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ON A MORE ACCURATE MULTIDIMENSIONAL HILBERT–TYPE INEQUALITY WITH PARAMETERS

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Abstract. In this paper, by using the way of weight coefficients and technique of real analysis and complex analysis, a more accurate multidimensional discrete Hilbert-type inequality with a best possible constant factor and some parameters is given. The equivalent form, the operator expression with the norm are also considered.

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