Review Article DOI: 10.36959/673/366

On Model Checking of a Robotic Mechanism

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Abstract

Developing robot control systems can get complex even for small number of functions to be carried by the robot. Finite state machines are representing a frequent approach to model complex systems in a formal way. In this paper we are presenting a methodology for modelling the kinematics of a robotic mechanism represented by a sequence of bodies linked by joints. Each movement is decomposed as a sequence of rotations and translations and a finite state machine modelling the behavior of each of these is built. The general methodology is applied on a case study: A 2 joints manipulator. An Event-B model of each machine is implemented in the Rodin platform, then the models are validated and some LTL properties corresponding to the behavior of the robot are verified using ProB, the associated model checker.

Keywords

Model checking, Robotic mechanism, FSM, Rodin, ProB, 2 joints manipulator

AMS Subject Classification

68Q05; 68Q10; 68Q19; 68Q45; 68Q60

Introduction

In this section some general aspects regarding model checking, Rodin platform, finite states machines and the kinematics of a robotic mechanism with several joints are given.

Model checking, Rodin and ProB

Event-B is a rigorous mathematical modelling language used to implement discrete systems [1]. It was developed by J.R. Abrial as an improvement to the B language. Rodin [2], a platform dedicated to Event-B models is the result of two European Union Projects: RODIN (2004-2007) and DEPLOY (2008-2012) [3]. It is an Eclipse-based IDE that provides effective support for Event-B models including refinement and automatic proving. The platform was extended with plugins such as ProB [4], Camille or iUML-B State-machines.

One of the features of Rodin platform is the possibility to develop the model gradually. The modelling process can start with a simplified version of the system under analysis and more details can be added in a process called refinement. One of the main advantages it that the correctness of each step is proved in order to achieve a reliable system, as the tool assists the development process, by generating proof obligations.

Introduced by Clark and Emerson, model checking is an automatic verification technique of finite-state systems [5]. Since all the possible states of the system are explored in a brute-force manner, the main issue related to this technique

is the state explosion problem [6].

The B language is rooted in predicate logic, arithmetic and set theory and it provides support for data structures such as (higher-order) relations, functions and sequences. In addition to the B language, ProB also supports Event-B, CSP-M, TLA+, and Z. ProB is a model checker which accepts B-models and that was also integrated in the Rodin platform as a plugin. It is being used within Siemens, Alstom, Thales and several other companies for data validation of complicated properties for safety critical systems. Animation of Event-B models and verification of properties specified using the LTL or CTL formalisms can be enabled using Pro-B. The provided automated consistency checking can be used to detect various errors in B specifications (deadlocks, invariant violation, etc.). The animation facilities allow: To visualize the state space or to execute a given number of random events.

An Event-B model is a collection of machines and con-

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Accepted: August 10, 2020

Published online: August 12, 2020

Citation: Turcanu A, Shaikh T, Mazilu CN (2020) On Model Checking of a Robotic Mechanism. J Robotics Autom 4(1):158-

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texts. Contexts describe the static structure of the system: Sets, constants and axioms. Axioms represent properties of sets and constants. Machines contain the dynamic structure of the system: Variables, invariants, and events. Invariants state the properties of variables, and events defines the dynamic of the transition between the states of the system.

Event-B has been successfully applied in some vast areas of investigation from modelling formal ontologies in the engineering area where concepts have been integrated as theories into a specific formal method development process [7], to modelling biological systems such as a basic cell-like P system defined as a hierarchical arrangement of membranes [8], the kernel P system representation of E. coli [9], validating and verifying the requirements and design of a haemodialysis machine [10], up to specifying the dynamic semantics of some real-life industry applications like the formal modelling of a cruise control system [11], of a controller of a water pump for the goal of groundwater conservation [12], modeling a landing gear system of an aircraft [13], a speed control system available in some German cars [14], towards sophisticated air traffic control system using formal methods [15] and applying model transformation and Event-B for specifying an industrial DSL (Domain-Specific Languages) [16].

Moreover, because the development of safety-critical reactive systems is demanding and Event-B allows for a formal software development methodology in which software systems are initially designed in a abstract way and then refined in code, some papers report the work on generating codes for Event-B, applied to very relevant case studies: On the development of an Android application with EventB2Java, on testing an Event-B model of the To-keneer safety-critical system [17] and work towards a translation tool that automatically generates efficient target programming language code (C, C++, Java and C#) from Event-B formal specification related to the analysis of complex problems [18].

Finite state machines

According to [19]: A finite state machine (FSM) is a model of computation consisting of a set of states, a start state, an input alphabet, and a transition function that maps input symbols and current states to a next state.

Several types of finite state machines have been defined starting with the well-known Moore [20] and Mealy [21] machines, and more recently UML state machines [22] and hierarchical featured state machines [23].

Formally, a deterministic finite state machine is a quintuple $(\Sigma, S, s_{\alpha}, Act, F)$, where:

- Σ is the input alphabet (a finite, non-empty set of symbols).
- S is a finite, non-empty set of states
- $s_0 \in S$ is the initial state
- $Act: S \times \Sigma \rightarrow S$ is the state-transition function
- F is the set of final states, a (possibly empty) subset of S

Describing the transition between states, Act is a partial function, i.e. Act (s, x) does not have to be defined for every combination of $s \in S$ and $x \in \Sigma$. The word "deterministic" refers to the fact that from any state s, there is only one transition for any input x such that Act (s, x) is defined.

On the other hand, for a non-deterministic FSM a particular state and an input can lead to more than one state. Since in the next sections we are considering only deterministic FSMs, we will not go into furthermore details regarding the differences between the two types of FSMs.

Finite state machines have been studied intensively due to their simplicity and their computational power, which is equivalent to that of Turing machines.

The kinematics of a robot

One of the most fundamental aspects of robot design, control and simulation, kinematics refers to the motion of bodies in a robotic mechanism without regard to the forces/torques that cause the motion [24].

In general, robotic mechanisms are systems of rigid bodies connected by joints. Therefore, robot kinematics describes aspects like: Position and orientation of the bodies in space, velocity or acceleration. The most common topologies in which bodies can be connected are: Serial chains and fully parallel mechanisms. In a serial chain system, each member is connected to two others, except for the first and last ones that are each connected to only one other member. In a fully parallel mechanism there are two members that are connected together by multiple joints [24].

Related work

The majority of Robot control systems that are developed are Software Engineering based where most of them are following the MDE approach [25]. Finite state machines are good tool to model complex systems that can be formally verified by the different automata tools. The approach taken in developing a FSM model in a tool like Rodin with the Event B language is that it gives a user a methodical way to develop a complex system by using simple construction parts for forming a robust and maintainable system. This is done by breaking down a complex control problem into smaller units which in turn provides a good overview of the overall process. If there are any problems with the structuring or implementation logic it could be easier to diagnose the issue.

A robotic system comprises of at least one robot and the associated devices. Development of such system requires the specifications of the architectures in terms of the structure and the activities to be performed by the system. The structure refers to how the deferent subsystems are composed of and how each of these subsystems is interrelated whereas the activities refer to the actual feature of the subsystem computation and inter-subsystem communications. FSM's have been used in robot control systems to model complex behaviors and implementation as discussed in [26]. Zielinski, et al. [27] have demonstrated the use of FSM to model the behavior template of a table tennis ball collecting robot. Bolagh and Obdrzalek [28] have also shown the FSM's can be

used in robotic education to teach control systems for different kinds of robots.

An FSM Model of an Arm Robot

Any movement of an arm robot can be decomposed as a sequence of rotations and translations. Therefore, in linear algebra, a complex movement is described as the product of some rotation and some translation matrices. Following this idea, we are defining two categories of FSMs: One corresponding to the rotation with a given angle and another one corresponding to a translation with a given length. For the rotation, the reference point is the origin of the arm and we consider that the arm is able to rotate with 180 degrees clockwise or anti-clockwise. For the translation, the reference point is the end point of the arm which we consider that can be extended up to a maximum length.

For the FSM of a rotation we are considering:

- Σ = {ϑ}
- S = {INIT, s1, s2, STOP, CRASH}
- $s_0 = INIT$
- $ACT = \{act_i | 1 \le i \le 10\}$
- F = {STOP, CRASH}

The diagram of the rotation FSM is given in Figure 1.

In the following we are describing the actions of the rotation FSM:

- act_1 and act_2 are corresponding to the rotation of the arm robot anti-clockwise or clockwise with the angle ϑ . If $0 < \vartheta < 180$, then the movement is anticlockwise, and the state will change to s1. If $-180 < \vartheta < 0$, then the movement is clockwise and the state will change to s2
- act_3 and act_4 are corresponding to any change of the angle ϑ that are maintaining the states s_1 , and respectively s_2

- act_5 and act_6 are corresponding to a change of states between s_1 and s_2 or vice versa. Any movement that is changing the sign of the value of ϑ will enable such a transition between states
- act_7 and act_8 are corresponding to transitions between any of the states s1 or s2 and the state STOP. This happens when the value of ϑ is -180 or 180
- act₉ and act₁₀ are corresponding to transitions between any of the states s1 or s2 and the state CRASH.
 Such a transition must be avoided in practice as it corresponds to a movement that will break the arm robot.

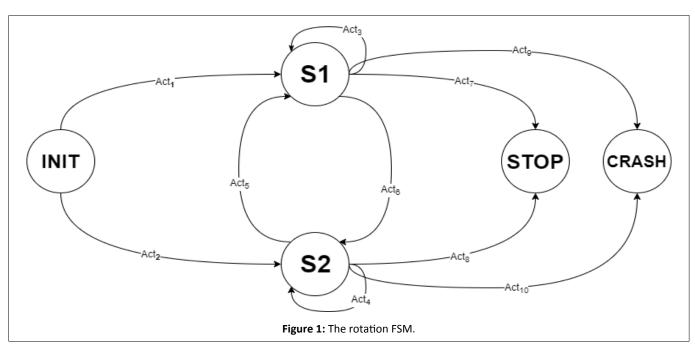
For the FSM of a translation we are considering:

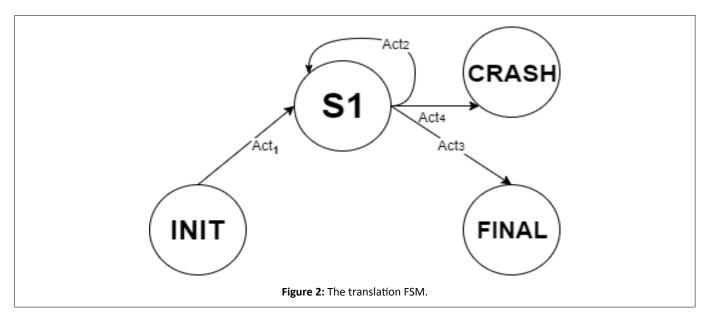
- $\Sigma = \{x\}$
- *S* = {INIT, s1, FINAL}.
- $s_0 = INIT$
- $ACT = \{act_i | 1 \le i \le 4\}$
- *F* = {FINAL}

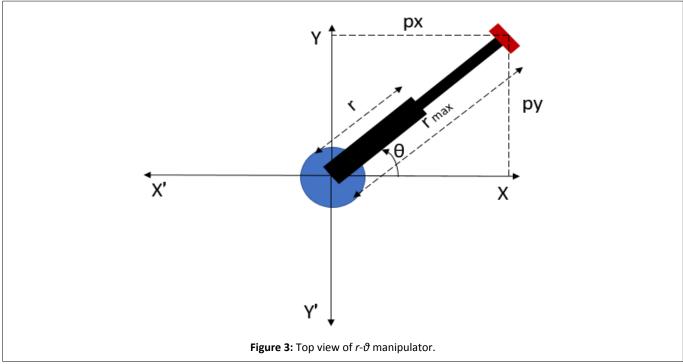
The diagram of the translation FSM is given in Figure 2.

In the following we are describing the actions of the translation FSM:

- act₁ is corresponding to an extension of the arm with a value t < MAX. In this case the state of the system will change to s1.
- act₂ is corresponding to any move of the arm such that the maximum length of the arm is not reached. In this case the state is maintained as s1.
- *act*₃ is corresponding to the reach of the maximum length of the arm and consequently of the *FINAL* state.
- act₄ is corresponding to any "unusual" movement of the arm such that the maximum extension length is exceeded; in this case, state "CRASH" is reached.







Case Study: A Two Joints Manipulator r-9

In this section an Event-B model corresponding to the kinematics of a two joints manipulator r- ϑ is investigated. In this case, the kinematics is simple: One joint rotates around the robot's trunk with an angle ϑ and one joint slides an arm with length r radially in and out. The model is validated using some of the Rodin facilities and then some properties are verified using ProB.

The Event-B model

The Event-B model is developed following the above methodology, and thus only one rotation FSM and one translation FSM are needed (Figure 3).

The model contains 2 contexts and 2 machines which are corresponding to the static and respectively to the dynamic

part of the two FSMs.

The first context (C1) contains the set of states of the rotation FSM: {INIT, s1, s2, STOP, CRASH} and {interm} a state that we are considering for the simplicity of the modelling. The corresponding machine (M1) is describing the transition between these states according to the given set of actions.

The context C1 is given below:

CONTEXT

C1

SETS

STATES

CONSTANTS

axm1: partition (STATES, {INIT}, {s1}, {s2}, {interm}, {STOP}, {CRASH})

END

AXIOMS

The axiom *axm*1 shows that any two states are different and their union is the set of states.

The *initialisation* event for *M*1 is used to assign initial values for the five variables used in the model. The logics of the assignments is that the system is at the beginning in the initial state (*INIT*), as a consequence the value of *theta* is 0, then the arm can rotate with any value (*auxTheta*) in the interval [1, 359] and the direction of the rotation is given by the sign (+1 is associated with a clockwise and -1 is associated with a anti-clockwise rotation). The variable *newTheta* is used to update the value of *theta*, after checking how this will affect the state of the system. The *initialisation* event is given below:

INITIALISATION

BEGIN

act1 : state = INIT act2 : theta = 0 act3 : auxTheta : ϵ 1..359 act4 : sign : ϵ {-1, +1} act5 : newTheta = 0

END

One of the key events of M1 is move that is enabled if the state has one of the values: INIT, s1 or s2. In this, the values of two variables are randomly generated: $aux\vartheta \in -359..359$ and $sign \in \{-1, +1\}$ and the state changes to interm. Then, the value of the rotation angle ϑ is calculated by adding $sign \times aux\vartheta$, and depending of the obtained value, the state of the FSM changes to s1, s2, STOP or CRASH. Furthermore, the event move is enabled after each change of states, as soon as none of the states STOP or CRASH is reached.

The event move is given below:

move

WHEN

grd1 : state \in {INIT,s1,s2} grd2 : theta + sign * auxTheta \ge -180 grd3 : theta + sign * auxTheta \le 180

THEN

All the other events correspond to transitions between the states of the system according to the updated value of *theta*. As an example, we give below the event corresponding to the reach of state *STOP*. Obviously, this event is enabled in the intermediary state when the value of newTheta, the variable standing for the updated value of theta has one of the extremal values -180 or 180

reachStop

WHEN

grd1 : newTheta \in {180, 180} grd2 : state = interm

THEN

act1 : state := STOP
act2 : theta := newTheta

END

The second context (*C*2) contain the set of states of the translation FSM: {INIT,s1,final,CRASH} and *interm* an intermediate state.

The context C2 is given below:

CONTEXT

C2

SETS

STATES

CONSTANTS

init

interm

final

r

 MAX

s1

CRASH

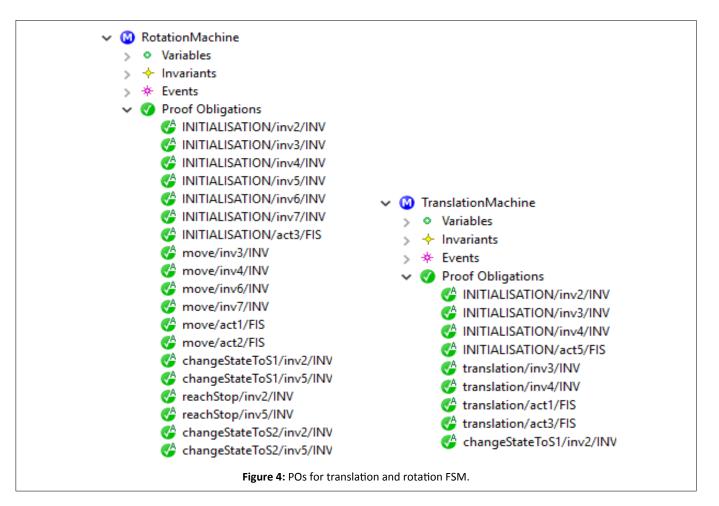
AXIOMS

 $\mathit{axm1}$: partition (STATES, {init}, {interm}, {final}, {s1}, {CRASH})

axm2 : r = 10axm3 : MAX = 10

END

The axiom *axm*1 has a similar meaning to the one in context *C*1. The other two axioms are used to set the initial length



of the arm r and the maximum value of its extension MAX.

In this case, the key event is *translation* which is enabled in any of the states *INIT* and s1, and in which the values of two variables are randomly generated: $sign \in \{-1; +1\}$ and $t \in 1..MAX$. The event is given below:

translation

WHEN

 $grd1: state \in \{init,s1\}$

THEN

$$\label{eq:act1:t} \begin{split} &\text{act1:t}: \varepsilon \text{ 1..MAX} \\ &\text{act2:state}:= \text{interm} \\ &\text{act3:sign:} \varepsilon \left\{\text{-1; 1}\right\} \end{split}$$

END

Then the value of the variable corresponding to the length of the arm is calculated by adding $sign \times t$ and as soon as the maximum length is not reached, s1 is enabled. When the maximum length of the arm is reached, the state is updated to FINAL, and state CRASH is associated with the unlikely behavior that the length of the arm could exceed r + MAX or could be less than r.

Model validation: Model checking, proof obligations and properties verification

This section is dedicated to the validation of the model by using various Rodin features.

As can be seen in Figure 4 all proof obligations (POs) have been automatically generated and validated by the system.

Furthermore, running the model checking on both machines, it can be seen that all states have been visited and there is no invariant violation (see Figure 5).

All these ensure a primary validation of the model which can be enhanced with verifying LTL properties that are describing the behavior of the manipulator.

Thus, the model is verified against some properties and the results are given in Table 1. Although most of the verified properties are simple, we consider them to be significant in terms of model correctness and functionality.

Advantages and limitations

The main advantages of using Event-B and the Rodin platform are the simplicity of modelling, the automatic validation of the models and the model checking and animation facilities. The robustness of an Event-B model is rooted in the rigor of the mathematical language behind and in the correctness of the model that is ensured in each stage of the modelling process through various automatic mechanisms. Moreover, the refinement technique allow users to develop the models gradually, and thus to include in the current model only those features essential for the purpose of that stage.

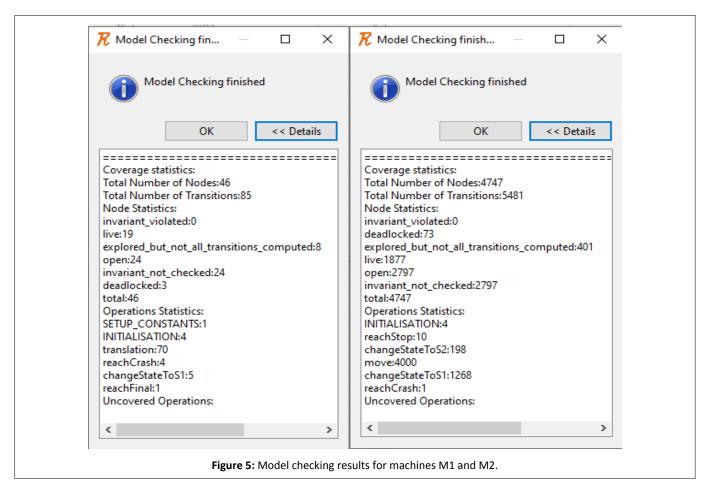


Table 1: LTL property verification using ProB.

LTL property	Meaning	Result
G{state/ = STOP}		A counterexample has been found:
	State stop is not reached for M1.	(Move \rightarrow changeStatetoS2) ¹⁷⁹
		→ move → reachStop
G{(theta > -50)&(theta < 50)}	Theta is in (-50, 50)	A counterexample has been found:
		(Move → changeStatetoS2) ⁵⁰
		A counterexample has been found:
G {x < 12}	The length of arm is less than 12	$(Translation \rightarrow changeStatetoS1)^2$
		A counterexample has been found:
		(Translation \rightarrow changeStatetoS1) ³⁵
G{state/ = final}	State final is not reached for M2.	\rightarrow translation \rightarrow reachFinal

On the other hand, we mention as the main limitation the numerical data types that are restricted to subsets of integers.

Conclusions and Future Work

Robotics is one of the main research areas nowadays, and several methodologies have been developed, however using mathematical modelling combined with model checking is a new approach for simulating and testing the behavior of a robot.

Although our methodology has some restrictions arising

from the limitations of the Event-B language and of the Rodin platform, we consider that our paper represents a significant step in this direction.

Our future work will concentrate on applying a similar methodology for other types of robotic mechanisms. We are considering as a first extension to develop a hierarchical state machine based model of a redundant robotic mechanism, and to implement the corresponding Event-B model into the Rodin platform. Moreover, we also plan to investigate other modelling languages and platforms that could help to overcome some of the current limitations.

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DOI: 10.36959/673/366

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