## Observation of $\boldsymbol{B}^{+} \rightarrow \overline{\boldsymbol{K}}^{\mathbf{0}} \boldsymbol{K}^{+}$and $\boldsymbol{B}^{\mathbf{0}} \rightarrow \boldsymbol{K}^{\mathbf{0}} \overline{\boldsymbol{K}}^{\mathbf{0}}$

B. Aubert, ${ }^{1}$ M. Bona, ${ }^{1}$ D. Boutigny, ${ }^{1}$ F. Couderc, ${ }^{1}$ Y. Karyotakis, ${ }^{1}$ J. P. Lees,,${ }^{1}$ V. Poireau, ${ }^{1}$ V. Tisserand, ${ }^{1}$ A. Zghiche, ${ }^{1}$ E. Grauges, ${ }^{2}$ A. Palano, ${ }^{3}$ J. C. Chen, ${ }^{4}$ N. D. Qi, ${ }^{4}$ G. Rong, ${ }^{4}$ P. Wang, ${ }^{4}$ Y. S. Zhu, ${ }^{4}$ G. Eigen, ${ }^{5}$ I. Ofte, ${ }^{5}$ B. Stugu, ${ }^{5}$ G. S. Abrams, ${ }^{6}$ M. Battaglia, ${ }^{6}$ D. N. Brown, ${ }^{6}$ J. Button-Shafer, ${ }^{6}$ R. N. Cahn, ${ }^{6}$ E. Charles, ${ }^{6}$ M. S. Gill, ${ }^{6}$ Y. Groysman, ${ }^{6}$ R. G. Jacobsen, ${ }^{6}$ J. A. Kadyk, ${ }^{6}$ L. T. Kerth, ${ }^{6}$ Yu. G. Kolomensky, ${ }^{6}$ G. Kukartsev, ${ }^{6}$ G. Lynch, ${ }^{6}$ L. M. Mir, ${ }^{6}$ T. J. Orimoto, ${ }^{6}$ M. Pripstein, ${ }^{6}$ N. A. Roe, ${ }^{6}$ M. T. Ronan, ${ }^{6}$ W. A. Wenzel, ${ }^{6}$ P. del Amo Sanchez, ${ }^{7}$ M. Barrett, ${ }^{7}$ K. E. Ford, ${ }^{7}$ T. J. Harrison, ${ }^{7}$ A. J. Hart, ${ }^{7}$ C. M. Hawkes, ${ }^{7}$ A. T. Watson, ${ }^{7}$ T. Held, ${ }^{8}$ H. Koch, ${ }^{8}$ B. Lewandowski, ${ }^{8}$ M. Pelizaeus, ${ }^{8}$ K. Peters, ${ }^{8}$ T. Schroeder, ${ }^{8}$ M. Steinke, ${ }^{8}$ J. T. Boyd, ${ }^{9}$ J. P. Burke, ${ }^{9}$ W. N. Cottingham, ${ }^{9}$ D. Walker, ${ }^{9}$ D. J. Asgeirsson,,${ }^{10}$ T. Cuhadar-Donszelmann,,$^{10}$ B. G. Fulsom, ${ }^{10}$ C. Hearty, ${ }^{10}$ N. S. Knecht, ${ }^{10}$ T. S. Mattison, ${ }^{10}$ J. A. McKenna, ${ }^{10}$ A. Khan, ${ }^{11}$ P. Kyberd, ${ }^{11}$ M. Saleem, ${ }^{11}$ D. J. Sherwood, ${ }^{11}$ L. Teodorescu, ${ }^{11}$ V.E. Blinov, ${ }^{12}$ A. D. Bukin, ${ }^{12}$ V. P. Druzhinin, ${ }^{12}$ V. B. Golubev, ${ }^{12}$ A. P. Onuchin, ${ }^{12}$ S. I. Serednyakov, ${ }^{12}$ Yu. I. Skovpen, ${ }^{12}$ E. P. Solodov, ${ }^{12}$ K. Yu Todyshev, ${ }^{12}$ M. Bondioli, ${ }^{13}$ M. Bruinsma, ${ }^{13}$ M. Chao, ${ }^{13}$ S. Curry, ${ }^{13}$ I. Eschrich, ${ }^{13}$ D. Kirkby, ${ }^{13}$ A. J. Lankford, ${ }^{13}$ P. Lund, ${ }^{13}$ M. Mandelkern, ${ }^{13}$ R. K. Mommsen, ${ }^{13}$ W. Roethel, ${ }^{13}$ D. P. Stoker, ${ }^{13}$ S. Abachi, ${ }^{14}$ C. Buchanan, ${ }^{14}$ S. D. Foulkes, ${ }^{15}$ J. W. Gary, ${ }^{15}$ O. Long, ${ }^{15}$ B. C. Shen, ${ }^{15}$ K. Wang, ${ }^{15}$ L. Zhang, ${ }^{15}$ H. K. Hadavand, ${ }^{16}$ E. J. Hill, ${ }^{16}$ H. P. Paar, ${ }^{16}$ S. Rahatlou, ${ }^{16}$ V. Sharma, ${ }^{16}$ J. W. Berryhill, ${ }^{17}$ C. Campagnari, ${ }^{17}$ A. Cunha, ${ }^{17}$ B. Dahmes,,$^{17}$ T. M. Hong, ${ }^{17}$ D. Kovalskyi, ${ }^{17}$ J. D. Richman, ${ }^{17}$ T. W. Beck, ${ }^{18}$ A. M. Eisner, ${ }^{18}$ C. J. Flacco, ${ }^{18}$ C. A. Heusch, ${ }^{18}$ J. Kroseberg, ${ }^{18}$ W. S. Lockman, ${ }^{18}$ G. Nesom, ${ }^{18}$ T. Schalk, ${ }^{18}$ B. A. Schumm, ${ }^{18}$ A. Seiden, ${ }^{18}$ P. Spradlin, ${ }^{18}$ D. C. Williams, ${ }^{18}$ M. G. Wilson, ${ }^{18}$ J. Albert, ${ }^{19}$ E. Chen, ${ }^{19}$ A. Dvoretskii, ${ }^{19}$ F. Fang, ${ }^{19}$ D. G. Hitlin, ${ }^{19}$ I. Narsky, ${ }^{19}$ T. Piatenko, ${ }^{19}$ F. C. Porter, ${ }^{19}$
A. Ryd, ${ }^{19}$ G. Mancinelli, ${ }^{20}$ B. T. Meadows, ${ }^{20}$ K. Mishra, ${ }^{20}$ M. D. Sokoloff, ${ }^{20}$ F. Blanc, ${ }^{21}$ P. C. Bloom, ${ }^{21}$ S. Chen, ${ }^{21}$ W. T. Ford, ${ }^{21}$ J.F. Hirschauer, ${ }^{21}$ A. Kreisel, ${ }^{21}$ M. Nagel, ${ }^{21}$ U. Nauenberg, ${ }^{21}$ A. Olivas, ${ }^{21}$ W. O. Ruddick, ${ }^{21}$ J. G. Smith, ${ }^{21}$ K. A. Ulmer, ${ }^{21}$ S. R. Wagner, ${ }^{21}$ J. Zhang, ${ }^{21}$ A. Chen, ${ }^{22}$ E. A. Eckhart, ${ }^{22}$ A. Soffer, ${ }^{22}$ W. H. Toki, ${ }^{22}$ R. J. Wilson, ${ }^{22}$ F. Winklmeier, ${ }^{22}$ Q. Zeng, ${ }^{22}$ D. D. Altenburg, ${ }^{23}$ E. Feltresi, ${ }^{23}$ A. Hauke, ${ }^{23}$ H. Jasper, ${ }^{23}$ J. Merkel, ${ }^{23}$ A. Petzold, ${ }^{23}$ B. Spaan, ${ }^{23}$ T. Brandt, ${ }^{24}$ V. Klose, ${ }^{24}$ H. M. Lacker, ${ }^{24}$ W. F. Mader, ${ }^{24}$ R. Nogowski, ${ }^{24}$ J. Schubert, ${ }^{24}$ K. R. Schubert, ${ }^{24}$ R. Schwierz, ${ }^{24}$ J. E. Sundermann, ${ }^{24}$ A. Volk, ${ }^{24}$ D. Bernard, ${ }^{25}$ G. R. Bonneaud, ${ }^{25}$ E. Latour, ${ }^{25}$ Ch. Thiebaux, ${ }^{25}$ M. Verderi, ${ }^{25}$ P. J. Clark, ${ }^{26}$ W. Gradl, ${ }^{26}$ F. Muheim, ${ }^{26}$ S. Playfer, ${ }^{26}$ A. I. Robertson, ${ }^{26}$ Y. Xie, ${ }^{26}$ M. Andreotti, ${ }^{27}$ D. Bettoni, ${ }^{27}$ C. Bozzi, ${ }^{27}$ R. Calabrese, ${ }^{27}$ G. Cibinetto, ${ }^{27}$ E. Luppi, ${ }^{27}$ M. Negrini, ${ }^{27}$ A. Petrella, ${ }^{27}$ L. Piemontese, ${ }^{27}$ E. Prencipe, ${ }^{27}$ F. Anulli, ${ }^{28}$ R. Baldini-Ferroli, ${ }^{28}$ A. Calcaterra, ${ }^{28}$ R. de Sangro, ${ }^{28}$ G. Finocchiaro, ${ }^{28}$ S. Pacetti, ${ }^{28}$ P. Patteri, ${ }^{28}$ I. M. Peruzzi, ${ }^{28, *}$ M. Piccolo, ${ }^{28}$ M. Rama, ${ }^{28}$ A. Zallo, ${ }^{28}$ A. Buzzo, ${ }^{29}$ R. Contri, ${ }^{29}$ M. Lo Vetere, ${ }^{29}$ M. M. Macri, ${ }^{29}$ M. R. Monge, ${ }^{29}$ S. Passaggio, ${ }^{29}$ C. Patrignani, ${ }^{29}$ E. Robutti, ${ }^{29}$ A. Santroni, ${ }^{29}$ S. Tosi, ${ }^{29}$ G. Brandenburg, ${ }^{30}$ K. S. Chaisanguanthum, ${ }^{30}$ M. Morii, ${ }^{30}$ J. Wu, ${ }^{30}$ R. S. Dubitzky, ${ }^{31}$ J. Marks, ${ }^{31}$ S. Schenk, ${ }^{31}$ U. Uwer, ${ }^{31}$ D. J. Bard, ${ }^{32}$ W. Bhimji, ${ }^{32}$ D. A. Bowerman, ${ }^{32}$ P. D. Dauncey, ${ }^{32}$ U. Egede, ${ }^{32}$ R. L. Flack, ${ }^{32}$ J. A. Nash, ${ }^{32}$ M. B. Nikolich, ${ }^{32}$ W. Panduro Vazquez, ${ }^{32}$ P. K. Behera, ${ }^{33}$ X. Chai, ${ }^{33}$ M. J. Charles, ${ }^{33}$ U. Mallik, ${ }^{33}$ N. T. Meyer, ${ }^{33}$ V. Ziegler, ${ }^{33}$ J. Cochran, ${ }^{34}$ H. B. Crawley, ${ }^{34}$ L. Dong, ${ }^{34}$ V. Eyges, ${ }^{34}$ W. T. Meyer, ${ }^{34}$ S. Prell, ${ }^{34}$ E. I. Rosenberg, ${ }^{34}$ A. E. Rubin, ${ }^{34}$ A. V. Gritsan, ${ }^{35}$ A. G. Denig, ${ }^{36}$ M. Fritsch, ${ }^{36}$ G. Schott, ${ }^{36}$ N. Arnaud, ${ }^{37}$ M. Davier, ${ }^{37}$ G. Grosdidier, ${ }^{37}$ A. Höcker, ${ }^{37}$ F. Le Diberder, ${ }^{37}$ V. Lepeltier, ${ }^{37}$ A. M. Lutz, ${ }^{37}$ A. Oyanguren, ${ }^{37}$ S. Pruvot, ${ }^{37}$ S. Rodier, ${ }^{37}$ P. Roudeau, ${ }^{37}$ M. H. Schune, ${ }^{37}$ A. Stocchi, ${ }^{37}$ W. F. Wang, ${ }^{37}$ G. Wormser, ${ }^{37}$ C. H. Cheng, ${ }^{38}$ D. J. Lange, ${ }^{38}$ D. M. Wright, ${ }^{38}$ C. A. Chavez, ${ }^{39}$ I. J. Forster, ${ }^{39}$ J. R. Fry, ${ }^{39}$ E. Gabathuler, ${ }^{39}$ R. Gamet, ${ }^{39}$ K. A. George, ${ }^{39}$ D. E. Hutchcroft, ${ }^{39}$ D. J. Payne, ${ }^{39}$ K. C. Schofield, ${ }^{39}$ C. Touramanis, ${ }^{39}$ A. J. Bevan, ${ }^{40}$ F. Di Lodovico, ${ }^{40}$ W. Menges, ${ }^{40}$ R. Sacco, ${ }^{40}$ G. Cowan, ${ }^{41}$ H. U. Flaecher, ${ }^{41}$ D. A. Hopkins, ${ }^{41}$ P. S. Jackson, ${ }^{41}$ T. R. McMahon, ${ }^{41}$ S. Ricciardi, ${ }^{41}$ F. Salvatore, ${ }^{41}$ A. C. Wren, ${ }^{41}$ D. N. Brown, ${ }^{42}$ C. L. Davis, ${ }^{42}$ J. Allison, ${ }^{43}$ N. R. Barlow, ${ }^{43}$ R. J. Barlow, ${ }^{43}$ Y. M. Chia, ${ }^{43}$ C. L. Edgar, ${ }^{43}$ G. D. Lafferty, ${ }^{43}$ M. T. Naisbit, ${ }^{43}$ J. C. Williams, ${ }^{43}$ J.I. Yi, ${ }^{43}$ C. Chen, ${ }^{44}$ W. D. Hulsbergen, ${ }^{44}$ A. Jawahery, ${ }^{44}$ C. K. Lae, ${ }^{44}$ D. A. Roberts, ${ }^{44}$ G. Simi, ${ }^{44}$ G. Blaylock, ${ }^{45}$ C. Dallapiccola, ${ }^{45}$ S. S. Hertzbach, ${ }^{45}$ X. Li, ${ }^{45}$ T. B. Moore, ${ }^{45}$ S. Saremi, ${ }^{45}$ H. Staengle, ${ }^{45}$ R. Cowan, ${ }^{46}$ G. Sciolla, ${ }^{46}$ S. J. Sekula, ${ }^{46}$ M. Spitznagel, ${ }^{46}$ F. Taylor, ${ }^{46}$ R. K. Yamamoto, ${ }^{46}$ H. Kim, ${ }^{47}$ S. E. Mclachlin, ${ }^{47}$ P. M. Patel, ${ }^{47}$ S. H. Robertson, ${ }^{47}$ A. Lazzaro, ${ }^{48}$ V. Lombardo, ${ }^{48}$ F. Palombo, ${ }^{48}$ J. M. Bauer, ${ }^{49}$ L. Cremaldi, ${ }^{49}$ V. Eschenburg, ${ }^{49}$ R. Godang, ${ }^{49}$ R. Kroeger, ${ }^{49}$ D. A. Sanders, ${ }^{49}$ D. J. Summers, ${ }^{49}$ H. W. Zhao, ${ }^{49}$ S. Brunet, ${ }^{50}$ D. Côté, ${ }^{50}$ M. Simard, ${ }^{50}$ P. Taras, ${ }^{50}$ F. B. Viaud, ${ }^{50}$ H. Nicholson,,${ }^{51}$ N. Cavallo, ${ }^{52, \dagger}$ G. De Nardo, ${ }^{52}$ F. Fabozzi, ${ }^{52, \dagger}$ C. Gatto, ${ }^{52}$ L. Lista, ${ }^{52}$ D. Monorchio, ${ }^{52}$ P. Paolucci, ${ }^{52}$ D. Piccolo, ${ }^{52}$ C. Sciacca, ${ }^{52}$ M. A. Baak, ${ }^{53}$ G. Raven, ${ }^{53}$ H. L. Snoek, ${ }^{53}$ C. P. Jessop, ${ }^{54}$ J. M. LoSecco, ${ }^{54}$ T. Allmendinger, ${ }^{55}$ G. Benelli, ${ }^{55}$ L. A. Corwin, ${ }^{55}$ K. K. Gan, ${ }^{55}$ K. Honscheid, ${ }^{55}$ D. Hufnagel, ${ }^{55}$ P. D. Jackson, ${ }^{55}$ H. Kagan, ${ }^{55}$ R. Kass, ${ }^{55}$ A. M. Rahimi, ${ }^{55}$ J. J. Regensburger, ${ }^{55}$ R. Ter-Antonyan, ${ }^{55}$ Q. K. Wong, ${ }^{55}$ N. L. Blount, ${ }^{56}$ J. Brau, ${ }^{56}$ R. Frey, ${ }^{56}$ O. Igonkina, ${ }^{56}$ J. A. Kolb, ${ }^{56}$ M. Lu, ${ }^{56}$ R. Rahmat, ${ }^{56}$ N. B. Sinev, ${ }^{56}$ D. Strom, ${ }^{56}$ J. Strube, ${ }^{56}$ E. Torrence, ${ }^{56}$ A. Gaz, ${ }^{57}$ M. Margoni, ${ }^{57}$ M. Morandin, ${ }^{57}$ A. Pompili, ${ }^{57}$ M. Posocco, ${ }^{57}$
M. Rotondo, ${ }^{57}$ F. Simonetto, ${ }^{57}$ R. Stroili, ${ }^{57}$ C. Voci, ${ }^{57}$ M. Benayoun, ${ }^{58}$ H. Briand, ${ }^{58}$ J. Chauveau, ${ }^{58}$ P. David, ${ }^{58}$ L. Del Buono, ${ }^{58}$ Ch. de la Vaissière, ${ }^{58}$ O. Hamon, ${ }^{58}$ B. L. Hartfiel, ${ }^{58}$ Ph. Leruste, ${ }^{58}$ J. Malclès, ${ }^{58}$ J. Ocariz, ${ }^{58}$ L. Roos, ${ }^{58}$ G. Therin, ${ }^{58}$ L. Gladney, ${ }^{59}$ M. Biasini, ${ }^{60}$ R. Covarelli, ${ }^{60}$ C. Angelini, ${ }^{61}$ G. Batignani, ${ }^{61}$ S. Bettarini, ${ }^{61}$ F. Bucci, ${ }^{61}$ G. Calderini, ${ }^{61}$ M. Carpinelli, ${ }^{61}$ R. Cenci, ${ }^{61}$ F. Forti, ${ }^{61}$ M. A. Giorgi, ${ }^{61}$ A. Lusiani, ${ }^{61}$ G. Marchiori, ${ }^{61}$ M. A. Mazur, ${ }^{61}$ M. Morganti, ${ }^{61}$ N. Neri, ${ }^{61}$ E. Paoloni, ${ }^{61}$ G. Rizzo, ${ }^{61}$ J. J. Walsh, ${ }^{61}$ M. Haire, ${ }^{62}$ D. Judd, ${ }^{62}$ D. E. Wagoner, ${ }^{62}$ J. Biesiada, ${ }^{63}$ N. Danielson, ${ }^{63}$ P. Elmer, ${ }^{63}$ Y. P. Lau, ${ }^{63}$ C. Lu, ${ }^{63}$ J. Olsen, ${ }^{63}$ A. J. S. Smith, ${ }^{63}$ A. V. Telnov, ${ }^{63}$ F. Bellini, ${ }^{64}$ G. Cavoto, ${ }^{64}$ A. D'Orazio, ${ }^{64}$ D. del Re, ${ }^{64}$ E. Di Marco, ${ }^{64}$ R. Faccini, ${ }^{64}$ F. Ferrarotto, ${ }^{64}$ F. Ferroni, ${ }^{64}$ M. Gaspero, ${ }^{64}$ L. Li Gioi, ${ }^{64}$ M. A. Mazzoni, ${ }^{64}$ S. Morganti, ${ }^{64}$ G. Piredda, ${ }^{64}$ F. Polci, ${ }^{64}$ F. Safai Tehrani, ${ }^{64}$ C. Voena, ${ }^{64}$ M. Ebert, ${ }^{65}$ H. Schröder, ${ }^{65}$ R. Waldi, ${ }^{65}$ T. Adye, ${ }^{66}$ N. De Groot, ${ }^{66}$ B. Franek, ${ }^{66}$ E. O. Olaiya, ${ }^{66}$ F. F. Wilson, ${ }^{66}$ R. Aleksan, ${ }^{67}$ S. Emery, ${ }^{67}$ A. Gaidot, ${ }^{67}$ S. F. Ganzhur, ${ }^{67}$ G. Hamel de Monchenault, ${ }^{67}$ W. Kozanecki, ${ }^{67}$ M. Legendre, ${ }^{67}$ G. Vasseur, ${ }^{67}$ Ch. Yèche, ${ }^{67}$ M. Zito, ${ }^{67}$ X. R. Chen,,$^{68}$ H. Liu, ${ }^{68}$ W. Park, ${ }^{68}$ M. V. Purohit, ${ }^{68}$ J. R. Wilson, ${ }^{68}$ M. T. Allen, ${ }^{69}$ D. Aston, ${ }^{69}$ R. Bartoldus, ${ }^{69}$ P. Bechtle, ${ }^{69}$ N. Berger, ${ }^{69}$ R. Claus, ${ }^{69}$ J. P. Coleman, ${ }^{69}$ M. R. Convery, ${ }^{69}$ M. Cristinziani, ${ }^{69}$ J. C. Dingfelder, ${ }^{69}$ J. Dorfan, ${ }^{69}$ G. P. Dubois-Felsmann, ${ }^{69}$ D. Dujmic, ${ }^{69}$ W. Dunwoodie, ${ }^{69}$ R. C. Field, ${ }^{69}$ T. Glanzman, ${ }^{69}$ S. J. Gowdy, ${ }^{69}$ M. T. Graham, ${ }^{69}$ P. Grenier, ${ }^{69}$ V. Halyo, ${ }^{69}$ C. Hast, ${ }^{69}$ T. Hryn'ova, ${ }^{69}$ W. R. Innes, ${ }^{69}$ M. H. Kelsey, ${ }^{69}$ P. Kim, ${ }^{69}$ D. W. G. S. Leith, ${ }^{69}$ S. Li, ${ }^{69}$ S. Luitz, ${ }^{69}$ V. Luth, ${ }^{69}$ H. L. Lynch, ${ }^{69}$ D. B. MacFarlane, ${ }^{69}$ H. Marsiske, ${ }^{69}$ R. Messner, ${ }^{69}$ D. R. Muller, ${ }^{69}$ C. P. O'Grady, ${ }^{69}$ V. E. Ozcan, ${ }^{69}$ A. Perazzo, ${ }^{69}$ M. Perl, ${ }^{69}$ T. Pulliam, ${ }^{69}$ B. N. Ratcliff, ${ }^{69}$ A. Roodman, ${ }^{69}$ A. A. Salnikov, ${ }^{69}$ R. H. Schindler, ${ }^{69}$ J. Schwiening, ${ }^{69}$ A. Snyder, ${ }^{69}$ J. Stelzer, ${ }^{69}$ D. Su, ${ }^{69}$ M. K. Sullivan, ${ }^{69}$ K. Suzuki, ${ }^{69}$ S. K. Swain, ${ }^{69}$ J. M. Thompson, ${ }^{69}$ J. Va'vra, ${ }^{69}$ N. van Bakel, ${ }^{69}$ M. Weaver, ${ }^{69}$ A. J. R. Weinstein, ${ }^{69}$ W. J. Wisniewski, ${ }^{69}$ M. Wittgen, ${ }^{69}$ D. H. Wright, ${ }^{69}$ A. K. Yarritu, ${ }^{69}$ K. Yi, ${ }^{69}$ C. C. Young, ${ }^{69}$ P. R. Burchat, ${ }^{70}$ A. J. Edwards, ${ }^{70}$ S. A. Majewski, ${ }^{70}$ B. A. Petersen, ${ }^{70}$ C. Roat, ${ }^{70}$ L. Wilden, ${ }^{70}$ S. Ahmed, ${ }^{71}$ M. S. Alam, ${ }^{71}$ R. Bula, ${ }^{71}$ J. A. Ernst, ${ }^{71}$ V. Jain, ${ }^{71}$ B. Pan, ${ }^{71}$ M. A. Saeed, ${ }^{71}$ F. R. Wappler, ${ }^{71}$ S.B. Zain, ${ }^{71}$ W. Bugg, ${ }^{72}$ M. Krishnamurthy, ${ }^{72}$ S. M. Spanier, ${ }^{72}$ R. Eckmann, ${ }^{73}$ J. L. Ritchie, ${ }^{73}$ A. Satpathy, ${ }^{73}$ C. J. Schilling, ${ }^{73}$ R. F. Schwitters, ${ }^{73}$ J. M. Izen, ${ }^{74}$ X. C. Lou, ${ }^{74}$ S. Ye, ${ }^{74}$ F. Bianchi, ${ }^{75}$ F. Gallo, ${ }^{75}$ D. Gamba, ${ }^{75}$ M. Bomben, ${ }^{76}$ L. Bosisio, ${ }^{76}$ C. Cartaro, ${ }^{76}$ F. Cossutti, ${ }^{76}$ G. Della Ricca, ${ }^{76}$ S. Dittongo, ${ }^{76}$ L. Lanceri, ${ }^{76}$ L. Vitale, ${ }^{76}$ V. Azzolini, ${ }^{77}$ N. Lopez-March, ${ }^{77}$ F. Martinez-Vidal, ${ }^{77}$ Sw. Banerjee, ${ }^{78}$ B. Bhuyan, ${ }^{78}$ C. M. Brown, ${ }^{78}$ D. Fortin, ${ }^{78}$ K. Hamano, ${ }^{78}$ R. Kowalewski, ${ }^{78}$ I. M. Nugent, ${ }^{78}$ J. M. Roney, ${ }^{78}$ R. J. Sobie, ${ }^{78}$ J. J. Back, ${ }^{79}$ P. F. Harrison, ${ }^{79}$ T. E. Latham, ${ }^{79}$ G. B. Mohanty, ${ }^{79}$ M. Pappagallo, ${ }^{79}$ H. R. Band, ${ }^{80}$ X. Chen, ${ }^{80}$ B. Cheng, ${ }^{80}$ S. Dasu, ${ }^{80}$ M. Datta, ${ }^{80}$ K. T. Flood, ${ }^{80}$ J. J. Hollar, ${ }^{80}$ P.E. Kutter, ${ }^{80}$ B. Mellado, ${ }^{80}$ A. Mihalyi, ${ }^{80}$ Y. Pan, ${ }^{80}$ M. Pierini, ${ }^{80}$ R. Prepost, ${ }^{80}$

$$
\text { S.L. Wu, }{ }^{80} \mathrm{Z} . \mathrm{Yu},{ }^{80} \text { and H. Neal }{ }^{81}
$$

## (BABAR Collaboration)

${ }^{1}$ Laboratoire de Physique des Particules, IN2P3/CNRS et Université de Savoie, F-74941 Annecy-Le-Vieux, France
${ }^{2}$ Universitat de Barcelona, Facultat de Fisica, Departament ECM, E-08028 Barcelona, Spain
${ }^{3}$ Università di Bari, Dipartimento di Fisica and INFN, I-70126 Bari, Italy ${ }^{4}$ Institute of High Energy Physics, Beijing 100039, China
${ }^{5}$ University of Bergen, Institute of Physics, N-5007 Bergen, Norway
${ }^{6}$ Lawrence Berkeley National Laboratory and University of California, Berkeley, California 94720, USA
${ }^{7}$ University of Birmingham, Birmingham, B15 2TT, United Kingdom
${ }^{8}$ Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany
${ }^{9}$ University of Bristol, Bristol BS8 1TL, United Kingdom
${ }^{10}$ University of British Columbia, Vancouver, British Columbia, Canada V6T $1 Z 1$
${ }^{11}$ Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom
${ }^{12}$ Budker Institute of Nuclear Physics, Novosibirsk 630090, Russia
${ }^{13}$ University of California at Irvine, Irvine, California 92697, USA
${ }^{14}$ University of California at Los Angeles, Los Angeles, California 90024, USA
${ }^{15}$ University of California at Riverside, Riverside, California 92521, USA
${ }^{16}$ University of California at San Diego, La Jolla, California 92093, USA
${ }^{17}$ University of California at Santa Barbara, Santa Barbara, California 93106, USA
${ }^{18}$ University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, California 95064, USA
${ }^{19}$ California Institute of Technology, Pasadena, California 91125, USA
${ }^{20}$ University of Cincinnati, Cincinnati, Ohio 45221, USA
${ }^{21}$ University of Colorado, Boulder, Colorado 80309, USA
${ }^{22}$ Colorado State University, Fort Collins, Colorado 80523, USA
${ }^{23}$ Universität Dortmund, Institut für Physik, D-44221 Dortmund, Germany
${ }^{24}$ Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany

${ }^{25}$ Laboratoire Leprince-Ringuet, CNRS/IN2P3, Ecole Polytechnique, F-91128 Palaiseau, France<br>${ }^{26}$ University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom<br>${ }^{27}$ Università di Ferrara, Dipartimento di Fisica and INFN, I-44100 Ferrara, Italy<br>${ }^{28}$ Laboratori Nazionali di Frascati dell'INFN, I-00044 Frascati, Italy<br>${ }^{29}$ Università di Genova, Dipartimento di Fisica and INFN, I-16146 Genova, Italy<br>${ }^{30}$ Harvard University, Cambridge, Massachusetts 02138, USA<br>${ }^{31}$ Universität Heidelberg, Physikalisches Institut, Philosophenweg 12, D-69120 Heidelberg, Germany<br>${ }^{32}$ Imperial College London, London, SW7 2AZ, United Kingdom<br>${ }^{33}$ University of Iowa, Iowa City, Iowa 52242, USA<br>${ }^{34}$ Iowa State University, Ames, Iowa 50011-3160, USA<br>${ }^{35}$ Johns Hopkins University, Baltimore, Maryland 21218, USA<br>${ }^{36}$ Universität Karlsruhe, Institut für Experimentelle Kernphysik, D-76021 Karlsruhe, Germany<br>${ }^{37}$ Laboratoire de l'Accélérateur Linéaire, IN2P3/CNRS et Université Paris-Sud 11, Centre Scientifique d'Orsay, B.P. 34, F-91898 ORSAY Cedex, France<br>${ }^{38}$ Lawrence Livermore National Laboratory, Livermore, California 94550, USA<br>${ }^{39}$ University of Liverpool, Liverpool L69 7ZE, United Kingdom<br>${ }^{40}$ Queen Mary, University of London, E1 4NS, United Kingdom<br>${ }^{41}$ University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom<br>${ }^{42}$ University of Louisville, Louisville, Kentucky 40292, USA<br>${ }^{43}$ University of Manchester, Manchester M13 9PL, United Kingdom<br>${ }^{44}$ University of Maryland, College Park, Maryland 20742, USA<br>${ }^{45}$ University of Massachusetts, Amherst, Massachusetts 01003, USA<br>${ }^{46}$ Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA<br>${ }^{47}$ McGill University, Montréal, Québec, Canada H3A $2 T 8$<br>${ }^{48}$ Università di Milano, Dipartimento di Fisica and INFN, I-20133 Milano, Italy<br>${ }^{49}$ University of Mississippi, University, Mississippi 38677, USA<br>${ }^{50}$ Université de Montréal, Physique des Particules, Montréal, Québec, Canada H3C 3J7<br>${ }^{51}$ Mount Holyoke College, South Hadley, Massachusetts 01075, USA<br>${ }^{52}$ Università di Napoli Federico II, Dipartimento di Scienze Fisiche and INFN, I-80126, Napoli, Italy<br>${ }^{53}$ NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands<br>${ }^{54}$ University of Notre Dame, Notre Dame, Indiana 46556, USA<br>${ }^{55}$ Ohio State University, Columbus, Ohio 43210, USA<br>${ }^{56}$ University of Oregon, Eugene, Oregon 97403, USA<br>${ }^{57}$ Università di Padova, Dipartimento di Fisica and INFN, I-35131 Padova, Italy<br>${ }^{58}$ Laboratoire de Physique Nucléaire et de Hautes Energies, IN2P3/CNRS, Université Pierre et Marie Curie-Paris6, Université Denis Diderot-Paris7, F-75252 Paris, France<br>${ }^{59}$ University of Pennsylvania, Philadelphia, Pennsylvania 19104, USA<br>${ }^{60}$ Università di Perugia, Dipartimento di Fisica and INFN, I-06100 Perugia, Italy<br>${ }^{61}$ Università di Pisa, Dipartimento di Fisica, Scuola Normale Superiore and INFN, I-56127 Pisa, Italy<br>${ }^{62}$ Prairie View A\&M University, Prairie View, Texas 77446, USA<br>${ }^{63}$ Princeton University, Princeton, New Jersey 08544, USA<br>${ }^{64}$ Università di Roma La Sapienza, Dipartimento di Fisica and INFN, I-00185 Roma, Italy<br>${ }^{65}$ Universität Rostock, D-18051 Rostock, Germany<br>${ }^{66}$ Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom<br>${ }^{67}$ DSM/Dapnia, CEA/Saclay, F-91191 Gif-sur-Yvette, France<br>${ }^{68}$ University of South Carolina, Columbia, South Carolina 29208, USA<br>${ }^{69}$ Stanford Linear Accelerator Center, Stanford, California 94309, USA<br>${ }^{70}$ Stanford University, Stanford, California 94305-4060, USA<br>${ }^{71}$ State University of New York, Albany, New York 12222, USA<br>${ }^{72}$ University of Tennessee, Knoxville, Tennessee 37996, USA<br>${ }^{73}$ University of Texas at Austin, Austin, Texas 78712, USA<br>${ }^{74}$ University of Texas at Dallas, Richardson, Texas 75083, USA<br>${ }^{75}$ Università di Torino, Dipartimento di Fisica Sperimentale and INFN, I-10125 Torino, Italy<br>${ }^{76}$ Università di Trieste, Dipartimento di Fisica and INFN, I-34127 Trieste, Italy<br>${ }^{77}$ IFIC, Universitat de Valencia-CSIC, E-46071 Valencia, Spain<br>${ }^{78}$ University of Victoria, Victoria, British Columbia, Canada V8W 3P6<br>${ }^{79}$ Department of Physics, University of Warwick, Coventry CV4 7AL, United Kingdom<br>${ }^{80}$ University of Wisconsin, Madison, Wisconsin 53706, USA<br>${ }^{81}$ Yale University, New Haven, Connecticut 06511, USA<br>(Received 12 August 2006; published 25 October 2006)

We report observations of the $b \rightarrow d$ penguin-dominated decays $B^{+} \rightarrow \bar{K}^{0} K^{+}$and $B^{0} \rightarrow K^{0} \bar{K}^{0}$ in $316 \mathrm{fb}^{-1}$ of $e^{+} e^{-}$collision data collected with the $B A B A R$ detector. We measure the branching fractions $\mathcal{B}\left(B^{+} \rightarrow \bar{K}^{0} K^{+}\right)=(1.61 \pm 0.44 \pm 0.09) \times 10^{-6}$ and $\mathcal{B}\left(B^{0} \rightarrow K^{0} \bar{K}^{0}\right)=(1.08 \pm 0.28 \pm 0.11) \times 10^{-6}$ and the $C P$-violating charge asymmetry $\mathcal{A}_{C P}\left(\bar{K}^{0} K^{+}\right)=0.10 \pm 0.26 \pm 0.03$. Using a vertexing technique previously employed in several analyses of all-neutral final states containing kaons, we report the first measurement of time-dependent $C P$-violating asymmetries in $\quad B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$, obtaining $S=$ $-1.28_{-0.73}^{+0.80+0.11}$ and $C=-0.40 \pm 0.41 \pm 0.06$. We also report improved measurements of the branching fraction $\mathcal{B}\left(B^{+} \rightarrow K^{0} \pi^{+}\right)=(23.9 \pm 1.1 \pm 1.0) \times 10^{-6}$ and $C P$-violating charge asymmetry $\mathcal{A}_{C P}\left(K^{0} \pi^{+}\right)=-0.029 \pm 0.039 \pm 0.010$.

DOI: 10.1103/PhysRevLett.97.171805
PACS numbers: $13.25 . \mathrm{Hw}, 11.30 . \mathrm{Er}$, 12.15.Hh

The decays $B^{+} \rightarrow \bar{K}^{0} K^{+}$and $B^{0} \rightarrow K^{0} \bar{K}^{0}$ are expected to be dominated by the flavor-changing neutral-current process $b \rightarrow d \bar{s} s$, which is highly suppressed in the standard model and potentially sensitive to the presence of new particles in a way analogous to $b \rightarrow s \bar{s} s$ decays such as $B \rightarrow \phi K[1,2]$. Assuming top-quark dominance in the virtual loop mediating the $b \rightarrow d$ transition [3], the charge asymmetry in $B^{+} \rightarrow \bar{K}^{0} K^{+}$and the time-dependent $C P$-violating asymmetry parameters in $B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$ are expected to vanish, while contributions from lighter quarks or supersymmetric particles could induce observable asymmetries [4]. It has been noted [5] that the branching fraction and $C P$ asymmetries in $B^{0} \rightarrow K^{0} \bar{K}^{0}$ are related in a nearly model-independent way, providing a sensitive test of the standard model description of $C P$ violation.

In this Letter, we report observations of $B^{+} \rightarrow \bar{K}^{0} K^{+}$ and $B^{0} \rightarrow K^{0} \bar{K}^{0}$ using a data sample approximately $50 \%$ larger than the one used in our previous search [6]. (The use of charge-conjugate modes is implied throughout this Letter unless otherwise stated.) In addition to establishing these decay modes, we present measurements of the timedependent $C P$-violating asymmetries in $B^{0} \rightarrow K^{0} \bar{K}^{0}$ for the first time. We also report updated measurements of the branching fraction and charge asymmetry in the $S U(3)$-related decay $B^{+} \rightarrow K^{0} \pi^{+}$.

The $C P$ asymmetry in $B^{0} \rightarrow K^{0} \bar{K}^{0}$ (observed in the $K_{S}^{0} K_{S}^{0}$ final state) is determined from the difference in the time-dependent decay rates for $B^{0}$ and $\bar{B}^{0}$. In the process $e^{+} e^{-} \rightarrow \Upsilon(4 S) \rightarrow B^{0} \bar{B}^{0}$, the decay rate $f_{+}\left(f_{-}\right)$is given by [7]

$$
\begin{equation*}
f_{ \pm}(\Delta t)=\frac{e^{-|\Delta t| / \tau}}{4 \tau}\left[1 \pm S \sin \left(\Delta m_{d} \Delta t\right) \mp C \cos \left(\Delta m_{d} \Delta t\right)\right] \tag{1}
\end{equation*}
$$

when the second $B$ meson in the event (denoted $B_{\mathrm{tag}}$ ) is identified as $B^{0}\left(\bar{B}^{0}\right)$. Here $\Delta t$ is the time difference between the decays of the signal and $B_{\mathrm{tag}}$ mesons, $\tau$ is the average $B^{0}$ lifetime, and $\Delta m_{d}$ is the $B^{0}-\bar{B}^{0}$ mixing frequency. The amplitude $S$ describes $C P$ violation in the interference between mixed and unmixed decays into the same final state, while $C$ describes direct $C P$ violation in decay.

The data sample used in this analysis contains ( $347.5 \pm$ 3.8) $\times 10^{6} Y(4 S) \rightarrow B \bar{B}$ decays collected by the BABAR
detector [8] at the Stanford Linear Accelerator Center's (SLAC) PEP-II asymmetric-energy $e^{+} e^{-}$collider. The primary detector elements used in this analysis are a charged-particle tracking system, consisting of a five-layer silicon vertex tracker and a 40-layer drift chamber surrounded by a $1.5-\mathrm{T}$ solenoidal magnet, and a dedicated particle-identification system, consisting of a detector of internally reflected Cherenkov light.

We identify two separate event samples corresponding to the decays $B^{+} \rightarrow K_{S}^{0} h^{+}$and $B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$, where $h^{+}$is either a pion or a kaon. Neutral kaons are reconstructed in the mode $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$by combining pairs of oppositely charged tracks originating from a common decay point and satisfying selection requirements on their invariant mass and proper decay time. Candidate $h^{+}$tracks are assigned the pion mass and are required to originate from the interaction region and to have a well-measured Cherenkov angle $\left(\theta_{c}\right)$ consistent with either the pion or kaon particle hypothesis.

For each $B^{0}$ candidate, we require the absolute value of the difference $\Delta E$ between its reconstructed energy in the center-of-mass (c.m.) frame and the beam energy ( $\sqrt{s} / 2$ ) to be less than 100 MeV . For $B^{+}$candidates, we require $-115<\Delta E<75 \mathrm{MeV}$, where the lower limit accounts for an average shift in $\Delta E$ of -45 MeV in the $\bar{K}^{0} K^{+}$mode due to the assignment of the pion mass to the $K^{+}$candidate. We also define a beam-energy substituted mass $m_{\mathrm{ES}} \equiv \sqrt{\left(s / 2+\mathbf{p}_{i} \cdot \mathbf{p}_{B}\right)^{2} / E_{i}^{2}-\mathbf{p}_{B}^{2}}$, where the $B$-candidate momentum $\mathbf{p}_{B}$ and the four-momentum of the initial $e^{+} e^{-}$state $\left(E_{i}, \mathbf{p}_{i}\right)$ are calculated in the laboratory frame. We require $5.20<m_{\mathrm{ES}}<5.29 \mathrm{GeV} / c^{2}$ for $B$ candidates in both samples. To suppress the dominant background arising from the process $e^{+} e^{-} \rightarrow q \bar{q}(q=u, d, s, c)$, we calculate the c.m. angle $\theta_{S}^{*}$ between the sphericity axis [9] of the $B$ candidate and the sphericity axis of the remaining charged and neutral particles in the event and require $\left|\cos \theta_{S}^{*}\right|<0.8$.

After applying all of the above requirements, we find 2321 (30 159) candidates in the $B^{0}\left(B^{+}\right)$sample. The total detection efficiencies are given in Table I and include the branching fraction for $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$[11] and a probability of $50 \%$ for $K^{0} \bar{K}^{0} \rightarrow K_{S}^{0} K_{S}^{0}$ [12]. We use data and simulated Monte Carlo samples [13] to verify that backgrounds from other $B$ decays are negligible.

TABLE I. Summary of results for the total detection efficiencies $\varepsilon$, fitted signal yields $n$, signal-yield significances $s$ (including systematic uncertainty), charge-averaged branching fractions $\mathcal{B}$, and charge asymmetries $\mathcal{A}_{C P}$ (including $90 \%$ confidence intervals). The efficiencies include the branching fraction for $K_{S}^{0} \rightarrow \pi^{+} \pi^{-}$and the probability of $50 \%$ for $K^{0} \bar{K}^{0} \rightarrow K_{S}^{0} K_{S}^{0}$. Branching fractions are calculated assuming equal rates for $Y(4 S) \rightarrow B^{0} \bar{B}^{0}$ and $B^{+} B^{-}$[10].

| Mode | $\varepsilon(\%)$ | $n$ | $s(\sigma)$ | $\mathcal{B}\left(10^{-6}\right)$ | $\mathcal{A}_{C P}$ | $\mathcal{A}_{C P}(90 \%$ C.L.) |
| :---: | ---: | :---: | :---: | :---: | :---: | :---: |
| $B^{+} \rightarrow K^{0} \pi^{+}$ | $12.9 \pm 0.4$ | $1072 \pm 46_{-37}^{+32}$ |  | $23.9 \pm 1.1 \pm 1.0$ | $-0.029 \pm 0.039 \pm 0.010$ | $[-0.092,0.036]$ |
| $B^{+} \rightarrow \bar{K}^{0} K^{+}$ | $12.6 \pm 0.4$ | $71 \pm 19 \pm 4$ | 5.3 | $1.61 \pm 0.44 \pm 0.09$ | $0.10 \pm 0.26 \pm 0.03$ | $[-0.31,0.54]$ |
| $B^{0} \rightarrow K^{0} \bar{K}^{0}$ | $8.5 \pm 0.3$ | $32 \pm 8 \pm 3$ | 7.3 | $1.08 \pm 0.28 \pm 0.11$ |  |  |

A multivariate technique [14] is employed to determine the flavor of the $B_{\text {tag }}$ meson in the $B^{0}$ sample. Separate neural networks are trained to identify primary leptons, kaons, low-momentum pions from $D^{*}$ decays, and highmomentum charged particles from $B$ decays. Events are assigned to one of six mutually exclusive "tagging" categories. The quality of tagging is expressed in terms of the effective efficiency $Q=\sum_{k} \epsilon_{k}\left(1-2 w_{k}\right)^{2}$, where $\epsilon_{k}$ and $w_{k}$ are the efficiencies and mistag probabilities, respectively, for events tagged in category $k$. We measure the tagging performance in a data sample of fully reconstructed neutral $B$ decays ( $B_{\text {flav }}$ ) to $D^{(*)-}\left(\pi^{+}, \rho^{+}, a_{1}^{+}\right)$, where the flavor of the decaying $B$ meson is known, and find a total effective efficiency of $Q=(30.4 \pm 0.3) \%$.

The time difference $\Delta t \equiv \Delta z / \beta \gamma c$ is obtained from the known boost of the $e^{+} e^{-}$system $(\beta \gamma=0.56)$ and the measured distance $\Delta z$ along the beam $(z)$ axis between the $B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$ and $B_{\text {tag }}$ decay vertices. The position of the $B_{\text {tag }}$ vertex is determined from the remaining charged particles in the event after removing the four tracks composing the signal candidate. Despite the relatively long lifetime of the $K_{S}^{0}$ mesons, the $z$ position of the $B$-candidate decay point is obtained reliably by exploiting the precise knowledge of the interaction point using the technique described in Ref. [15]. We compute $\Delta t$ and its error from a combined fit to the $Y(4 S) \rightarrow B^{0} \bar{B}^{0}$ decay, including the constraint from the known average lifetime of the $B^{0}$ meson. Approximately $82 \%$ of signal events contain a $K_{S}^{0}$ reconstructed from pions that each have at least two hits in the silicon vertex tracker, providing sufficiently small $\Delta t$ uncertainty ( 0.9 ps ) to perform the measurement. We require $|\Delta t|<20 \mathrm{ps}$ and $\sigma_{\Delta t}<2.5 \mathrm{ps}$, where $\sigma_{\Delta t}$ is the uncertainty on $\Delta t$ determined separately for each event. The resolution function for signal candidates is a sum of three Gaussian distributions with parameters determined from the $B_{\text {flav }}$ sample [14]. The background $\Delta t$ distribution has the same functional form as the signal resolution function, with parameters determined directly from data.

To obtain the yields and $C P$ violating asymmetry parameters in each sample, we apply separate unbinned maximum-likelihood fits incorporating discriminating variables that account for differences between $B \bar{B}$ and $q \bar{q}$ events. In addition to the kinematic variables $m_{\mathrm{ES}}$ and $\Delta E$, we include a Fisher discriminant $\mathcal{F}$ [16], defined as
an optimized linear combination of the event-shape variables $\sum_{i} p_{i}^{*}$ and $\sum_{i} p_{i}^{*} \cos ^{2} \theta_{i}^{*}$, where $p_{i}^{*}$ is the c.m. momentum of particle $i, \theta_{i}^{*}$ is the c.m. angle between the momentum of particle $i$ and the $B$-candidate thrust axis, and the sum is over all particles in the event excluding the $B$ daughters. For the fit to the $B^{+}$sample, we include the Cherenkov angle measurement to separate $K_{S}^{0} \pi^{+}$and $K_{S}^{0} K^{+}$decays. For the $B^{0}$ sample, we include $\Delta t$ to determine the $C P$-violating asymmetry parameters $S$ and $C$ simultaneously with the signal yield.

The likelihood function to be maximized is defined as $\mathcal{L}=\exp \left(-\sum_{i} n_{i}\right) \prod_{j=1}^{N}\left[\sum_{i} n_{i} \mathcal{P}_{i}\right]$, where $n_{i}$ and $\mathcal{P}_{i}$ are the yield and probability density function (PDF) for each component $i$ in the fit, and $N$ is the total number of events in the sample. For the $B^{0}$ sample, there are two components (signal and background), and the total PDF is calculated as the product of the individual PDFs for $m_{\mathrm{ES}}, \Delta E, \mathcal{F}$, and $\Delta t$. The signal $\Delta t$ PDF is derived from Eq. (1), modified to take into account the mistag probability, and convolved with the resolution function. We combine $B^{+}$and $B^{-}$candidates in a single fit and include the PDF for $\theta_{c}$ to determine separate yields and charge asymmetries for the two signal components $K_{S}^{0} \pi$ and $K_{S}^{0} K$ and two corresponding background components. For both signal and background, the $K_{S}^{0} h^{ \pm}$yields are parametrized as $n_{ \pm}=n\left(1 \mp \mathcal{A}_{C P}\right) / 2$; we fit directly for the total yield $n$ and the charge asymmetry $\mathcal{A}_{C P}$. We have found correlations among the PDF variables in the fit to be negligible in both the $B^{0}$ and the $B^{+}$ samples.

The parametrizations of the PDFs are determined from data wherever possible. In both samples, we exploit the large sideband regions in $m_{\text {ES }}$ and $\Delta E$ to determine all background PDF parameters simultaneously with the yields and $C P$ asymmetries in the fits. For the $B^{+}$sample, the large signal $K_{S}^{0} \pi^{+}$component allows for an accurate determination of the peak positions for $m_{\mathrm{ES}}$ and $\Delta E$, as well as the parameters describing the shape of the PDF for $\mathcal{F}$. The remaining shape parameters describing $m_{\text {ES }}$ and $\Delta E$ are determined from simulated Monte Carlo samples and are fixed in the fit. We use the $K_{S}^{0} \pi^{+}$parameters to describe signal $K_{S}^{0} K^{+}$PDFs in $m_{\mathrm{ES}}, \Delta E$, and $\mathcal{F}$, taking into account the known shift in the mean of $\Delta E$ due to the pionmass hypothesis. For both signal and background, the $\theta_{c}$ PDFs are obtained from a sample of $D^{*+} \rightarrow D^{0} \pi^{+}\left(D^{0} \rightarrow\right.$ $K^{-} \pi^{+}$) decays reconstructed in data, as described in

Ref. [17]. For the $B^{0}$ sample, all shape parameters describing the $m_{\mathrm{ES}}, \Delta E$, and $\mathcal{F}$ signal PDFs are fixed to the values determined from Monte Carlo simulation except the peak position for $\Delta E$, which is derived from the results of the fit to the $B^{+}$sample.

Several cross-checks were performed to validate the fitting technique before data in the signal region were examined. We checked for biases by performing pseudoexperiments where simulated Monte Carlo signal events were mixed with background events generated directly from the PDFs according to the expected yields in the data. The resulting small biases on the yields include effects of incorrect particle identification and are accounted for in the systematic uncertainties.

The fit results supersede our previous measurements of these quantities and are summarized in Table I. The signal yields for $B^{+} \rightarrow K_{S}^{0} K^{+}$and $B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$ correspond to significances of $5.3 \sigma$ and $7.3 \sigma$ (including systematic uncertainties), respectively, and are consistent with our previous measurements [6], as well as with recent results by the Belle Collaboration [18]. The significances are computed by taking the square root of the change in $2 \ln \mathcal{L}$ when the appropriate yield is fixed to zero. The fit to the $B^{0}$ sample yields $S=-1.28_{-0.73-0.16}^{+0.80+0.11}$ and $C=-0.40 \pm$ $0.41 \pm 0.06$, where the first errors are statistical and the second are systematic. The linear correlation coefficient between $S$ and $C$ is $-32 \%$.

In Fig. 1, we compare data and PDFs using the eventweighting technique described in Ref. [19]. We perform fits excluding the variable being shown; the covariance
matrix and remaining PDFs are used to determine a weight that each event is either signal (main plot) or background (inset). The resulting distributions (points with errors) are normalized to the appropriate yield and can be directly compared with the PDFs (solid curves) used in the fits. We find good agreement between data and the assumed shapes in both $m_{\mathrm{ES}}$ and $\Delta E$. In Fig. 2, we display the $\Delta t$ distributions for $K_{S}^{0} K_{S}^{0}$ events tagged as $B^{0}$ or $\bar{B}^{0}$ and the asymmetry $\mathcal{A}=\left(N_{B^{0}}-N_{\bar{B}^{0}}\right) /\left(N_{B^{0}}+N_{\bar{B}^{0}}\right)$. The projections are enhanced in signal decays by selecting on probability ratios calculated from the signal and background PDFs (excluding $\Delta t$ ). The likelihood function in the $B^{0} \rightarrow$ $K_{S}^{0} K_{S}^{0}$ fit is used to derive Bayesian confidence-level contours in the $C$ vs $S$ plane by fixing $(S, C)$ to specific values, refitting the data, and recording the change in $-2 \log \mathcal{L}$. Figure 2 shows the resulting $n \sigma$ contours in the physical region defined by $S^{2}+C^{2}<1$.

Systematic uncertainties on the signal yields are primarily due to the imperfect knowledge of the PDF shapes. We evaluate this uncertainty by varying the PDF parameters that are fixed in the fit within their statistical errors and by substituting different functional forms for the PDF shapes. For the charged modes, the largest contribution is due to the signal parametrization of $m_{\mathrm{ES}}$ and $\Delta E\left(3 \%\right.$ for $K_{S}^{0} \pi^{+}$, $4 \%$ for $K_{S}^{0} K^{+}$), while for the neutral mode it is due to the potential fit bias ( $8.6 \%$ ) determined from the pseudoexperiments. We use the larger of the value or uncertainty on the background asymmetries to set the systematic uncertainty on $\mathcal{A}_{C P}$ due to potential charge bias [17]. We measure background asymmetries $\mathcal{A}_{C P}\left(K_{S}^{0} \pi^{+}\right)=-0.010 \pm 0.008$


FIG. 1 (color online). Distributions of (left) $m_{\mathrm{ES}}$ and (right) $\Delta E$ for signal (main plot) and background (inset) (a),(b) $K_{S}^{0} \pi^{+}$, (c),(d) $K_{S}^{0} K^{+}$, and (e),(f) $K_{S}^{0} K_{S}^{0}$ candidates (points with error bars) in data obtained with the weighting technique described in the text. The solid curves represent the assumed shapes used in the fits.


FIG. 2 (color online). Left: Distributions of $\Delta t$ for $B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$ decays in data tagged as $B^{0}$ (top) or $\bar{B}^{0}$ (middle) and the asymmetry (bottom). The data are enhanced in signal decays using requirements on probability ratios. The solid curve represents the PDF projection for the sum of signal and background, while the dotted curve shows the contribution from background only. Right: Likelihood contours in the $S$ vs $C$ plane, where $n \sigma$ corresponds to a change in $-2 \log \mathcal{L}$ of 2.3 for $n=1,6.2$ for $n=2$, and 11.8 for $n=3$. The circle indicates the physically allowed region, while the point with error bars denotes the result of the fit to the data.
and $\mathcal{A}_{C P}\left(K_{S}^{0} K^{+}\right)=-0.005 \pm 0.009$, which are consistent with no bias and lead to a systematic uncertainty of 0.010 . The dominant sources of systematic uncertainty on $S$ and $C$ are due to the positions of the means in $m_{\mathrm{ES}}$ and $\Delta E$. The statistical uncertainties of the measured values of the $C P$ parameters are in good agreement with the expected error values $(0.8 \pm 0.3$ for $S$ and $0.6 \pm 0.2$ for $C)$, while Monte Carlo studies confirm that the fit technique is unbiased for large values of the $C P$ parameters.

In summary, we have observed the decays $B^{+} \rightarrow \bar{K}^{0} K^{+}$ and $B^{0} \rightarrow K^{0} \bar{K}^{0}$ with significances of $5.3 \sigma$ and $7.3 \sigma$, respectively. The observed branching fractions are consistent with recent theoretical estimates [5,20]. The measured values of the time-dependent $C P$-violating asymmetry parameters in the $B^{0} \rightarrow K_{S}^{0} K_{S}^{0}$ mode reported here indicate that large positive values of $S$ are disfavored, although more data will be needed to confirm this result. We have also improved our measurements of the branching fraction and $C P$-violating charge asymmetry in $B^{+} \rightarrow K_{S}^{0} \pi^{+}$; both are consistent with previous measurements by other experiments [21].

We are grateful for the excellent luminosity and machine conditions provided by our PEP-II colleagues and for the substantial dedicated effort from the computing organizations that support $B A B A R$. The collaborating institutions wish to thank SLAC for its support and kind hospitality. This work is supported by DOE and NSF (USA), NSERC (Canada), IHEP (China), CEA and CNRS-IN2P3 (France),

BMBF and DFG (Germany), INFN (Italy), FOM (The Netherlands), NFR (Norway), MIST (Russia), and PPARC (United Kingdom). Individuals have received support from CONACyT (Mexico), A.P. Sloan Foundation, Research Corporation, and Alexander von Humboldt Foundation.
*Also Università di Perugia, Dipartimento di Fisica, Perugia, Italy.
${ }^{\dagger}$ Also Università della Basilicata, Potenza, Italy.
[1] D. London and R.D. Peccei, Phys. Lett. B 223, 257 (1989); H. R. Quinn, Nucl. Phys. B, Proc. Suppl. 37A, 21 (1994).
[2] B. Aubert et al. (BABAR Collaboration), Phys. Rev. D 71, 091102 (2005); K. Abe et al. (Belle Collaboration), Phys. Rev. Lett. 91, 261602 (2003).
[3] R. Fleischer, Phys. Lett. B 341, 205 (1994).
[4] A. K. Giri and R. Mohanta, J. High Energy Phys. 11 (2004) 084.
[5] R. Fleischer and S. Recksiegel, Eur. Phys. J. C 38, 251 (2004).
[6] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 95, 221801 (2005).
[7] For a review, see D. Kirkby and Y. Nir in Ref. [11].
[8] B. Aubert et al. (BABAR Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 479, 1 (2002).
[9] G. Hanson et al., Phys. Rev. Lett. 35, 1609 (1975).
[10] B. Aubert et al. (BABAR Collaboration), Phys. Rev. D 69, 071101 (2004).
[11] S. Eidelman et al. (Particle Data Group), Phys. Lett. B 592, 1 (2004).
[12] The decay $B^{0} \rightarrow K^{0} \bar{K}^{0}$ proceeds in an $S$ wave, which produces equal fractions of $K_{S}^{0} K_{S}^{0}$ and $K_{L}^{0} K_{L}^{0}$, but no $K_{S}^{0} K_{L}^{0}$, neglecting $C P$ violation in the kaon system.
[13] The BABAR detector simulation is based on GEANT4, S. Agostini et al., Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
[14] B. Aubert et al. (BABAR Collaboration), Phys. Rev. D 66, 032003 (2002).
[15] B. Aubert et al. (BABAR Collaboration), Phys. Rev. D 71, 111102 (2005).
[16] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 89, 281802 (2002).
[17] B. Aubert et al. (BABAR Collaboration), Phys. Rev. Lett. 93, 131801 (2004).
[18] Y. Chao et al. (Belle Collaboration), Phys. Rev. Lett. 95, 231802 (2005).
[19] M. Pivk and F. R. Le Diberder, Nucl. Instrum. Methods Phys. Res., Sect. A 555, 356 (2005).
[20] M. Beneke and M. Neubert, Nucl. Phys. B675, 333 (2003); Y.-Y. Keum, Pramana 63, 1151 (2004); R. Fleischer and S. Recksiegel, Phys. Rev. D 71, 051501 (2005).
[21] Y. Chao et al. (Belle Collaboration), Phys. Rev. D 71, 031502 (2005); S. Chen et al. (CLEO Collaboration), Phys. Rev. Lett. 85, 525 (2000).

