

On Measuring Process Model Similarity based on High-level Change Operations

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Abstract. For various applications there is the need to compare the similarity between two process models. For example, given the as-is and to-be models of a particular business process, we would like to know how much they differ from each other and how we can efficiently transform the as-is to the to-be model; or given a running process instance and its original process schema, we might be interested in the deviations between them (e.g. due to ad-hoc changes at instance level). Respective considerations can be useful, for example, to minimize the efforts for propagating the schema changes to other process instances as well. All these scenarios require a method to measure the similarity or distance between two process models based on the efforts for transformation. In this paper, we provide an approach using digital logic to evaluate the distance and similarity between two process models based on high-level change operations (e.g. to add, delete or move activities). In this way, we can not only guarantee that the transformation results in a sound process model, but also ensure that the efforts are minimized.

1 Introduction

Business world is getting increasingly dynamic, requiring from companies to continuously adapt their *Process-Aware Information Systems* (PAIS) [6] in order to cope with the frequent and unprecedented changes in their business environment [23, 25]. Organizations and enterprises need to continuously Re-engineer their Business Processes (BPR), i.e. they need to be able to flexibly upgrade and optimize their business processes in order to stay competitive in their market. Furthermore, PAIS should allow for process flexibility, i.e., they should allow users to deviate from the standard process model at the instance level if required. Finally, organizational learning should be supported by analyzing these process instance deviations. The latter provides useful information about the past which can be utilized by a company to evolve and optimize its business processes and supporting PAIS [17].

The pivotal research on process flexibility over the last years [3–5] has provided the foundation for dynamic process change to reduce the cost of change

in PAIS. In this context, business process flexibility denotes the capability to reflect externally triggered change by modifying only those aspects of a process that need to be changed, while keeping the other parts stable, i.e., the ability to change or evolve the process without completely replacing it [4]. When comparing two process models, we would like to be able to calculate their minimal difference based on high level changes so that if we need to transform one model to another, efforts can be reduced and the transformation can go smoothly (i.e. we do not need to re-implement the new process model from scratch, but only apply these high level changes either at process type or process instance level).

Several approaches like ADEPT [5], WASA [10] or TRAM [9], have emerged to enable full lifecycle support in PAIS (for an overview see [7]). All these systems support ad-hoc deviations at the instance level and record them in *change logs*. Thus, they provide additional information when compared to traditional PAISs which only record *execution logs*.

1.1 Problem Statement

Based on the two assumptions that: (1) process models are block-structured and (2) all activities in a process model have unique labels, this paper deals with the following research question:

Given two process models S and S' , how much do they differ from each other in terms of high-level change operations? And what is the minimal effort, i.e. the minimal number of change operations needed to transform S into S' ?

Clearly, our focus is on minimizing the number of changes necessary to transform process model S into process model S' . However, soundness of the resulting process model should be also not sacrificed. When modifying a process model, we apply the high-level change operations as introduced by the ADEPT method [5] to guarantee soundness. By considering high-level change operations, we can distinguish ourselves from traditional similarity measures like graph isomorphism [2] or sub-graph isomorphism [24], which only consider basic change primitives like the insertion or deletion of single nodes and edges. At process type level, answering this question will lead to better cost efficiency when performing BPR, since the efforts to implement the corresponding changes in the supporting PAIS is minimized. At process instance level, answering this question can reduce the efforts to propagate the process type changes to the running instances [7, 18]; or when there are thousands of instances, the derived differences between the original process model and each process instance can be used as a set of pure and concise logs for process mining [17].

1.2 Contribution

Previous work on ADEPT [5] has provided the technical foundation for users to flexibly change process models at both the process type and the process instance level. For example, users may dynamically *insert*, *delete* or *move* an activity [5] at these two levels. In addition, snapshot differential algorithms [1], known from database technology, can be used as a fast and secure method to detect the

change primitives (e.g. concerning differences of the activities or control flow edges) needed to transform one process model into another.

Based on the ADEPT framework and snapshot differential algorithm, this paper applies Digital Logic in Boolean Algebra [20] to provide a new method to transform a process model to another based on high-level change operations. This method does not only minimize the number of changes needed in this context, but also guarantees soundness of the changed process model, i.e. the process model remains correct when applying a high-level change operation. Our paper also provides the two measures of *process distance* and *process similarity* based on high-level change operations. Such measures can be used to determine how difficult it is to transform a process model into another, and how different two process models are.

The remainder of this paper is organized as follows: Section 2 introduces backgrounds needed for the understanding of this paper. In Section 3, we discuss reasons and difficulties for deriving high-level change operations. Section 4 describes an approach to detect the changes between two block-structured process models, and Section 5 discuss related work. The paper concludes with a summary and outlook in Section 6.

2 Backgrounds

A *process model* $S = (N, E, \dots) \in \mathcal{P}$ is defined as a Well-Structured Marking (WSM) Net [5]. \mathcal{P} stands for all the possible process models. N constitutes a set of activities a_i associated to S and E is a set of control edges linking all these activities. To limit the scope, we assume process models to be block structured. A detailed description and correctness issues of WSM Nets are out of the scope of this paper, (see [22]).

We assume that a process change is accomplished by applying a sequence of change operations to a given process model S over time [5]. Such change operations modify the initial process model by altering the set of activities and/or by changing their order relations. Thus, each application of a change operation to a process model results in another process model. In this context, we define *high-level change operations* on a process model as follows:

Definition 1 (Change in Process Model). *Let \mathcal{P} be the set of possible process models and \mathcal{C} the set of possible process changes. Let $S, S' \in \mathcal{P}$ be two process models, let $\Delta \in \mathcal{C}$ be a process change, and let $\sigma = \langle \Delta_1, \Delta_2, \dots, \Delta_n \rangle \in \mathcal{C}^*$ be a sequence of process changes performed on initial process model S . Then we can define:*

- $S[\Delta]S'$ iff Δ is applicable to S and S' is the process schema resulting from the application of Δ to S .
- $S[\sigma]S'$ iff $\exists S_1, S_2, \dots, S_{n+1} \in \mathcal{P}$ with $S = S_1$, $S' = S_{n+1}$, and $S_i[\Delta]S_{i+1}$ with $i = \{1, \dots, n\}$.

Examples of high-level change operations and their effects on a process model are depicted in Table 1. Issues concerning the correct use of these operations and

Table 1. Examples of High-Level Change Operations on Process Schemas

Change Operation Δ Applied to S	opType	subject	paramList
insert(S, X, \mathcal{A} , \mathcal{B} , [sc])	insert	X	S, \mathcal{A} , \mathcal{B} , [sc]
Effects on S: inserts activity X between activity sets \mathcal{A} and \mathcal{B} . It is a conditional insert if [sc] is specified (i.e. [sc] = XOR)			
delete(S, X, [sc])	delete	X	S, [sc]
Effects on S: deletes activity X from S, i.e. X turns into a silent activity. [sc] is specified ([sc] = XOR) when we block the branch with X, i.e. the branch which contains X will not be activated			
move(S, X, \mathcal{A} , \mathcal{B} , [sc])	move	X	S, \mathcal{A} , \mathcal{B} , [sc]
Effects on S: moves activity X from its original position to another position between activity sets \mathcal{A} and \mathcal{B} . (it is a conditional insert if [sc] is specified)			
replace(S, X, Y)	replace	X	Y
Effects on S: replaces activity X by activity Y			

related pre/post conditions are described in [5]. If some additional constraints are met, the high-level change operations depicted in Table 1 are also applicable at the process instance level (e.g. to deal with exceptional situations [18]). Although the depicted change operations are discussed in relation to the ADEPT meta model (see [5] for details), they are generic in the sense that they can be easily transferred to other meta models as well, (e.g. Petri Nets) [18]. We are referring to ADEPT in this paper since it covers by far most high-level change operations and change patterns respectively when compared to other approaches [25].

In our context, a trace t on process model S denotes a valid execution sequence $t \equiv \langle a_1, a_2, \dots, a_k \rangle$ of activities $a_i \in N$ on S according to the control flow defined by S . All the traces process model S can produce are summarized in set \mathcal{T}_S . Finally, $t(a \prec b)$ is denoted as precedence relationship between activities a and b in trace $t \equiv \langle a_1, a_2, \dots, a_k \rangle$ iff $\exists i < j : a_i = a \wedge a_j = b$. Here, we only consider traces composing 'real' activities, but no events related to silent activities (i.e. activity nodes which contain no operation and exist only for control flow purpose). The reason of why not considering silent activities is given later (c.f. Section 4.4). At this stage, we consider two process models as being the same if they are *trace equivalent*, i.e. $S \equiv S'$ iff $\mathcal{T}_S \equiv \mathcal{T}_{S'}$. The stronger notion of bi-similarity [26] is not considered at this stage.

3 high-level change operations

3.1 Complementary Nature of Change and Execution Logs

Change logs and execution logs document different run time information on process instances and are not interchangeable. Even when the original process model is given, it is not possible to convert the change log of a process instance to its execution log or vice-versa. As an example, take the original model of a patient treatment process as depicted in Figure 1a): a patient is **admitted** to a

hospital, where he first **registers**, then **receives treatment**, and finally **pays**. Assume that, due to an occurring emergency situation, for one particular patient, we want to first start the treatment of this patient and allow him to register during treatment. To represent this exceptional situation in the process model of the respective instance, the needed change would be to move activity **receive treatment** from its current position to a position parallel to activity **register**. This leads to a new model S' ($S[\sigma]S'$) and the corresponding change log is $\sigma = \langle \text{move}(S, \text{receive treatment}, \text{admitted}, \text{pay}) \rangle$. Meanwhile, the execution log for this particular instance is then $\{\text{admitted}, \text{receive treatment}, \text{register}, \text{pay}\}$ (as numbers indicate in the Figure 1b). If we only have process model S and its execution log, it is not possible to determine this change because the process model which can produce such execution log is not unique (for example, a process model with the four activities contained in four parallel branches could produce this execution log as well). On the contrary, it is generally not possible to derive the execution log from a change log, because the execution behavior of S' is also not unique (for example, a trace $\langle \text{admitted}, \text{register}, \text{receive treatment}, \text{pay} \rangle$ is also producible on S'). Consequently, change logs provide additional information compared to pure execution logs.

3.2 Why High-level Change Operations?

After showing the importance of changes, in this section we discuss why we need high level change operations rather than change primitives (i.e. low-level changes at edge and node level). Left side of Figure 2 shows original process model S which consists of a parallel branching, a conditional branching and a silent activity τ (depicted as empty node) connecting these two blocks. Assume that two high-level change operations are applied to S resulting in two models S_1, S_2 : Δ_1 moves activity C from its current location to the position between activities A and B, which leads to S_1 (i.e. $S[\Delta_1]S_1$ with $\Delta_1 = \text{move}(S, C, A, B)$); Δ_2 moves activity A to the position between activities B and C, i.e. $S[\Delta_2]S_2$ with $\Delta_2 = \text{move}(S, A, B, C)$. Figure 2 additionally depicts the change primitives, representing snapshot differences between the model S and the models S_1 and S_2 , respectively.

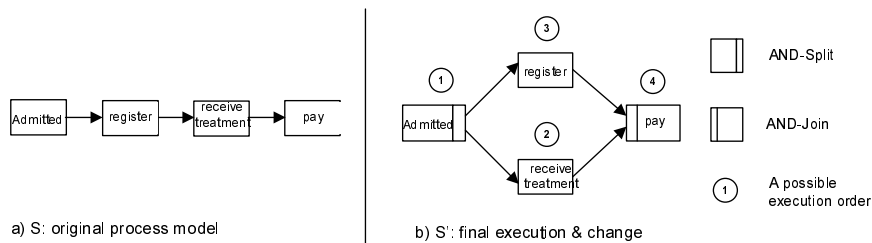


Fig. 1. change log and execution log is not interchangeable

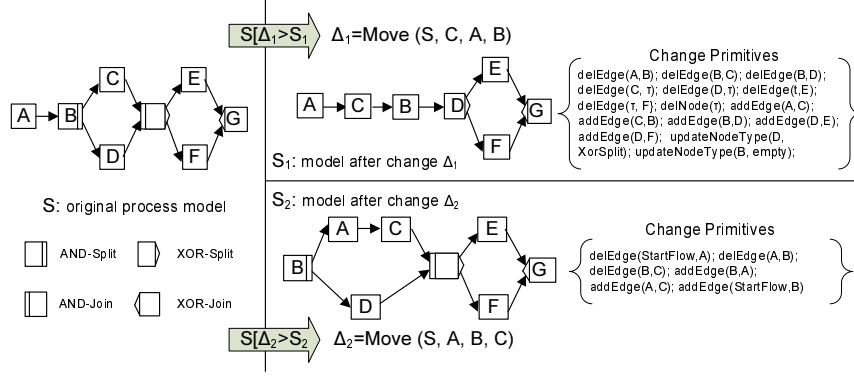


Fig. 2. high-level change operation compared with change primitive

When compared to change primitives, using high-level change operations like 'move' or 'insert' offers the following advantages:

1. High-level change operations, as supported by ADEPT, guarantee soundness: i.e., the application of a high-level change operation on a sound model S results in another sound model S' [5]. This also applies to our example from Figure 2. By contrast, when applying one single change primitive (e.g. deleting an edge in S), soundness cannot be guaranteed anymore. Generally, if we delete any of the edges in S , the resulting process model will not be necessarily sound.
2. High-level change operations provide richer syntactical meanings than change primitives. Generally, a high-level change operation is built upon a set of change primitives which collectively represent a semantic modification of a process model. As example, take Δ_1 from Figure 2. This high-level change operation requires 15 change primitives for its realization (deleting edges, adding edges, deleting the silent activity, and updating the node types).
3. An important aspect, not discussed so far, concerns the number of change operations needed to transform a process model S into a target model S' . For example, we need only *one* move operation to transform S to either S_1 or S_2 . However, when using change primitives, migrating S to S_1 necessitates 15 changes, while the second change Δ_2 can be realized based on 6 change primitives. This simple example shows that change primitives do not provide an adequate means to determine the difference between two process models. Thus the number of the change primitives cannot represent the efforts for process model transformations.

3.3 The Challenge to Derive High-level Change Operations

After sketching the benefits coming with high-level change operations, this section discusses challenges of Deriving them. When comparing two process models,

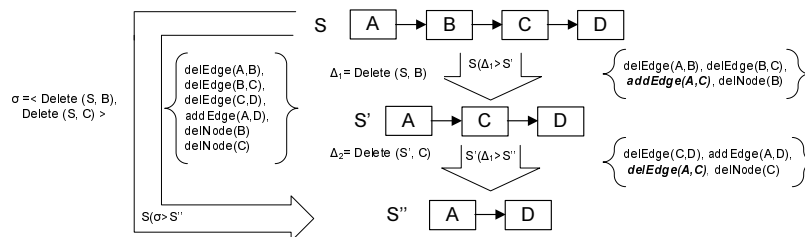


Fig. 3. undetectable change primitives

the change primitives needed for transforming one model into another can be easily determined by performing two snapshots and a delta analysis on them [1]. An algorithm to minimize the number change primitives has been given in [11]. However, when trying to derive the high-level change operations needed for model transformation, several challenges occur. Consider Figure 3 as example:

1. When performing two delete operations on S , i.e. $\Delta_1 = delete(S, B)$ and $\Delta_2 = delete(S, C)$, we obtain a new model S'' with $S[\sigma]S''$ with $\sigma = \langle \Delta_1, \Delta_2 \rangle$, as well as an undetectable intermediate model S' with $S[\Delta_1]S'$ and $S'[\Delta_2]S''$. When examining the change primitives corresponding to each high-level change operation, we need to first add edge (A, C) after the first *delete* operation Δ_1 , and remove this edge (A, C) when applying the second *delete* operation Δ_2 . However, when performing a delta analysis for the original process model S and the resulting process model S'' , the two change primitives (addEdge(A,C) introduced by the first *delete* operation and delEdge(A,C) introduced by the second *delete* operation) jointly have no effect on the resulting process model S'' so that they cannot be detected by snapshot analysis. Consequently, deriving high-level change operations from change primitive would be challenging because the change primitives required for every high-level change will not always appear in the snapshot differences between the original and resulting models (like in Figure 3, none of the two sets of change primitives associated to Δ_1 or Δ_2 are a sub-set of the set of change primitives associated with σ).
2. Even when there is just one high-level change operation, it remains difficult to derive it with a delta algorithm. For example, in Figure 3, the delta algorithm shows that when transforming S to S_1 , 15 change primitives need to be applied to the original model S . However, the depicted change can be also realized by just applying one high level move operation to S .

4 Detecting The Minimal Number Of High-level Change Operations

In this section, we introduce our method to detect the minimal number of change operations needed to transform a given process model S into another model S' . As example, consider the process models S and S' in Figure 4.

4.1 General Description of our Method

As mentioned in Section 1, the key issue of this work is to minimize the number of change operations needed to transform a process model S to another model S' . In this context, let N and N' be the two sets of activities based on which S and S' are defined. Generally, three steps are needed (cf. Figure 4) to realize this minimal transformation:

1. $\forall a_i \in N \setminus N'$: *delete* all activities being present in S , but not in S' . As depicted in our example from Figure 4, this first step transforms S to S_{same} (cf. Figure 4b).
2. $\forall a_i \in N \cap N'$: *move* all activities being present in both models to the locations as reflected by S' . As depicted in our example from Figure 4, this second step transforms S_{same} to S'_{same} (cf. Figure 4c).
3. $\forall a_i \in N' \setminus N$: *insert* those activities being present in S' , but not S . As depicted in Figure 4, the third step transforms S'_{same} to S' (cf. Figure 4d).

Insertions and deletions deal with changes of the set of activities and we can hardly do anything here to reduce efforts (i.e. the number of required high-level insert/delete operations): New activities ($a_i \in N' \setminus N$) must be added and obsolete activities ($a_j \in N \setminus N'$) must be deleted. The focus of minimality can therefore be shifted to the use of the *move* operation, which changes the structure of a process model, but not its set of activities. Since a move operation logically corresponds to a delete followed by an insert operation, we can transform S_{same} to S'_{same} by maximal $n = |N \cap N'|$ move operations. Reason is that n move operations correspond to deleting all activities and then inserting them back to their new positions. So n would be the maximal number of change operations needed to transform one process model into another, with the same set of activities (S_{same} and S'_{same} in our example from Figure 4). However, this would be not in line with our goal of minimality. To measure the complete transformation from S to S' , we formally define *process distance* and *process similarity* as follow:

Definition 2 (Process distance & process similarity.)

Let $S, S' \in \mathcal{P}$ be two process models. Let N and N' be two sets of activities based on which S and S' are defined. Let further $\sigma = \langle \Delta_1, \Delta_2, \dots, \Delta_n \rangle \in \mathcal{C}^*$ be a sequence of change operations transforming S into S' (i.e. $S[\sigma]S'$). Then the distance between S and S' is given by $d_{(S,S')} = \min\{|\sigma| \mid \sigma \in \mathcal{C}^* \wedge S[\sigma]S'\}$. Furthermore, the process similarity between S and S' then equals to $1 - \frac{d_{(S,S')}}{|N|+|N'|-|N \cap N'|}$. i.e. the similarity equals ((maximal number of changes - minimal number of changes) / maximal number of changes).

4.2 Determining Required Activity Deletions and Insertions

To accomplish Step 1 and Step 3 of our method, we have to deal with the change of the activity set when transforming S to S' . It can be easily detected by applying existing snapshot algorithms [1] to both S and S' . As described in Section 4.1, as first step we need to *delete* all activities $a_i \in N \setminus N'$ contained in S , but not in S' . Regarding our example from Figure 4, we therefore can derive as our first high-level change operation $\Delta_1 = delete(S, X)$. Similarly, activities contained in S' , but not in S , are to be inserted in Step 3 of our method, after we moved the shared activities to their respective position in S' (S'_{same} respectively). The parameters of the insert operation, i.e. the predecessors and successors of the inserted activity, are just like how they appear in S' . In this way, we obtain the last two change operations for our example: $Insert(S, Y, StartFlow, \{A, B\})$ and $Insert(S, Z, D, E)$.

4.3 Determining Required Move Operations to Deal With Structure Changes

In this section, we focus on Step 2 of our method, i.e. to transform two process models with same activity set using move operations. Here, we can ignore the activities not contained in both S and S' (they have already been handled in Section 4.2). We therefore consider the two process models S_{same} and S'_{same} respectively, as depicted in Figure 4.

Determine the Order Matrix of a Process Model One key feature of the ADEPT change framework is to maintain the structure of the unchanged parts of a process model [5]. For example, if we delete an activity, this will neither influence the successors nor the predecessors of this activity, and also not their control relationships. To incorporate this feature in our approach, rather than

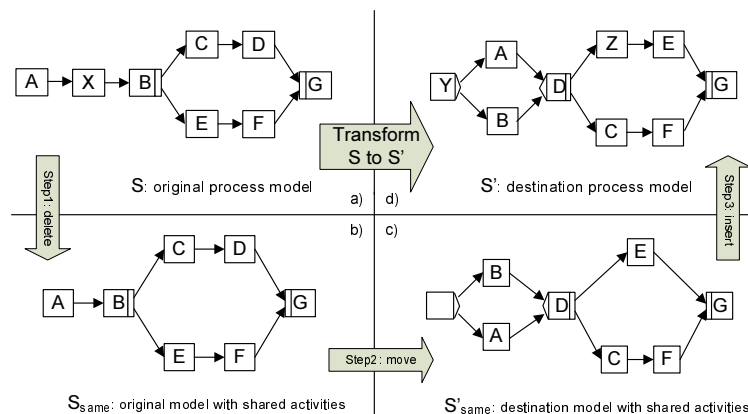


Fig. 4. Three steps to transform S into S'

only looking at direct predecessor successor relationships between two activities (i.e. control flow edges), we consider the transitive control dependencies between all pairs of activities; i.e. for every pair of activities $a_i, a_j \in N \cap N'$, $a_i \neq a_j$, their execution order compared to each other is examined. Logically, we check the execution orders by considering all traces a process model can produce. The results can be formally described in a matrix $A_{n \times n}$ with $n = |N \cap N'|$. Four types of control relations can be identified (cf. Def. 3):

Definition 3 (Order Matrix). *Let $S \in \mathcal{P}$ be a process model with $N = \{a_1, a_2, \dots, a_n\}$. Let further \mathcal{T}_S denote the set of all traces producible on S . Then, matrix $A_{n \times n}$ is called order matrix of S with A_{ij} representing the relation between different activities $a_i, a_j \in N$ iff:*

- $A_{ij} = '1'$ iff $(\forall t \in \mathcal{T}_S \text{ with } a_i, a_j \in t \Rightarrow t(a_i \prec a_j))$
If for all traces containing activities a_i and a_j , activity a_i always appears BEFORE a_j , we will denote A_{ij} as '1', i.e., a_i is a predecessor of a_j in the flow of control.
- $A_{ij} = '0'$ iff $(\forall t \in \mathcal{T}_S \text{ with } a_i, a_j \in t \Rightarrow t(a_j \prec a_i))$
If for all traces containing activity a_i and activity a_j , activity a_i always appears AFTER a_j , then we will denote A_{ij} as a '0', i.e. a_i is a successor of a_j in the flow of control.
- $A_{ij} = '*'$ iff $(\exists t_1 \in \mathcal{T}_S, \text{ with } a_i, a_j \in t_1 \wedge t_1(a_i \prec a_j)) \wedge (\exists t_2 \in \mathcal{T}, \text{ with } a_i, a_j \in t_2 \wedge t_2(a_j \prec a_i))$
If there exists at least one trace in which a_i appears before a_j and at least one other trace in which a_i appears after a_j , we will denote matrix element A_{ij} as '*', i.e. a_i and a_j are contained in different parallel branches.
- $A_{ij} = '-'$ iff $(\neg \exists t \in \mathcal{T}_S : a_i \in t \wedge a_j \in t)$
If there exists no trace containing both activity a_i and a_j , we will denote A_{ij} as '-', i.e. a_i and a_j are contained in different branches of a conditional branching.

We re-visit our example from Figure 4. The order matrices of S_{same} and S'_{same} are shown in Figure 5. The main diagonal is empty since we do not compare an activity with itself. As one can see, elements A_{ij} and A_{ji} can be derived from each other. If activity a_i is a predecessor of activity a_j , (i.e. $A_{ij} = 1$), we can always conclude that $A_{ji} = 0$ holds. Similarly, if $A_{ij} \in \{ '*', '-' \}$, then we will obtain $A_{ji} = A_{ij}$. As a consequence, we can simplify our problem by only considering the upper triangular matrix $A = (A_{ij})_{j > i}$.

Under certain constraints, an order matrix A can uniquely represent the process model, based on which it was built on. This is stated by Theorem 1. Before giving this theorem, we need to define *substring of trace*:

Definition 4 (Substring of trace).

Let t and t' be two traces. We define t a sub-string of t' iff $\forall a_i, a_j \in t, t(a_i \prec a_j) \Rightarrow a_i, a_j \in t' \wedge t'(a_i \prec a_j)$ and $\exists a_k \in N : a_k \notin t \wedge a_k \in t'$.

Theorem 1. *Let $S, S' \in \mathcal{P}$ be two process models, with same set of activities $N = \{a_1, a_2, \dots, a_n\}$. Let further $\mathcal{T}_S, \mathcal{T}_{S'}$ be the related trace sets and $A_{n \times n}$,*

$A'_{n \times n}$ be the order matrices of S and S' . Then $S \neq S' \Leftrightarrow A \neq A'$, if $(\neg \exists t_1, t'_1 \in \mathcal{T}_S: t_1 \text{ is a substring of } t'_1)$ and $(\neg \exists t_2, t'_2 \in \mathcal{T}_{S'}: t_2 \text{ is a substring of } t'_2)$.

According to Theorem 1, a process model S and order matrix A is a one-to-one mapping if the substring constraint is satisfied. A detailed discussion of the sub-string restriction is given further in Section 4.4. A proof of Theorem 1 can be found in [27]. Thus, when comparing two process models, it is sufficient to compare their order matrices (cf. Def. 3), since a order matrix can uniquely represent the process model. This also means that the *differences of two process models* can be related to the *differences of their order matrices*. If two activities have different execution order in two process models, we define the notion *conflict* as follows:

Definition 5 (Conflict). . Let $S, S' \in \mathcal{P}$ be two process models with same set of activities N . Let further A and A' be the order matrices for S and S' respectively. Then: Activities a_i and a_j are conflicting iff $A_{ij} \neq A'_{ij}$. We formally denote this as $C_{(a_i, a_j)}$. $\mathcal{CF} := \{C_{(a_i, a_j)} \mid A_{ij} \neq A'_{ij}\}$, then corresponds to the set of all existing conflicts.

Figure 5 marks up differences between our two order matrices in grey. The set of conflicts is as follows: $\mathcal{CF} = \{C_{(A, B)}, C_{(C, D)}, C_{(C, F)}, C_{(D, E)}, C_{(D, F)}, C_{(E, F)}\}$.

Optimizing the Conflicts To come from S_{same} to S'_{same} , we have to eliminate conflicts between them by applying *move* operations. Obviously, if there is no

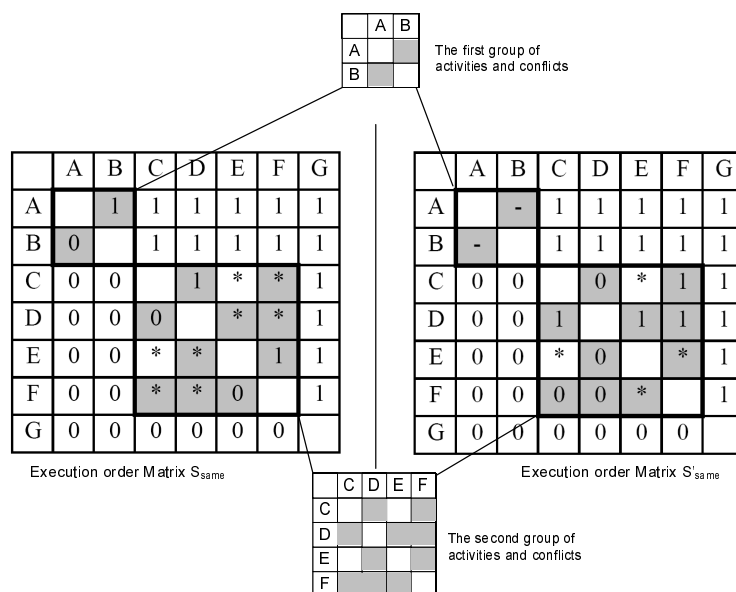


Fig. 5. the execution order matrices of S_{same} and S'_{same} in Figure 4

conflict for the two process models S_{same} and S'_{same} , they are identical. Every time we move an activity from its current position in S_{same} to the position it has in S'_{same} , we can eliminate the conflicts this activity has with other activities. For example, consider activity A in Figure 4. If we move activity A from its position in S_{same} (preceding B) to its new position in S'_{same} (A and B are contained in two different branches of a conditional branching block), then we can eliminate conflict $C_{(A,B)}$. Shown in the order matrices, moving activity A requires two steps. First, set the elements in the first row and first column of $A_{n \times n}$ (which corresponds to activity A) to empty, since A is moved away. Second, reset these elements according to the new order relation of A, when compared to the other activities from S'_{same} . So every time we move an activity, we are able to change the value of its corresponding row and column in the order matrices, i.e., we change these values corresponding to the original model to the values compliant with the target model. By doing this iteratively, we can change all the values and eliminate all the conflicts so that we could achieve the transformation from S_{same} to S'_{same} .

A none-optimal solution to transform the processes would be to move all the activities contained in the conflicts in \mathcal{CF} , from their positions in S_{same} to the positions they have in S'_{same} . Regarding our example from Figure 5, to apply this straightforward method, we would need to move activities A, B, C, D, E and F from their positions in S_{same} to the ones in S'_{same} . However, this naive method is not in line with our goal to minimize the number of applied change operations. For example, after moving activity A from its current position in S_{same} to the position it has in S'_{same} , we do not need to move activity B anymore, because after this change operation, there are no activities with which activity B still has conflicts.

Digital logic in Boolean algebra [20] helps to solve this minimization problem. Digital logic constitutes the basis for digital electronic circuit design and optimization. In this field, engineers face the challenge to optimize the internal circuit design given the required input and output signals. To apply such a technique in our context, we consider each process activity as an independent input signal and we want to design a circuit which can cover all conflicts defined by \mathcal{CF} (cf. Def 5). If activity a_i conflicts to activity a_j , we can either move one of them or both of them from the positions they have in S_{same} to the ones they have in S'_{same} . Doing so, the conflict will not exist any more. Reason is that every time we move an activity from the position it has in S_{same} to the position it has in S'_{same} , we reset the corresponding row and column of this activity in the order matrix. A conflict can be interpreted as a digital signal as follows: when the two input signals a_i and a_j are both "true" (this means we do not move activity a_i and a_j), we cannot solve the conflict and the 'circuit' shall give an output signal of "false", (i.e. $a_i a_j = 0$). If we apply this to all conflicts in \mathcal{CF} , we will obtain all the "false" signals. Meanwhile, the "circuit" should be able to tell us what will result in a "true" output, (i.e. the negative of all "false" signals). This "true" output represents which activities we need to move. Regarding our

example from Figure 5, given the set of conflicts \mathcal{CF} , our logic expression then is: $\overline{AB} + \overline{CD} + \overline{CF} + \overline{DE} + \overline{DF} + \overline{EF}$.

The complexity for optimizing the logic expression is NP-Hard [20]. Therefore it is advantageous to reduce the size of the problem. Concerning our example, we can cut down the optimization problem into two groups: one with activities A and B, and conflict $C_{(A,B)}$; another one with activities C, D, E and F and conflicts $\{C_{(C,D)}, C_{(C,F)}, C_{(D,E)}, C_{(D,F)}, C_{(E,F)}\}$.

Such a division can be achieved in $O(n)$ time in the following three steps. Step 1: List all the conflicting activities, and set every activity as a group. Step 2: If conflicting activities a_i and a_j (i.e. $C_{(a_i,a_j)}$) are contained in two different groups, merge these two groups. Step 3: Repeat Step 2 for all conflicts in \mathcal{CF} . After these three steps, we can divide the activities as well as the associated conflicts into several groups. Regarding our example, the optimization problem can be divided into two sub-optimization problems: \overline{AB} and $\overline{CD} + \overline{CF} + \overline{DE} + \overline{DF} + \overline{EF}$. We depict this in the two small matrices in Figure 5.

Optimizing logic expression has been discussed intensively in Discrete Mathematics. Therefore we omit details here and refer to Karnaugh map [20] and Quine-McCluskey algorithm [20]. We have implemented the latter in our proof-of-concept prototype. Regarding our example in Figure 4, the two optimization results are: $\overline{AB} = \overline{A} + \overline{B}$ for the first group, and $\overline{CD} + \overline{CF} + \overline{DE} + \overline{DF} + \overline{EF} = \overline{D}\overline{F} + \overline{C}\overline{E}\overline{F} + \overline{C}\overline{D}\overline{E}$ for the second group. We can interpret this result as follows. For the second group, either we move activities D and F, or we move activities C, E and F, or we move activities C, D and E from their position in S_{same} to the positions they have in S'_{same} . Based on this, we can transform S_{same} to S'_{same} , since all conflicts are eliminated. As can be seen from the order matrices, if we change the value of the corresponding rows and columns of these activities in S_{same} , we can turn S_{same} into S'_{same} . As we want to minimize the number of change operations, we can draw the conclusion that activities D and F must be moved. Same rule applies to the result of the first group. However, there is no difference to move either A or B, since both operations count as one change operation. Here, we arbitrarily decide to move activity B.

So far we have determined the set of activities to be moved. The next step is to determine the positions where the activities need to be moved to. Operation $move(S, X, \mathcal{A}, \mathcal{B}, [sc])$ will be independent from other move operations (i.e. it does not matter in which order to move the respective activity) if its direct predecessors \mathcal{A} and direct successors \mathcal{B} do not belong to the set of activities to be moved. Regarding our example from Figure 4, activity F satisfies this condition since its predecessor C and successor G are not moved. If this had not been the case, we would have to introduce silent activities to put the moved activity to its corresponding place in S'_{same} . For example, if we want to first move B to its position in S'_{same} , we will have to introduce a silent activity after B and before C and E. Only in this way, we can change the execution order of B to what it appears in S'_{same} . However, such silent activity will be not required if we first move activity D to the position it has in S'_{same} . A detailed discussion

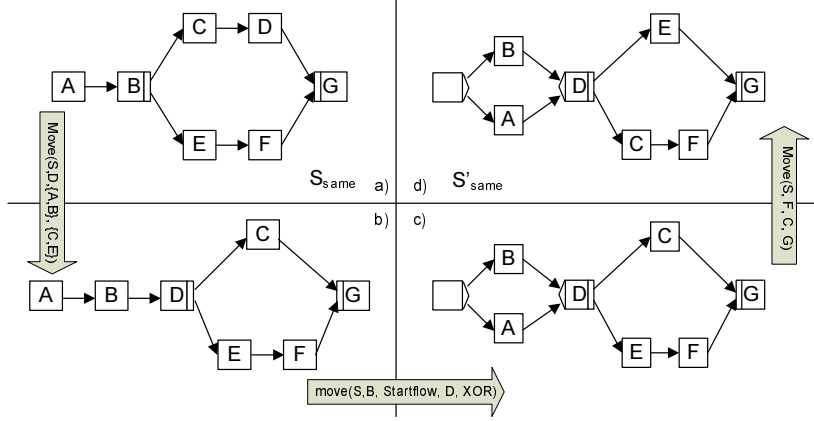


Fig. 6. Process models after every move operation

is out of the scope here; we refer readers to the reduction rules introduced with the ADEPT method [5].

According to the position the moved activities have in S'_{same} , we can determine the parameters (i.e. the predecessors, successors and conditions) for every move operation. In S'_{same} , activity D has predecessors A and B, and successors E and C. So one move operations therefore is: $move(S, D, \{B, A\}, \{C, E\})$. Similarly, we obtain the other two move operations: $move(S, B, StartFlow, D, XOR)$ and $move(S, F, C, G)$. The intermediate process models resulting after every move operation is shown in Figure 6. When comparing order matrices for each model in Figure 6, it becomes clear that every move operation changes the values of the row and the column corresponding to the moved activity.

4.4 Silent Activities

A silent activity is an activity which does not contain any operation or action, and which only exists for control flow purpose. There are two reasons why we do not consider silent activities in our similarity measure:

1. The appearance of a silent activity can be random. We can add or remove silent activities without changing the behavior of the process model. For example, we can replace a control flow edge in a process model by one silent activity or even a block of silent activities without influencing the behavior of the process model.
2. The existence of a silent activity also depends on other activities and is subject to change as other activities change. As example consider Figure 2. When applying change operation Δ_1 to S , the silent activity τ is automatically removed after activity C is moved away.

However, there is one exception for which we need to consider silent activities. Consider the two process models S_1 and S_2 as depicted in Figure 7. If we ignore

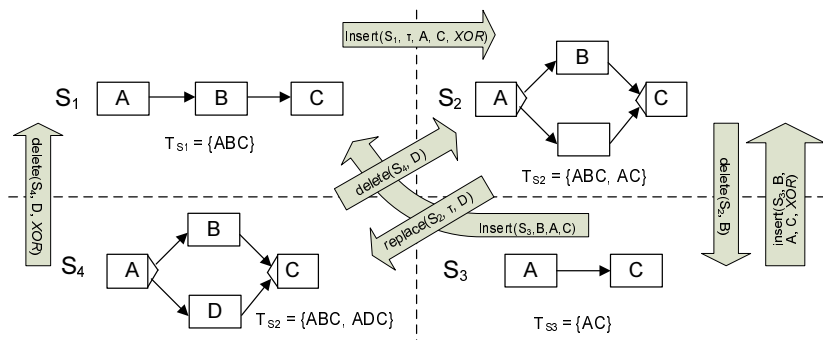


Fig. 7. The influence of silent activity

the silent activity τ (depicted as an empty node) in S_2 , and derive the order matrix of process model S_2 , it will be the same as the one of S_1 . Obviously, the two process model are not equivalent since the trace sets producible by them are not identical. More precisely, \mathcal{T}_{S_2} contains one additional trace when compared to \mathcal{T}_{S_1} . In general, if one process model can produce additional traces, which are the sub-string of other traces (cf. Def.4), there must be some silent activities we cannot ignore. Or if the direct predecessor and direct successor of one silent activity constitute XORsplit and XORjoin, we can also not ignore this silent activity (cf. S_2 in Figure 7).

Figure 7 shows several process model transformations based on high level change operations. Here we can identify the difference between the two types of deletion: $delete(S_4, D)$ and $delete(S_4, D, XOR)$ (cf. Figure 7). The former one turns an activity into a silent one (transforming S_4 into S_2), while the latter one blocks the branch which contains activity D (transforming S_4 to S_1). When a branch is blocked, we do not allow the activities of the branch to become activated [14, 5]. Since process models S_1 and S_2 have same order matrix, purely comparing order matrices (cf. Section 4) would not be sufficient in the given situation. Reason is that an order matrix does not uniquely represent a process model, since the sub-string constraint (cf. Def.4) in Theorem 1 is violated. To extend our method such that it can uniquely represent a process model without the sub-string constraint, we must consider these special silent activities (i.e. a silent activity which has direct predecessor of XORsplit and direct successor of XORjoin) as well. They will appear in the order matrix and their execution orders compared with other activities will be documented.

However, the existence of a silent activity is still very much dependent on other activities, including the scenario described above. For example, if we delete activity B in S_2 as depicted in Figure 7, we will transform S_2 into S_3 , i.e. the silent activity will be simultaneously deleted when activity B is deleted. We can identify this situation by either examining the process model or the order matrix. In the process model, a silent activity τ can be automatically deleted if there is another silent activity τ' which is contained in the same block but in another

		Figure 2			Figure 4			
		S	S ₁	S ₂	S	S _{same}	S' _{same}	S'
Figure 2	S	0 / 100%	1 / 86%	1 / 86%	4 / 50%	3 / 57%	3 / 57%	5 / 44%
	S ₁		0 / 100%	2 / 71 %	4 / 50%	3 / 57%	3 / 57%	5 / 44%
	S ₂			0 / 100%	5 / 38%	4 / 42%	3 / 57%	5 / 44%
Figure 4	S				0 / 100%	1 / 88%	4 / 50 %	6 / 40%
	S _{same}					0 / 100%	3 / 57%	5 / 44%
	S' _{same}						0 / 100%	2 / 78 %
	S'							0 / 100%

Fig. 8. The distances and similarities of different process models

conditional branch (e.g. transforming S_2 to S_3 Figure 7). In the order matrix, we can automatically remove a silent activity τ if there is another silent activity τ' which has the same order relations to the rest of the activities as τ has.

In general, when a silent activity has an XORsplit as direct predecessor and an XORjoin as direct successor, we need to consider this silent activity when computing the order matrix of a process model. However, these silent activities can automatically be deleted when changing the process model. This requires us to perform additional checks on the process model or order matrix (as described above) after every change operation.

4.5 Summary

Taking our example from Figure 4, to transform S into S' ($S[\sigma]S'$), the following *six* change operations are required: $\sigma = \{delete(S, X), move(S, F, C, G), move(S, D, \{A, B\}, \{C; E\}), move(S, B, StartFlow, D, XOR), insert(S, Y, StartFlow, \{A, B\}), insert(S, Z, D, E)\}$. The distance between the two process models is *six*, and the similarity is 0.4 (cf. Def.2).

To illustrate our method and these numbers in more detail, we compare the distances and similarities between seven process models discussed so far: S , S_1 and S_2 in Figure 2 as well as S , S_{same} , S'_{same} and S' in Figure 4. The distance and similarity of two process models are specified as *distance/similarity* in each corresponding cell in Figure 8. As the transformation is commutable, we only fill in the upper triangle matrix. Taking Figure 8, we can conclude the following:

1. Changing the activity set always leads to changing distance. For example, $d_{(S_n, S'_{same})}$ always equals $d_{(S_n, S')} + 2$, where S_n stands for a process model other than S' or S'_{same} in Figure 8. Reason is that S' contains two unique activities Y and Z when compared to S'_{same} , while the rest are identical.
2. If three process models S , S' , and S'' have the same set of activities, $d_{(S, S'')} \leq d_{(S, S')} + d_{(S', S'')}$ will hold. It is also easy to understand this because some activities could be moved twice when transforming S into S' and S' into S'' .

5 related work

Various papers have studied the process similarity problem and provided some useful results [12–14, 21]. In graph theory, graph isomorphism [2] and sub-graph isomorphism [24] are often used to measure the similarity between two graphs. Unfortunately, these measures usually only examine edges and nodes and cannot catch the syntactical issues of a PAIS. In the database field, the delta-algorithm [1] is used to measure the difference between the two models. It extends the above mentioned approaches by assigning attributes to edges and nodes [11]. Still, it can only catch change primitives, and will further run into problems when catching the high-level change operations (as described in Section 3). In the fields of Petri-nets and state automata, similarity based on change is difficult to measure since these formalisms are not very tolerant for changes. Inheritance rules [14] are one of the very few techniques given to show the transformation of a process model described as Petri-net. Trace equivalence is commonly used to compare whether two process models are similar or identical [26]. In addition, bisimulation [14, 15] extends trace equivalence by considering stronger notions. Also based on traces, [12] assign weights to each trace based on execution logs which reflect the importance of a certain trace. Respective techniques are applied, for example in genetic process mining [13]. The edit distance [21] is also used to measure the difference between traces; the sum of them represents the differences of two models. Some similarity measures use two figures (*precision* and *recall*) to evaluate the difference between process models S_1 to S_2 [12, 16]. However, this asymmetric way might lead confusion since it is therefore not commutable. None of these approaches measures the similarity by a unique and commutative figure, based on the effort for change.

6 Summary and Outlook

We have provided a method to quantitatively measure the distance and similarity between two process models based on the efforts for model transformation. High-level change operations are used to evaluate the similarity since they guarantee soundness and also provide more meaningful results. We further applied digital logic in boolean algebra so that the number of change operations required to transform process model S into process model S' is minimized.

Some additional work is needed to enrich our knowledge on process similarity. As a first step, we will extend our method so that it will be able to measure the similarity between process models using additional constituents (e.g., synchronization and loopback edges [5]). The next step will be to incorporate data flow, temporal constraints, and resources, so that the similarity measure can be further applied to practice.

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