying the individual key constraints. In [Ehr86.EDG86] it is proved that a unique largest subalgebra exists provided that all individual key constraints are positive formulae. We shall assume that in the sequel. Note that UNIVERSE = (DT+KY), in the sense that it satisfies the key constraints and its Σ_{DT} -reduct satisfies the DT axioms.

Finally. the state specification $ST_{=}(\Sigma_{ST}, C_{ST})$ specification providing completes the structure by the object attributes and their constraints. The state adds no new sorts. lt signature $\Sigma_{ST} = (\emptyset, \Omega_{ST})$ attributes the of each object introduces state where sort, as follows: $\Omega_{ST} = {\Omega_{ST}(s): s \in S_{OB}}$ $\Omega_{ST}(s) = {\Omega_{ST}(s)(s'): s' \in S_{DT} \cup S_{OB}}.$ As usual, we write b; s \rightarrow s' instead of b $\in \Omega_{ST}(s)(s')$. Note that state attributes can be data or object-valued. Recall also that we assumed that an existence boolean is available for every object sort s: attribute $s \rightarrow$ bool. The index is omitted if it is there-is_e : clear from the context. The state constraints are language SL: a formulated using the structure temporal extension of the first order predicate language over the structure signature. The only temporal operators we use in this paper are the "temporal quantifiers" always in the future G and sometime in the future F. As for the key language KL, we also use a "local dialect" SL(s) for each object sort s whenever convenient. Indeed, in the specification of s, we write ϕ as an abbreviation $(\forall y:s)$ ((there-is_s(y)=true) Implies of φ(y)). The set of state constraints is given as follows: CST=LCSTUGCST, where the former is the set of local state constraints (of every object sort) latter is of alobal and the the set state constraints (also of every object sort).

Now, at last, the semantics of the structure specification STRUCT can be given as any "temporal interpretation" satisfying the state constraints. Before defining what we mean by a temporal interpretation, the concept of situation should be formalized as follows: a situation σ for STRUCT is a ΣSTRUCT-algebra (without the key maps) whose $(\Sigma_{DT}+\Sigma_{KY})$ -reduct is UNIVERSE. Then, a temporal interpretation for STRUCT=DT+KY+ST is a triple TI=<UNIVERSE,S,T>, where the first component is the UNIVERSE of data and objects satisfying DT+KY; S is a class of situations for STRUCT; and T is a reflexive and transitive binary relation on S. The latter corresponds to the transition or reachability relationship between situations: $\sigma T \sigma'$ iff the situation σ is reachable starting from situation σ , i.e. iff the transition from σ to σ' is possible.

Given a temporal interpretation TI=<UNIVERSE,S,T>, a situation σ in **S** and a variable assignment A, every term of SL can be evaluated as usual: data operations and values are interpreted according to DATA; key attributes and objects are interpreted according to UNIVERSE; state attributes are interpreted according to the situation σ . Hence, every atomic formula can easily be evaluated, since we have only the equality predicate (for each sort): $V_{TI.\sigma,A}(t=t')$ = if $(V_{TI,\sigma,A}(t) = V_{TI,\sigma,A}(t'))$ then 1 else 0. Finally, nonatomic formulae are evaluated as expected. For example: $V_{TI,\sigma,A}(F\phi) = if (V_{TI,\sigma',A}(\phi)=1$ for every σ' such that $\sigma T \sigma'$) then 1 else 0. Note the role of the transition relation T in the interpretation of temporal formulae, following the Kripke approach. It is beyond the scope of this paper to discuss the properties of that relationship in the context of database specification. A temporal interpretation TI=<UNIVERSE.S.T> is said to satisfy a structure specification STRUCT, TI |= STRUCT, iff every state constraint has the value 1 in TI for every situation s in S and every variable assignment. We shall take as the semantics KRIPKE of a structure specification

STRUCT the class of temporal interpretations for STRUCT that satisfy its state constraints.

4 - BEHAVIOR SPECIFICATION

The purpose of the behavior specification is to define the life trajectories of the objects in the society, in terms of their events, as well as their interactions. This specification is organized into four successive steps: BEHAV=EV+TJ+TA+TD, where EV is the specification of the events. includina the interactions, TJ establishes the set of all possible (global) trajectories and their traces, TA provides the trace attributes and their equations, and, finally, acceptable TD specifies the domain of the trajectories and their traces.

The event specification $EV = (\Sigma_{EV}, E_{EV})$ consists of an event signature $\Sigma_{EV}=(S_{EV},\Omega_{EV})$ and a set of interaction axioms. An event signature consists of a single set S_{EV} with the sort e of events, an S_{OB} indexed family of event generator tools and a collection of event predicates. Each $\Omega_{FV}(s)$ is a triple <creation(s),modification(s),destruction(s)>, where. for instance, creation(s) {creation(s)(w): we $(S_{DT} \cup S_{OB})^*$. Each set creation(s)(w) contains the creation-event generator symbols for object sort s (the sort of the life or primary parameter) parameter sorts. As with list w of secondary we write when expected, g: S w A gecreation(s)(w). The event predicates cre, mod and des are used to identify the category of each event. When writing the interaction axioms we use the event language EL: the equational language over the signature of DT+KY+EV, prefixing the life parameter. As an example, recall the equation: C.issue(N,K,R) = ord(C,N).creation(K,R).

The semantics EVENT of the specification DT+KY+EV is the free extension of UNIVERSE with respect to the specification EV. Thus, EVENT is а event $(\Sigma_DT+\Sigma_KY+\Sigma_EV)$ -algebra (without the maps) key satisfying the EFV equations and containing UNIVERSE as $(\Sigma_{DT}+\Sigma_{KY})$ -reduct. Thus, EVENT |= (DT+KY+EV). The algebra EVENT contains, in addition to the components of UNIVERSE, the carrier set E for the as as well the appropriate event sort θ, interpretation of each event generator and predicate.

 $TJ=(\Sigma_{TJ},C_{TJ})$ extension The trajectory is of signature $\Sigma_{TJ}=$ composed the trajectory and the set of universal trajectory $(S_{T,I},\Omega_{T,I})$ conditions: equations the the trajectory and trajectory constraints. The trajectory

signature includes one sort: the sort e⁺ of sequences events or trajectories and the sort r of of traces. It also includes the following operation symbols: the trajectory constructors $<>: \Theta \rightarrow \Theta^+$ [>>]: $e^+ e \rightarrow e^+$, as well as the trace and constructor tr: e^+ int \rightarrow r and some auxilliary operators, such as ev: r int \rightarrow e and ip: e⁺ int \rightarrow e+. Note that ev(R,N) denotes the N-th event in trace R; and ip(S,N) denotes the sequence of the N first events of S. The trajectory equations written in the equational language over the signature of DT+KY+EV+TJ impose the expected relationships between traiectories. traces and events. For instance: the ev(tr(<X>,one),one)=X. On other hand, the trajectory constraints (easily formalized in the suitable first order language over the DT+KY+EV+TJ) impose the signature restrictions described in section 2. For instance, they include the requirement that every trajectory must start with a creation event.

The semantics TRAJECTORY of the specification DT+KY+EV+TJ is the largest subalgebra, satisfying the trajectory constraints above. the free of extension of EVENT (forgetting the trajectory constructors) with respect to the indicated trajectory extension without those constraints. lt contains, inter alia, the carrier set E⁺ of sort e⁺ (the set of all trajectories). Fixing a trajectory τ , that is to say, fixing an element τ of **E**⁺. TRAJECTORY(T) the largest subalgebra is of TRAJECTORY such that the carrier set of e⁺ is the set { τ }. Hence, its carrier set $\mathbf{R}(\tau)$ for **r** contains all initial parts of τ .

attributes specification The trace $TA=(\Sigma_{TA},E_{TA})$ consists of the signature $\Sigma_{TA}=(\emptyset,\Omega_{TA})$ and a collection of trace equations: equations the trace equivalence and the valuation equations. The trace attributes adds łt introduces a signature no sorts. new attribute symbols. collection of trace includina: $\{\Omega_{TA}(\mathbf{r},s'): s' \in (S_{DT} \cup S_{OB})\},\$ where each $\Omega_{TA}(\mathbf{r},s')$ is the set of attribute symbols mapping traces into elements of sort s'. We assume that each $\Omega_{TA}(\mathbf{r},s')$ contains every state attribute symbol (see section 3) returning values of sort s'. Hence, we use the symbol for а state attribute and the same corresponding trace attribute, since there is no possibility of confusion. As an illustration, recall the state attribute *qoh:* STOCK \rightarrow integer. The same symbol is used in the behavior specification denoting a trace attribute that maps traces into integers.

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Moreover, after is introduced at this point as an event-dependent boolean trace attribute with no counterpart in the collection of state attributes after: e r \rightarrow bool. When writing trace equations we use the trace language TL: the equational language over the signature DT+KY+TJ+TA. suffixing the argument of the attributes through the trace For instance, recall connective at. the following STOCK the specification: equations in [T>>failure(O,R)]=T and (qoh at <open>)=zero. The former is a trace equivalence equation that simply equates traces (only for the purpose of attribute evaluation). The other is a valuation equation that states the value of the attribute at the indicated Actually, the former equation is trace. ลก abbreviation of the schema stating for each attribute att of arbitrary object K of sort STOCK: (att at [T>>K.failure(O,R)])=(att **Besides** at 🛛 **T)**. the specified trace equations, we assume some implicit trace equations that indicate the value of the boolean existence and event-dependent attributes. and that impose the necessary frame conditions. As an example of the former, consider the following valuation equation: (there-is Kat <K.open>) = true.

Fixing a trajectory τ in TRAJECTORY, the semantics ATTRIBUTE(τ) of specification DT+KY+EV+TJ+TA is extensions of TRAJECTORY(τ) with the class of attributes respect the indicated trace to specification (including the implicit equations). Note that each element θ of ATTRIBUTE(τ) contains TRAJECTORY(T) $(\Sigma_{DT}+\Sigma_{KY}+\Sigma_{FV}+\Sigma_{TJ})$ -reduct. as Consequently, also contains EVENT as it $(\Sigma_{DT}+\Sigma_{KY}+\Sigma_{EV})$ -reduct. In this sense, we can say that any such algebra satisfies the specification DT+KY+EV+TJ+TA. Thus, we write: ATTRIBUTE(τ) |= (DT+KY+EV+TJ+TA).

Finally, it remains to define precisely the semantics of the fourth part of the behavior specification: TD defines the set of acceptable trajectories restricting at the same time the possible values of the trace domain attributes. The trace extension TD=(Ø,CTD) further sorts introduces no or operations. It consists of a collection of domain constraints of the general form: T only if φ(T), where $\omega(T)$ is a formula of TL (the trace language introduced above) and T is a term of sort e+. Fixing a particular trajectory τ in TRAJECTORY, such a constraint is to be interpreted as stating (3v:int) ip(τ, v)=T implies $\phi(T)$. Within each algebra θ of ATTRIBUTE(τ), this assertion is either true or false. We select each algebra θ of ATTRIBUTE(τ) only if it satisfies all domain constraints. When that is the case, we write $\theta \models TD$ and, thus, by introducing the set of such algebras DOMAIN(τ) = { $\theta \in ATTRIBUTE(\tau)$: $\theta \models TD$ }, we can write: DOMAIN(τ) |= (DT+KY+ EV+TJ+TA+TD). Note that it is possible that for some τ the class DOMAIN(τ) is empty. Every such trajectory is said to be forbidden (by the domain constraints).

Naturally, the behavior semantics as defined above was not required to satisfy the full structure specification, since the state constraints could not be taken into account. We say that the behavior specification complies with the structure specification state constraints when the are satisfied by every model of the behavior specification in the following sense: (∀te TRAJECTORY) $(\forall \theta \in DOMAIN(\tau))$ TIA =CST. The (linear) temporal interpretation Tla corresponding to each algebra θ in DOMAIN(τ) is defined as follows: Tia=<UNIVERSE, Sa, Ta>, where UNIVERSE is the $(\Sigma_{DT}+\Sigma_{KY})$ -reduct of TRAJECTORY. S_{A=} $\{\mu_{\Theta}(\rho): \rho \in \mathbf{R}(\tau)\}$ and $\mu_{\Theta}(\rho) \mathbf{T}_{\Theta} \mu_{\Theta}(\rho')$ iff ρ is initial part of p'. It remains to define the mapping μ_{Θ} from $\mathbf{R}(\tau)$ into the class of all STRUCT-situations. From the algebra 0 it is easy to build for each trace (initial part of τ) the corresponding situation. Indeed, it is the Σ_{STRUCT} -algebra that maps each state attribute symbol to the value of the corresponding trace attribute symbol at that trace as given by θ .

5 - CONCLUDING REMARKS

The rigorous algebraic semantics of an effective language for the specification of abstract object types (AOTs) was outlined. This semantics provides the Kripke interpretation structure for the envisaged logic of object behavior. Some of the requirements for this logic were discussed, namely concerning the proof of liveness and safety properties of the object societies. Such a language was shown to be useful when describing the universe of discourse as a society of interacting objects. This approach to conceptual modeling provides the means for the complete description of the relevant entities, including their individual and interaction behavior. This description is the starting point for the design of both the database schema and the associated transactions. Indeed, both records and transactions can and should be seen as objects, although the former tend to be more persistent than the latter. Hence, it is possible to design the database and the associated applications as a society of objects of varying persistency. This view also opens up the possibility of extending the current architectures of database management systems (DBMS) towards real **object society management systems** (OSMS).

interesting developments not reported Some were limitations. Namely, the herein due to space quidelines methodological for database desian according to the proposed approach (already under experimentation) and the detailed development of the algebraic semantics concerning the key mechanisms and the object universe construction. On the other hand, further work is necessary concerning the refinement of the behavior semantics in order to deal with infinite trajectories and also to establish the desired temporal structure (either linear or branching). Afterwards, it will be possible to put together the logical calculus for proving properties of the object societies. Other important lines of research are related to the problems of dealing with incomplete information about the objects and of supervising and enforcing database state constraints. Finally, we are also looking at further developments of the language in order to allow parameterized specifications, as well inheritance and as aggregation.

formalism AOT Although the proposed for specification seems rather complex compared to the traditional formalisms for ADT (abstract data type) specification, we believe that it will be rather difficult to simplify it further. Indeed, objects are temporal entities rather more complex than simple values. We expect that future DBMS should incorporate basic facilities for object society management along the lines of our proposal where the chosen interaction mechanism is as simple as possible (event sharing by the interacting objects).

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7 - APPENDIX: trader's world

object type CLIENT key map cli(string) attributes name : string constraints population name(cli(S))=S; cli(name(C))=C individual upper(first(name))=true state attributes integer count : constraints local (zero≤count)=true; (G(N≤count)=true) if (count=N) behavior events creation birth modification issue(integer,STOCK,integer) traces domain [T>>issue(N.K.R)] only If (count at T)=pre(N) equations valuation (count at <birth>)=zero; (count at [T>>issue(N,K,R)])= suc(count at T)

object type ORDER

end

key map ord(CLIENT, integer) attributes numb : integer; CLIENT cli constraints population cli(ord(C,N))=C; numb(ord(C,N))=N;

ord(cli(O),numb(O))=O individual (zero≤numb)=true state attributes stk : STOCK; req : integer constraints local (zero<req)=true; (G(stk=K)) if (stk=K) global there-is cli there-is stk behavior events creation creation(STOCK,integer) destruction satisfaction(STOCK, integer); rejection(STOCK, integer) traces domain [T>>satisfaction(K,R)] only if (stk at T)=K and (req at T)=R; [T>>rejection(K,R)] only if (stk at T)=K and (reg at T)=R equations valuation (stk at <creation(K,R)>)=K; (req at <creation(K,R)>)=R interaction equations C.issue(N,K,R)=ord(C,N).creation(K,R) end object type STOCK key map stk(string,string) attributes prdid : string; depid : string constraints population prdid(stk(S1,S2))=S1; depid(stk(S1,S2))=S2; stk(prdid(K),depid(K))=K state attributes qoh : integer constraints local (zero≤qoh)=true behavior events creation

open destruction close modification delivery(ORDER, integer); failure(ORDER, integer); update(integer) traces domain [T>>update(R)] only if (minus(R)≤(qoh at T))=true; [T>>delivery(O,R)] only if -(R≤(qoh at T))=true; [T>>failure(O,R)] only if ((qoh at T)<R)=true equations equivalence [T>>delivery(O,R)]=[T>>update(-R)]; [T>>failure(O,R)]=T; [T>>update(R1)>>update(R2)]= [T>>update(R1+R2)] valuation (qoh at <open>)=zero; (qoh at <open,update(R)>)=R interaction equations O.satisfaction(K.R)=K.delivery(O,R); O.rejection(K,R)=K.failure(O,R)

end