

ON THE CHEBYSHEV FUNCTIONAL

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Abstract. In this paper we prove an inequality for certain orthoprojectors. For orthoprojectors of rank one we obtain a Chebyshev type inequality. Grüss-Lupaş type inequalities are also discussed.

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